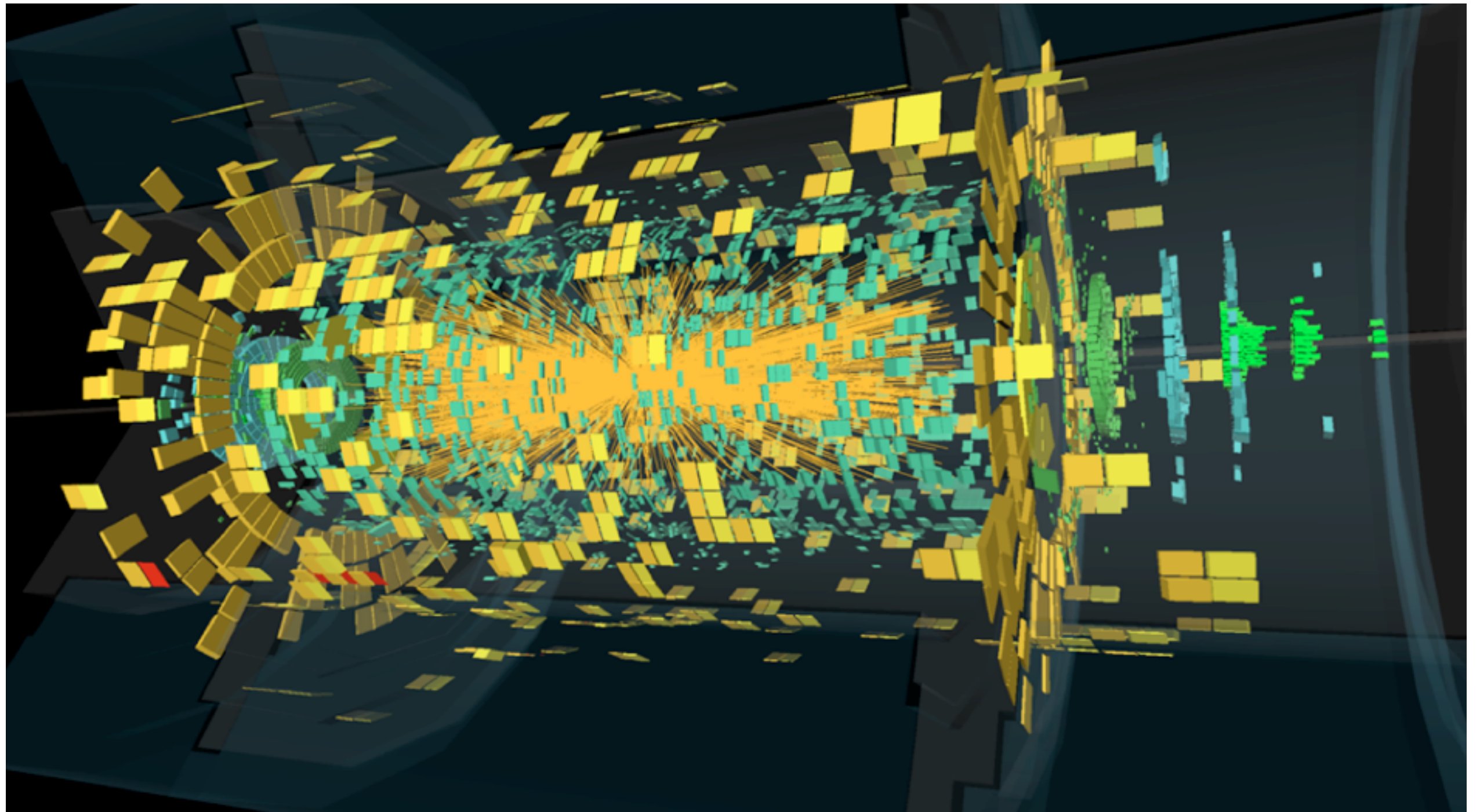




# Overview of ATLAS Heavy Ions Results

*Marisilvia Donadelli*  
for the ATLAS Collaboration  
University of Sao Paulo  
SILAFEA 2012



# Outline

ATLAS detector

Pb+Pb data samples

Jets

- Jet suppression

- Jet fragmentation

Photons and Z bosons

Photons, Z – jet correlations

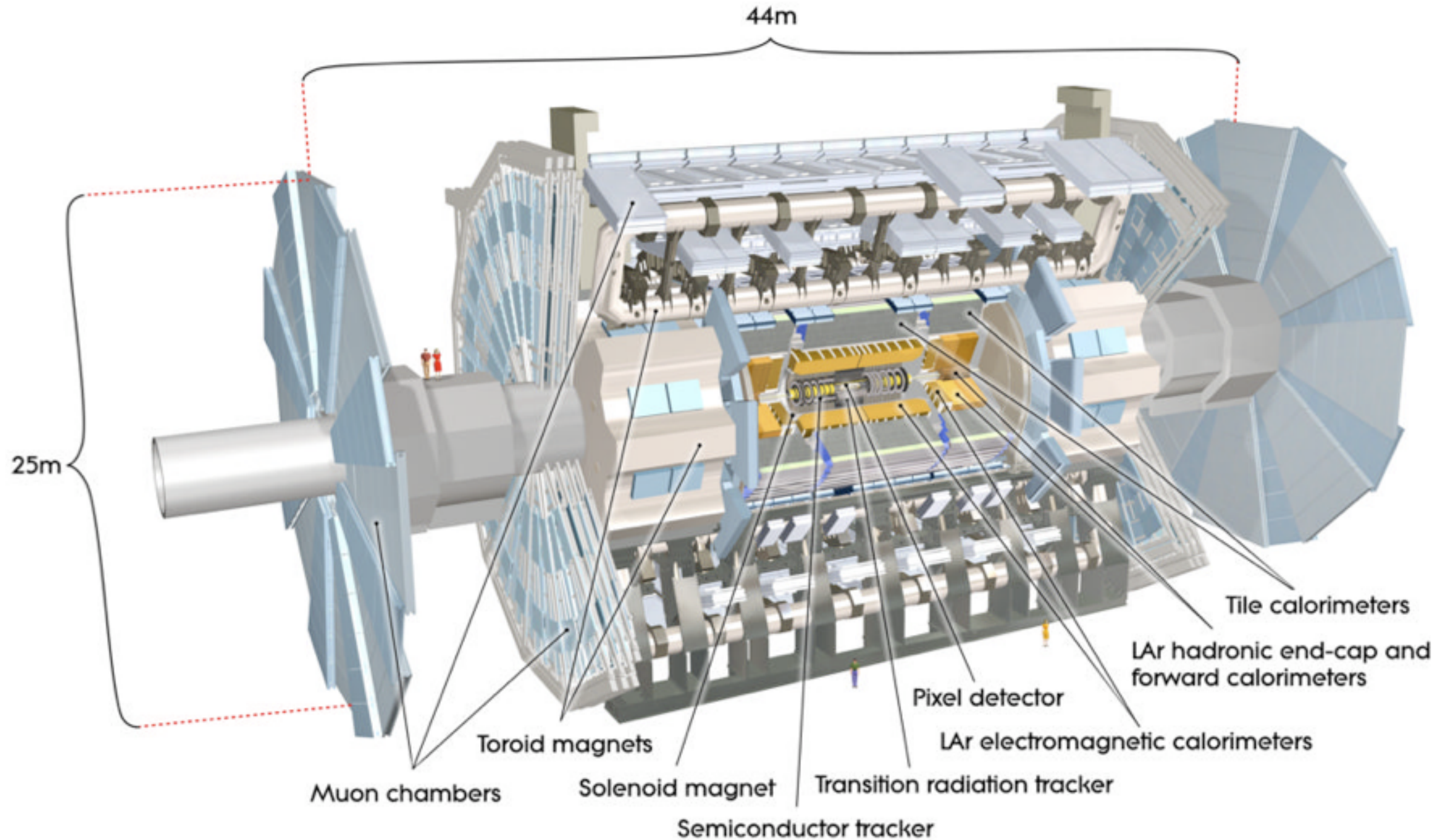
Azimuthal anisotropy

- Event plane method

- Event by Event method

- Event plane correlations

# ATLAS Detector



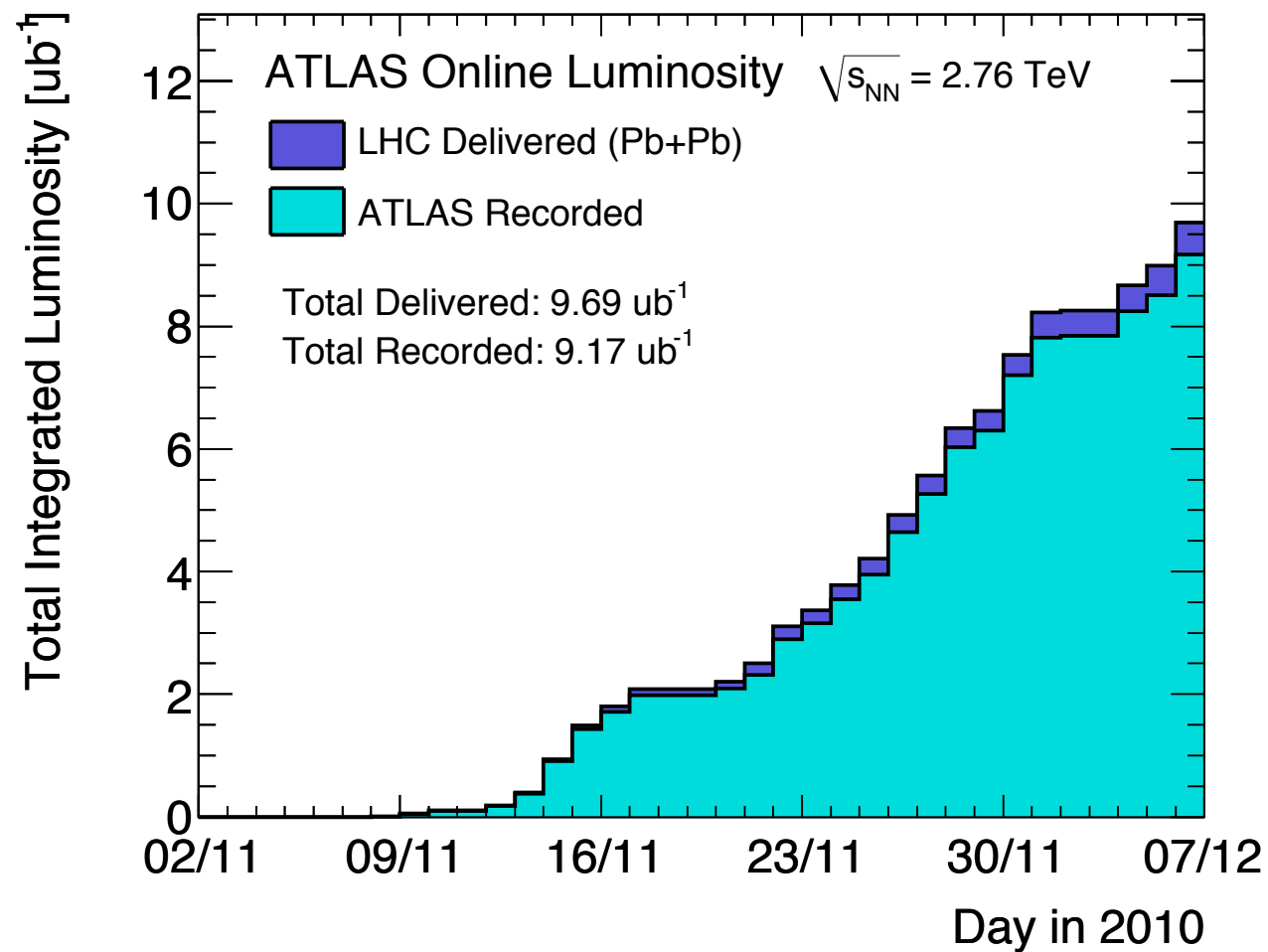
***Inner Detector – Tracking  $|\eta| < 2.5$***

***Calorimetry –  $|\eta| < 4.9$***

***Muon Spectrometer -  $|\eta| < 2.7$***

# Pb+Pb Data Samples

## 2010



$L_{int}$

8  $\mu\text{b}^{-1}$

*Detector efficiency*

> 97%

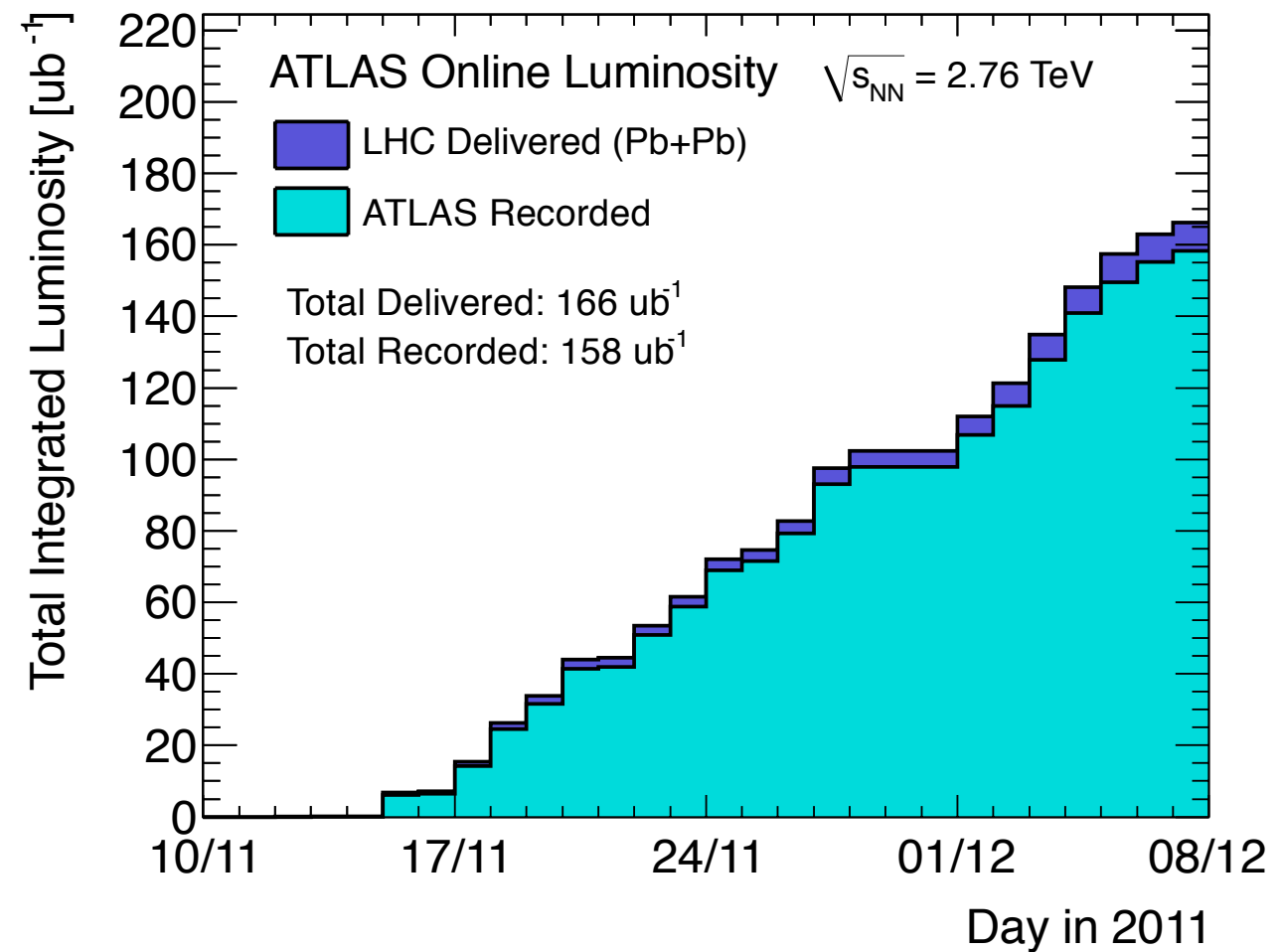
*Triggers*

Minimum Bias (MB)

*Events [ $\times 10^6$ ]*

~ 50

## 2011



0.15  $\text{nb}^{-1}$

> 97%

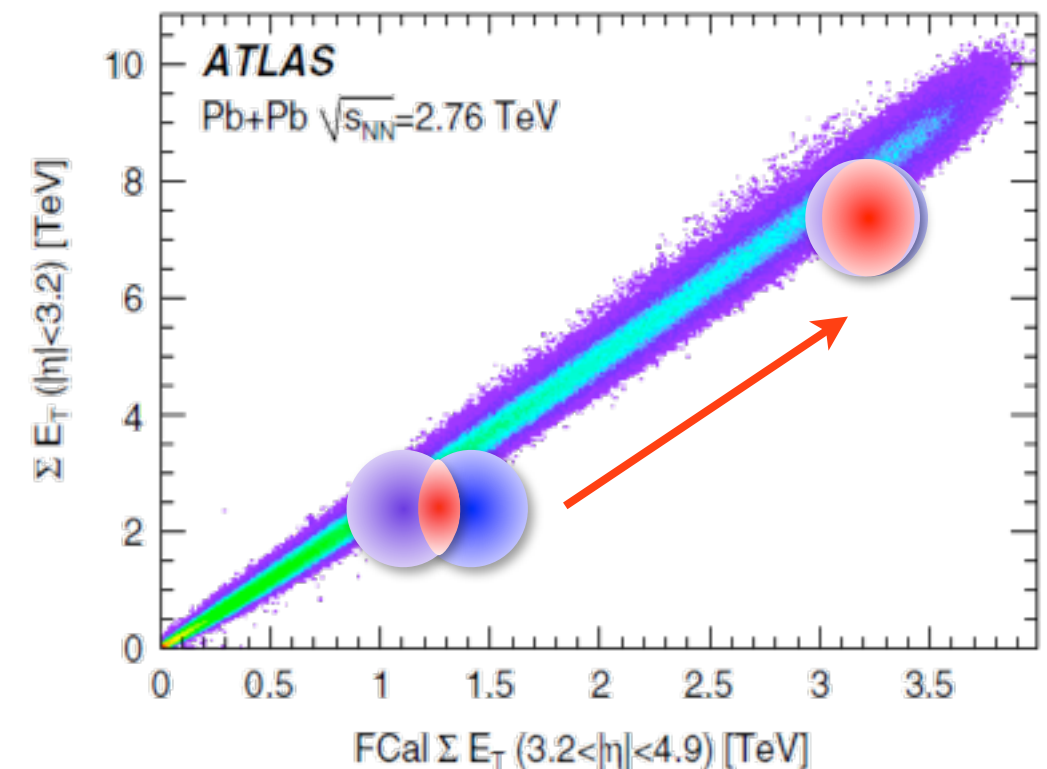
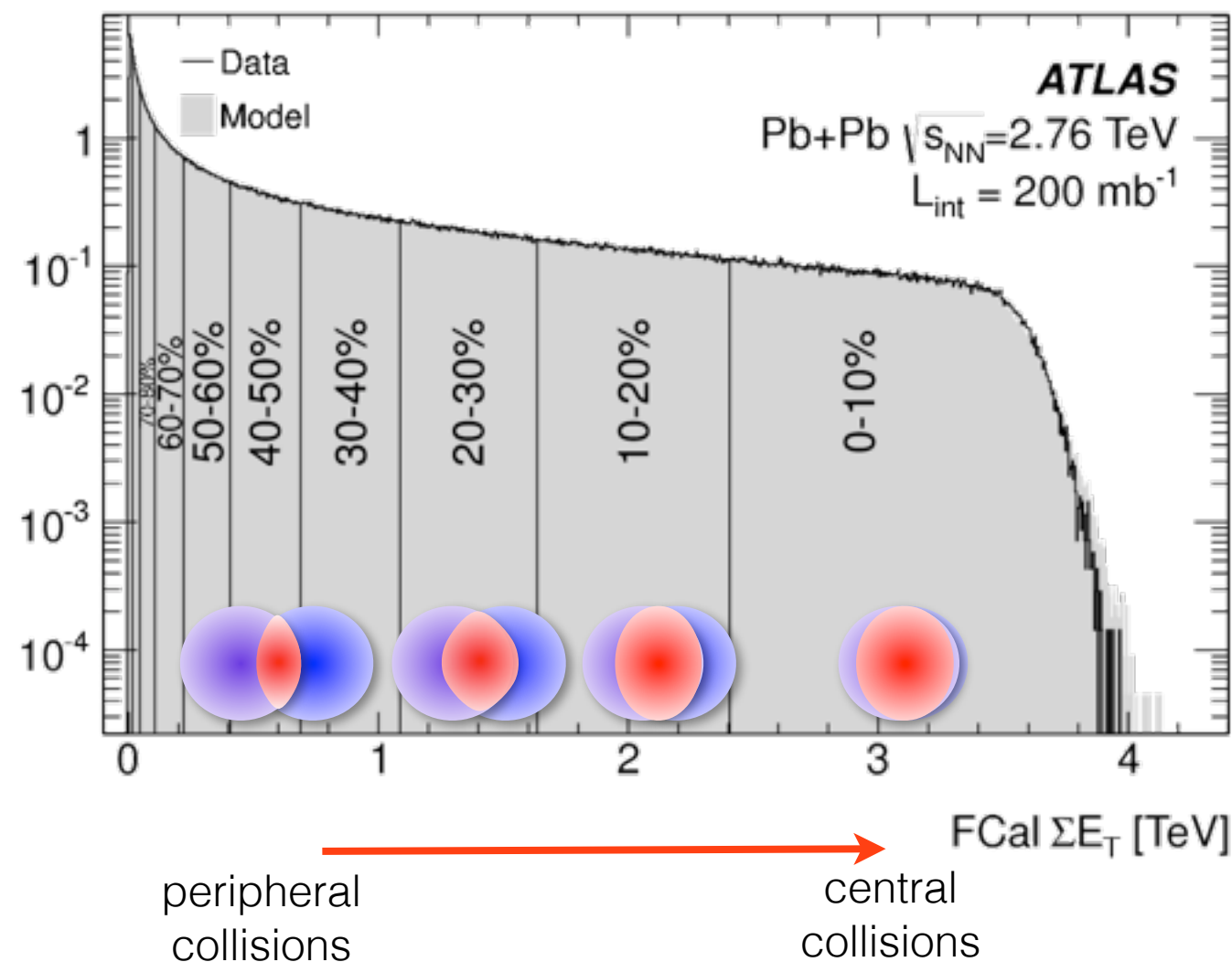
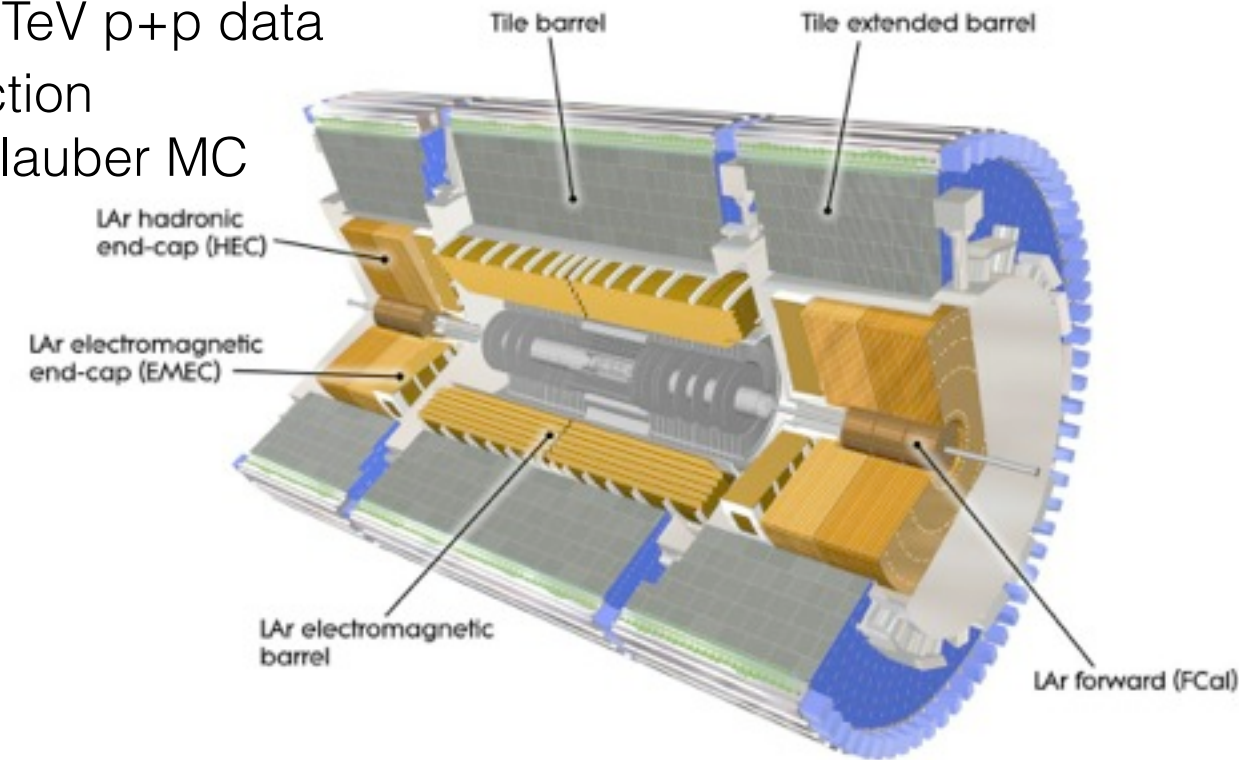
MB, e,  $\mu$ ,  $\gamma$ , jets, UPC

~1000

# Pb+Pb Collision Centrality

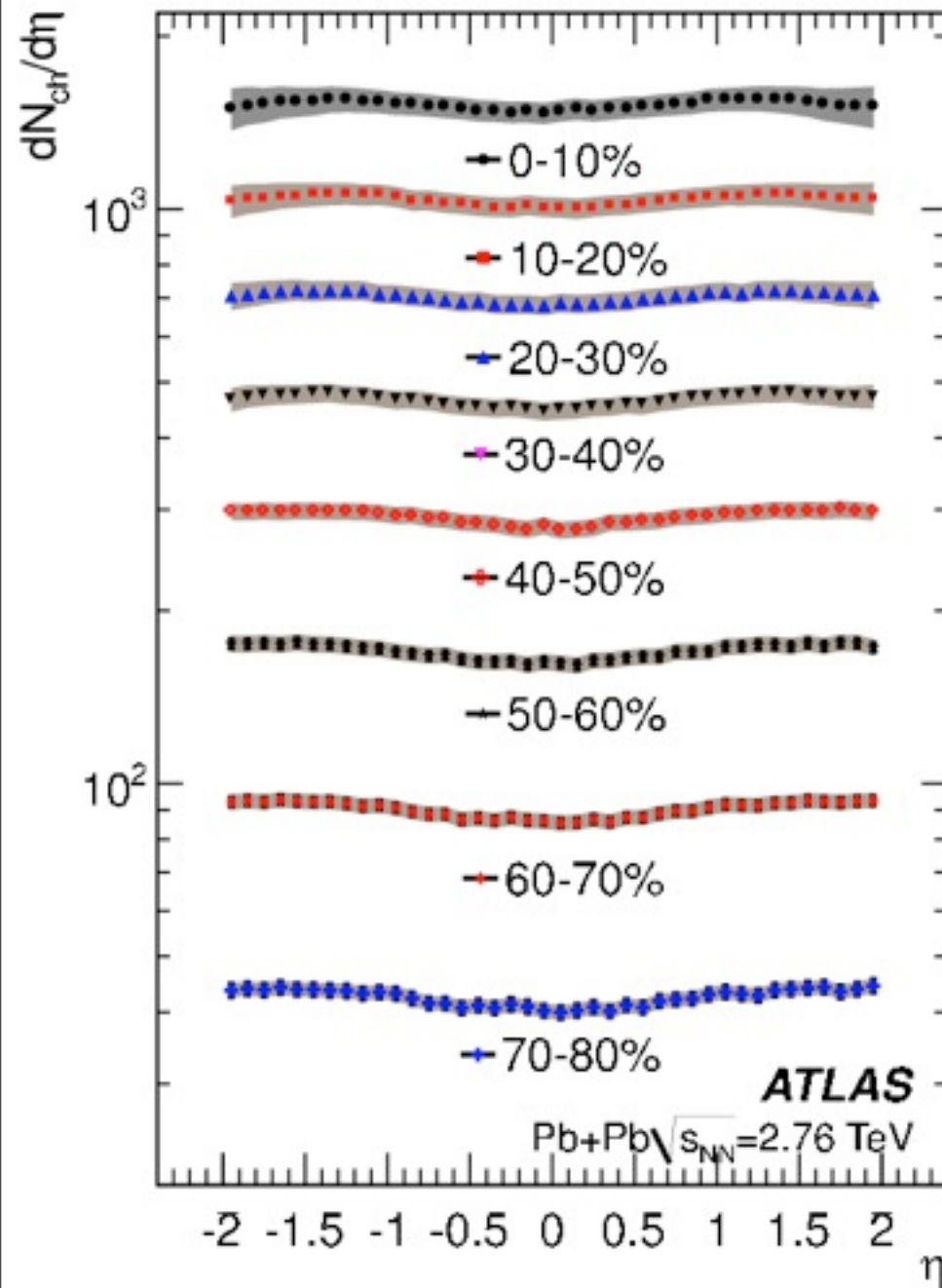
Characterize centrality by percentiles of the total cross-section using forward calorimeter (FCal)  $\Sigma E_T$  ( $3.2 < |\eta| < 4.9$ )

Energy sum in FCal compared with Glauber MC  $\otimes$  2.76 TeV p+p data  
Sampling fraction  $f = 98 \pm 2\%$  of total inelastic cross-section  
Centrality parameters  $\langle N_{\text{part}} \rangle$ ,  $\langle N_{\text{coll}} \rangle$  calculated from Glauber MC  
(binning in the simulated FCal  $\Sigma E_T$ )

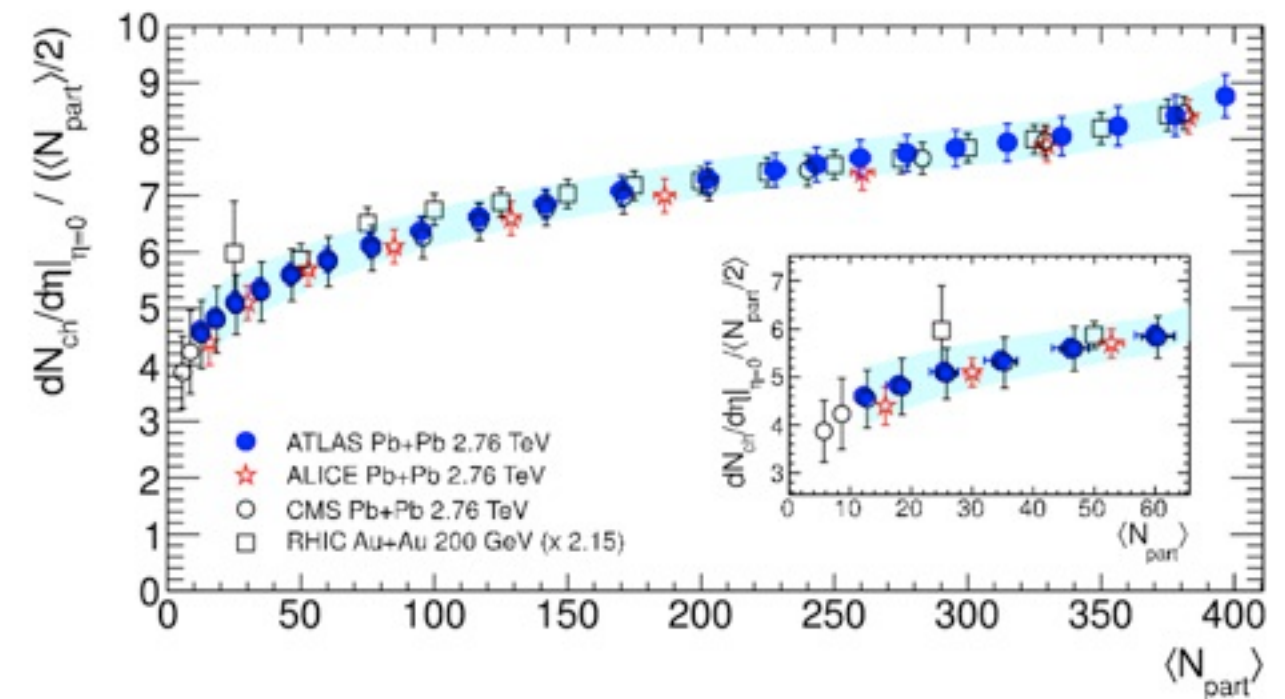
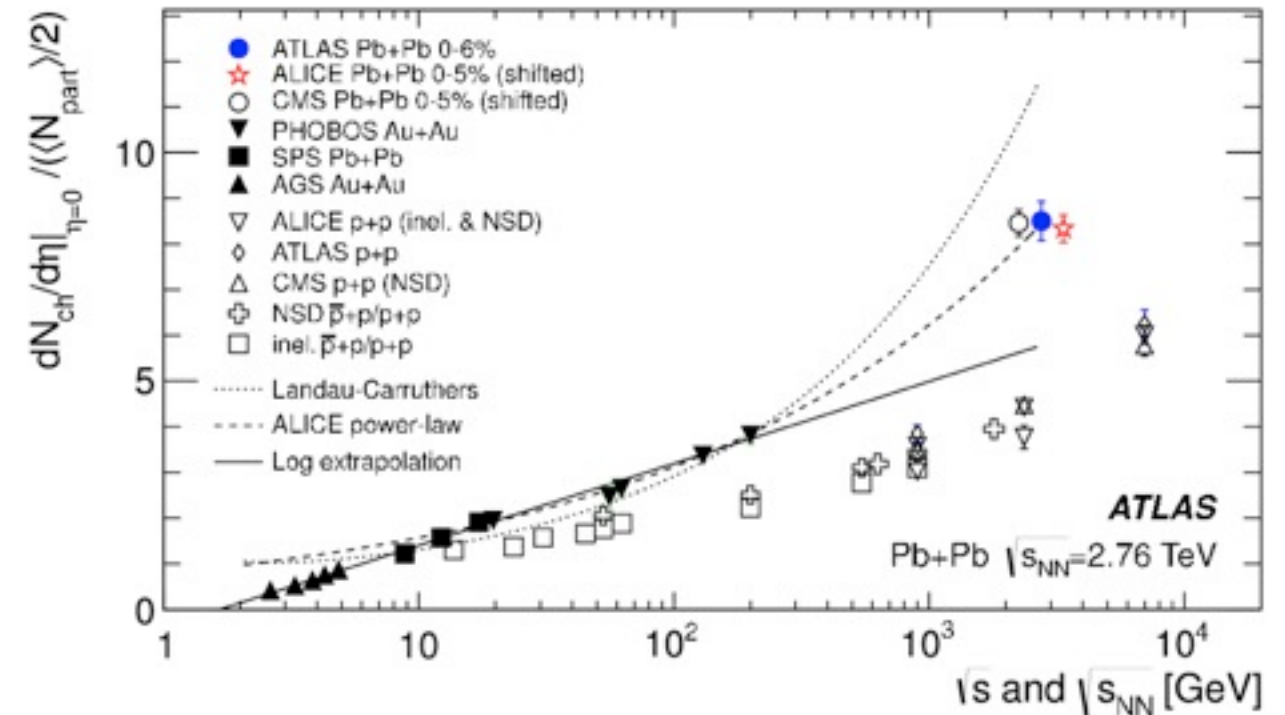
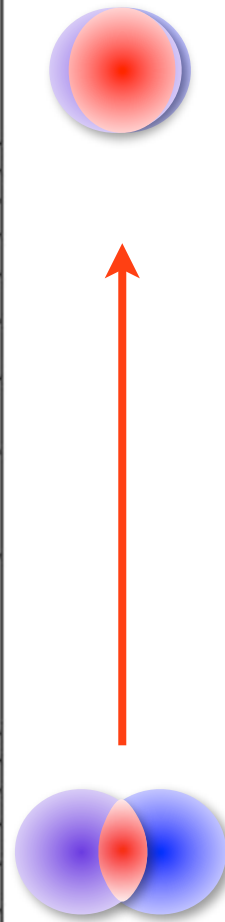


# Multiplicity

*Phys.Lett. B710 (2012) 363-382*

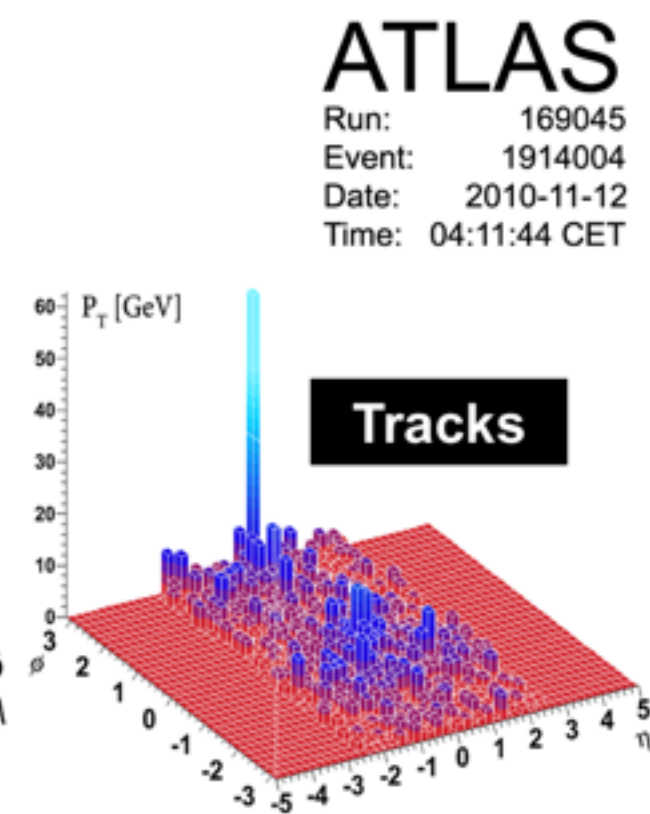
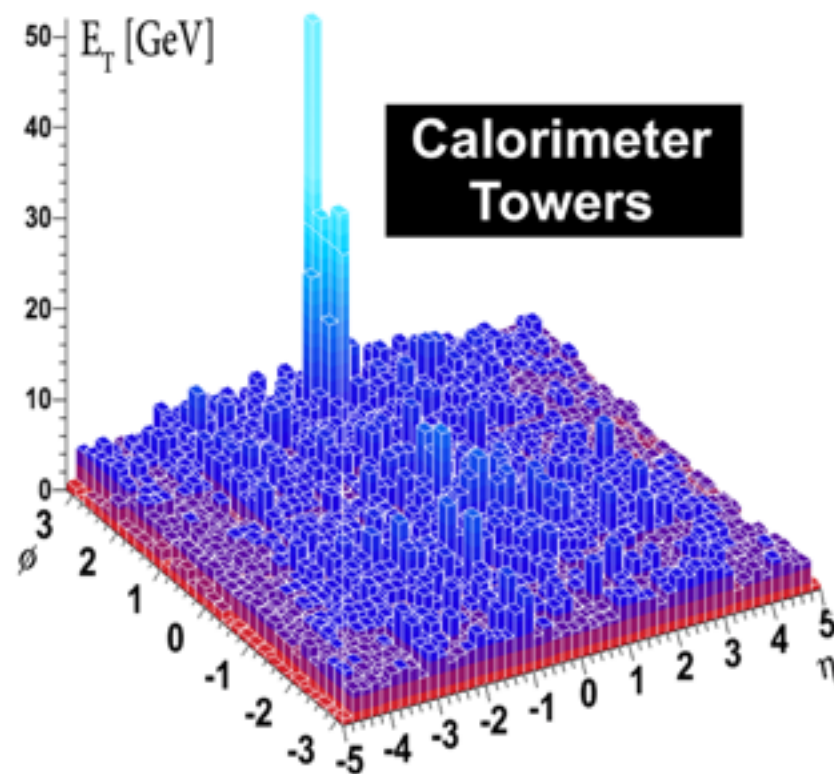
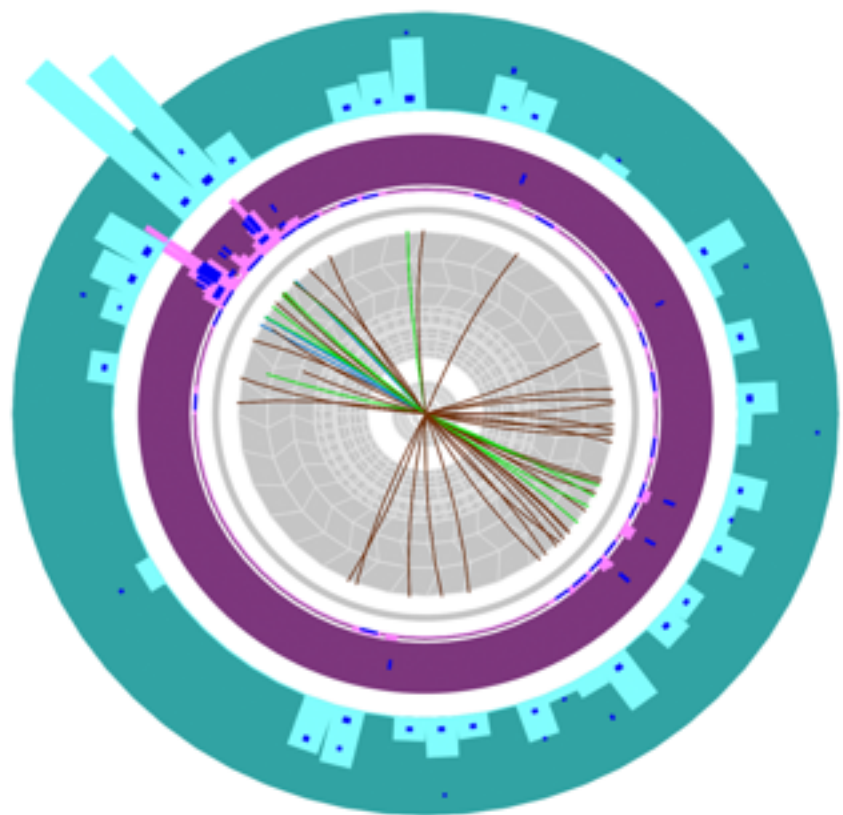


5% increase of yield from  $\eta \sim 0$  to  $\eta \sim 1$  in peripheral events (30-80% centrality class)



Up to 8,000 charged particles in ATLAS tracking @  $\sqrt{s_{NN}} = 2.76$  TeV  
 Twice more particles per participant pair compared to p+p

# Jets





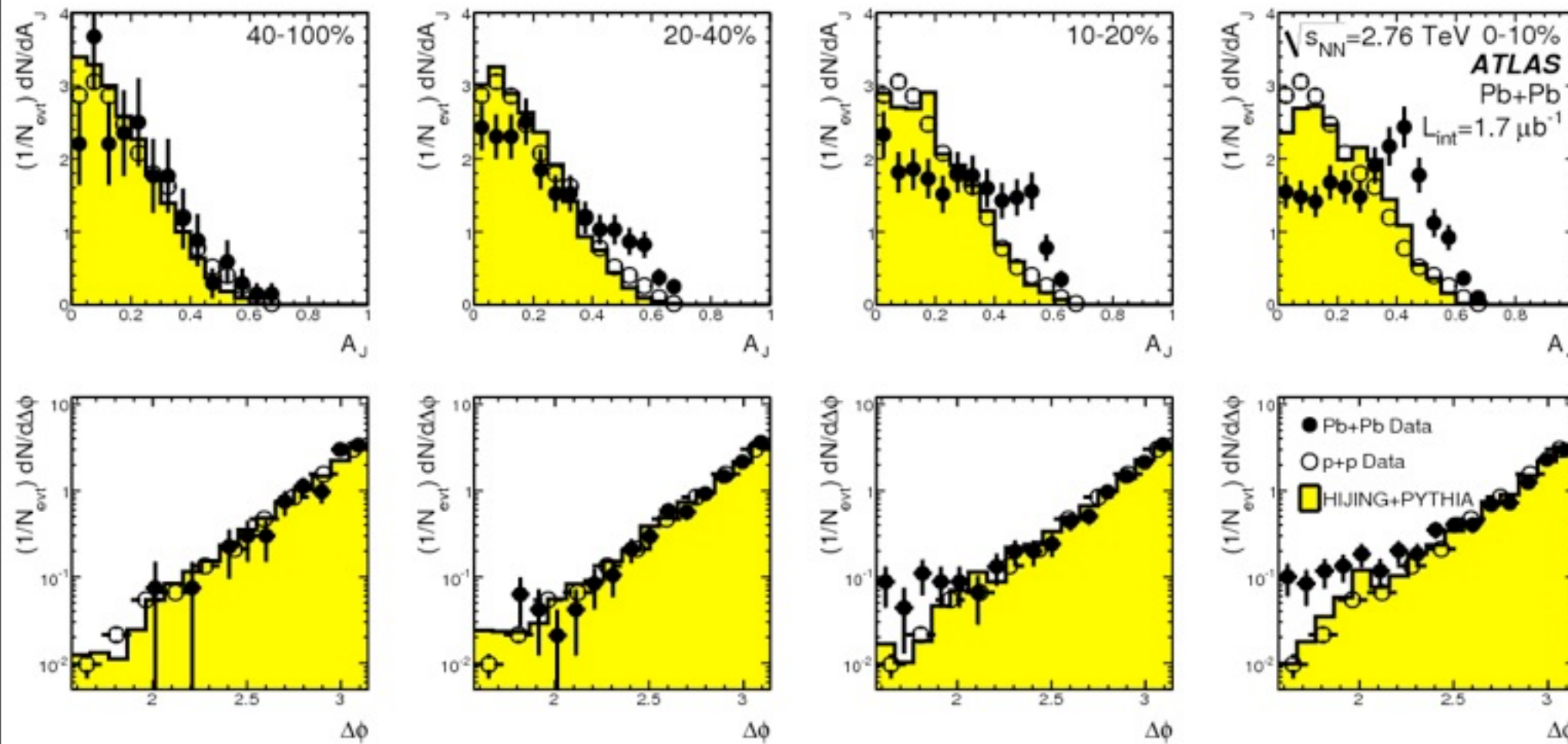
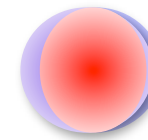
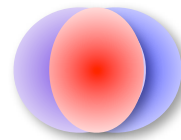
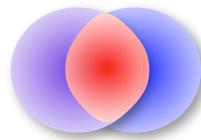
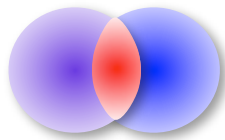
# Observation of a Centrality-Dependent Dijet Asymmetry in Lead-Lead Collisions at $\sqrt{s_{NN}} = 2.76$ TeV with the ATLAS Detector at the LHC

$$A_J = \frac{E_{T1} - E_{T2}}{E_{T1} + E_{T2}}, \quad \Delta\phi > \frac{\pi}{2}$$

$$\begin{aligned} E_{T1} &> 100 \text{ GeV} \\ E_{T2} &> 25 \text{ GeV} \end{aligned}$$

peripheral  
collisions

central  
collisions



Significant fraction of events with enhanced dijet asymmetry imbalance in  $E_T$  ...

...preserving the back-to-back angular correlation: dijet  $|\Delta\phi|$  balance in  $E_T$

# Jet $R_{CP}$

Asymmetry alone cannot provide information about the details of parton energy loss for radiative energy loss, jet energies can be reduced by greater “out of cone” radiation depending on the jet radii, according theoretical calculations (e.g., Y. He et al. *arXiv:1105.2566*).

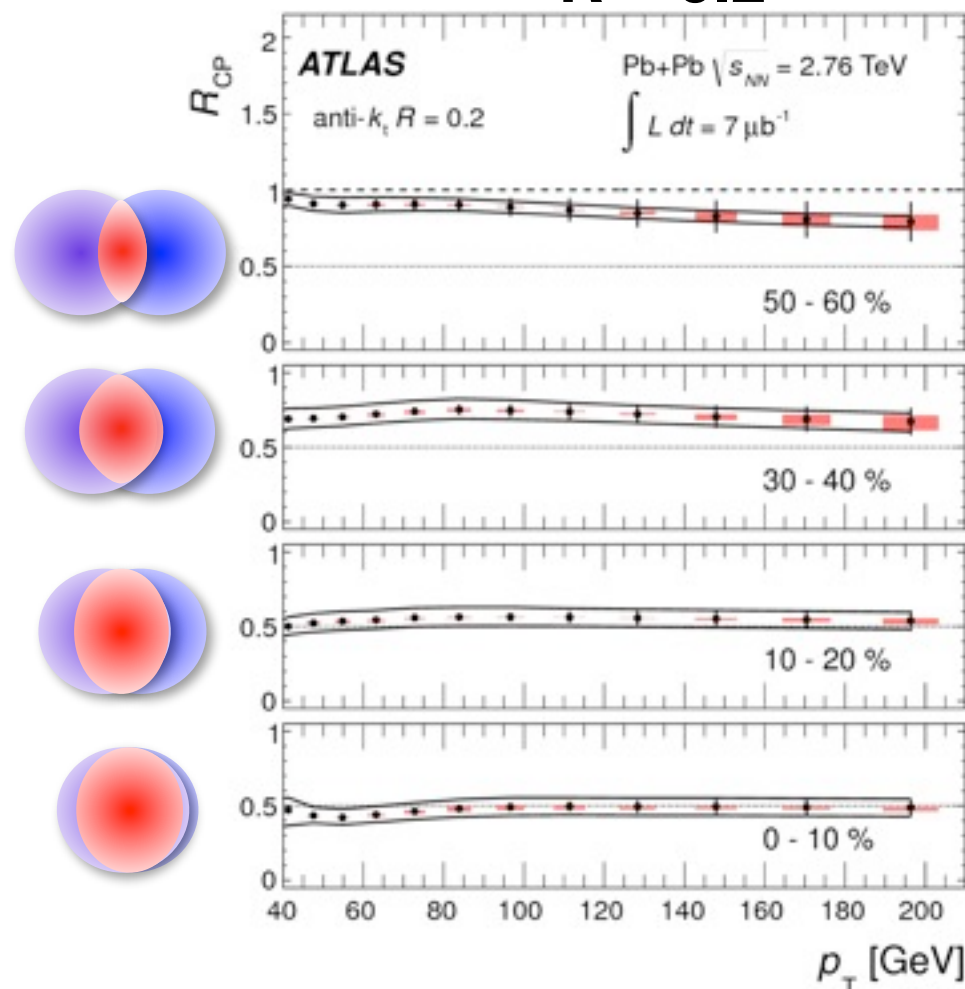
Single inclusive jet spectra and central to peripheral ratio  $R_{CP}$ :

$$R_{CP} = \frac{\frac{1}{N_{coll}} \frac{1}{N_{evt}} \frac{dN}{dp_T} \Big|_{cent}}{\frac{1}{N_{coll}} \frac{1}{N_{evt}} \frac{dN}{dp_T} \Big|_{60-80}}$$

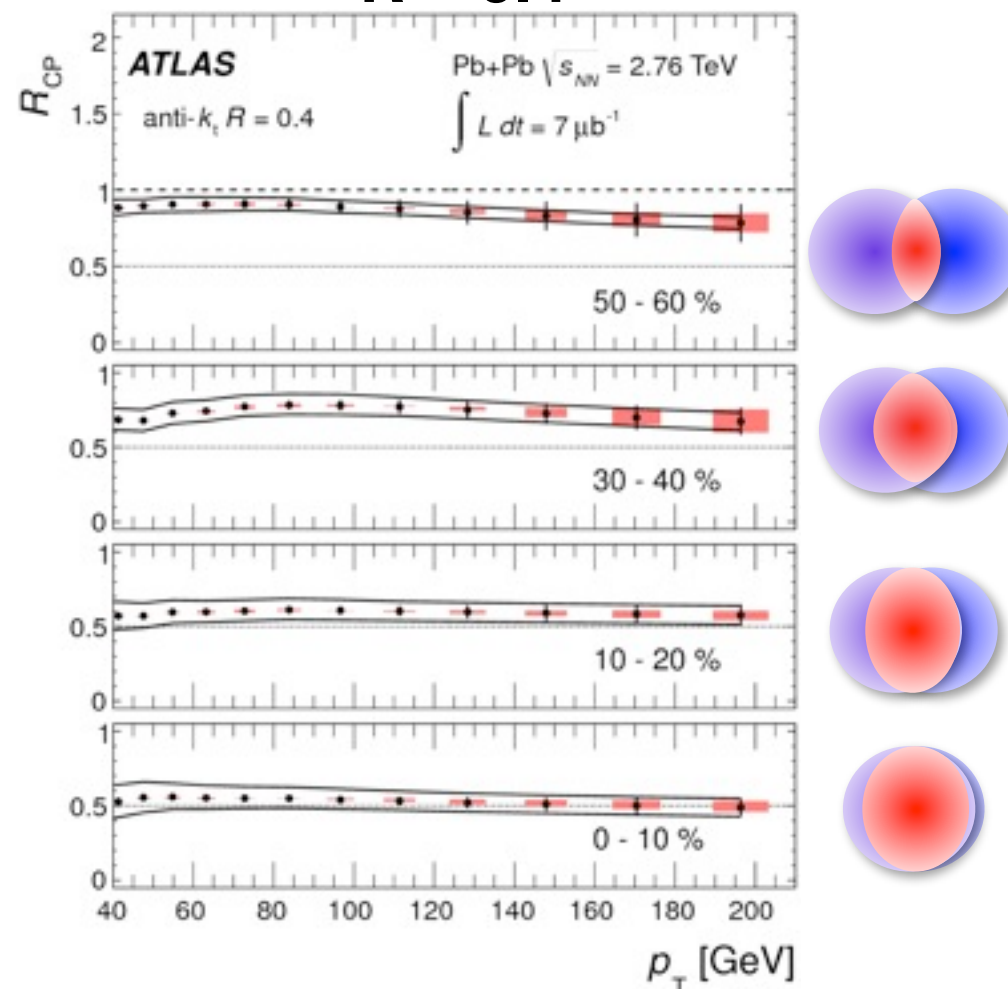
use anti- $k_t$  algorithm with  $R=0.2, 0.3, 0.4$  and  $0.5$ ;  
result using SVD unfolding to remove detector effects;  
~ 50 million events from 2010 PbPb data.

First LHC result on jet suppression (submitted to *PLB arXiv:1208.1967*)

**$R = 0.2$**



**$R = 0.4$**



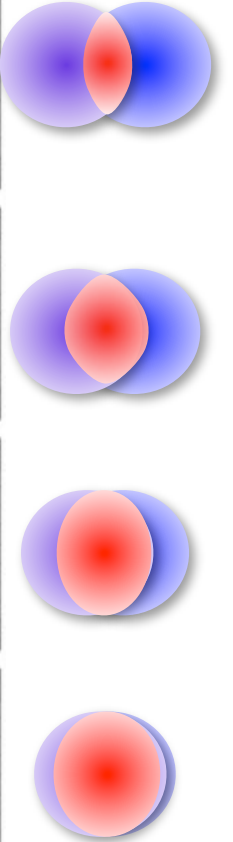
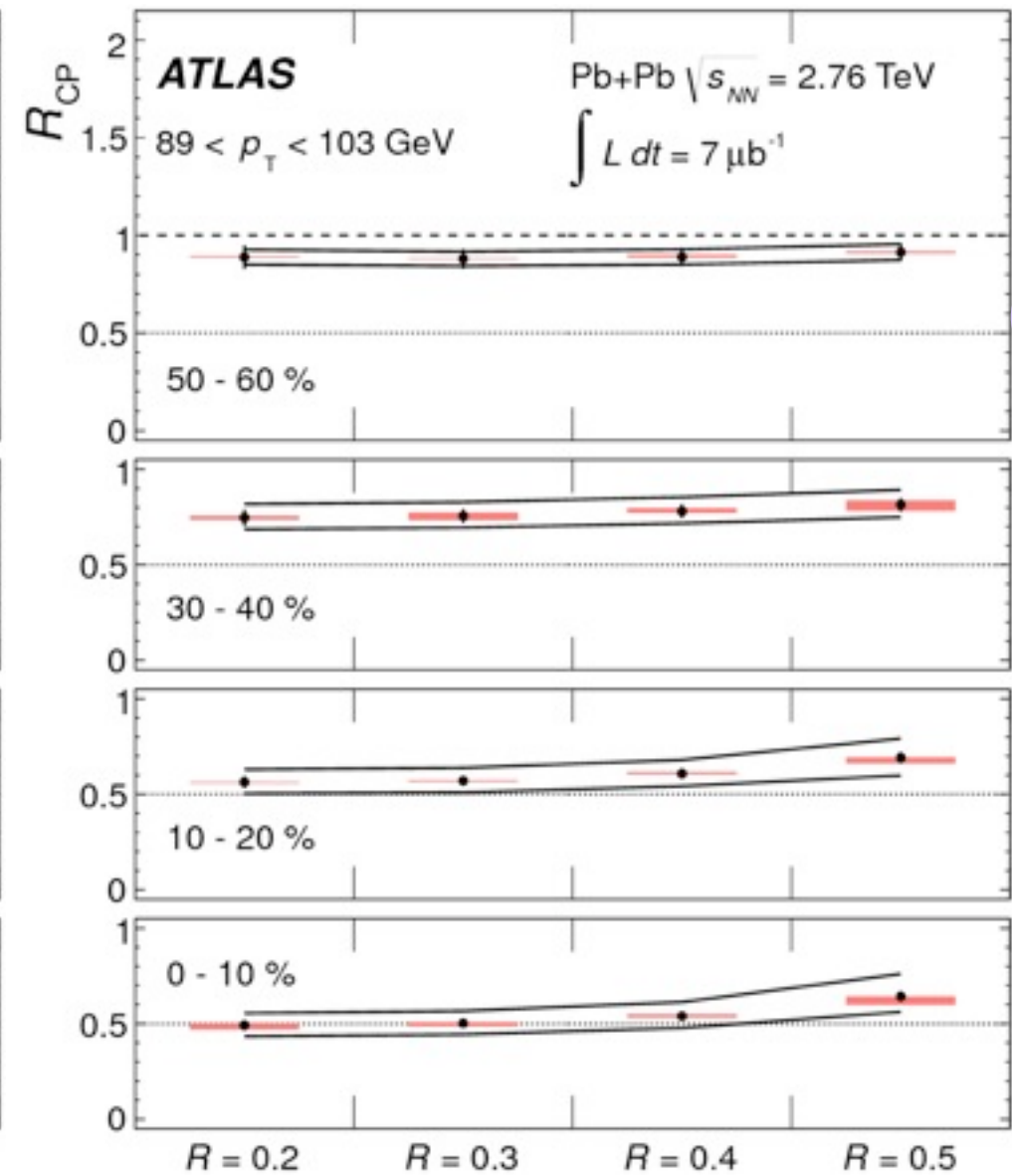
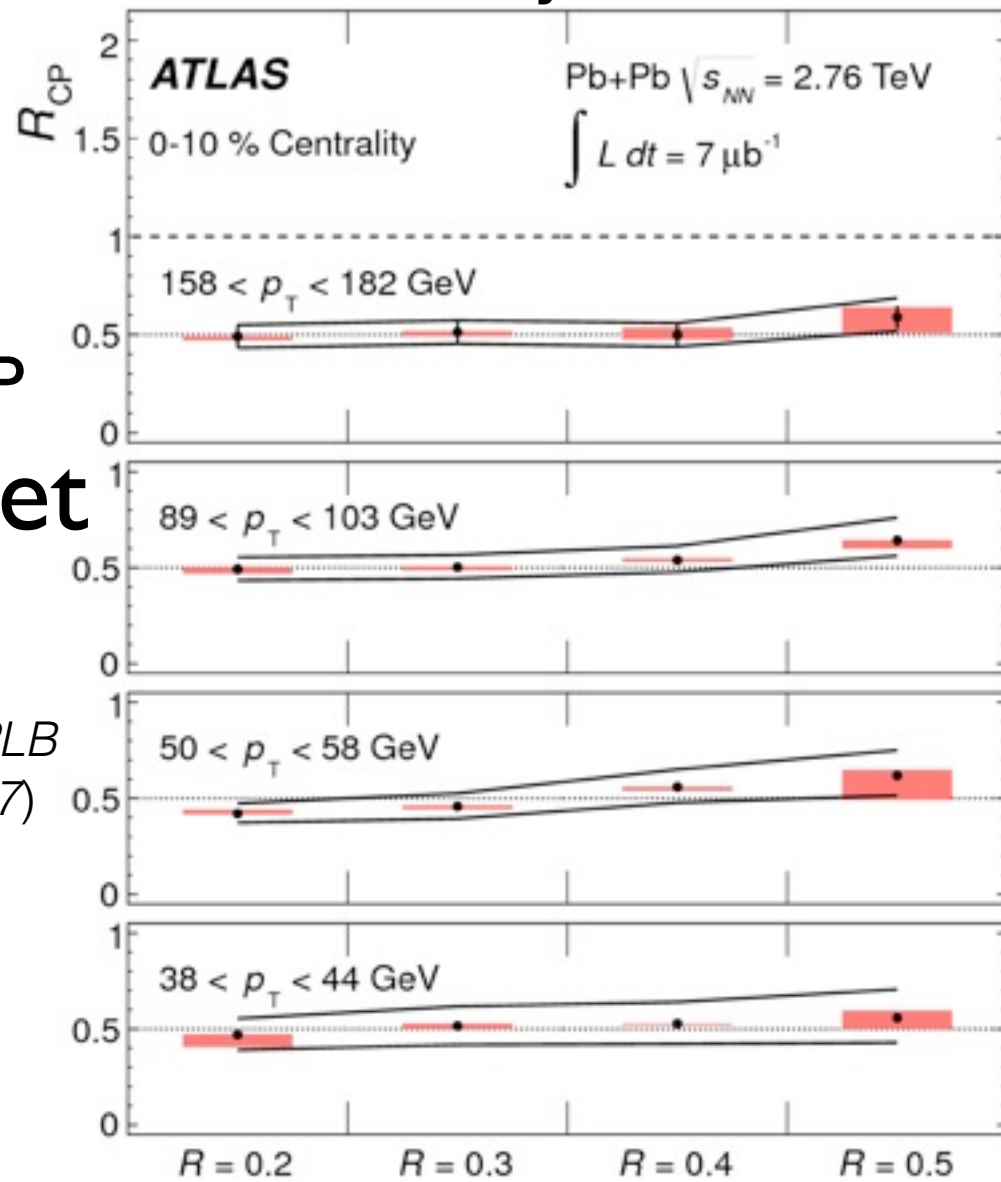
Suppression by a factor of 2 in central comparing to peripheral collisions.  
 $R_{CP}$  for all centralities and for both radii show weak variation with  $p_T$ .

**$R_{CP}$  in 0-10%  
centrality bin**

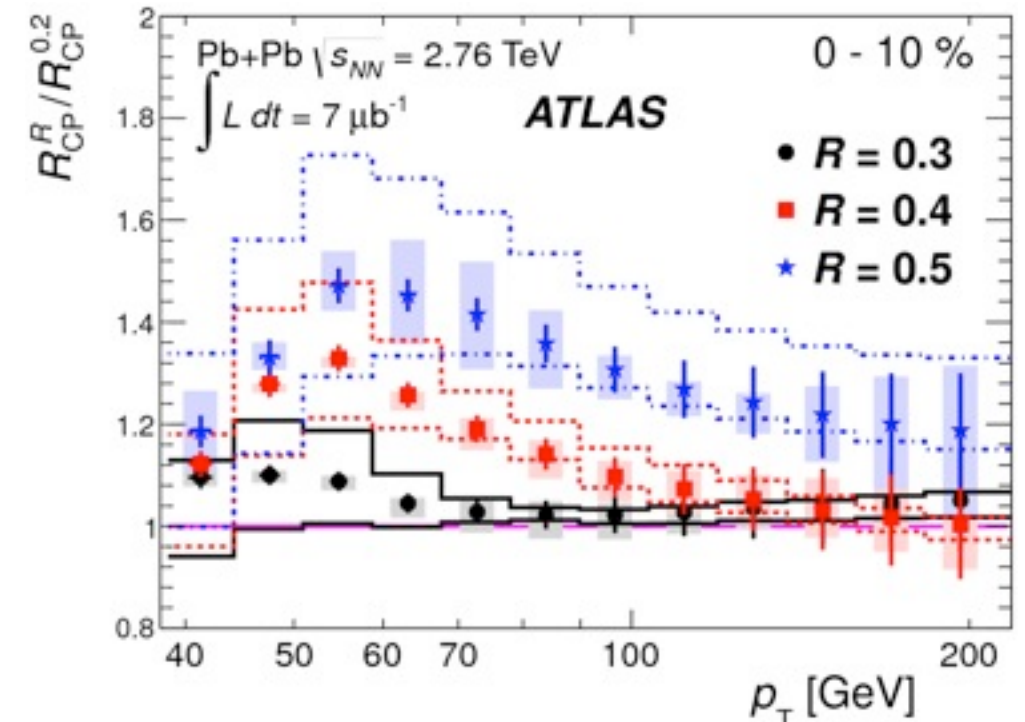
**$R_{CP}$  in  
 $89 < p_T < 103$  GeV**

# Jet $R_{CP}$ versus jet size

(submitted to *PLB*  
*arXiv:1208.1967*)



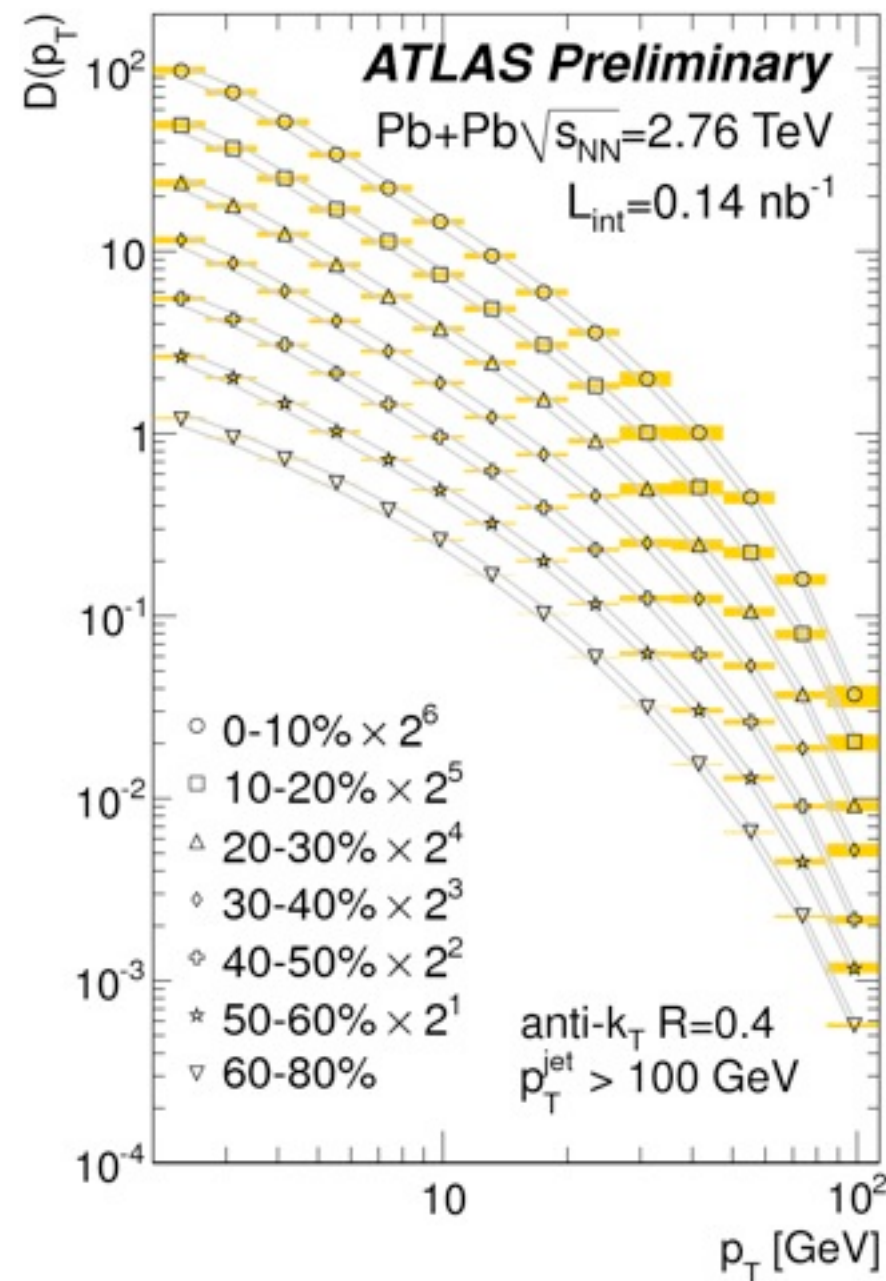
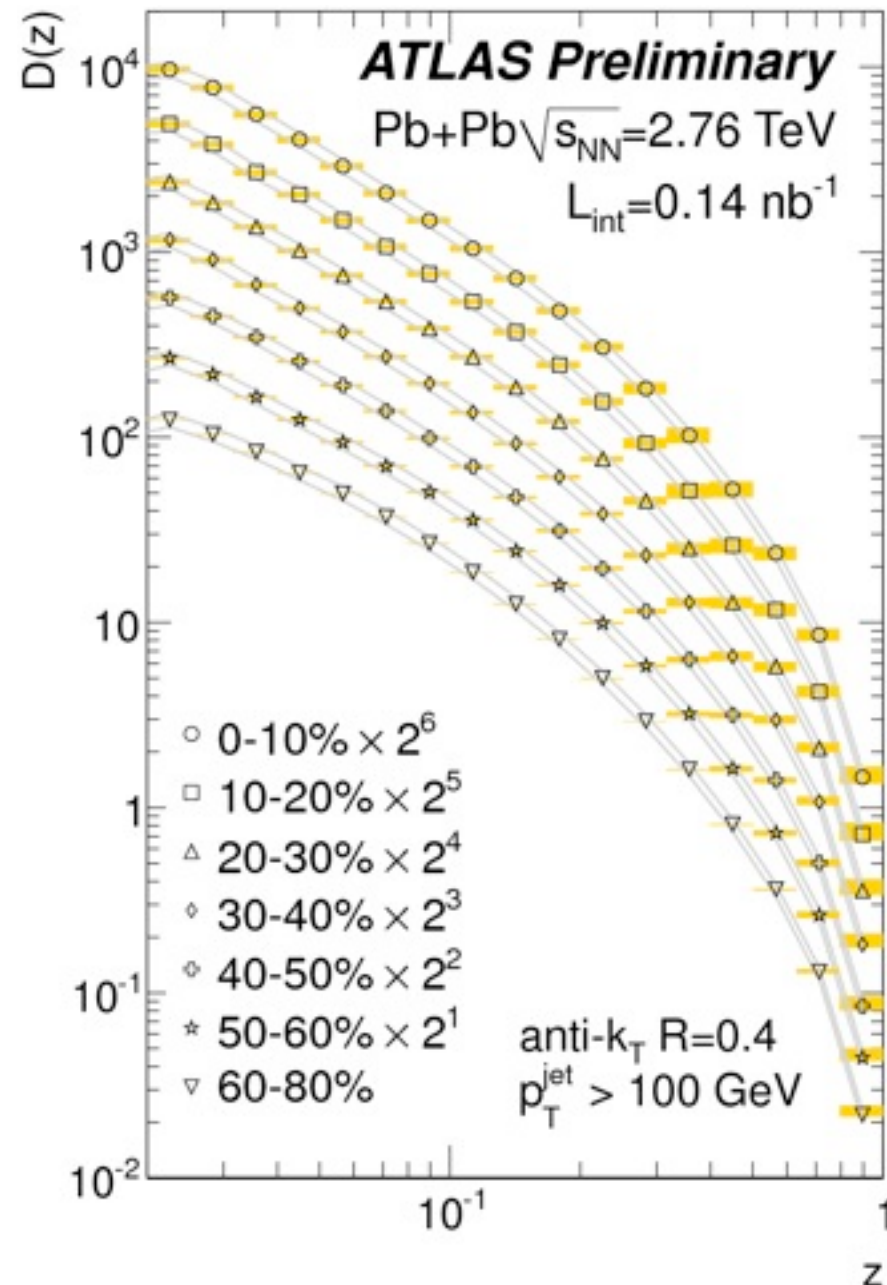
Ratio of  $R_{CP}$  values between  $R=0.3$ , 0.4 and 0.5  
jets and  $R=0.2$  jets  
significant dependence of  $R_{CP}$  on jet radius!



# Jet fragmentation

Asymmetry alone cannot provide information about the details of parton energy loss  
 A modification of jet internal structure was predicted by different theoretical models *N.Armento et al., JHEP0802 (2008) 048*.

$R = 0.4$



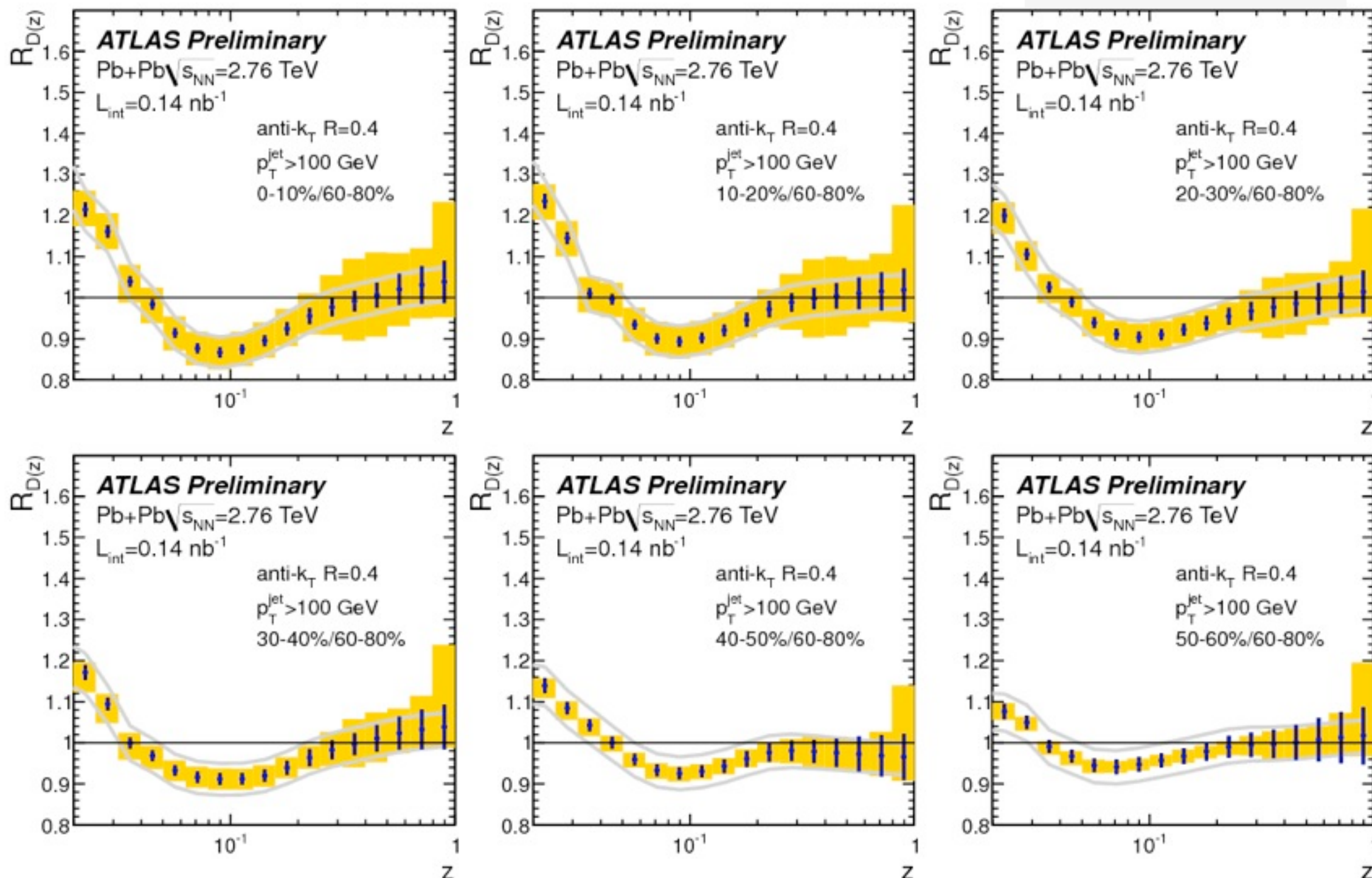
ATLAS-CONF-2012-115

SVD unfolding was used to correct detector effects and to reduce the effect of statistical fluctuations:  
 $D(z)$  unfolding accounts for track momentum and jet energy resolution;  
 $D(p_T)$  for track momentum resolution.  
 $D(z)$  and  $D(p_T)$  distributions have similar shape in all centrality bins.

# D(z) centrality dependence

Ratios are needed to study centrality dependence

$$R_{D(z)} = \frac{D(z)|_{cent}}{D(z)|_{60-80\%}}$$

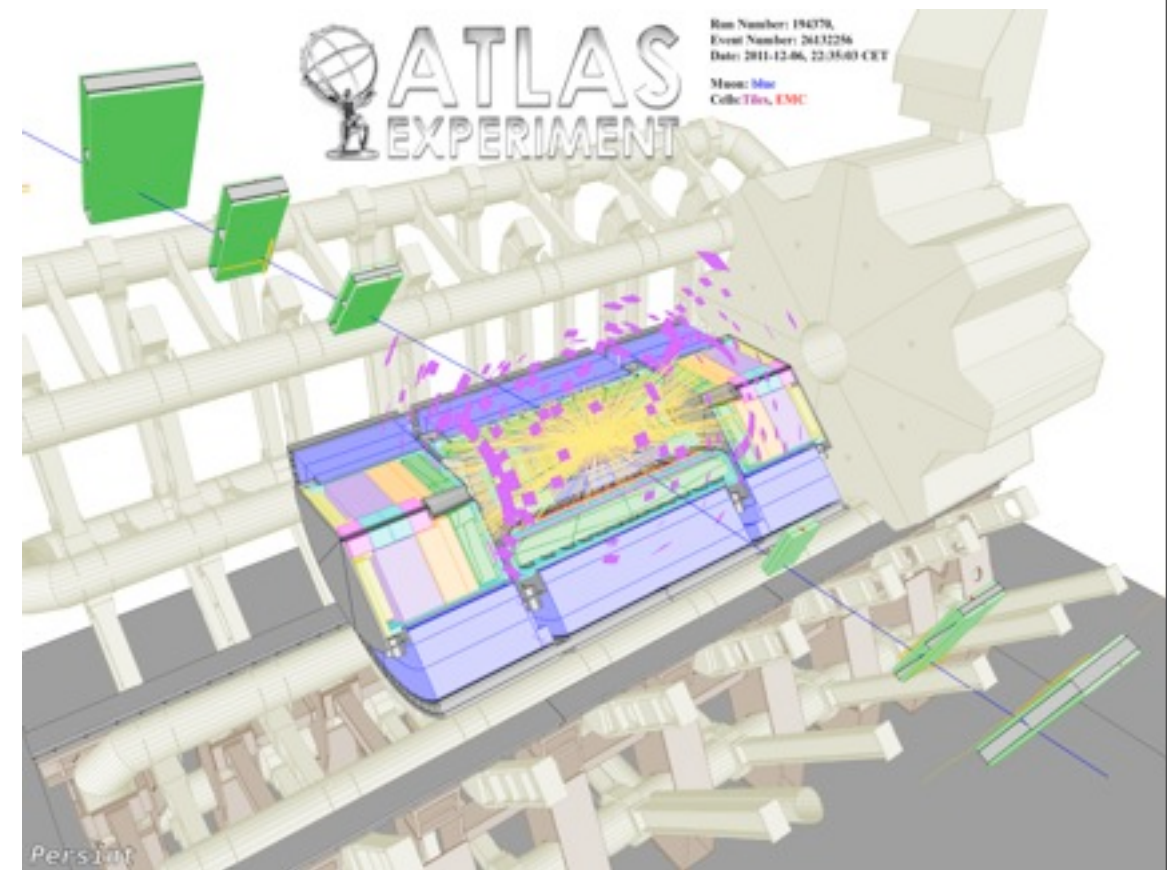
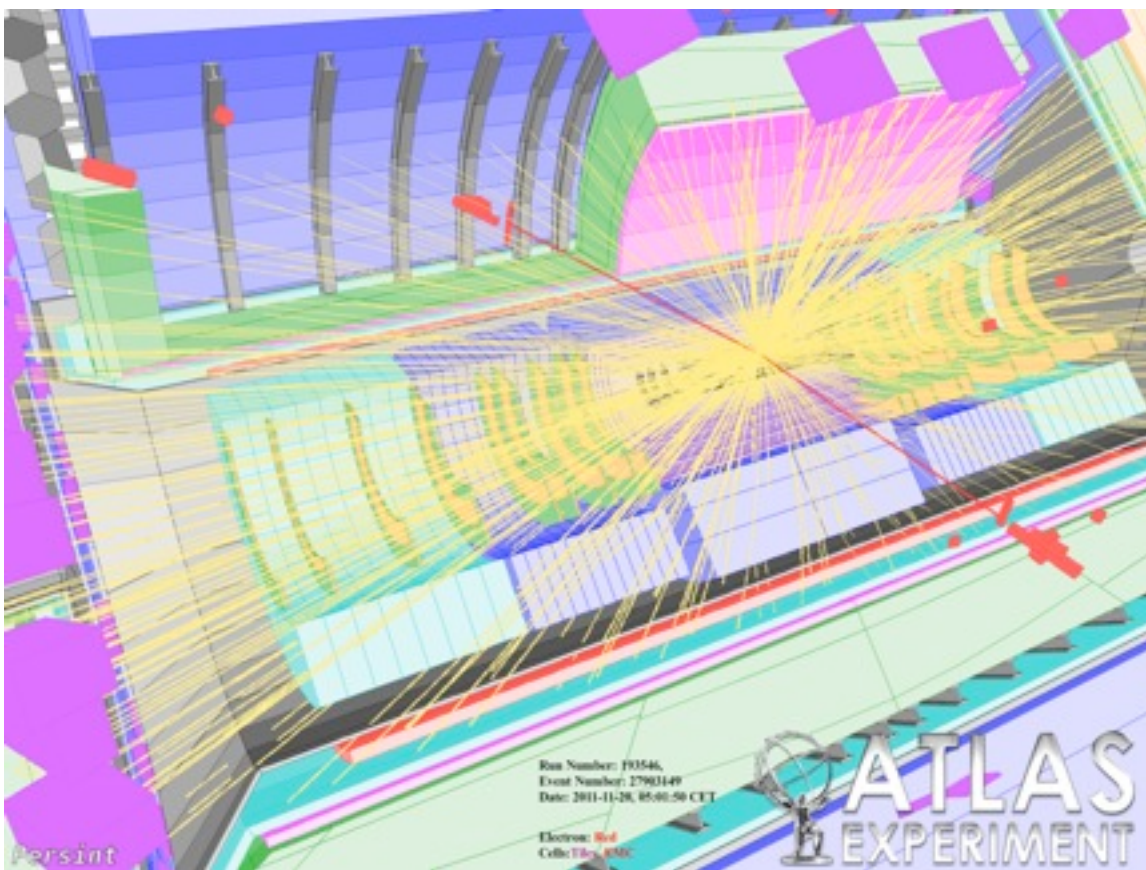


~15% suppression at intermediate  $z$  ( $\sim 0.1$ ) and 25% enhancement at very low  $z$  ( $\sim 0.02$ )  
no strong modification at large  $z$  in central collisions with respect to peripheral ones  
similar results found for  $R=0.2$  and  $0.3$  jets

# Z bosons,

$$Z \rightarrow e^+ e^-$$

$$Z \rightarrow \mu^+ \mu^-$$

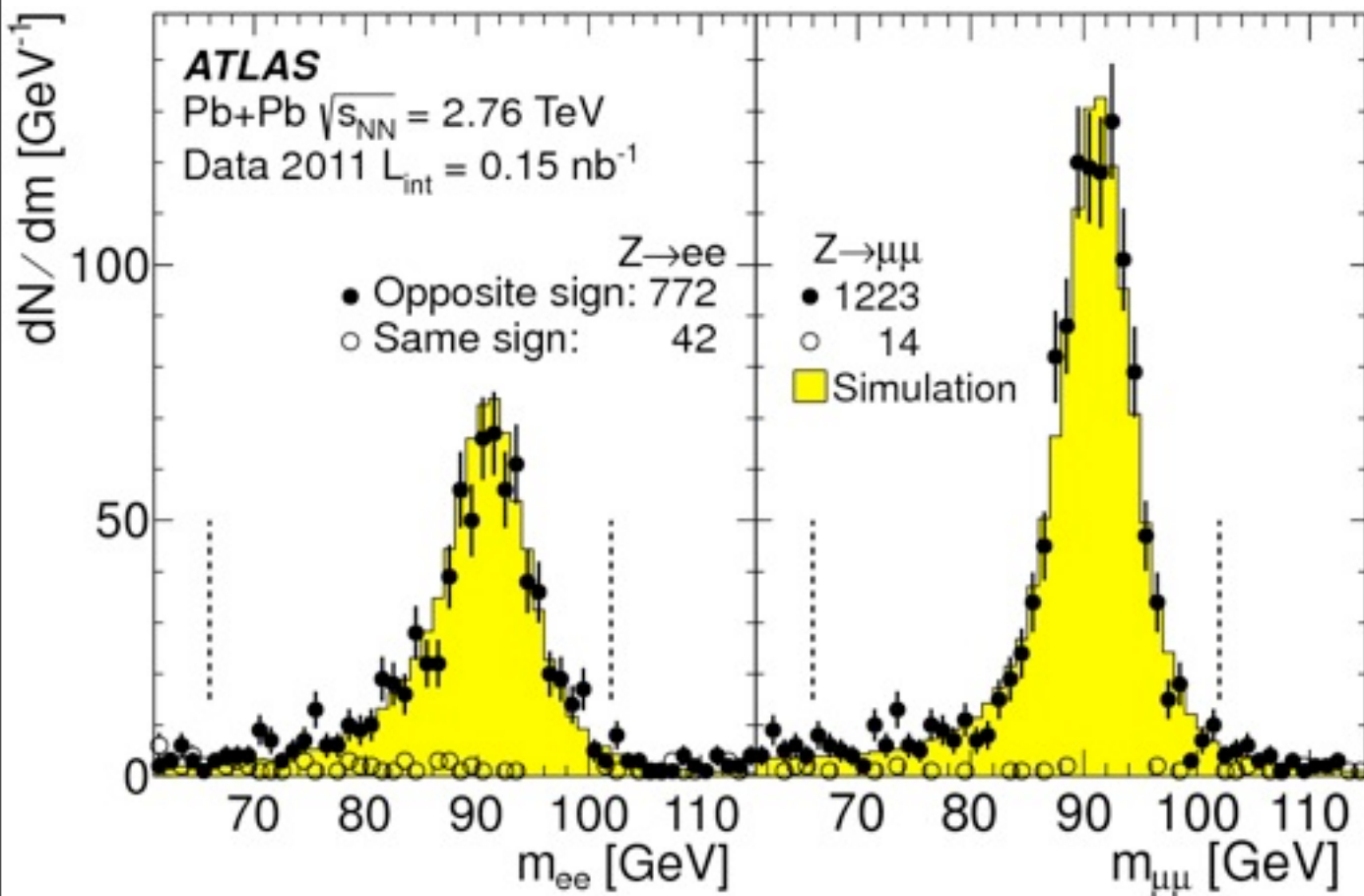


# Photons and Z, photons - jet correlations

# Z boson distributions

(submitted to *PRL*, arXiv: 1210.6486)

## invariant mass

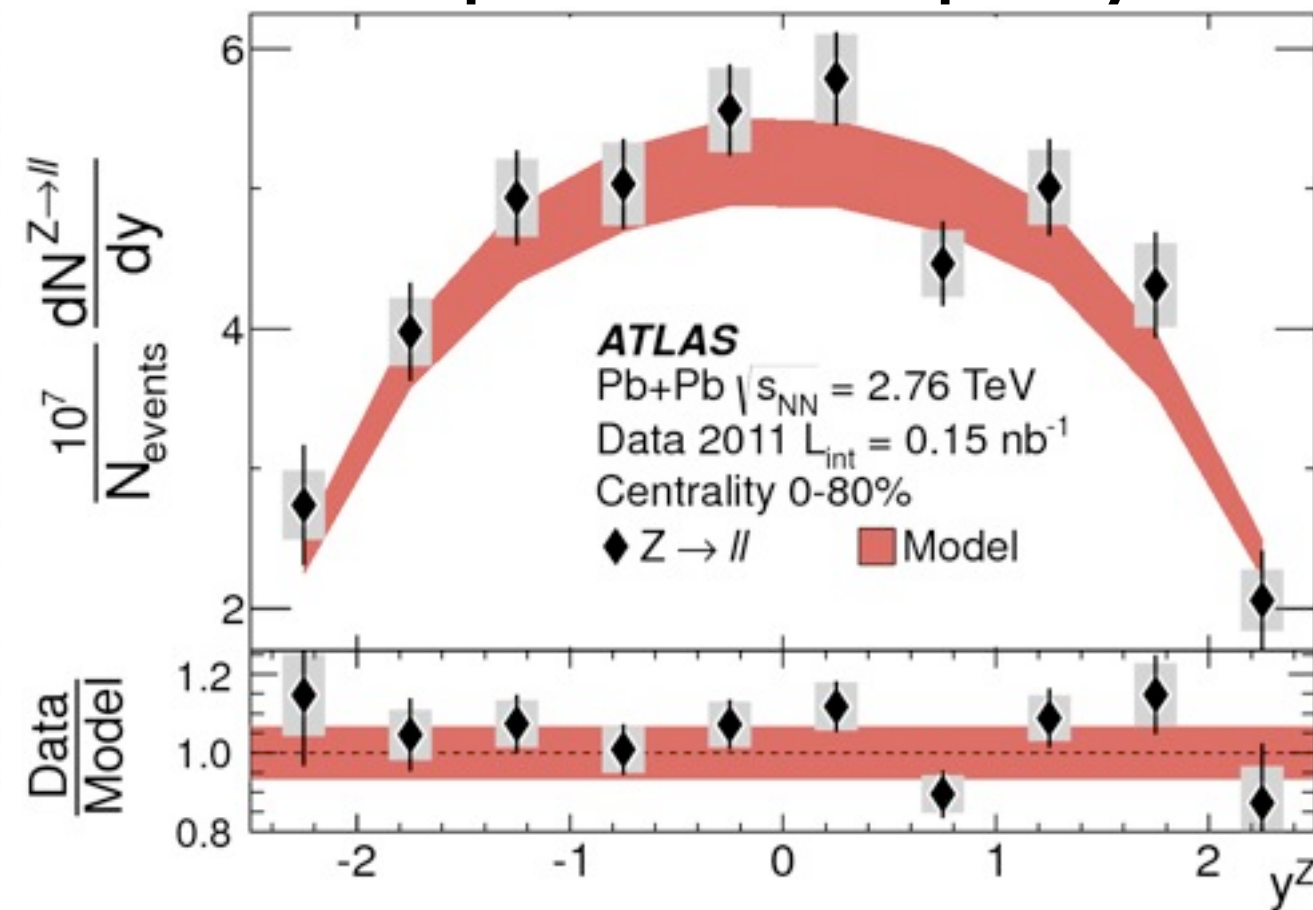


$Z \rightarrow e^+ e^-$   
 $E_T > 20$  GeV,  $|\eta| < 2.5$   
background  $\sim 5\%$

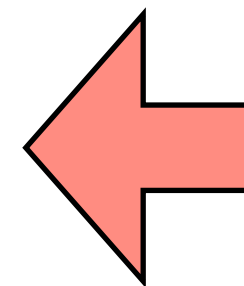
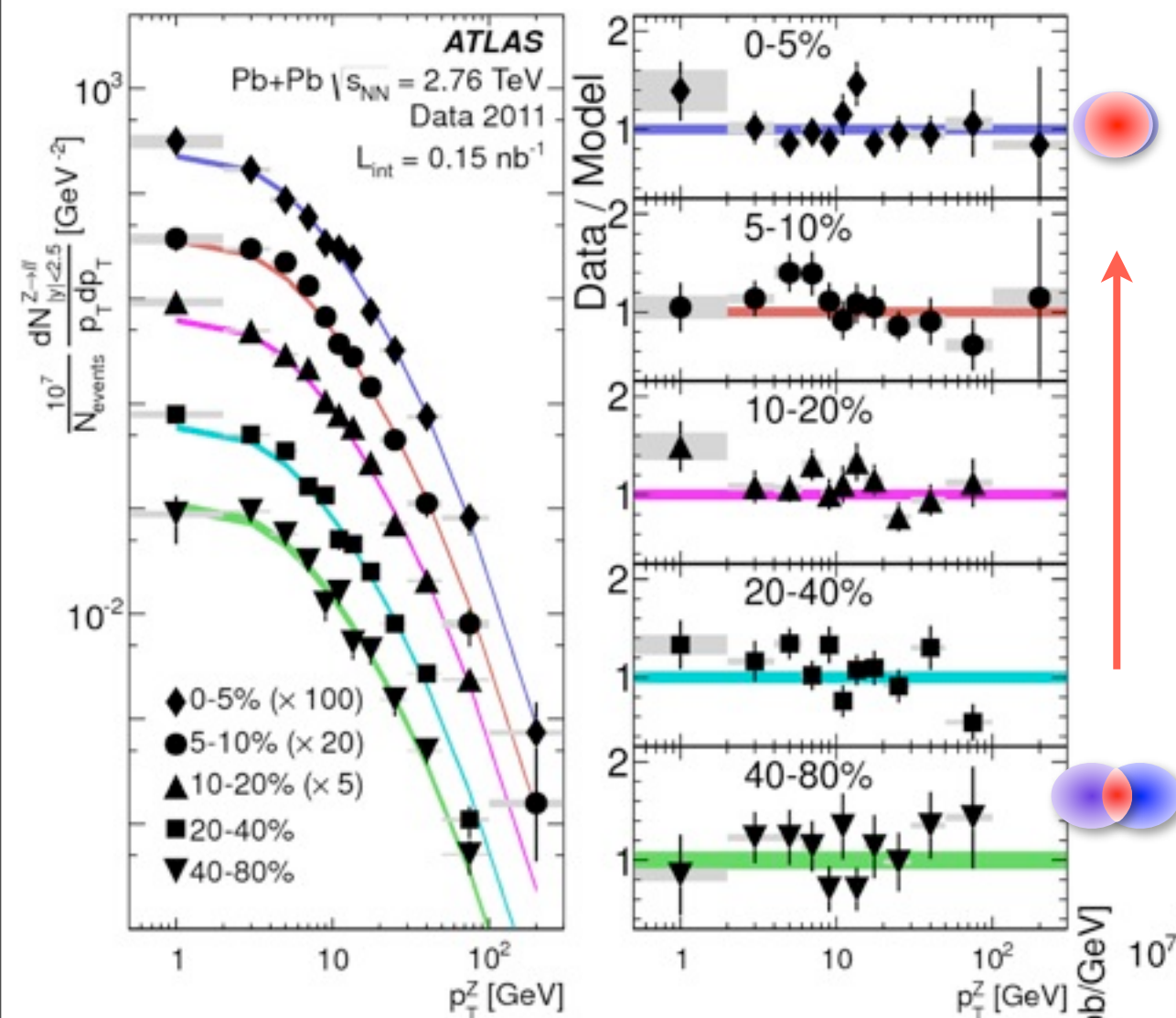
$Z \rightarrow \mu^+\mu^-$   
 $p_T > 10$  GeV,  $|\eta| < 2.5$   
background  $\sim 1\%$

simulation weighted to match  
centrality distribution in data and  
normalized in the region of vertical  
dashed lines:  $66 < m_{ll} < 102$  GeV

## per event rapidity



consistent with PYTHIA  
simulations in p+p scaled to  
NNLO cross section  $\times \langle T_{AA} \rangle$



Z's

transverse momentum distribution  
averaged over  $|y| < 2.5$

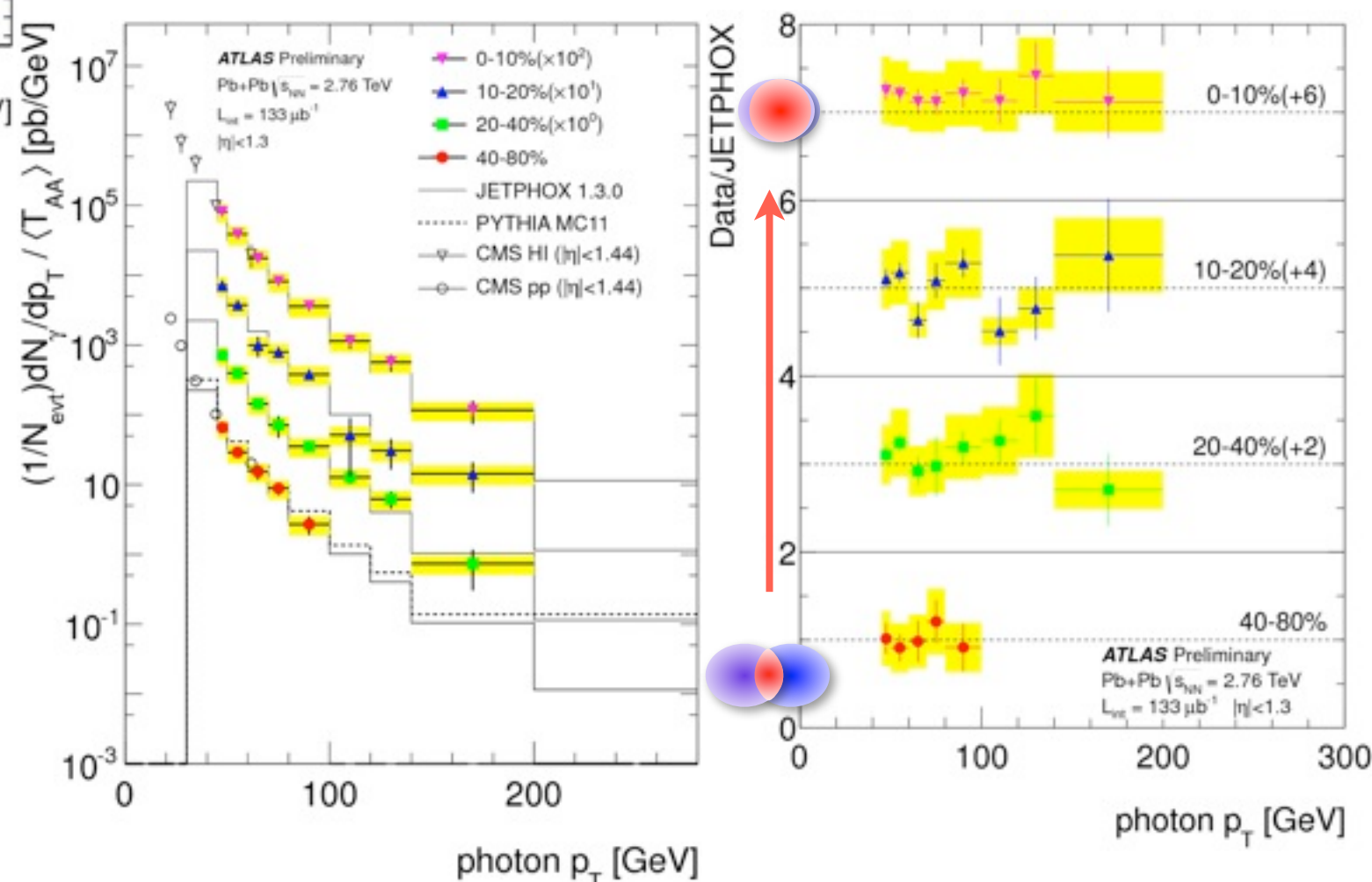
spectral shape is centrality independent  
consistent with PYTHIA simulations in p+p  
scaled to NNLO cross section  $\times \langle T_{AA} \rangle$   
(submitted to *PRL*, *arXiv: 1210.6486*)

Photons

yields scaled by  $\langle T_{AA} \rangle$  and  
compared to JETPHOX  
predictions

ratio: Data/JETPHOX  $\approx 1$

ATLAS-CONF-2012-051



# Photon per-event yields

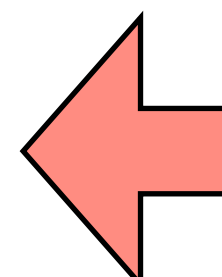
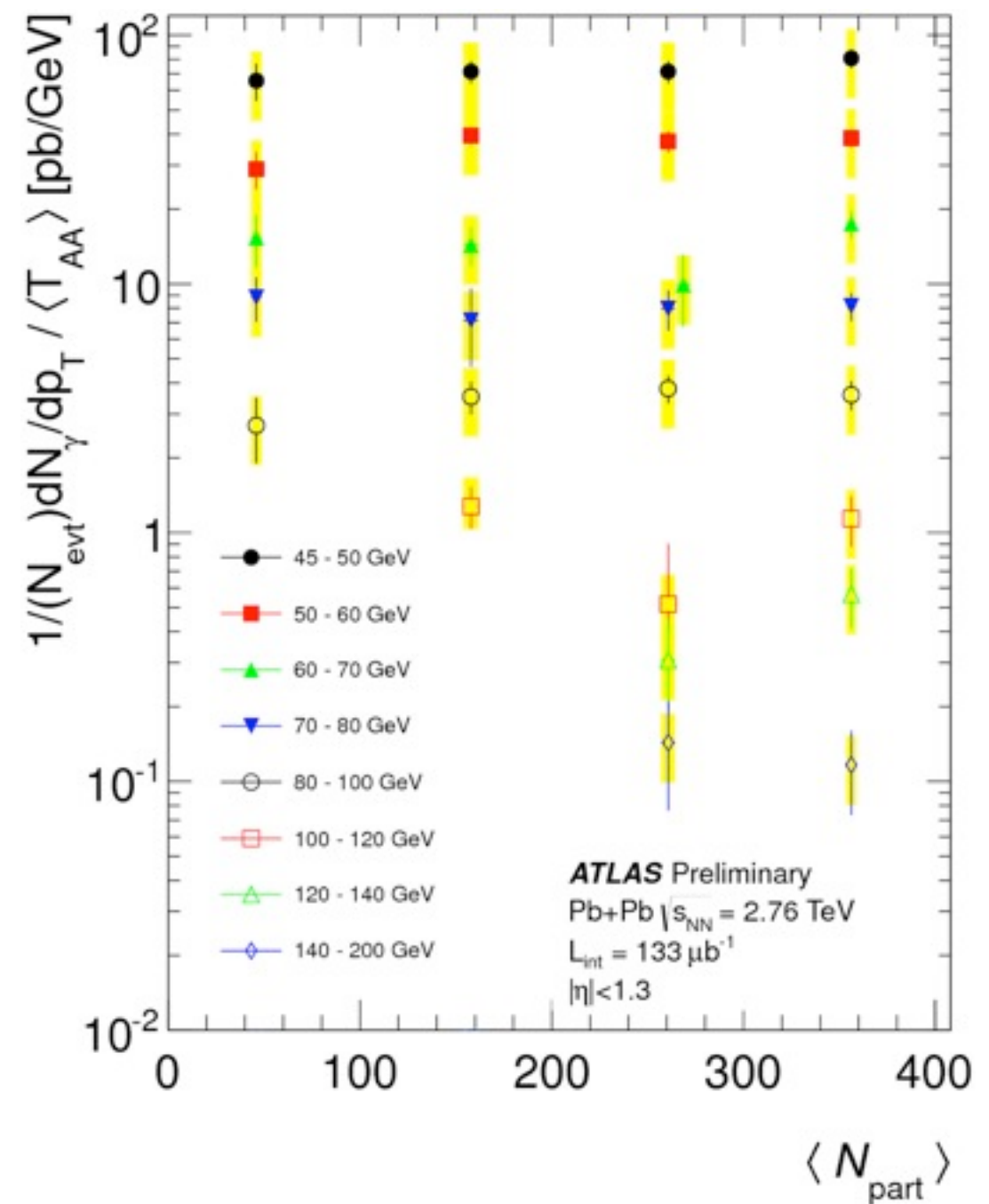
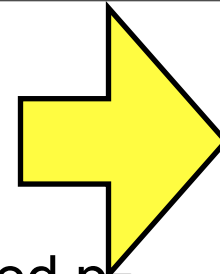
ATLAS-CONF-2012-051

no centrality dependence in any of the measured  $p_T$  intervals

photon yields in HI collisions scale linearly with  $\langle T_{AA} \rangle$  or equivalently with  $\langle N_{coll} \rangle$

photon production rates are not affected by QGP

isolated direct photons seem to be a perfect probe to help in understanding of the jet quenching phenomenon

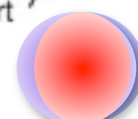
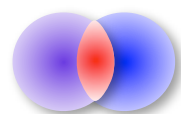
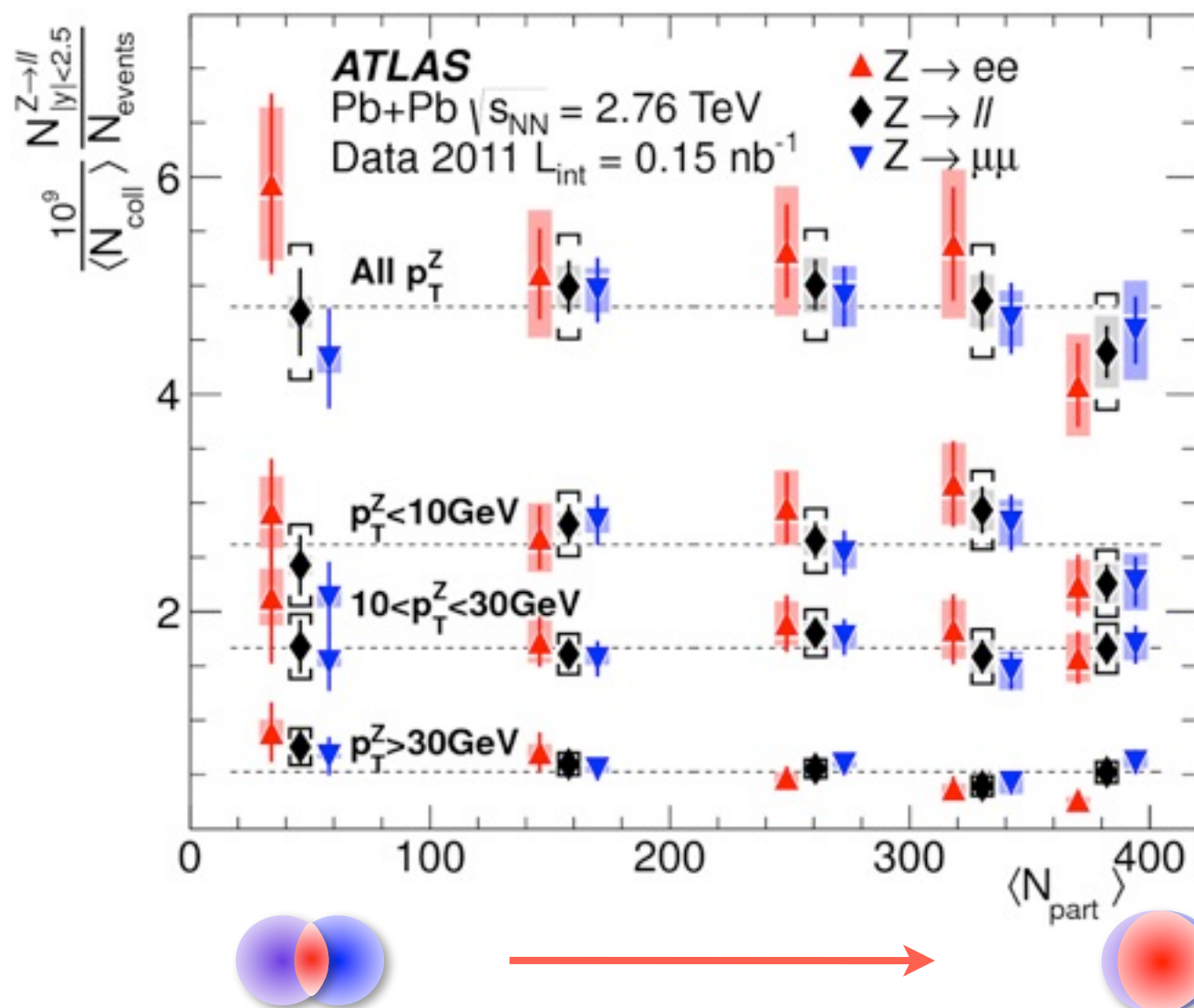


## Z boson per-event yields

integrated yields show a clear scaling with number of binary collisions

same dependence observed for three momentum ranges ( $<10$ ,  $10-30$ ,  $>30$  GeV)

(submitted to *PRL*, arXiv: 1210.6486)

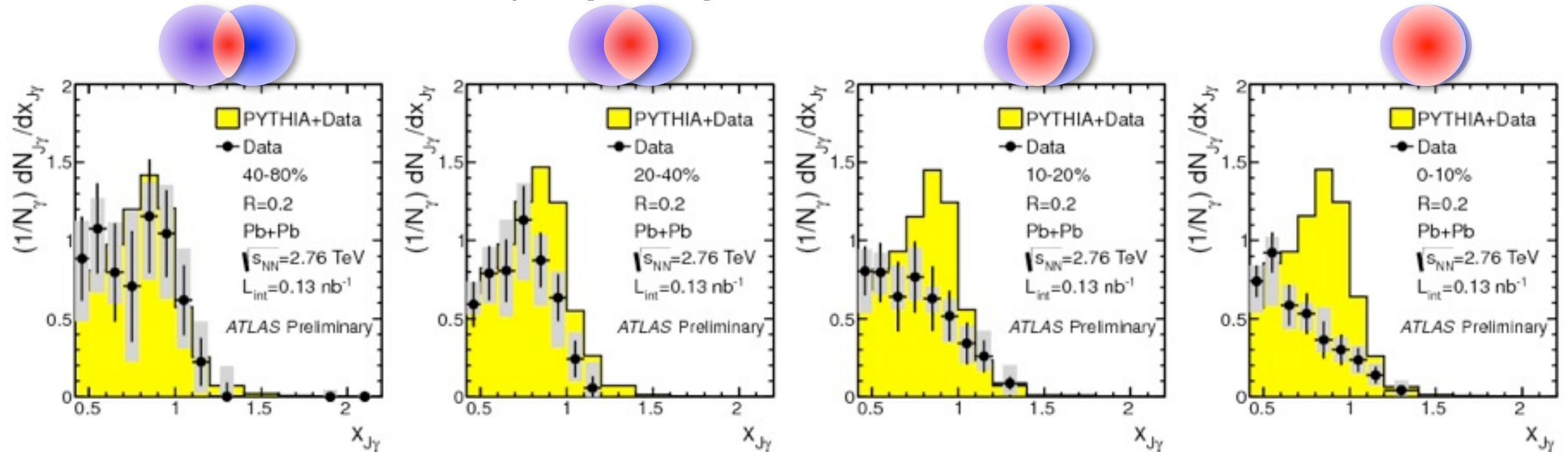


# Photon- jet $x_{J\gamma}$ distributions

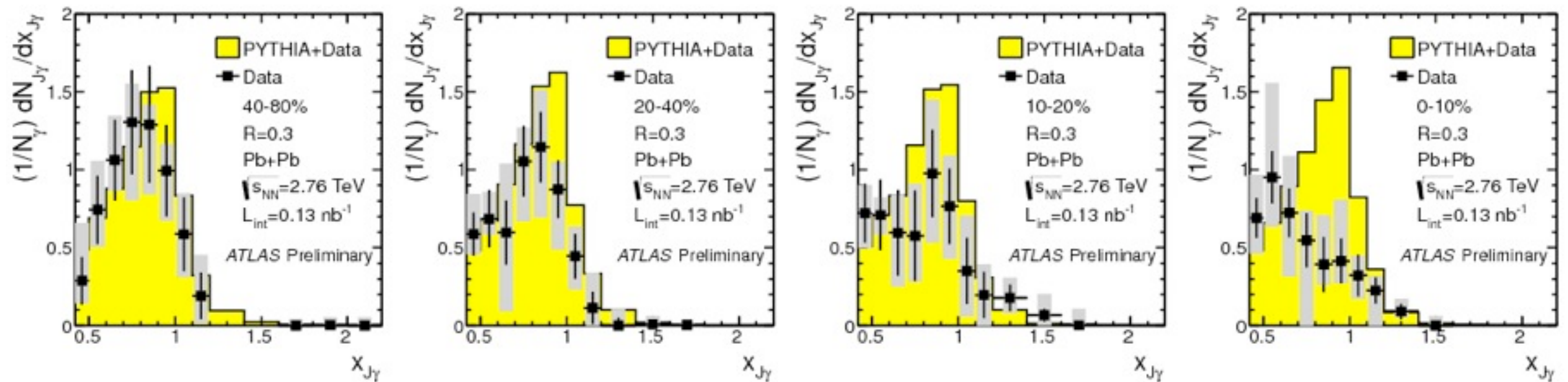
$E_\gamma > 60$  GeV: 60-90 GeV,  $|\eta| < 1.3$   
 Jet: anti- $k_T$ ,  $R=0.2, 0.3$ ,  $p_T > 25$  GeV,  $|\eta| < 2.1$   
 $\gamma$ -jet separation  $\Delta\varphi > 7\pi/8$  (back-to-back)

$$x_{J\gamma} = p_T^{\text{jet}} / p_T^\gamma$$

$R = 0.2$



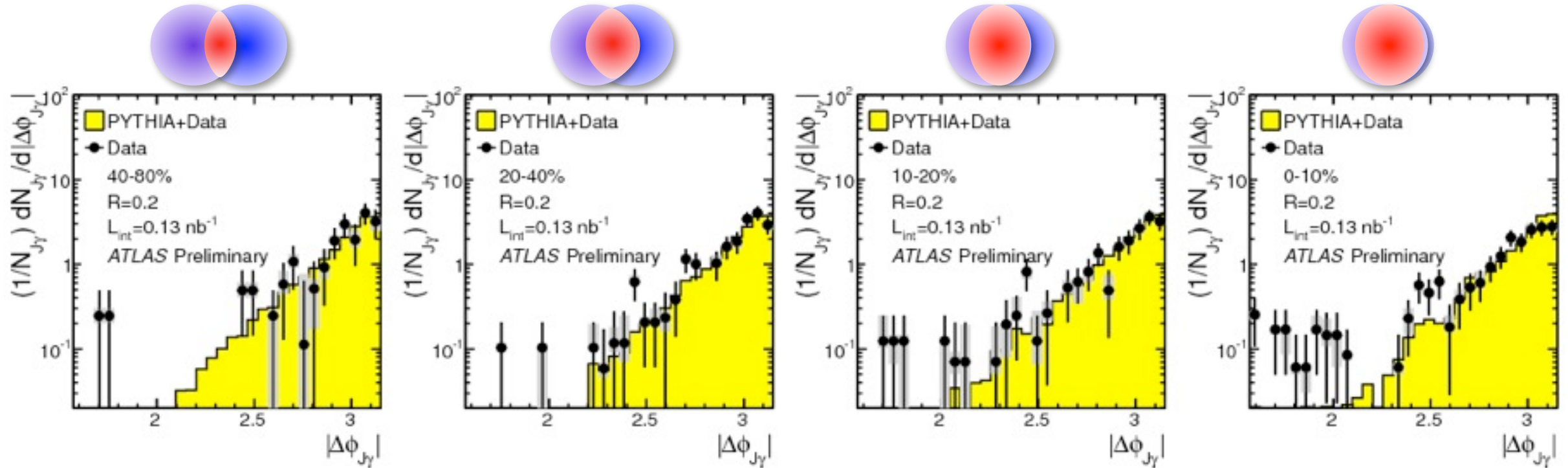
$R = 0.3$



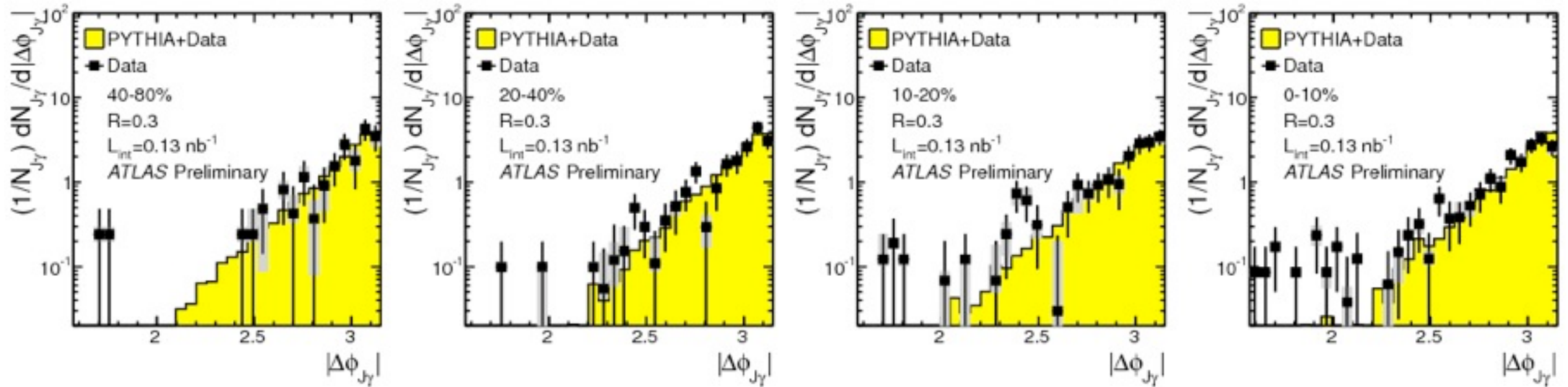
Shape and integral compatible with PYTHIA for peripheral collisions.  
 With increasing centrality shift towards smaller  $x_{J\gamma}$  and reduction of the integral.

# Photon- jet $\Delta\Phi$ distributions

$R = 0.2$



$R = 0.3$



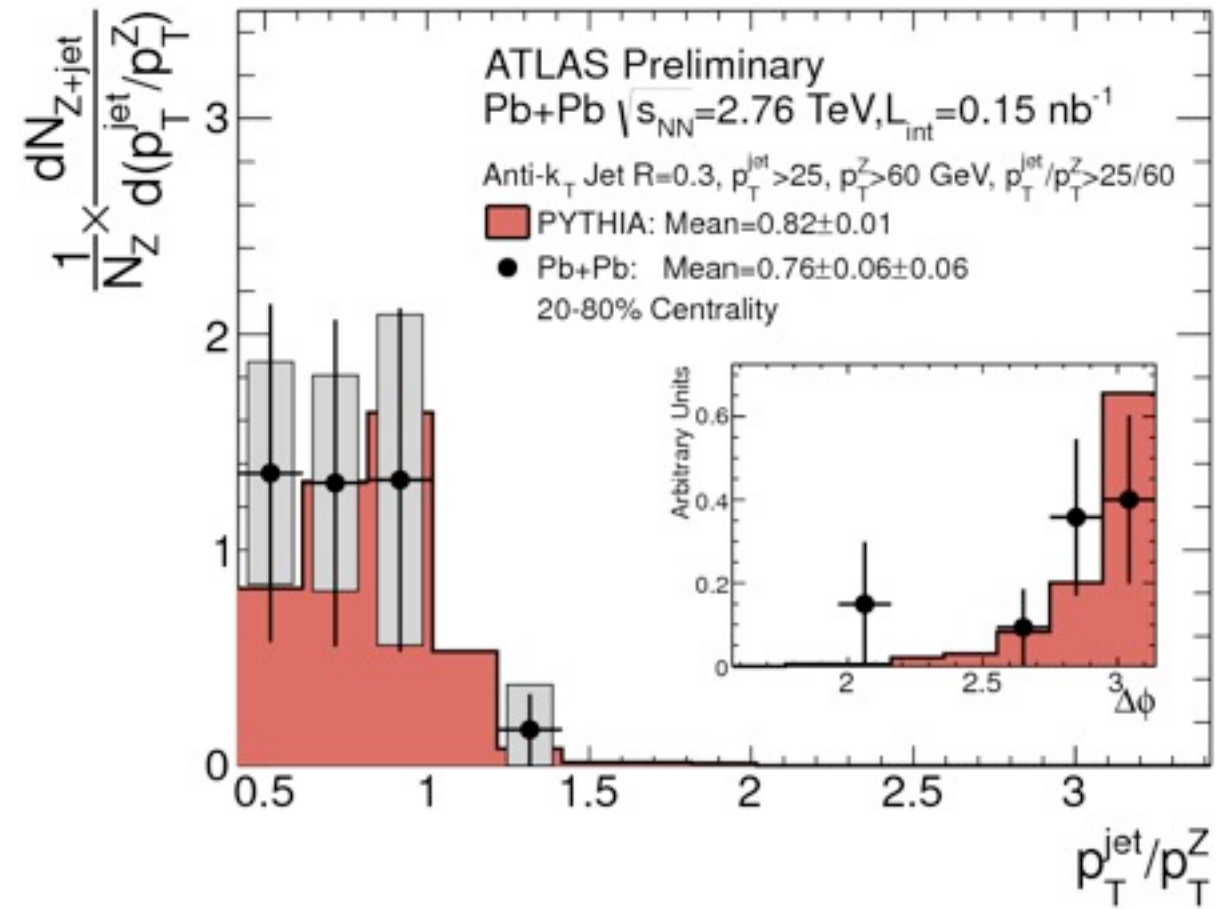
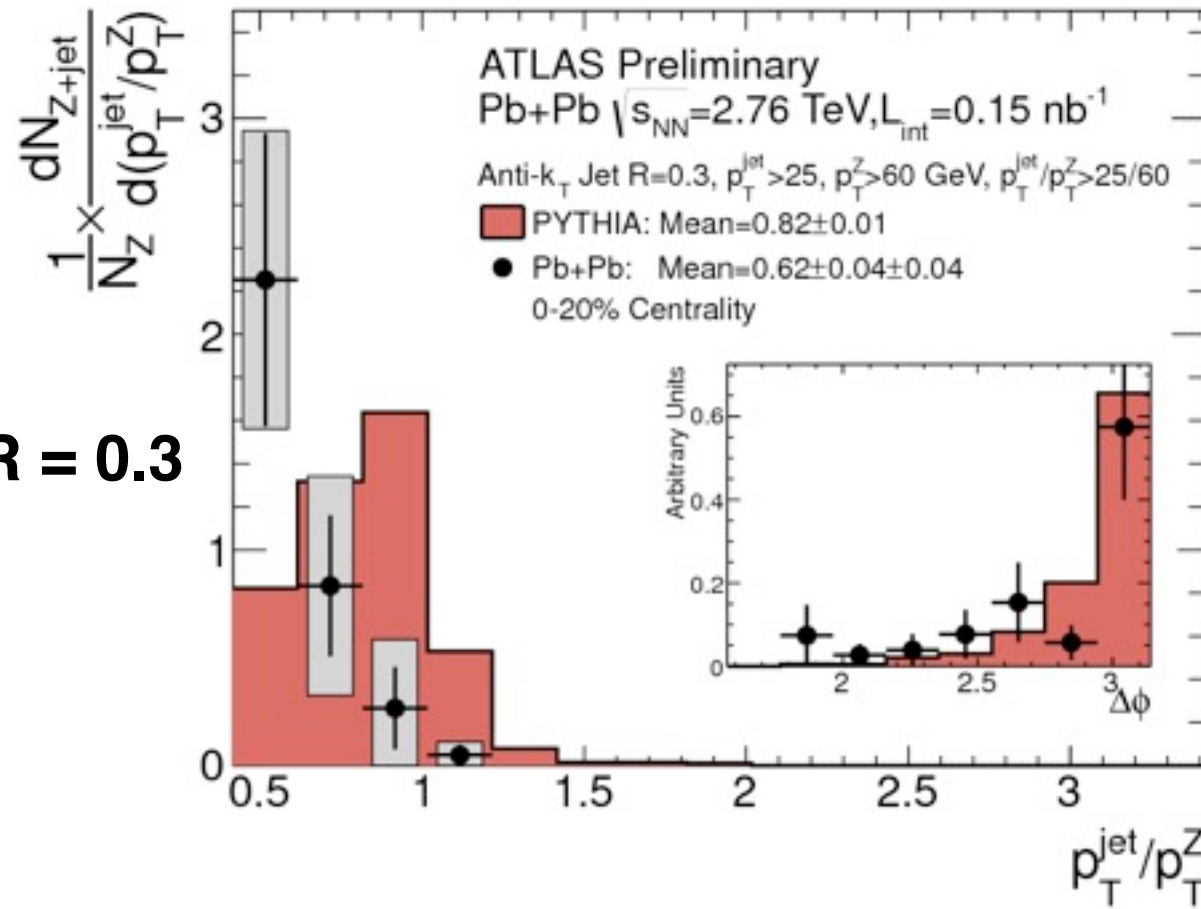
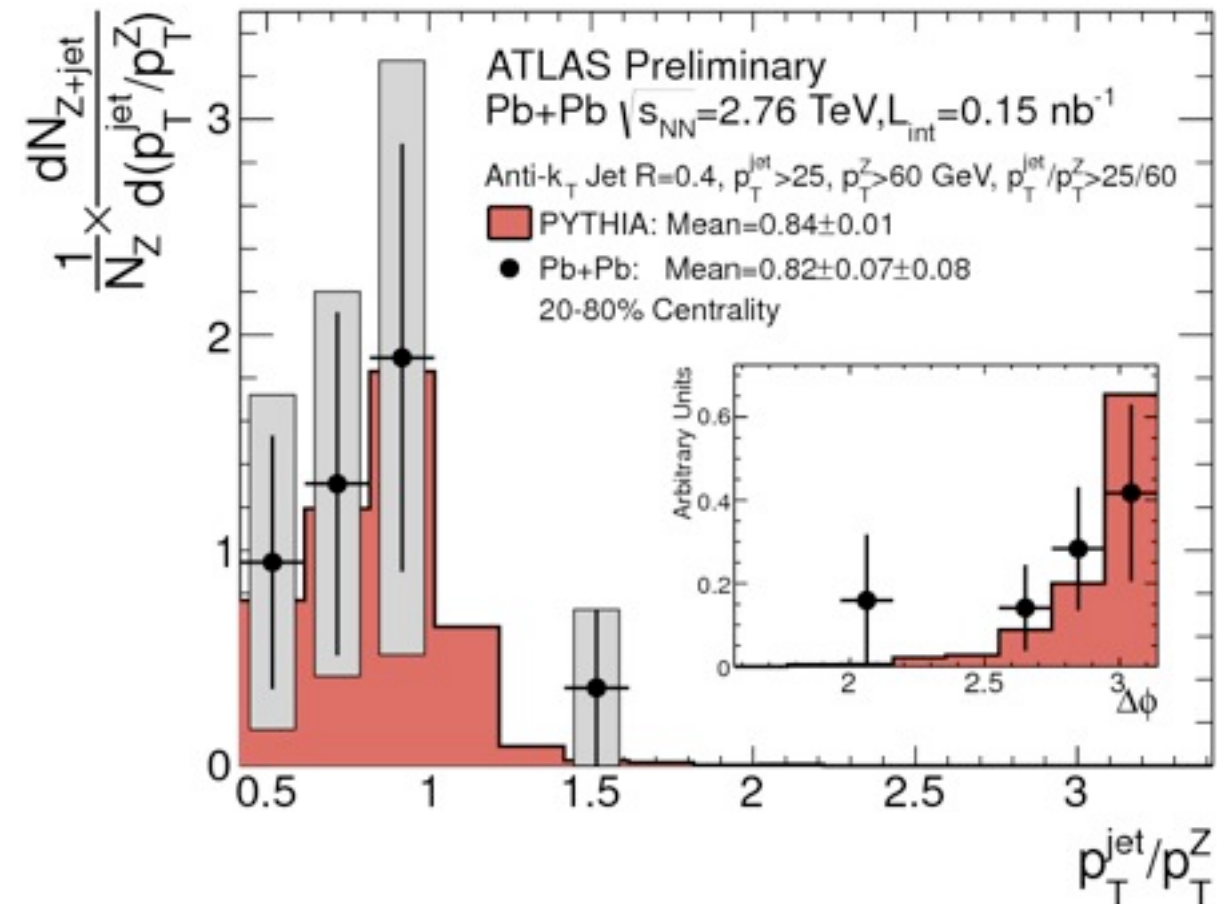
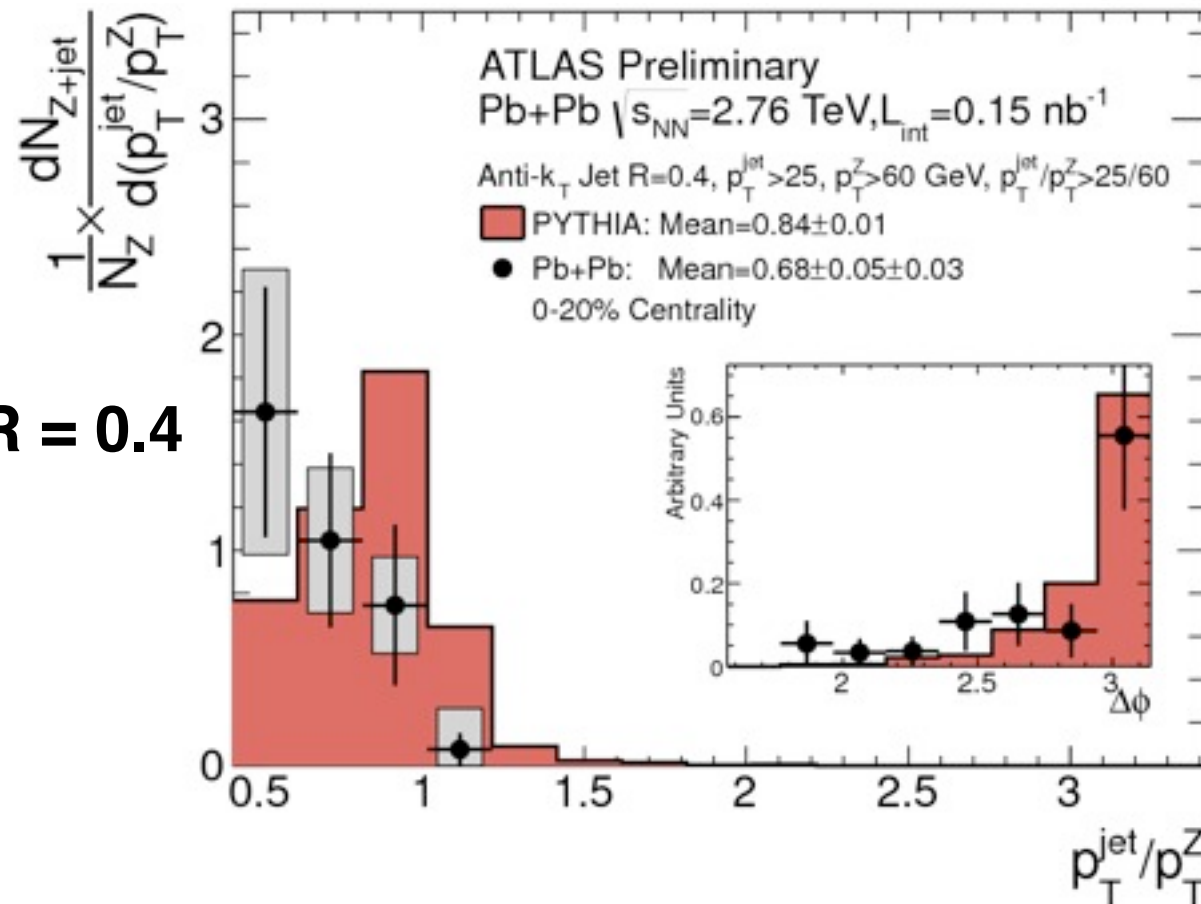
$\Delta\phi$  between photon and jet (normalized by integral).

Shapes are consistent between data and simulation in all centrality, jet cone size.

## Z - jet correlations

0-20 % centrality

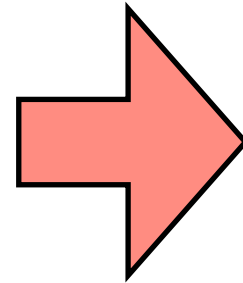
20-80 % centrality

**R = 0.3****R = 0.4**

# Centrality evolution I

ATLAS-CONF-2012-119

## Z's-jets



Extracted  $\langle p_T^{\text{jet}}/p_T^Z \rangle$  relative to MC simulations with no energy loss (PYTHIA: Z+jet events).

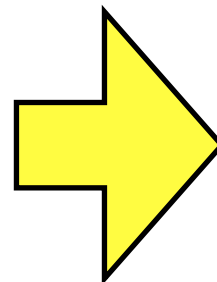
Stronger suppression for more central collisions.

The blue points refer to 0-80% centrality, and therefore are not independent relative to the black points.

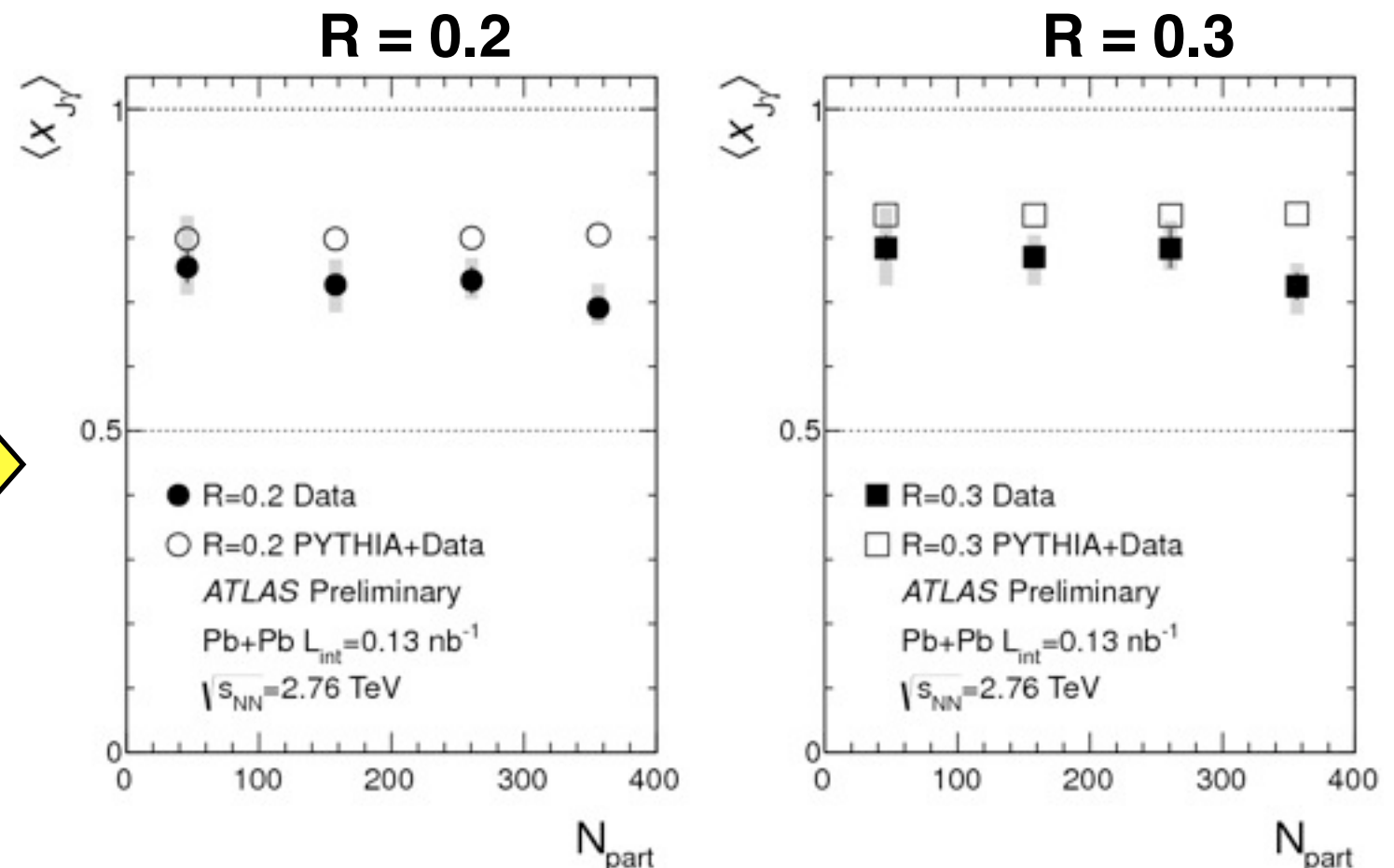


ATLAS-CONF-2012-121

## Photons-jets



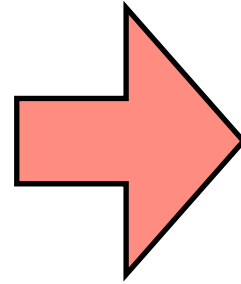
Downward shift of  $\langle x_{j\gamma} \rangle$  (jets more quenched).



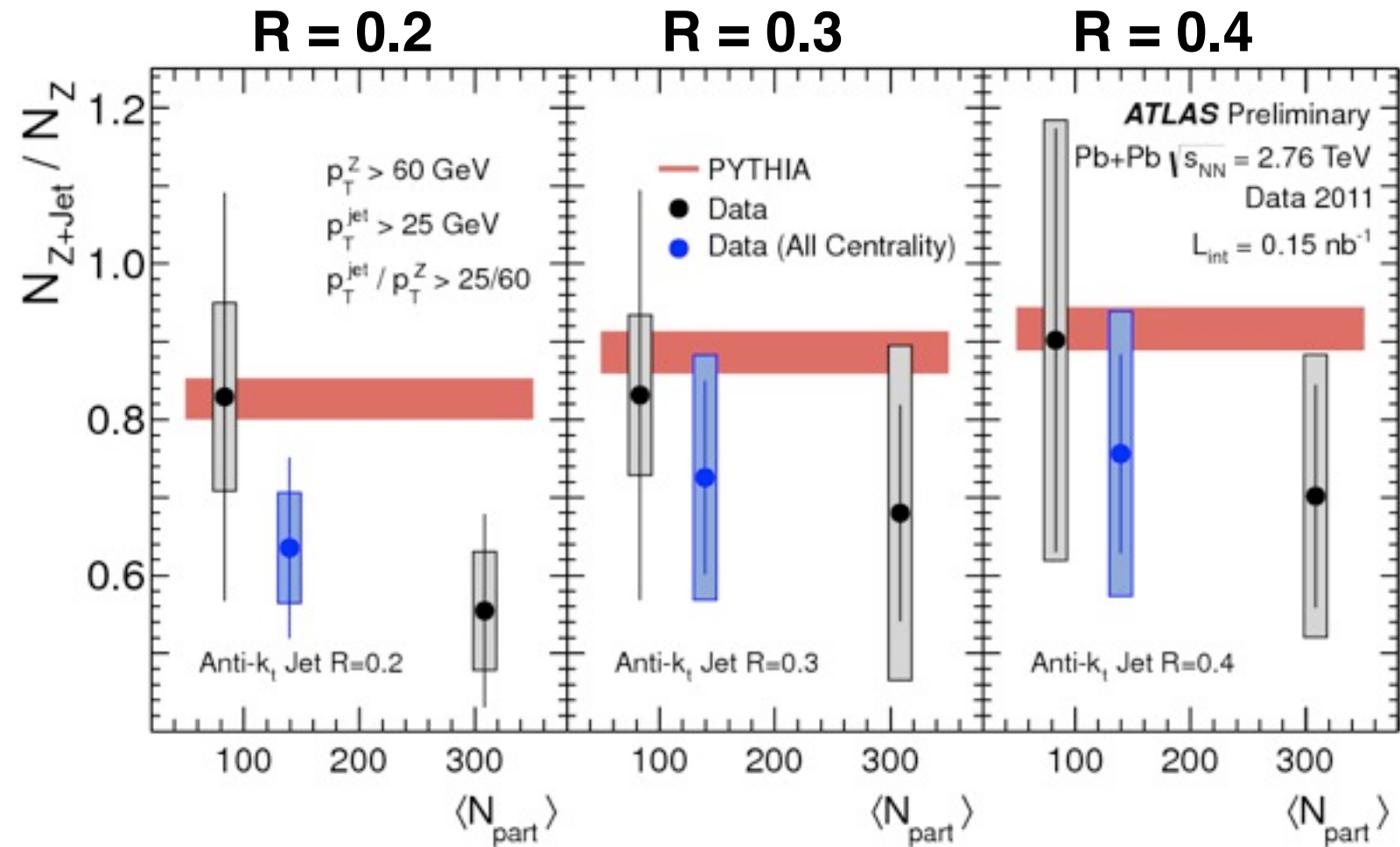
# Centrality evolution II

ATLAS-CONF-2012-119

## Z's-jets

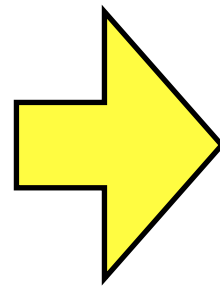


The fraction of events with a Z boson ( $p_T^Z > 60$  GeV) that also have a jet reconstructed ( $p_T^{\text{jet}} > 25$  GeV,  $p_T^{\text{jet}}/p_T^Z > 25/60$ ).

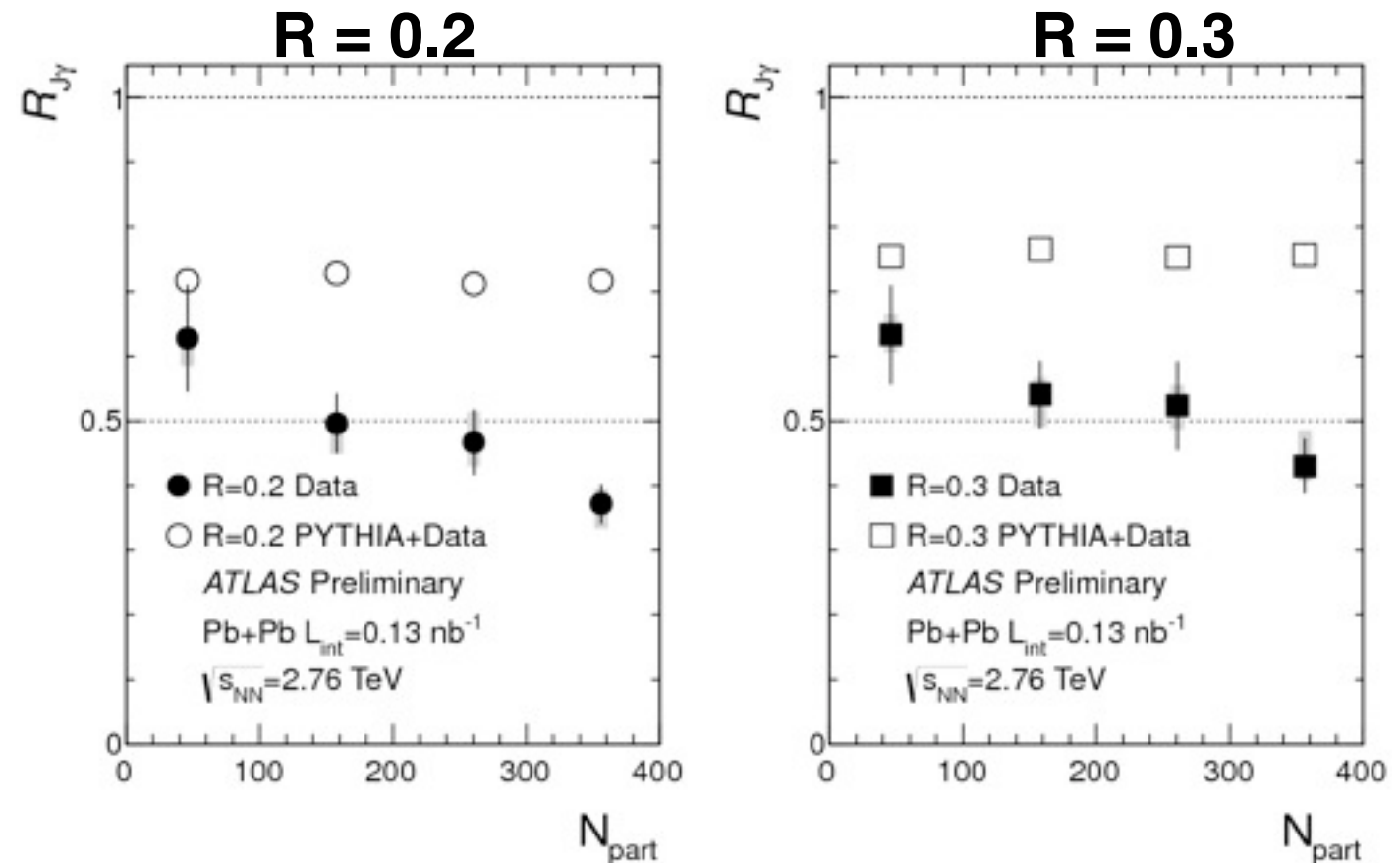


ATLAS-CONF-2012-121

## Photons-jets



Most peripheral events consistent with PYTHIA truth, and strong centrality dependence: nearly half of the photons in central events do not have a matching jet: downward shift of  $R_{j\gamma}$ .

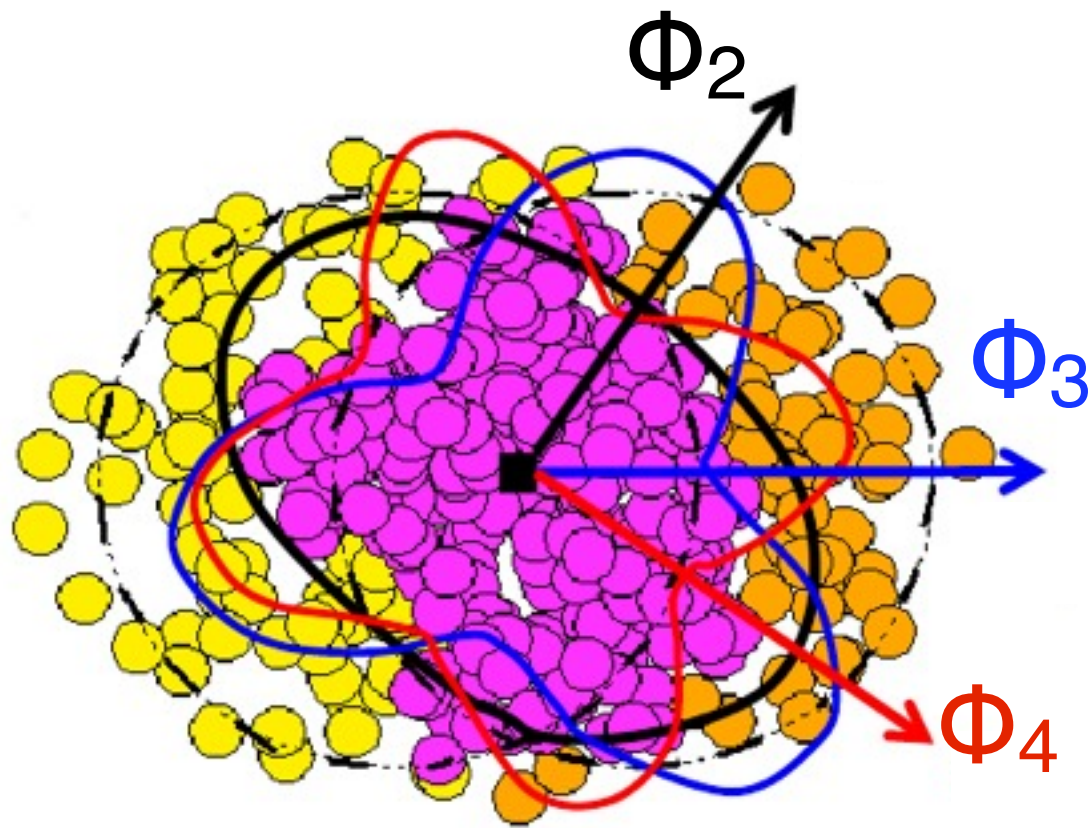


# Azimuthal anisotropy

Spatial deformations in the initial overlap region are transformed into the final state momentum anisotropy

studied via Fourier decomposition of the azimuthal angle distribution measured relative to the initial symmetry plane  $\Phi_n$   
A.M. Poskanzer, S. A. Voloshin, Phys. Rev. C58, 1671 (1998) :

$$E \frac{d^3 N}{dp^3} = \frac{1}{2\pi p_T} \frac{d^2 N}{dp_T d\eta} \left( 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos[n(\phi - \Phi_n)] \right)$$



phase of  $v_n$  accumulated over many events;

this event-averaged  $v_n$  mostly reflects the hydrodynamic response of the created matter to the average collision geometry in the initial state.

$$v_n = \langle \cos[n(\phi - \Phi_n)] \rangle$$

Event plane is measured based on energy deposition in the first sampling layer of FCal  
Fourier harmonics are reconstructed in inner detector from charged particle tracks:

$$p_T > 0.5 \text{ GeV}$$

$$|\eta| < 2.5$$

Reaction plane ( $\Psi^{\text{RP}}$ ) is approximated by event plane ( $\Psi_n^{\text{EP}}$ ) measured in FCal:

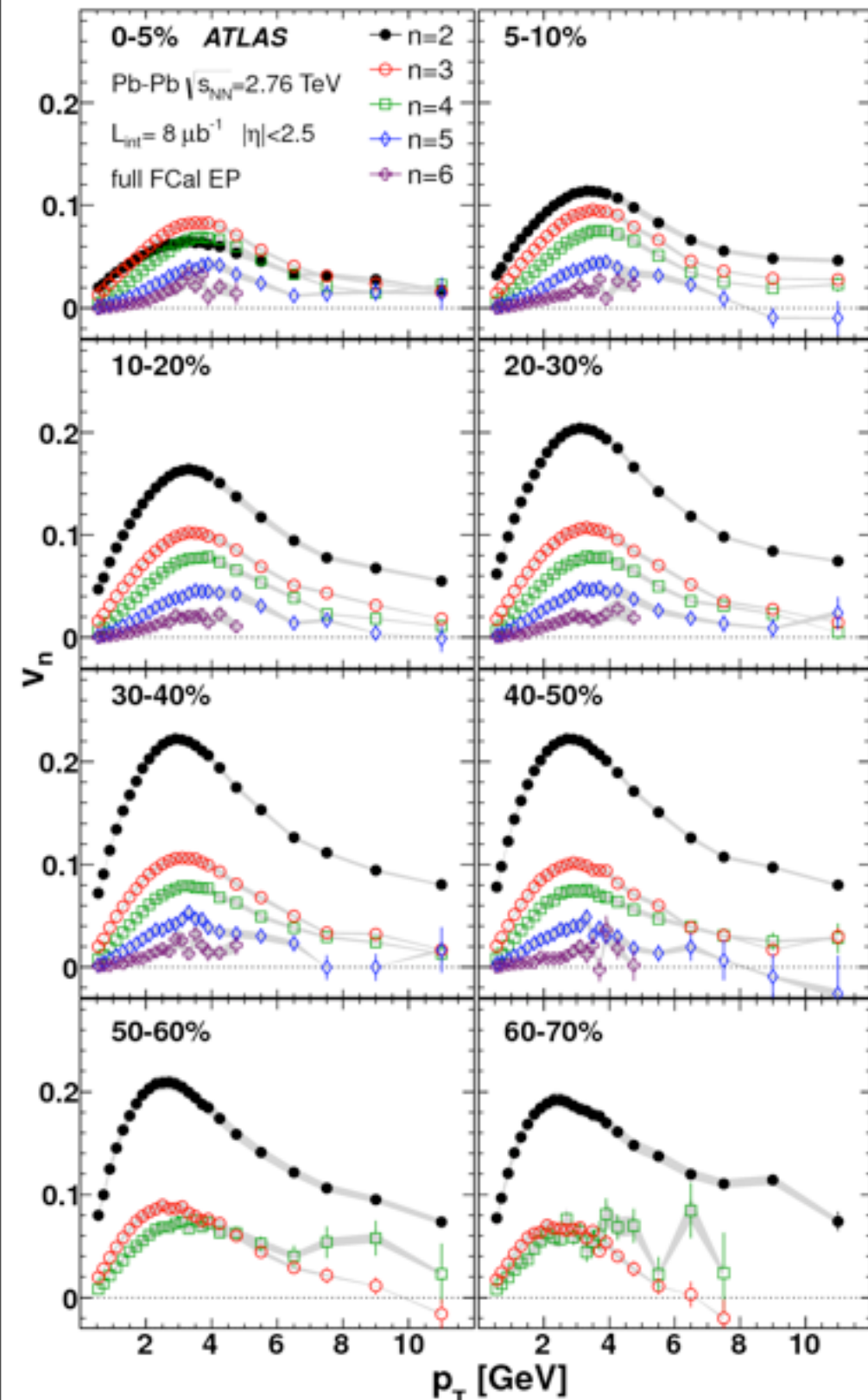
$$\Psi_n^{\text{EP}} = \frac{1}{n} \tan^{-1} \frac{\sum_i E_{T,i}^{\text{tower}} w_i \sin(n\phi_i)}{\sum_i E_{T,i}^{\text{tower}} w_i \cos(n\phi_i)}$$

# v2-v6 from the event plane method

PHYSICAL REVIEW C 86, 014907 (2012)



Measurement of the azimuthal anisotropy for charged particle production in  $\sqrt{s_{NN}} = 2.76$  TeV lead-lead collisions with the ATLAS detector

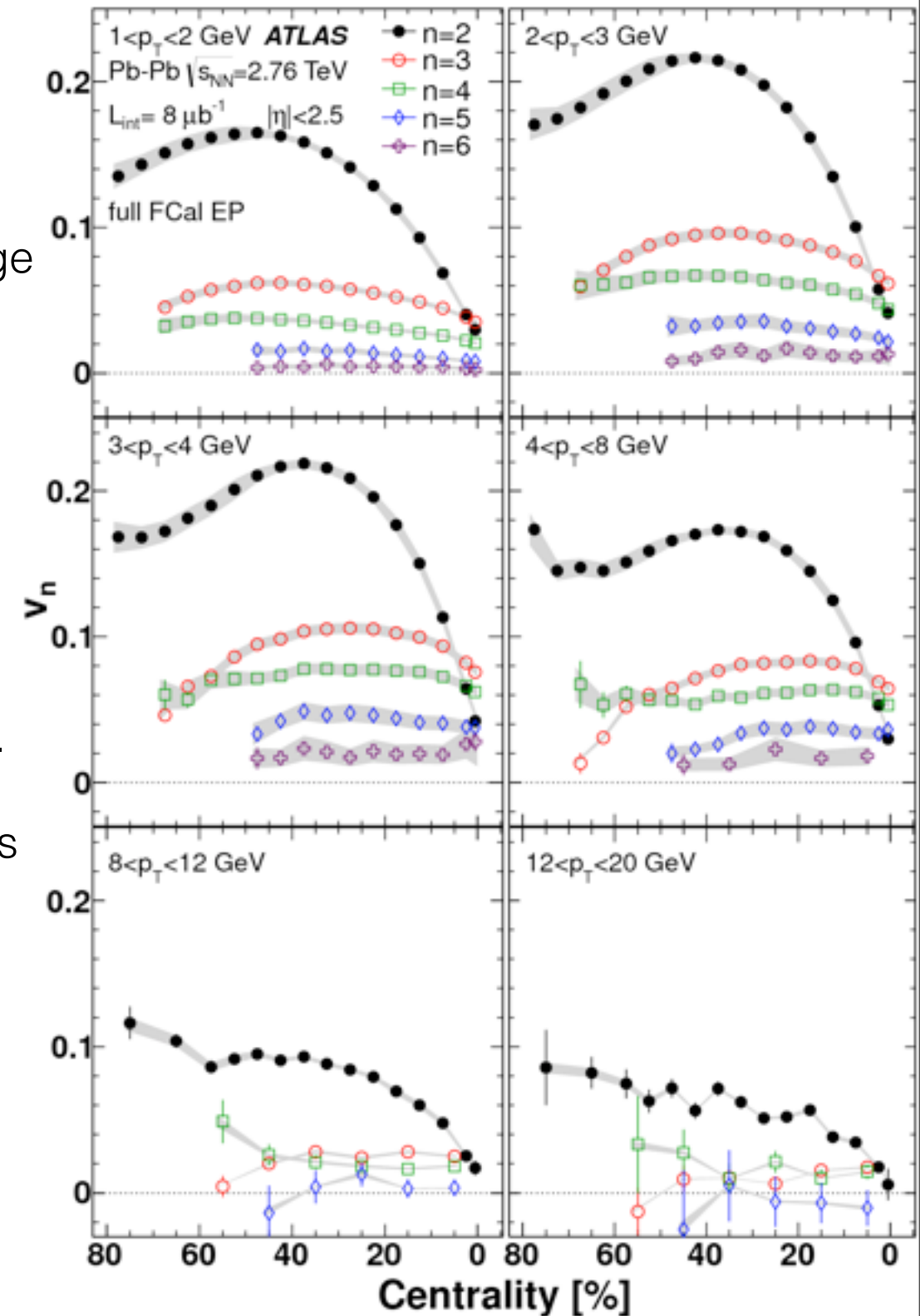


Significant  $v_2 - v_6$  are measured in broad range of  $p_T$ ,  $\eta$  and centrality.

$p_T$  dependence for all measured amplitudes show similar trend.

Stronger centrality dependence of  $v_2$  than higher order harmonics.

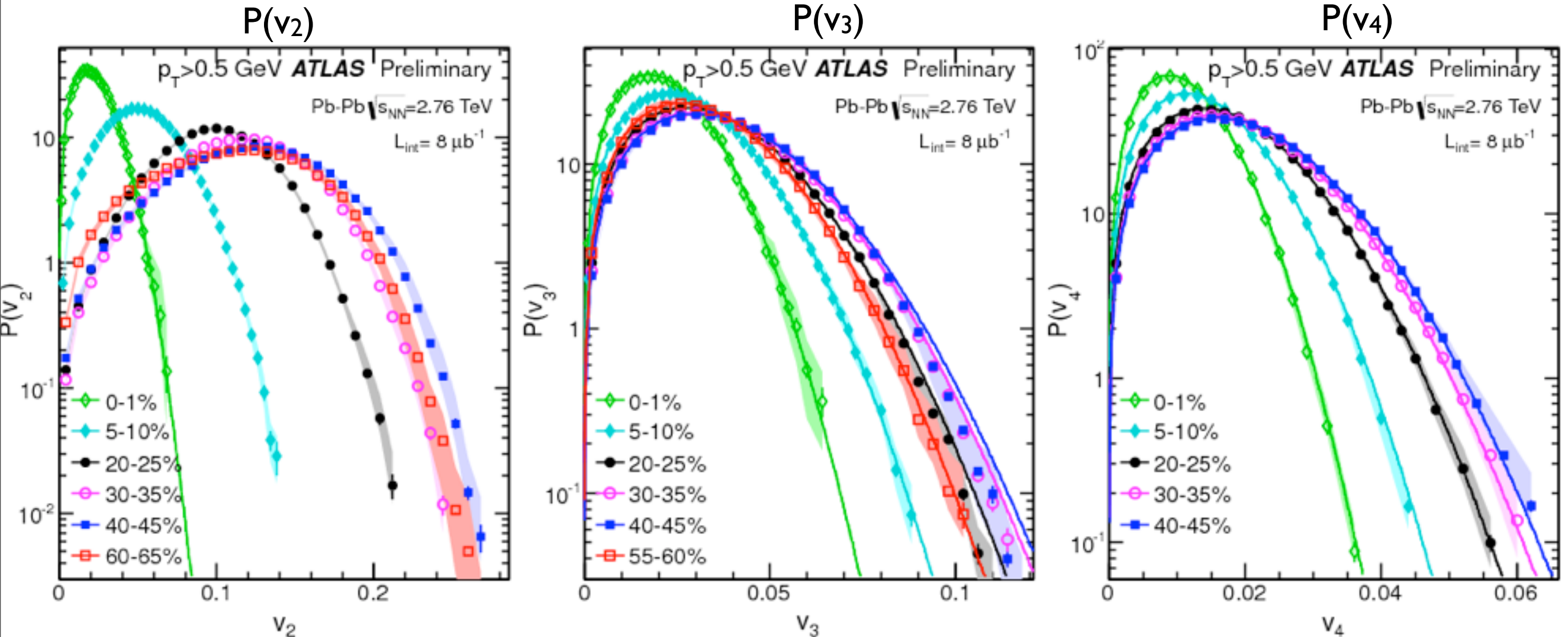
In most central collisions (0-5%):  $v_3$ ,  $v_4$  can be larger than  $v_2$ .



# Event-by-event flow harmonics

New technique – direct measure of flow harmonics fluctuations!

Event-by-event unfolded  $v_n$  distributions normalized to unit, for  $n=2-4$



$$P(v_n) = \frac{v_n}{\sigma^2} e^{-\frac{v_n^2}{2\sigma^2}}, \sigma = \sqrt{\frac{2}{\pi}} \langle v_n \rangle$$

Lines represent radial projections of 2D Gaussians, rescaled to  $\langle v_n \rangle$

for  $v_2$  only in the 0-2% of most central collisions

for  $v_3$  and  $v_4$  over all centralities

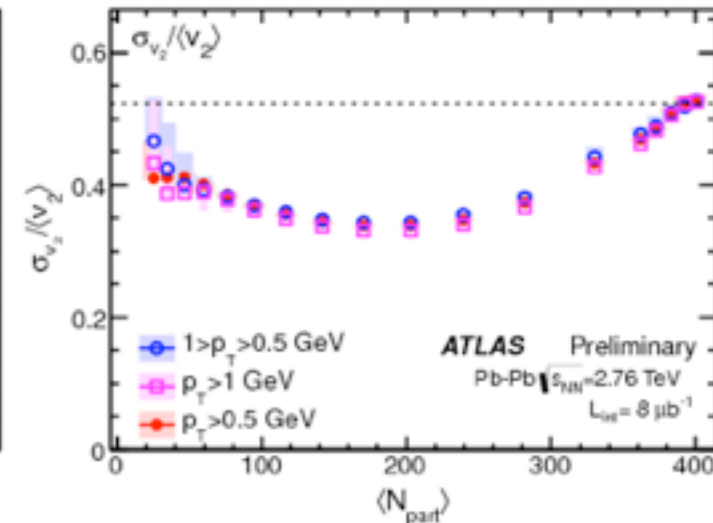
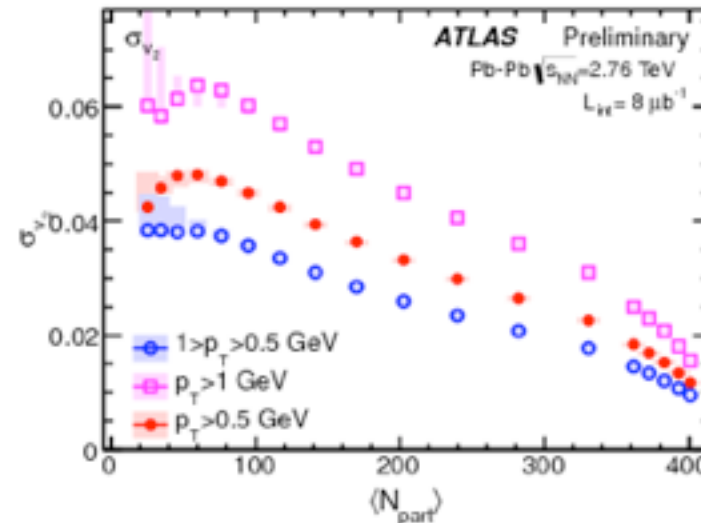
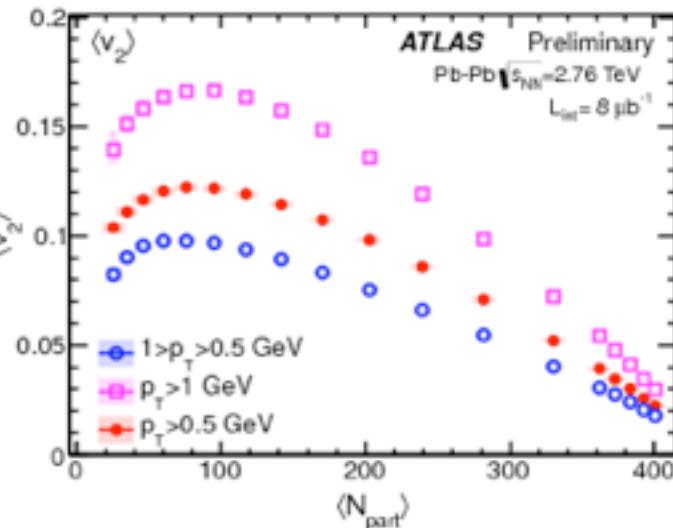
Quantities calculated directly from these distributions:

mean  $\langle v_n \rangle$ ,

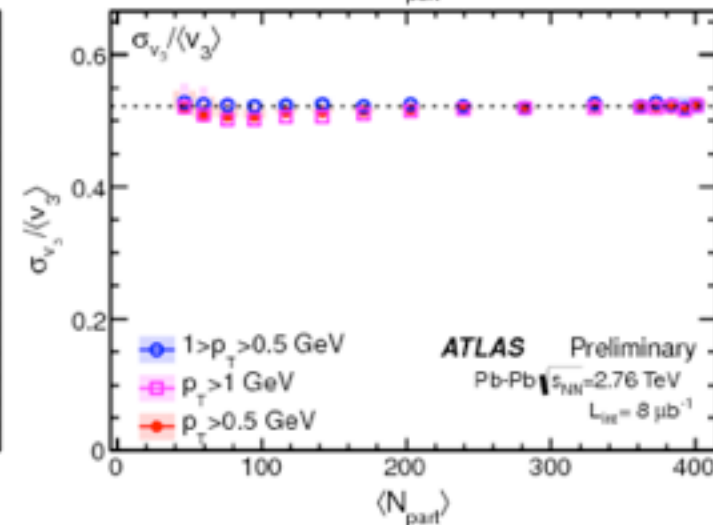
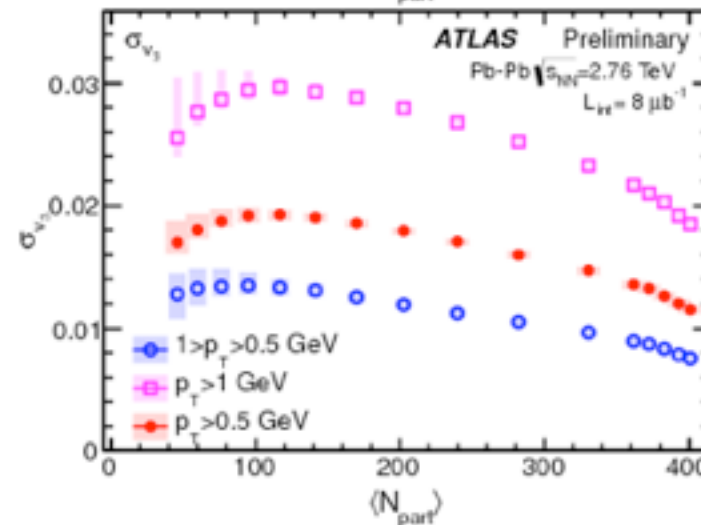
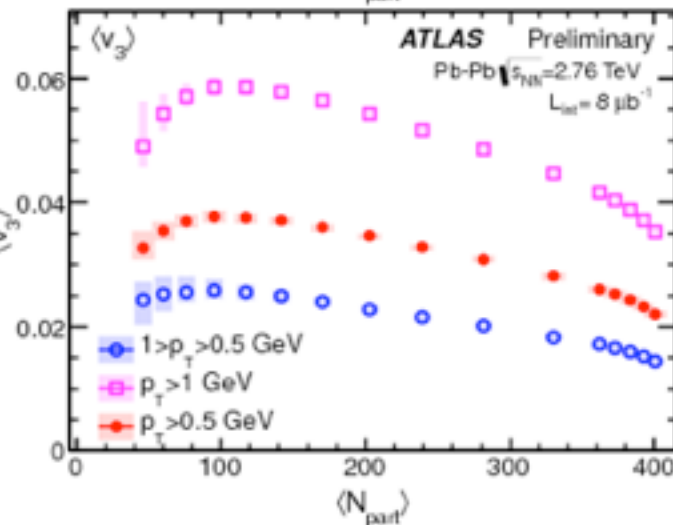
width  $\sigma_{v_n}$ ,

ratio  $\sigma_{v_n} / \langle v_n \rangle$

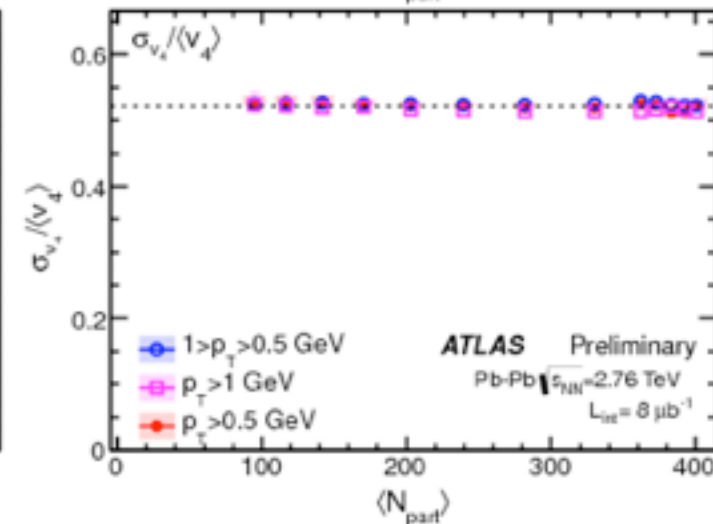
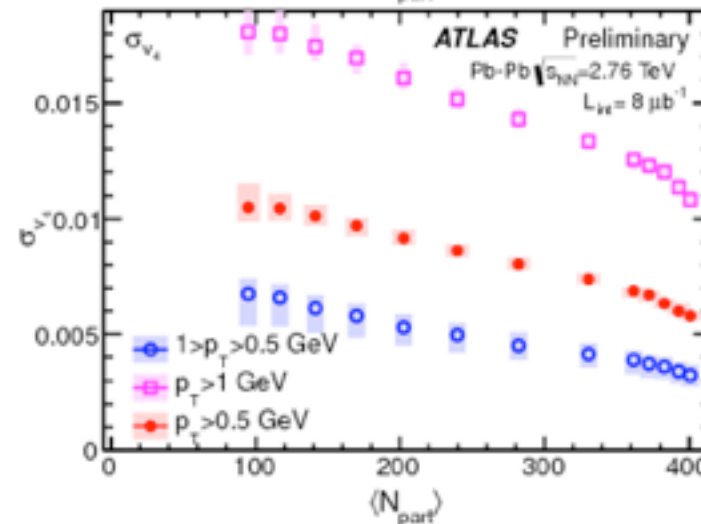
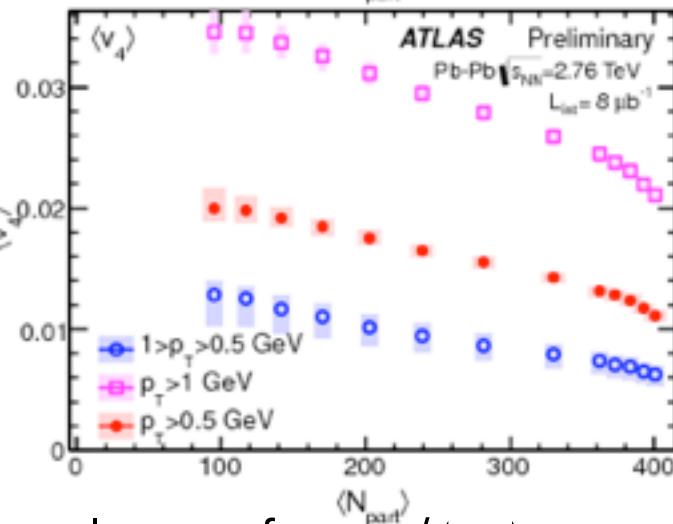
RMS value:  $\sqrt{\langle v_n^2 \rangle} \equiv \sqrt{(\langle v_n \rangle^2 + \sigma_{v_n}^2)}$

$n = 2$ 

$\sigma_{v2} / \langle v_2 \rangle$   
shows  
significant  
centrality  
dependence

 $n = 3$ 

$\sigma_{v3} / \langle v_3 \rangle$ ,  $\sigma_{v4} / \langle v_4 \rangle$   
are consistent  
with Gaussian  
fluctuations

 $n = 4$ 

The values of  $\sigma_{v_n} / \langle v_n \rangle$  :

found to be independent of  $p_T$ , suggesting that the hydrodynamic response to the eccentricity of the initial geometry has little  $p_T$  dependence,

found to reach a minimum of 0.34 for  $v_2$  around  $\langle N_{part} \rangle \sim 200$ .



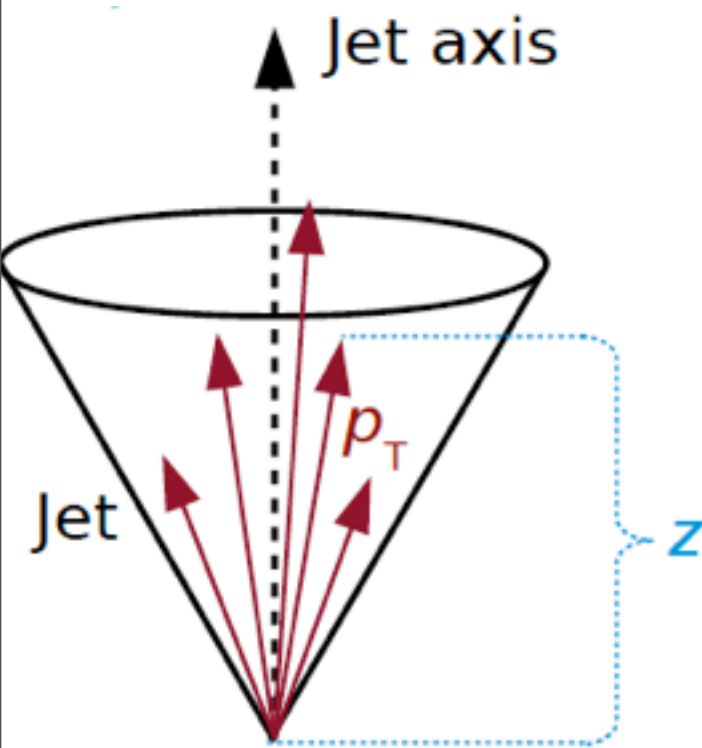
# Summary

- \* Jet yields suppressed by a factor of 2 in central collisions.
- \* Jet suppression depends on the jet size in central collisions.
- \* Jet fragmentation function shows no modification at high  $z$ , but significant suppression with centrality at  $z \approx 0.1$  and enhancement at very low  $z$  is observed.
- \* Jet quenching also studied with  $Z, \gamma$  - jet correlations.
- \*  $Z$  and  $\gamma$  production consistent with  $N_{\text{coll}}$  scaling.
- \* ATLAS measured significant flow harmonics of charged particles in Pb+Pb collisions at  $\sqrt{s_{\text{NN}}} = 2.76$  TeV.
- \* New results on flow harmonics fluctuations.
- \* Mixed reaction plane correlations were obtained.

Thank you!

# Additional Slides

# Jet fragmentation



Spectra of charged particles in jets  $\rightarrow D(p_T)(p_T^{\text{jet}}) = \frac{1}{N_{\text{jet}}} \frac{1}{\epsilon} \frac{dN}{dp_T}(p_T^{\text{jet}}) =$

$$\frac{1}{N_{\text{jet}}(p_T^{\text{jet}})} \frac{1}{\epsilon(p_T, \eta)} \left( \frac{\Delta N_{ch}(p_T, p_T^{\text{jet}})}{\Delta p_T} - \frac{\Delta N_{ch}^{UE}(p_T, p_T^{\text{jet}})}{\Delta p_T} \right)$$

Tracking efficiency corrected  $\uparrow$  Underlying event subtracted  $\uparrow$

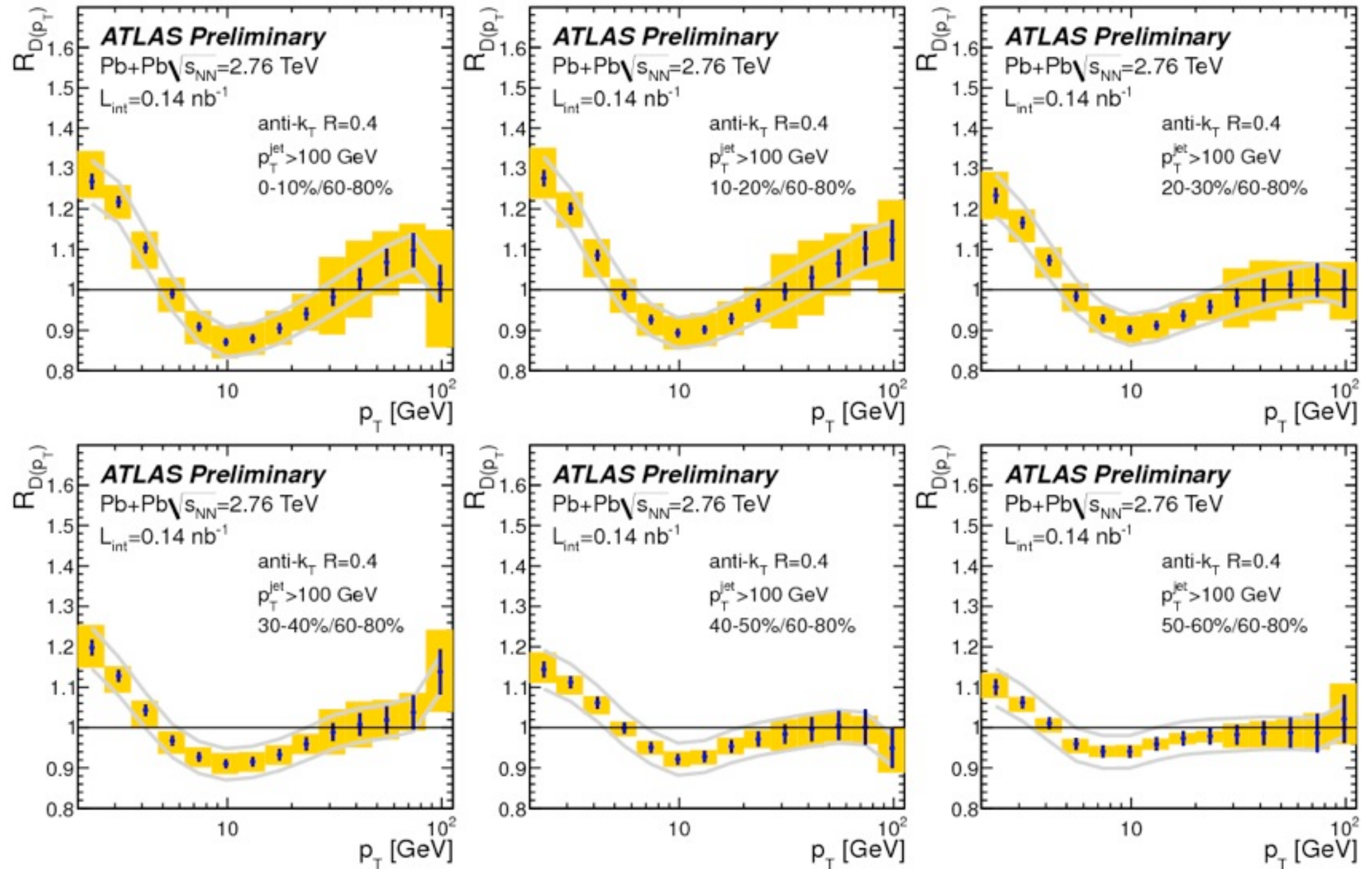
$$D(z)(p_T^{\text{jet}}) = \frac{1}{N_{\text{jet}}} \frac{1}{\epsilon} \frac{dN}{dz}(p_T^{\text{jet}}) =$$

$$\frac{1}{N_{\text{jet}}(p_T^{\text{jet}})} \frac{1}{\epsilon(p_T, \eta)} \left( \frac{\Delta N_{ch}(z, p_T^{\text{jet}})}{\Delta z} - \frac{\Delta N_{ch}^{UE}(z, p_T^{\text{jet}})}{\Delta z} \right)$$

$$z = p_T / p_T^{\text{jet}} \cos \Delta R$$

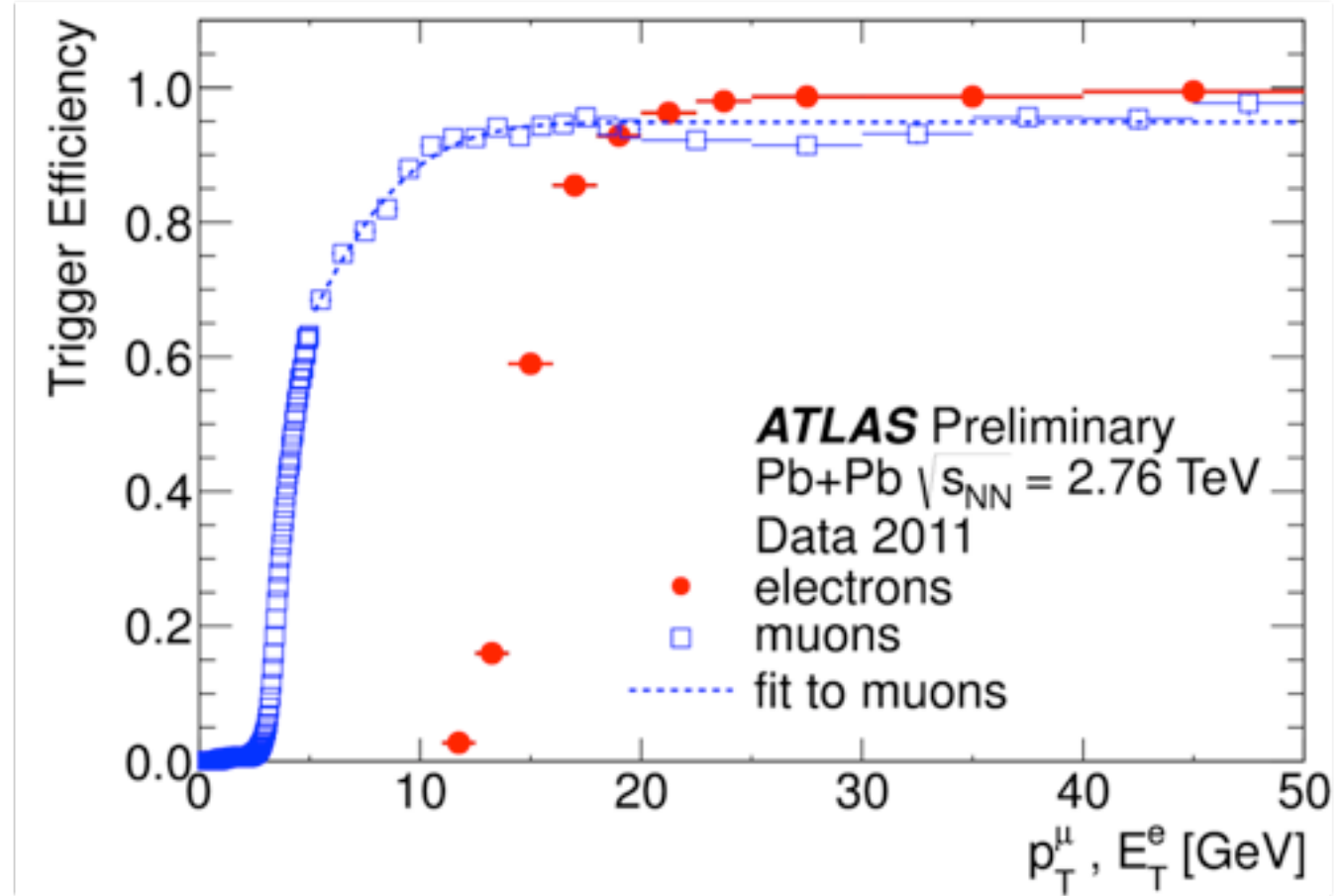
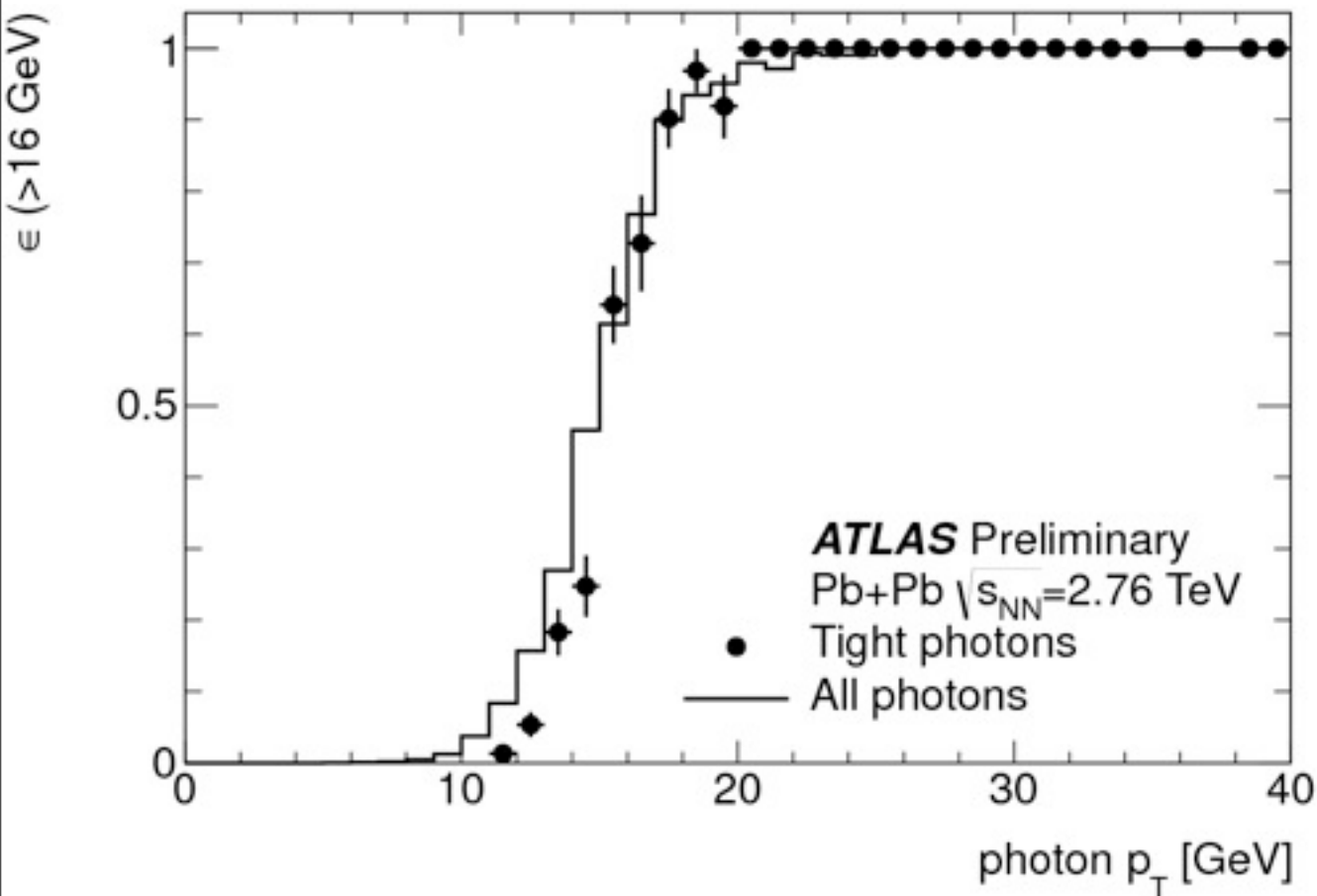
# D(p<sub>T</sub>) centrality dependence

Ratios are needed to study centrality dependence



Similar behaviour as for D(z) distribution.

# Event selection and triggers



## Photons and electrons

based on EM calorimeter

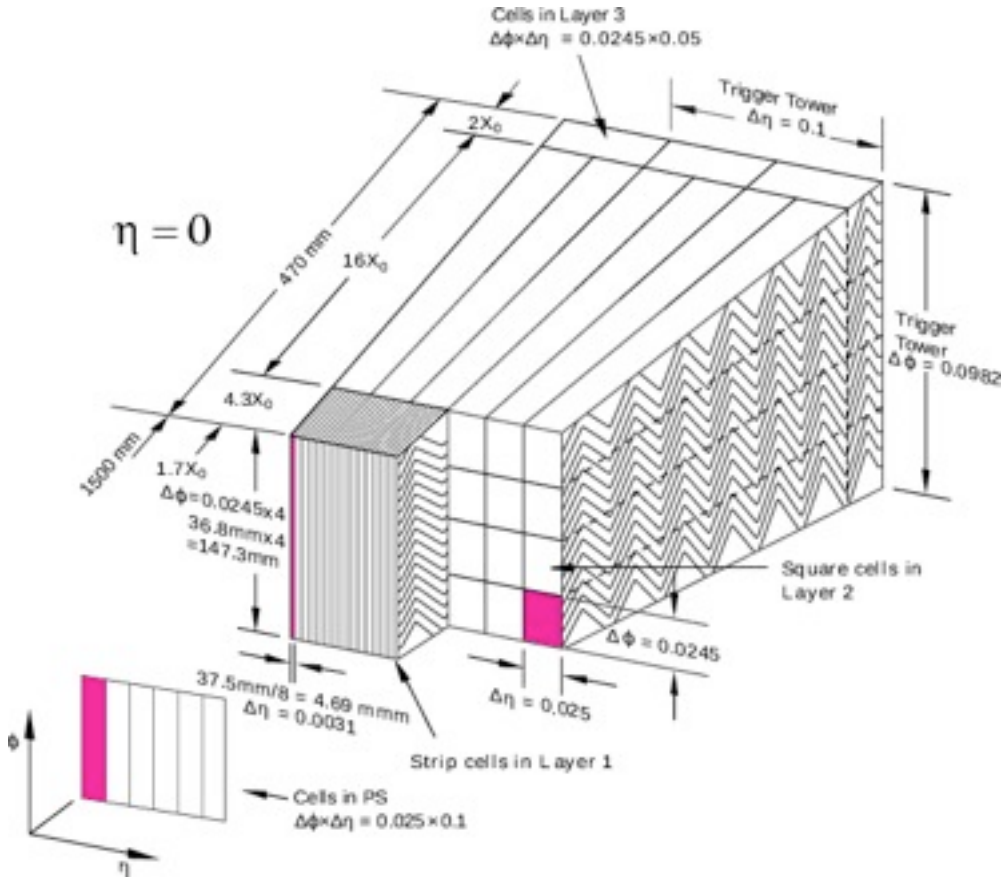
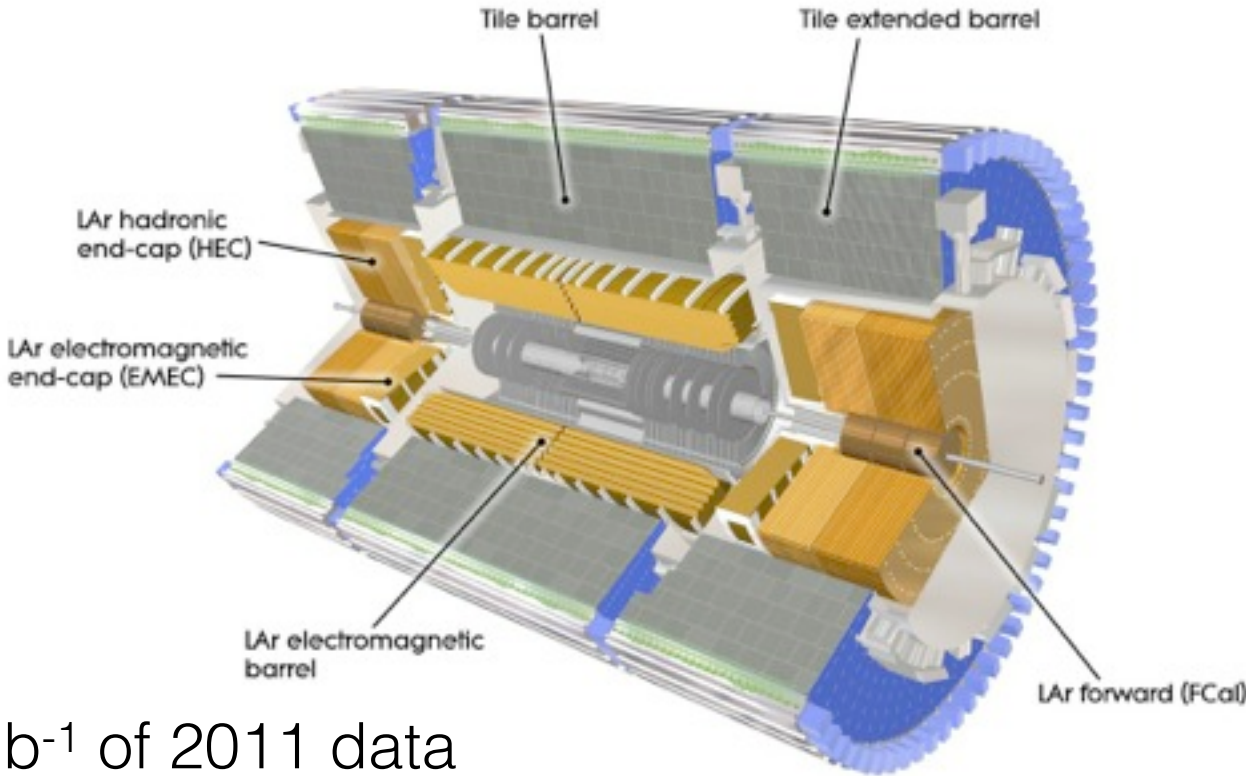
efficiency  $> 98\%$  for  $E_T > 20$  GeV

## Muons

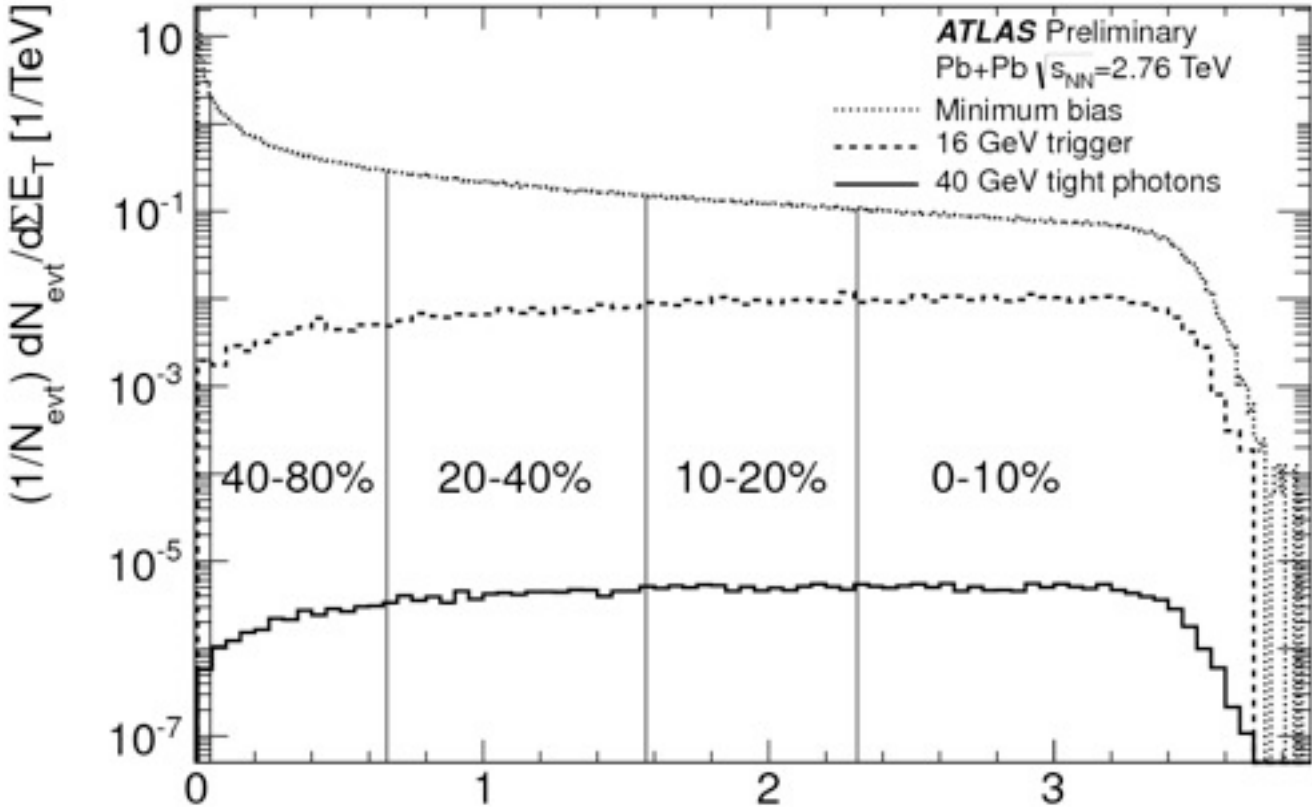
L1  $\mu$  trigger with  $p_T > 4$  GeV, HLT (MS OR MS + ID), additional  $p_T > 10$  GeV  $\mu$  scan

efficiency  $> 90\%$  above 10 GeV

# Direct Photon Reconstruction



0.13 nb<sup>-1</sup> of 2011 data  
Trigger: EM cluster with E<sub>T</sub> >16 GeV at L1  
100% efficient for photons with E<sub>T</sub> > 20 GeV  
Underlying-event background (UE) is subtracted event-by-event



Photon reconstruction with a sliding window algorithm seeded by clusters of at least 2.5 GeV in the second sampling layer.

Photon energy using all three layers and the presampler.

Photon conversions are not reconstructed in the HL environment.

Nine shower-shape variables used to choose high-quality photons (tight photons).

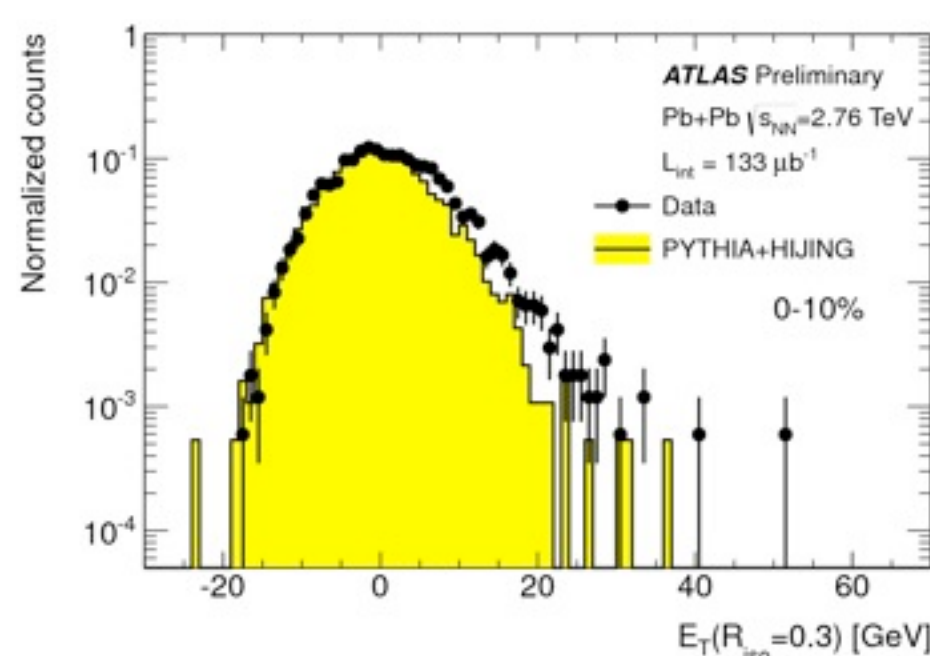
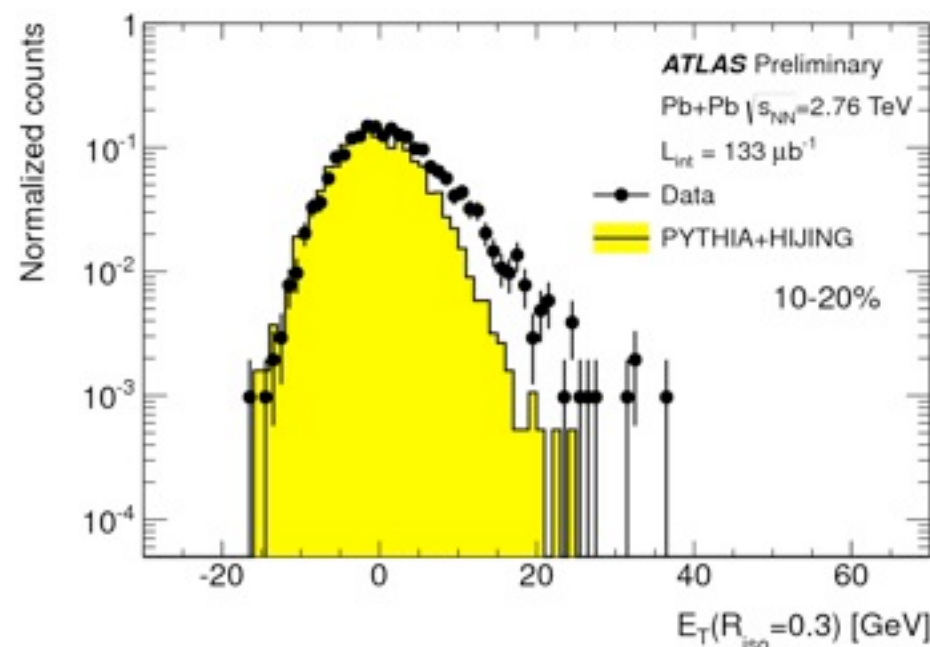
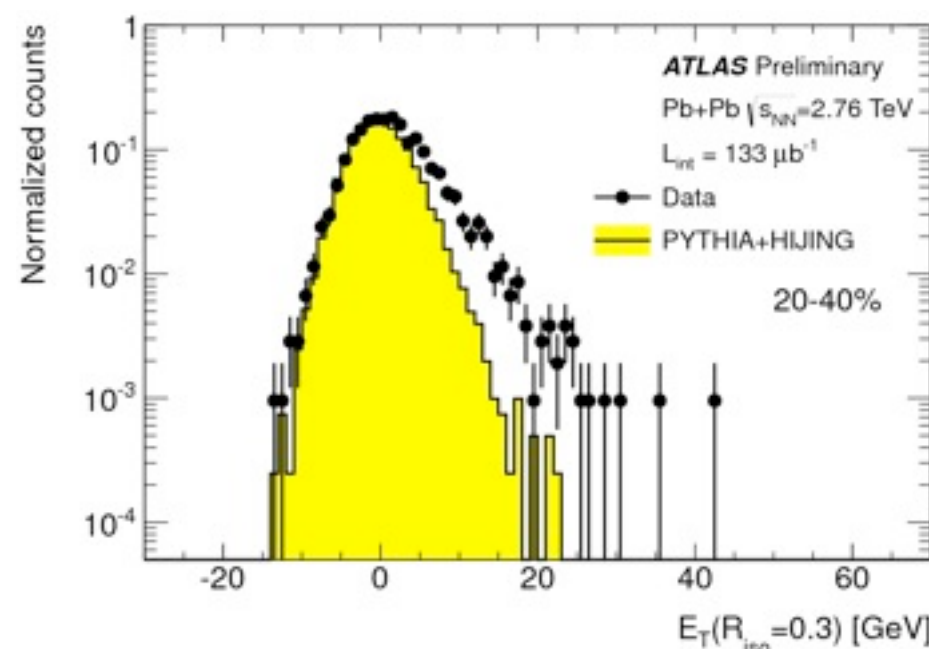
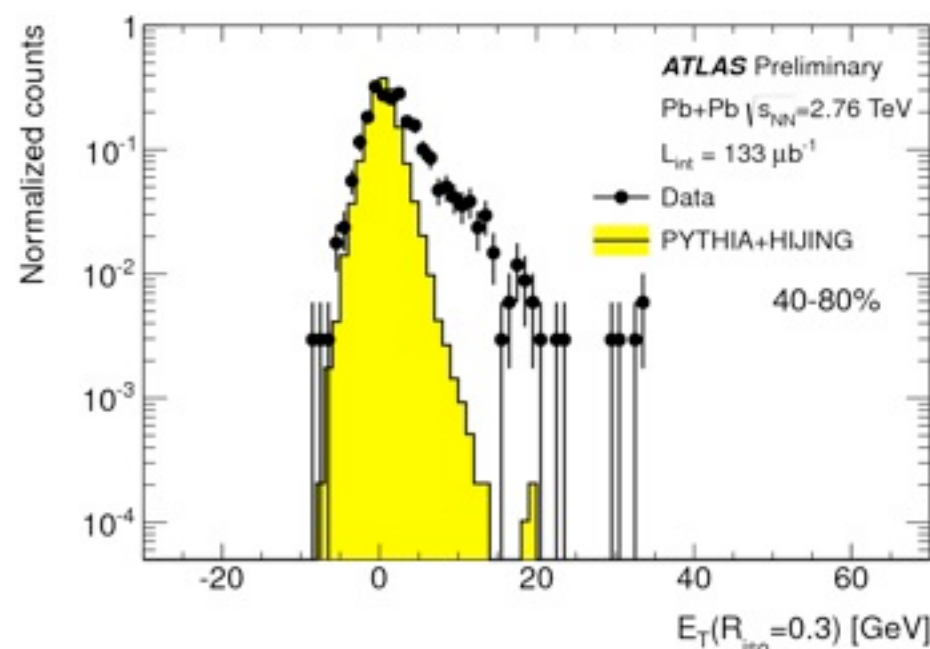
# Direct Photon Reconstruction

6435 tight photon candidates with  $p_T > 45$  GeV and  $|\eta| < 1.3$  before applying the isolation requirement  
 Isolation criterion optimized for HI photons:  $E_T(R_{iso}=0.3)$  – transverse energy in a cone of  $R_{iso}$  around the photon axis

Enhancement of data for  $E_T(R_{iso}=0.3) > 0$  due to two components: UE energy fluctuations and di-jet background

Width of  $E_T(R_{iso}=0.3)$  in 0-10% photon+jet events is 6 GeV

Isolation requirement:  $E_T(R_{iso}=0.3) < 6$  GeV



# Double side banded method

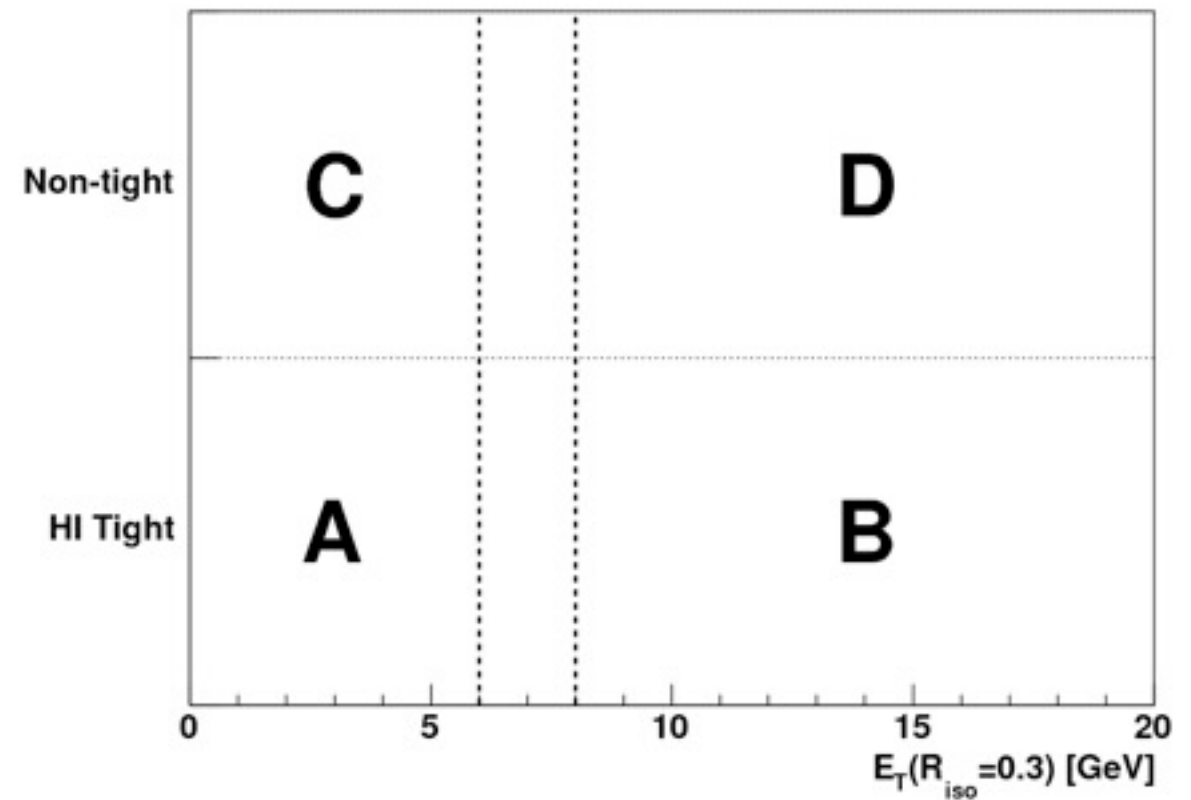
used for background subtraction. All photon candidates classified to one of four regions:

A: Primary signal region

B: Photons which happen to be in the vicinity of a jet or an UE fluctuation

C: Isolated jet fragments or photons which have shower shape fluctuations which fail the cuts

D: Primary background region



Leak of the signal to other regions is evaluated using MC

Leakage factors  $c_i = N_i^{sig} / N_A^{sig}$

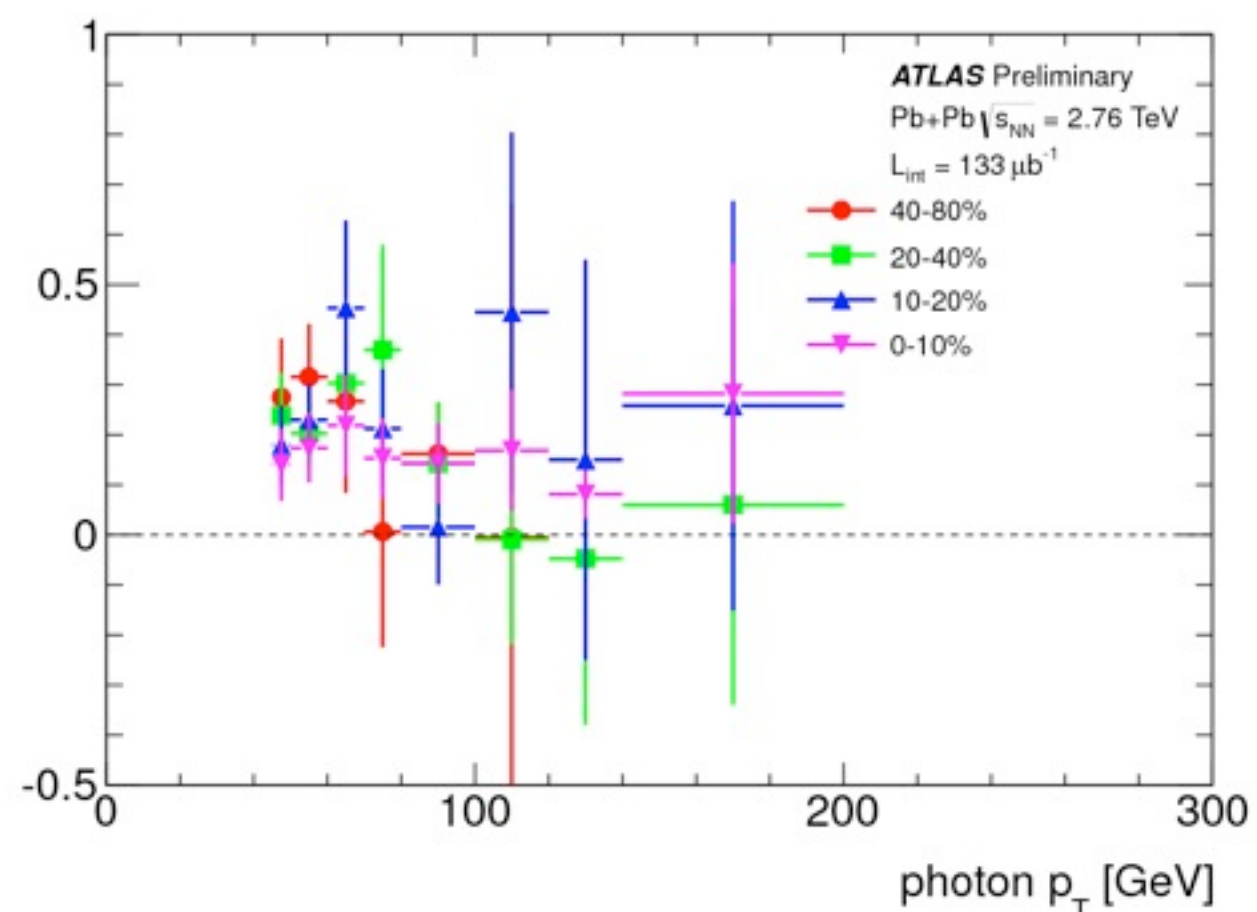
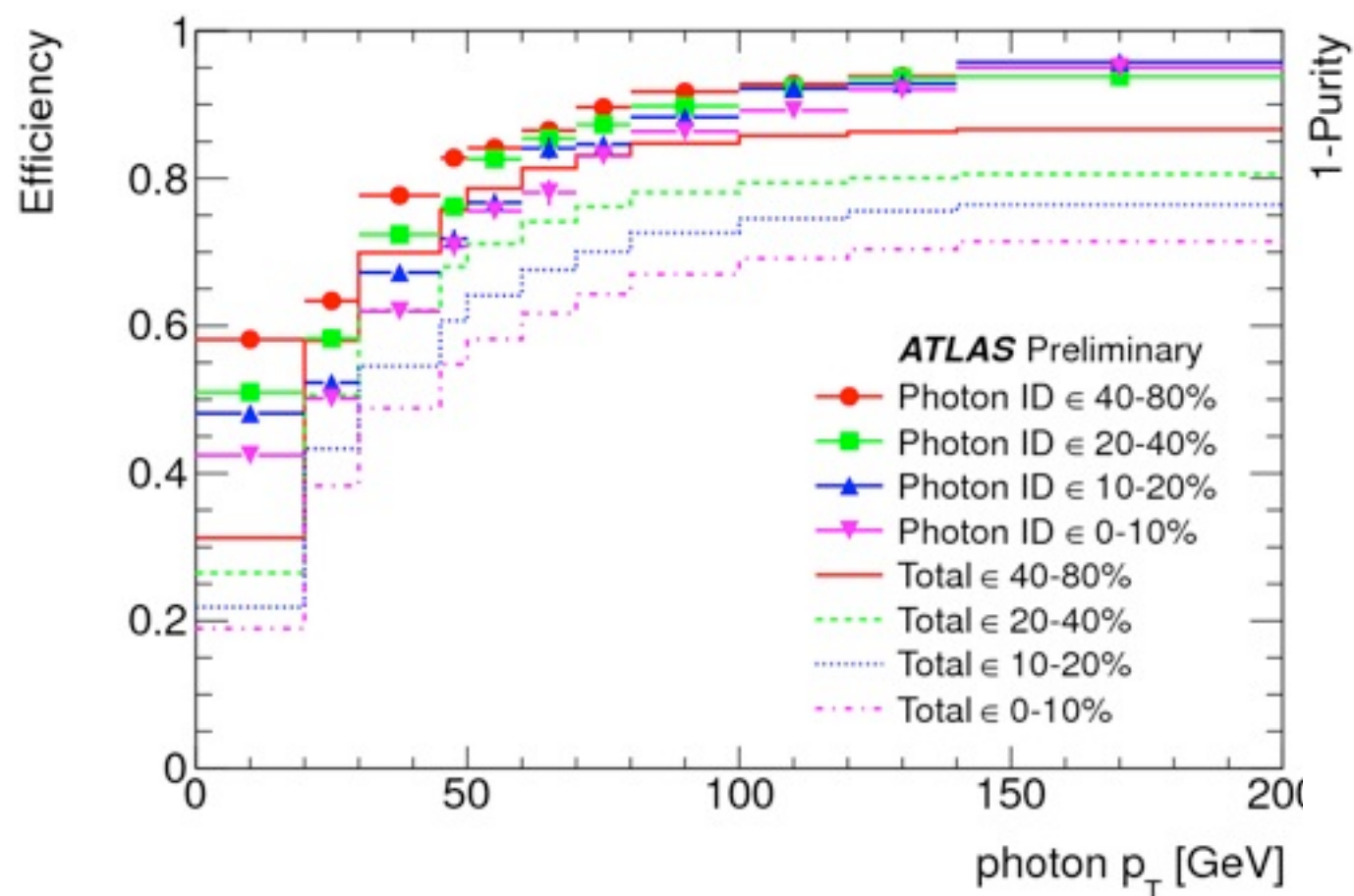
$c_i$  range from 0.005-0.06, no dependence on centrality

$$N_A^{sig} = N_A^{obs} - (N_B^{obs} - c_B N_A^{sig}) \frac{(N_C^{obs} - c_C N_A^{sig})}{(N_D^{obs} - c_D N_A^{sig})}$$

# Photon purity and efficiency

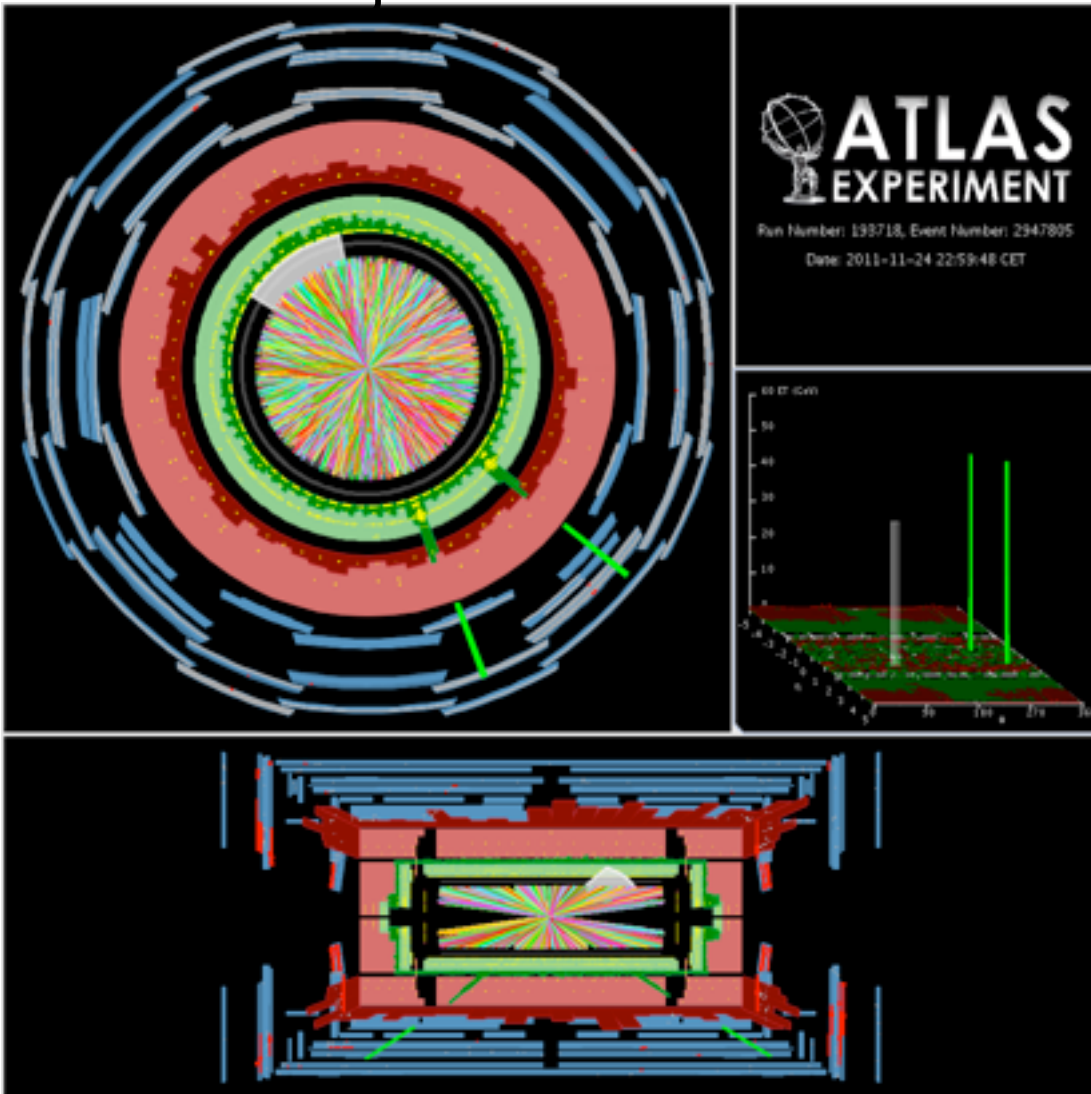
Efficiencies extracted from MC and normalized to all PYTHIA isolated photons with  $E_T(R_{\text{iso}}=0.3) < 6\text{GeV}$  (the isolation removes 1.5% photons)

Purity is determined by double side band method: fraction of di-jet background in photon sample: 20-30% in low  $p_T$  bins

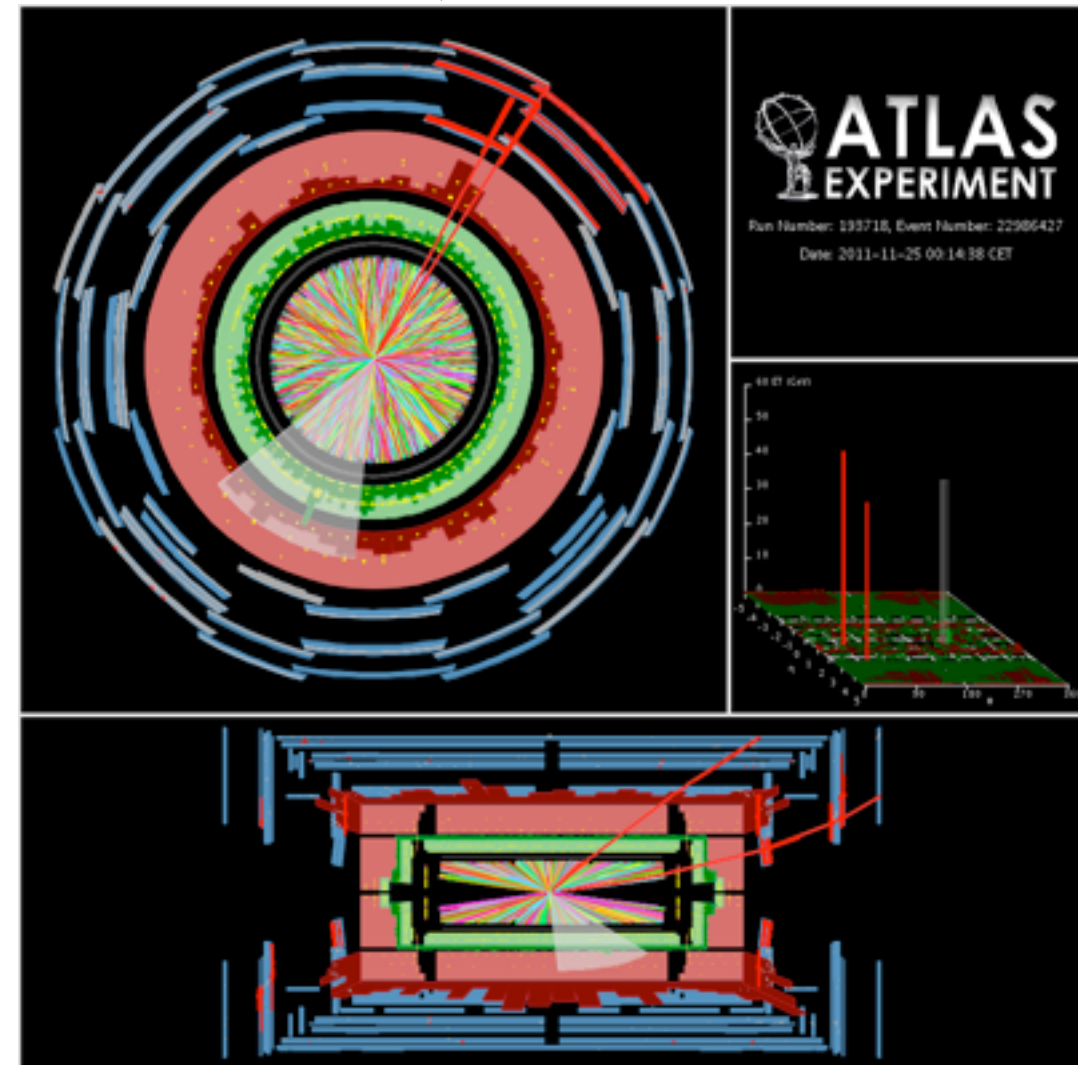


# Z - jet correlations

$Z \rightarrow e^+e^- + \text{jet}$  event candidate

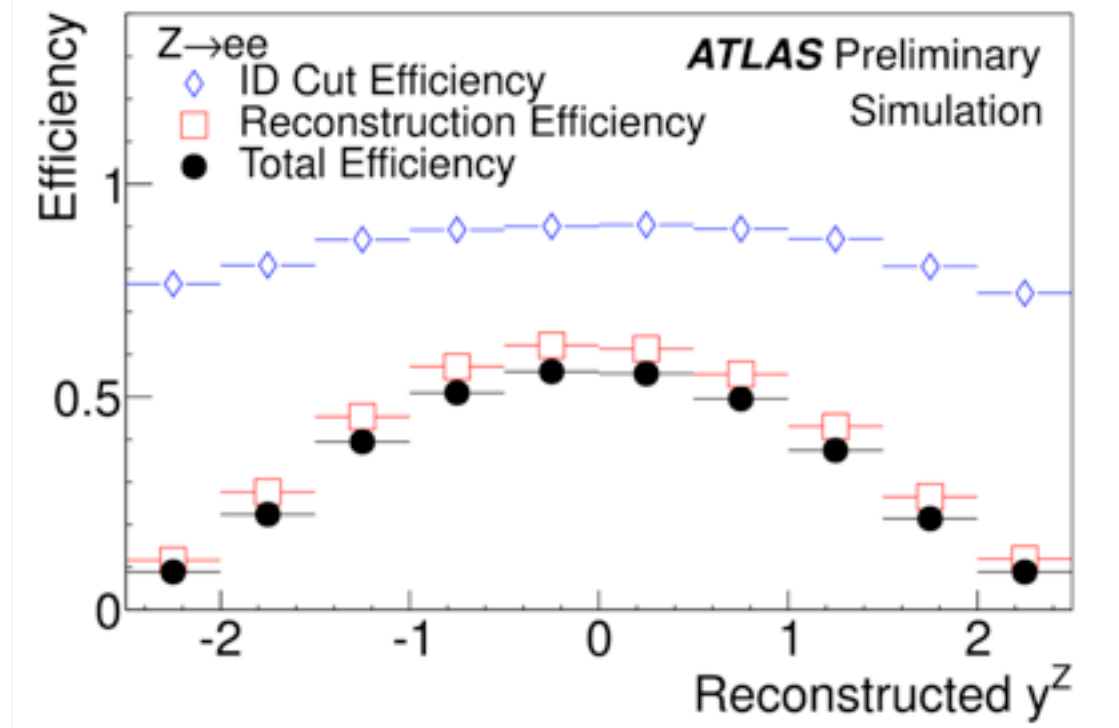
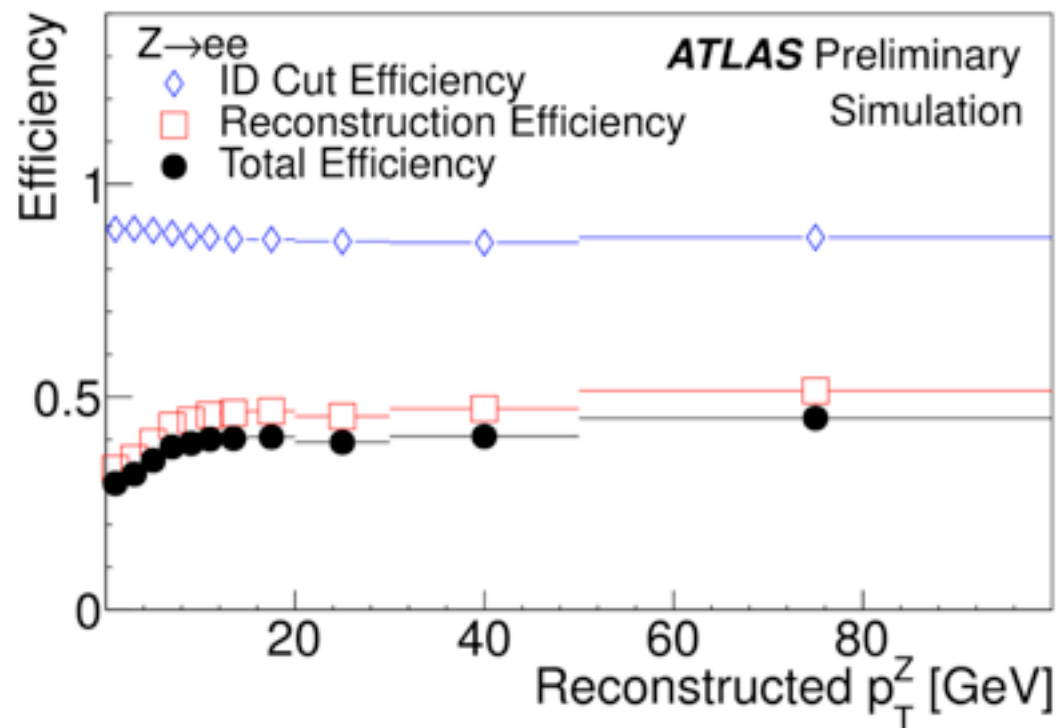


$Z \rightarrow \mu^+\mu^- + \text{jet}$  event candidate

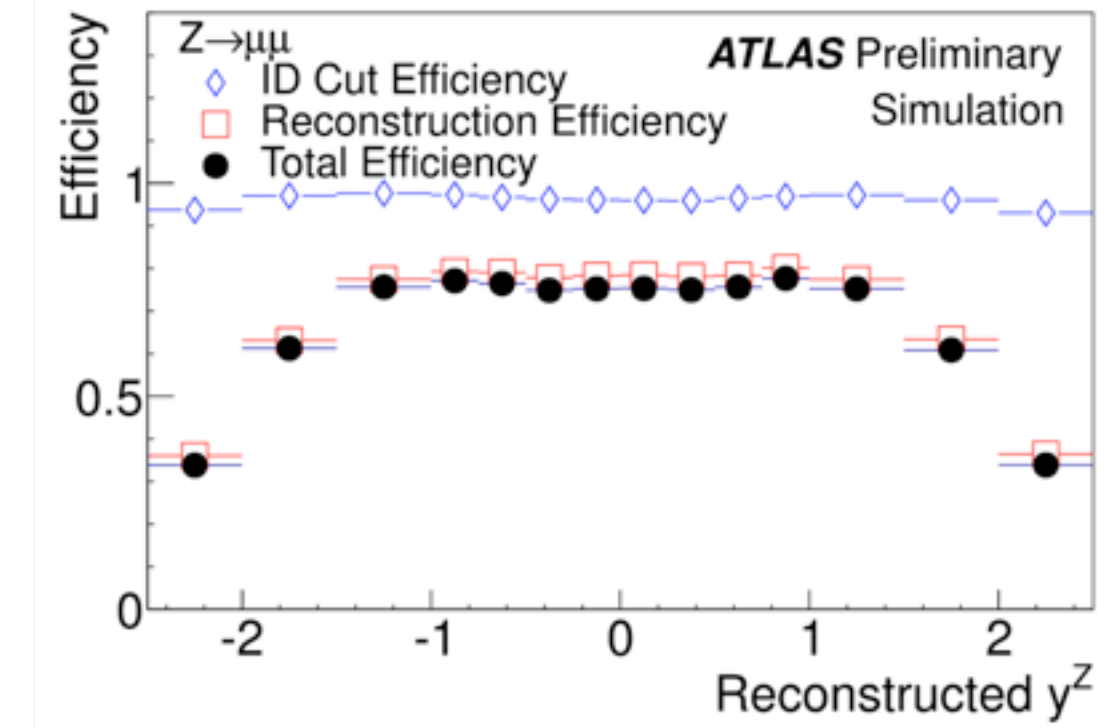
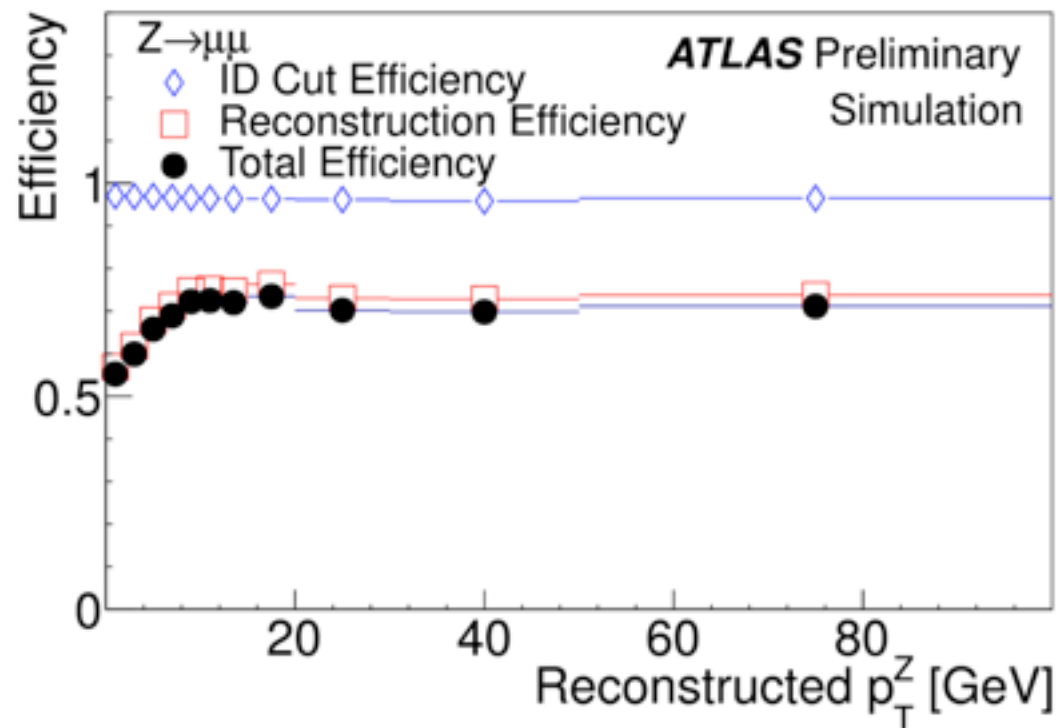


# Z boson efficiencies

electrons

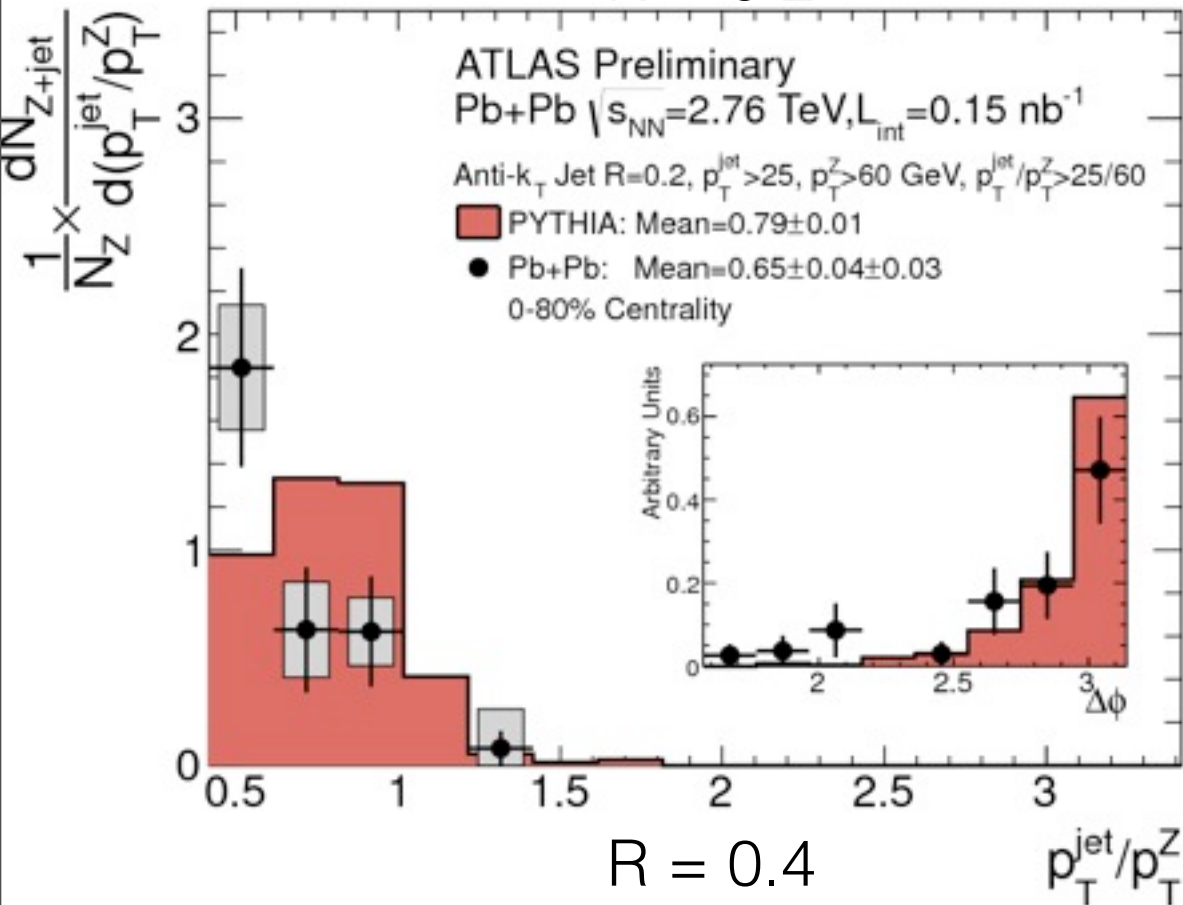


muons

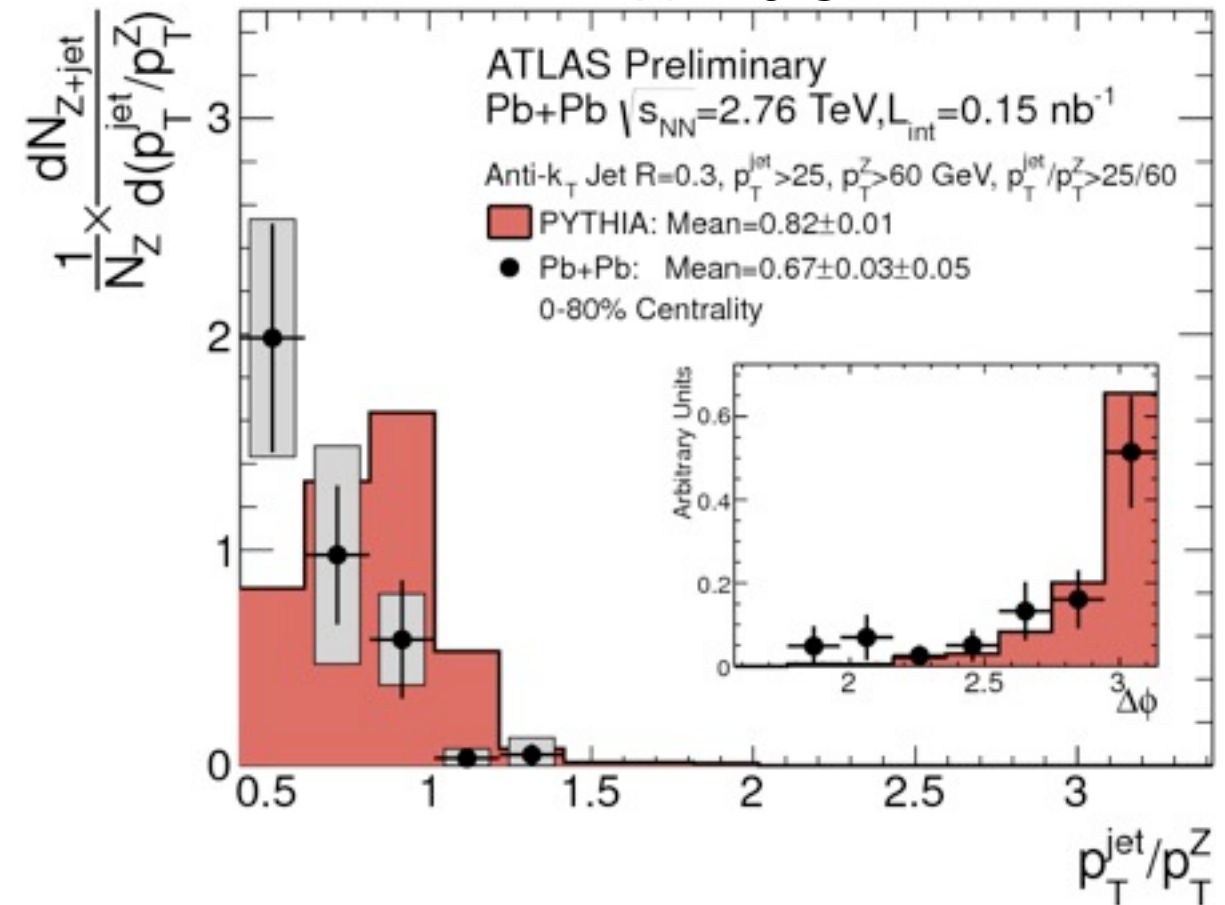


# Z - jet correlations 0-80% centrality

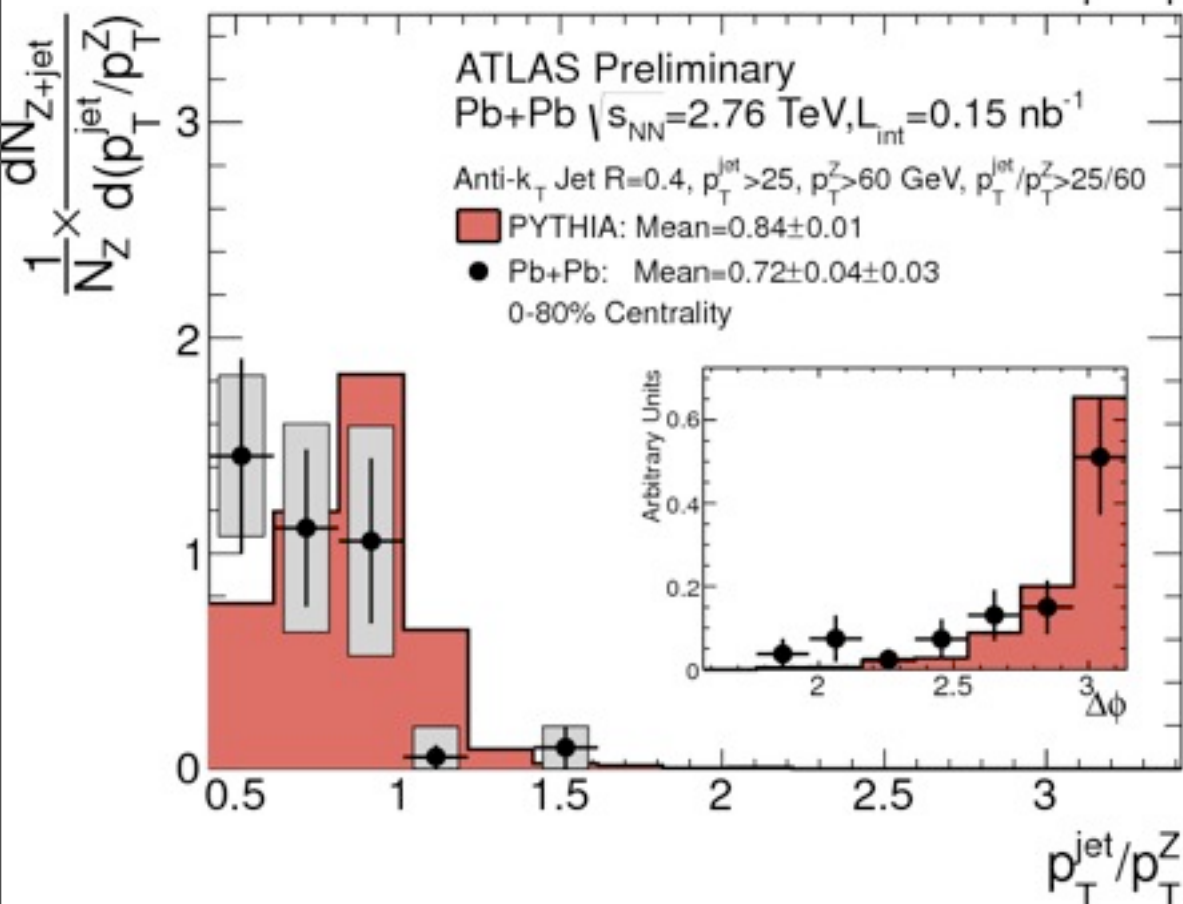
$R = 0.2$



$R = 0.3$



$R = 0.4$



Ratio of jet and Z boson transverse momenta.

Normalized per Z boson.

Inset  $\Delta\phi$  distribution, normalized to unity

Low statistics but data distributions in the momentum ratio are

different from PYTHIA null hypothesis

# Z production – e, $\mu$ selection and efficiencies

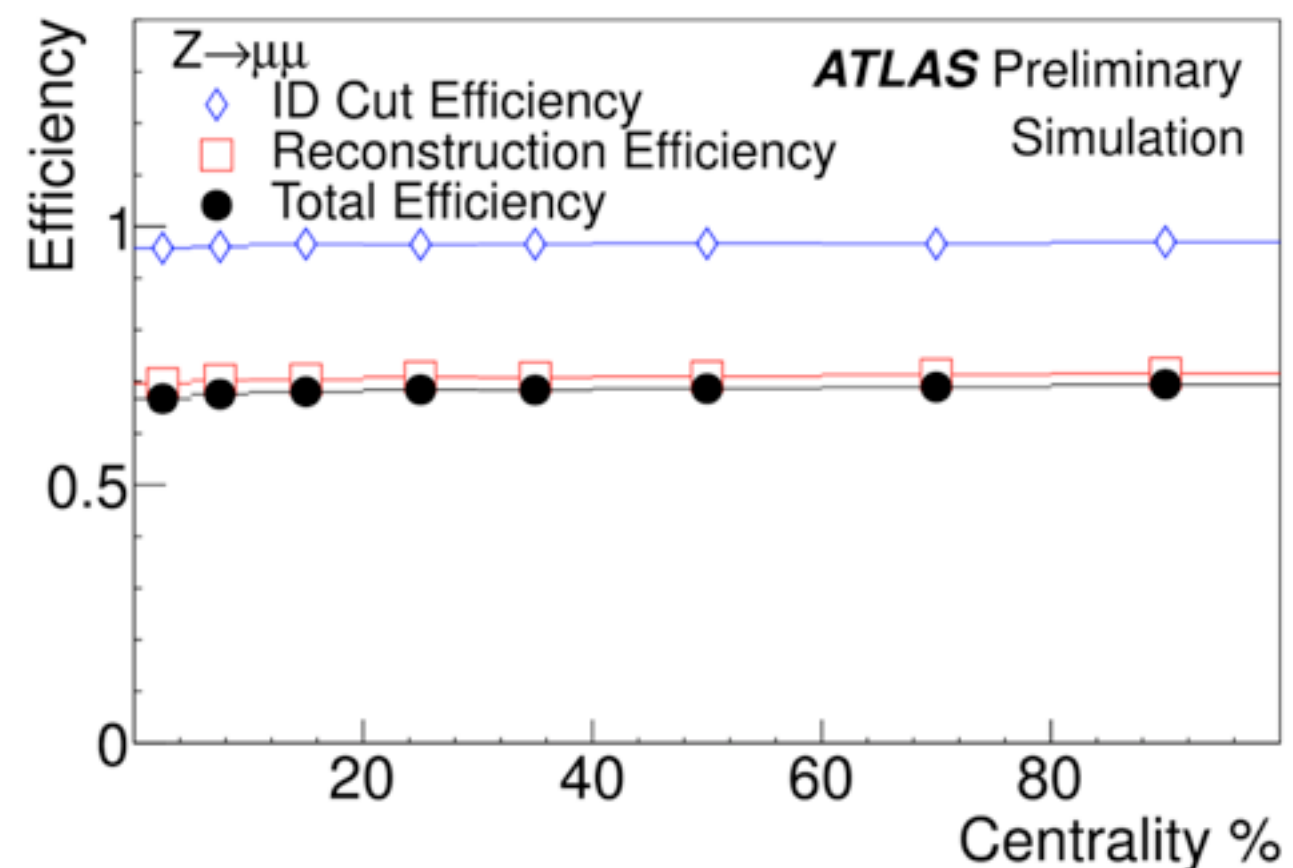
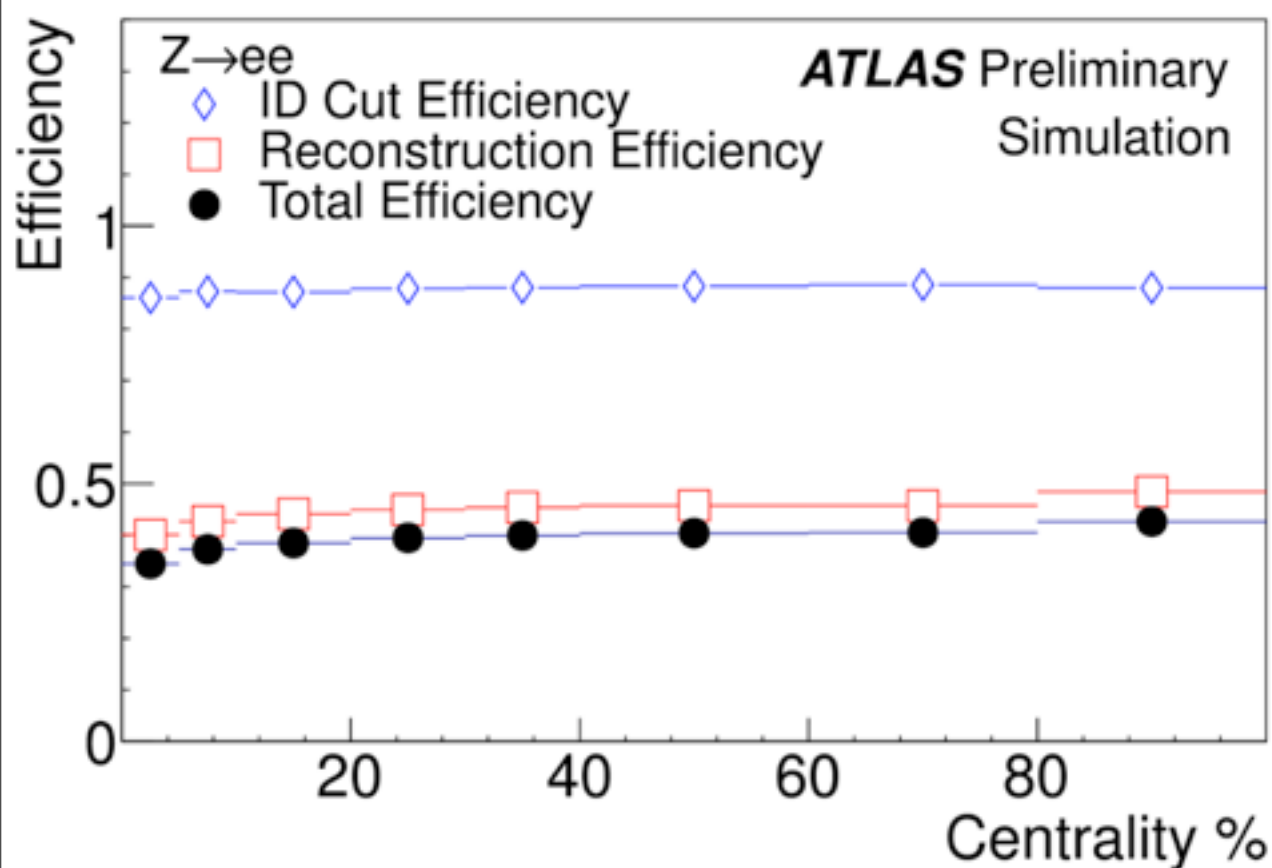
electrons:

identified at L1 as a cluster of cells in the electromagnetic calorimeter, formed into  $(\Delta\phi \times \Delta\eta) = 0.1 \times 0.1$  trigger towers;  
 $|\eta| < 2.5$ , excluding the transition region between calorimeter sections ( $1.37 < |\eta| < 1.52$ )  
 $E_T > 14$  GeV.

muons:

selected using all three trigger levels;  
combination of MS and/or ID:  
“high quality” MS & ID, combined:  $p_T > 10$  GeV required for both,  
“low quality”,  $p_T > 20$  GeV required for both

weak centrality dependence:



# Photon- jet correlations

## Jet quenching physics:

opening angle between leading jet and photon,  $\Delta\phi$ ;  
 transverse momentum ratio,  $x_{j\gamma} = p_T^{\text{jet}}/p_T^\gamma$ ;  
 $R_{j\gamma} = (1/N_\gamma) dN_{j\gamma}/dx_{j\gamma}$ , fraction of photon events that  
 have a jet.

## Correlation between the photon and the leading jet with:

$p_T^{\text{jet}} > 25 \text{ GeV}$ ,  $|\eta^{\text{jet}}| < 2.1$ ;  
 $60 < p_T^\gamma < 90 \text{ GeV}$ ,  $|\eta^\gamma| < 1.3$ ;  
 (For  $x_{j\gamma}$  and  $R_{j\gamma}$ )  $\Delta\phi > 7/8\pi$ , and  $x_{j\gamma} > 25/60$ .

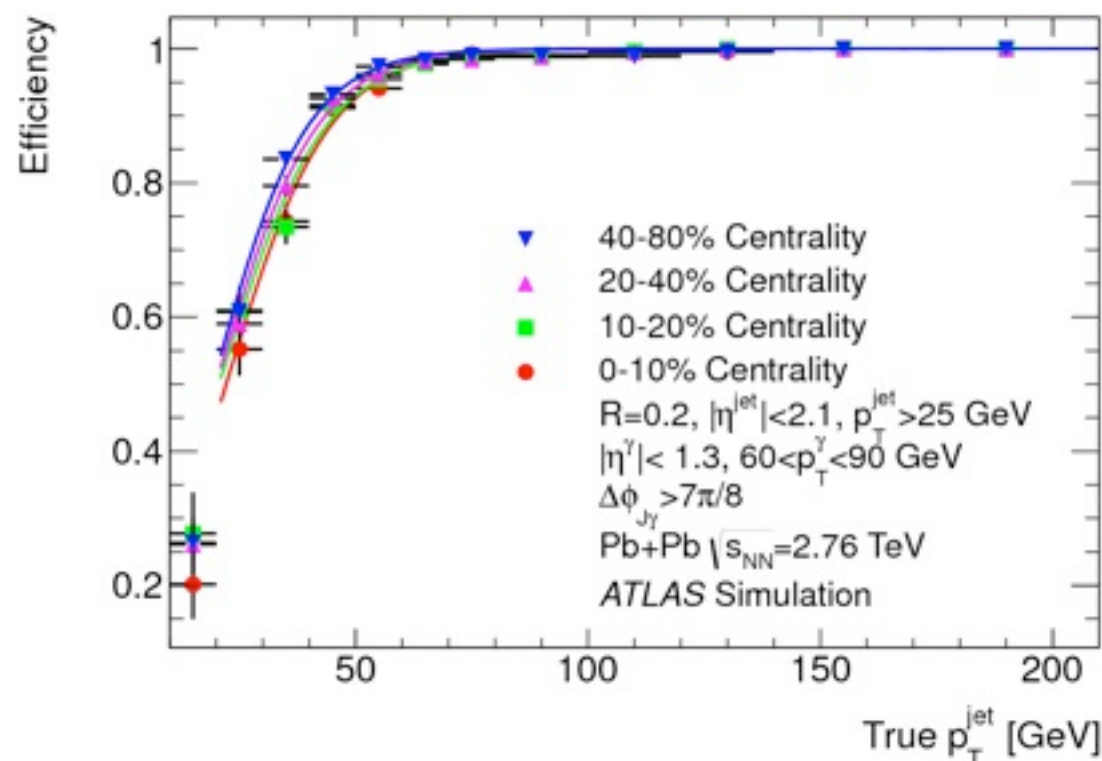
## Background subtraction

“double sideband” method to find the background.

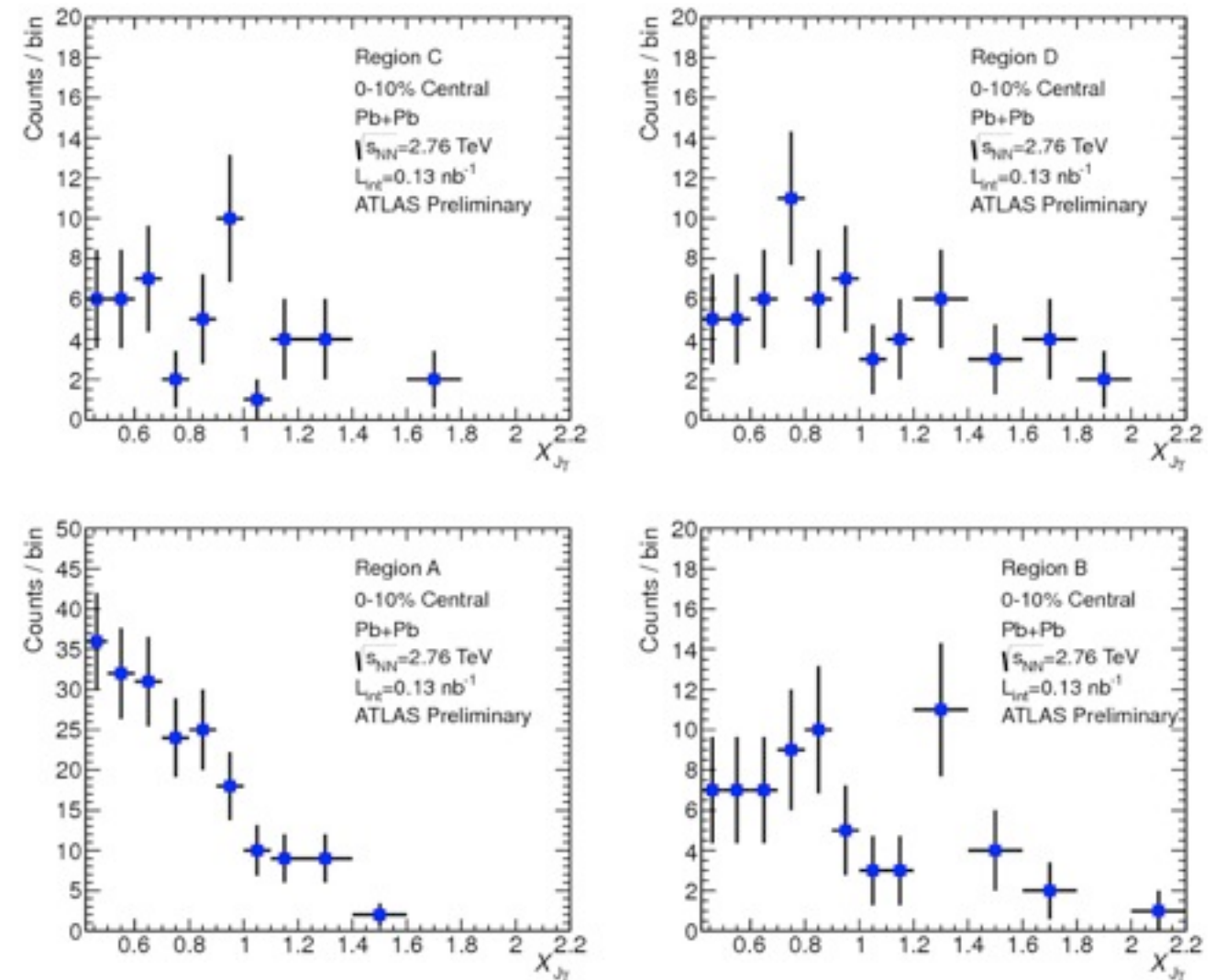
## Unfold jet spectrum

unfolding matrix for inclusive jets (SVD) from PYTHIA  
 embedded into data;  
 apply to single events;  
 $p_T^{\text{jet}}$  mapped to different values with different weights;  
 fill  $x_{j\gamma}$  distribution.

## Photon efficiency

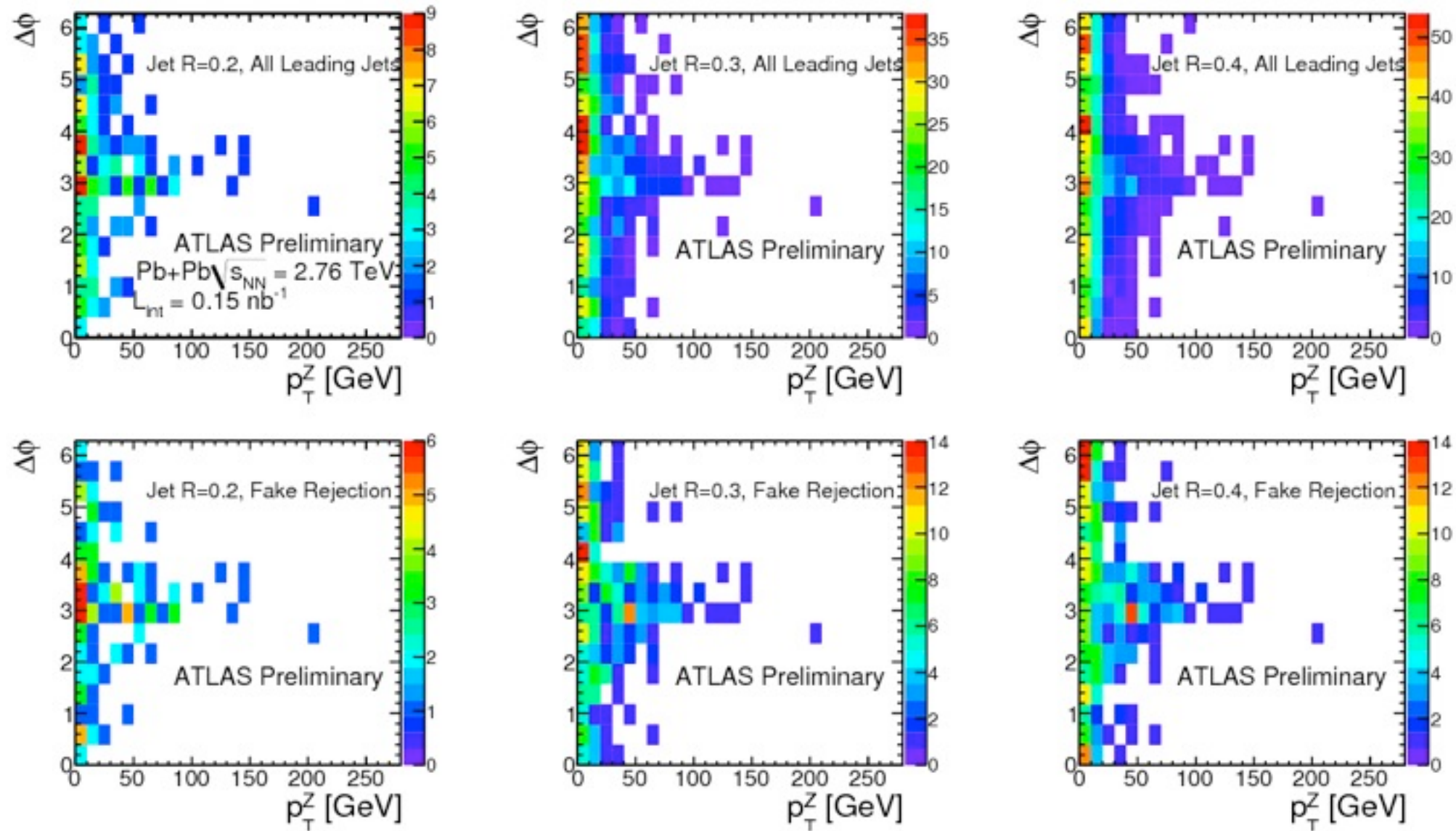


## Raw $x_{j\gamma}$ distributions



Jet reconstruction efficiency in photon-jet events.

# Z - jet correlations



Jets reconstructed using standard iterative background subtraction.

Above 50-60 GeV jet and Z are emitted back to back.

Fake rejection (based on track jet or EM cluster within jet), removes uncorrelated jets (esp. in  $R=0.3$ ).

Similar to photon – jet analysis

Lower statistics  
Higher purity

Correlation between Z boson and leading jet with:

$p_T^{\text{jet}} > 25$  GeV,  $|\eta^{\text{jet}}| < 2.1$

$p_T^Z > 60$  GeV

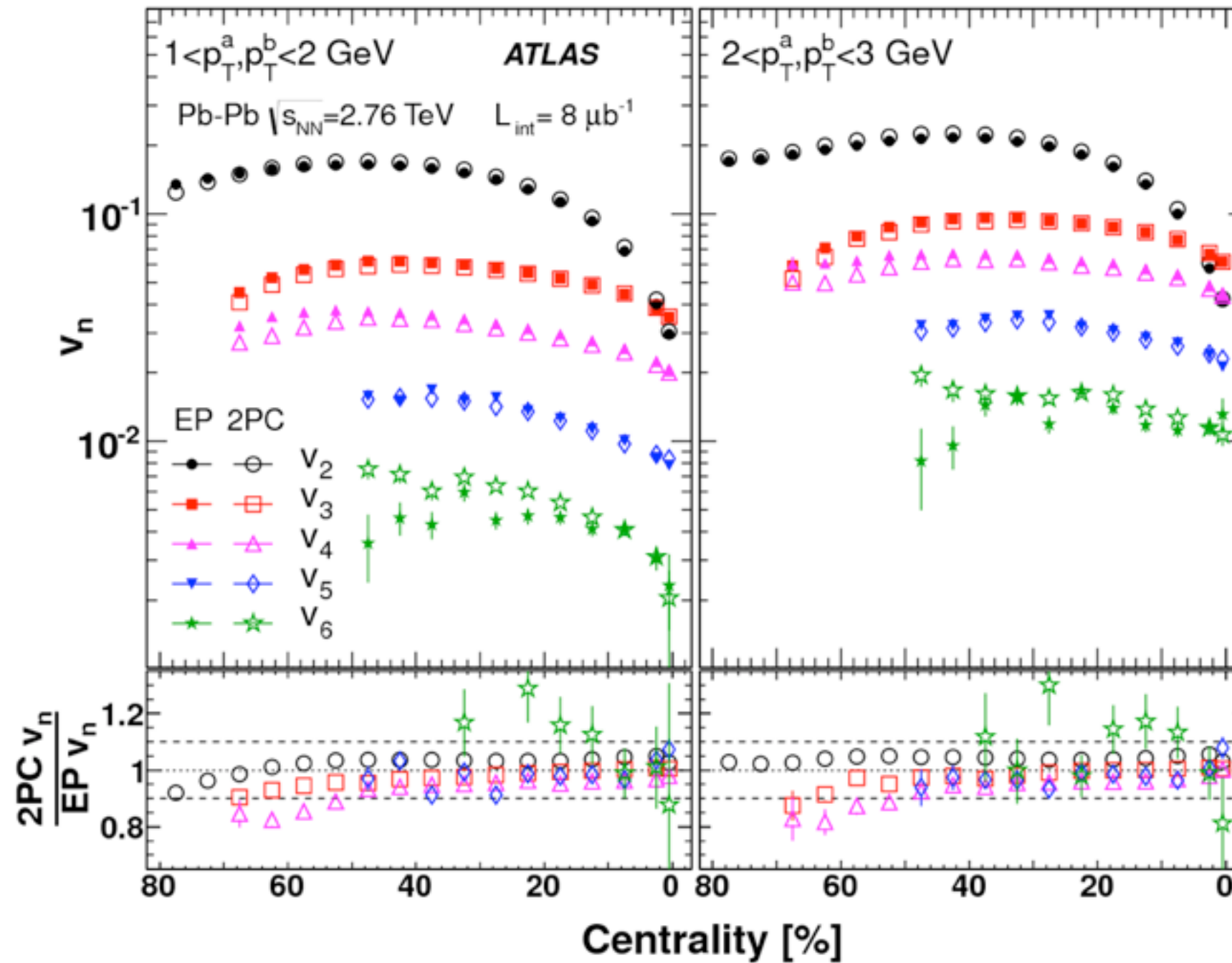
$\Delta\phi > 1/2\pi$ , and  $x_{jZ} > 25/60$

# The result: 2PC compared to EP

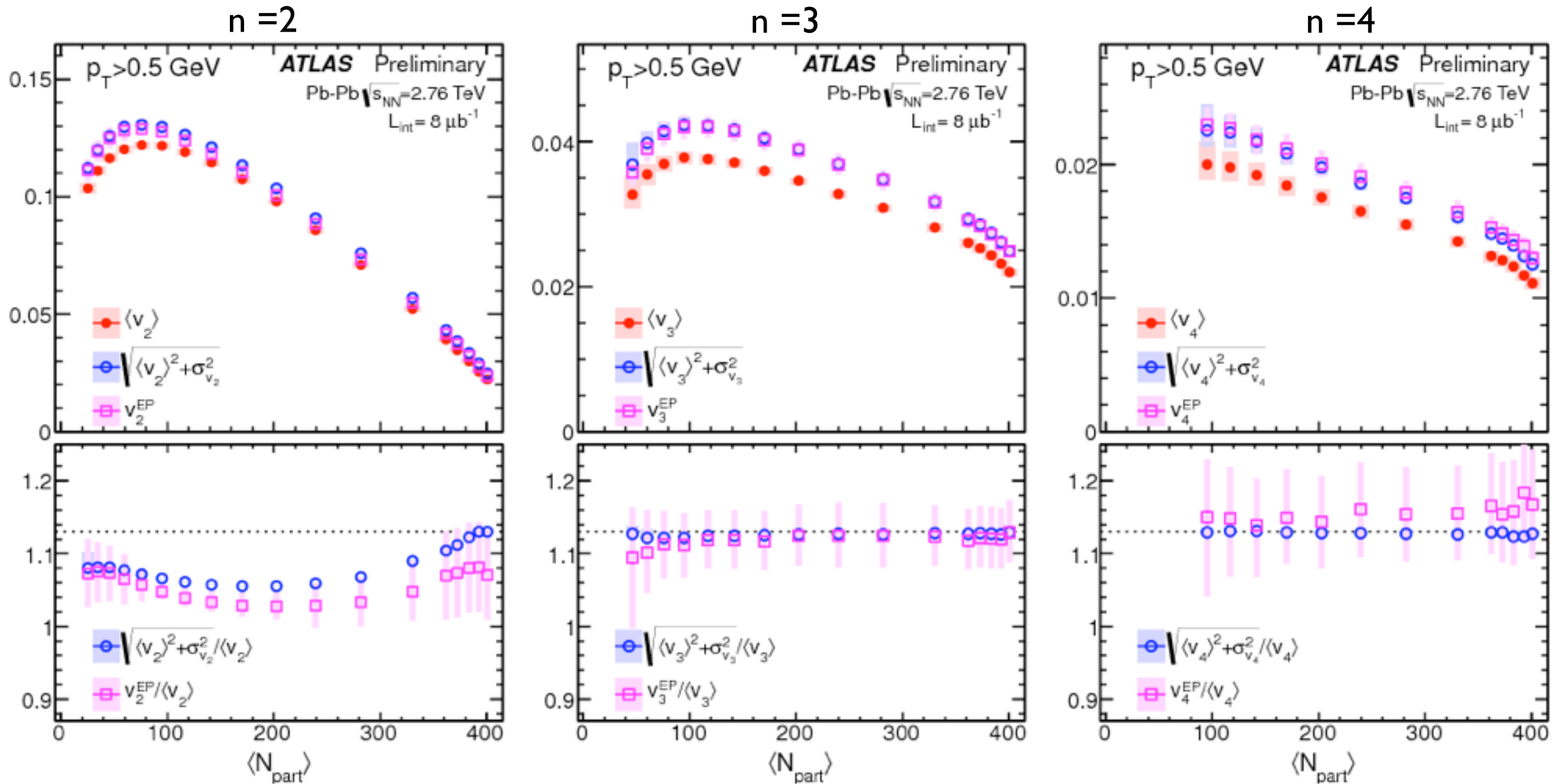
PHYSICAL REVIEW C 86, 014907 (2012)



Measurement of the azimuthal anisotropy for charged particle production in  $\sqrt{s_{NN}} = 2.76$  TeV lead-lead collisions with the ATLAS detector



EP method in general is known to measure a  $v_n$  value between the simple average and the RMS of the true  $v_n$ :  $\langle v_n \rangle \leq v_n^{\text{EP}} \leq \sqrt{\langle v_n^2 \rangle}$  *Phys.Rev.C77,014906(2008)*.



for  $v_3$  and  $v_4$  the values of  $v_n^{\text{EP}}$  are almost identical to  $\text{RMS } \sqrt{\langle v_n^2 \rangle}$  ;

for  $v_2$  the values of  $v_n^{\text{EP}}$  are in between  $\langle v_n \rangle$  and  $\sqrt{\langle v_n^2 \rangle}$  : they are closer to  $\langle v_n \rangle$  in mid-central collisions where the EP resolution factor is close to one, and approach  $\sqrt{\langle v_n^2 \rangle}$  in peripheral collisions where the resolution factor is small.