

# Perturbative QCD in hadron collisions

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An exciting past 24 months

Higgs(-like) discovery

$t\bar{t}$  asymmetry

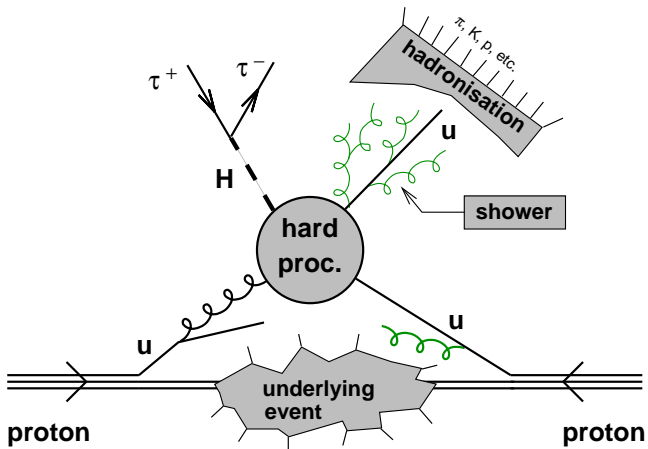
$W + \text{dijet}$  CDF anomaly

Exclusion of swathes of SUSY, etc.

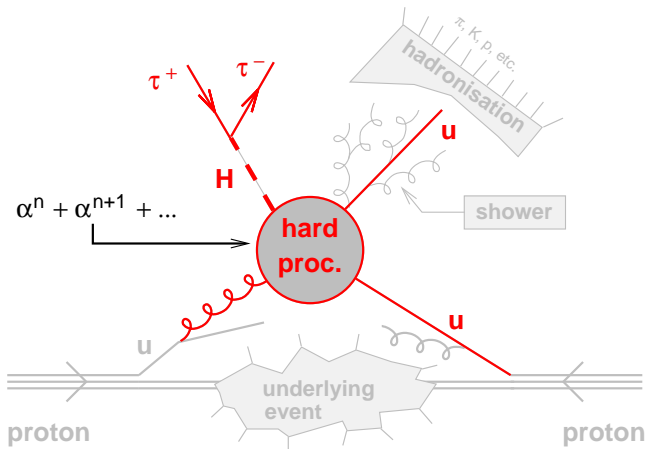
...

This talk: examine recent collider-QCD developments and the role they're playing in some of these "headline" topics, as well as touch on some open problems

# Some of what goes into collider predictions



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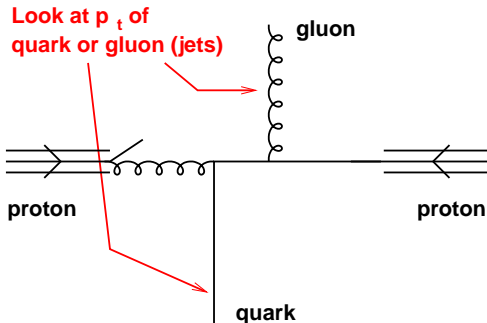
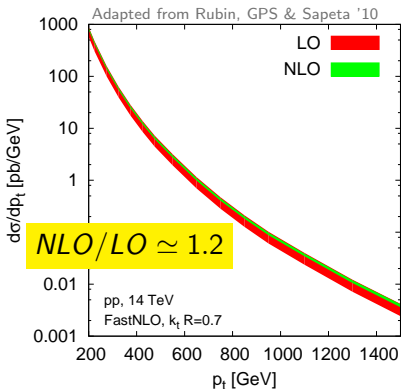
E.g. QCD corrections to  $e^+e^- \rightarrow$  hadrons cross section:

$$R = 1 + 0.32\alpha_s + 0.14\alpha_s^2 - 0.41\alpha_s^3 - 0.82\alpha_s^4$$

keep in mind  $\alpha_s(m_Z) \simeq 0.118$

# What it looks like at hadron colliders

Consider LO, NLO and their ratio  $K = \frac{\text{NLO}}{\text{LO}}$

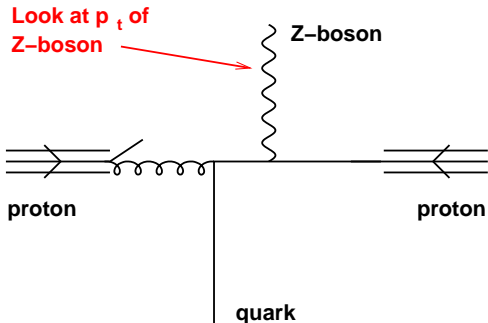
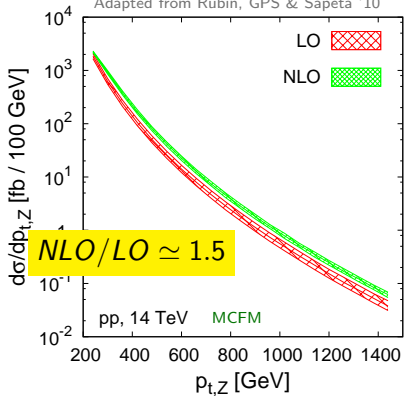


$1 + 2\alpha_s$  looks like a reasonable series

# What it looks like at hadron colliders

Consider LO, NLO and their ratio  $K = \frac{\text{NLO}}{\text{LO}}$

Adapted from Rubin, GPS & Sapeta '10

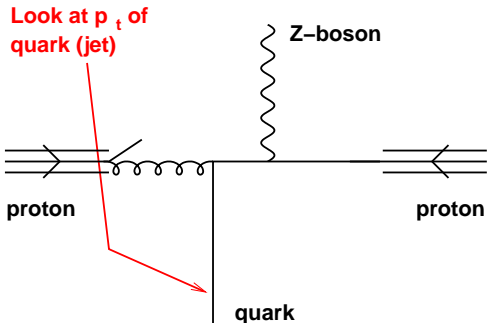
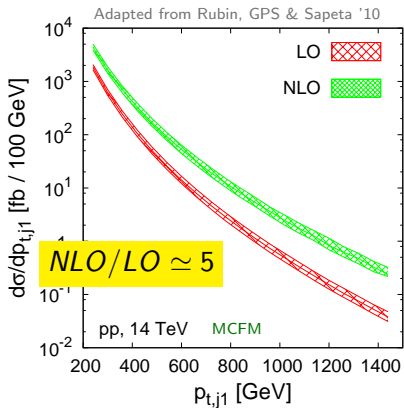


$1 + C \times \alpha_s$ , with quite large  $C \simeq 5$

To date, no generalised understanding of size of  $C$  when in range 5 – 10

# What it looks like at hadron colliders

Consider LO, NLO and their ratio  $K = \frac{\text{NLO}}{\text{LO}}$



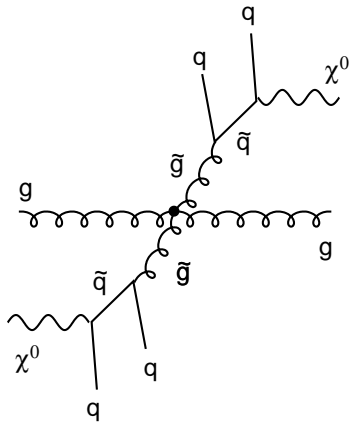
$1 + C\alpha_s \rightarrow C = 50$  ?!! Often driven by new topologies



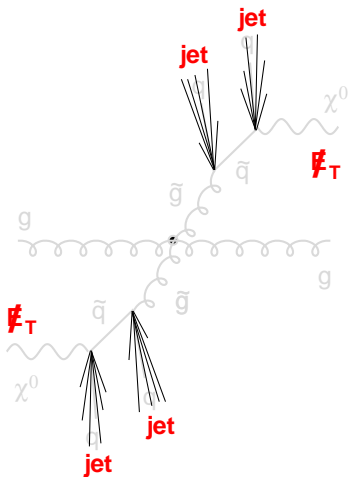
# The NLO revolution

and one way it's being used

## Signal

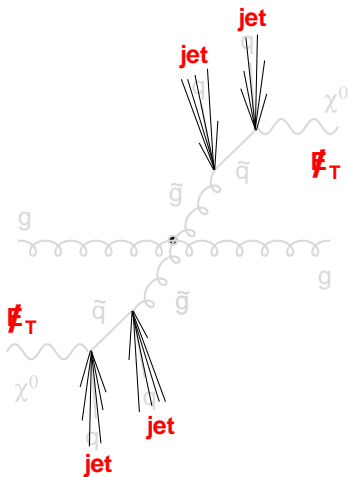


Signal

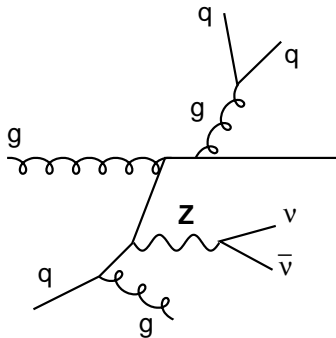


# SUSY example: gluino pair production

Signal

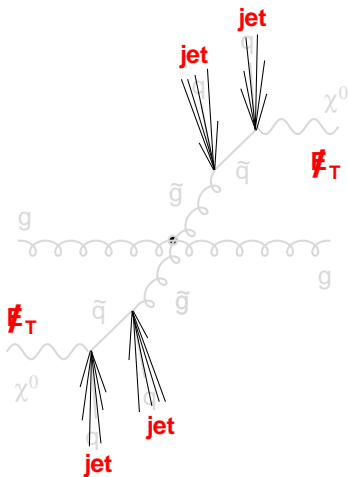


Background

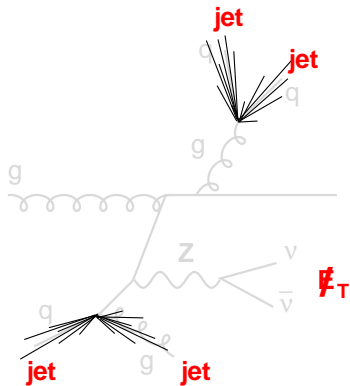


# SUSY example: gluino pair production

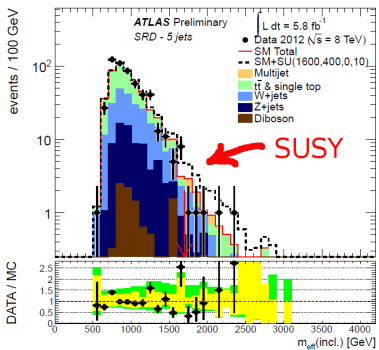
Signal



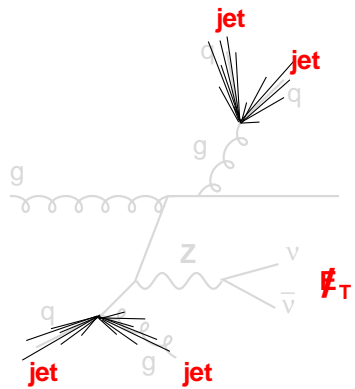
Background



## Signal

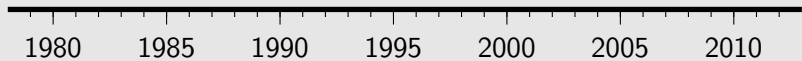


## Background

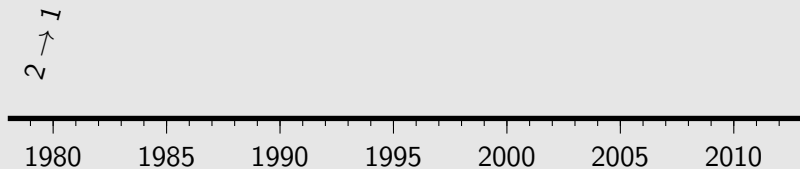


**Complexity of NLO calculation determined by final-state multiplicity: a  $2 \rightarrow 5$  process.**

## NLO timeline



## NLO timeline

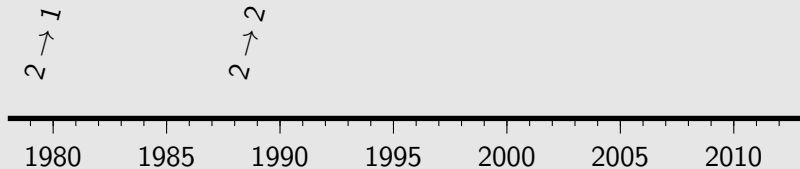


1979: NLO Drell-Yan [Altarelli, Ellis & Martinelli]

1991: NLO  $gg \rightarrow$  Higgs [Dawson; Djouadi, Spira & Zerwas]



# NLO timeline



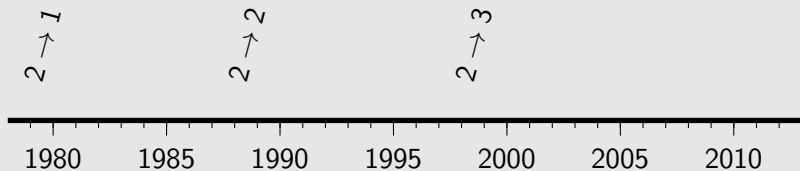
1987: NLO high- $p_t$  photoproduction [Aurenche et al]

1988: NLO  $b\bar{b}$ ,  $t\bar{t}$  [Nason et al]

1988: NLO dijets [Aversa et al]

1993:  $V_j$  [JETRAD, Giele, Glover & Kosower]

# NLO timeline



1998: NLO  $Wb\bar{b}$  [MCFM: Ellis & Veseli]

2000: NLO  $Zb\bar{b}$  [MCFM: Campbell & Ellis]

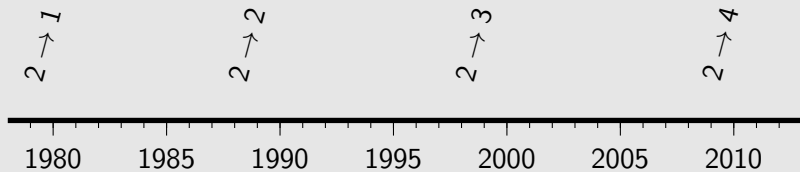
2001: NLO  $3j$  [NLOJet++: Nagy]

...

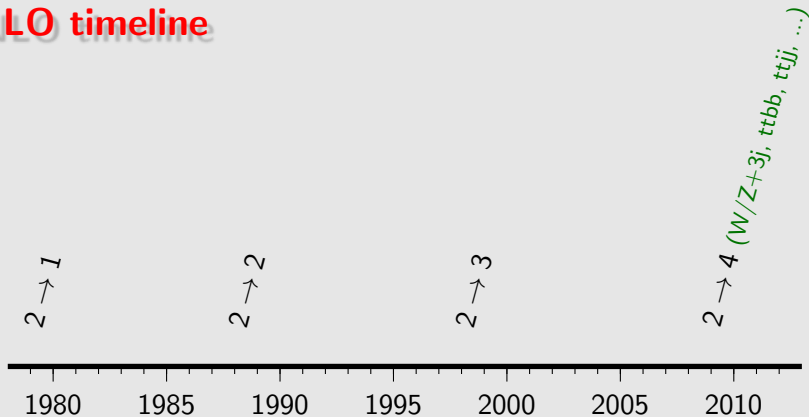
2007: NLO  $t\bar{t}j$  [Dittmaier, Uwer & Weinzierl '07]

...

## NLO timeline



# NLO timeline



2009: NLO  $W+3j$  [Rocket: Ellis, Melnikov & Zanderighi]

[unitarity]

2009: NLO  $W+3j$  [BlackHat+Sherpa: Berger et al]

[unitarity]

2009: NLO  $t\bar{t}b\bar{b}$  [Bredenstein et al]

[traditional]

2009: NLO  $t\bar{t}b\bar{b}$  [HELAC-NLO: Bevilacqua et al]

[unitarity]

2009: NLO  $q\bar{q} \rightarrow b\bar{b}b\bar{b}$  [Golem: Binoth et al]

[traditional]

2010: NLO  $t\bar{t}jj$  [HELAC-NLO: Bevilacqua et al]

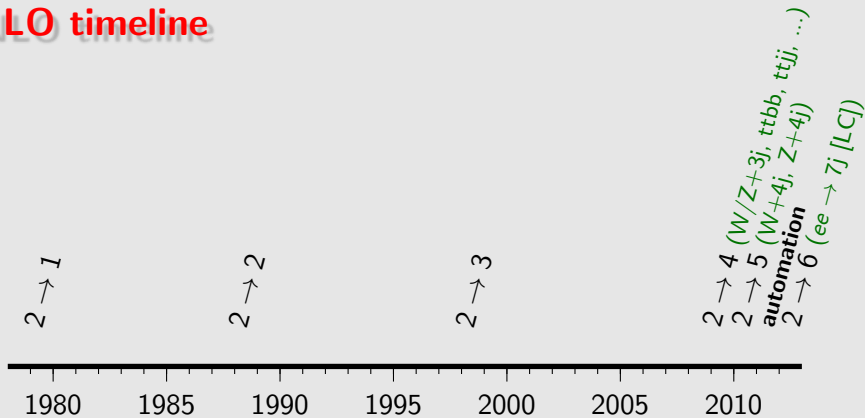
[unitarity]

2010: NLO  $Z+3j$  [BlackHat+Sherpa: Berger et al]

[unitarity]

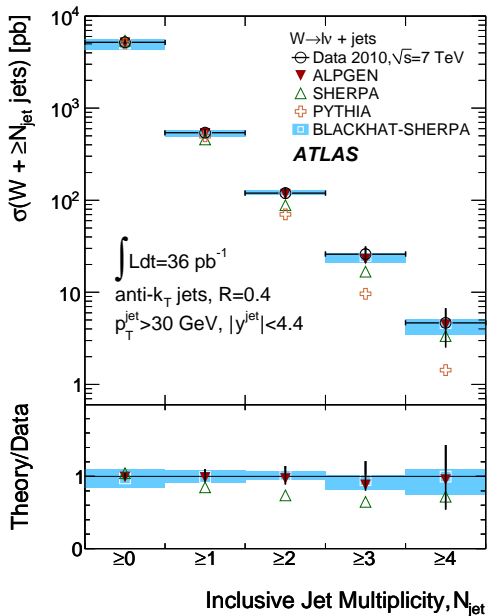
...

# NLO timeline



- 2010: NLO  $W+4j$  [BlackHat+Sherpa: Berger et al] [unitarity]
- 2011/12: NLO  $WWjj$  [Rocket: Melia et al; GoSaM+MadX Greiner et al] [unitarity]
- 2011: NLO  $Z+4j$  [BlackHat+Sherpa: Ita et al] [unitarity]
- 2011/12: NLO  $4j$  [BlackHat/NGLuons+Sherpa: Bern et al; Badger et al] [unitarity]
- 2011–: first automation [MadNLO: Hirschi et al] [unitarity + feyn.diags]
- 2011–: first automation [Helac NLO: Bevilacqua et al] [unitarity]
- 2011–: first automation [GoSam: Cullen et al] [feyn.diags(+unitarity)]
- 2011:  $e^+e^- \rightarrow 7j$  [Becker et al, leading colour] [numerical loops]

# W + 0,1,2,3,4 jets @NLO



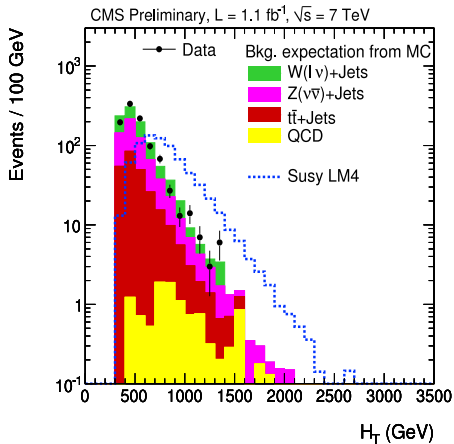
Technical revolution has gone hand-in-hand with LHC measurements of these complex processes.

Powerful validation of NLO approach.

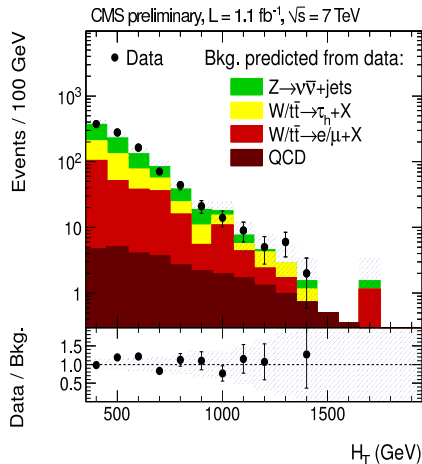
So do SUSY searches now just compare data to NLO?

# Two plots from a CMS SUSY analysis

## Data v. Monte Carlo backgrounds



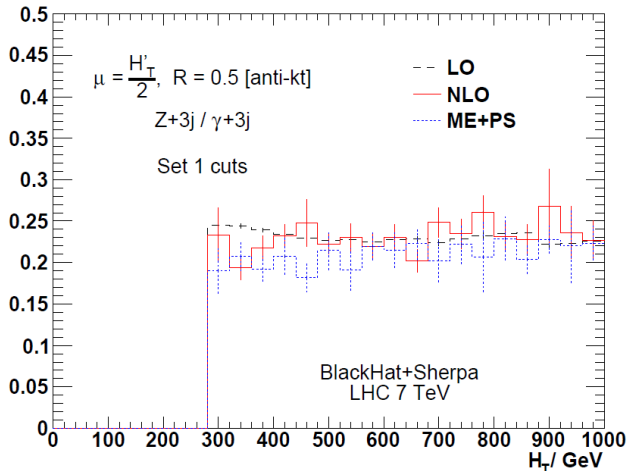
## Data v. “data-driven” backgrounds



So where are the NLO predictions being used?

The CMS search did **not** estimate  $Z+\text{jets}$  bkgd from NLO. Instead used

$$\frac{d\sigma^{Z+\text{jets}}}{dH_T} = \left( \frac{d\sigma^{\gamma+\text{jets}}}{dH_T} \right)_{\text{data}} \times \left( \frac{d\sigma^{Z+\text{jets}}}{dH_T} / \frac{d\sigma^{\gamma+\text{jets}}}{dH_T} \right)_{\text{NLO}}$$



Example of widely used **data-driven** bkgd estimates

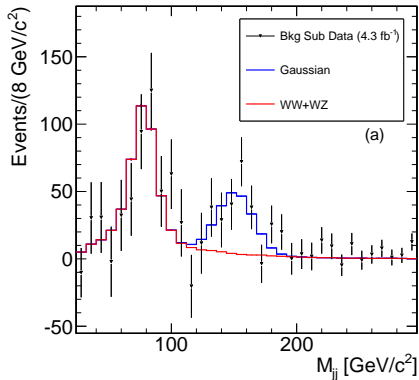
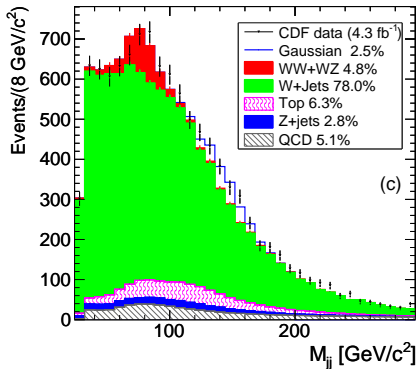
Combine best of theory knowledge with best of experimental knowledge.



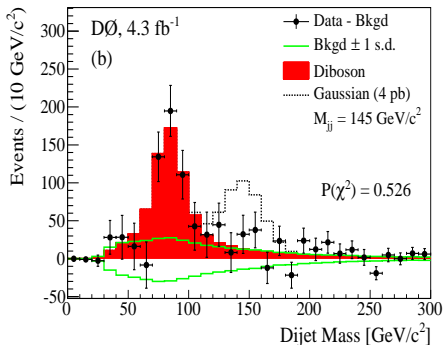
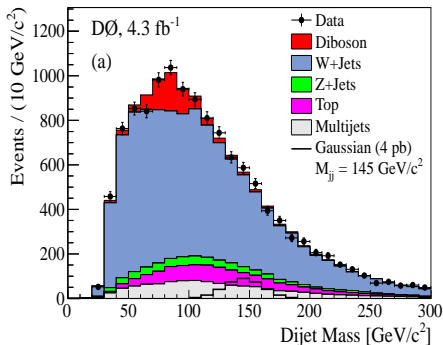
# Merging NLO and showers

and the CDF  $W + \text{dijet}$  anomaly

# Remember the CDF $W$ +dijet excess?



# and the D0 W+dijet non-excess?



CDF and D0 data are **not** being compared to NLO (=W+partons):

They are “detector-level” data and can only be compared to hadron-level calculations + detector simulation.

In this case hadron-level = Alpgen  $\otimes$  Pythia

Perturbative expansion: for precision.

Parton Showers (PS): for realism;

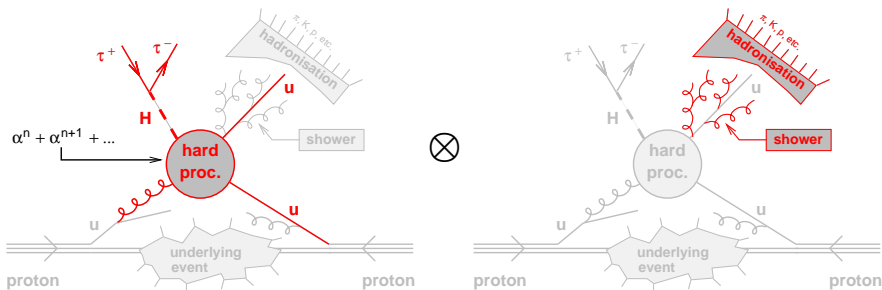
**To combine them: must remove double counting**

## Tree-level (LO) + PS

Different tree-level multiplicities ( $W$ ,  $W+1j$ ,  $W+2j$ , etc.) get combined

MLM/CKKW: Alpgen+Pythia/Herwig, MadGraph, Sherpa, ...

Fully automated



## NLO + PS — MC@NLO, POWHEG

Greater accuracy, but harder to perform than LO+PS:

NLO contains more physics than LO,  
so more double-counting with parton shower

Less “available” than tree+PS: until recently,

- ↳ A single (low) multiplicity, e.g. W@NLO + PS
- ↳ Programmed manually for each process

### Recently: move towards automation:

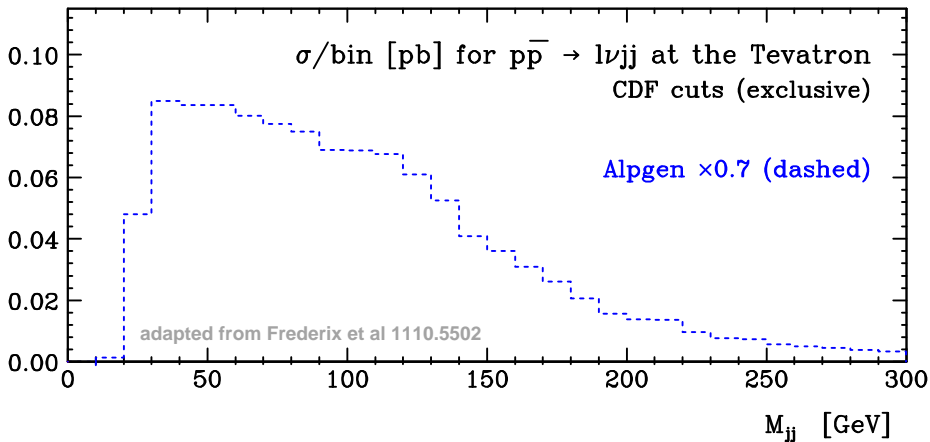
POWHEGBox:  $t\bar{t}$ +jet,  $W^+W^++2j$ , ...

aMC@NLO (MadLoop + auto MC@NLO):  $W+2j$ ,  $Z+2b$ , ...

+ ideas for combining multiplicities, extending their applicability  
e.g. MENLOPS, MINLO, FxFx merging, Sherpa merging, UNLOPS, ...

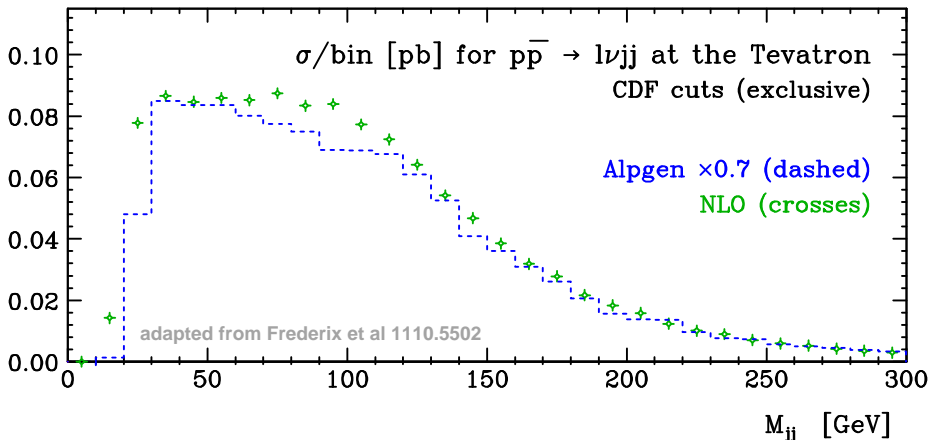
One application of this progress has been to the W+dijet anomaly

# CDF & DØ use Alpgen (scaled): tree level QCD + parton shower



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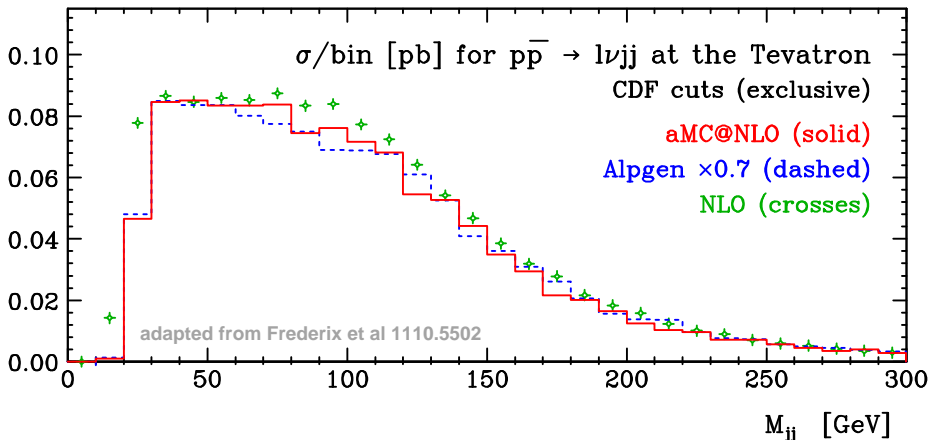
NLO has substantial shape differences: should we worry?



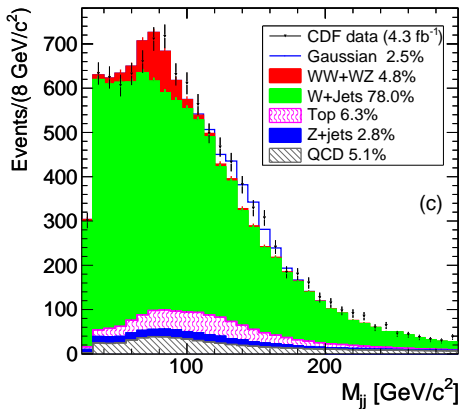
CDF & DØ use Alpgen (scaled): tree level QCD + parton shower

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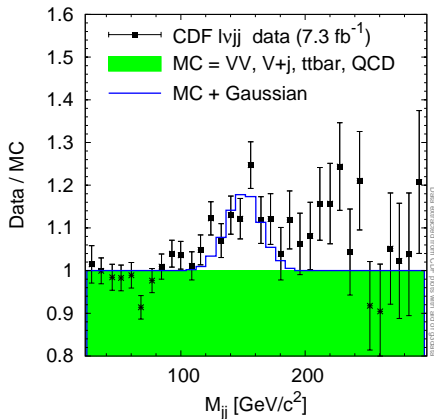
NLO + parton shower (aMC@NLO) is close to Alpgen  
→ QCD under good control

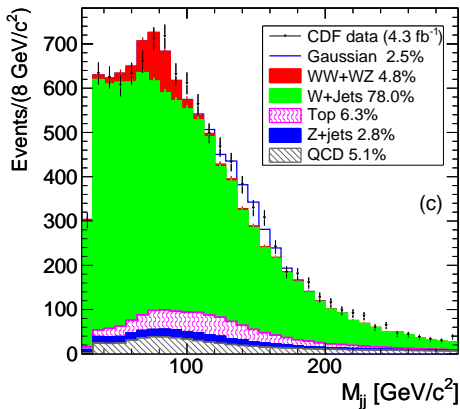




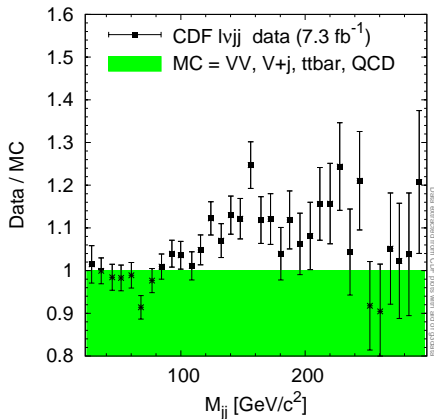


Instead of data – MC  $\Rightarrow$  **data/MC**

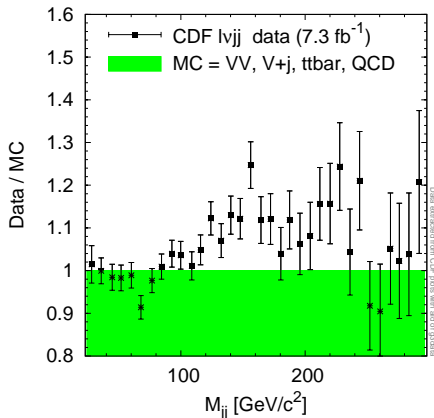
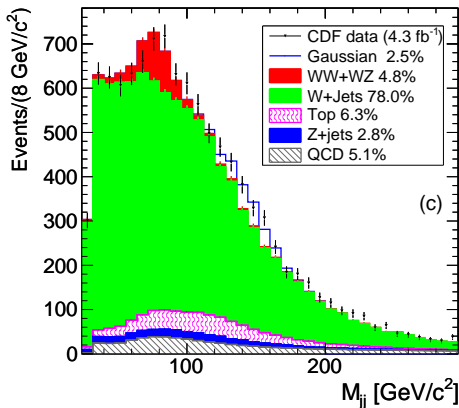




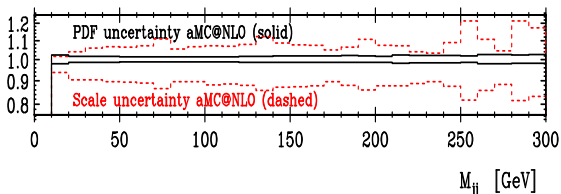
Instead of data – MC  $\Rightarrow$  **data/MC**



Instead of data – MC  $\Rightarrow$  **data/MC**



**aMC@NLO**  
uncertainties:  $\rightarrow$

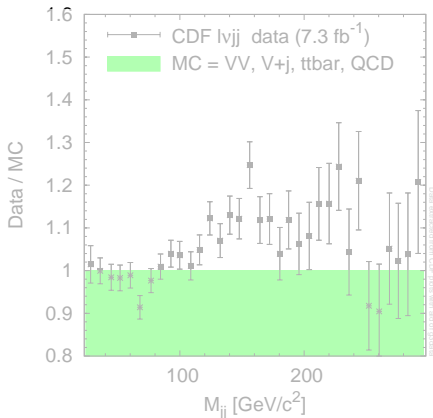
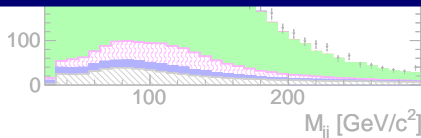


Instead of data – MC  $\Rightarrow$  **data/MC**

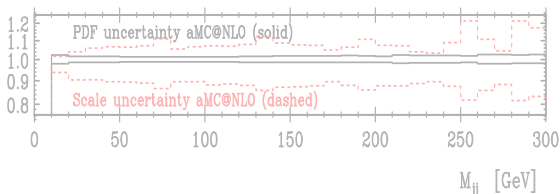


“Anomaly” is a 10% effect  
(not clear it’s really a peak)

10% is clearly at limit  
of NLO accuracy



aMC@NLO  
uncertainties:  $\rightarrow$



# Going beyond limitations of NLO

[two of the options]

High precision — NNLO — is crucial for key processes, but not yet always available:

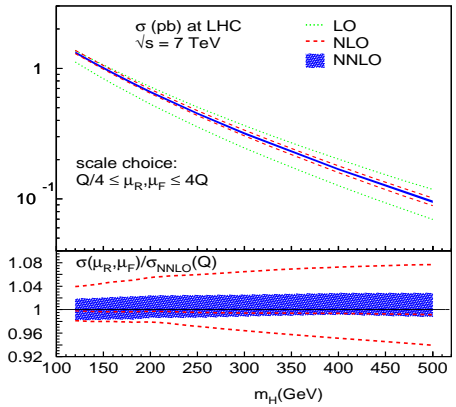
✓  $W, Z, \text{Higgs}, \gamma\gamma, \text{VBF}, VH, (t\bar{t})$

✗  $VV, (t\bar{t}), \text{inclusive jets, etc.}$

Important also to develop methods so that we're less sensitive to limits on our precision.

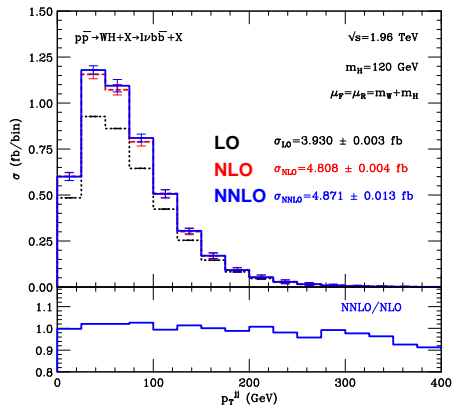
Generally by finding ways to distinguish signals from the background more efficiently, i.e. increasing  $S/B$ .

## New in 2010: NNLO VBF $\rightarrow$ H



Bolzoni, Maltoni, Moch & Zaro

## New in 2011: NNLO WH (differential)



Ferrera, Grazzini & Tramontano

Most groundbreaking new NNLO calculation of past years:

$$q\bar{q} \rightarrow t\bar{t}$$

Baernreuther, Czakon and Mitov 2012

First NNLO calculation with coloured particles in the initial **and** final state. Its new techniques may help open the way to many other important NNLO calculations.

Until now analyzed in approximate NNLO

Beneke, Czakon, Falgari, Mitov, Schwinn '09

... as an extension of the NLO

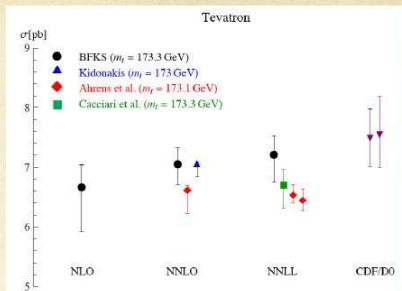
Nason, Dawson, Ellis '88  
Beenakker et al '89

... resummed NLL

Sterman, Kidonakis '97  
Bonciani, Catani, Mangano, Nason '98

and now NNLL resummation

Beneke, Falgari, Schwinn '10  
Czakon, Mitov, Sterman '10  
Ahrens et al '10-'11



Beneke, Falgari, Klein, Schwinn '11

Comparison between various groups shows:

- ✓ Significant differences between various predictions
- ✓ Suggests the true approximate NNLO uncertainty
- ✓ The realistic improvements over NLO+NLL are small (to be expected)

Cacciari, Czakon, Mangano, Mitov, Nason '11

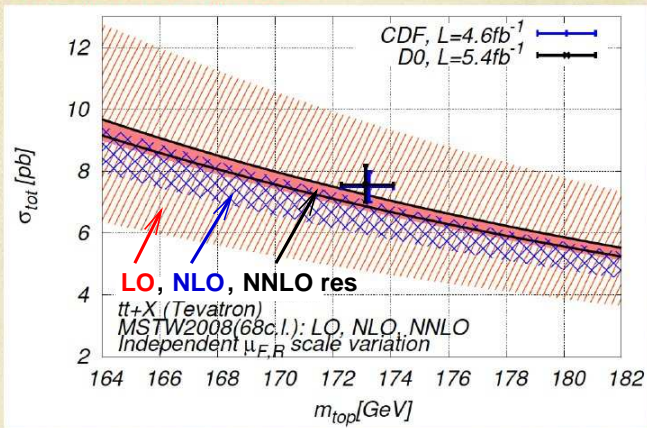


# Baernreuther, Czakon & Mitov NNLO $q\bar{q} \rightarrow t\bar{t}$ cross-section

Good perturbative convergence:

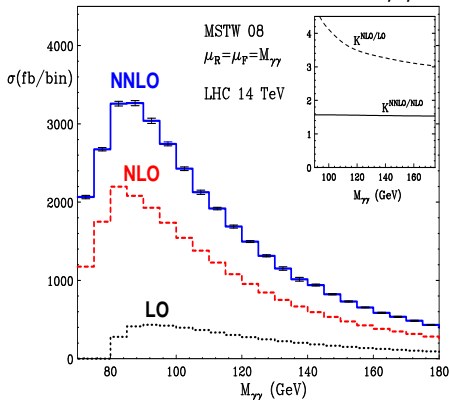
- ✓ Independent F/R scales
- ✓  $m_t=173.3$

P. Baernreuther et al arXiv:1204.5201



- ✓ Good overlap of various orders (LO, NLO, NNLO).
- ✓ Suggests our (restricted) independent scale variation is good

New in 2011: NNLO  $\gamma\gamma$



Some key processes see large or giant NLO/NNLO corrections.

Can't help but wonder if we're missing something, especially in the  $gg \rightarrow H$  case.

Catani, Cieri, de Florian, Ferrera & Grazzini

# One series that's ugly: gluon fusion Higgs cross section

For 8 TeV pp collisions,  $m_H = 125$  GeV:

$$\begin{aligned}\sigma_{gg \rightarrow H} &= 6.8 \text{ pb} (1 + 9.9\alpha_s + 36\alpha_s^2 + \dots) \\ &= 6.8 \text{ pb} (1 + 1.23 + 0.56 + \dots) = 19.0 \text{ pb}\end{aligned}$$

$$\text{for } \mu_R = \mu_F = \frac{1}{2}m_H, \alpha_s(\mu_R) = 0.124$$

$$\begin{aligned}\sigma_{gg \rightarrow H} &= 5.6 \text{ pb} (1 + 11.4\alpha_s + 63\alpha_s^2 + \dots) \\ &= 5.6 \text{ pb} (1 + 1.27 + 0.79 + \dots) = 17.2 \text{ pb}\end{aligned}$$

$$\text{for } \mu_R = \mu_F = m_H, \alpha_s(\mu_R) = 0.112$$

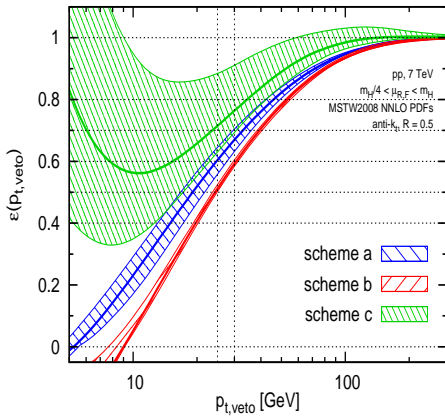
There are explanations: threshold logarithms,  $\pi^2$  terms from analytic continuation. A problem is perhaps that there are too many explanations. . .

Baglio & Djouadi have raised the convergence issue before

Everything else you try about (gluon-fusion) Higgs production suffers as a result of the original bad series: e.g. **jet veto efficiency**

## FIXED ORDER PREDICTION

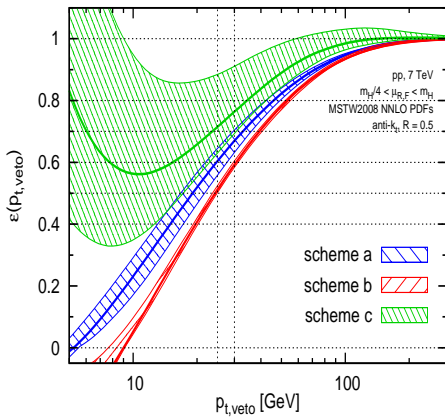
Higgs production ( $m_H = 125$  GeV), NNLO



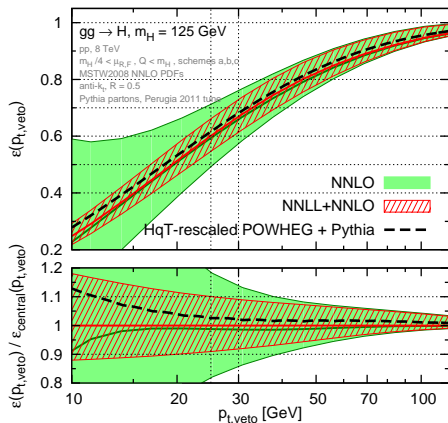
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## FIXED ORDER PREDICTION

Higgs production ( $m_H = 125$  GeV), NNLO



## RESUMMED PREDICTION

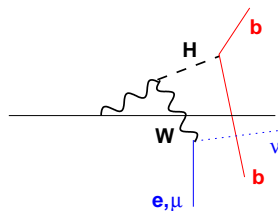


Banfi, Monni, GPS & Zanderighi '12  
 see also Becher & Neubert '12

# Looking at data differently

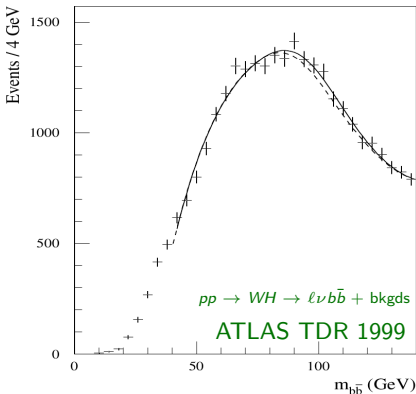
$H \rightarrow b\bar{b}$  (57% of decays) v. hard to see

Best hope is  $pp \rightarrow W^\pm H$  (and  $ZH$ ),  $W^\pm \rightarrow \ell^\pm \nu$ ,  $H \rightarrow b\bar{b}$ .



$H \rightarrow b\bar{b}$  (57% of decays) v. hard to see

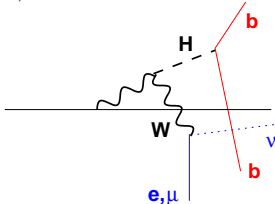
Best hope is  $pp \rightarrow W^\pm H$  (and  $ZH$ ),  $W^\pm \rightarrow \ell^\pm \nu$ ,  $H \rightarrow b\bar{b}$ .



**Conclusion (ATLAS TDR):**

*“The extraction of a signal from  $H \rightarrow b\bar{b}$  decays in the  $WH$  channel will be very difficult at the LHC, even under the most optimistic assumptions [...]”*

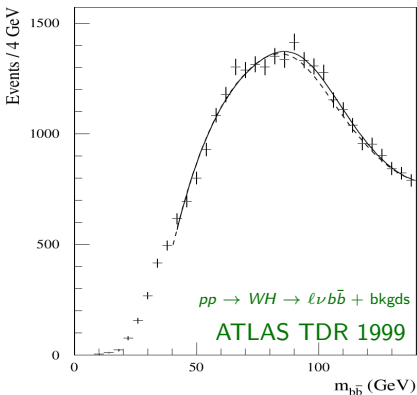
Low efficiency, huge backgrounds, e.g.  $t\bar{t}$   
NB: Evidence of this channel seen recently at Tevatron, but similar difficulties





# $H \rightarrow b\bar{b}$ (57% of decays) v. hard to see

Best hope is  $pp \rightarrow W^\pm H$  (and  $ZH$ ),  $W^\pm \rightarrow \ell^\pm \nu$ ,  $H \rightarrow b\bar{b}$ .



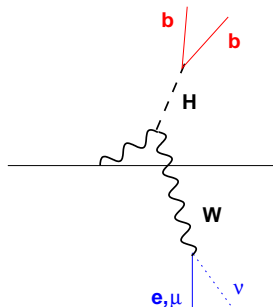
## Conclusion (ATLAS TDR):

*“The extraction of a signal from  $H \rightarrow b\bar{b}$  decays in the  $WH$  channel will be very difficult at the LHC, even under the most optimistic assumptions [...]”*

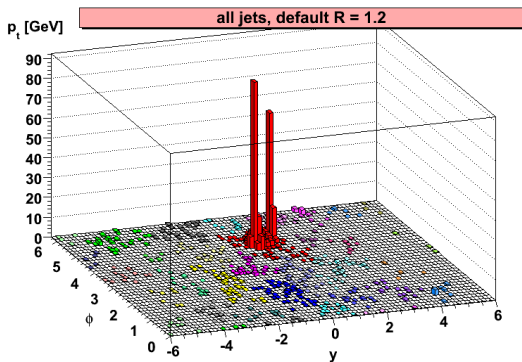
Low efficiency, huge backgrounds, e.g.  $t\bar{t}$

## Analysis of signal/bkgd suggests:

- ▶ Go to high  $p_t$  ( $p_{tH}, p_{tW} > 200$  GeV)
- ▶ Lose 95% of signal, but more efficient?
- ▶ Maybe kill  $t\bar{t}$  & gain clarity?



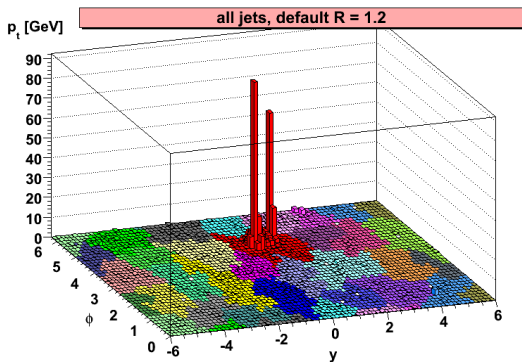
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



Cluster event, C/A, R=1.2

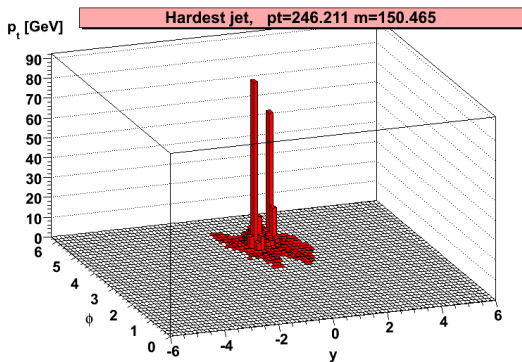
Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

Fill it in,  $\rightarrow$  show jets more clearly

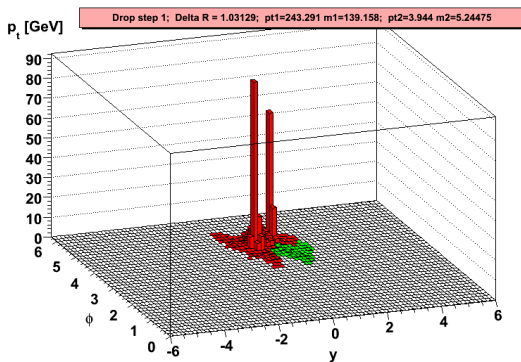
Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

Consider hardest jet,  $m = 150$  GeV

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

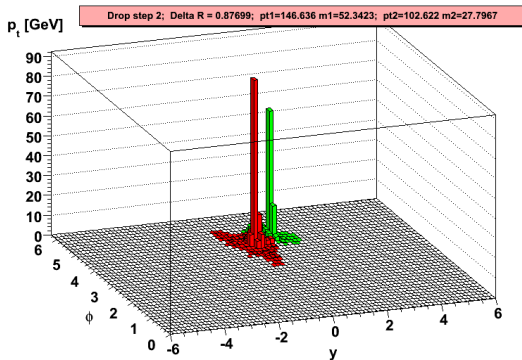
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



split:  $m = 150$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.92 \rightarrow$  repeat

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

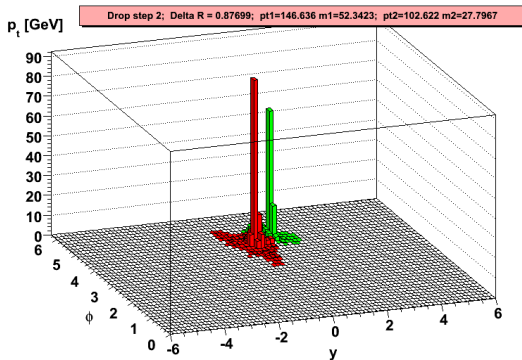
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



split:  $m = 139$  GeV,  $\frac{\max(m_1, m_2)}{m} = 0.37 \rightarrow$  mass drop

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

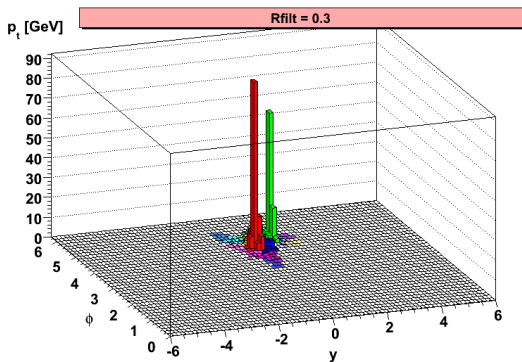
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3



check:  $y_{12} \simeq \frac{p_{t2}}{p_{t1}} \simeq 0.7 \rightarrow \text{OK} + 2 \text{ } b\text{-tags (anti-QCD)}$

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

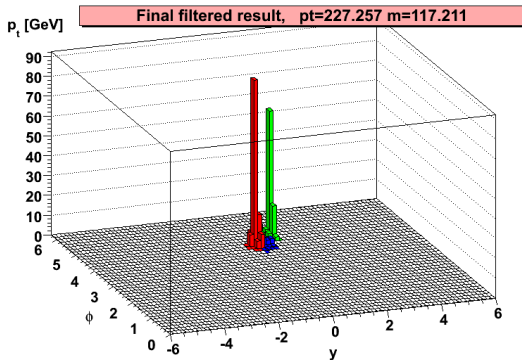
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

 $R_{filt} = 0.3$ 

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al



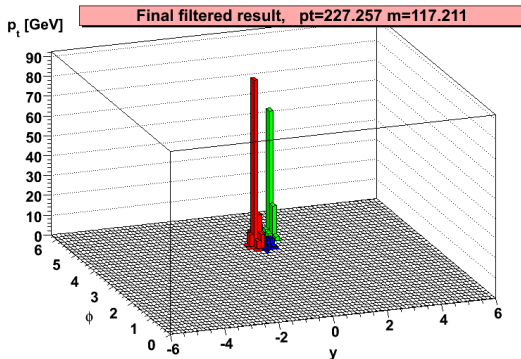
Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

 $R_{filt} = 0.3$ : take 3 hardest,  $m = 117$  GeV

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al

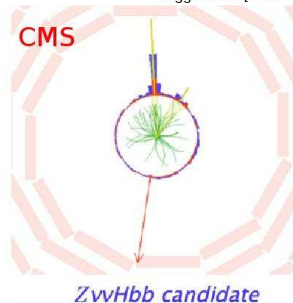
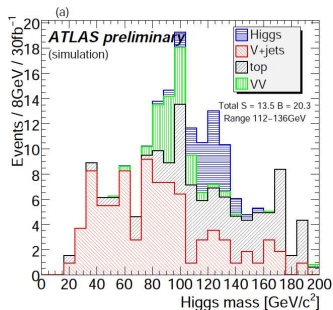
# $pp \rightarrow ZH \rightarrow \nu\bar{\nu}b\bar{b}$ , @14 TeV, $m_H = 115$ GeV

Herwig 6.510 + Jimmy 4.31 + FastJet 2.3

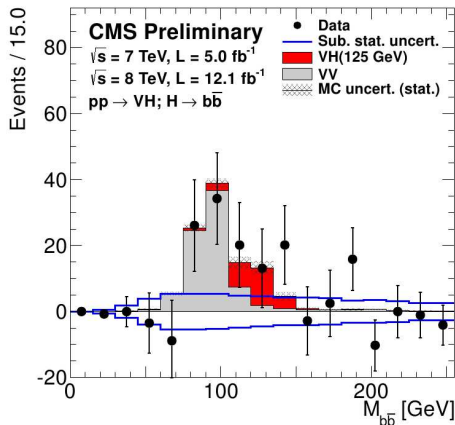
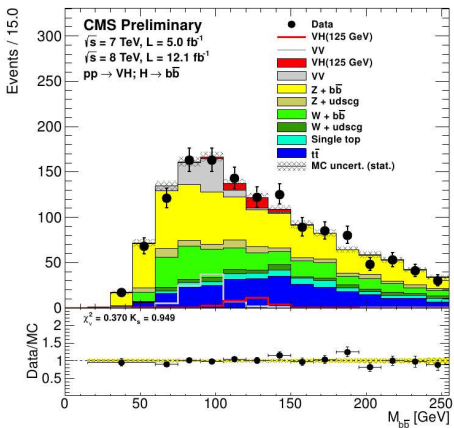


$R_{filt} = 0.3$ : take 3 hardest,  $m = 117$  GeV

Butterworth, Davison, Rubin & GPS '08  
also earlier work by Seymour; Butterworth et al



# ATLAS and CMS $H \rightarrow b\bar{b}$ are high- $p_t$ , but 2-jet based

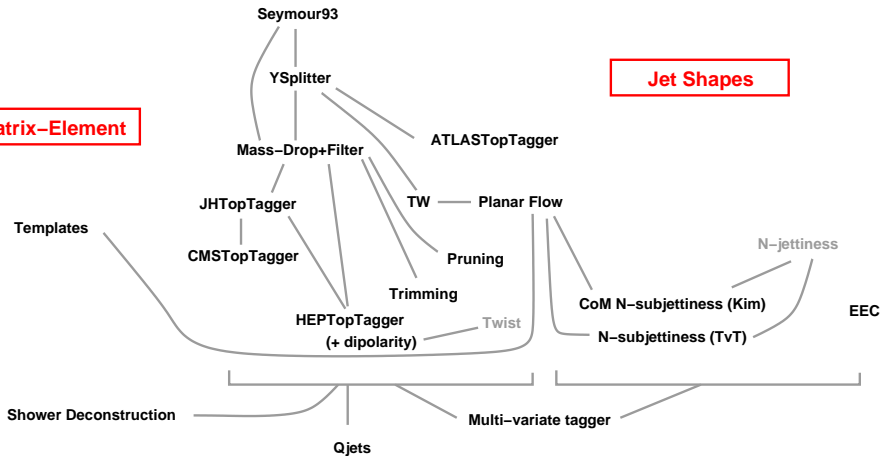


# Some taggers and jet-substructure observables

Jet Declustering

Jet Shapes

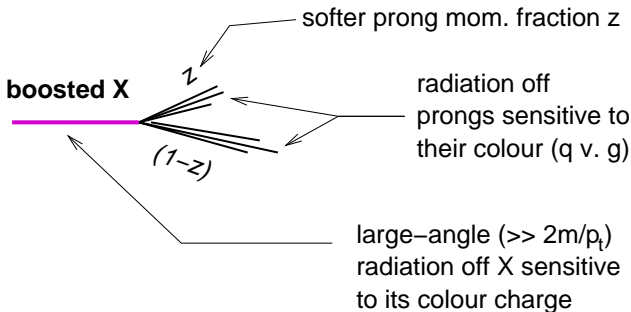
Matrix-Element



apologies for omitted taggers, arguable links, etc.

[NB: many of the tools available in FastJet & SpartyJet]

# Handles for distinguishing signal v. background



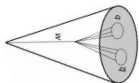
	$g \rightarrow gg(g)$	$q \rightarrow qg(g)$	$g \rightarrow b\bar{b}$	$H \rightarrow b\bar{b}$	$t \rightarrow qq\bar{q}$
softer prong $z$	soft	soft	hard	hard	hard
prong colour factors	$2 \times C_A$	$C_F + C_A$	$2 \times C_F$	$2 \times C_F$	$3 \times C_F$
system colour factor	$C_A$	$C_F$	$C_A$	0	$C_F$

Background-like

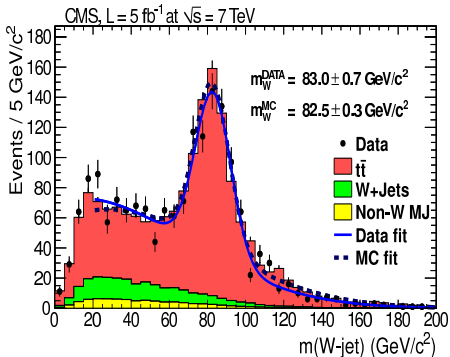
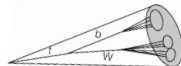
Signal-like

# Boosted Ws and tops in single jets: data!

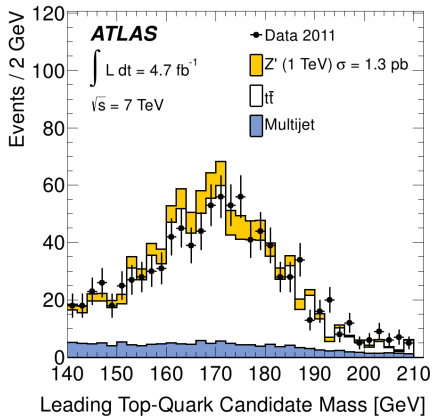
## W's in a single jet



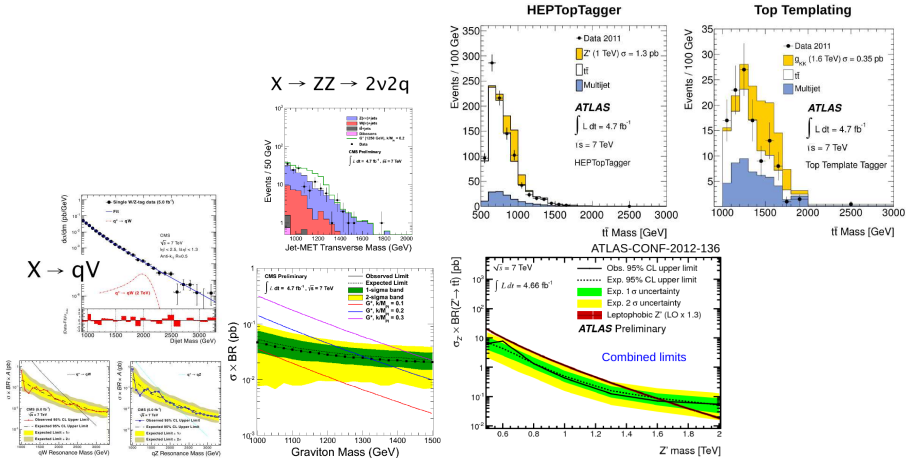
## tops in a single jet



with Pruning + Mass Drop requirement  
 NB: combined in IR unsafe way...



# Some BSM searches with jet-substructure techniques



A range of techniques being used for varied BSM scenarios

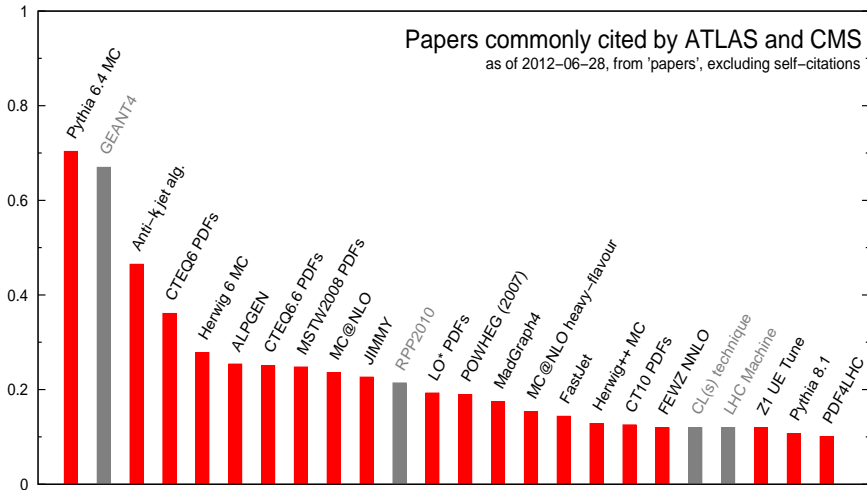
# Closing



fraction of ATLAS & CMS papers that cite them

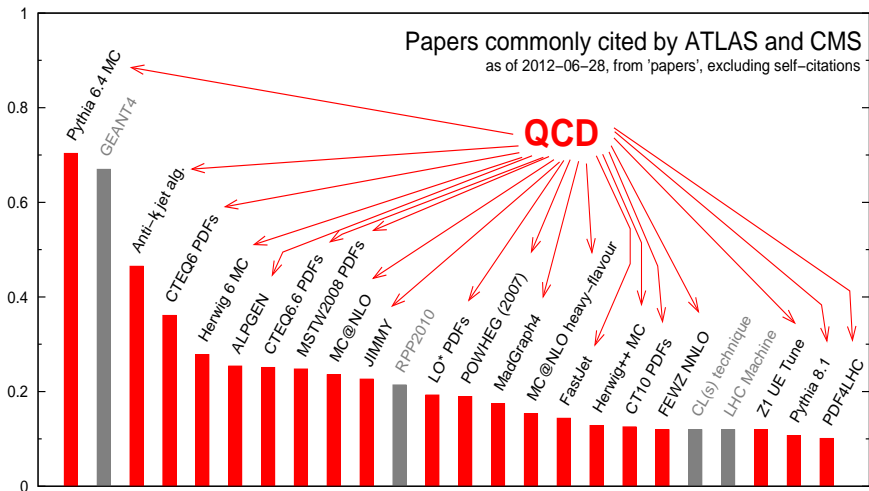
# Papers commonly cited by ATLAS and CMS

as of 2012-06-28, from 'papers', excluding self-citations



Plot by GP Salam based on data from ATLAS, CMS and INSPIREHEP

fraction of ATLAS & CMS papers that cite them



Plot by GP Salam based on data from ATLAS, CMS and INSPIREHEP

today's progress in QCD = tomorrow's workhorse

# EXTRAS

## Traditional

Draw all Feynman diagrams with 1 loop. Work out formulae for them.

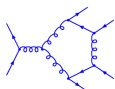
Work hard to reduce integrals to known forms (+ tricks).

### Tree and one-loop contributions to $pp \rightarrow t\bar{t}b\bar{b} + X$

Ansgar Denner (PSI)



7 trees



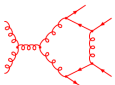
24 pentagons



8 hexagons



36 trees



114 pentagons

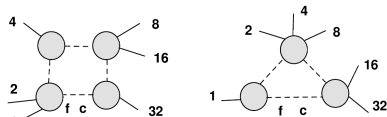


40 hexagons

## Recursive/unitarity methods

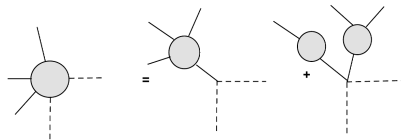
Assemble loop-diagrams from individual tree-level diagrams.

Build trees by sticking together simpler tree-level diagrams



Costas G. Papadopoulos (Athens)

Blobs are always tree-like objects



## Traditional

Draw all Feynman diagrams with 1 loop. Work out formulae for them.

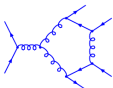
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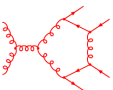
24 pentagons



8 hexagons



36 trees



114 pentagons



40 hexagons

## Recursive/unitarity methods

Assemble loop-diagrams from individual tree-level diagrams.

Build trees by sticking together simpler tree-level diagrams

## Some main ideas:

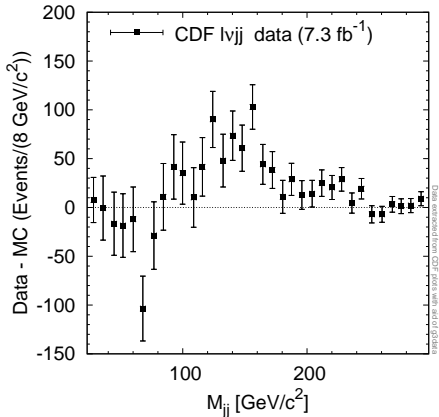
Bern, Dixon & Kosower '93  
[sewing together trees]

Britto, Cachazo & Feng '04  
[on-shell complex loop momenta]

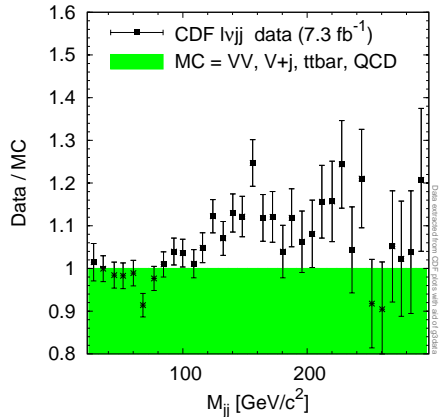
Ossola, Pittau & Papadopoulos '06  
[handful of loop momentum choices give full amplitude]

# CDF $W_{jj}$ : difference wrt MC v. ratio to MC

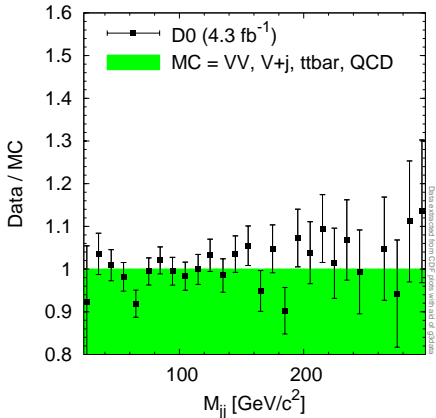
## CDF difference



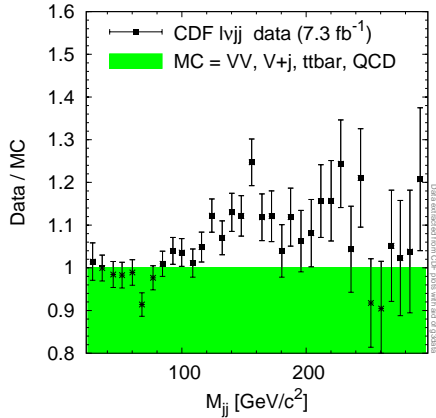
## CDF ratio



## DØ ratio



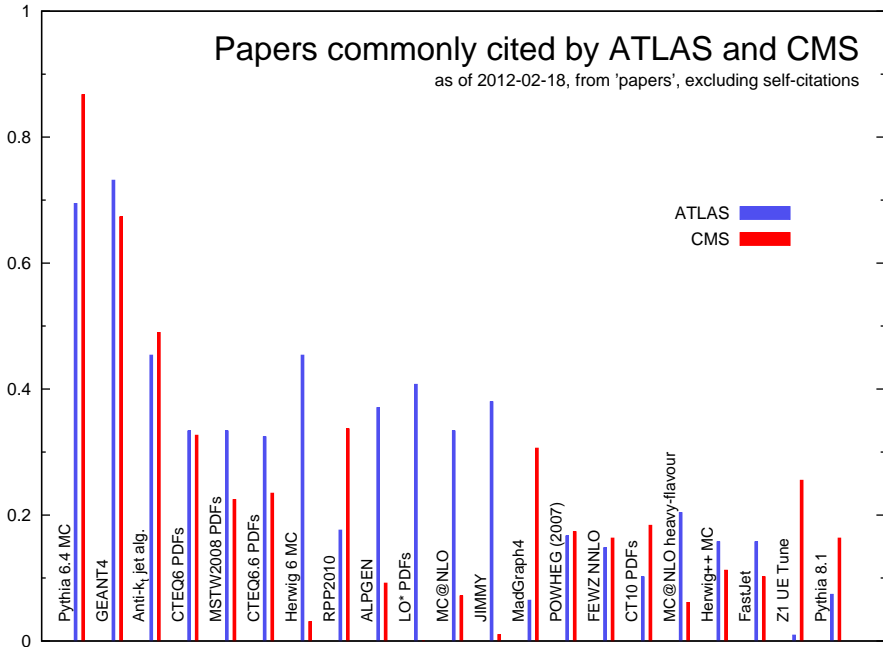
## CDF ratio



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as of 2012-02-18, from 'papers', excluding self-citations

fraction of ATLAS & CMS papers that cite them



Plot by GP Salam based on data from ATLAS, CMS and INSPIREHEP