

# All about the Triplet

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- Introduction
- Increasing the Higgs mass w/o fine-tuning
- The Georgi-Machacek model, solving the T-parameter: susy breaking and dark matter.
- Conclusions

# Introduction

- The run I of the LHC has discovered the last building block of the SM: The Higgs
- Its properties are compatible with the ones of the SM: minimal realization of the Higgs potential
- But an extended Higgs sector is not yet excluded and can have different and interesting signatures.

- One way of deviating from the minimal model is to include extra Higgses:
  - More doublets
  - singlets
  - Triplets
  - .....

- These extra fields could appear in a UV completion of the model and could remain light by the same mechanism as the SM Higgs
  - Pseudo-goldstone boson
  - Supersymmetry

- In this talk I am going to explore different aspects of an extended Higgs sector with triplets in a supersymmetric model.
- In general there are two possible triplets that could mix with the Higgs,  $Y=0$  and  $Y=1$ .
- The kind of couplings are:

$$W = \lambda_0 H_u T_0 H_d + \lambda_{+1} H_d T_{+1} H_d + \lambda_{-1} H_u T_{-1} H_u$$

- In principle the triplet will get a vev once EWSB occurs and can lead to a dangerous contribution to the T-parameter
- I will either make sure that the vev of the triplet component is small or implement a symmetry to avoid contributions to the T-parameter.

# Increasing the Higgs mass w/o fine tuning

C. Alvarado, AD, A. Martin, B. Ostdiek

- One of the properties of adding an extended Higgs sector in supersymmetry is that one can deviate from the usual formula:

$$m_h^2 \leq m_z^2$$

- Unfortunately one has to pay a price in fine tuning, in order to maximize the new contribution one has to decouple non-supersymmetrically the new states.

- One way to avoid the fine-tuning is to double the fields, to couple one to the Higgs and decouple the other one:

$$W = \mu H_u \cdot H_d + \mu_\Sigma \text{Tr}(\Sigma_1 \cdot \Sigma_2) + W_{H-\Sigma} + W_{\text{Yukawa}}$$

- This trick was previously exploited for the case of singlets [arXiv:1308.0792](https://arxiv.org/abs/1308.0792)
- We will use triplets for a different dependence on  $\tan \beta$



- In the case of  $Y=0$  the effect is similar than the singlet.
- On the other hand for the case of  $Y=1$  the two fields are already needed to cancel anomalies
- I will couple one of the two triplets to the Higgses and the other one will be inert:

$$W_{H-\Sigma} = \lambda H_u \cdot \Sigma_1 H_u$$

- We can write the potential in the following way:

$$\Sigma_1 = \begin{pmatrix} T^-/\sqrt{2} & -T^0 \\ T^{--} & -T^-/\sqrt{2} \end{pmatrix}$$

$$\Sigma_2 = \begin{pmatrix} \chi^+/\sqrt{2} & -\chi^{++} \\ \chi^0 & -\chi^+/\sqrt{2} \end{pmatrix}$$

$$\begin{aligned} V_{\text{neutral}} = & m_{H_u}^2 |H_u|^2 + m_{H_d}^2 |H_d|^2 + m_\chi^2 |\chi^0|^2 + m_T^2 |T^0|^2 \\ & + |2\lambda H_u^0 T^0 + \mu H_d^0|^2 + |\mu H_u^0|^2 + |\mu_\Sigma T^0|^2 + |\mu_\Sigma \chi^0 + \lambda H_u^0 H_u^0|^2 \\ & + \frac{g^2 + g'^2}{8} (H_d^0 H_d^{0*} - H_u^0 H_u^{0*} + 2T^0 T^{0*} - 2\chi^0 \chi^{0*})^2 \\ & + (-\lambda A_\lambda H_u^0 H_u^0 T^0 - \mu B_\mu H_d^0 H_u^0 - \mu_\Sigma B_\Sigma T^0 \chi^0 + \text{h.c.}) \end{aligned}$$

- Upon integration of the triplets and going to the decoupling limit one gets the following mass for the Higgs (SM-like):

$$m_h^2 = m_Z^2 \cos^2(2\beta) + (\text{stop loops}) + 4v^2 \lambda^2 \sin^4(\beta) \left( \frac{m_\chi^2}{\mu_\Sigma^2 + m_\chi^2} \right) - \frac{v^2 \lambda^2 \sin^2(2\beta)}{\mu_\Sigma^2 + m_T^2} |2\mu^* - A_\lambda \tan(\beta)|^2.$$

- Problems:

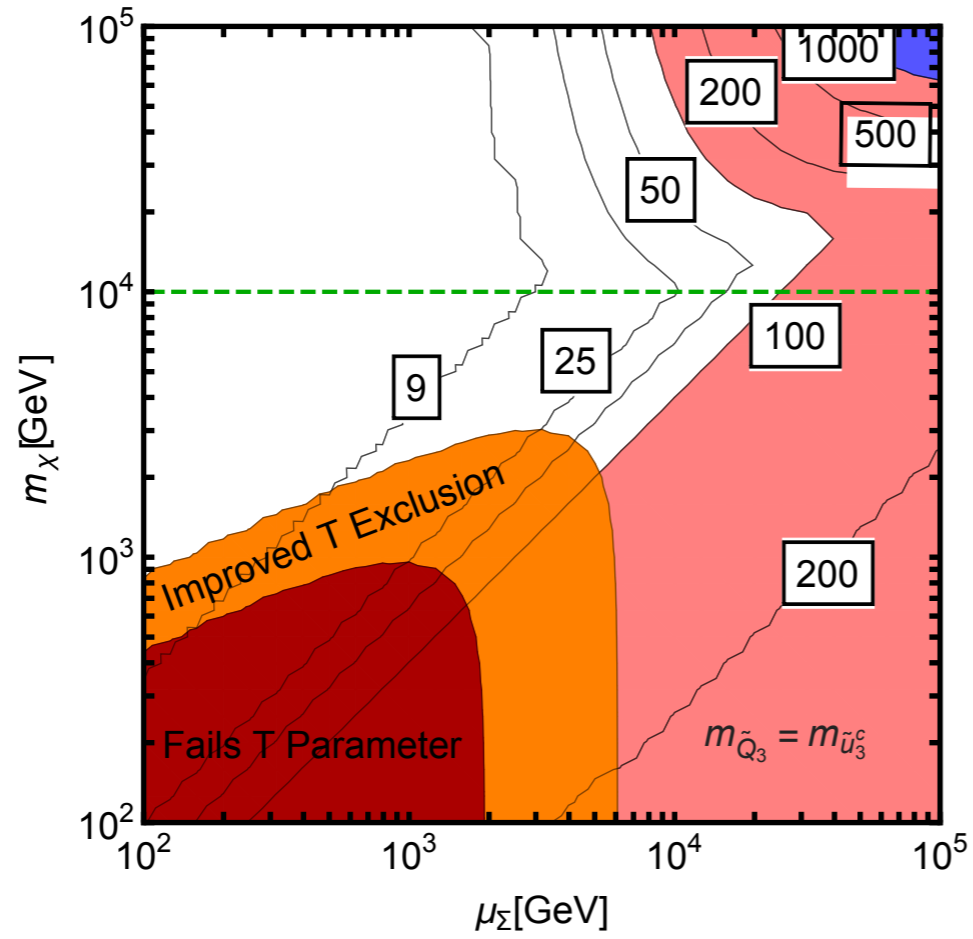
- Fine-tuning:

$$\Delta = \frac{2}{m_h^2} \max \left( m_{H_u}^2, m_{H_d}^2, \frac{dm_{H_u}^2}{d \log(u)} L, \frac{dm_{H_d}^2}{d \log(u)} L, \delta m_{H_u^0}^2, \mu B_{\mu, \text{eff}} \right)$$

- T-parameter:

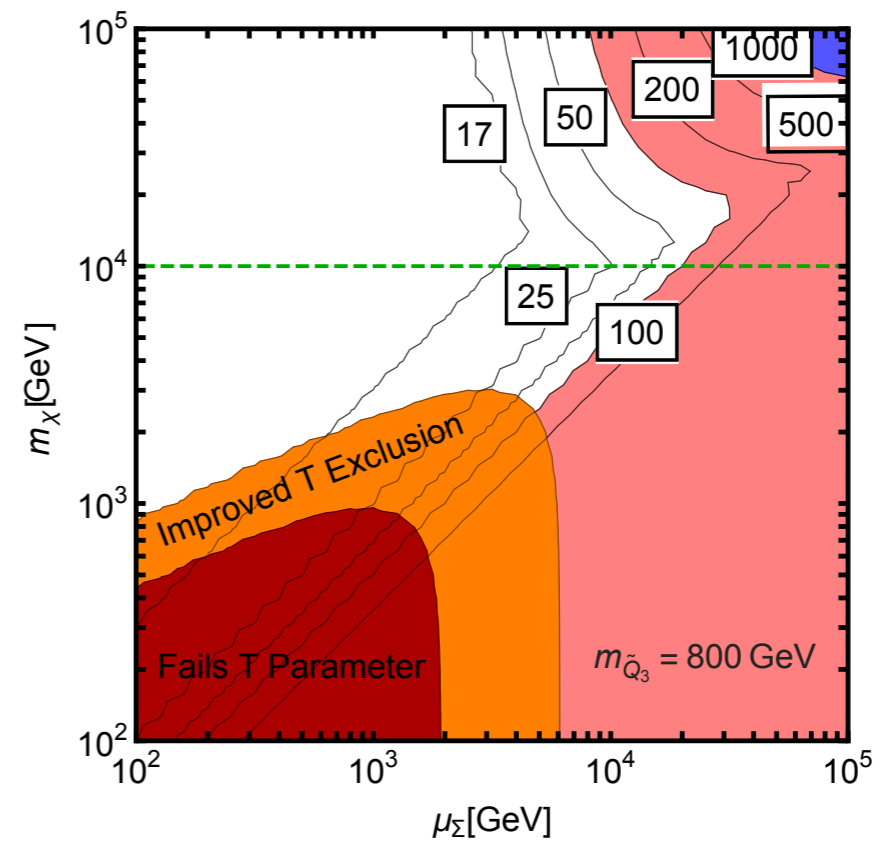
$$\langle T^0 \rangle_{Y=-1} \approx -\frac{v^2 \lambda \sin(2\beta) (2\mu^* - A_\lambda \tan(\beta))}{2(\mu_\Sigma^2 + m_T^2)} \quad \text{and} \quad \langle \chi^0 \rangle_{Y=1} \approx v^2 \frac{-\lambda \mu_\Sigma \sin^2(\beta)}{\mu_\Sigma^2 + m_\chi^2}$$

Fine Tuning of  $m_h^2$



$$m_T = 800 \text{ TeV} \quad \lambda = 0.25$$

Fine Tuning of  $m_h^2$



- This model also changes the different decays channels since there are more states.
- Specially having more charginos can lead to distinct patterns of decays of stops
- The main drawback are the bounds that come from the T-parameter

# The (SUSY)-Georgi-Machacek model: SUSY breaking and DM

- The GM model was proposed to ensure a custodial structure with triplets.
- It was supersymmetrized in [arXiv:1308.4025](https://arxiv.org/abs/1308.4025)

$$\bar{H} = \begin{pmatrix} H_1 \\ H_2 \end{pmatrix}, \quad \bar{\Delta} = \begin{pmatrix} -\frac{\Sigma_0}{\sqrt{2}} & -\Sigma_{-1} \\ -\Sigma_1 & \frac{\Sigma_0}{\sqrt{2}} \end{pmatrix}$$

$$W_0 = \lambda \bar{H} \cdot \bar{\Delta} \bar{H} + \frac{\lambda_3}{3} \text{tr} \bar{\Delta}^3 + \frac{\mu}{2} \bar{H} \cdot \bar{H} + \frac{\mu_\Delta}{2} \text{tr} \bar{\Delta}^2 + h_t \bar{Q}_L \cdot H_2 t_R + h_b \bar{Q}_L \cdot H_1 b_R$$

- RGE evolution, yukawa and U(1) break the custodial limit and generate a non-zero  $\rho$  so in general:

$$W = -\lambda_a H_1 \cdot \Sigma_1 H_1 + \lambda_b H_2 \cdot \Sigma_{-1} H_2 + \sqrt{2}\lambda_c H_1 \cdot \Sigma_0 H_2 + \sqrt{2}\lambda_3 \text{tr} \Sigma_1 \Sigma_0 \Sigma_{-1} \\ - \mu H_1 \cdot H_2 + \frac{\mu_{\Delta_a}}{2} \text{tr} \Sigma_0^2 + \mu_{\Delta_b} \text{tr} \Sigma_1 \Sigma_{-1} + h_t \bar{Q}_L \cdot H_2 t_R + h_b \bar{Q}_L \cdot H_1 b_R$$

$$V_{\text{SOFT}} = m_{H_1}^2 H_1^\dagger H_1 + m_{H_2}^2 H_2^\dagger H_2 + m_{\Sigma_0}^2 \Sigma_0^\dagger \Sigma_0 + m_{\Sigma_1}^2 \Sigma_1^\dagger \Sigma_1 + m_{\Sigma_{-1}}^2 \Sigma_{-1}^\dagger \Sigma_{-1} - m_3^2 H_1 \cdot H_2 \\ + \left\{ \frac{B_{\Delta_a}}{2} \text{tr} \Sigma_0^2 + B_{\Delta_b} \text{tr} \Sigma_1 \Sigma_{-1} - A_{\lambda_a} H_1 \cdot \Sigma_1 H_1 + A_{\lambda_b} H_2 \cdot \Sigma_{-2} H_2 \right. \\ \left. + \sqrt{2} A_{\lambda_c} H_1 \cdot \Sigma_0 H_2 + \sqrt{2} A_{\lambda_3} \text{tr} \Sigma_1 \Sigma_0 \Sigma_{-1} + a_t \tilde{Q}_L \cdot H_2 \tilde{t}_R + a_b \tilde{Q}_L \cdot H_1 \tilde{b}_R + h.c. \right\}$$



- I am going to embed this model into a predictive scenario of SUSY breaking like GMSB to see the deviation from the custodial limit:

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$$W = \left( \tilde{\lambda}_8^{ij} X + \mathcal{M}_8^{ij} \right) \Phi_{8i} \Phi_{8j} + \left( \tilde{\lambda}_3^{ij} X + \mathcal{M}_3^{ij} \right) \Phi_{3i} \Phi_{3j} + \left( \tilde{\lambda}_1^{ij} X + \mathcal{M}_1^{ij} \right) \bar{\Phi}_{1i} \Phi_{1j}$$

$$M_3 = \frac{\alpha_3(\mathcal{M})}{4\pi} 3n_8 g(\Lambda_8/\mathcal{M}) \Lambda_8,$$

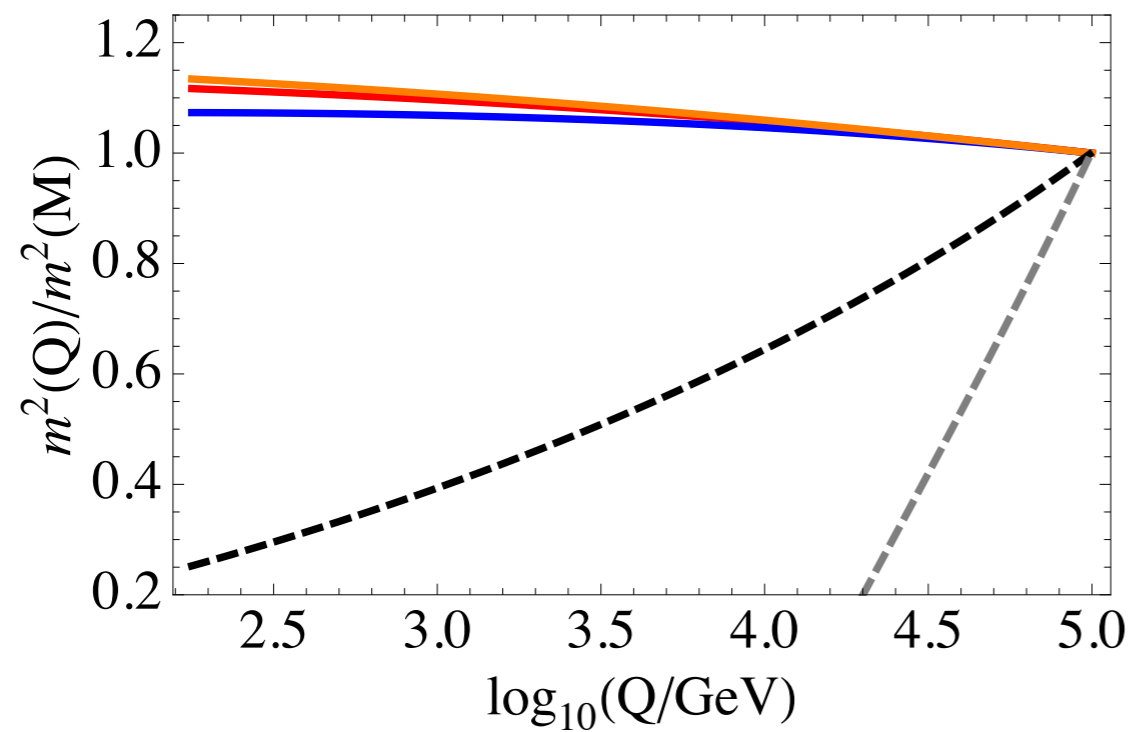
$$M_2 = \frac{\alpha_2(\mathcal{M})}{4\pi} 2n_3 g(\Lambda_3/\mathcal{M}) \Lambda_3,$$

$$M_1 = \frac{\alpha_1(\mathcal{M})}{4\pi} \frac{6}{5} n_1 g(\Lambda_1/\mathcal{M}) \Lambda_1,$$

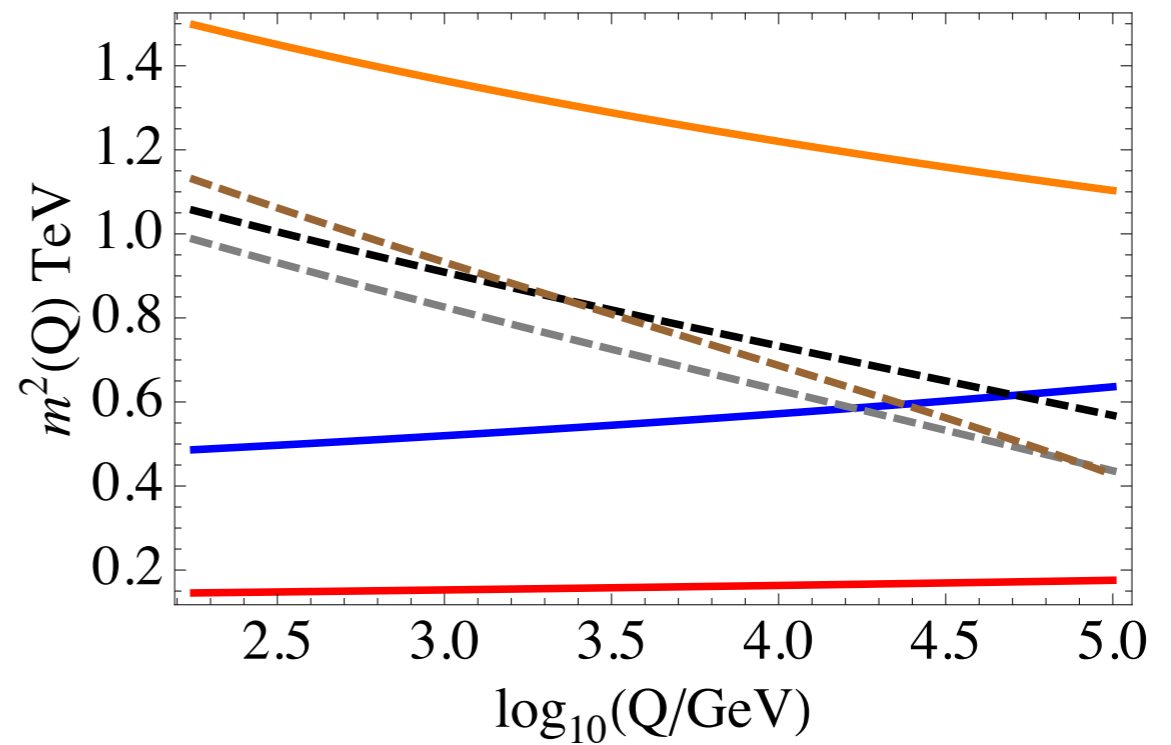
$$m_{\tilde{f}}^2 = 2 \left[ C_3^f \left( \frac{\alpha_3(\mathcal{M})}{4\pi} \right)^2 3n_8 f(\Lambda_8/\mathcal{M}) \Lambda_8^2 + C_2^f \left( \frac{\alpha_2(\mathcal{M})}{4\pi} \right)^2 2n_3 f(\Lambda_3/\mathcal{M}) \Lambda_3^2 \right. \\ \left. + C_1^f \left( \frac{\alpha_1(\mathcal{M})}{4\pi} \right)^2 \frac{1}{2} \left( \frac{6}{5} \right)^2 n_1 f(\Lambda_1/\mathcal{M}) \Lambda_1^2 \right].$$

- The spectrum is generated at a high scale  $M$
- Run down to the EW scale
- EWSB it is imposed
- $m_h = 125 \text{ GeV}$
- All experimental constrains (direct & indirect) are satisfied

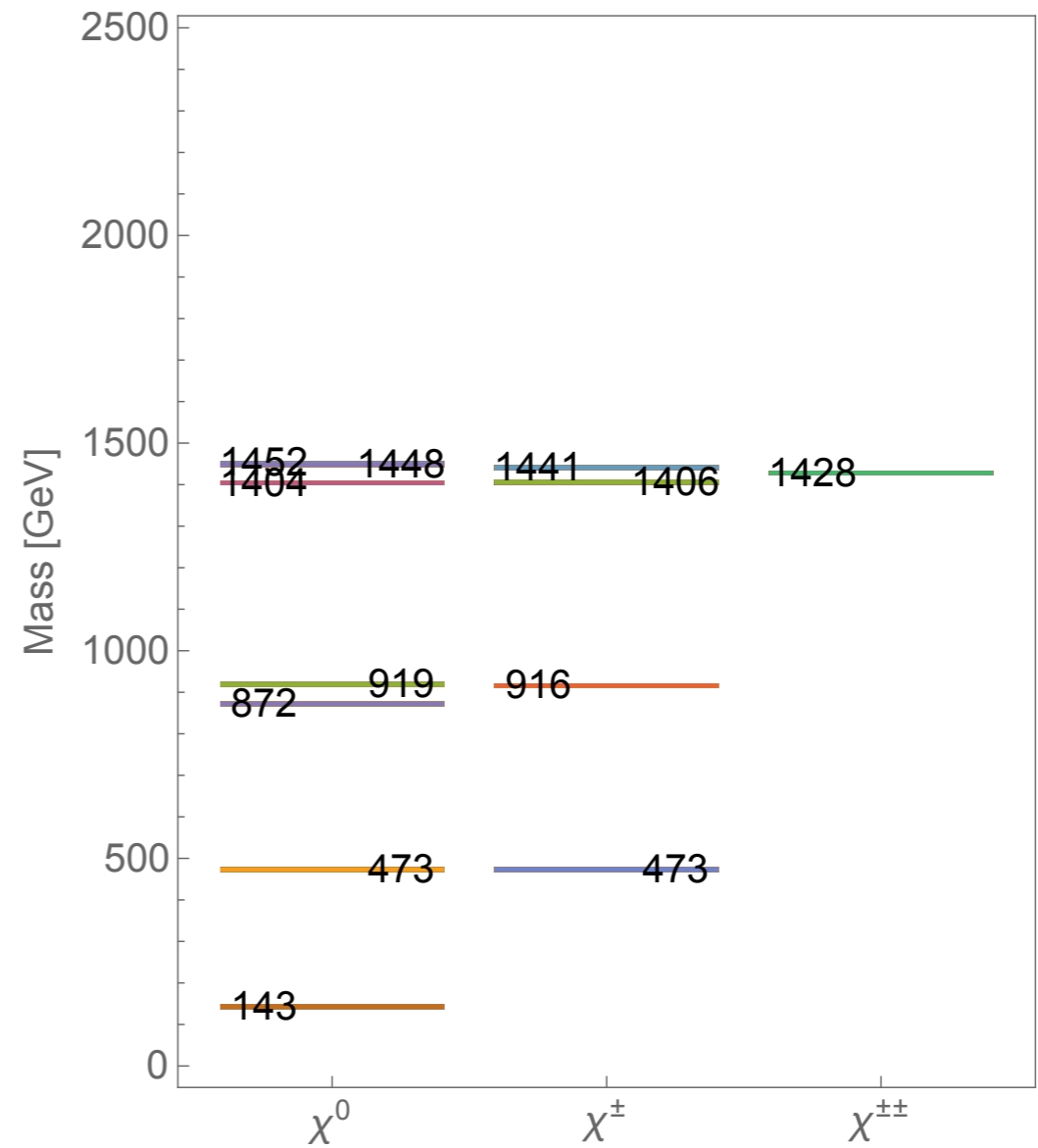
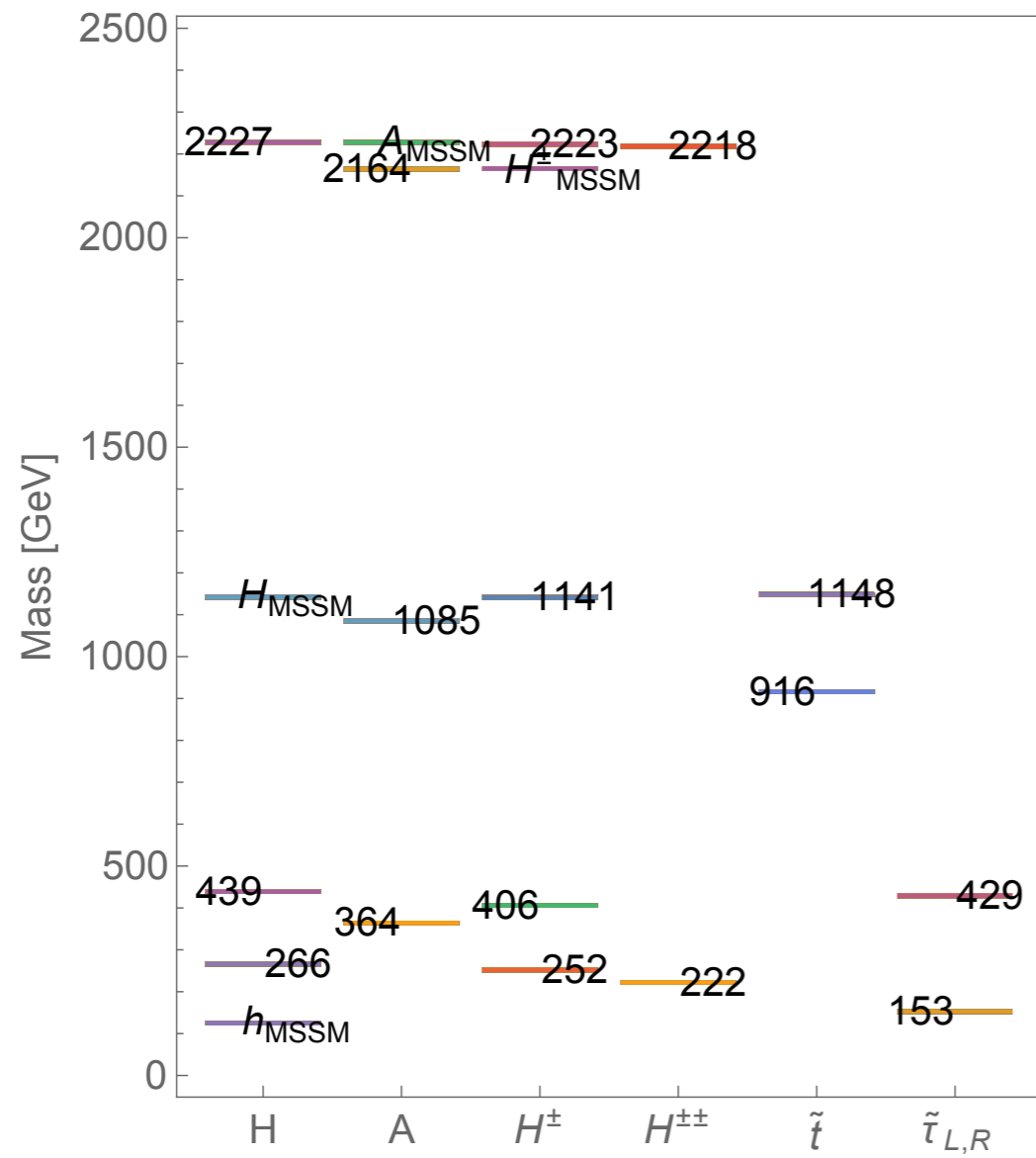
$$n_1 = 1, n_3 = 2, n_8 = 6 \quad \text{and} \quad \tilde{\lambda}_1 = 0.9, \tilde{\lambda}_3 = 0.5, \tilde{\lambda}_8 = 0.1.$$



Higgses



squarks & gauginos



$\tan \beta = 1.38$

- There are deviations on Higgs properties and exotic decays like:

$$H^\pm \rightarrow W^\pm Z$$

Scenario #1	$WW$	$ZZ$	$b\bar{b}$	$t\bar{t}$	$\gamma\gamma$
$r_{hXX}$	1.05	1.04	1.01	1.01	1.22
$\mu_{hXX}^{(gF)}, \mu_{hXX}^{(htt)}$	1.07	1.05	1	0.99	1.45
$\mu_{hXX}^{(WF)}, \mu_{hXX}^{(Wh)}$	1.16	1.14	1.08	1.07	1.58
$\mu_{hXX}^{(ZF)}, \mu_{hXX}^{(Zh)}$	1.14	1.11	1.06	1.05	1.54

# How about DM?

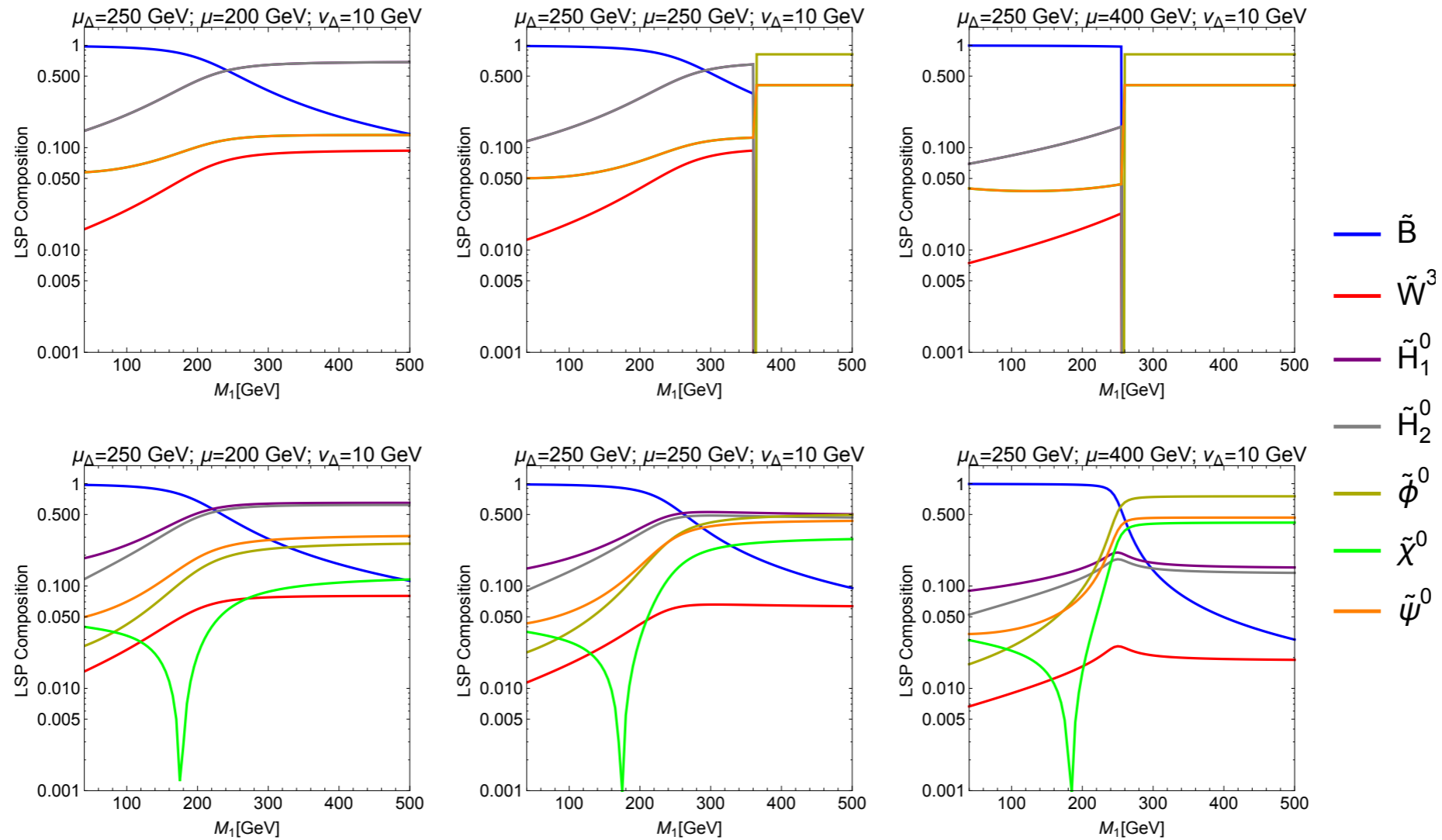
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- Having extra fermionic states can have an impact in the composition and properties of the LSP
- I am going to present different cases where the relic abundance is obtained
- NB: I am deviating from GMSB. i.e. the gravitino is not the LSP!!!!!! (thanks to E. Pontón)

$$\mathbf{M} = \begin{pmatrix} M_1 & 0 & -\frac{1}{\sqrt{2}}g'c_\beta v_H & \frac{\sqrt{2}}{2}g's_\beta v_H & 0 & -g'v_\Delta & g'v_\Delta \\ 0 & M_2 & \frac{\sqrt{2}}{2}g_2c_\beta v_H & -\frac{1}{\sqrt{2}}g_2s_\beta v_H & 0 & g_2v_\Delta & -g_2v_\Delta \\ -\frac{1}{\sqrt{2}}g'c_\beta v_H & \frac{1}{\sqrt{2}}g_2c_\beta v_H & -\sqrt{2}\lambda v_\Delta & -\frac{1}{\sqrt{2}}\lambda v_\Delta - \mu & -\lambda s_\beta v_H & 0 & -2\lambda c_\beta v_H \\ \frac{\sqrt{2}}{2}g's_\beta v_H & -\frac{1}{\sqrt{2}}g_2s_\beta v_H & -\frac{1}{\sqrt{2}}\lambda v_\Delta - \mu & -\sqrt{2}\lambda v_\Delta & -\lambda c_\beta v_H & -2\lambda s_\beta v_H & 0 \\ 0 & 0 & -\lambda s_\beta v_H & \lambda c_\beta v_H & \mu_\Delta & -\frac{1}{\sqrt{2}}\lambda_3 v_\Delta & -\frac{1}{\sqrt{2}}\lambda_3 v_\Delta \\ g'v_\Delta & g_2v_\Delta & 0 & -2\lambda s_\beta v_H & -\frac{1}{\sqrt{2}}\lambda_3 v_\Delta & 0 & \mu_\Delta - \frac{1}{\sqrt{2}}\lambda v_\Delta \\ g'v_\Delta & -g_2v_\Delta & -2\lambda c_\beta v_H & 0 & -\frac{1}{\sqrt{2}}\lambda_3 v_\Delta & \mu_\Delta - \frac{1}{\sqrt{2}}\lambda_3 v_\Delta & 0 \end{pmatrix}$$

Neutralino Mass-Matrix

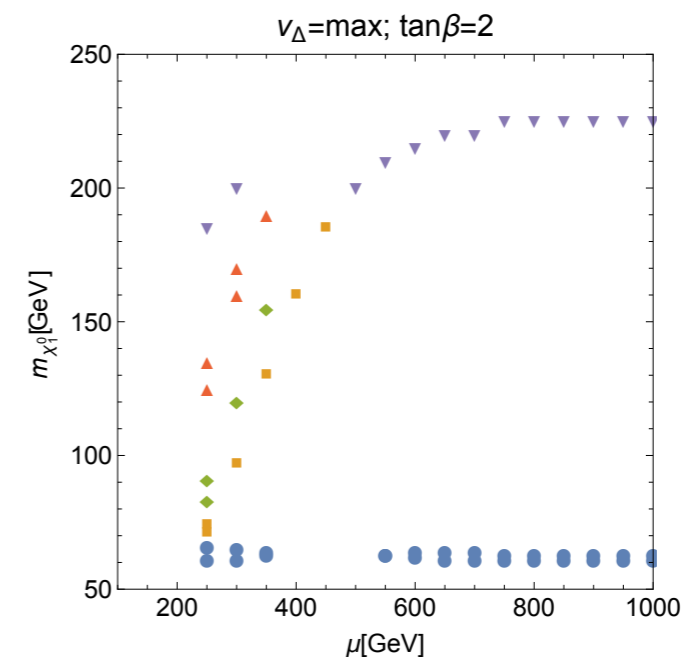
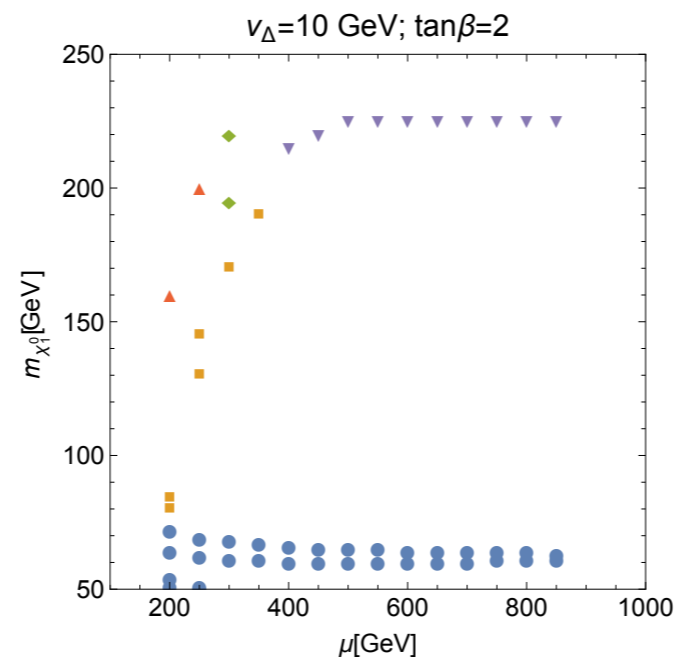
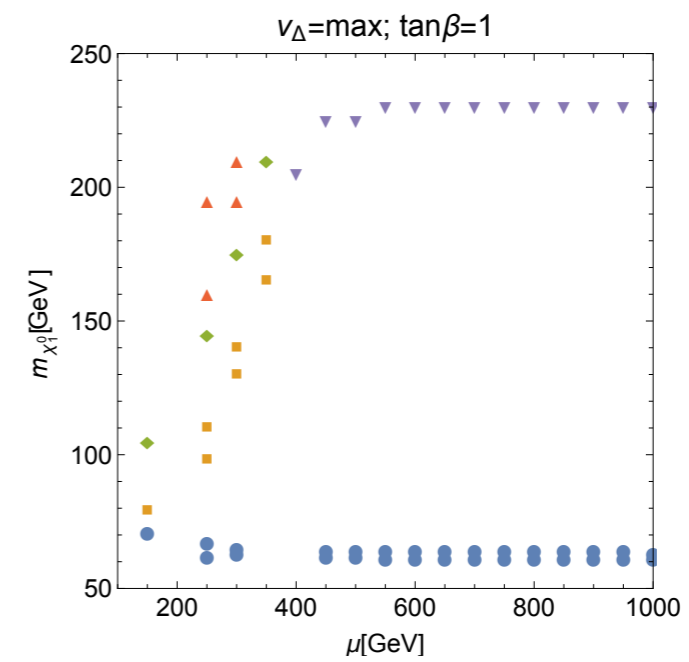
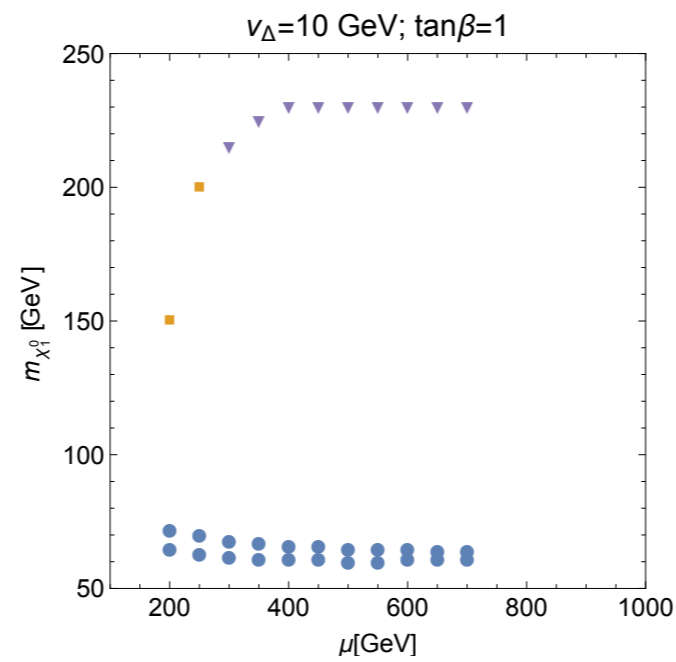
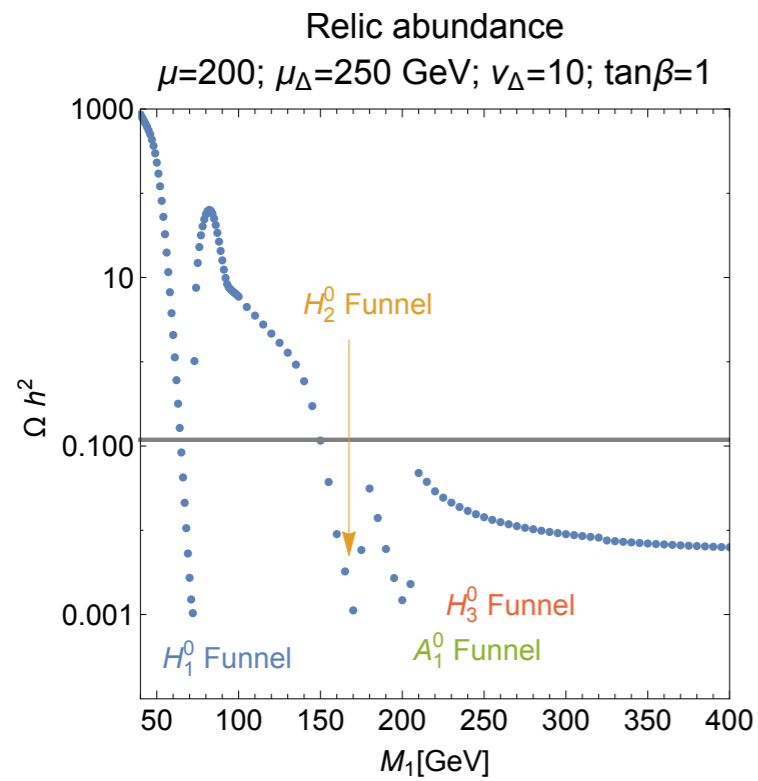
# Composition of the LSP



$M_2 = 1 \text{ TeV}$

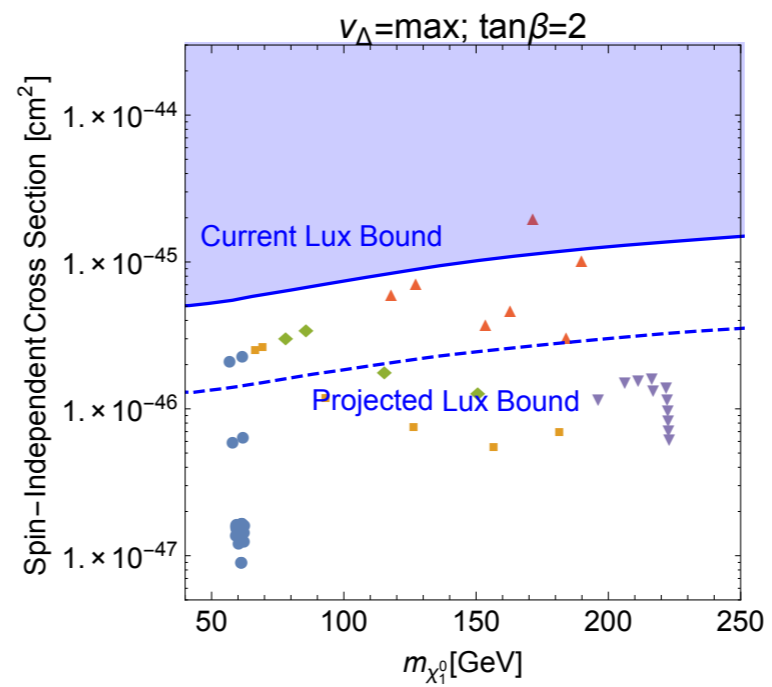
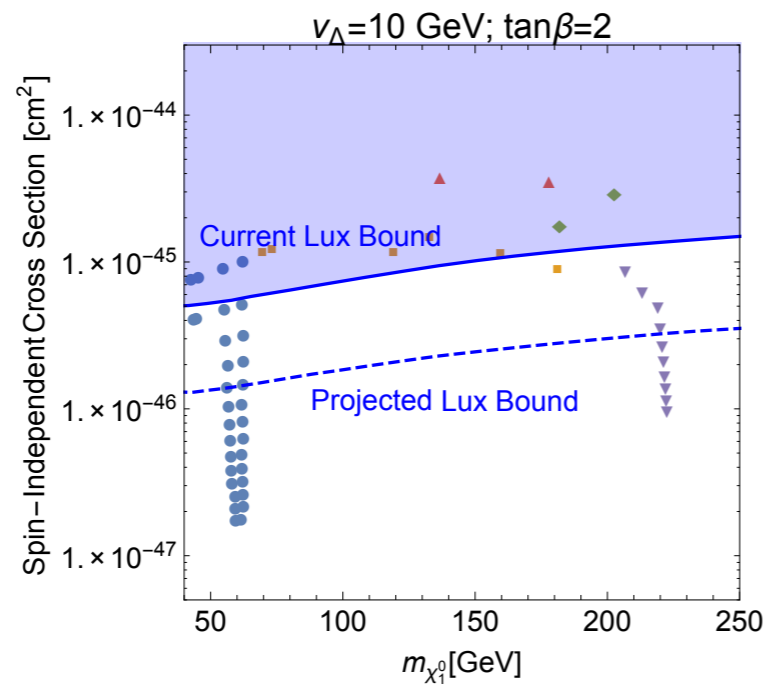
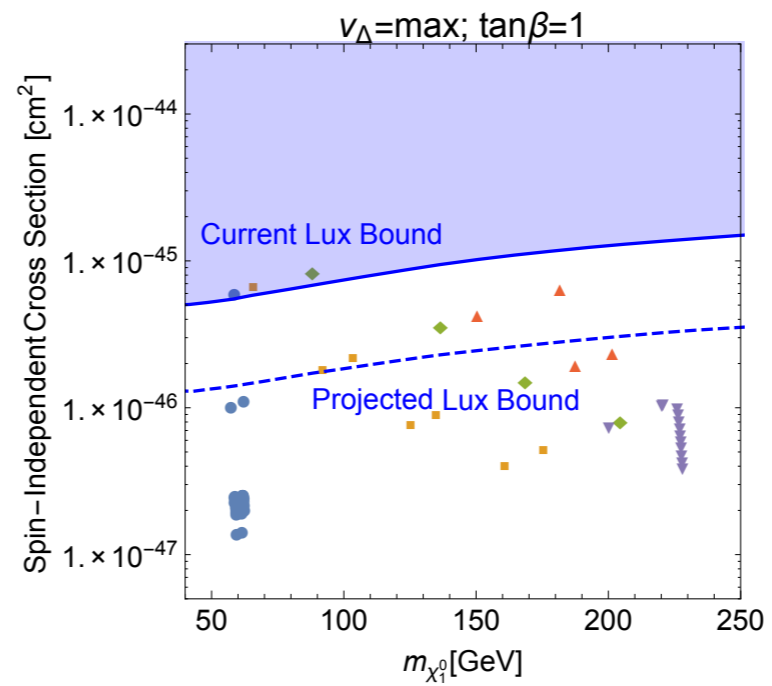
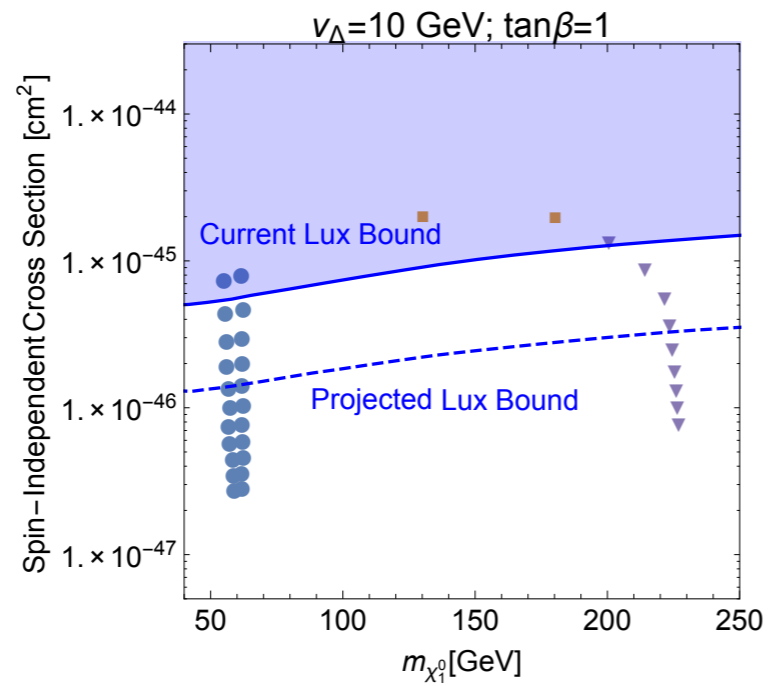


# Relic Abundance



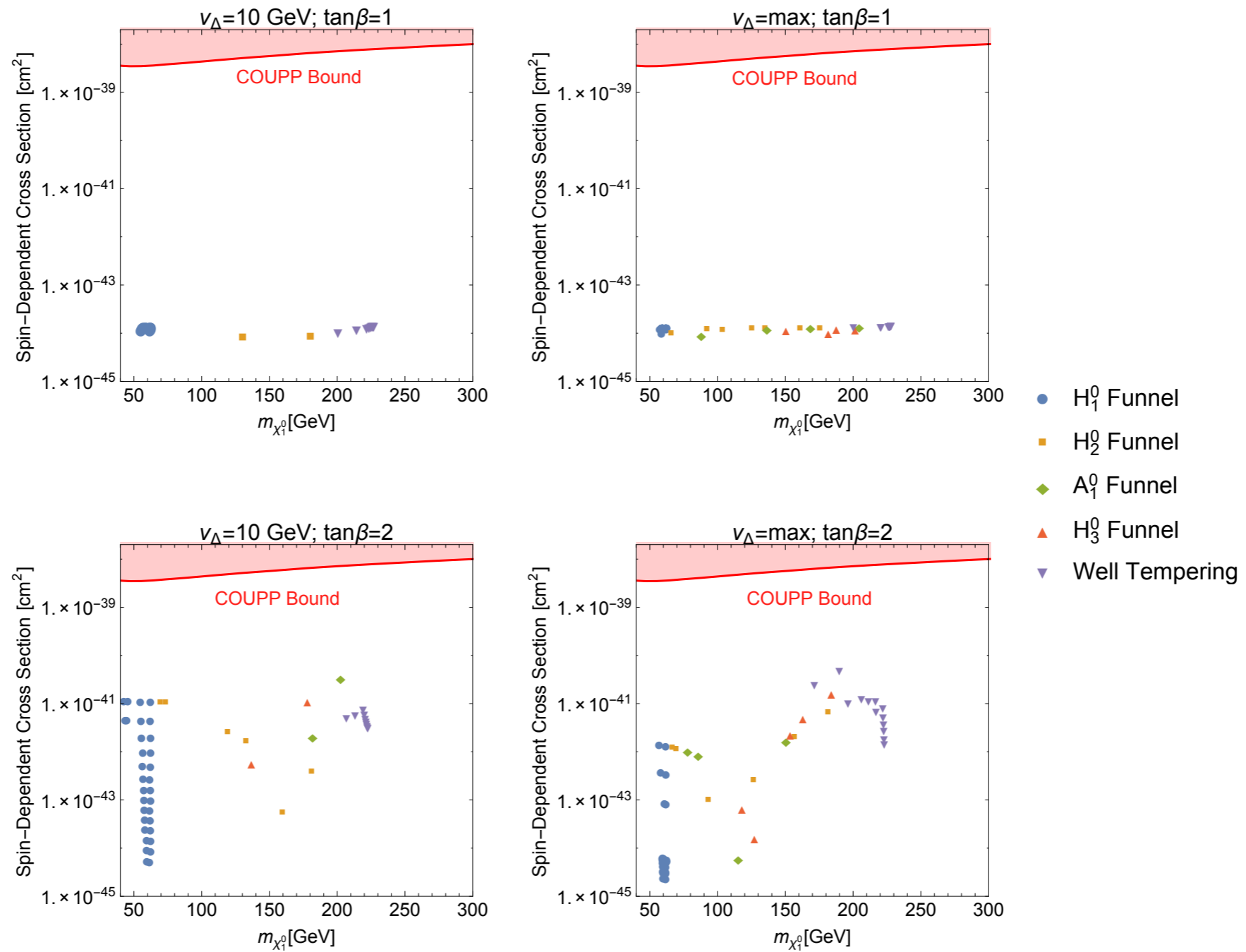
- $H_1^0$  Funnel
- $H_2^0$  Funnel
- ◆  $A_1^0$  Funnel
- ▲  $H_3^0$  Funnel
- ▼ Well Tempering

# Spin independent xsec

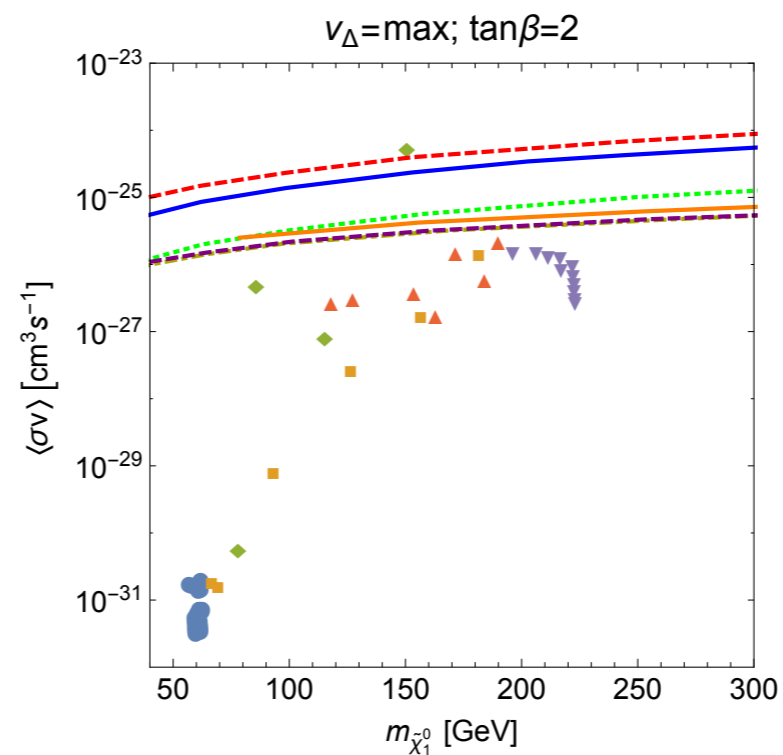
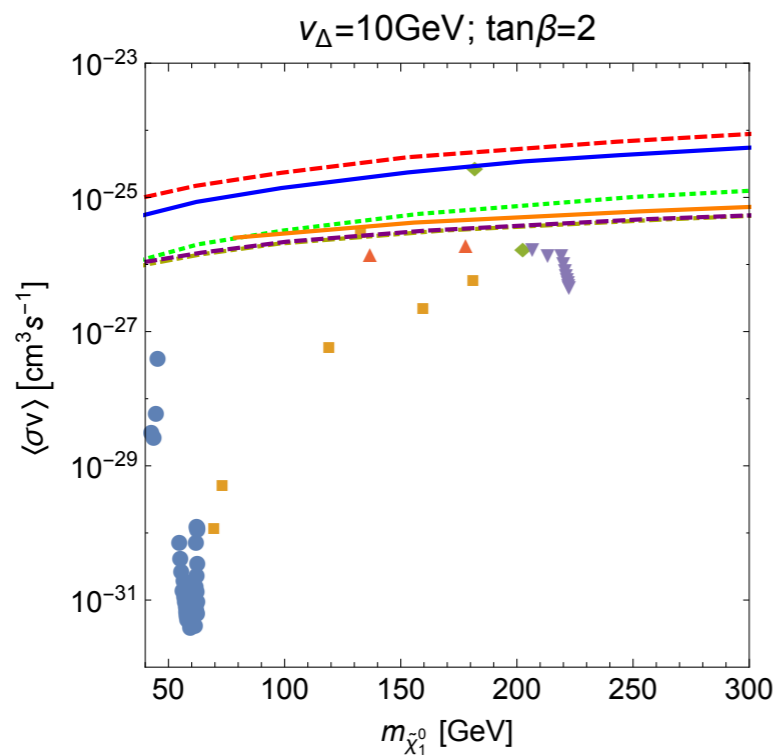
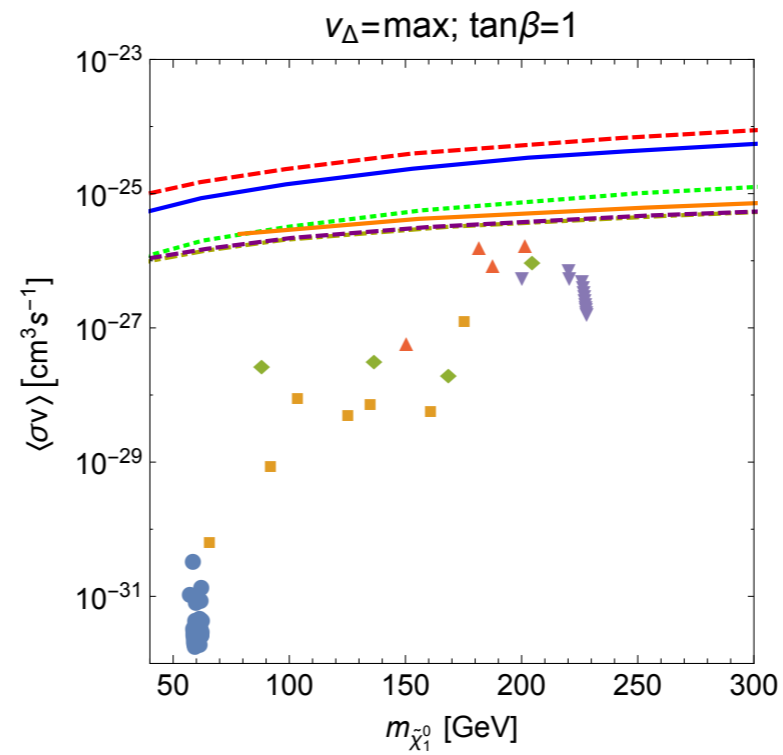
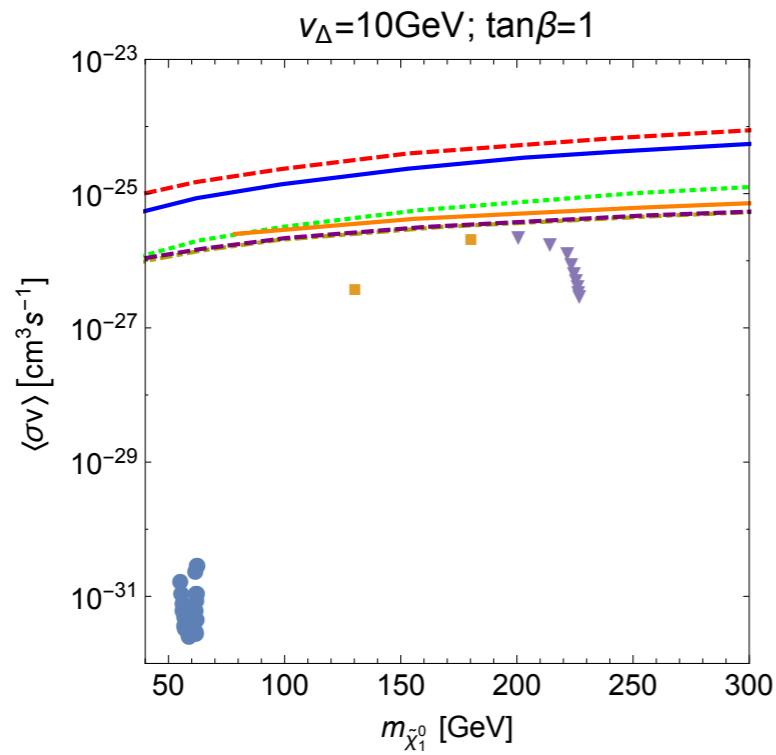


- $H_1^0$  Funnel
- $H_2^0$  Funnel
- ◆  $A_1^0$  Funnel
- ▲  $H_3^0$  Funnel
- ▼ Well Tempering

# Spin dependent xsec



# Indirect detection



- $H_1^0$  Funnel
  - $H_2^0$  Funnel
  - ◆  $A_1^0$  Funnel
  - ▲  $H_3^0$  Funnel
  - ▼ Well Tempering
- 
- $e^+e^-$
  - -  $\mu^+\mu^-$
  - · -  $\tau^+\tau^-$
  - · -  $u\bar{u}$
  - · -  $b\bar{b}$
  - $W^+W^-$

# Conclusions

- One of the multiple possibilities for physics beyond the SM is an extended Higgs sector
- Extra scalars appear naturally in UV theories attempting to explain the Hierarchy problem
- In this talk I have supposed that supersymmetry is the explanation of the EW scale and moreover that there are triplets coupled to the usual Higgses.

- I have studied the reduction of fine tuning in the case where there is only a triplet of  $Y=1$ .
- Indeed one can find regions of the parameter space where there is sensibly much less tuning and the phenomenology of stops can be greatly changed.
- The main drawback is that one has to be careful about contributions to the T-parameter.

- One way to automatically have the T-parameter under control is the GM model.
- I have introduced the SCTM and study how can it be embedded into GMSB
- It naturally leads to a low messenger scale
- But one can successfully have a complete model with low  $\tan \beta$

- Finally I have analyzed the implications that having an extended sector of neutralinos on DM.
- New regions appear that can have very interesting implications for direct and indirect detection.
- The SCTM has very exotic decays for the Higgs sectors that I am currently studying.