

# DARK MATTER HALO PROFILES IN MODIFIED GRAVITY SIMULATIONS

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Observational cosmology workshop

## 1 MODIFIED GRAVITY SIMULATIONS

- Simulations
- Power spectrum
- Halo mass function
- Halo profiles

## 2 STRONG GRAVITATIONAL LENSING

- Time-delays
- Bayesian analysis
- Testing on synthetic catalogs
- Results from observational data

# MODIFIED GRAVITY

## MODIFIED GRAVITY SIMULATIONS

SIMULATIONS

POWER SPECTRUM

HALO MASS FUNCTION

HALO PROFILES

## STRONG GRAVITATIONAL LENSING

TIME-DELAYS

BAYESIAN ANALYSIS

TEST

RESULTS

- ▶ alternative to general relativity
- ▶ small scales: gives back standard gravity
- ▶ large scales: compatible with current constraints
- ▶ expansion history similar to  $\Lambda$ CDM

Collaborators: Marcos Lima, Claudio Llinares, David Mota, Leonardo Duarte, Rodrigo Voivodic

## ISIS CODE

Llinares, Mota & Winther, 2014  
 DM only. 128 Mpc/h,  $512^3$  particles  
 $\Lambda$ CDM,  $f(R)$ , Symmetron

Model	$\lambda_0$	$z_{SSB}$	$\beta$	Model	$n$	$ f_{R0} $	$\lambda_0$
Symm A	1	1	1	fofr4	1	$10^{-4}$	23.7
Symm B	1	2	1	fofr5	1	$10^{-5}$	7.5
Symm C	1	1	2	fofr6	1	$10^{-6}$	2.4
Symm D	1	3	1				

# POWER SPECTRUM

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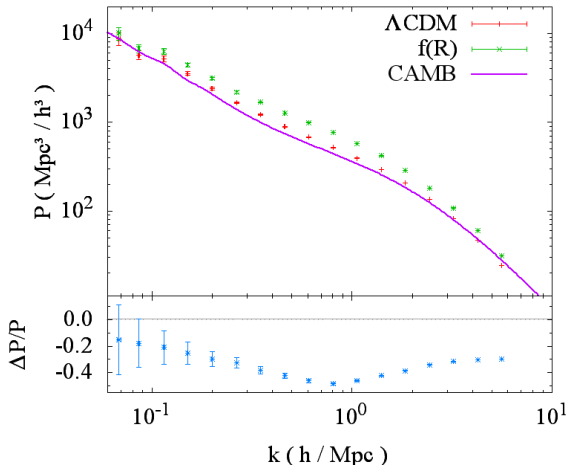
STRONG  
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# HALO MASS FUNCTION

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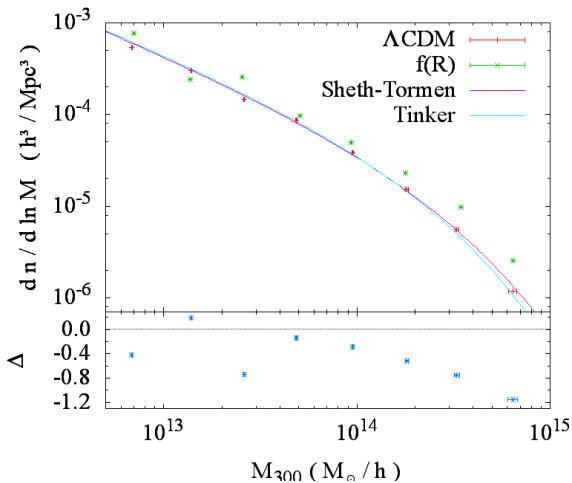
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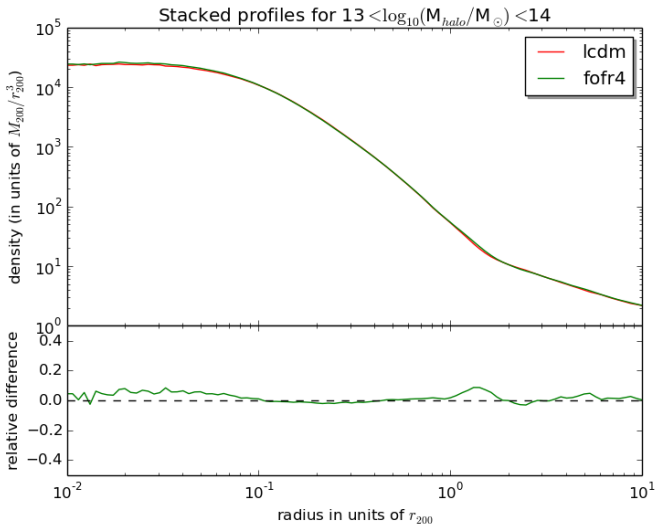
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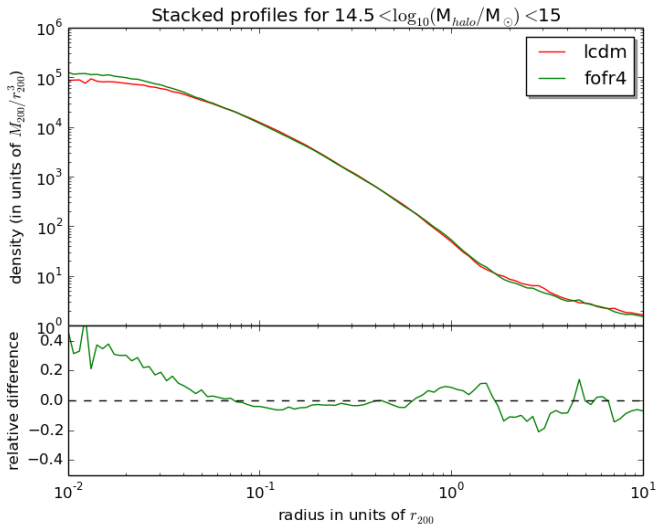
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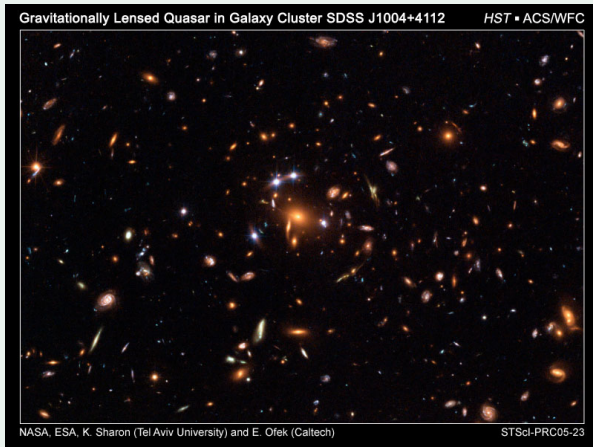
TEST

RESULTS





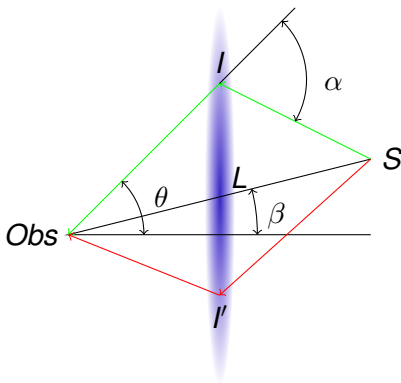
## WHAT IS A GRAVITATIONAL LENS?



## DENOMINATION

2 images : double lens

4 images : quadruple lens



## FERMAT'S PRINCIPLE

Images are formed at extremum of the arrival time.

$\beta$ : source position

$\theta$ : image position on the sky

$\alpha$ : light deviation

$$t = (1 + z_l) \frac{d_l d_s}{d_{ls}} \left[ \frac{1}{2} (\theta - \beta)^2 - \psi(\theta) \right]$$

## TIME DELAY EXPRESSION

$$\Delta t_{A,B} = (1 + z_l) \frac{d_l d_s}{d_{ls}} \left\{ \frac{1}{2} \left[ (\theta_A - \beta)^2 - (\theta_B - \beta)^2 \right] + \psi(\theta_A) - \psi(\theta_B) \right\}$$

with

$$\frac{d_l d_s}{d_{ls}} \propto H_0^{-1}$$

- ▶  $\Delta t_{AB}$ : measured when the source is variable (quasar)
- ▶ mass distribution: reconstructed through a model

# LENS MODELS

## SPHERICAL MODEL

$$\rho(r) \propto r^{-n}$$

$$\psi(\vec{\theta}) = \frac{\theta_E^2}{3-n} \left( \frac{\theta}{\theta_E} \right)^{3-n}$$

## ELLIPTICAL MODEL

$$\psi(\vec{\theta}) = \frac{\theta_E^2}{3-n} \left( \frac{\sqrt{(1-\epsilon)\theta_1^2 + (1+\epsilon)\theta_2^2}}{\theta_E} \right)^{3-n}$$

# INFLUENCE OF THE ENVIRONMENT

## SEVERAL COMPONENTS

$$\psi(\vec{\theta}) = \psi_0(\vec{\theta}) + \psi_1(\vec{\theta}) + \dots$$

or

## GLOBAL SHEAR TERM

$$\psi(\vec{\theta}) = \psi_0(\vec{\theta}) - \frac{1}{2}\gamma\theta^2 \cos 2(\phi - \phi_\gamma)$$

High number of parameters ( $\theta_E$ ,  $n$ ,  $\epsilon$ ,  $\phi_\epsilon$ ,  $\gamma$ ,  $\phi_\gamma$ ...): models underconstrained.

# TWO COMPETING MODELS

## SPHERICAL MODEL $\mathcal{M}_0$

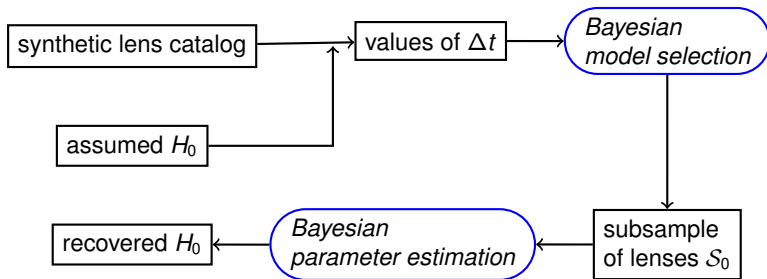
$$\psi(\vec{\theta}) = \frac{\theta_E^2}{3-n} \left( \frac{\theta}{\theta_E} \right)^{3-n}$$

## MODEL INCLUDING ANGULAR STRUCTURE $\mathcal{M}_1$

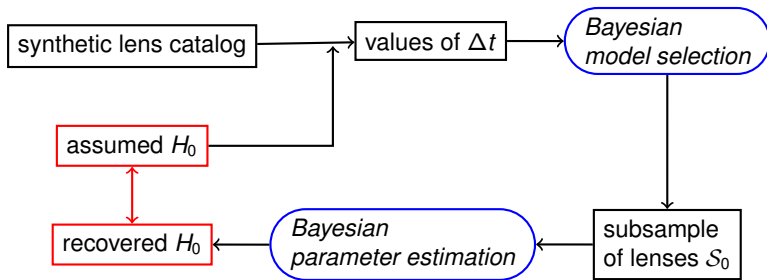
$$\psi(\vec{\theta}) = \frac{\theta_E^2}{3-n} \left( \frac{\theta}{\theta_E} \right)^{3-n} - \frac{1}{2} \gamma \theta^2 \cos 2(\phi - \phi_\gamma)$$

Use of Bayesian evidence to determine whether the data requires model  $\mathcal{M}_1$ .

# TESTING OUR METHOD



# TESTING OUR METHOD





## CATALOG WITH SHEAR

500 lenses simulated using `gravlens` (Keeton, 2011)  
with model  $\mathcal{M}_1$ :

$$\psi(\vec{\theta}) = \frac{\theta_E^2}{3-n} \left( \frac{\theta}{\theta_E} \right)^{3-n} - \frac{1}{2} \gamma \theta^2 \cos 2(\phi - \phi_\gamma)$$

## RANDOMLY GENERATED PARAMETERS

- ▶  $\theta_E = 1$
- ▶  $n = 2 \pm 0.3$
- ▶  $\gamma = 0.2 \pm 0.1$
- ▶  $\phi_\gamma = 0$
- ▶ source position:  $-1 < x, y < 1$

→ 280 double lenses

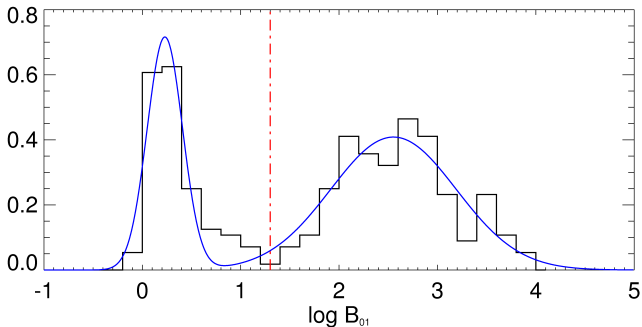
# COMPARISON OF THE EVIDENCES

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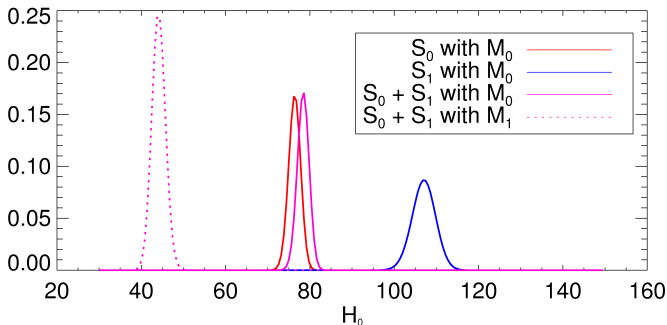
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favors  $\mathcal{M}_1$   
←  
model with shear

favors  $\mathcal{M}_0$   
→  
spherical model

RECOVERED VALUE OF  $H_0$ Starting value for  $h = H_0/100$  km/s/Mpc: 0.72RESULT FROM THE ANALYSIS OF  $\mathcal{S}_0$ 

$h = 0.76^{+0.016}_{-0.015}$ : compatible within  $3\sigma$  with the starting value.

# OBSERVATIONAL DATA

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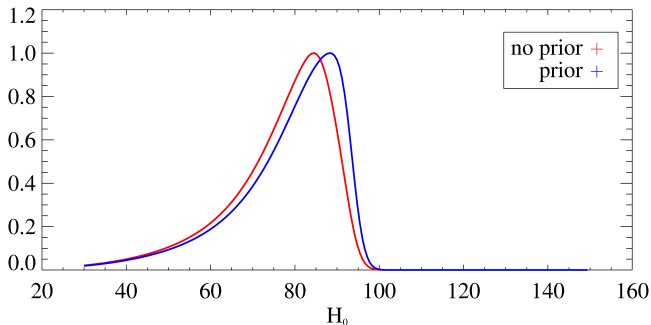
## LENSES WITH MEASURED $\Delta t$

- ▶ 12 doubles
- ▶ 8 quads

## BAYES FACTOR SELECTION

3 lenses favor model  $\mathcal{M}_0$ :

- ▶ B1600+434
- ▶ SBS 1520+530
- ▶ SDSS J1650+4251

RESULTS ON  $H_0$ 

$$H_0 = 76_{-5}^{+15} \text{ km/s/Mpc}$$

results published in Balmès & Corasaniti, 2013

# CONCLUSION

- ▶ Modified gravity differs from  $\Lambda$ CDM at transition scales, creating differences in structure formation.
- ▶ Bayesian statistics can help select homogeneous data samples.
- ▶ Time-delays give additional constraint on  $H_0$ .