

# Constraining sterile neutrinos with AMANDA and IceCube atmospheric neutrino data

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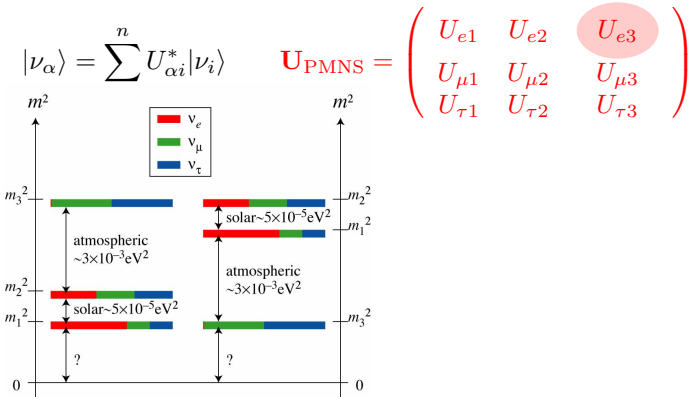
In collaboration with F. Halzen and Arman Esmaili-  
10-14 December 2012-IX Latin American Symposium on  
High Energy Physics



# Standard scenario for neutrino oscillations

- Most (all data) can be understood if we assume that Neutrino flavor states are linear combination of mass eigenstates. a Mixing matrix, named Pontecorvo, Maki-Nakagawa-Sakata (PMNS).

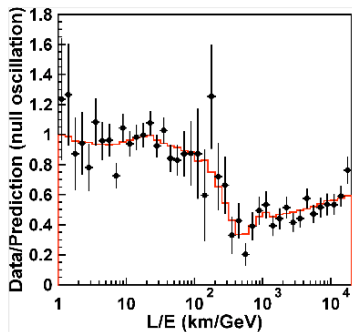
For 3 flavor neutrinos we have a  $3 \times 3$  matrix,



# Standard scenario for neutrino oscillations

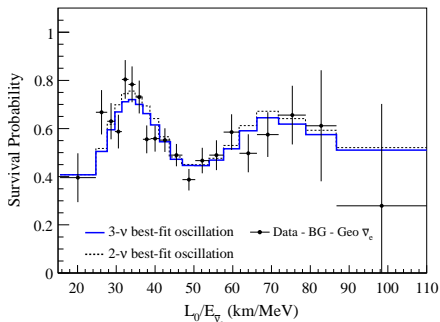
- In different experiments, it was proved that neutrinos oscillate,

$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2(2\theta) \sin^2\left(1.27 \frac{\Delta m^2}{(\text{eV})^2} \frac{L/\text{Km}}{E/\text{GeV}}\right)$$



(a) SK  $\nu_\mu$  data

$$\Delta M^2 = 2.5 \cdot 10^{-3} \text{eV}^2$$



(b) KamLand  $\bar{\nu}_e$  data

$$\Delta m^2 = 7.5 \cdot 10^{-5} \text{eV}^2$$



# Sterile neutrino phenomenology

- Recently, there are a few anomalies that did not fit in the standard view of three light neutrinos:
  - LSND anomaly and related <sup>1</sup>
  - The reactor neutrino anomaly <sup>2</sup>
  - The Gallium anomaly
  - The Dark radiation
  - The absence of up-turn in solar neutrino data

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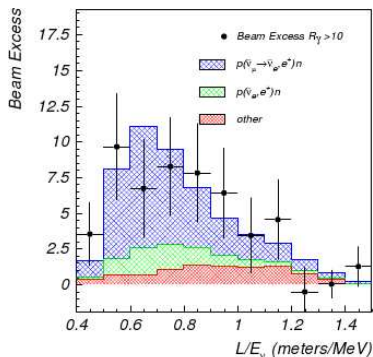
<sup>1</sup>See talk by Aguilar-Arevalo (Th4)

<sup>2</sup>See the talk by Thierry Lasserre at this conference

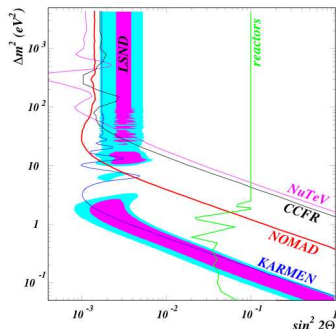


# Sterile neutrino phenomenology

- LSND experiment (2001)<sup>1</sup>:  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  L  $\sim$  30m  $E_\nu \sim$  20 – 200 MeV



(c)



(d)

$$\Delta m_{LSND}^2 \sim 1 \text{ eV}^2 \gtrsim \Delta m_{21}^2, \Delta m_{31}^2$$

$$\Delta m_{21}^2 = 2.5 \times 10^{-3} \text{ eV}^2, \Delta m_{31}^2 = 7 \times 10^{-5} \text{ eV}^2$$

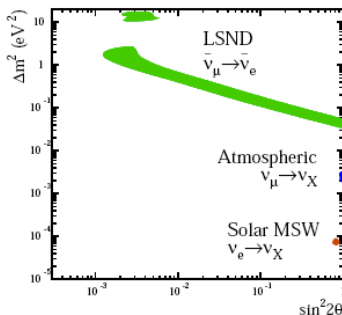
<sup>1</sup>LSND, PRD 64 (2001) 112007, hep-ex/0104049

# Sterile neutrino phenomenology

- to explain LSND experiment require:  $\frac{L}{E_\nu} \sim \frac{1m}{MeV} \sim \frac{1Km}{GeV}$   
that it is not compatible with the results from other  
oscillation experiment :  $\frac{L}{E_\nu} > \sim \frac{10^3 Km}{GeV}$ .

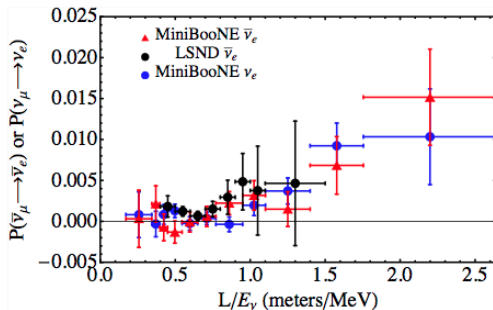
$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2(2\theta) \sin^2 \left( 1.27 \frac{\Delta m^2}{(eV)^2} \frac{L/Km}{E/GeV} \right)$$

A possible explanation is to have  $\Delta m_{LSND}^2 \sim 1eV^2$



# Sterile neutrino phenomenology

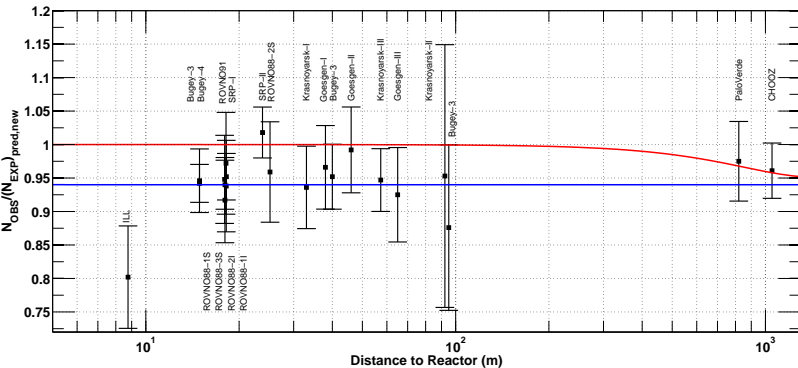
- A new generation experiment MINI-BOONE <sup>1</sup> was designed to test the LSND result. If we compare the probabilities of three experiments: LSND, Mini-Boone neutrino and Mini-Boone anti-neutrino (the three have the same  $L/E_\nu$ , but different  $L$  and different  $E_\nu$ .)



<sup>1</sup>See talk by Aguilar-Arevalo (Th4)

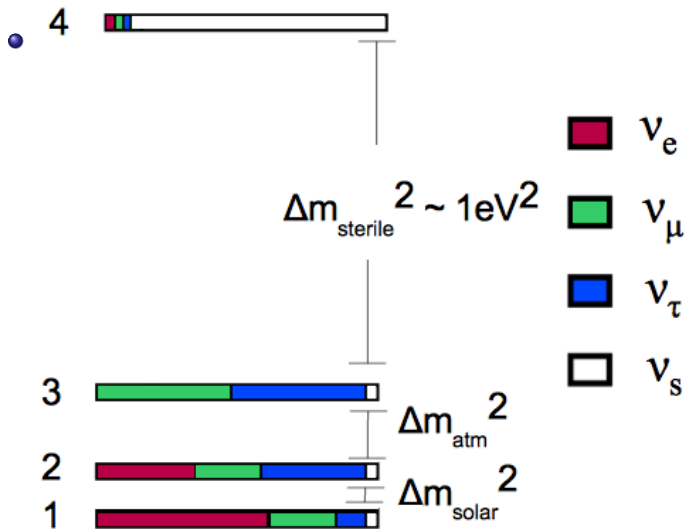
# Sterile neutrino phenomenology

- Reactor  $\bar{\nu}_e$  anomaly:  
Recent reevaluation of expected reactor  $\bar{\nu}_e$  flux is 3.5% higher than previous prediction: Mueller et al. arXiv:1101.2663, confirmed by P. Huber arXiv:1106.0687.
- Reactor anomaly: With new fluxes there is a deficit of  $\bar{\nu}_e$





# Framework: 3+1 model



- The mixing matrix for the 3+1 mass scheme

$$U_{\text{PMNS}} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} & U_{\mu4} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} & U_{\tau4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

for disappearance channel,  $P(\nu_\alpha \rightarrow \nu_\alpha)$  we did not see neutrino oscillation and a very small signal for appearance channel:

$$P(\nu_\mu \rightarrow \nu_e)$$

# The 3+1 properties

For very short baselines, we can write down the survival probability as

$$P(\nu_\alpha \rightarrow \nu_\alpha) = 1 - \sin^2(2\theta_{\alpha\alpha}) \sin^2 \left( 1.27 \frac{\Delta m^2}{(\text{eV})^2} \frac{\text{L/Km}}{\text{E/GeV}} \right)$$

where  $\sin^2(2\theta_{\alpha\alpha}) = 4|U_{\alpha 4}|^2(1 - |U_{\alpha 4}|^2)$   
and the conversion probability as

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2(2\theta_{\alpha\beta}) \sin^2 \left( 1.27 \frac{\Delta m^2}{(\text{eV})^2} \frac{\text{L/Km}}{\text{E/GeV}} \right)$$

where  $\sin^2(2\theta_{\alpha\beta}) = 4|U_{\alpha 4}|^2|U_{\beta 4}|^2$



# The 3+1 properties

From  $\sin^2(2\theta_{\alpha\alpha}) = 4|U_{\alpha 4}|^2(1 - |U_{\alpha 4}|^2)$  and  $\sin^2(2\theta_{\alpha\beta}) = 4|U_{\alpha 4}|^2|U_{\beta 4}|^2$  and because all parameters  $|U_{\alpha 4}|^2$  are small, we can write down  $\sin^2(2\theta_{\mu\mu}) \sim 4|U_{\mu 4}|^2$ , and  $\sin^2(2\theta_{\mu e}) = 4|U_{\mu 4}|^2|U_{e 4}|^2$ .

This allow us to relate the survival amplitude with the conversion amplitude <sup>1</sup>:

$$\sin^2(2\theta_{\mu e}) = \frac{1}{4} \sin^2(2\theta_{\mu\mu}) \sin^2(2\theta_{ee})$$

To have a sizeable  $\sin^2(2\theta_{\mu e})$  we should also have sizeable  $\sin^2(2\theta_{\mu\mu}), \sin^2(2\theta_{ee})$ . if we assume that  $\sin^2(2\theta_{\mu\mu}) \sim \sin^2(2\theta_{ee}) \sim \epsilon^2$ , where  $\epsilon$  is a small parameter then

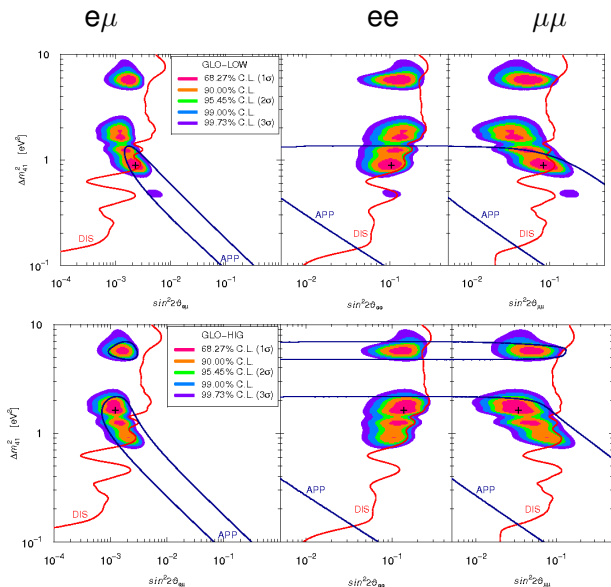
$$\sin^2(2\theta_{\mu e}) \sim \epsilon^4/4 \ll 1!!$$

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<sup>1</sup>O. L. G. P. and A. Y. .Smirnov, Nucl. Phys. B **599**, 3 (2001) [hep-ph/0011054].



# Combined analysis of sterile 3+1 scenario



# 3+1 summary

- A 3+1 scenario in principle can fit now both LSND and **MINI-BOONE neutrino e anti-neutrino**.
- Still the model have problems coinciling the **disappearance constrains and appearance signal**:  $\sin^2(2\theta_{\mu e}) \sim \epsilon^4/4$  and  $\sin^2(2\theta_{\mu\mu}) \sim \sin^2(2\theta_{ee}) \sim \epsilon^2$ .
- We need to confirm the reactor neutrino anomaly, new experiments are been planned.
- A positive signal 10% for  $\nu_{\mu} \rightarrow \nu_{\mu}$  and  $\nu_e \rightarrow \nu_e$  disappearance is expected, new short-baseline experiments?, ICECUBE, KATRIN? Can we search for that? <sup>2</sup>

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<sup>2</sup>*Light Sterile Neutrinos: A White Paper* K. N. Abazajian *et al.*,  
arXiv:1204.5379 [hep-ph].



# Fishing Sterile neutrino in ICE-CUBE

The complete evolution equation for sterile neutrinos (3+1 mass scheme) is given by

$$\frac{d}{dr}\nu_f = \left[ U_4 \frac{M^2}{2E_\nu} U_4^\dagger + A \right] \nu_f,$$

where  $\nu_f = (\nu_e \nu_\mu \nu_\tau \nu_s)^T$  and  $E_\nu$  is the neutrino energy. We get from Reference<sup>3</sup> the mixing matrix for the 3+1 case

$$U_4 = \mathbf{R}^{34}(\theta_{34}) \tilde{\mathbf{R}}^{24}(\theta_{24}, \delta_2) \tilde{\mathbf{R}}^{14}(\theta_{14}, \delta_1) \\ \mathbf{R}^{23}(\theta_{23}) \tilde{\mathbf{R}}^{13}(\theta_{13}, \delta) \mathbf{R}^{12}(\theta_{12})$$

The mixing matrix is parameterized by twelve real parameters: the six mixing angles  $\theta_{12}, \theta_{13}, \theta_{23}, \theta_{14}, \theta_{24}, \theta_{34}$ , the three Dirac phases  $\delta, \delta_1, \delta_2$ .

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<sup>3</sup>A. de Gouvea and J. Jenkins, Phys. Rev. D **78**, 053003 (2008)  
arXiv:0804.3627 [hep-ph]].



# Fishing Sterile neutrino in ICE-CUBE

$$H = \frac{1}{2E_\nu} U_{4 \times 4} \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 & 0 \\ 0 & 0 & \Delta m_{31}^2 & 0 \\ 0 & 0 & 0 & \Delta m_{41}^2 \end{pmatrix} U_{4 \times 4}^\dagger + \begin{pmatrix} A_{CC} & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & A_{NC} \end{pmatrix}$$

where  $U_{4 \times 4} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}_{4 \times 4} \begin{pmatrix} U_{3 \times 3} & 0 \\ 0 & I \end{pmatrix}$ ,

and  $A_{CC} = \sqrt{2} G_f n_e$  and  $A_{NC} = \frac{1}{\sqrt{2}} G_f n_n$





## Consequences for sterile neutrino phenomenology:

- **New MSW effects**, resonant conditions are:<sup>3</sup>

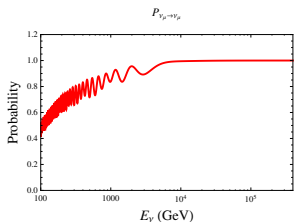
$$E_\nu \sim (2 - 5) \text{TeV} \left( -\frac{\Delta m_{41}^2}{1eV^2} \right)$$

For positive  $\Delta m_{41}^2$ , we have resonance for antineutrinos, for negative  $\Delta m_{41}^2$ , we have resonance for neutrinos.

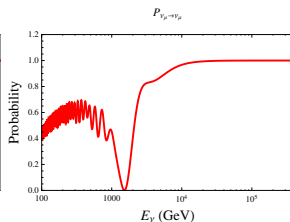
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<sup>3</sup>O. Yasuda, hep-ph/0102166; H. Nunokawa, O. L. G. P. and R. Z. Funchal, Phys. Lett. B **562**, 279 (2003)  
S. Choubey, JHEP **0712**, 014 (2007) ; S. Razzaque and A. Y. Smirnov, JHEP **1107**, 084 (2011)  
V. Barger, Y. Gao and D. Marfatia, Phys. Rev. D **85**, 011302 (2012)  
A. Esmaili, F. Halzen and O. L. G. P., arXiv:1206.6903 [hep-ph].

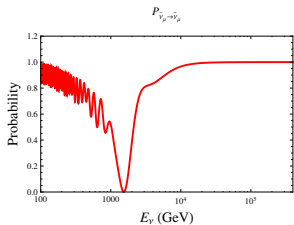
# Fishing Sterile neutrino in ICE-CUBE



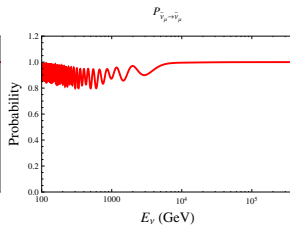
(e)



(f)



(g)

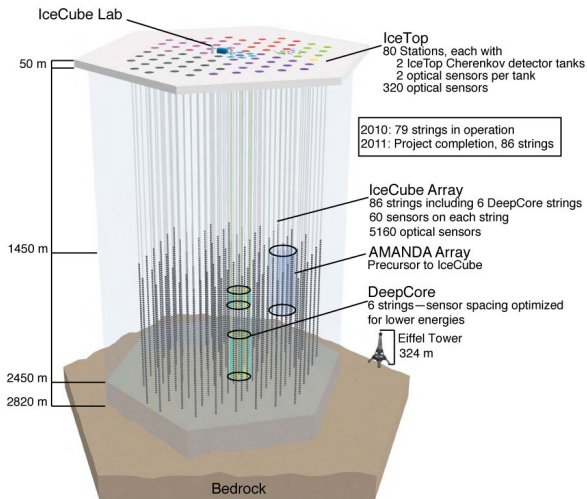


(h)



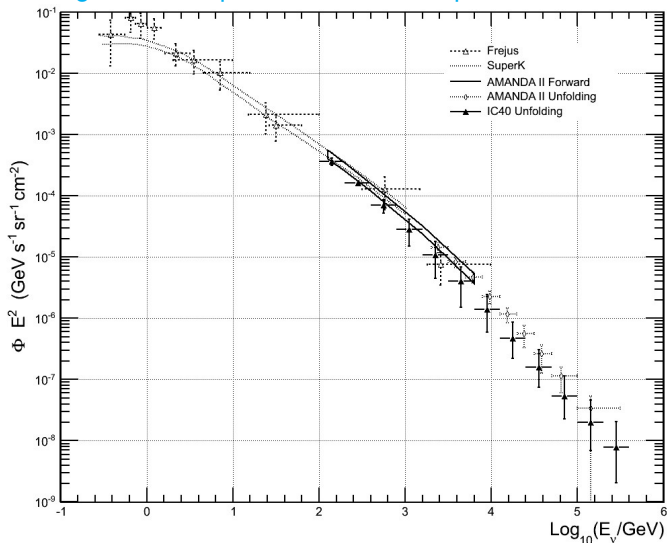
# Fishing Sterile neutrino in ICE-CUBE

A new generation of neutrino observatories: **The experiment**



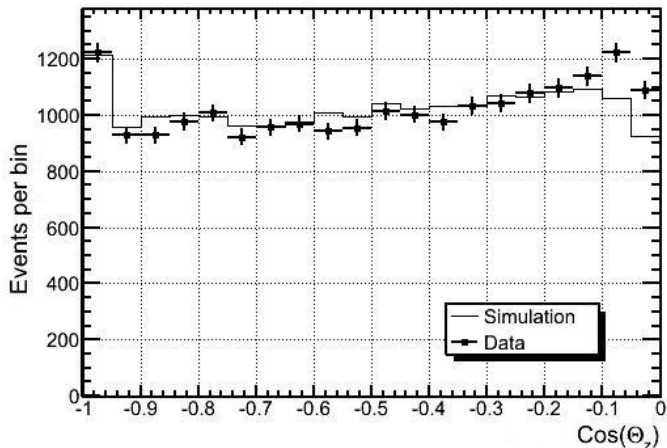
# Fishing Sterile neutrino in ICE-CUBE

The highest atmospheric neutrino sample ever measured!!



# Fishing Sterile neutrino in ICE-CUBE

The experiment ICECUBE see only upward-going neutrinos:  
matter effect!!



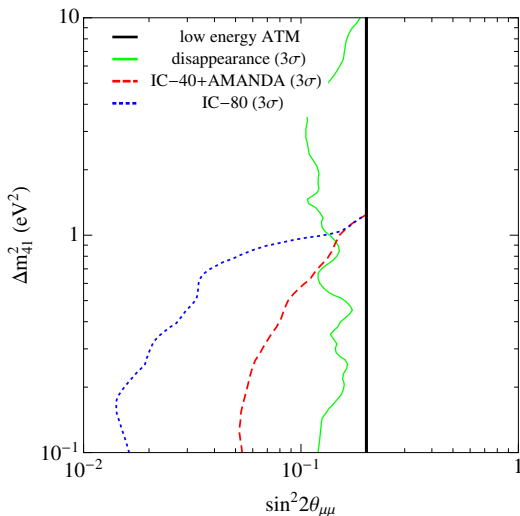
A  $\chi^2$  analysis

$$\chi^2(\Delta m_{41}^2, \theta_{34}, \theta_{24}; \alpha) = \sum_i \frac{(N_i^{\text{data}} - \alpha N_i^{3+1}(\Delta m_{41}^2, \theta_{34}, \theta_{24}))^2}{\sigma_i^2} + \frac{(1 - \alpha)^2}{\sigma_\alpha^2},$$

where  $\alpha$  fix the normalization uncertainty.



# Fishing Sterile neutrino in ICE-CUBE



The best constrains on  
 $\sin^2 2\theta_{\mu\mu}$  parameter



# Conclusions

- From a series of experiment there is evidence for a new species of neutrinos: **a sterile neutrino that mix with the other neutrinos.**
- A direct consequence of this scenario is the muon neutrino disappearance signal with  $\sin^2 2\theta_{\mu\mu} \sim 10^{-1}$  for typical  $\Delta m^2 \sim 0.1 - 1 \text{ eV}^2$ .
- It was predicted some yeas ago that the 3+1 scenario can be tested in neutrino telescope experiments. We made the analysis **using the data from ICECUBE and from AMANDA** and we have found that the sterile scenario **is disvafores by the ICECUBE/AMANDA data.**

We have put the **the best constrains on  $\sin^2 2\theta_{\mu\mu}$**  mixing angle so far.







- Kinematics of  $\beta$  decay, absolute mass scale  $m_\beta$

A effective neutrino mass can be used (for  $3\nu$ )  $m_\beta^2 = \sum_i |U_{ei}|^2 m_i^2$ .  
Present limits are  $m_\beta < 2.0$  eV.

KATRIN (2013?) expected to have sensitivity of  $m_\beta = 0.23$  eV.

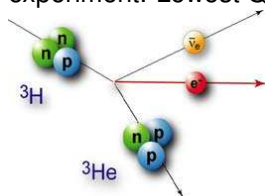


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New generation (and probably the last) search for  $\nu$  mass in  $\beta$  decay experiment. Lowest Q-value in  $\beta$  decay:  $Q = 18571.8 \pm 1.2$  eV.



$$\beta(T_e, m_0, R_{\text{ED}}) = N_s F^Z \quad (1)$$

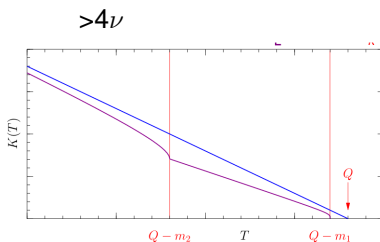
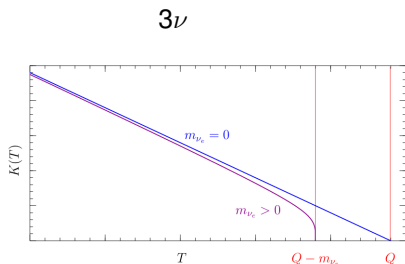
$$\sum_k p_k \mathcal{E}_k \sum_{i=1}^3 |U^{ei}|^2 \sqrt{\mathcal{E}_k^2 - m_i^2},$$

where  $F^Z$  is the Fermi function,  $\mathcal{E}_i = Q - W_i - K_e$ ,  $E_e$  and  $p_e$ ;  $W_i$  and  $p_i$  are respectively the excitation energy and transition probability for the excited state  $i$  of the daughter nucleus.



# KATRIN experiment

Effect of neutrino mass in  $\beta$  spectrum. For  $3\nu$  we can use  $m_\beta^2 = \sum_i |U_{ei}|^2 m_i^2$ , for other cases for KATRIN it is not possible to use this expression.



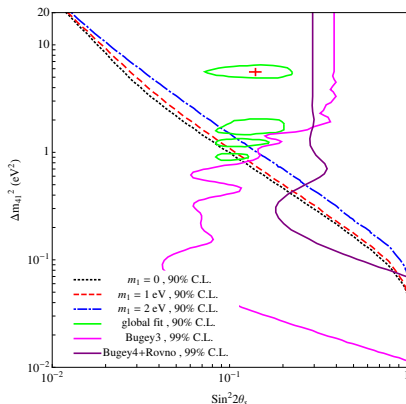
## Integrated measurement

$$S(Q, qU, [U_{ei}], [m_\nu]) = \int_0^\infty \beta(K_e, Q, [U_{ei}], [m_\nu]) T'(K_e, qU) dK_e,$$

- Thick Tritium source: atomic/molecular levels
- Energy loss of electrons inside source
- **Sanity test: We recover the quoted limite for  $3\nu$  neutrinos:**  
 $m_\beta < 0.23$  at 90 % C.L.



# Testing 3+1 model in KATRIN



Arman Esmaili and O. L. G. P, A. Esmaili and O. L. G. Peres, Phys. Rev. D **85**, 117301 (2012) [arXiv:1203.2632 [hep-ph]].

