the evolutionary dynamics of hematopoiesis (in health & disease)

Jorge M. Pacheco

http://dl.dropbox.com/u/6053055/SP2016-5-of-5.pdf







friday – 11:15 – 12:30

 hints for future refinements of the standard model (SM) telomere length & age ontogeny, symmetric and asymmetric cell division
 the ecology of cancer from an Evolutionary Game Theory perspective – a concrete application to yet another hematopoetic disease

telomere length & age

follow-up of telomere length with age in a cohort of 385 patients



same log during growth and linear/log during adulthood dependence with age is confirmed by an independent follow-up of a 2nd cohort with of 875 healthy humans;

telomere length & age

follow-up of telomere length with age in a cohort of 385 patients



during ontogeny, cell replication rates may change in time & symmetric self-renewal as well as asymmetric cell division are more likely (log) than in adulthood (lin).

telomere length & age math model investigates patterns of HSC replication in time



the telomere length distribution is a traveling wave (in time) that widens and shifts towards shorter length values; maximum scales like 1/Vt

telomere length & age

further analysis of 47 cord blood and 28 bone marrow samples reveals:

an increasing stem cell pool during childhood adolescence &

an approximately maintained stem cell population in adults

telomere length & age



single/measurement of telomere length

telomere length & age



telomere length & age

single measurement of telomere length model fit to same age



telomere length & age

single measurement of telomere length model fit to same age



single measurement of telomere length model fit to same age

Teance crait (k)p

<u>0.25 individual 1</u>

the math background model allows detection of individual differences from a single tissue sample

prospectively, this allows comparison of cell proliferation between individuals and identify abnormal HSC dynamics, affecting the risk of HSC related diseases. to other ages

Teonene lenen (kim)

the possibility that, during ontogeny, HSC cell replication rates may change in time allows the following generalization



ontogenic growth of active HSC pool in humans



refined SM leads to a context dependent cell replication dynamics that allows an understanding of some previously unexplained diseases :

ontogenic growth of active HSC pool in humans



Werner et al, Stem Cells (2016, in press)

what is known :

- arises in utero
- occurs in ~30% of infants with Down syndrome
 - (also known as trisomy 21)
- mutation in exon 2 of the gene coding for the transcription factor GATA1 is involved
- additional (unknown) factors on chromosome 21
 cooperate with GATA1 leading to disease
- can be fatal (so that effective incidence may be higher)

what is known :

In most cases, TL resolves without specific therapy

in a few cases, it progresses into acute megakaryoblastic leukemia (AMKL)

this may happen years after the TL clone had become undetectable.



mutational hit occurs early in embryonic development



clonal load (black line) reaches its peak on average shortly after birth (black dot)



as the clone proliferates, also total stem cell number increases



thus downregulating clonal expansion which is outcompeted once the size of the healthy stem cell population is high enough



contribution of the clone becomes negligible after approximately 1 year



however, total extinction of the clone requires about 4 years

the ecology of cancer from an Evolutionary Game Theory perspective

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Full Paper

Cancer phenotype as the outcome of an evolutionary game between normal and malignant cells

D Dingli^{*,1}, FACC Chalub², FC Santos³, S Van Segbroeck⁴ and JM Pacheco⁵

British Journal of Cancer (2009), 1–7 © 2009 Cancer Research UK All rights reserved 0007–0920/09

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Competition between species can stabilize public-goods cooperation within a species

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www.bjcancer.com

Full Paper Cancer phenotype as the outcome of an evolutionary game between normal and malignant cells

spatial populations of cells & other micro-organisms often show coexistence behavior in nature (coined recently as *negative frequency dependence*)

Nature Reviews Cancer | AOP, published online 17 April 2014; doi:10.1038/nrc3712

PERSPECTIVES

OPINION

Turning ecology and evolution against cancer

Kirill S. Korolev, Joao B. Xavier and Jeff Gore

of endangered and extinct species that were not able to adapt to the changing environment. So, in this Opinion article, we turn to conservation biology, ecology and evolution to identify the common mechanisms that cause extinction or that inhibit adaptation.

Despite the broad appreciation of cancer as an evolutionary process, much less work has gone into characterizing the ecological aspects

this being the case,

- what is the nature of the cell-cell interaction ?
- what is the "game" cells play ?

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this being the case,

- what is the nature of the cell-cell interaction ?
- what is the "game" cells play ?



this means f_a and f_b in the replicator equation are *frequency dependent*





this means *a* and *b* in the replicator equation are *frequency dependent*



frequency independent selection (2 cell lineages)

$$\begin{array}{cccc}
1 & 2 \\
1 & a \\
2 & b \\
\end{array}$$

 $\begin{aligned} f_1(x) &= x \times a + (1-x) \times a = a \\ f_2(x) &= x \times b + (1-x) \times b = b \end{aligned} \Rightarrow \dot{x} &= x(1-x)(a-b) \end{aligned}$

1 gets a from interacting with 1 and a from interacting with 2
2 gets b from interacting with 1 and b from interacting with 2



fitness is independent of the relative abundance of each cell lineage

frequency dependent selection (2 cell lineages)

$$\begin{array}{ccc}
1 & 2 \\
1 & a & c \\
2 & d & b
\end{array}$$

 $\begin{aligned} f_1(x) &= x \times a + (1-x) \times c \neq a \\ f_2(x) &= x \times d + (1-x) \times b \neq b \end{aligned} \Rightarrow \dot{x} &= x (1-x) (f_1(x) - f_2(x)) \end{aligned}$

I gets a from interacting with 1 and c from interacting with 2
2 gets d from interacting with 1 and b from interacting with 2



fitness now depends on the relative abundance of each cell lineage

Multiple Myeloma

[Dingli et al, Brit J Cancer (2009]

a case study: Multiple Myeloma Bone Disease (MM)

Multiple Myeloma is a cancer of the plasma cells, a type of blood cell present in the bone marrow

MM affects about 750,000 people worldwide, & although quite a few treatments are available, it remains incurable.

average rate of survival ~3 years

[Berenson, *Curr Treat Options Onc*, 2001] [Kyle and Rajkumar, *N Eng J Med* 2004] [Harper and Weber, *Endoc Metab Clin North Am* 1998]

a case study: Multiple Myeloma Bone Disease (MM)

Health problems caused by multiple myeloma cells (MM cells) can affect our bones, immune system, kidney and red blood cells.
 associated effects: pain, bone loss & fractures (focal lesions & osteoporosis) and neurologic deficits.



[Berenson, *Curr Treat Options Onc*, 2001] [Kyle and Rajkumar, *N Eng J Med* 2004] [Harper and Weber, *Endoc Metab Clin North Am* 1998]

a case study: Multiple Myeloma Bone Disease (MM)

normal bone remodeling is a consequence of the dynamic balance between:



Osteoclasts (OC) Mediate bone resorption





Osteoblasts (OB) Mediate bone formation

[Roodman*, Blood Cells Mol Dis* 2004] [Terpos et al, *Blood* 2007]



Myeloma cells (MM) MM cells disrupt this dynamical equilibrium between OC and OB cells, favouring OC cells



normal bone remodeling



 $\begin{cases} \dot{x}_{OC} = x_{OC}(f_{OC}(\vec{x}) - \phi) \\ \dot{x}_{OB} = x_{OB}(f_{OB}(\vec{x}) - \phi) \end{cases}$

 $\phi = x_{OC} f_{OC} + x_{OB} f_{OB}$ $f_{OC}(\vec{x}) = x_{OC} \cdot 0 + x_{OB} \cdot a$ $f_{OB}(\vec{x}) = x_{OC} \cdot e + x_{OB} \cdot 0$



without the effects of MM-cells

$$f_{OC}(\vec{x}) = x_{OC} \cdot 0 + x_{OR} \cdot a + x_{MM} \cdot 0$$

$$f_{OB}(\vec{x}) = x_{OC} \cdot e + x_{OB} \cdot 0 + x_{MM} \cdot 0$$

$$f_{MM}(\vec{x}) = x_{OC} \cdot 0 + x_{OB} \cdot 0 + x_{MM} \cdot 0$$







[Roodman, *Blood Cells Mol Dis* 2004] [Roux & Mariette, *Leuk Lymphoma* 2004] [Dinarello, Ann Rev Imm 2009] [Croucher et al *Blood* 2001] [Choi et al J Clin Invest 2001]

Osteoclast cells (OC) produce growth factors (IL-6) which stimulate the growth of MM cells

$$f_{OC}(\vec{x}) = x_{OC} \cdot 0 + x_{OB} \cdot a + x_{MM} \cdot b$$

$$f_{OB}(\vec{x}) = x_{OC} \cdot e + x_{OB} \cdot 0 + x_{MM} \cdot 0$$

$$f_{MM}(\vec{x}) = x_{OC} \cdot c + x_{OB} \cdot 0 + x_{MM} \cdot 0$$



[Terpos et al*, Blood* 2007] [Roux & Mariette, *Leuk Lymphoma* 2004]

Myeloma cells (MM) inhibit the differentiation of Osteoblasts (OBs) (Dkk1, sFRP-2, etc.)

$$f_{OC}(\vec{x}) = x_{OC}.0 + x_{OB}.a + x_{MM}b$$

$$f_{OB}(\vec{x}) = x_{OC}.e + x_{OB}.0 + x_{MM}.-d$$

$$f_{MM}(\vec{x}) = x_{OC}.c + x_{OB}.0 + x_{MM}.0$$

Dickkopf-1: inhibits **OB**-activity MM RANKL Lkk1 MIP-1α s RP-2 IL-B OC

[Terpos et al, *Blood* 2007] [Roux & Mariette, *Leuk Lymphoma* 2004] [Qiang et al. *Bone* 2008] [Qiang et al. *Blood* 2008]

$$OC \quad OB \quad MM$$
$$OC \quad \begin{bmatrix} 0 & a & b \\ e & 0 & -d \\ MM & \begin{bmatrix} c & 0 & 0 \end{bmatrix}$$

$$f_{OC}(\vec{x}) = x_{OC}.0 + x_{OB}.a + x_{MM}b$$

$$f_{OB}(\vec{x}) = x_{OC}.e + x_{OB}.0 + x_{MM}.(-d)$$

$$f_{MM}(\vec{x}) = x_{OC}.c + x_{OB}.0 + x_{MM}.0$$



[Dingli et al, Brit J Cancer (2009]

this is mathematically equivalent to an ecosystem where species interactions are specified by the game matrix

 $f_{OC}(\vec{x}) = x_{OC} \cdot 0 + x_{OB} \cdot a + x_{MM} b$ $f_{OB}(\vec{x}) = x_{OC} \cdot e + x_{OB} \cdot 0 + x_{MM} \cdot (-d)$ $f_{MM}(\vec{x}) = x_{OC} \cdot c + x_{OB} \cdot 0 + x_{MM} \cdot 0$

[Dingli et al, Brit J Cancer (2009]

disease evolution (math)

	<i>OC</i>	OE	B MN	Л
OC	$\begin{bmatrix} 0 \end{bmatrix}$	a	b	
$A_{ij} = OB$	e	0	-d	
MM	C	0	0	
	_		_	

$$\dot{x}_i(t) = x_i(t) [f_i(x_1, x_2, x_3) - \phi]$$

$$f_i(x_1, x_2, x_3) = \sum_{k=1}^3 A_{ik} x_k$$
$$\phi = \sum_{i=1}^3 \sum_{k=1}^3 x_i A_{ik} x_k$$

the nature of the fixed points of the evolutionary dynamics (though not their location) remains unaffected under a projective transformation of the relative cell
 frequencies

disease evolution (math)

$$B_{ij} = \frac{A_{ij}}{\eta_j} \quad \eta = (e, a, be/c)$$

$$OC \quad OB \quad MM$$

$$OC \quad \begin{bmatrix} 0 & a & b \\ e & 0 & -d \\ c & 0 & 0 \end{bmatrix}$$

$$I = OC \quad OC \quad OB \quad MM$$

$$B_{ij} = OC \quad \begin{bmatrix} 0C & OB & MM \\ 0 & 1 & c/e \\ 1 & 0 & -dc/be \\ c/e & 0 & 0 \end{bmatrix}$$

 the nature of the fixed points of the evolutionary dynamics (though not their location) remains unaffected under a projective transformation of the relative cell frequencies

disease evolution (math)

$$B_{ij} = \frac{A_{ij}}{\eta_j} \quad \eta = (e, a, be/c)$$

 $OC \quad OB \quad MM$ $OC \quad \begin{bmatrix} 0 & a & b \\ a & b \end{bmatrix}$ $A_{ij} = OB \quad \begin{bmatrix} e & 0 & -d \\ c & 0 & 0 \end{bmatrix}$

$$B_{ij} = \begin{array}{ccc} OC & OB & MM \\ OC & \left[\begin{array}{ccc} 0 & 1 & \beta \\ 1 & 0 & -\delta \\ MM & \beta & 0 & 0 \end{array} \right]$$

the nature of the fixed points of the evolutionary dynamics (though not their location) remains unaffected under a projective transformation of the relative cell frequencies

disease evolution (math & biology)



$$B_{ij} = \begin{array}{ccc} OC & OB & MM \\ OC & \left[\begin{array}{ccc} 0 & 1 & \beta \\ 1 & 0 & -\delta \\ MM & \beta & 0 & 0 \end{array} \right]$$

 δ measures the (net) negative impact on OB cells by MM cells

 β measures the synergistic effect between MM and OC cells

 a symmetric feedback OC ← → OB (=1) positions the equilibrium
 associated with normal physiology at x_{OC} = x_{OB} =0.5

Fixed points of the disease dynamics

fixed points (x_{oc}*,x_{OB}*,x_{MM}*) of the evolutionary dynamics under the reduced matrix :

- (0,1,0) and (1,0,0) are *unstable* fixed points
 (¹/₂,¹/₂,0) associated with a healthy physiology is *unstable* whenever β >1, being *stable* otherwise
- ($\frac{1}{2}$,0, $\frac{1}{2}$) is *stable* whenever $\beta > 1$ or whenever $\beta < 1$ and $\beta + \delta > 1$
- In the latter case, there is an internal saddle point located at

$$q^* = \left(\frac{\delta}{1+\delta+\beta(\delta+\beta-2)}, \frac{\beta(\delta+\beta-1)}{1+\delta+\beta(\delta+\beta-2)}, \frac{1-\beta}{1+\delta+\beta(\delta+\beta-2)}\right)$$



Fixed points of the disease dynamics

fixed points (x_{oc}*,x_{oB}*,x_{MM}*) of the evolutionary dynamics under the reduced matrix :

- (0,1,0) and (1,0,0) are *unstable* fixed points
 (¹/₂,¹/₂,0) associated with a healthy physiology is *unstable* whenever β >1, being *stable* otherwise
- ($\frac{1}{2}$,0, $\frac{1}{2}$) is *stable* whenever $\beta > 1$ or whenever $\beta < 1$ and $\beta + \delta > 1$
- In the latter case, there is an internal saddle point located at

$$q^{*} = \left(\frac{\delta}{1+\delta+\beta(\delta+\beta-2)}, \frac{\beta(\delta+\beta-1)}{1+\delta+\beta(\delta+\beta-2)}, \frac{1-\beta}{1+\delta+\beta(\delta+\beta-2)}\right)$$



possible dynamical scenarios under pathological conditions



possible dynamical scenarios under pathological conditions case 2 OC β <1 and β + δ >1 Stable Saddle Unstable $\beta = 1/2$ $\delta = 1$ OC OB MM MM OB negative -δ

possible dynamical scenarios under pathological conditions



possible dynamical scenarios under pathological conditions

(ex: bisphosphonates, MIP- α , IL-6) can lead the dynamics to a healthy state.

(ex: Dkk1) (ex: Dkk1) (ex: Dkk1) (b) (c) (



Case 3







$\beta > 1$

various studies suggest that
 β <1 is the exception rather than
 the norm [Roodman, 2002] & [Epstein, 2003]

δ has an impact on the time associated with disease progression

In the second stress of the second st

large δ mimics common
 myeloma-induced osteoporosis
 without large MM cell burden



the era of individualized medicine

genetic differences in myeloma cells
 normal physiology varies from patient to patient

characterizing host-specific disease progression

OC OB MM $\begin{bmatrix} 0 & a & b \end{bmatrix}$ OC $e \quad 0 \quad -d$ OB | 0 С MM 0



conclusions

employing the principles of EGT we managed to describe the core features of MM using 2 parameters.

therapies that kill MM cells can slow down the disease progression and improve bone structure (via chemo-therapy and stem cell transplantation).
 yet, the disease invariably relapses.

> [Dingli, Chalub, Santos, Segbroeck, Pacheco, British Journal of Cancer 101 1130-1136 (2009)]

conclusions

Solution in a mouse MM (an agent that contributes to β) blocked bone destruction in a mouse MM (Choi et al, *J Clin Invest* 2001).

in humans, Lust et al, Mayo Clin Proc 2009 showed that therapies which reduce one of the factors included in β (IL-1 β) slows down the progression of the disease.

Similarly, therapies that reduce δ may attenuate morbidity by slowing the speed of bone loss. This has also been tested by means of therapies against Dkk-1 (an agent that contributes to δ) (Yaccoby et al, *Blood* 2007) a common take-home message regarding the war on cancer

instead of trying to kill every cancer cell . . .



a common take-home message regarding the war on cancer

instead of trying to kill every cancer cell . . .





therapies should aim at reducing the fitness of malignant cells, allowing natural selection to eradicate cancer cells

