

ICTP-TS/ICTP-SAIFR Summer School 2018

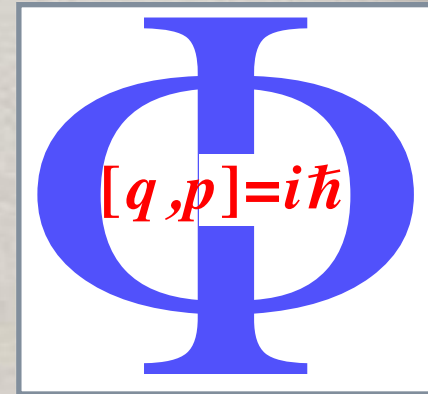
Sao Paulo, 18th - 29th June 2018

PARTICLE PHYSICS & THE EARLY UNIVERSE



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elusives-invisiblesPlus
neutrinos, dark matter & dark energy physics



OUTLINE

- Lecture 1: Standard Cosmology & the cosmological parameters
- Lecture 2: Inflation & the CMB
- Lecture 3: Thermal Universe and Big Bang Nucleosynthesis
- Lecture 4: Structure Formation & Dark Matter
- Lecture 5: Baryogenesis

LECTURE 1: OUTLINE

- Cosmology as a science
- The Standard Cosmological Model
- The History of our Universe
- Standard Candles and Standard Rulers
- Cosmological Parameters & Λ CDM
- Problems of Standard Cosmology

**COSMOLOGY
AS A SCIENCE**

IS COSMOLOGY SCIENCE ?

“Real science”
(Physics)

Many experiments
at different scales

Reproducible

Prepared/measured initial state

Measured final state
(very good statistics &
controlled systematics)

Cosmology

Few observations
at selected scales

Single Universe

Unknown initial state
Measured final state
(with limited statistics &
unknown systematics...)

BUT luckily not as bad as it looks ! Why ?

IS COSMOLOGY SCIENCE ?

Cosmology at Late Times

classical evolution:
deterministic

“hydrodynamics” with friction
or Boltzmann equation

Newtonian approximation
often sufficient (for DM)

Initial condition problem,
if not fixed by previous
evolution

Cosmology at Early Times

small quantum fluctuations:
linearized semiclassical
evolution
each mode/scale independent

Quantum nature encoded
in stochastic gaussian
initial conditions

“Ergodic hypothesis”:
quantum average = spatial average

EINSTEIN'S EQUATION: ENERGY IS GEOMETRY

$$\mathcal{R}_{\mu}^{\nu} - \frac{1}{2}\delta_{\mu}^{\nu}\mathcal{R} = 8\pi G_N T_{\mu}^{\nu} + \Lambda\delta_{\mu}^{\nu}$$

Einstein's Tensor:
Geometry of Space-time

Classical so far...

Energy-momentum Tensor:
ALL the Physics content

Quantum

The birth of Cosmology as a science:
the Universe's dynamics and fate is determined
by its Energy (Particle) content,
both the known and the unknown....

THE STANDARD MODEL

Our present understanding of the forces and particles is based on the symmetry group $SU(3)_C \times SU(2)_L \times U(1)_Y$.

Standard Model			
Matter			Forces
e	μ	τ	γ
ν_e	ν_μ	ν_τ	W^\pm, Z
u	C	t	g
d	S	b	G

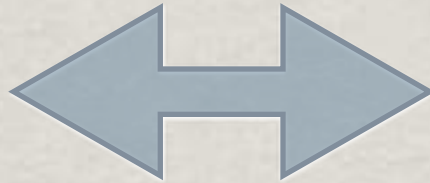
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It describes perfectly the data so far, but it is incomplete:

- theoretically it does not explain flavour and the presence of 3 generations, nor why the Higgs is light...
- it lacks a Dark Matter and inflaton candidate and also a mechanism to generate the baryon number...

WHICH MODEL BEYOND THE SM ?

weakly
coupled



strongly
coupled

Cosmology

(Collider-based)
Particle Physics

To pinpoint the completion of the SM, exploit the complementarity between Cosmology and Particle Physics to explore all the sectors of the theory:
the more weakly coupled and the more strongly coupled to the Standard Model fields...

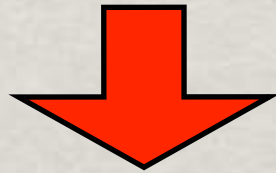
Best results if one has information from both sides,
e.g. neutrinos, axions, etc... ???

STANDARD MODEL OF COSMOLOGY

STANDARD COSMOLOGY

Cosmological Principle (nowadays also experimental result...):

The Universe is homogeneous and isotropic
on large scales (i.e. larger than ~ 100 Mpc)



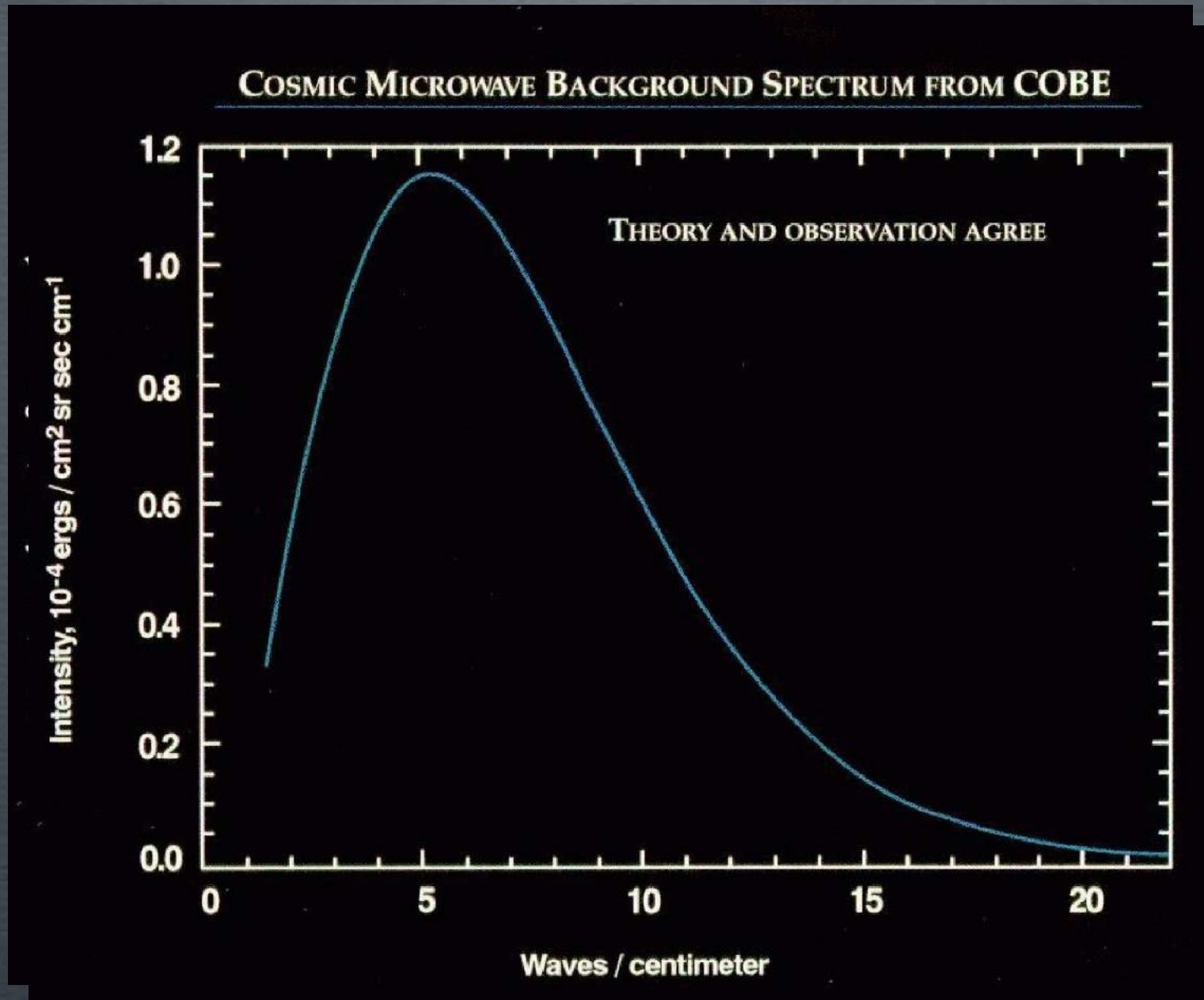
It is described by the Friedmann-Robertson-Walker Metric:

$$ds^2 = dt^2 - a^2(t) \left(\frac{dr^2}{1 - \kappa r^2} + r^2 d\Omega \right)$$

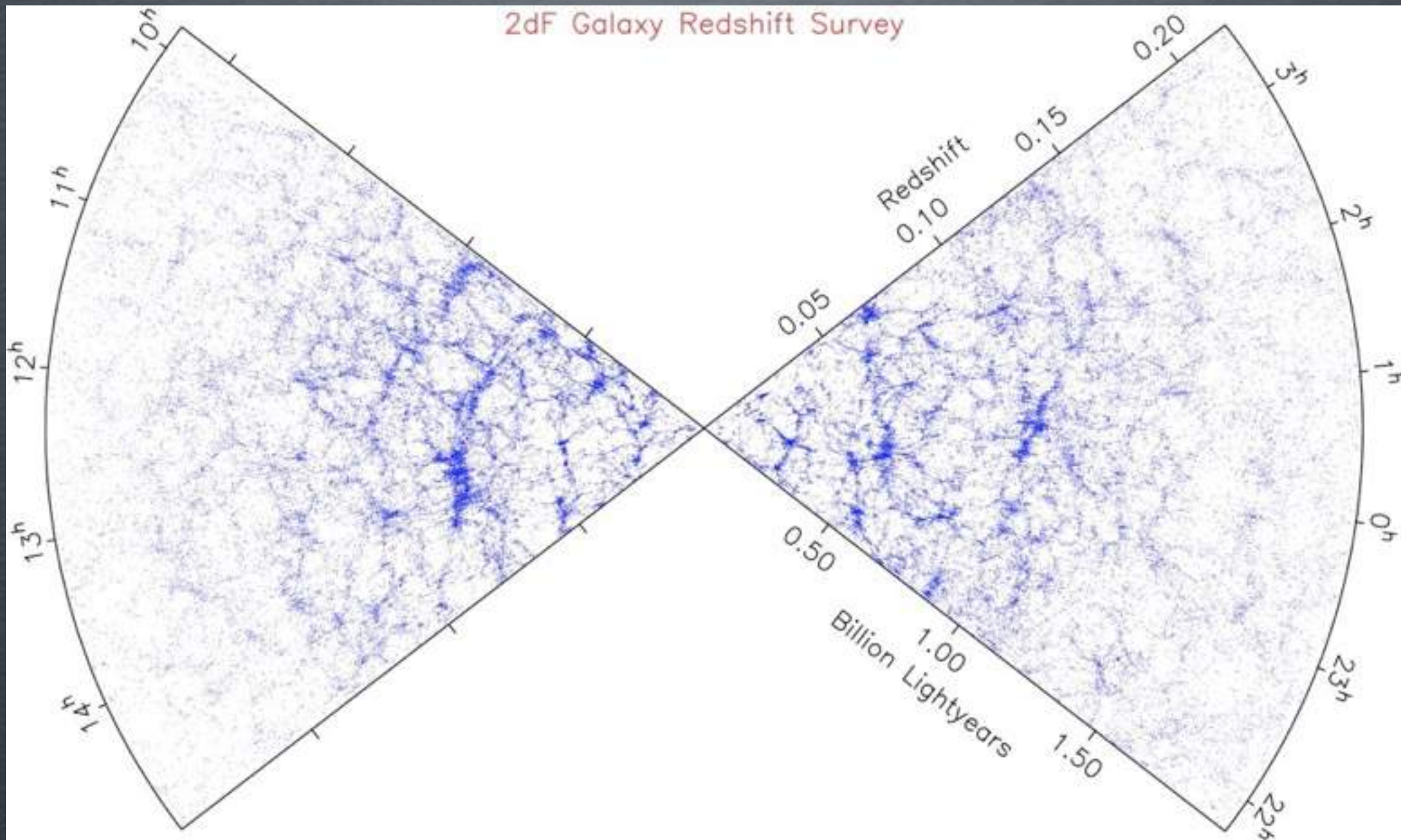
conformal to Minkowski for $dt^2 = a^2(\eta) d\eta^2$ $\kappa = 0$

- Only one dynamical variable: the scale factor $a(t)$
- One constant parameter: the spatial curvature κ

1/2 Physics Nobel Prize 2006 to J. Mather for COBE:
ISOTROPY: Perfect Black Body in all directions !



HOMOGENEITY: less structure at large redshifts !



HUBBLE FLOW

A FRW metric immediately gives for static objects

$$v = \frac{d(a(t)r)}{dt} = \dot{a}r = \frac{\dot{a}}{a}ar = H(t)d$$



Hubble Flow !

$$H_0 \sim 500 \text{ km/s/Mpc}$$

Nowadays

$$H_0 \sim 72 \text{ km/s/Mpc}$$

E. Hubble 1929

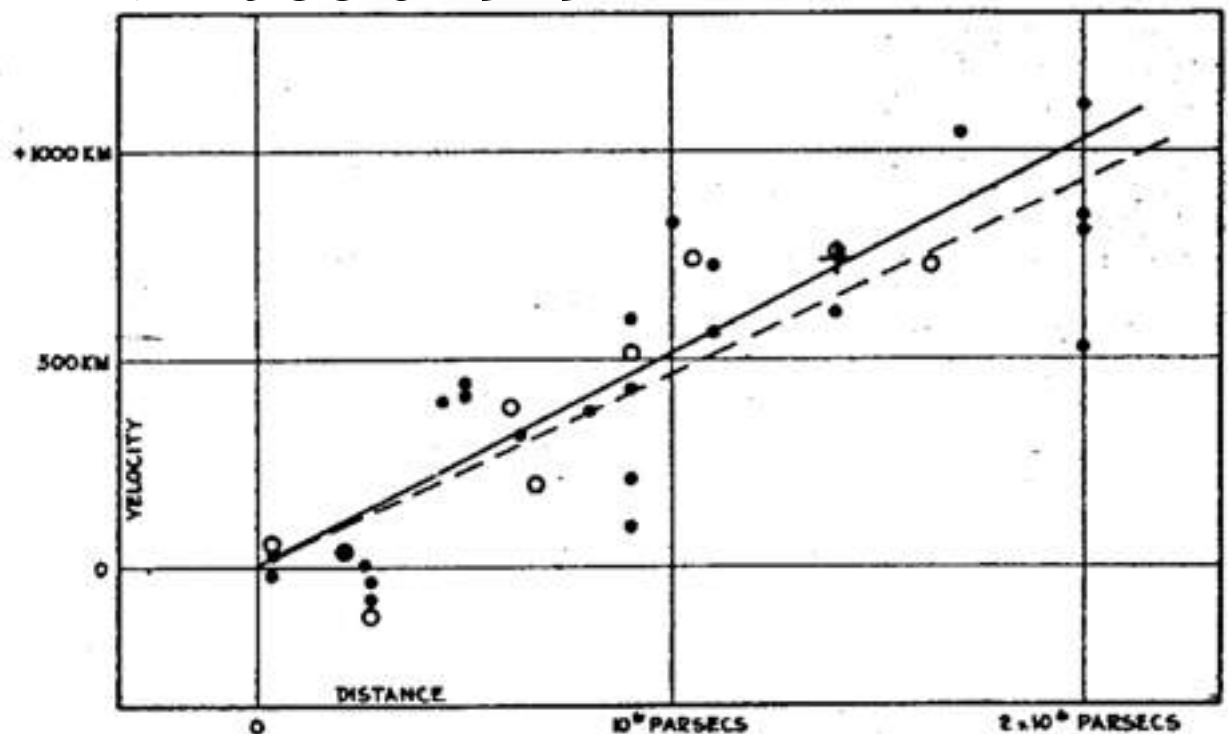


FIGURE 1

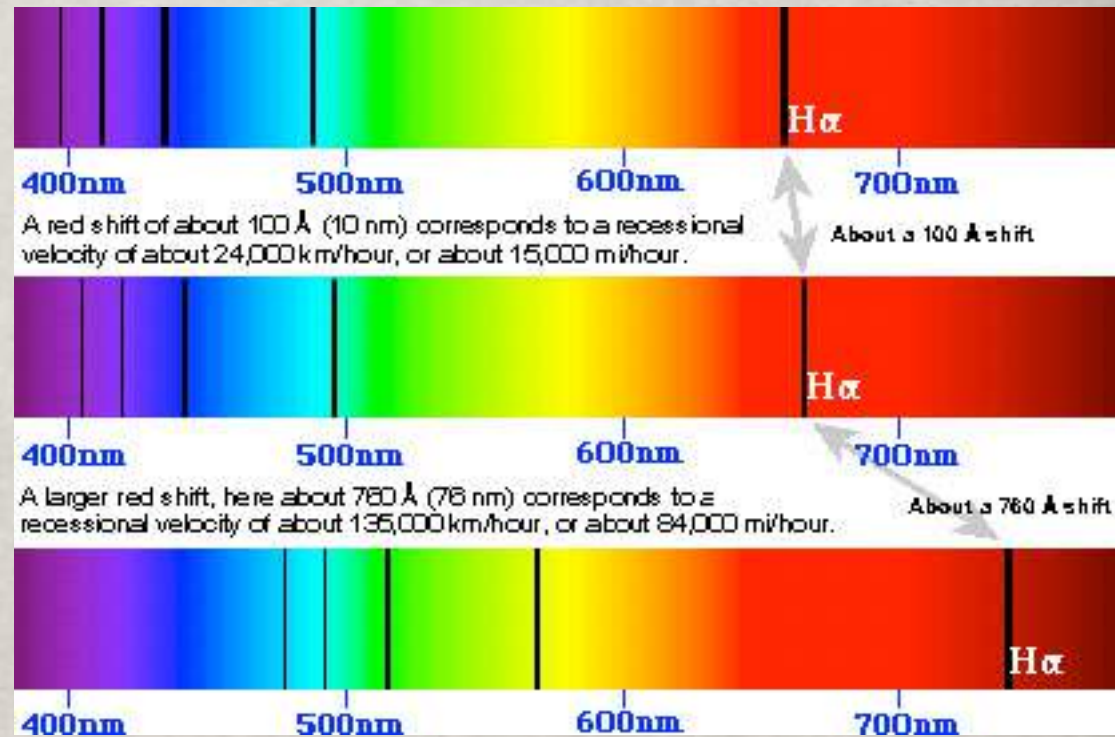
REDSHIFT MEASUREMENT

Due to the Universe's expansion
all spectra of astrophysical
object are red-shifted !

$$\frac{\lambda_{obs}}{\lambda_{em}} = \frac{a(t_{obs})}{a(t_{em})} = 1 + z$$

Redshift can be used to
parametrize the time
of emission !

For the *visible* Universe in cosmology we use the redshift instead
of time. The function $a(t)$ is needed to invert the relation.



EINSTEIN'S EQUATION: ENERGY IS GEOMETRY

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ENERGY MOMENTUM TENSOR

Perfect fluid approximation $T_{\nu}^{\mu} = (\rho + p)u^{\mu}u_{\nu} - p\delta_{\nu}^{\mu}$

where ρ and p are the fluid density and pressure, while u is the fluid 4-velocity. So in the rest-frame of the fluid, where $u = (1, \vec{0})$, i.e. assuming that the fluid is at rest in the Universe, we have

$$T_{\nu}^{\mu} = \begin{pmatrix} \rho & 0 & 0 & 0 \\ 0 & -p & 0 & 0 \\ 0 & 0 & -p & 0 \\ 0 & 0 & 0 & -p \end{pmatrix}$$

Moreover the energy-momentum tensor is covariantly conserved:

$$\mathcal{D}_{\mu}T^{\mu\nu} = 0 \quad \rightarrow \quad \dot{\rho} + 3H(\rho + p) = 0 \quad \text{continuity equation}$$

This can be solved if we know the equation of state $p(\rho) = w\rho$ then

$$\frac{\dot{\rho}}{\rho} = -3(1 + w)H \quad \Rightarrow \quad \rho \propto a^{-3(1+w)}$$

So the different energy types are modeled by perfect fluids with equation of state $w_i = p_i/\rho_i$.

FRIEDMANN EQUATION:

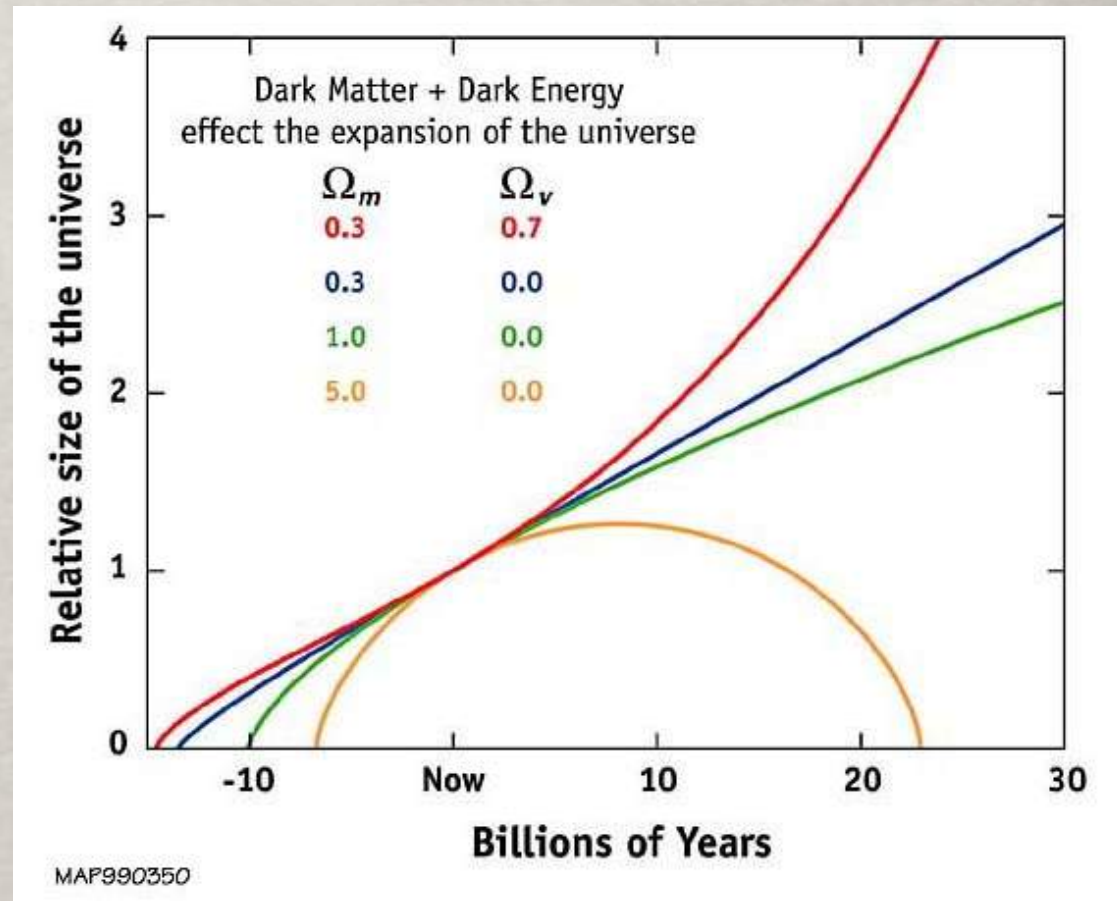
$$H^2 \equiv \left(\frac{\dot{a}}{a} \right)^2 = \frac{8\pi G_N}{3} \rho + \Lambda - \frac{\kappa}{a^2}$$

- The energy density & curvature decree the time evolution of the scale factor
- Key parameter is the critical density:

$$\rho_c = \frac{3H^2}{8\pi G_N} \quad \Omega_i = \frac{\rho_i}{\rho_c}$$

Ω_i : density in $\sim 10^4 \text{eV}/\text{cm}^3$

$\sim 10 \text{ protons}/\text{m}^3$

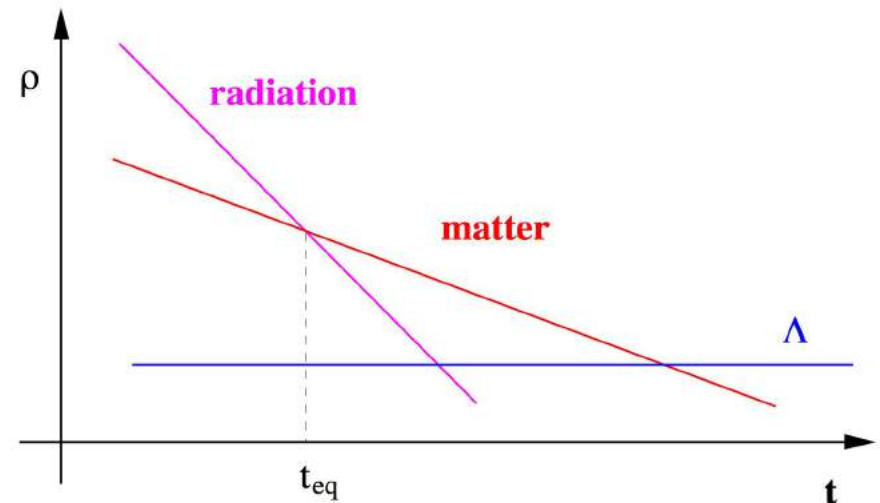


THE HISTORY OF THE UNIVERSE

DIFFERENT ENERGY TYPES

Depending on the pressure and the equation of state, the energy densities give different expansion rates:

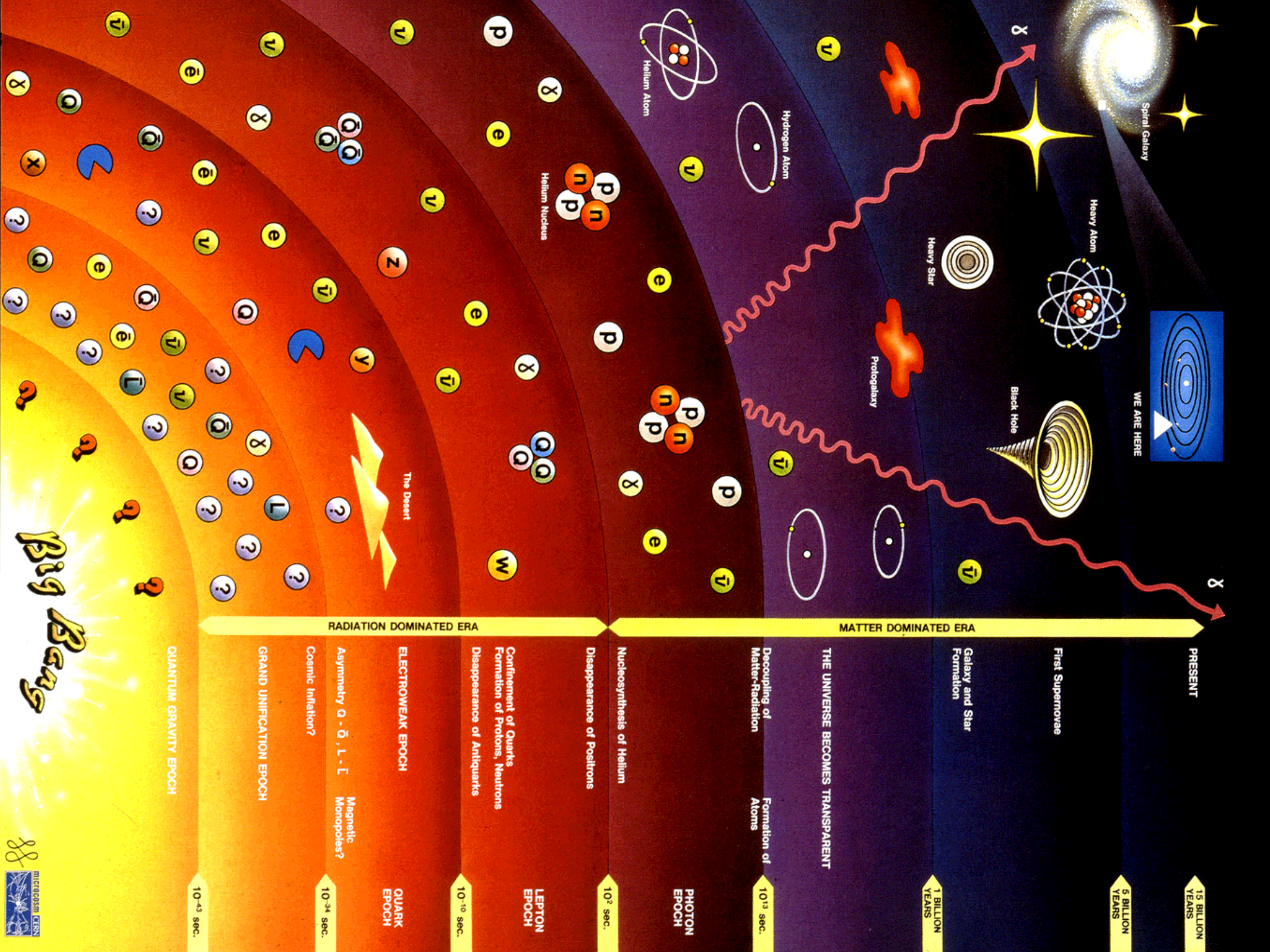
Type	p/ρ	$\rho(a)$	$a(t)$
Generic	w	$a^{-3(1+w)}$	$t^{2/(3(1+w))}$
Radiation	$1/3$	$\propto a^{-4}$	$\propto t^{1/2}$
Matter	0	$\propto a^{-3}$	$\propto t^{2/3}$
Λ	-1	const.	e^{Ht}
Curvature	$-1/3$	$\propto a^{-2}$	$\propto t^1$



Always decelerating apart for the cosmological constant !

Different epochs of the Universe history

Big Bang



RADIATION DOMINATED ERA | **MATTER DOMINATED ERA**

- PRESENT** (15 BILLION YEARS)
- First Supernovae** (5 BILLION YEARS)
- Galaxy and Star Formation** (1 BILLION YEARS)
- THE UNIVERSE BECOMES TRANSPARENT**
- Decoupling of Matter-Radiation** (10¹³ sec.)
- Formation of Atoms** (10¹³ sec.)
- Photon Epoch** (10¹³ sec.)
- Nucleosynthesis of Helium** (10² sec.)
- Disappearance of Positrons** (10² sec.)
- LEPTON EPOCH** (10² sec.)
- Confinement of Quarks**
- Formation of Protons, Neutrons**
- Disappearance of Antiquarks** (10⁻¹⁰ sec.)
- ELECTROWEAK EPOCH** (10⁻¹⁰ sec.)
- QUARK EPOCH** (10⁻¹⁰ sec.)
- Asymmetry Q - Q̄, L - L̄**
- Magnetic Monopoles?** (10⁻³⁴ sec.)
- Cosmic Inflation?** (10⁻³⁴ sec.)
- GRAND UNIFICATION EPOCH** (10⁻³⁴ sec.)
- QUANTUM GRAVITY EPOCH** (10⁻⁴³ sec.)



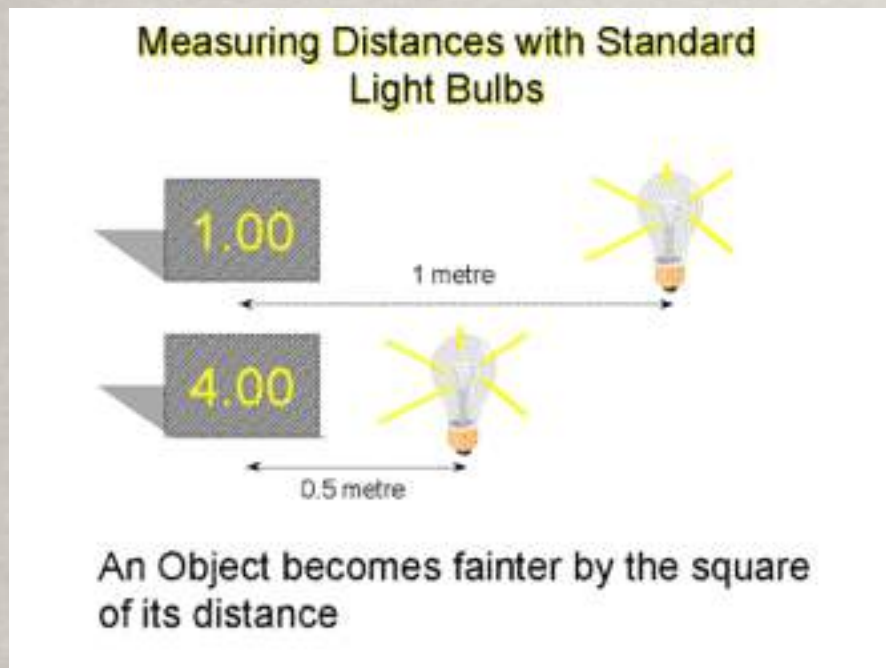
IMPORTANT EPOCHS

- Today: $T = 2.7K \sim 10^{-4} \text{ eV} \quad z = 0$
- First stars: $T \sim 10^{-3} \quad z \sim 15 - 20$
- Photon decoupling: CMB $T = 0.4 \text{ eV} \quad z = 1100$
- Matter and Radiation equality: $T = 1 \text{ eV} \quad z \sim 1300$
- Nucleosynthesis: $T = 0.1 \text{ MeV}$
- Neutrino decoupling: $C\nu B \quad T \sim 1 \text{ MeV}$
- QCD phase transition $T \sim 0.3 \text{ GeV}$
- EW phase transition $T \sim 100 \text{ GeV}$
- ?????

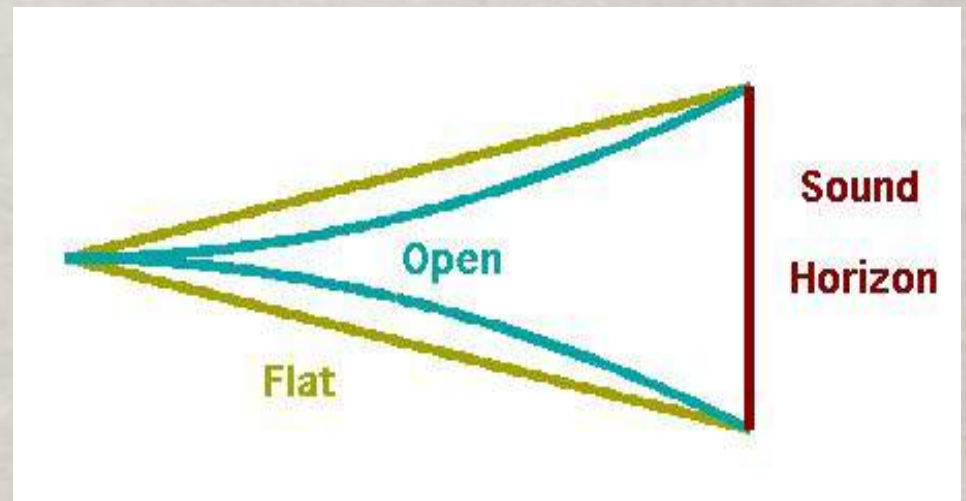
STANDARD CANDLES AND RULERS

HOW CAN WE MEASURE THE EXPANSION OF THE UNIVERSE ?

Standard Candle



Standard Ruler



LUMINOSITY DISTANCE

$$D_L^2 = \frac{L}{4\pi\Phi}$$

Intrinsic Luminosity
Measured Flux

For a FRW universe it is given simply by

$$D_L^2 = (1+z) \int_0^z \frac{dz}{H(z)}$$

where

$$H^2(z) = H_0^2 \sum_i \Omega_{i,0} (1+z)^{3(1+w_i)}$$



determination of the cosmological parameters

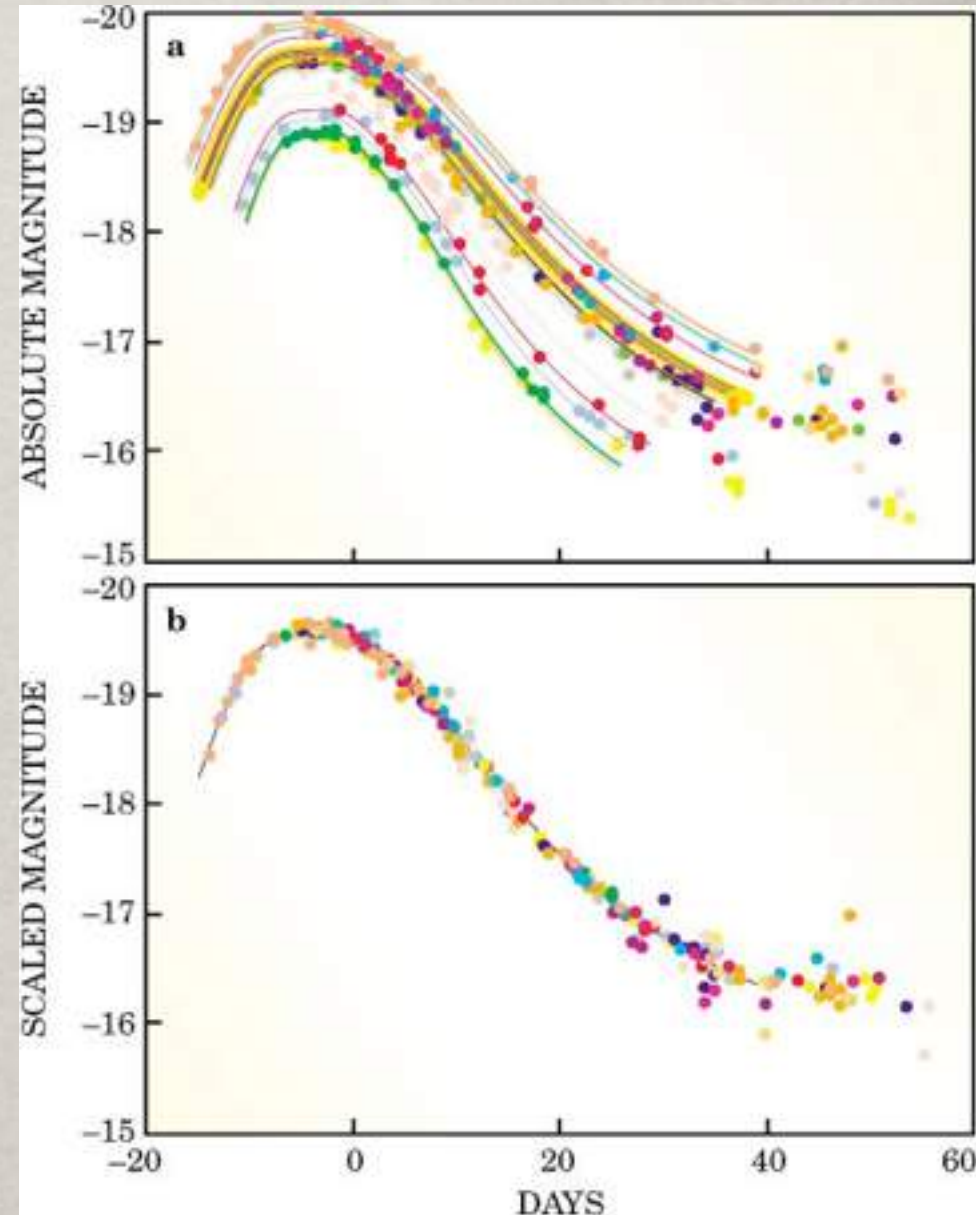
$$\Omega_{DM}(w = 0), \Omega_{\Lambda}(w = -1), \dots$$

SN-IA AS STANDARD CANDLES

Type Ia supernova is the explosion of a white dwarf star in a binary star system. Material from a companion red giant star is dumped on the white dwarf until the smaller star reaches a precise mass limit.



The spectra can be corrected to lie on the same line and follow a relation between peak luminosity and width of the light curve...

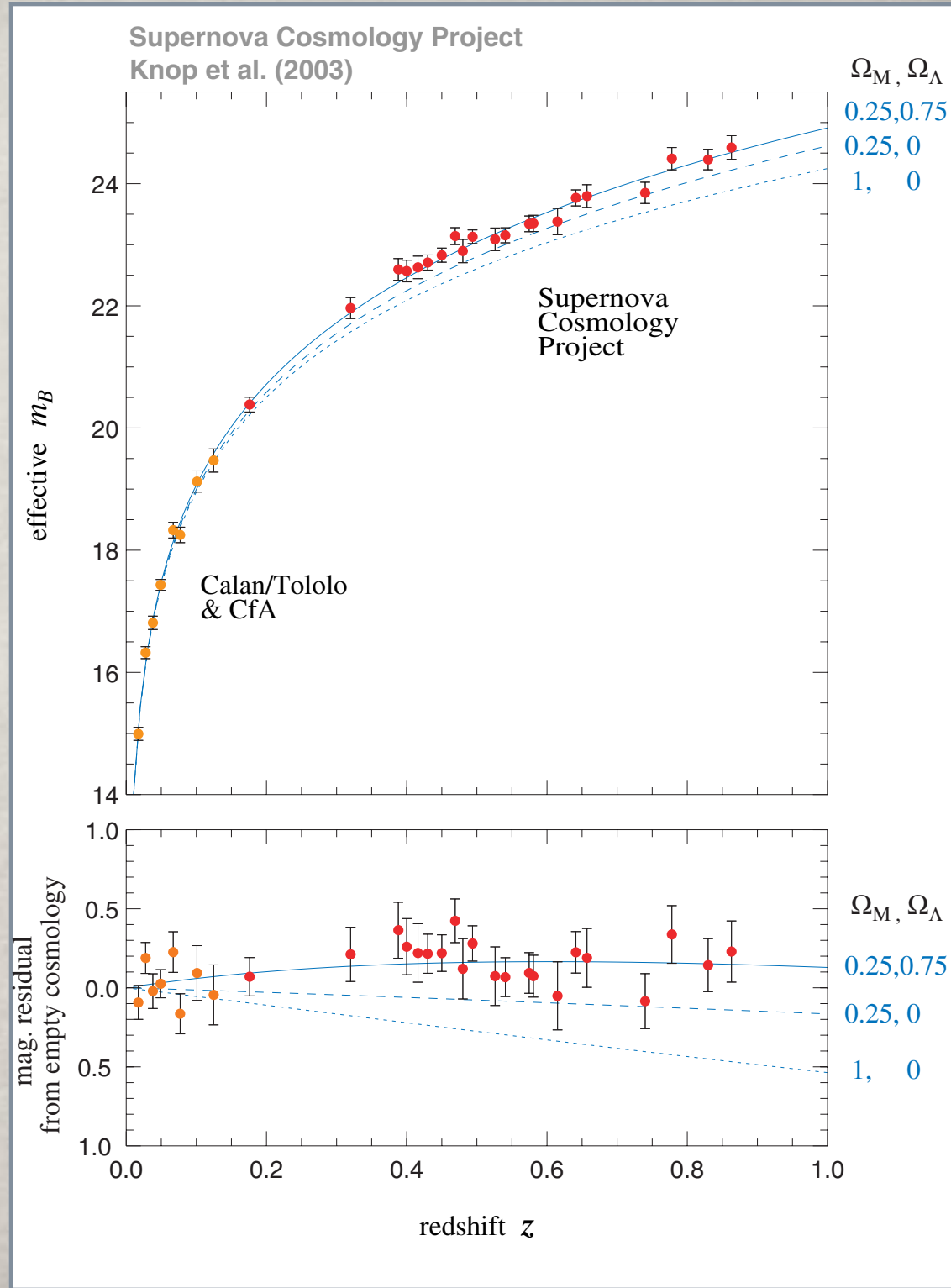


SUPERNOVAE IA AS STANDARD CANDLES

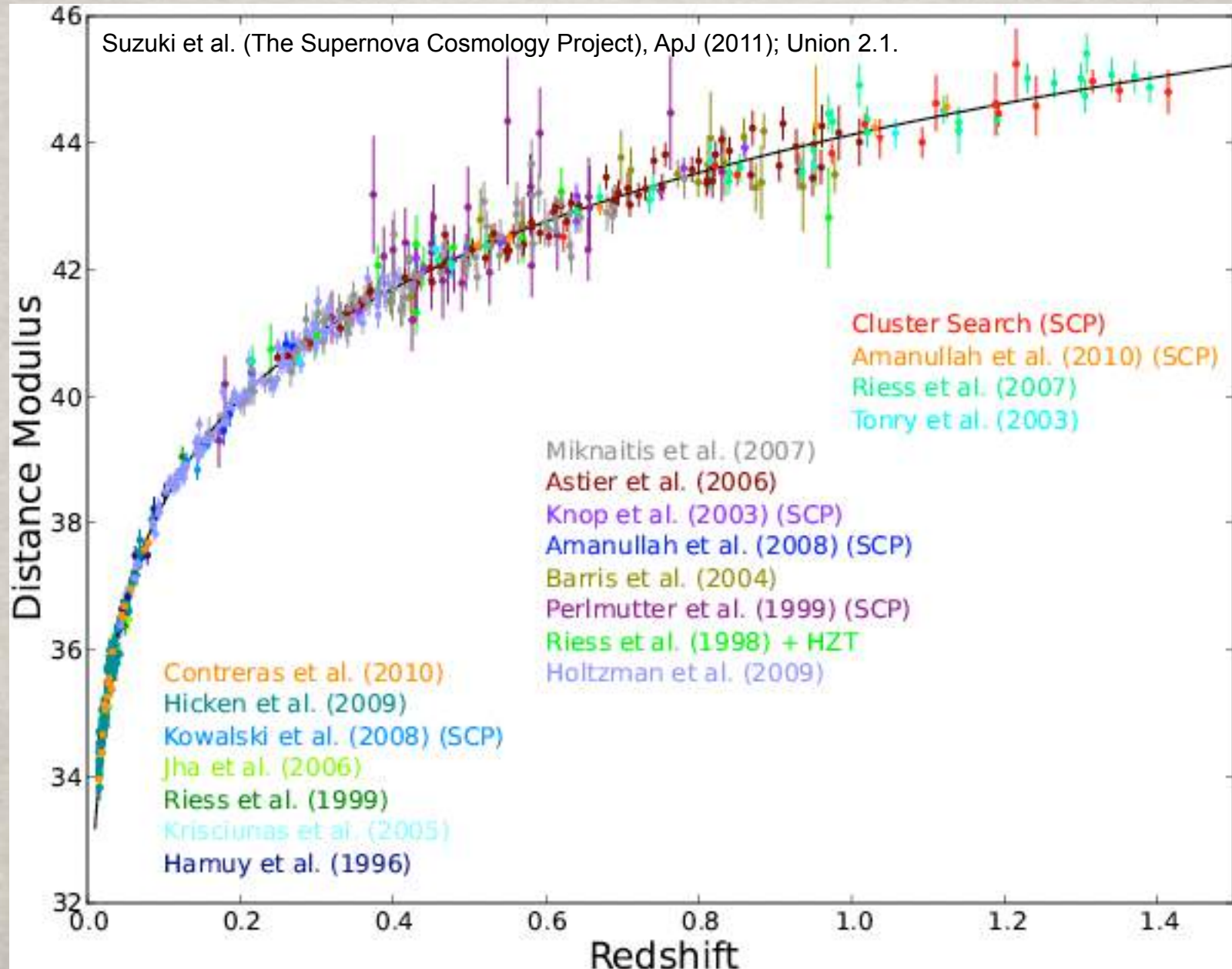
- Measure the apparent magnitude as a function of the redshift z and test the first correction to the Hubble flow

- The Universe is accelerating !

$$\Lambda > 0$$



SN-IA AS STANDARD CANDLES



ANGULAR DISTANCE

$$D_A = \frac{R}{d}$$


Standard Ruler
Distance to the Ruler

For a FRW universe it is given simply by

$$D_A = (1+z)R \left(\int_0^z \frac{dz}{H(z)} \right)^{-1}$$

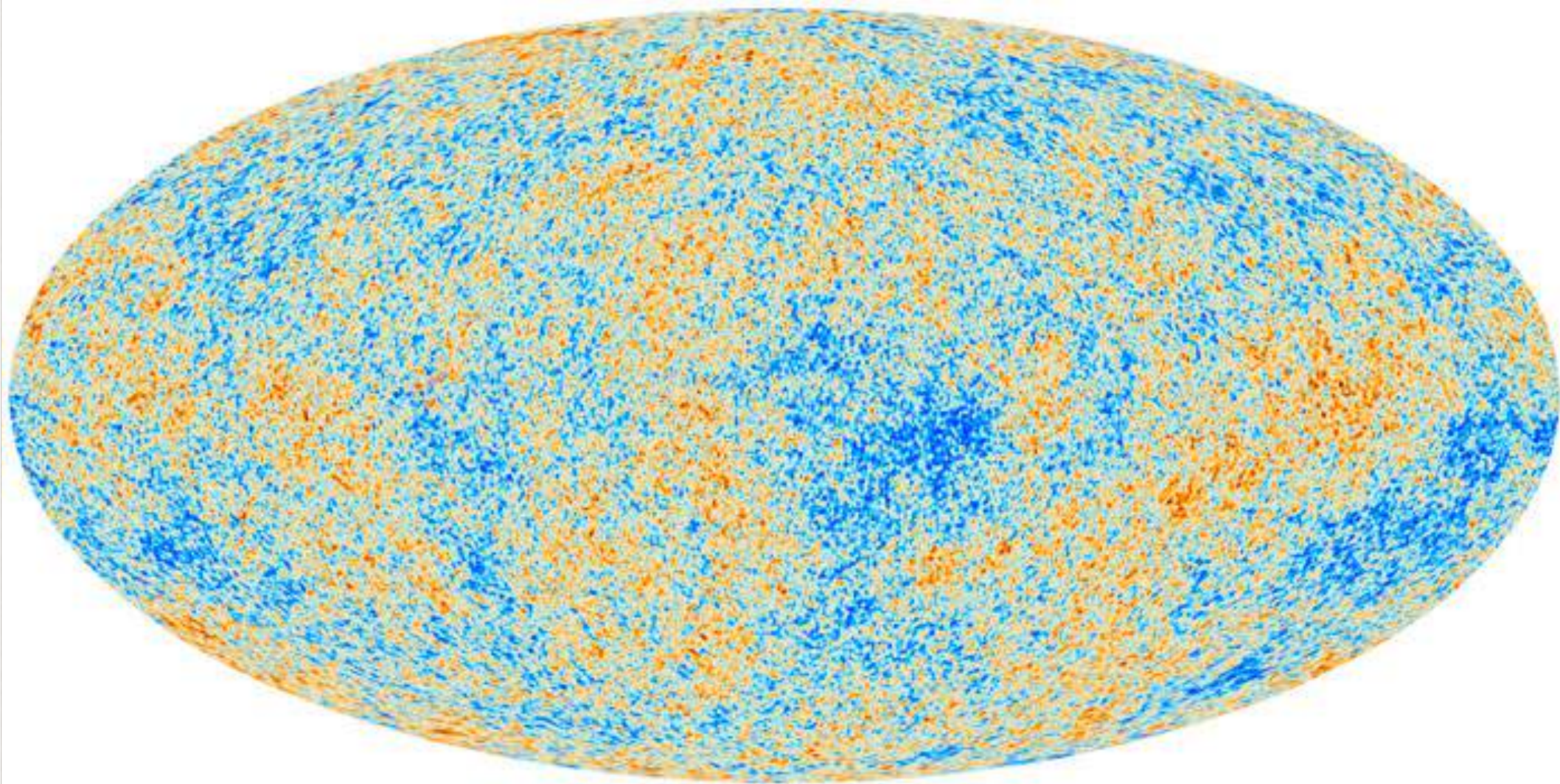
where $H(z) \sim H_0 \Omega_{D,0}^{1/2} (1+z)^{3/2(1+w_D)}$ for a dominant component

e.g. for the sound horizon at decoupling for MD


$$\frac{D_{A,CMB}}{(1+z_{CMB})} \sim \frac{2}{H_0 \Omega_{M,0}^{1/2}}$$

CMB ANISOTROPIES

Physics of the fluctuations on the homogeneous background !

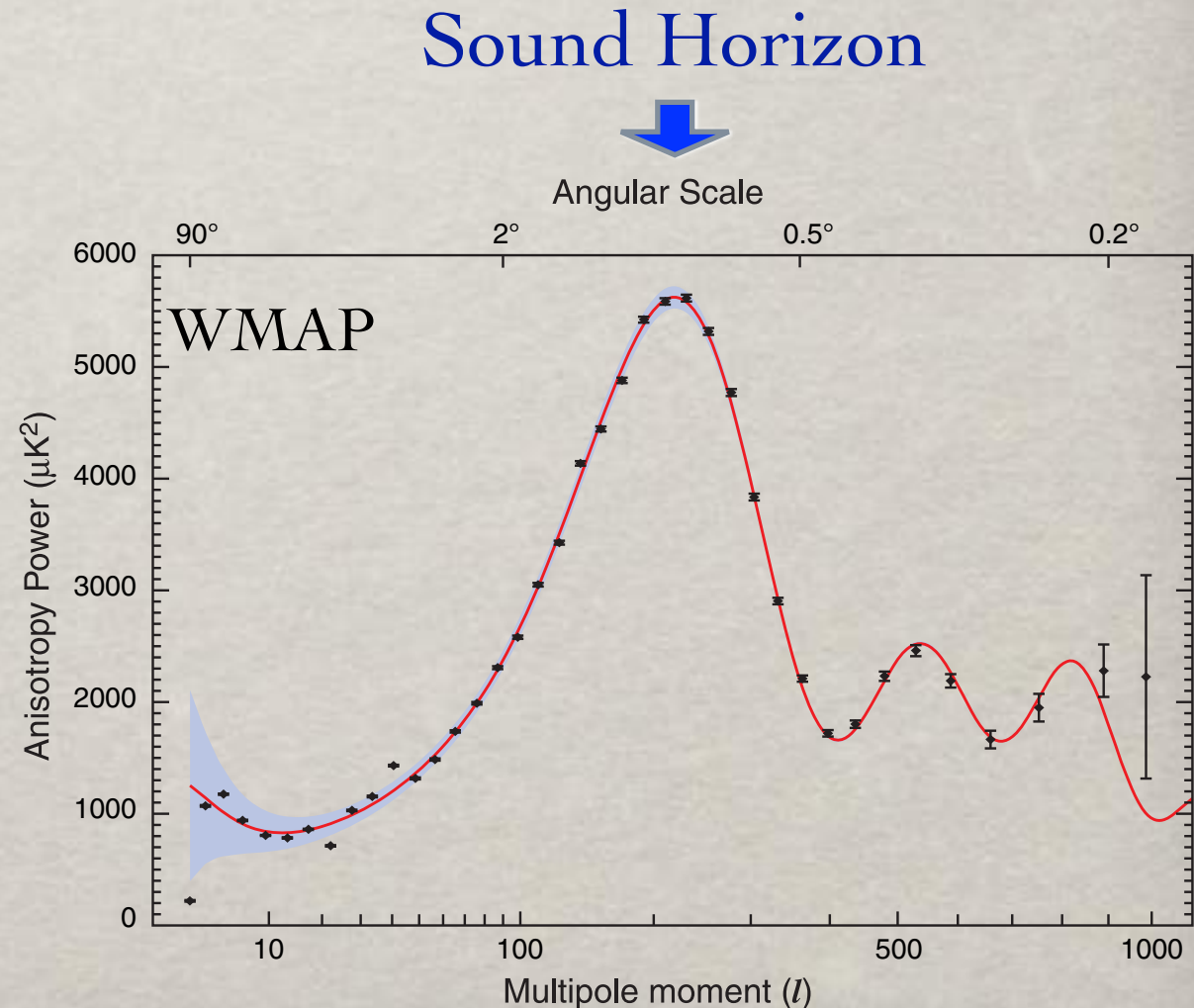


$$\langle T(\theta)T(0) \rangle = \sum_{\ell, m} a_{\ell m} Y_m^\ell(\theta)$$

THE SOUND HORIZON IN THE BARYON-PHOTON PLASMA AS STANDARD RULER

- Measure the angle corresponding to the first peak in the CMB anisotropies
- The Universe is **FLAT**

$$\Omega_{tot} = 1.014 \pm 0.017$$
$$\Rightarrow \kappa \simeq 0$$

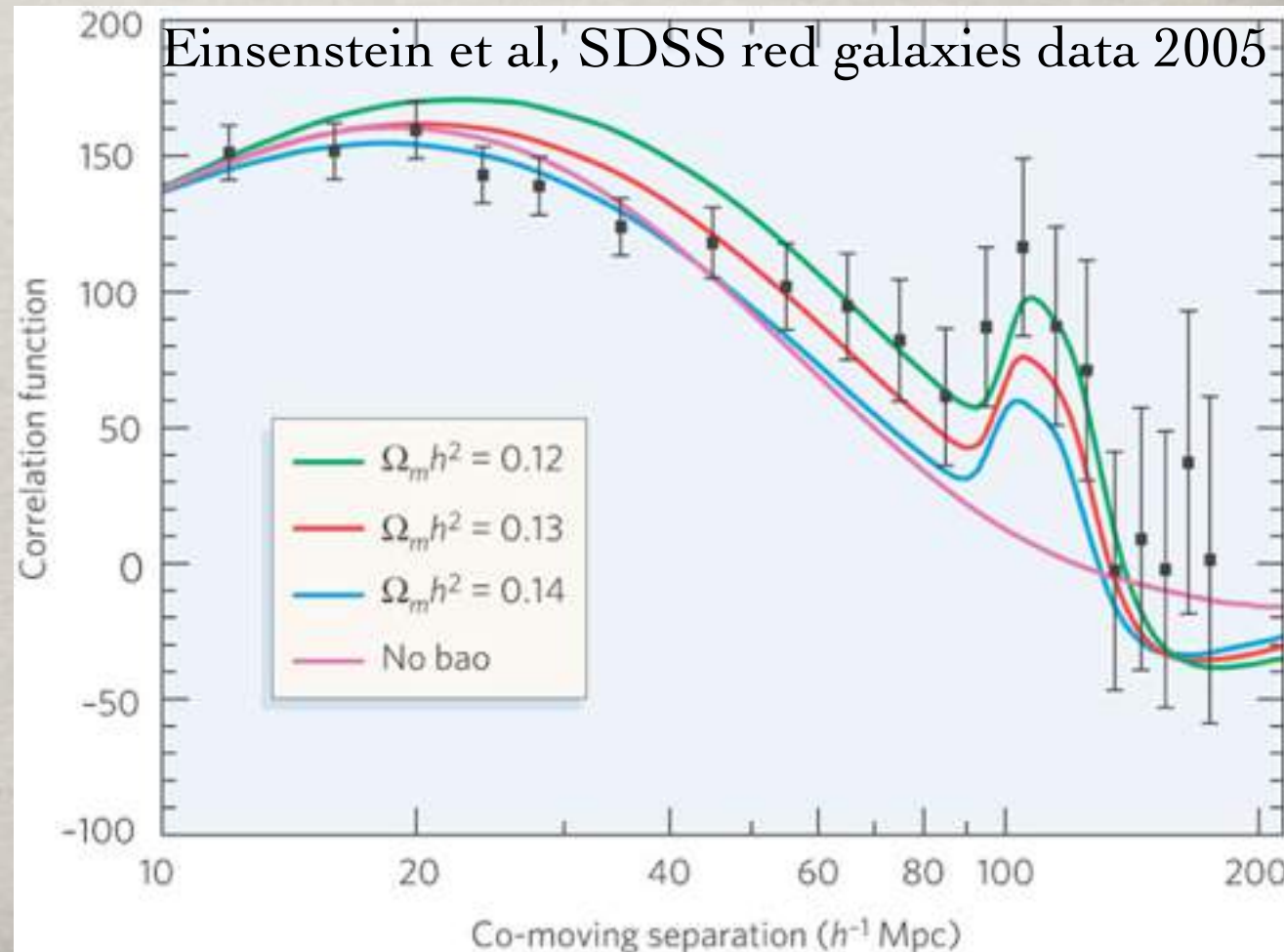


THE SOUND HORIZON IN THE BARYON-PHOTON PLASMA AS STANDARD RULER

Sound Horizon

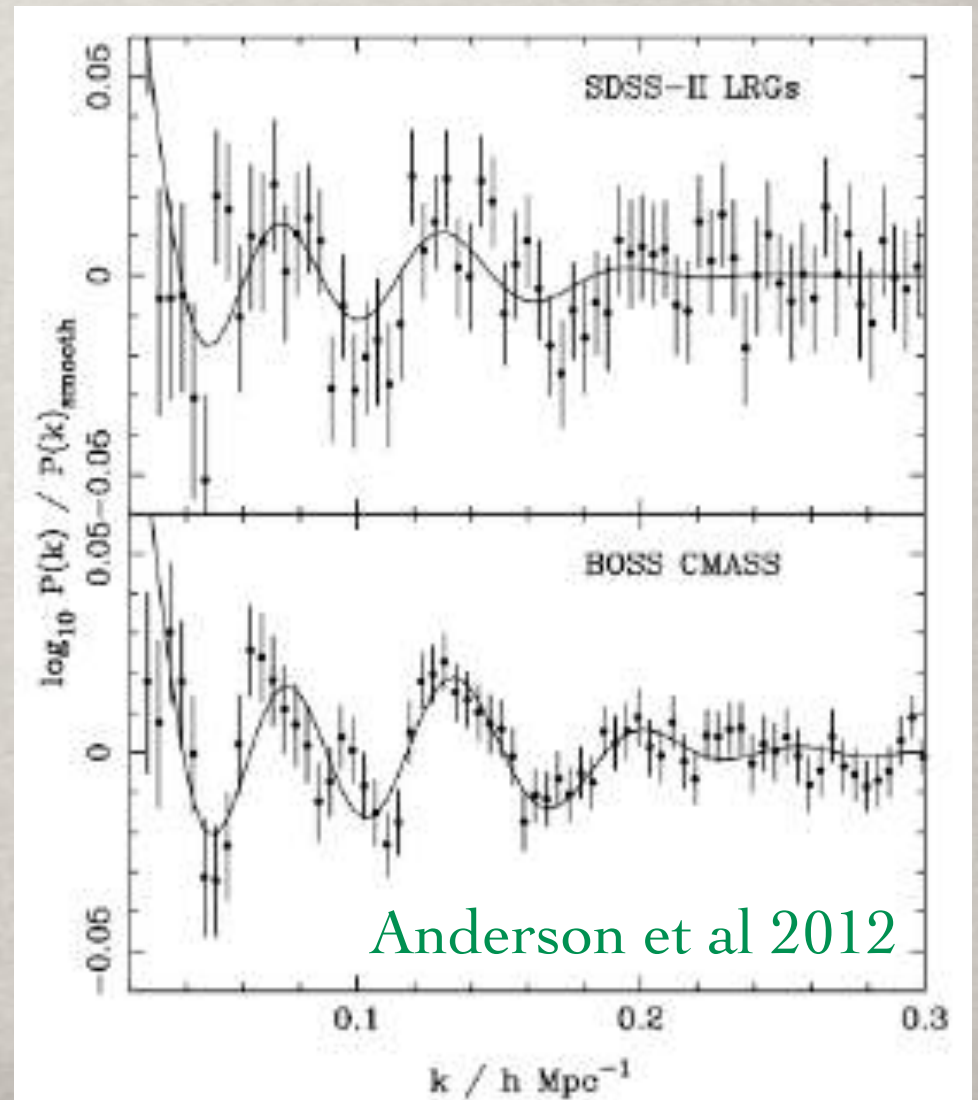


- The same scale is visible in the (baryonic) matter distribution (BAO)
- The more baryons (less CDM), the stronger the signal !

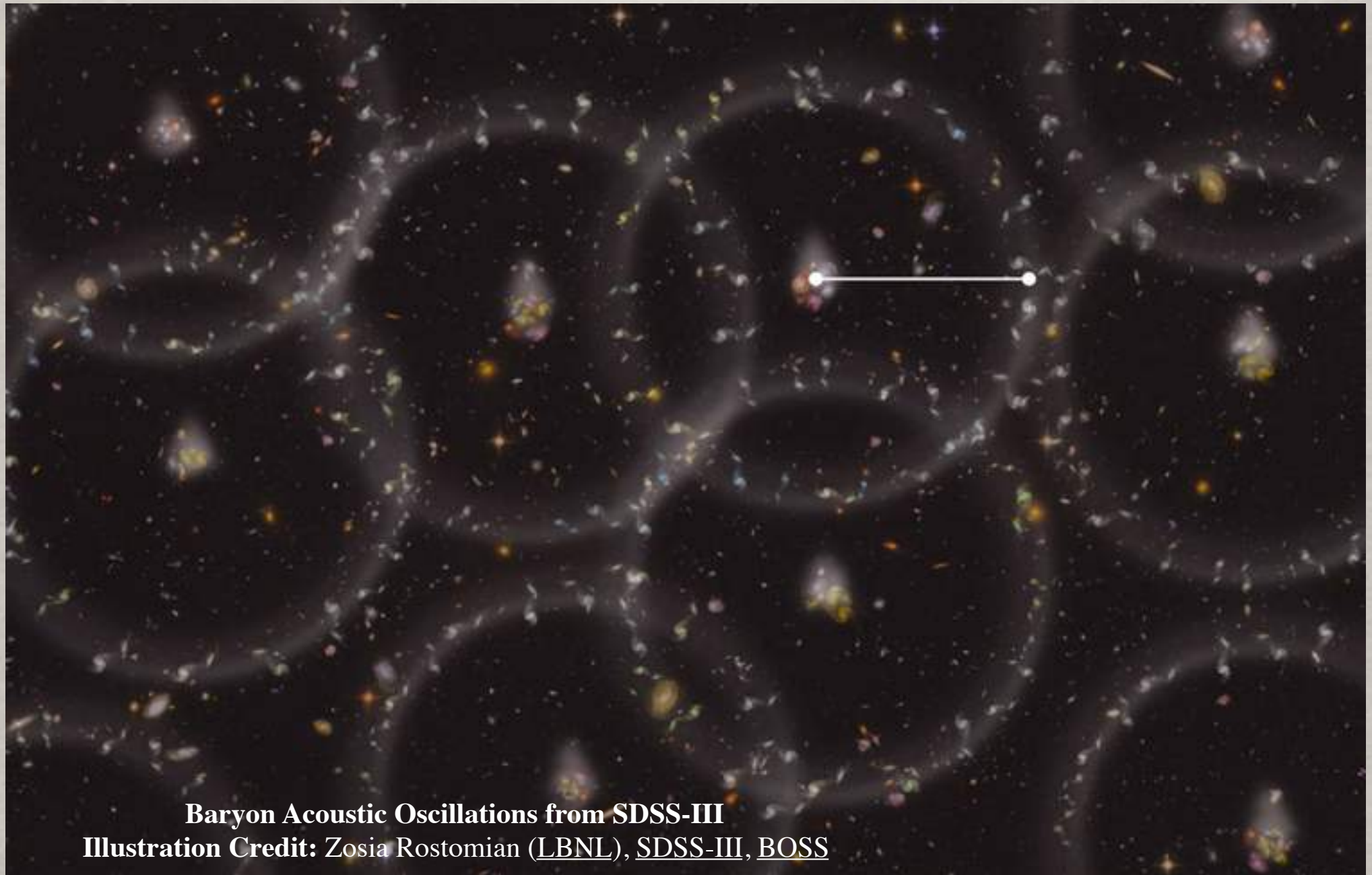


THE SOUND HORIZON IN THE BARYON-PHOTON PLASMA AS STANDARD RULER

- The signal has been now detected in the galaxy power spectrum (two-point correlation !) with high precision.
- All measurement are consistent !



BAO: AN ARTISTIC VIEW



Baryon Acoustic Oscillations from SDSS-III

Illustration Credit: Zosia Rostomian ([LBNL](#)), [SDSS-III](#), [BOSS](#)

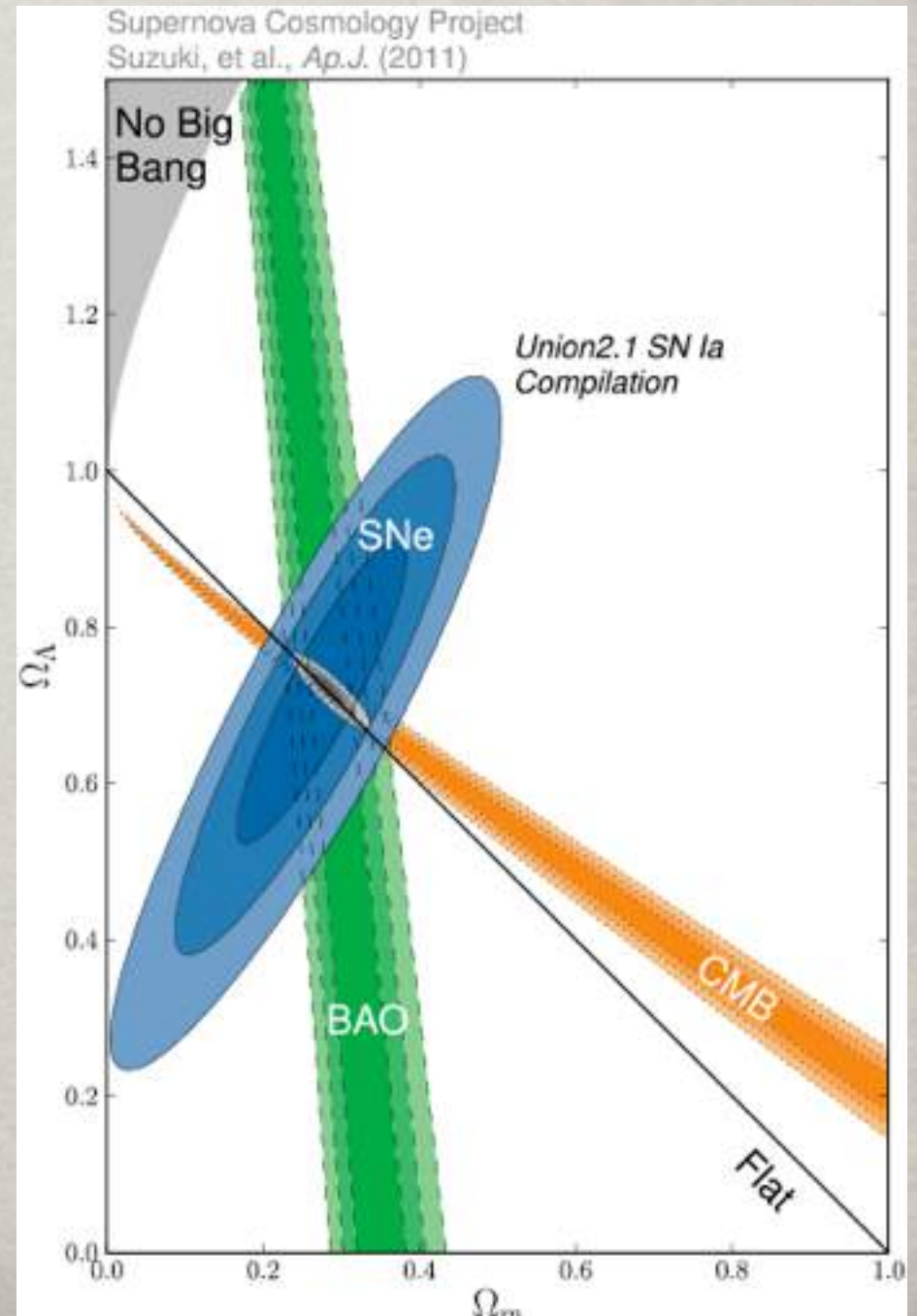
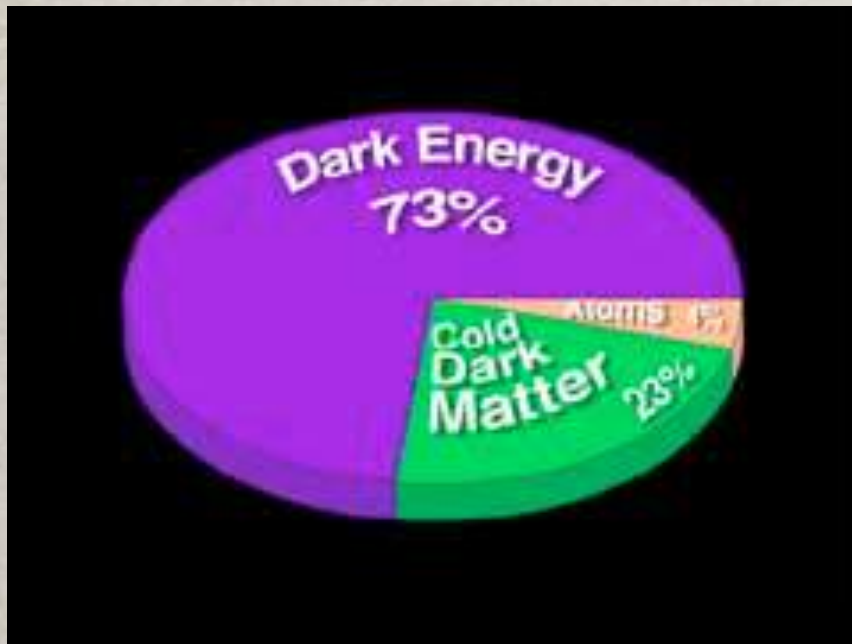
**COSMOLOGICAL
PARAMETERS &
 Λ CDM**

VANILLA COSMOLOGY

Consistent cosmological picture given in terms of only 6 parameters,

$$\Omega_M h^2, \Omega_b h^2, \tau, n_s, A_s$$

$$\theta_* (\Omega_k / \Omega_\Lambda, H_0)$$



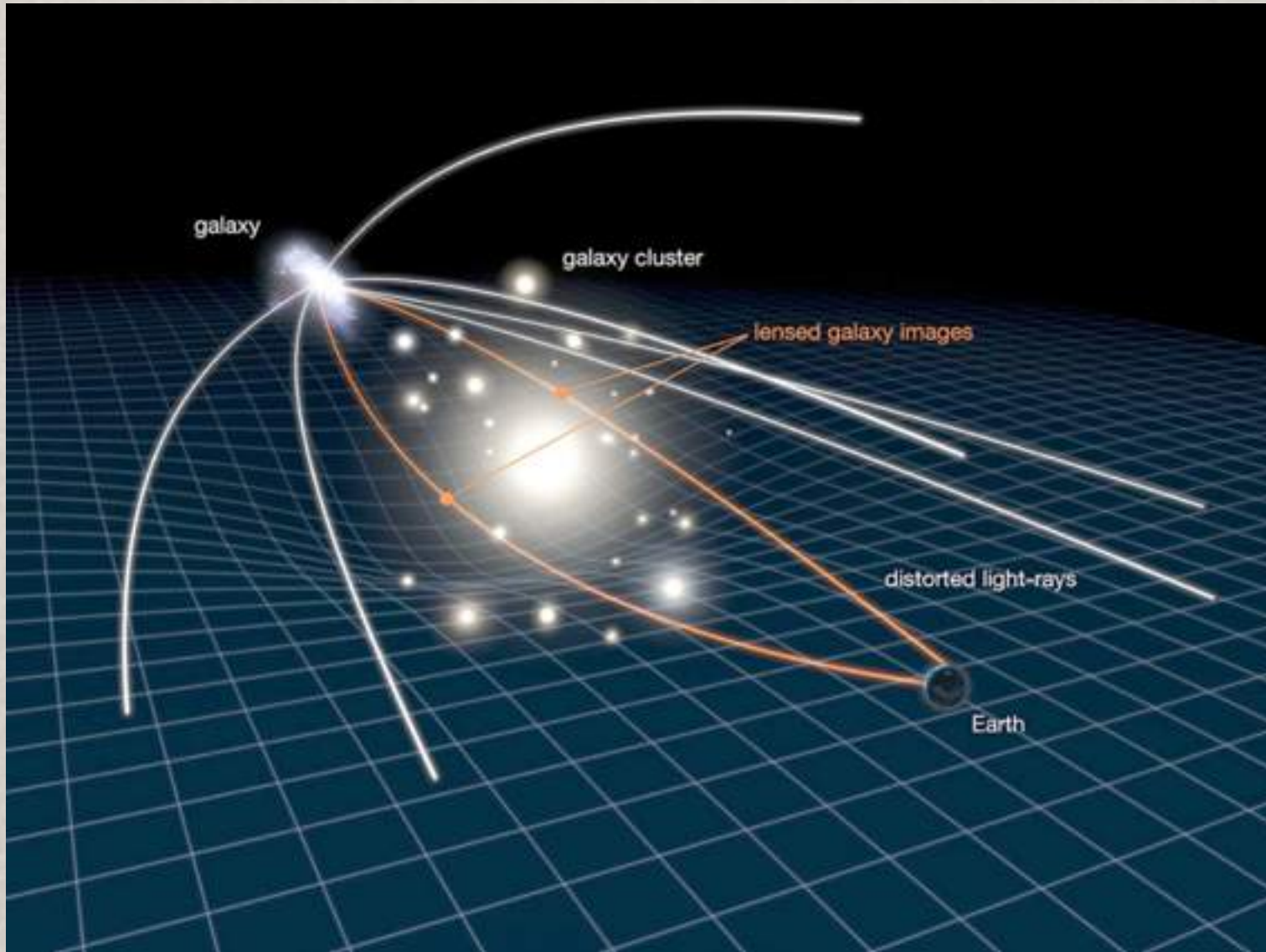
MEASURING THE UNIVERSE

As we have seen, we can obtain information on the evolution of the Universe from different probes at different times:

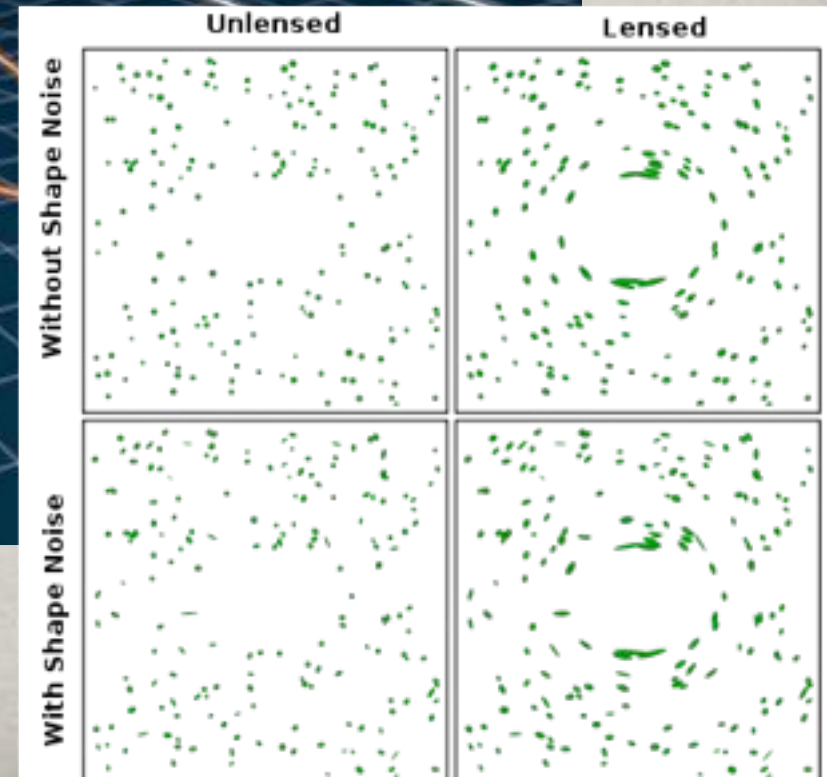
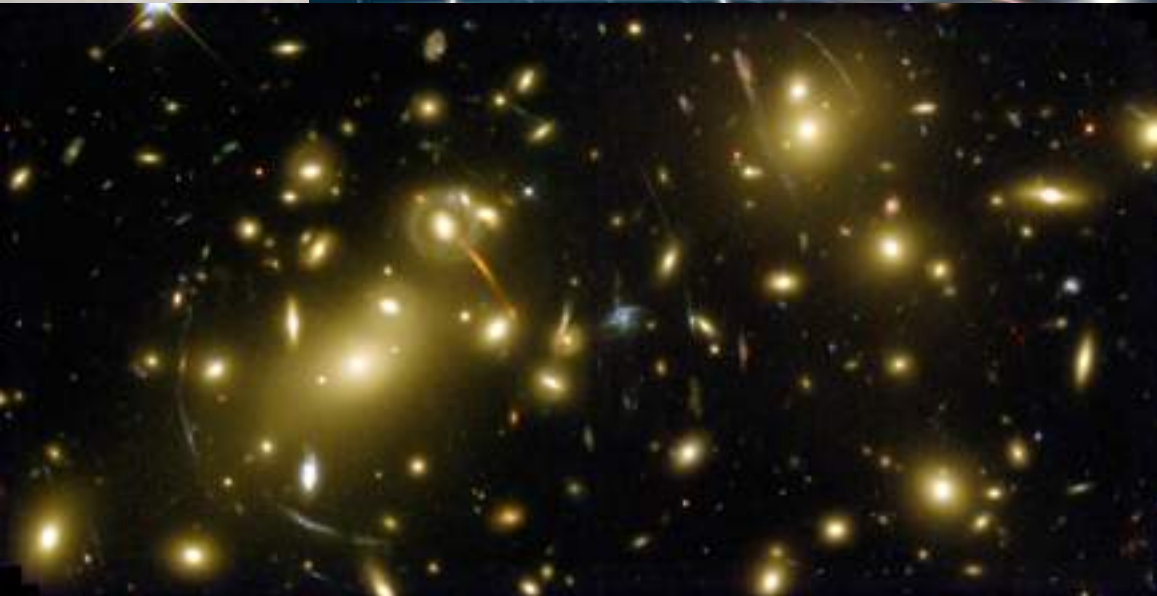
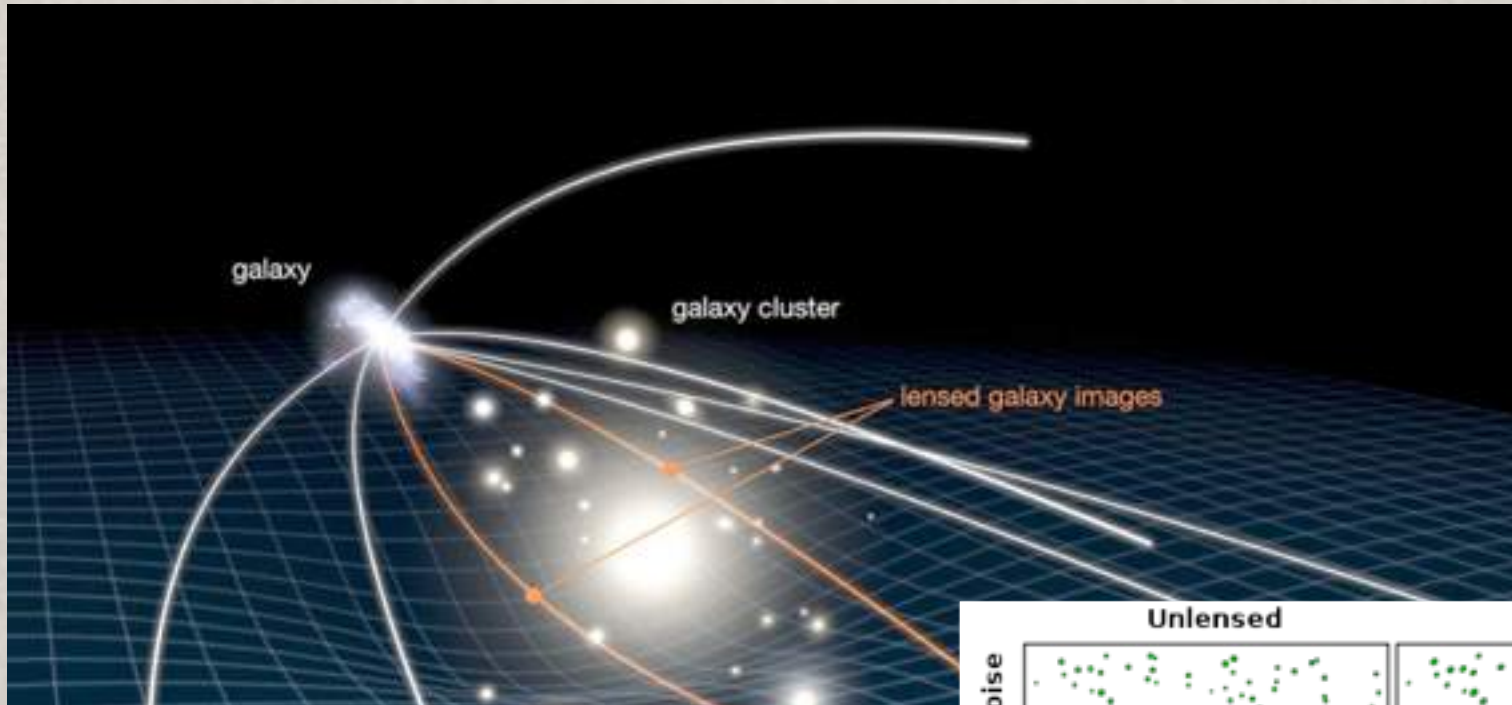
- **Nucleosynthesis** at $T \sim 1-0.01$ MeV, $t \sim 1-1000$ s
- **Recombination**, i.e. CMB for $z \sim 1100$, i.e. $T \sim 1$ eV or $t \sim 380,000$ years
- **Large Scale Structure** (galaxies, clusters), i.e. $z \sim 4-0$, i.e. $T \sim 0.01-0.0001$ eV or $t \sim 1-13$ Gy

All consistent so far, but is it possible to see more ???

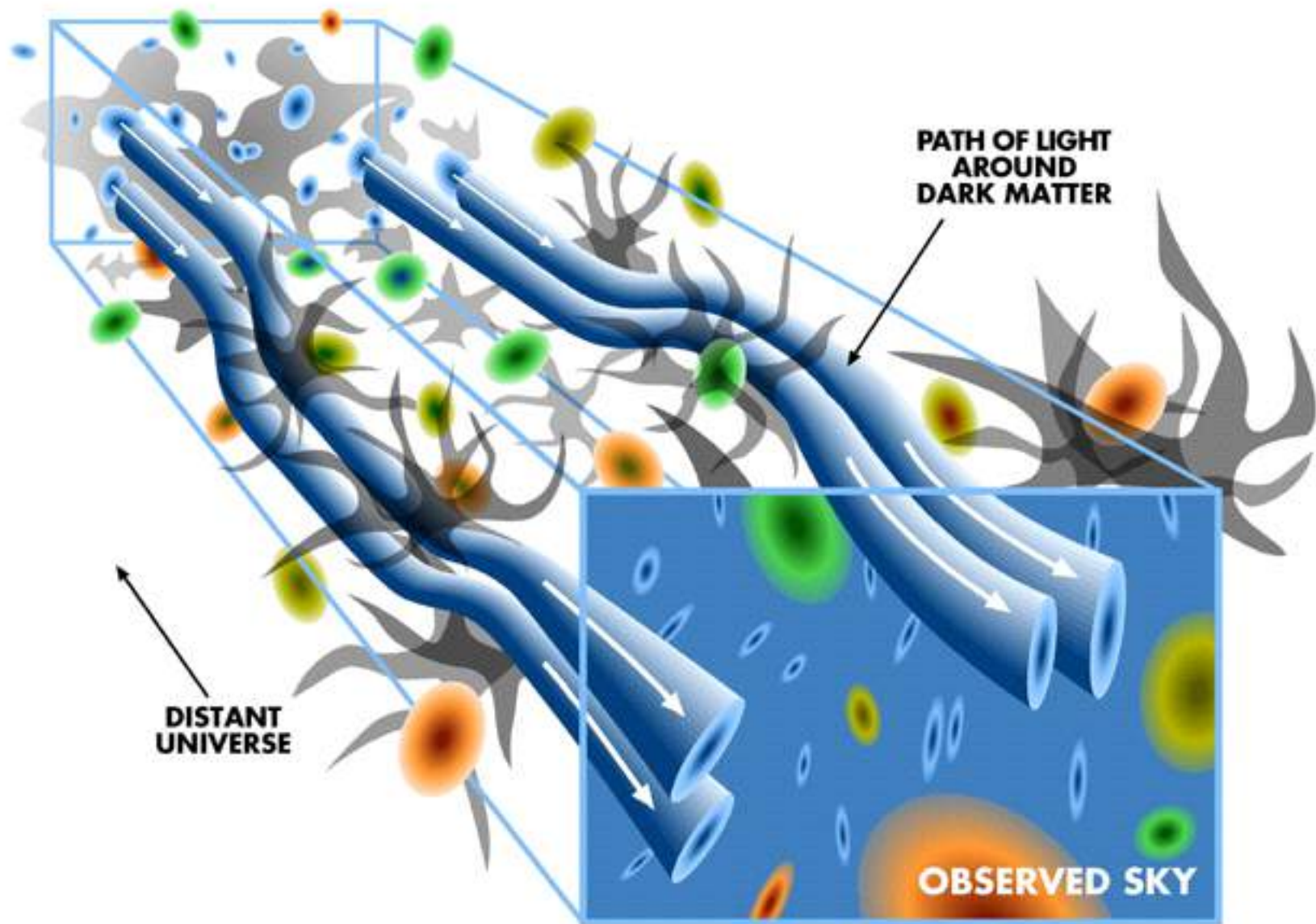
STRONG & WEAK LENSING



STRONG & WEAK LENSING

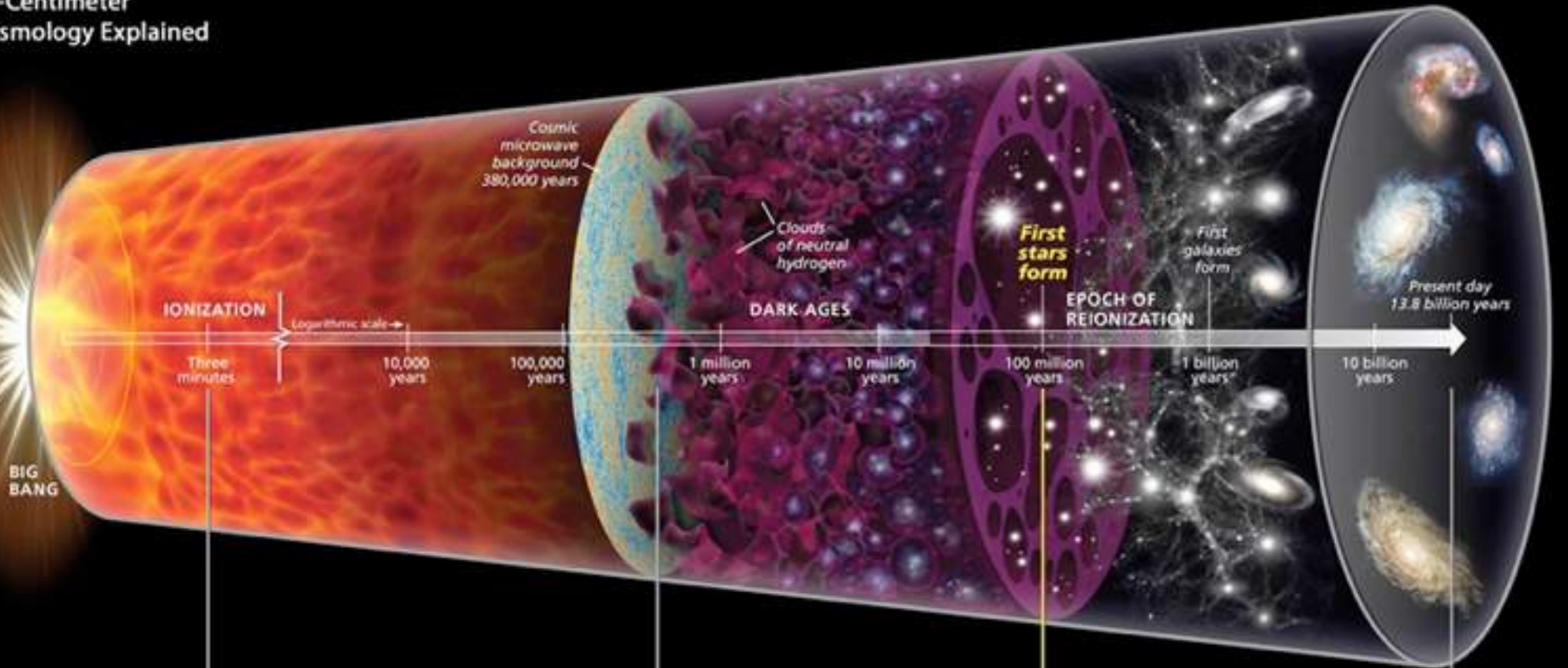


INTO THE DARK AGES...



INTO THE DARK AGES...

21-Centimeter
Cosmology Explained



After the Big Bang, the universe fills with ionized hydrogen, single positive protons.

Proton

As the universe expands, hydrogen clouds cool off. Positive protons combine with negative electrons to create neutral hydrogen. The atoms can shift between two energy states.

Absorbs 21cm photon

HIGHER STATE

LOWER STATE

Electron

Proton

Emits 21cm photon

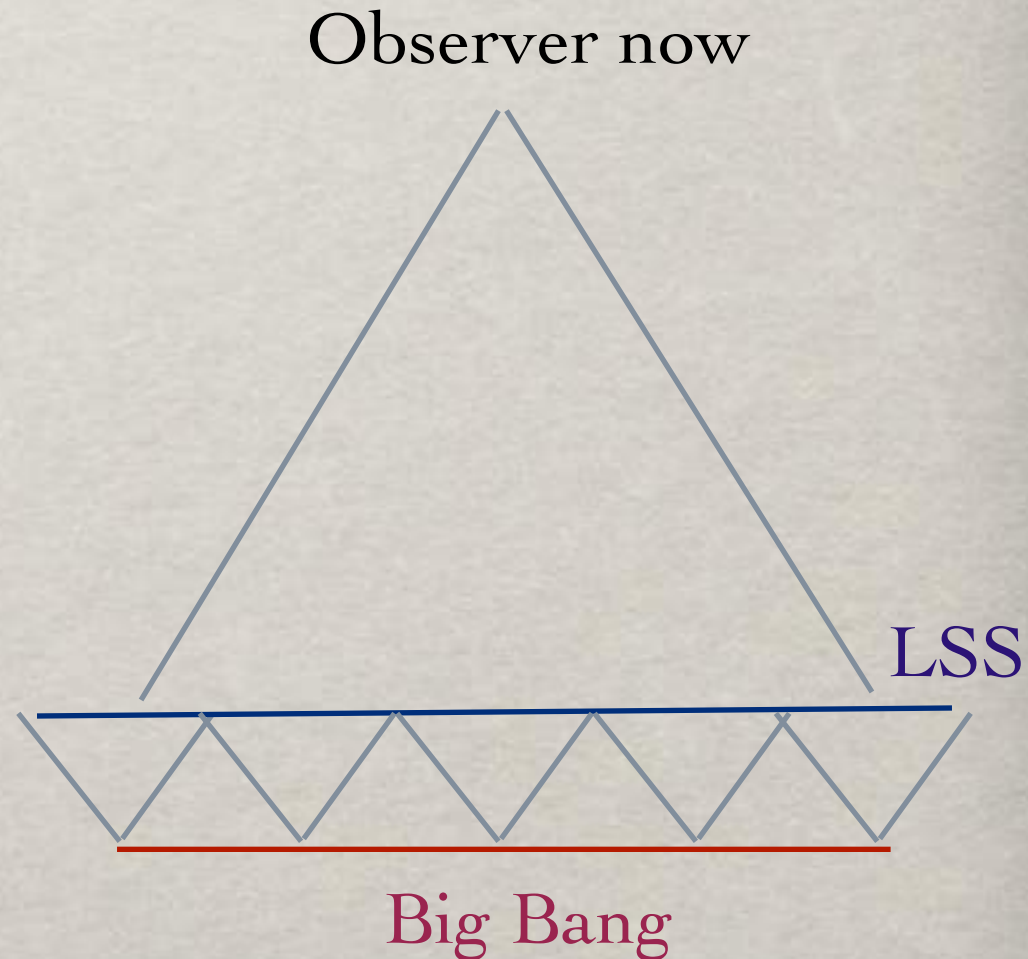
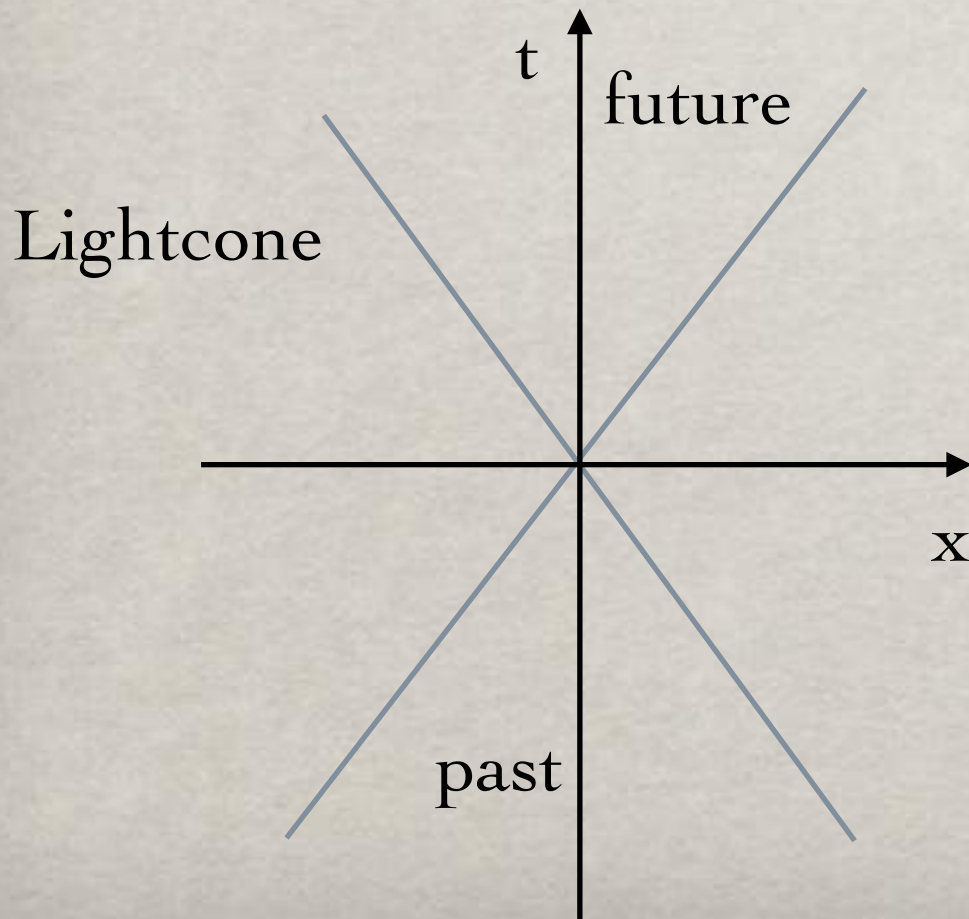
Due to ultraviolet radiation from the first stars, neutral hydrogen atoms lose their electrons and become positively charged again.

Radio telescopes detect the 21cm emissions, now stretched out by the universe's expansion. Whenever they no longer appear, the first stars have formed.

PROBLEMS OF STANDARD COSMOLOGY

PROBLEMS IN STANDARD COSMOLOGY

● Causality/Horizon



PROBLEMS IN STANDARD COSMOLOGY

- Causality/Horizon
- Flatness

$$\frac{d}{dt}(\Omega_{tot} - 1) = -2\frac{\ddot{a}}{aH}(\Omega_{tot} - 1)$$

For decelerating universe $\ddot{a} < 0 \Rightarrow |\Omega_{tot} - 1|$ grows !

Space becomes more and more curved with time...

Instead acceleration brings toward a spatially flat universe !

PROBLEMS IN STANDARD COSMOLOGY

- Causality/Horizon
- Flatness
- Relics/Topological defects

Often too many relics, e.g. topological defects like monopoles, strings or domain walls, are produced and must be diluted

PROBLEMS IN STANDARD COSMOLOGY

- Causality/Horizon
- Flatness
- Relics/Topological defects

- Entropy problem

The present Universe still contains a substantial entropy (in photons), which was much larger in early times...

Where did that come from ?

Non-adiabatic process, i.e. reheating after inflation !

PROBLEMS IN STANDARD COSMOLOGY

- Causality/Horizon
- Flatness
- Relics/Topological defects
- Entropy problem

Inflation solves these problems and sets the initial conditions for Standard Cosmology !