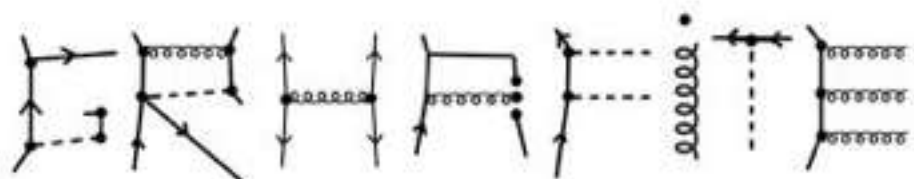




ICTP-SAIFR/FAIR Workshop on mass
Generation in QCD

Recent Developments on the X, Y and Z States



Marina Nielsen



arXiv:1812.08207

Albuquerque, Dias, Khemchandani, Martínez Torres, Navarra, MN, Zanetti

State	m (MeV)	Γ (MeV)	J^{PC}	Process (mode)	experiment	Year
$X(3872)$	3871.69 ± 0.17	< 1.2	1^{++}	$B \rightarrow K(\pi^+ \pi^- J/\psi)$ $p\bar{p} \rightarrow (\pi^+ \pi^- J/\psi) (\dots)$ $B \rightarrow K(\omega J/\psi)$ $B \rightarrow K(D^{*0} \bar{D}^0)$ $B \rightarrow K(\gamma J/\psi)$ $B \rightarrow K(\gamma \psi(2S))$ $e^+ e^- \rightarrow \pi^+ \pi^- J/\psi$ $pp \rightarrow (\pi^+ \pi^- J/\psi) (\dots)$	Belle [22–24], BaBar [25] CDF [26–28], DØ [29] Belle [30], BaBar [31] Belle [32, 33], BaBar [34] Belle [30], BaBar [35, 36] BaBar [36], LHCb [37] BESIII [38] LHCb [39, 40], CMS [41]	2003
$Z_c^+(3900)$	3886.6 ± 2.4	28.2 ± 2.6	1^{+-}	$Y(4260) \rightarrow (J/\psi \pi^+) \pi^-$ $Y(4260) \rightarrow (D \bar{D}^*)^+ \pi^-$	BESIII [42], Belle [43], CLEO-c [44]] BESIII [45]	2013
$Y(3940)$	3918.4 ± 1.9	20 ± 5	$0/2^{++}$	$B \rightarrow K(J/\psi \omega)$ $e^+ e^- \rightarrow e^+ e^- (\omega J/\psi)$	Belle [46], BaBar [31, 47] Belle [48], BaBar [49]	2004
$X(3940)$	3942_{-8}^{+9}	37_{-17}^{+27}	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (\dots)$ $e^+ e^- \rightarrow J/\psi (DD^*)$	Belle [50] Belle [51]	2005
$Y(4008)$	3891 ± 42	255 ± 42	1^{--}	$e^+ e^- \rightarrow \pi^+ \pi^- J/\psi$	Belle [43, 52], BESIII [53]	2007
$Z_c^+(4020)$	4024.1 ± 1.9	13 ± 5	$?^{?-}$	$e^+ e^- \rightarrow \pi^- (\pi^+ h_c)$ $Y(4260) \rightarrow \pi^- (D^* \bar{D}^*)^+$	BESIII [54] BESIII [55]	2013
$Z_1^+(4050)$	4051_{-43}^{+24}	82_{-55}^{+51}	$?^{?-}$	$B \rightarrow K(\pi^+ \chi_{c1}(1P))$	Belle [56], BaBar [57]	2008
$Z_c^+(4055)$	4054 ± 3	45	$(?^{?-})$	$e^+ e^- \rightarrow \pi^- (\pi^+ \psi(2S))$	Belle [58]	2014
$Z_c^-(4100)$	$(4096 \pm_{-32}^{+28})$	152_{-45}^{+70}	$0^{++}/1^{-+}$	$B^0 \rightarrow K^+ (\pi^- \eta_c(1S))$	LHCb [59]	2018
$Y(4140)$	4146.8 ± 2.4	22_{-7}^{+8}	1^{++}	$B \rightarrow K(\phi J/\psi)$	CDF [60, 61], D0 [62], LHCb [63], BESIII [64, 65]	2009
$X(4160)$	4156_{-25}^{+29}	139_{-65}^{+113}	$?^{?+}$	$e^+ e^- \rightarrow J/\psi (D^* \bar{D}^*)$	Belle [51]	2007
$Z_c^+(4200)$	4196_{-30}^{+35}	370_{-110}^{+99}	1^{+-}	$B \rightarrow K(\pi^+ J/\psi)$	Belle [66]	2014
$Y(4220)$	4218_{-4}^{+5}	59_{-10}^{+12}	1^{--}	$e^+ e^- \rightarrow \chi_{c0} \omega$ $e^+ e^- \rightarrow h_c \pi^+ \pi^-$ $e^+ e^- \rightarrow \psi(2S) \pi^+ \pi^-$ $e^+ e^- \rightarrow D^0 D^{*-} \pi^+$	BESIII [67] BESIII [68] BESIII [69] BESIII [70]	2014

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$Z_2^+(4250)$	4248_{-45}^{+185}	177_{-72}^{+321}	$?^{?+}$	$B \rightarrow K(\pi^+ \chi_{c1}(1P))$	Belle [56], BaBar [57]	2008
$Y(4260)$	4230 ± 8	55 ± 19	1^{--}	$e^+e^- \rightarrow \pi^+\pi^- J/\psi$ $e^+e^- \rightarrow K^+K^- J/\psi$ $e^+e^- \rightarrow \pi^0\pi^0 J/\psi$ $e^+e^- \rightarrow Z_c(3900)^\pm \pi^\mp$	BaBar [71, 72], CLEO-c [73], Belle [43, 52], BESIII [53] CLEO-c [74], BESIII [45] CLEO-c [74] Belle [43], BESIII [42]	2005
$X(4350)$	$4350.6_{-5.1}^{+4.6}$	$13.3_{-10.0}^{+18.4}$	$?^{?+}$	$e^+e^- \rightarrow \phi J/\psi$	Belle [75]	2009
$Y(4360)$	4368 ± 13	96 ± 7	1^{--}	$e^+e^- \rightarrow \pi^+\pi^- \psi(2S)$ $e^+e^- \rightarrow \pi^+\pi^- J/\psi$	BaBar [76, 77], Belle [58, 78], BESIII [69] BESIII [53]	2007
$Y(4390)$	$4391.5_{-7.8}^{+7.3}$	$139.5_{-20.7}^{+16.3}$	1^{--}	$e^+e^- \rightarrow h_c \pi^+\pi^-$	BESIII [68]	2016
$Z^+(4430)$	4478_{-18}^{+15}	181 ± 31	1^{+-}	$B \rightarrow K^-(\pi^+ \psi(2S))$ $B \rightarrow K^-(\pi^+ J/\psi)$	Belle [79–81], BaBar [82], LHCb [83] Belle [66], BaBar [82]	2007
$X(4630)$	4634_{-11}^{+9}	92_{-32}^{+41}	1^{--}	$e^+e^- \rightarrow \Lambda_c^+ \Lambda_c^-$	Belle [84]	2008
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first charged one \rightarrow not a $c\bar{c}$ state

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first charged one \rightarrow not a $c\bar{c}$ state



arXiv:0905.2869

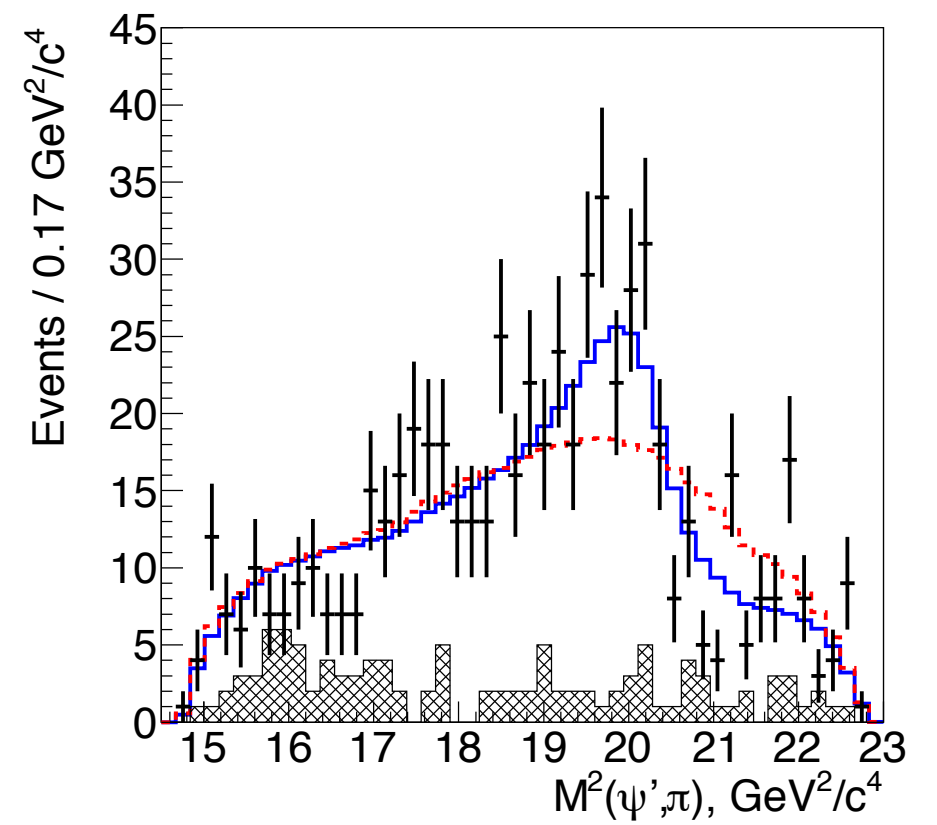
searched $Z^-(4430)$ in 4 decay modes:

no conclusive
evidence for the existence of $Z^+(4430)$ seen by
Belle



arXiv:1306.4894

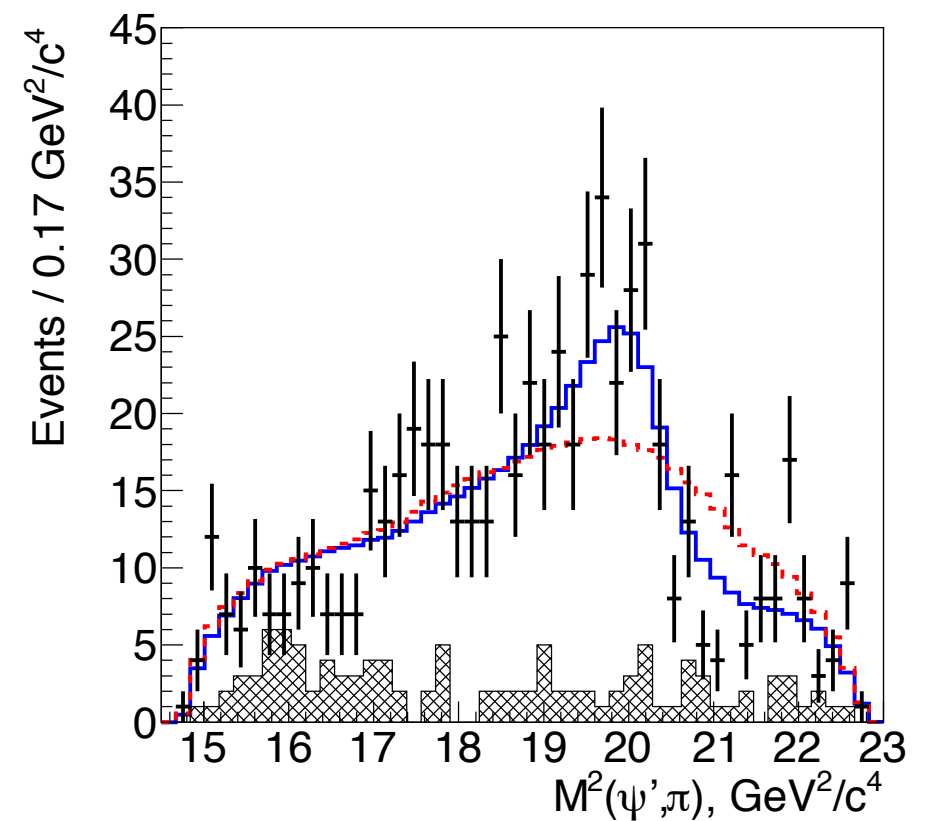
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 $Z^+(4430)$ with
 6.1σ and $J^P=1^+$





arXiv:1306.4894

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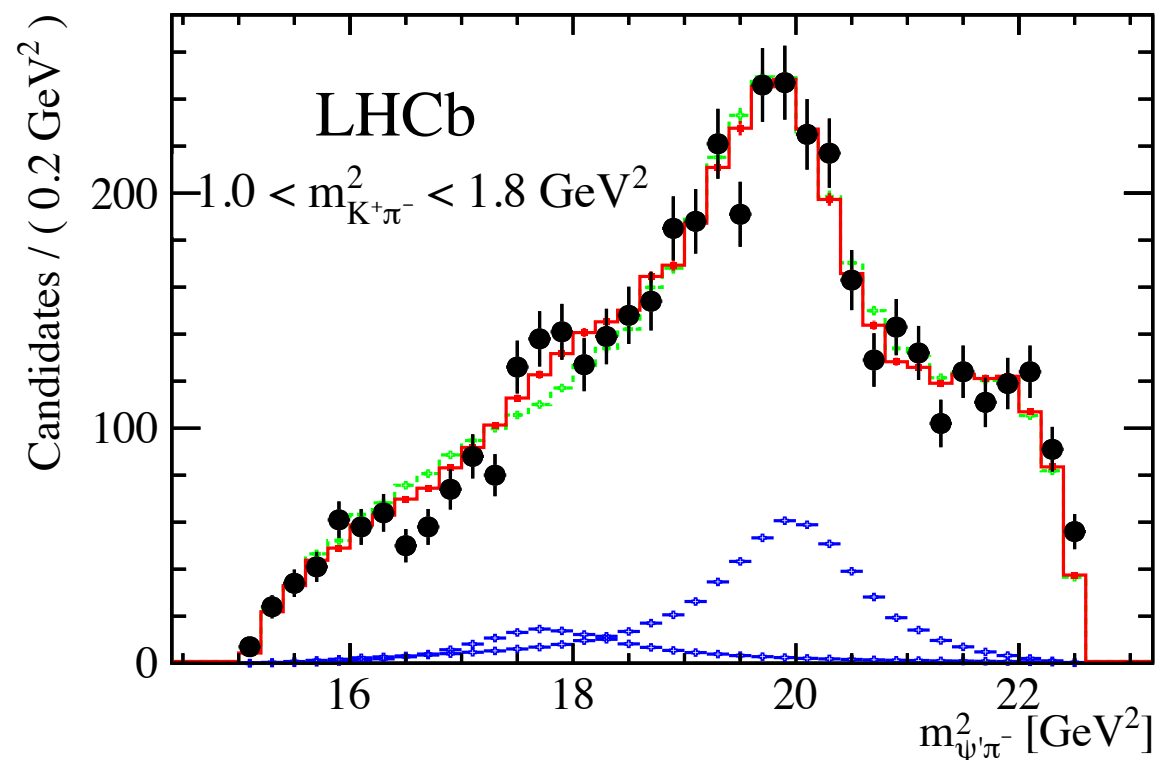


arXiv:1404.1903

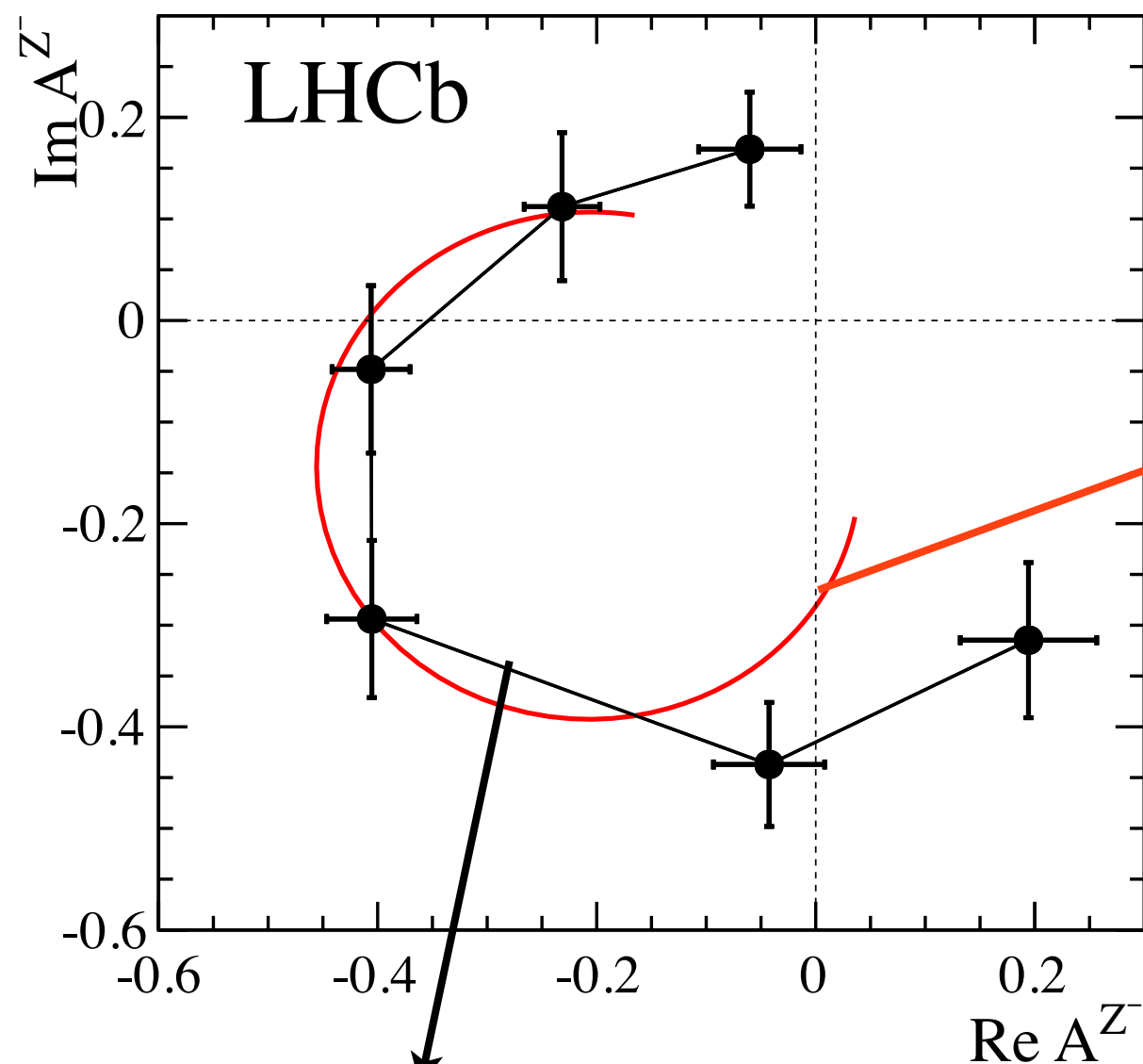
has confirmed the observation of
 $Z^+(4430)$ with 13.9σ and $J^+ = 1^+$

$$M = (4475 \pm 7 \pm 20) \text{ MeV}$$

$$\Gamma = (172 \pm 13 \pm 35) \text{ MeV}$$



(arXiv:1404.1903) also did the first attempt to demonstrate the resonant behavior of $Z^+(4430)$: the Breit-Wigner amplitude was replaced by a combination of independent complex amplitudes at six equally spaced points in $m_{\Psi'\pi}$ range covering the $Z^+(4430)$ peak region



Breit-Wigner

the Argand diagram is consistent with a rapid phase transition, as expected for a resonance

fitted values of Z
amplitude in six $m_{\Psi'\pi}$ bins

$Z^+(4430)$

threshold effect in the $D_1 D^*$ channel

Rosner, arXiv:0708.3496

four-quark radial excitation with $J^{PC} = 1^{+-}$

Maiani, Polosa & Riquer, arXiv:0708.3997

radial excitation of $\Lambda_c - \Sigma_c^0$ bound state

Qiao, arXiv:0709.4066

$D_1 D^*$ molecular state with $J^P = 0^-, 1^-, 2^-$

Meng & Cheng, arXiv:0708.4222

cusp in the $D_1 D^*$ channel

Bugg, arXiv:0709.1254

$D_1 D^*$ molecular state with $J^P = 1^+$

He, arXiv:1410.8645

$D_1 D^*$ or $D_2 D^*$ molecular state with $J^P = 1^+$

Ma, Liu, Liu, Zhu, arXiv:1404.3450; Barnes,

Close, Swanson, arXiv:1409.6651

not a real
state

$Z^+(4430)$

before LHCb



threshold effect in the $D_1 D^*$ channel
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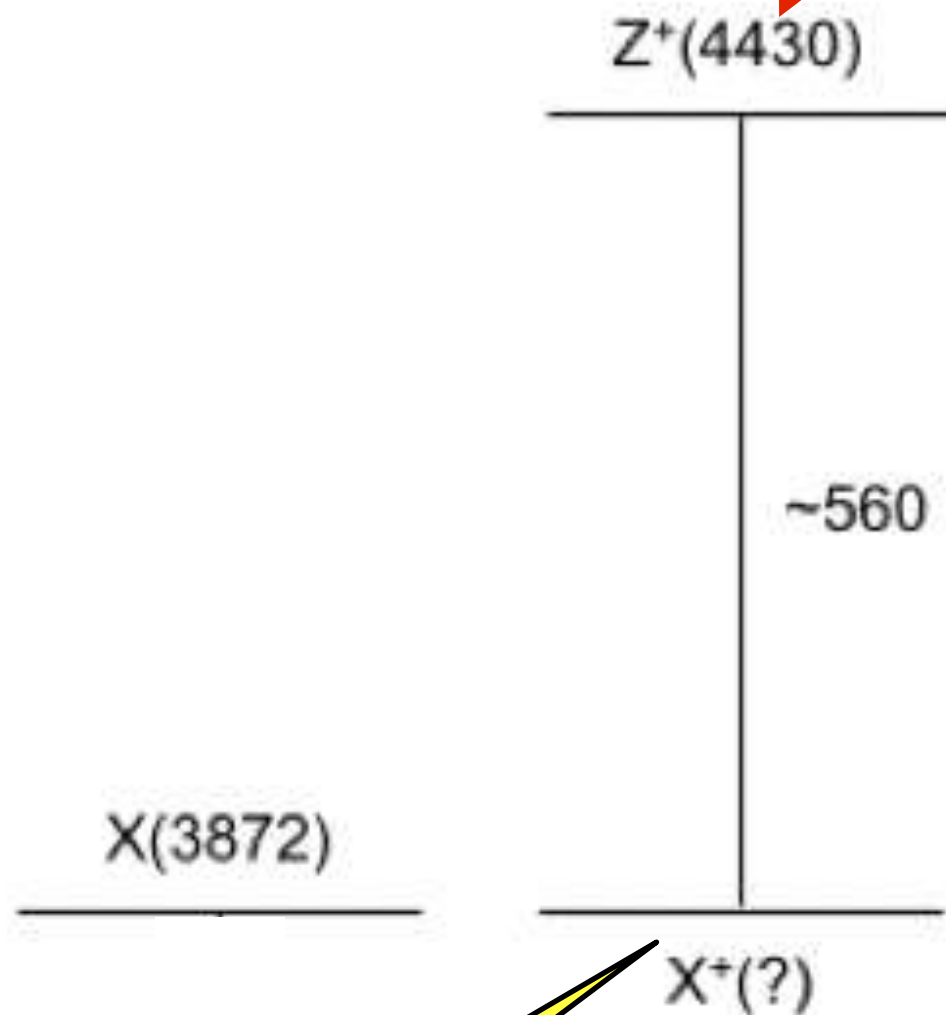
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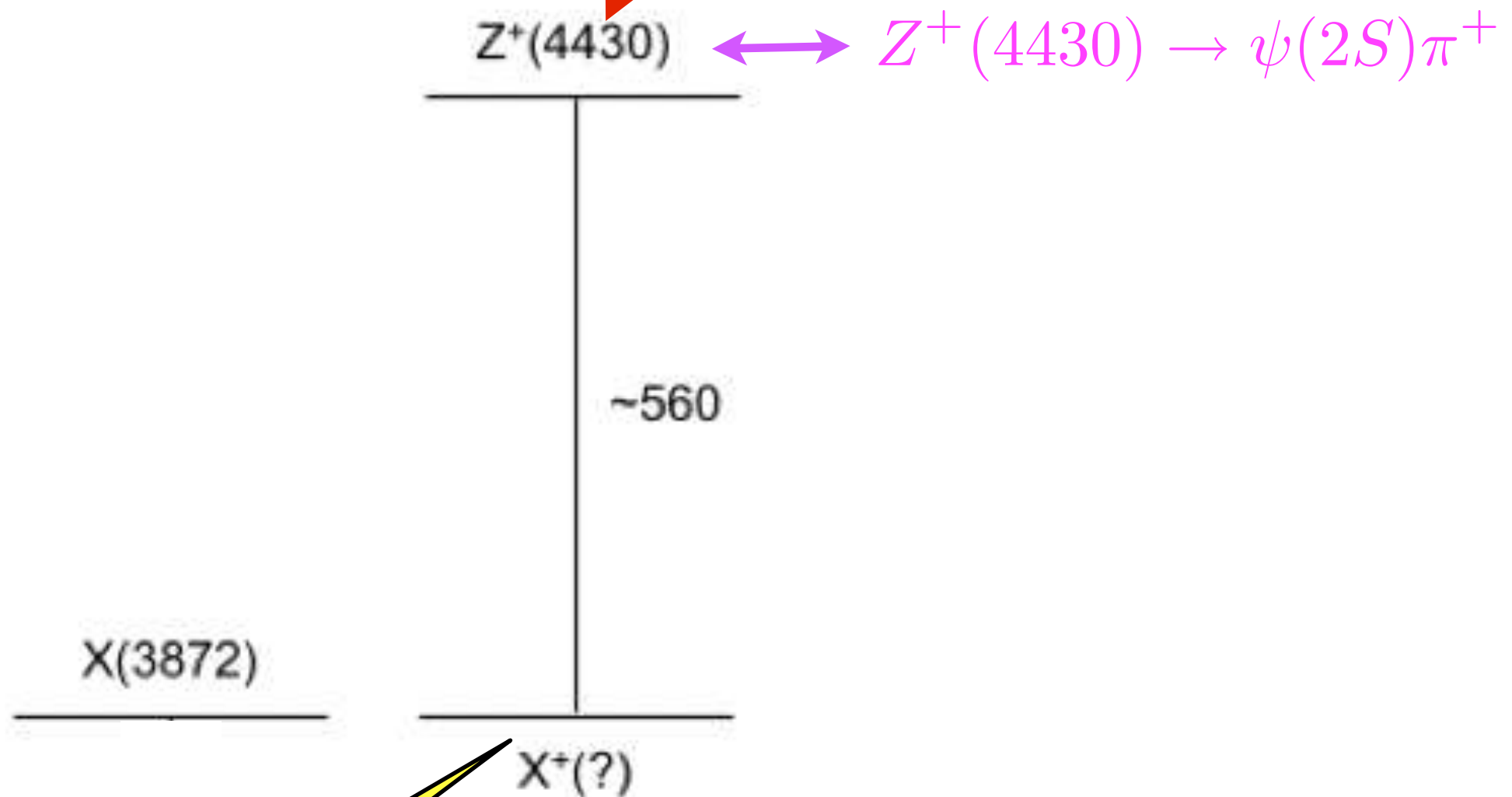


Maiani et al. (arXiv:0708.3997) : four-quark radial excitation of the I^+ charged state (X(3872) partner)



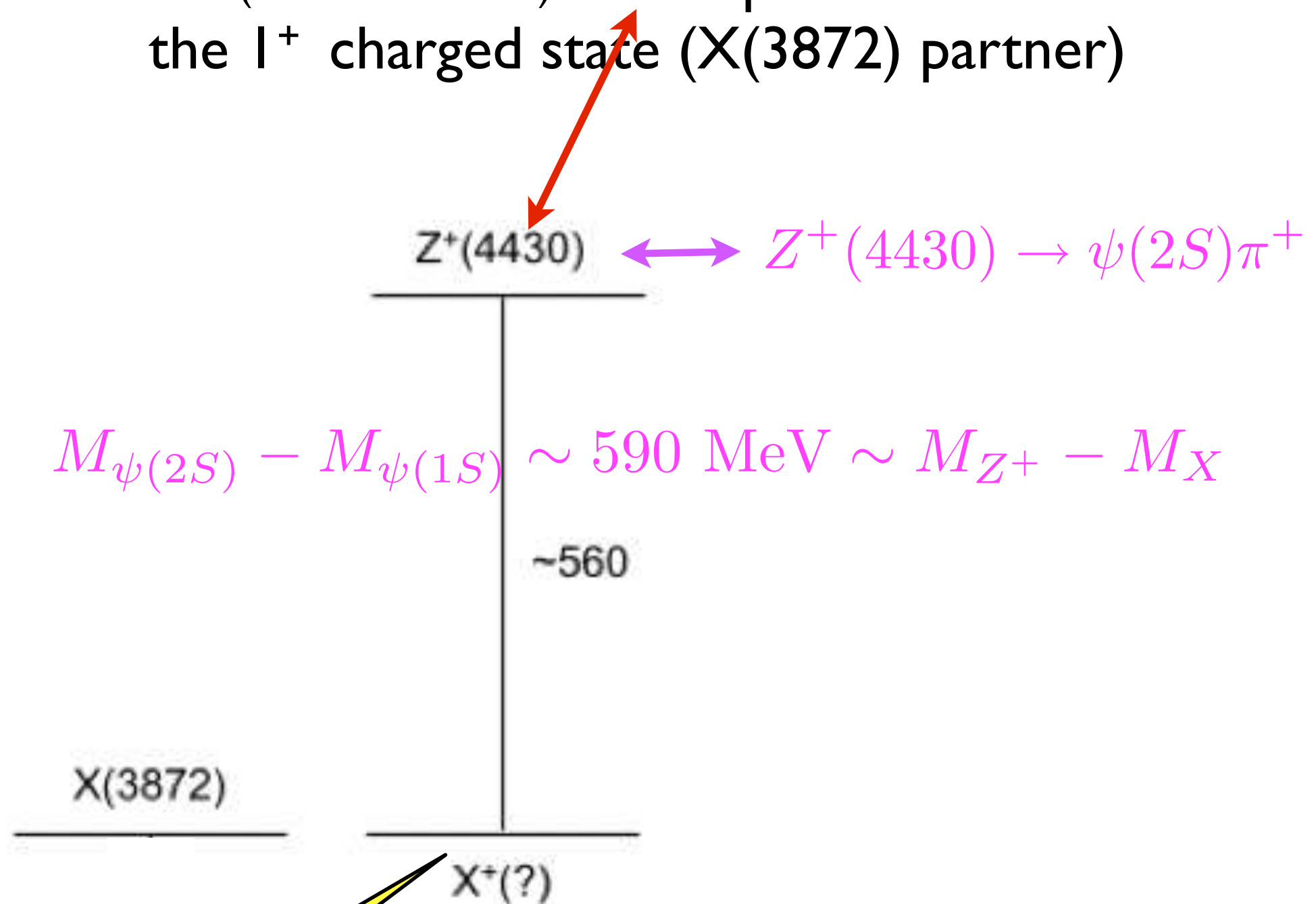
should be seen in $J/\psi\pi$
decay mode

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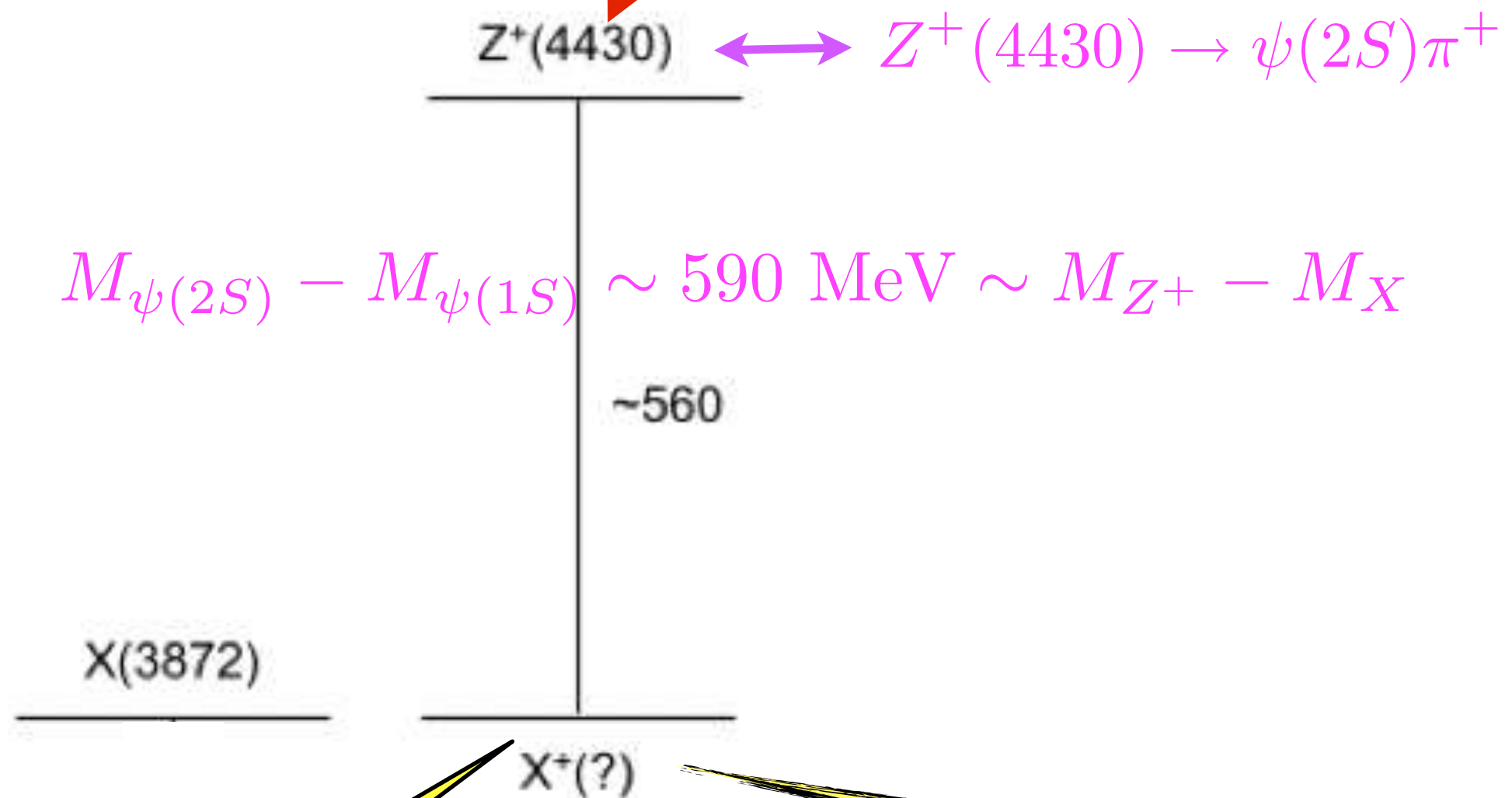
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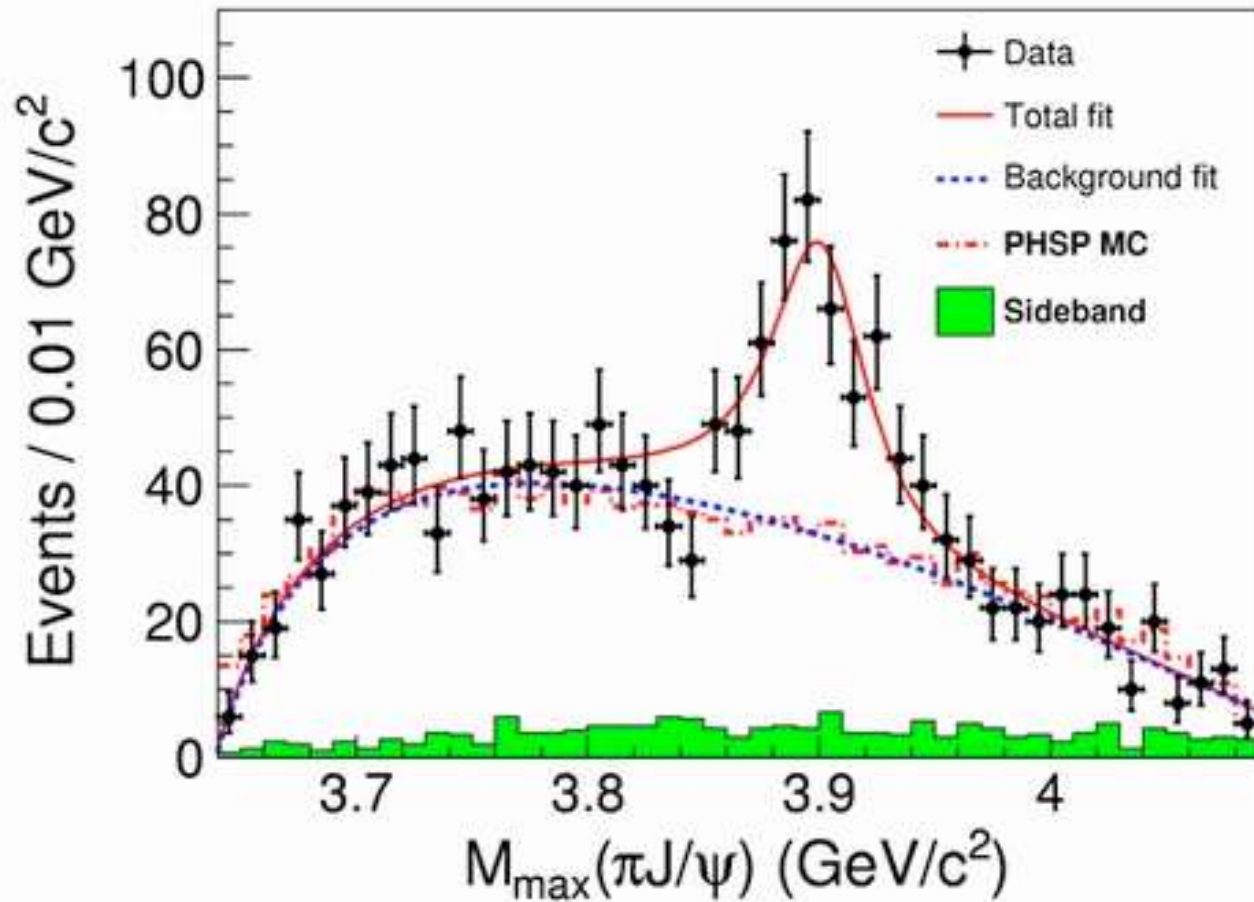
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BES III



2013

Charged Charmonium states discovered in 2013



$Z_c^+(3900)$

BES III

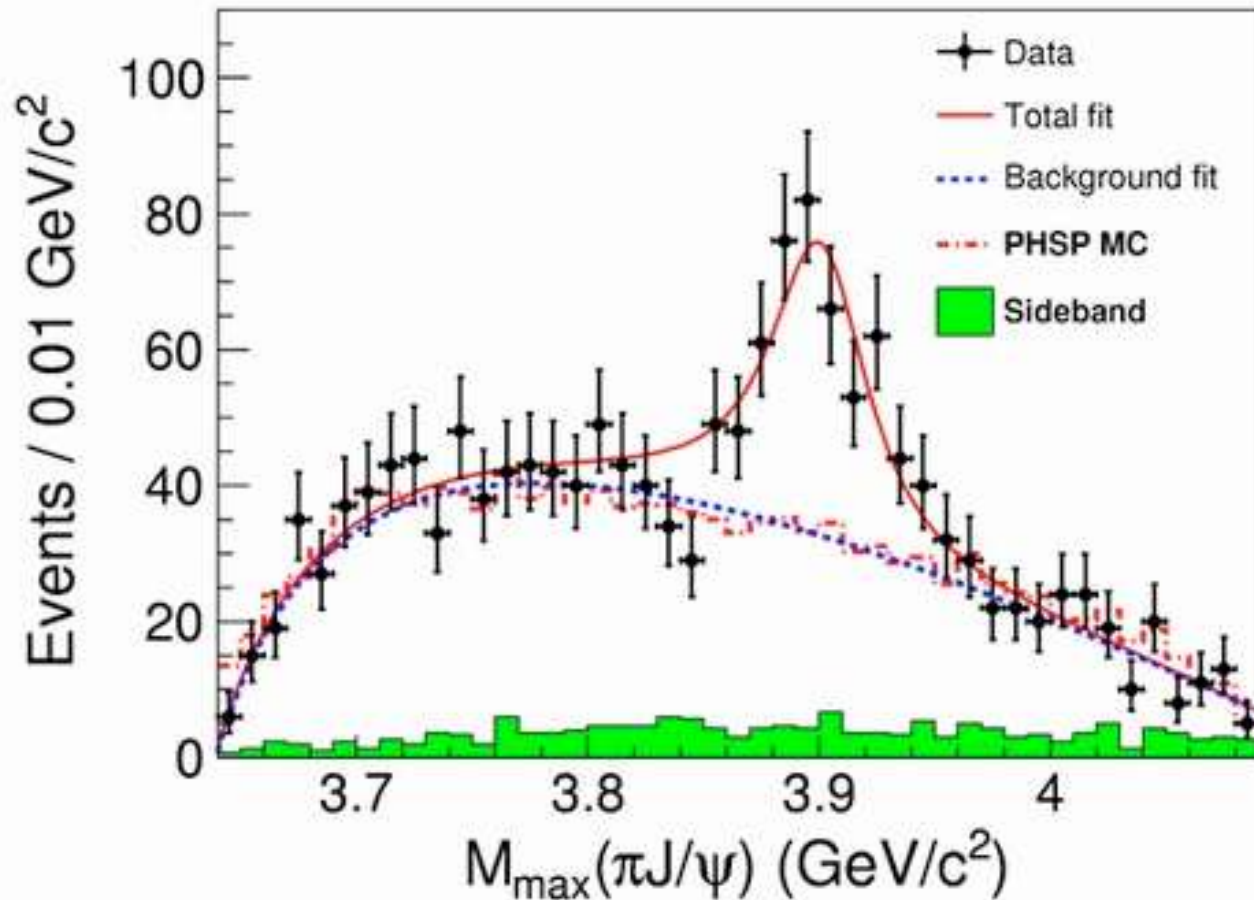


arXiv:1303.5949

arXiv:1304.0121

$$Y(4260) \rightarrow (J/\psi \pi^+) \pi^-$$

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$Z_c^+(3900)$

BES III



arXiv:1303.5949

arXiv:1304.0121

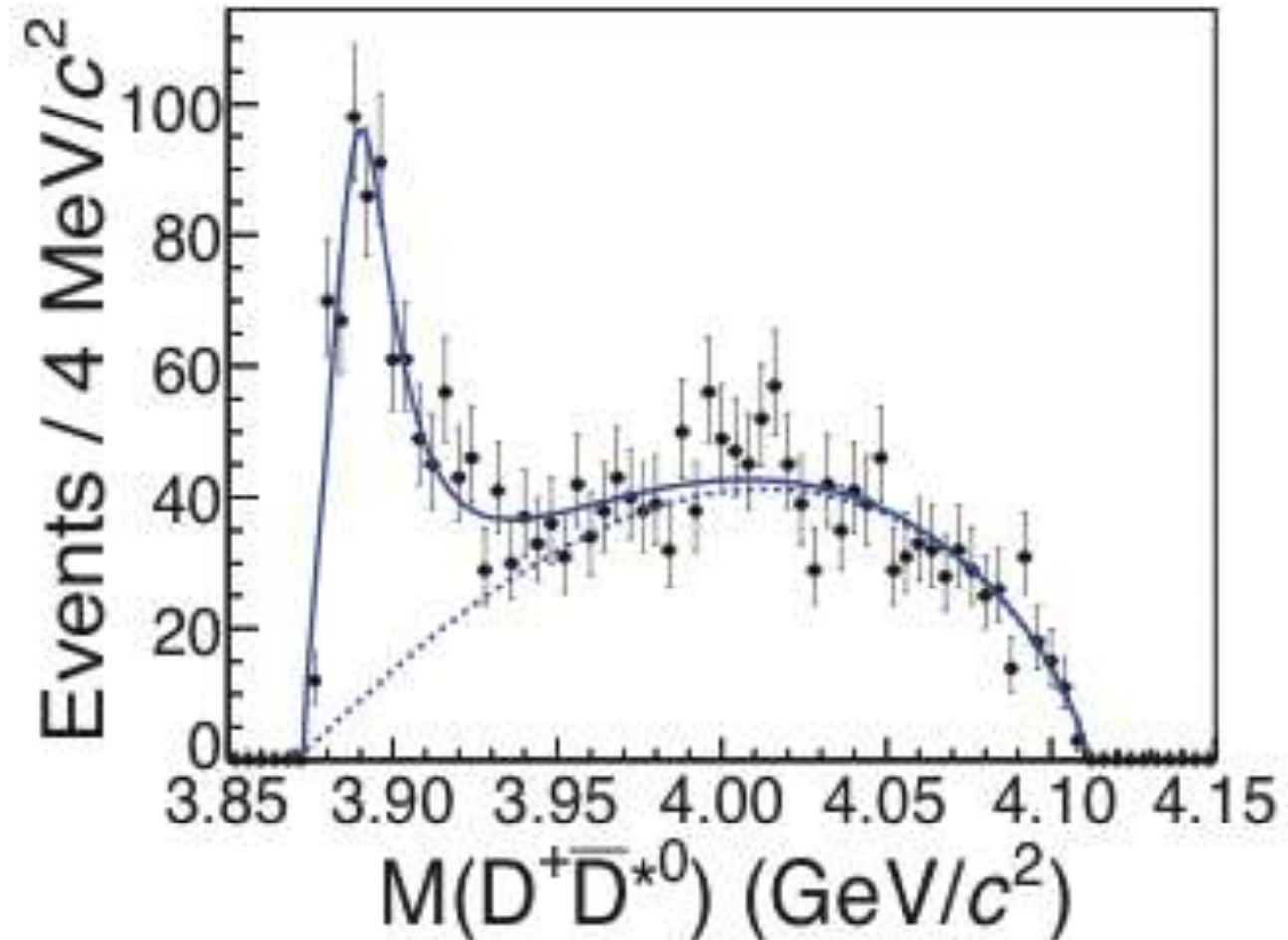
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$Z_c^+(3885)$

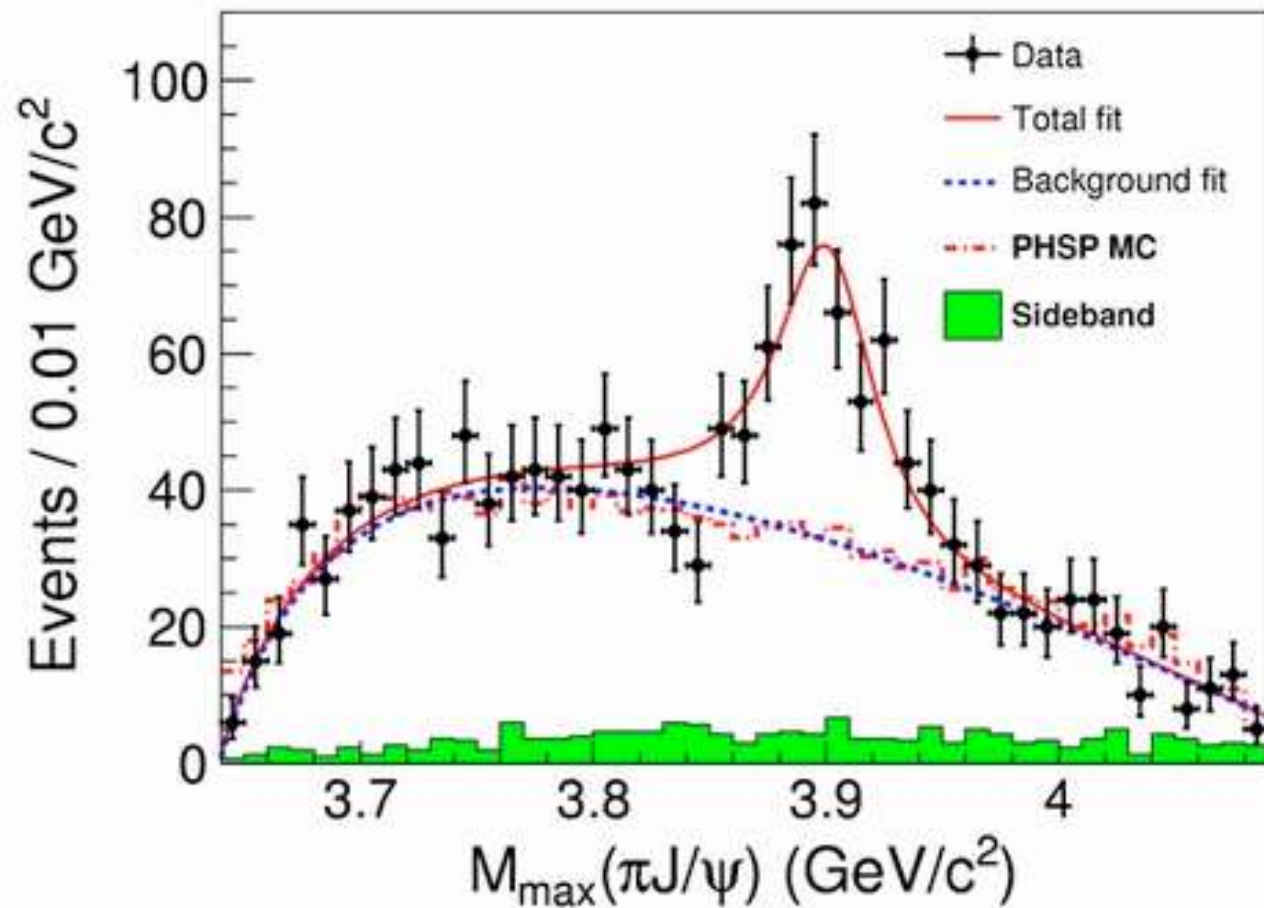
BES III

arXiv:1310.1163

$$e^+ e^- \rightarrow \pi^\pm (D \bar{D}^*)^\mp @ \sqrt{s} = 4.26 \text{ GeV}$$

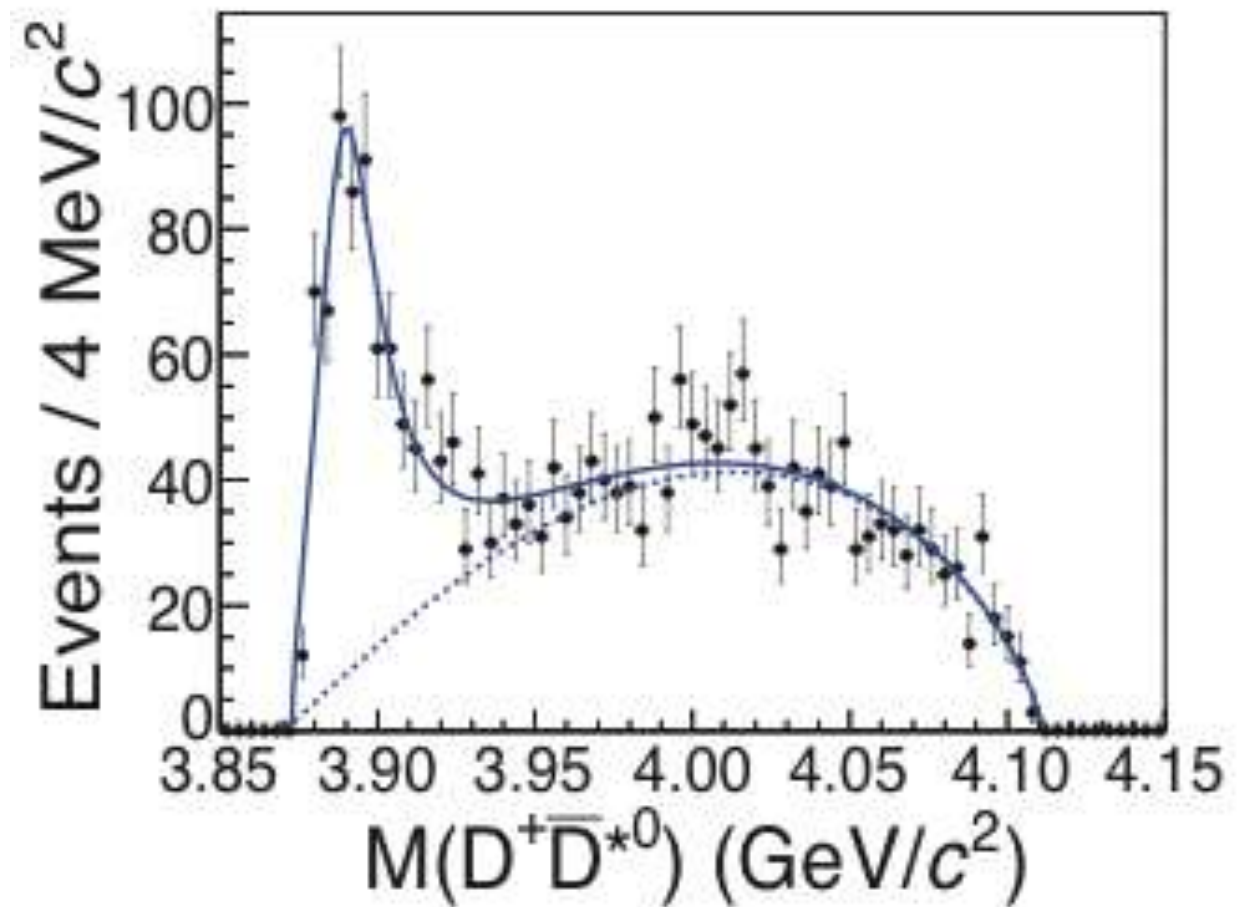


$Z_c^+(3900)$ and $Z_c^+(3885)$ could be the same state?



$$M = (3890 \pm 3.6 \pm 4.9) \text{ MeV}$$

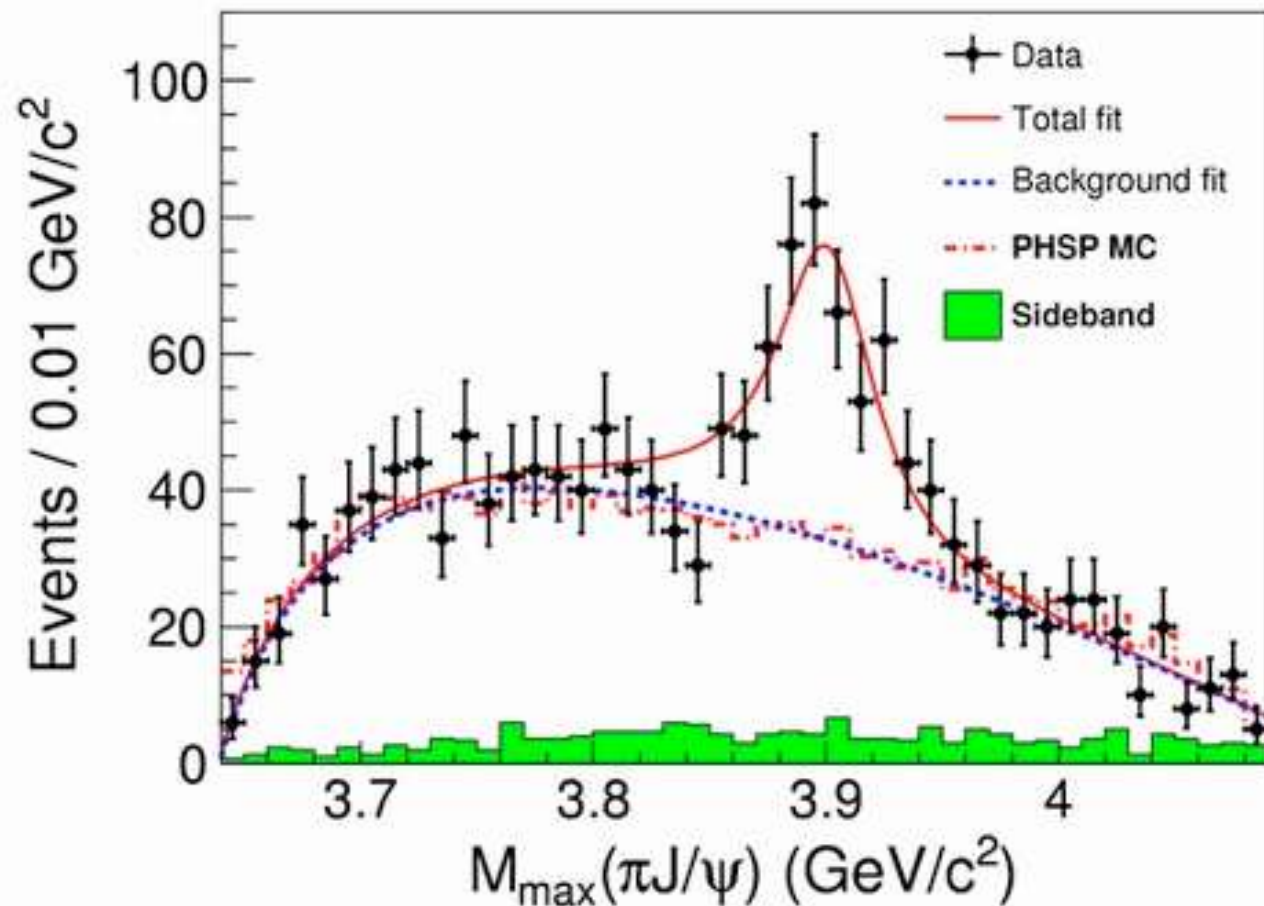
$$\Gamma = (46 \pm 10 \pm 20) \text{ MeV}$$



$$M = (3883.9 \pm 1.5 \pm 4.2) \text{ MeV}$$

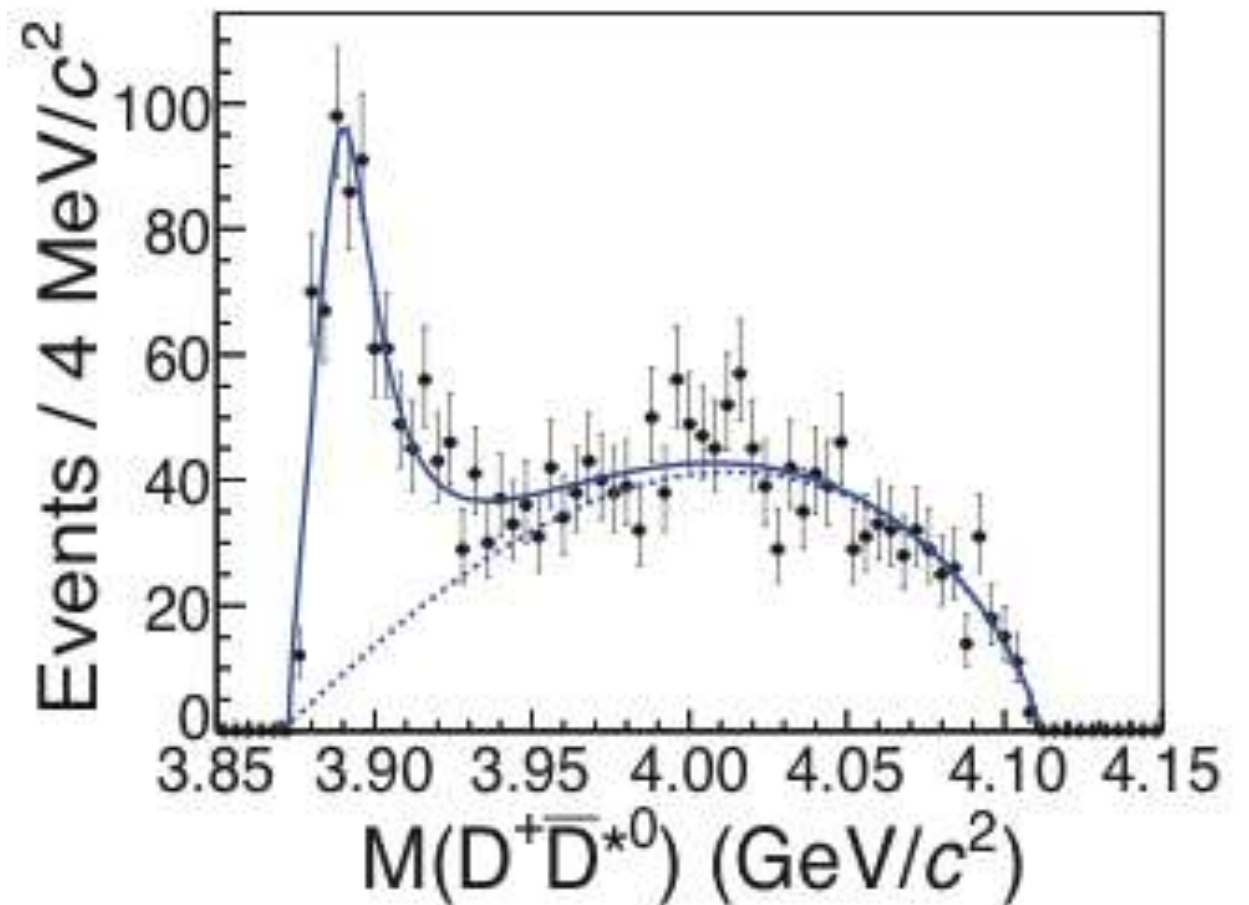
$$\Gamma = (24.8 \pm 3.3 \pm 11.0) \text{ MeV}$$

$Z_c^+(3900)$ and $Z_c^+(3885)$ could be the same state?



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BES III

arXiv:1310.1163

Assuming $Z_c(3885)$ and $Z_c(3900)$
to be the same state \Rightarrow

$$\frac{\Gamma(Z_c(3885) \rightarrow D \bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 6.2 \pm 1.1 \pm 2.7$$

$Z_c(3900)$ DECAY MODES

	Mode	Fraction (Γ_i/Γ)
Γ_1	$J/\psi \pi$	seen
Γ_2	$h_c \pi^\pm$	not seen
Γ_3	$\eta_c \pi^+ \pi^-$	not seen
Γ_4	$(D D^*)^\pm$	seen
Γ_5	$D^0 D^{*-} + \text{c.c.}$	seen
Γ_6	$D^- D^{*0} + \text{c.c.}$	seen
Γ_7	$\omega \pi^\pm$	not seen
Γ_8	$J/\psi \eta$	not seen
Γ_9	$D^+ D^{*-} + \text{c.c.}$	seen
Γ_{10}	$D^0 \bar{D}^{*0} + \text{c.c.}$	seen

PDG

$Z_c(3900)$ DECAY MODES

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Γ_3	$\eta_c \pi^+ \pi^-$	not seen
Γ_4	$(D D^*)^\pm$	seen
Γ_5	$D^0 D^{*-} + \text{c.c.}$	seen
Γ_6	$D^- D^{*0} + \text{c.c.}$	seen
Γ_7	$\omega \pi^\pm$	not seen
Γ_8	$J/\psi \eta$	not seen
Γ_9	$D^+ D^{*-} + \text{c.c.}$	seen
Γ_{10}	$D^0 \bar{D}^{*0} + \text{c.c.}$	seen

$Z_c(3900)$

$Z_c(3885)$

QCDSR Results for decay widths of the $Z_c^+(3900)$

Dias, Navarra, MN, Zanetti
arXiv:1304.6433

Vertex	coupling constant (GeV)	decay width (MeV)
$Z_c^+(3900) J/\psi \pi^+$	3.89 ± 0.56	29.1 ± 8.2
$Z_c^+(3900) \eta_c \rho^+$	4.85 ± 0.81	27.5 ± 8.5
$Z_c^+(3900) D^+ \bar{D}^{*0}$	2.5 ± 0.3	3.2 ± 0.7
$Z_c^+(3900) \bar{D}^0 D^{*+}$	2.5 ± 0.3	3.2 ± 0.7

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$Z_c^+(3900) D^+ \bar{D}^{*0}$	2.5 ± 0.3	3.2 ± 0.7
$Z_c^+(3900) \bar{D}^0 D^{*+}$	2.5 ± 0.3	3.2 ± 0.7

$$\frac{\Gamma(Z_c(3900) \rightarrow D \bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 0.22 \pm 0.12$$

same result as in Maiani et al.
using a tetraquark model
arXiv:1303.6857

QCDSR Results for decay widths of the $Z_c^+(3900)$

Dias, Navarra, MN, Zanetti
arXiv:1304.6433

Vertex	coupling constant (GeV)	decay width (MeV)
$Z_c^+(3900) J/\psi \pi^+$	3.89 ± 0.56	29.1 ± 8.2
$Z_c^+(3900) \eta_c \rho^+$	4.85 ± 0.81	27.5 ± 8.5
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$$\frac{\Gamma(Z_c(3900) \rightarrow D \bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 0.22 \pm 0.12$$















same result as in Maiani et al.
using a tetraquark model
arXiv:1303.6857

BES III














$$\frac{\Gamma(Z_c(3885) \rightarrow D \bar{D}^*)}{\Gamma(Z_c(3900) \rightarrow \pi J/\psi)} = 6.2 \pm 1.1 \pm 2.7$$

QCDSR and tetraquark model \Rightarrow not the same state!














up to now: 8 charmonium charged states

 $Z^+(4430)$ 2007   	 $Z_1^+(4050)$ 2008 	 $Z_2^+(4250)$ 2008 
 $Z_c^+(3900)$ 2013 	$Z_c^+(4020)$ 2013 	$Z_c^+(4055)$ 2014 
$Z_c^+(4200)$ 2014 	$Z_c^+(4100)$ 2018  3 σ ! needs confirmation	

up to now: 8 charmonium charged states

 $Z^+(4430)$ 2007  	 $Z_1^+(4050)$ 2008 $M=(4051 \pm 35)\text{MeV}$ $\Gamma=(82 \pm 52)\text{MeV}$ $\pi^+\chi_{c1}$ 	 $Z_2^+(4250)$ 2008 
 $Z_c^+(3900)$ 2013 	$Z_c^+(4020)$ 2013 	$Z_c^+(4055)$ 2014 $M=(4054 \pm 3)\text{MeV}$ $\Gamma=(45 \pm 15)\text{MeV}$ $\pi^+\Psi(2S)$ 
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Y ($J^{PC}=1^-$) Family

State	Name in PDG	Decay channel	Experiment	Year
Y(4220)	$\psi(4230)$	$Y(4220) \rightarrow \chi_{c0} \omega$	BESIII [67]	2015
		$Y(4220) \rightarrow h_c \pi^+ \pi^-$	BESIII [68]	2017
		$Y(4220) \rightarrow \psi(2S) \pi^+ \pi^-$	BESIII [69]	2017
		$Y(4220) \rightarrow D^0 D^{*-} \pi^+$	BESIII [70]	2018
Y(4260)	$\psi(4260)$	$Y(4260) \rightarrow J/\psi \pi^+ \pi^-$	BaBar [71, 72]; CLEO-c [73]; Belle [43, 52]	2005
		$Y(4260) \rightarrow J/\psi \pi^0 \pi^0$	CLEO-c [74]	2006
		$Y(4260) \rightarrow J/\psi K^+ K^-$	CLEO-c [74]; Belle [201, 202]	2006
		$Y(4260) \rightarrow J/\psi f_0(980)$	BaBar [72]	2012
		$Y(4260) \rightarrow Z_c(3900)^\pm \pi^\mp$	Belle [43]; BESIII [42]	2013
		$Y(4260) \rightarrow J/\psi \pi^+ \pi^-$	BESIII [53]	2017
Y(4360)	$\psi(4360)$	$Y(4360) \rightarrow \psi(2S) \pi^+ \pi^-$	Belle [58, 78]; BaBar [76, 77]; BESIII [69]	2007
		$Y(4360) \rightarrow J/\psi \pi^+ \pi^-$	BESIII [53]	2017
Y(4390)	$\psi(4390)$	$Y(4390) \rightarrow h_c \pi^+ \pi^-$	BESIII [68]	2017
		$Y(4390) \rightarrow \psi(2S) \pi^+ \pi^-$	BESIII [69]	2017
Y(4660)	$\psi(4660)$	$Y(4660) \rightarrow \psi(2S) \pi^+ \pi^-$	Belle [58, 78]; BaBar [77]	2007
		$Y(4660) \rightarrow \Lambda_c^+ \Lambda_c^-$	BESIII [84]	2008

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first one

last one

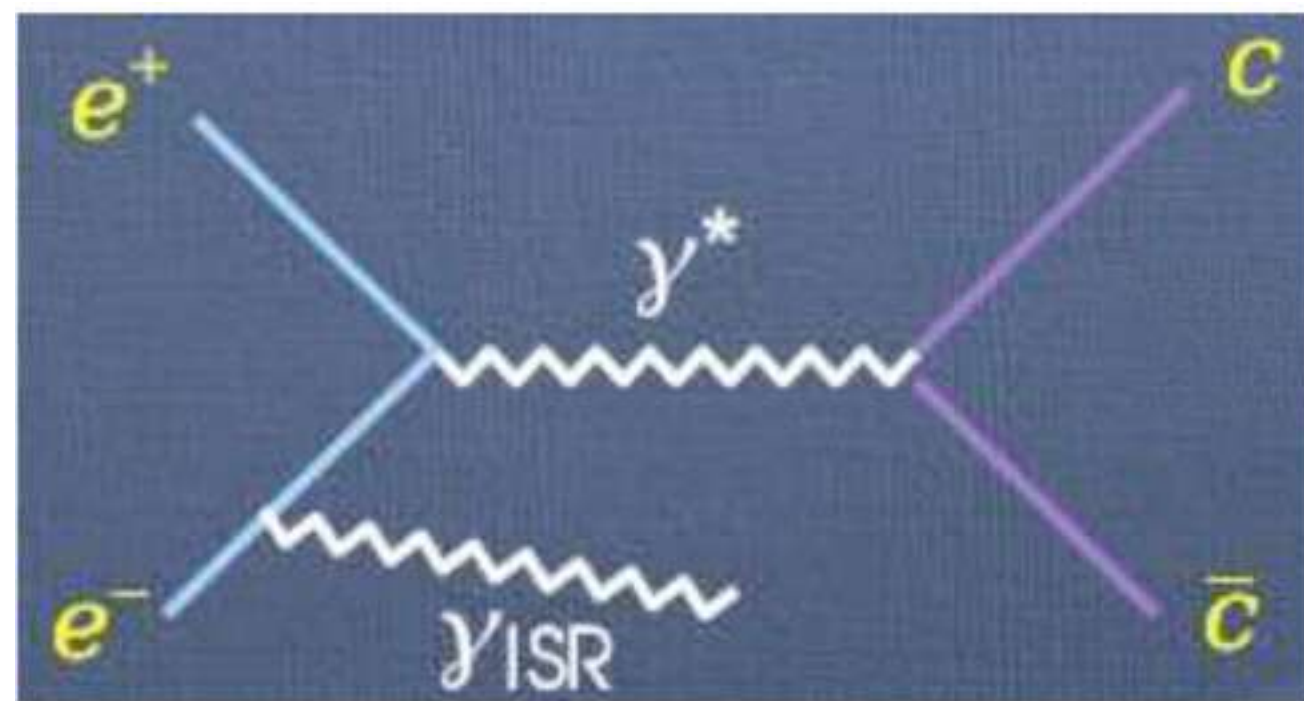
First three states

$e^+e^- \rightarrow 1^{--}$ **Final States**

via Initial State Radiation (ISR)

$$e^+e^- \rightarrow \gamma_{ISR}(c\bar{c})$$

data collected at 10.6 GeV



(05) $Y(4260) \rightarrow J/\psi \pi^+ \pi^-$



(07) $Y(4360) \rightarrow \psi(2S) \pi^+ \pi^-$

$Y(4660) \rightarrow \psi(2S) \pi^+ \pi^-$

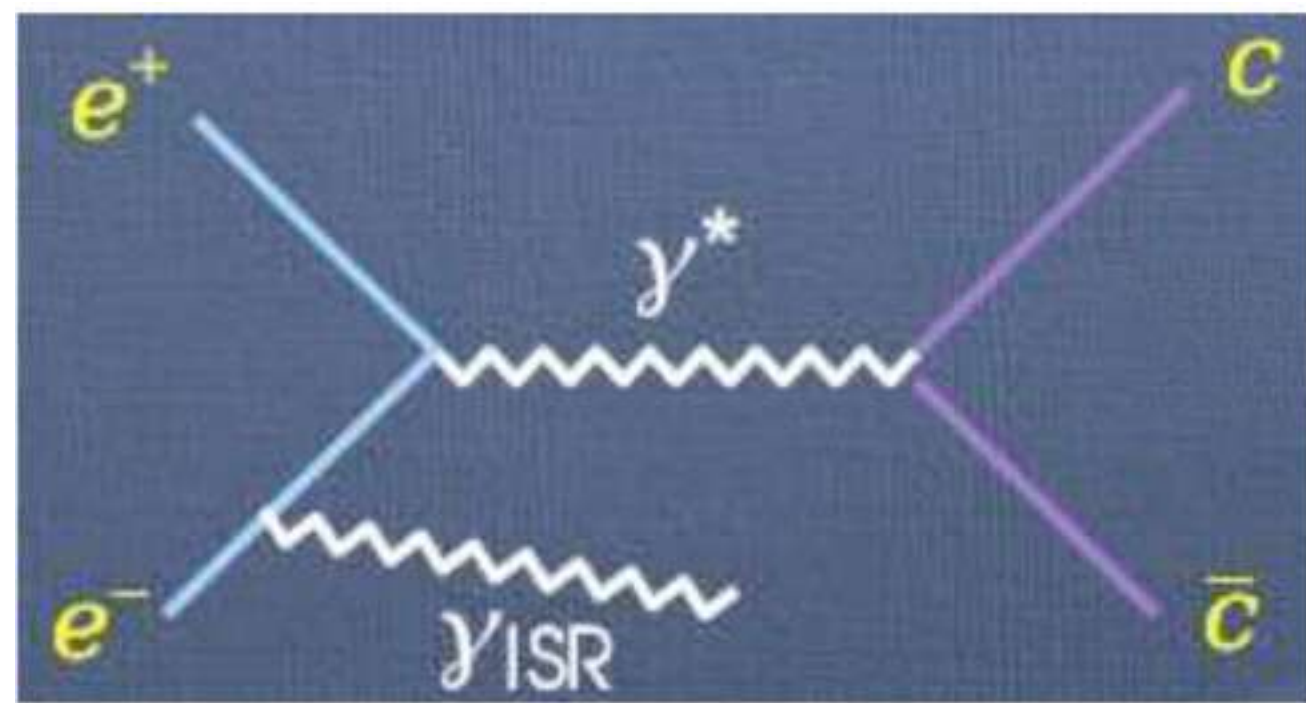
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2008

2018



(05) $Y(4260) \rightarrow J/\psi \pi^+ \pi^-$

$$M = (4263 \pm 9) \rightarrow (4230 \pm 8) \text{ MeV}$$

$$\Gamma = (95 \pm 14) \rightarrow (55 \pm 19) \text{ MeV}$$



(07) $Y(4360) \rightarrow \psi(2S) \pi^+ \pi^-$

$$M = (4361 \pm 15) \rightarrow (4368 \pm 13) \text{ MeV}$$

$$\Gamma = (74 \pm 23) \rightarrow (96 \pm 7) \text{ MeV}$$

$Y(4660) \rightarrow \psi(2S) \pi^+ \pi^-$

$$M = (4664 \pm 17) \rightarrow (4643 \pm 9) \text{ MeV}$$

$$\Gamma = (48 \pm 16) \rightarrow (72 \pm 11) \text{ MeV}$$

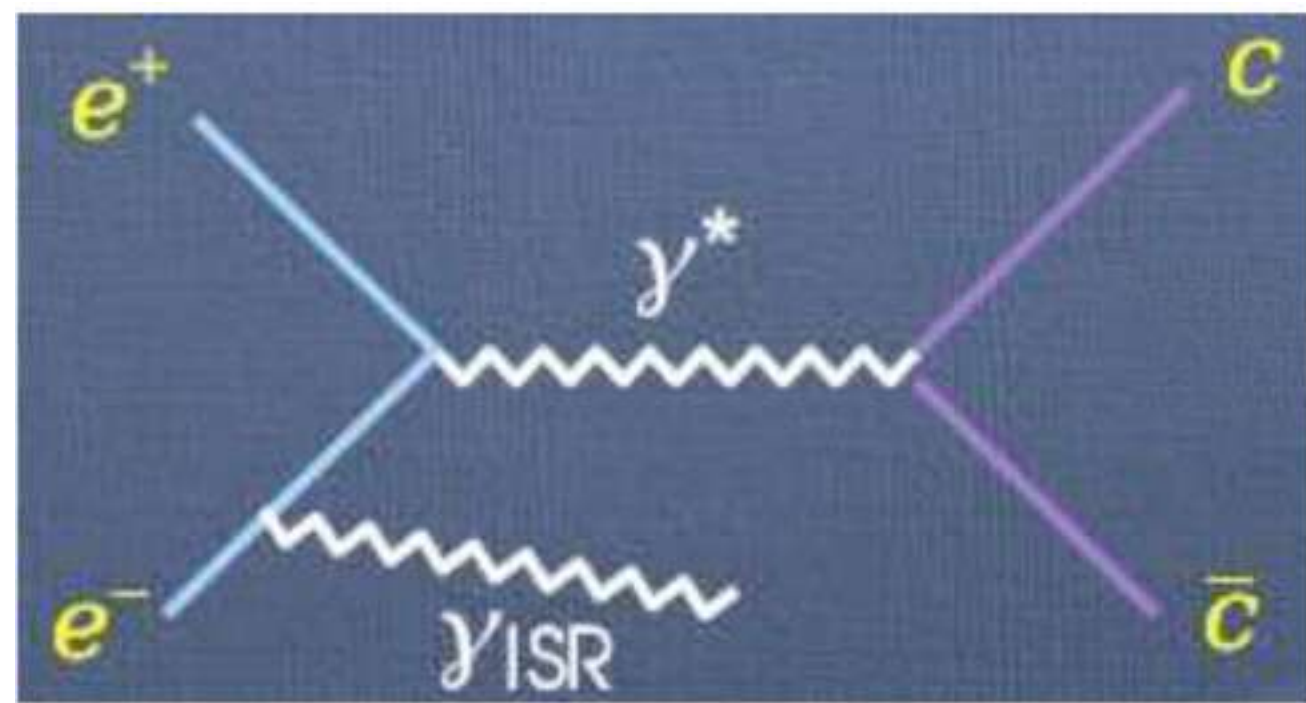
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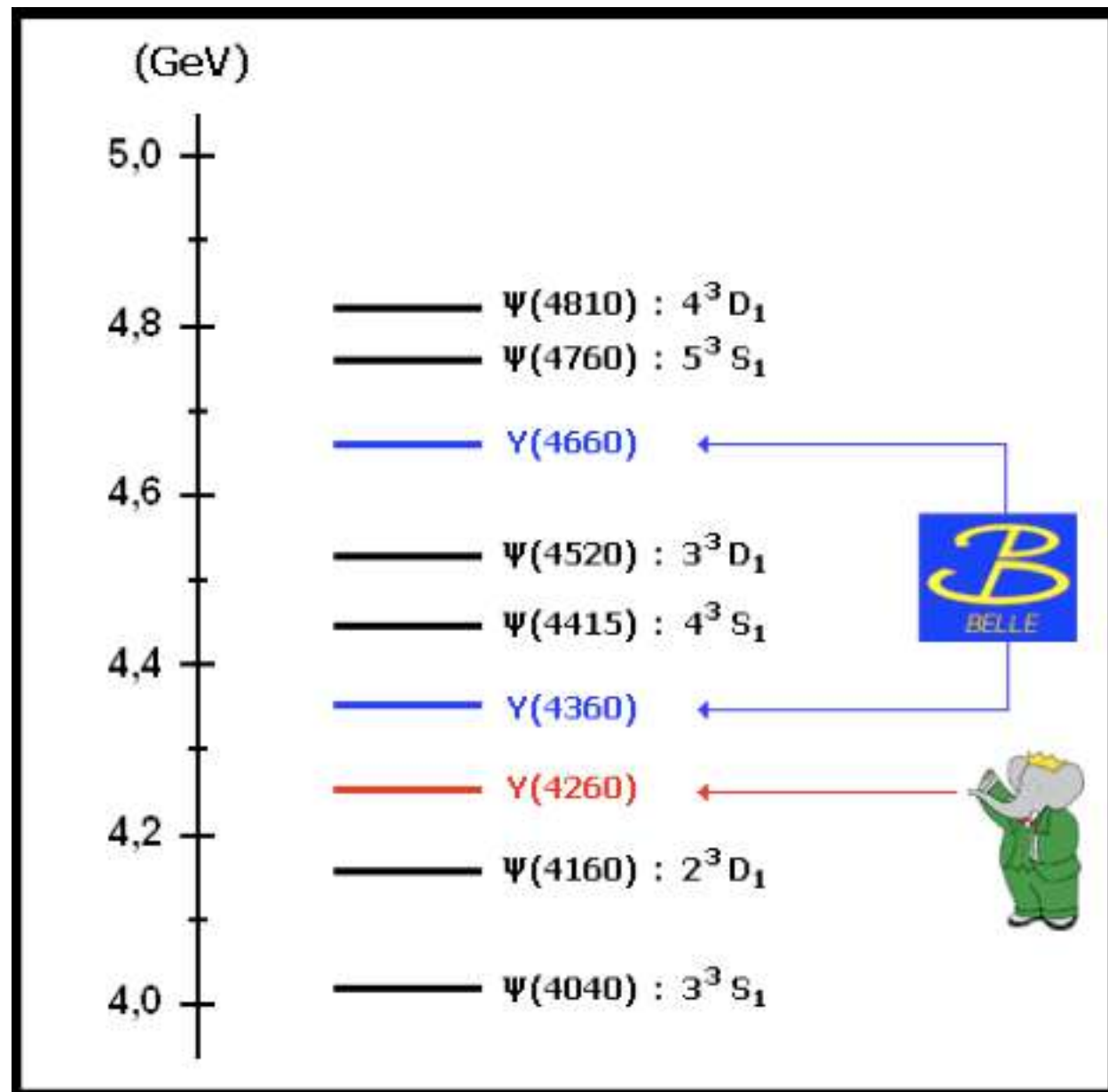
$Y(4660) \rightarrow \psi(2S) \pi^+ \pi^-$

$$M = (4664 \pm 17) \rightarrow (4643 \pm 9) \text{ MeV}$$

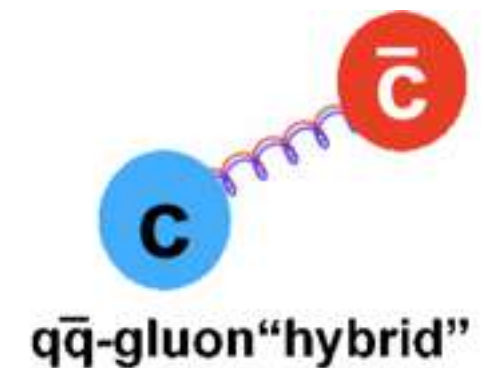
$$\Gamma = (48 \pm 16) \rightarrow (72 \pm 11) \text{ MeV}$$

Why exotics?

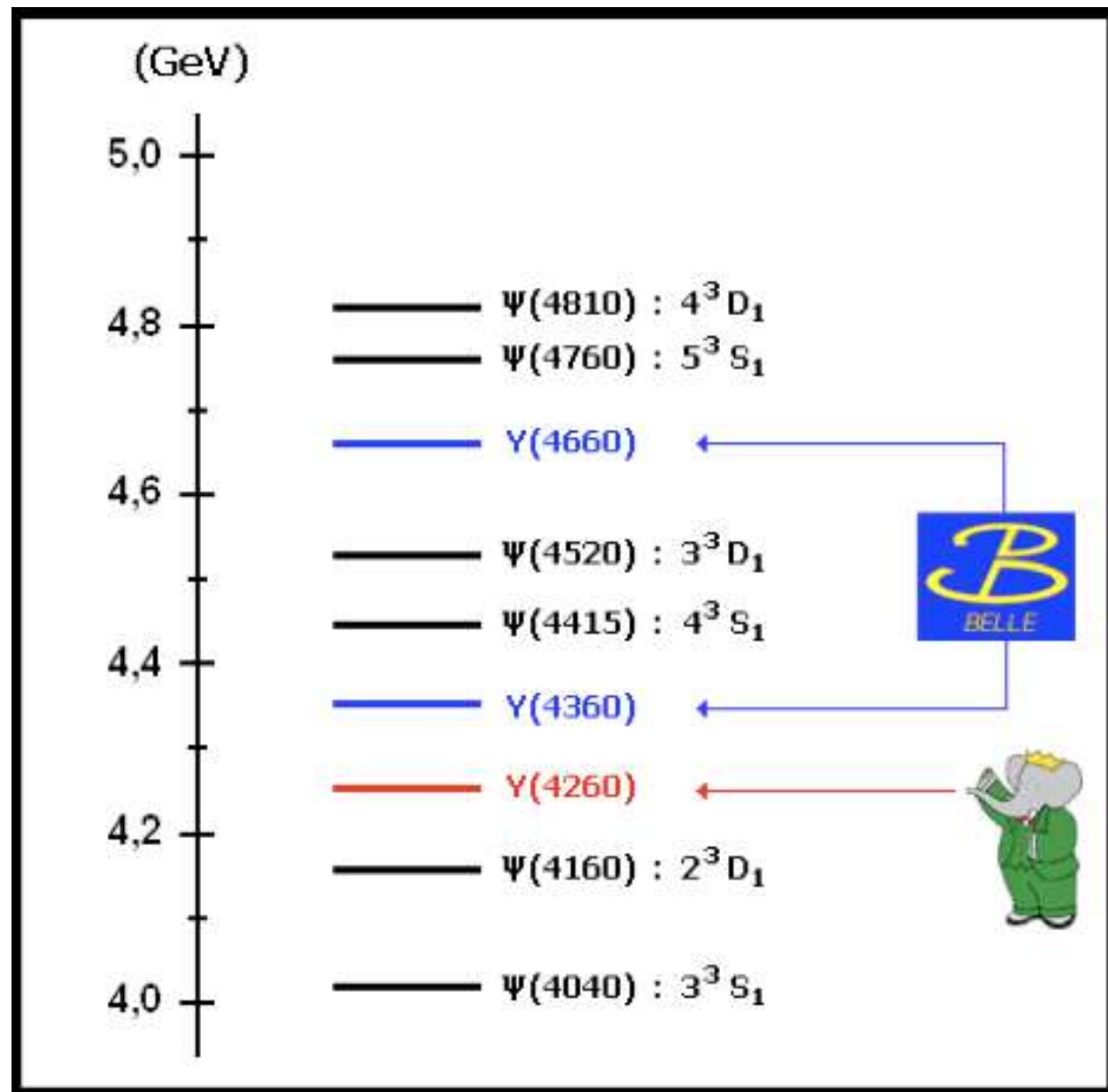
masses and widths of these states are not consistent with any of the 1^{--} charmonium states



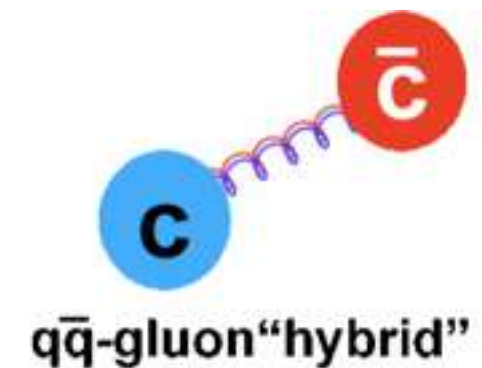
$Y(4260)$:
charmonium
hybrid



masses and widths of these states are not consistent with any of the 1^- charmonium states



$Y(4260)$:
charmonium
hybrid



Lattice (EJPA18(04) and string model
calc. (PRD77(08): $M \sim 4400$ MeV

Charmonium hybrids:

flux tube (PRD52(95): $M \sim 4200$ MeV

charmonium hybrid \Rightarrow dominant decay mode $D\bar{D}_1$

(Close & Page, PRLB628(05)215)

Maiani et al. (PRD72 (05)) tetraquark $J^{PC} = 1^{--}$ states:

$$Y(4260) = ([cs]_{S=0}[\bar{c}\bar{s}]_{S=0})P\text{-wave}$$

Ebert et al. (EPJC58(08)) \Rightarrow such state would have $M \sim 4450$ MeV

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Y(4260)

- 
- baryonium $\Lambda_c - \bar{\Lambda}_c$ state (Qiao, PLB639(06))
 - S-wave threshold effect (Rosner, PRD74(06))
 - molecular state (Ding, Liu et al., Yuan et al., MN et al.,...)
 - manifestations of Regge zeros (Beveren et al., arXiv:0811.1755)

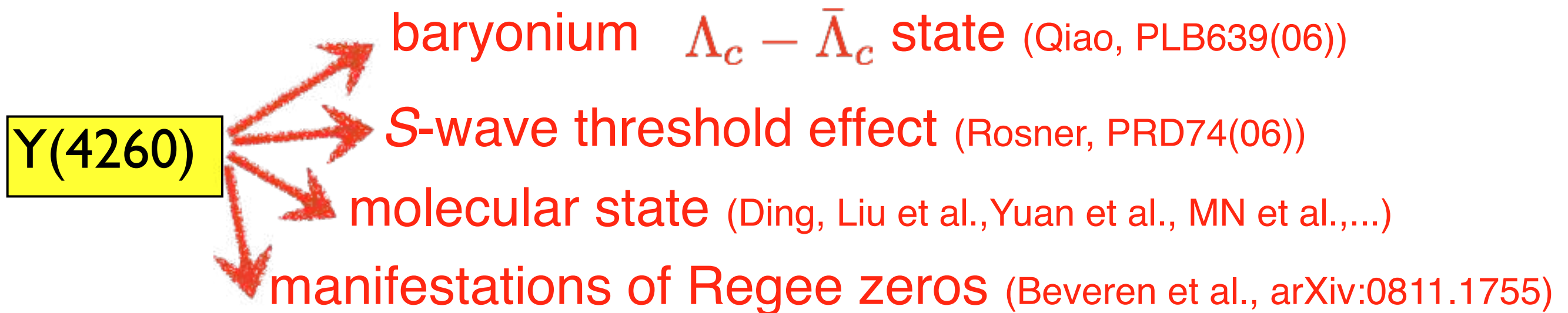
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Observed at B factories with limited statistics

High precision measurements at BESIII supply new insights



$$(05) \quad Y(4260) \rightarrow J/\psi \pi^+ \pi^-$$

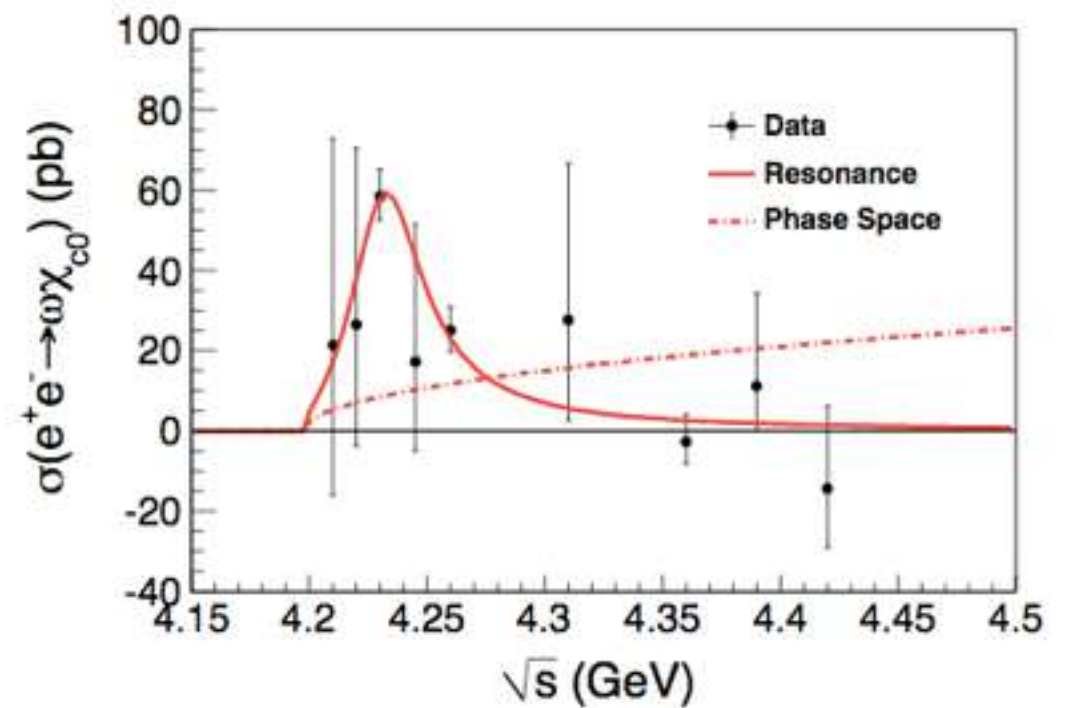
$$M = (4263 \pm 9) \rightarrow (4230 \pm 8) \text{ MeV}$$
$$\Gamma = (95 \pm 14) \rightarrow (55 \pm 19) \text{ MeV}$$

BES III

$$\text{arXiv:1410.6538} \Rightarrow e^+ e^- \rightarrow \omega \chi_{c0}$$

$$M = (4230 \pm 8 \pm 6) \text{ MeV}$$
$$\Gamma = (38 \pm 12 \pm 6) \text{ MeV}, 9\sigma$$

Inconsistent with the $Y(4260)$ line shape. It was called $Y(4220)$





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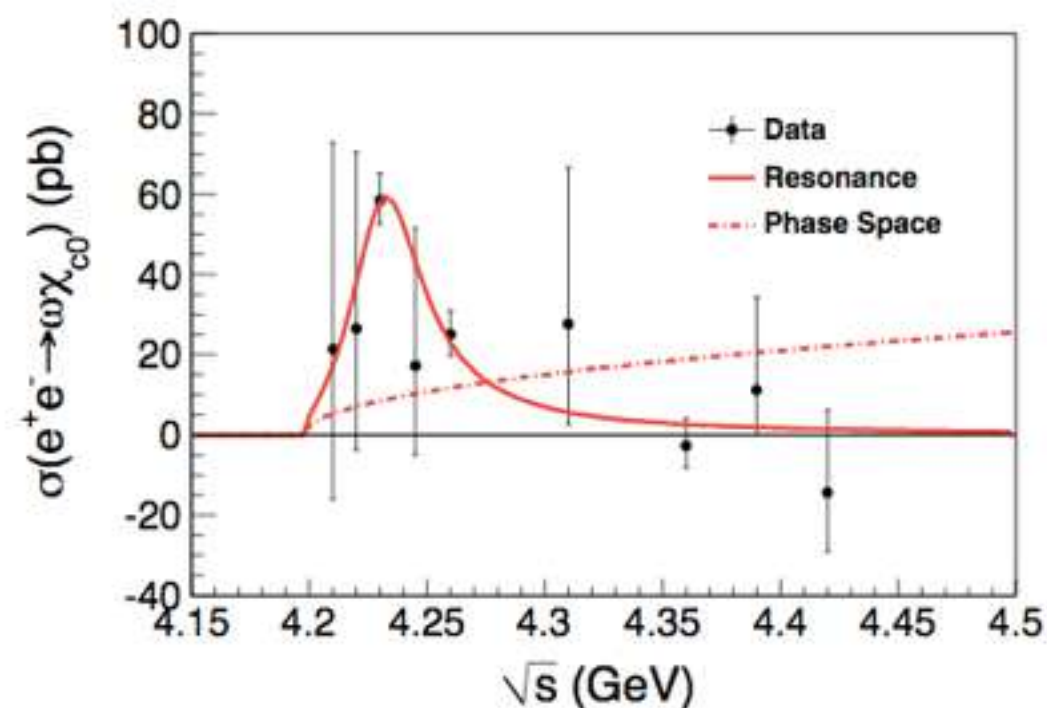
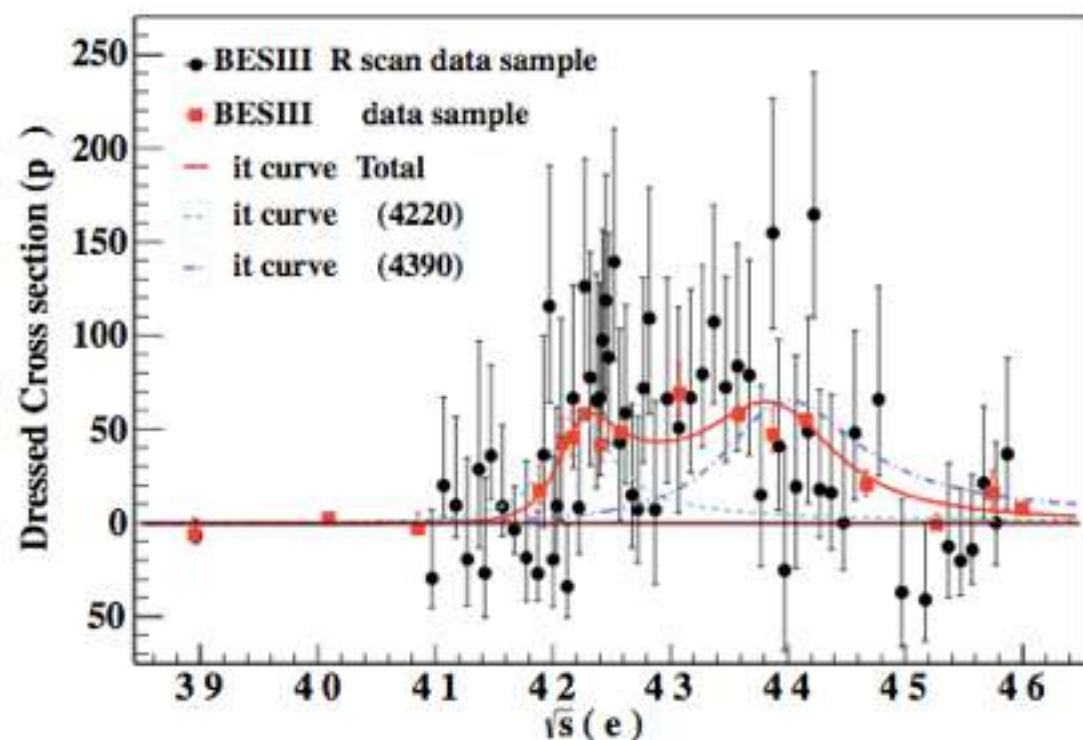
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arXiv:1610.07044 $\Rightarrow e^+ e^- \rightarrow \pi^+ \pi^- h_c$

$$M = (4218.4 \pm 5.1 \pm 0.9) \text{ MeV}$$

$$\Gamma = (66.0 \pm 10.3 \pm 0.4) \text{ MeV}, 10\sigma$$

$$M = (4391.5 \pm 6.5 \pm 1.0) \text{ MeV}$$

$$\Gamma = (139.5 \pm 18.4 \pm 1.0) \text{ MeV}, 10\sigma$$



(05) $Y(4260) \rightarrow J/\psi \pi^+ \pi^-$

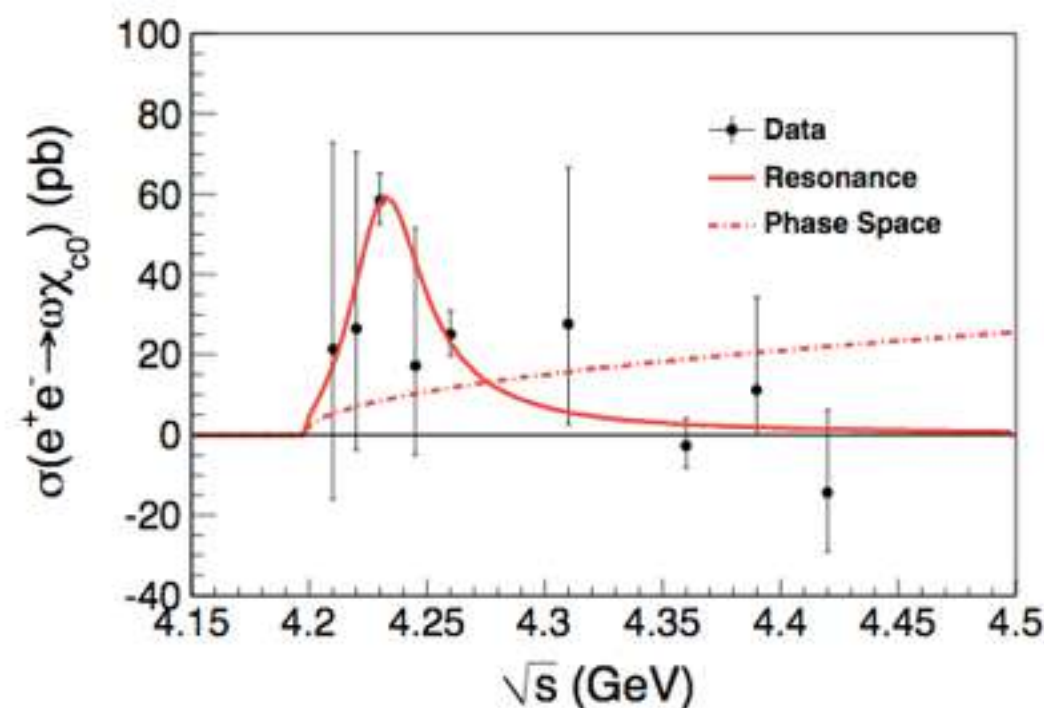
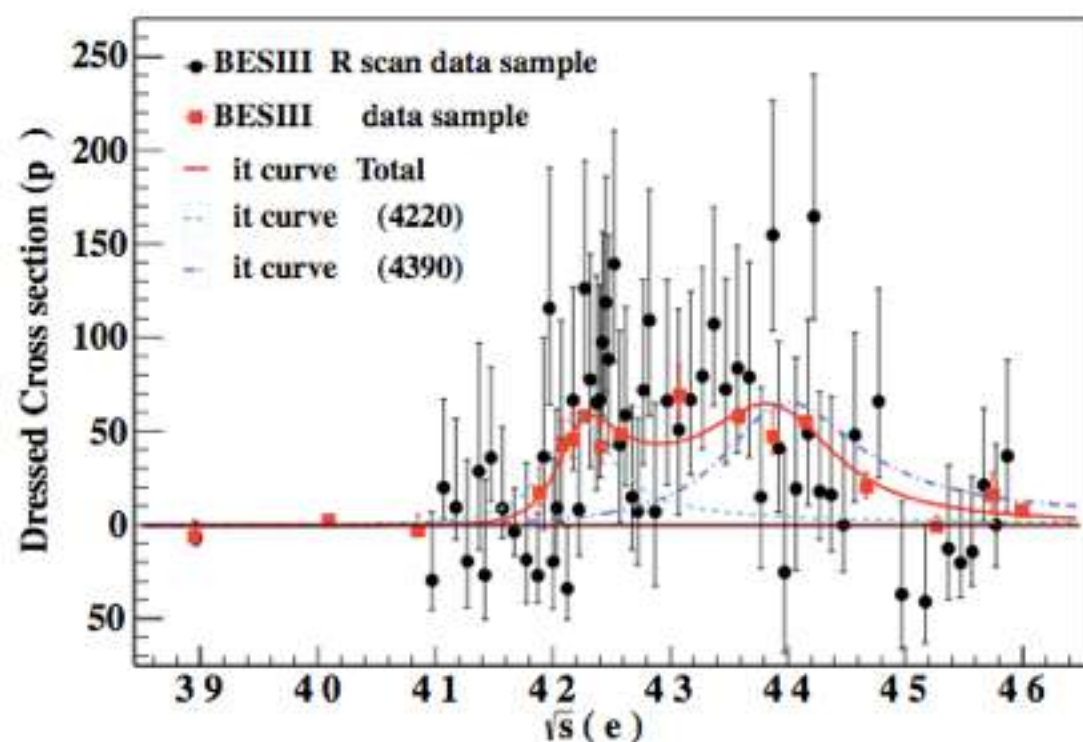
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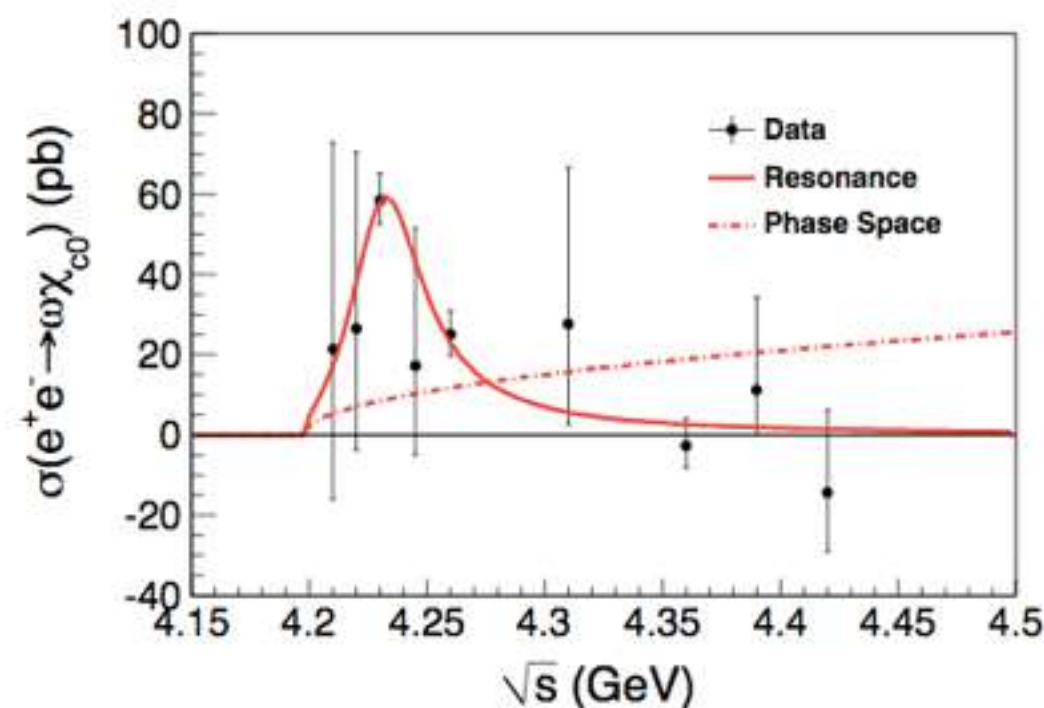
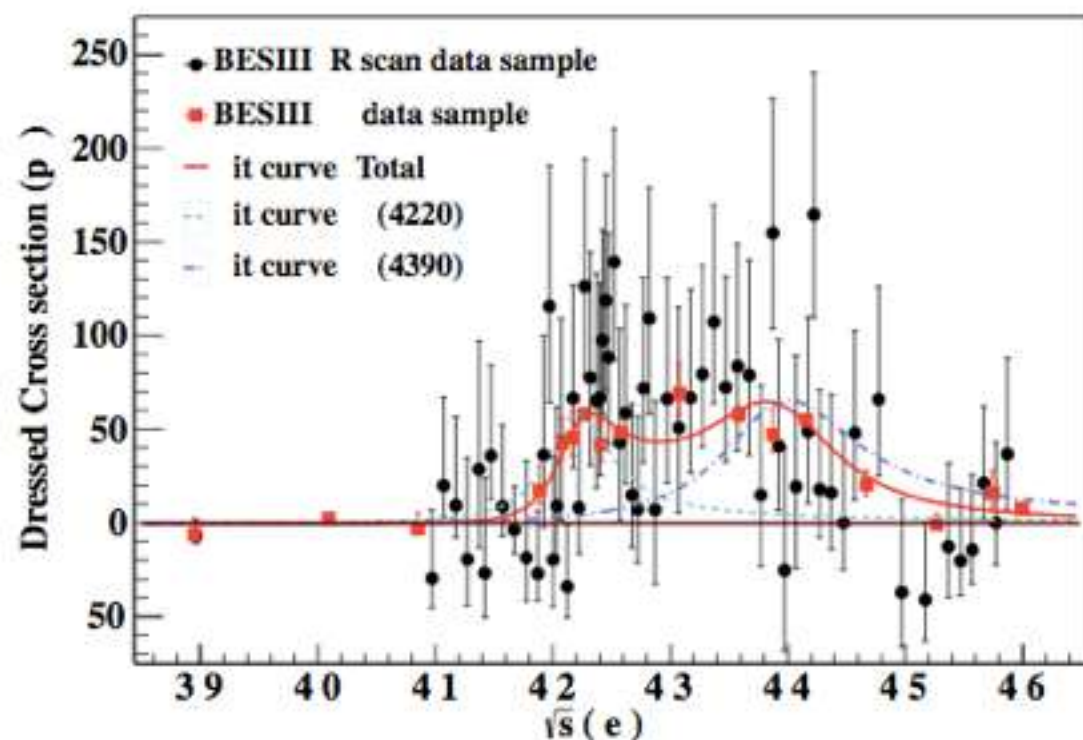
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Inconsistent with the $Y(4260)$ and $Y(4360)$, but consistent with $Y(4220)$

The higher mass state was called $Y(4390)$

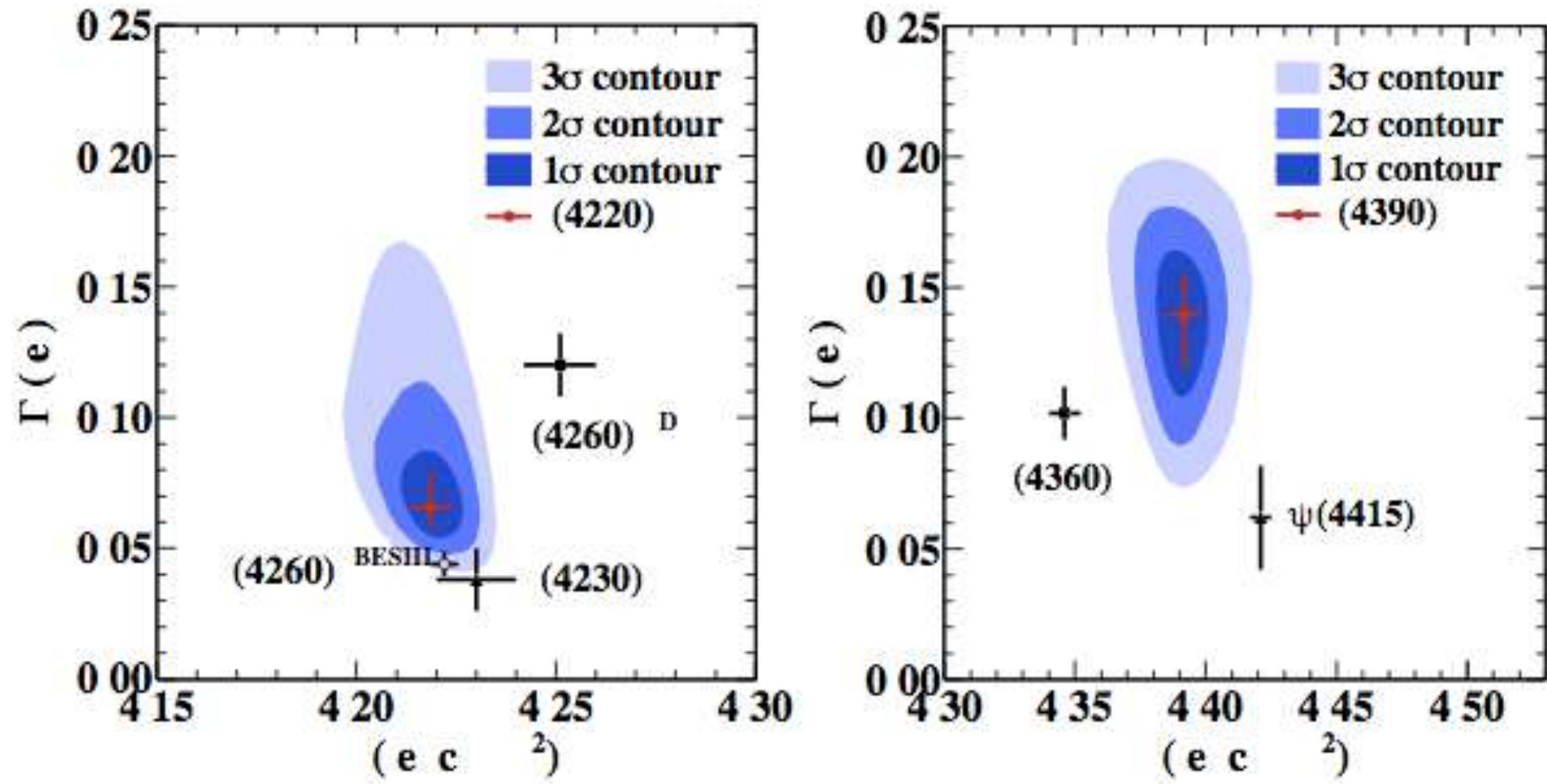
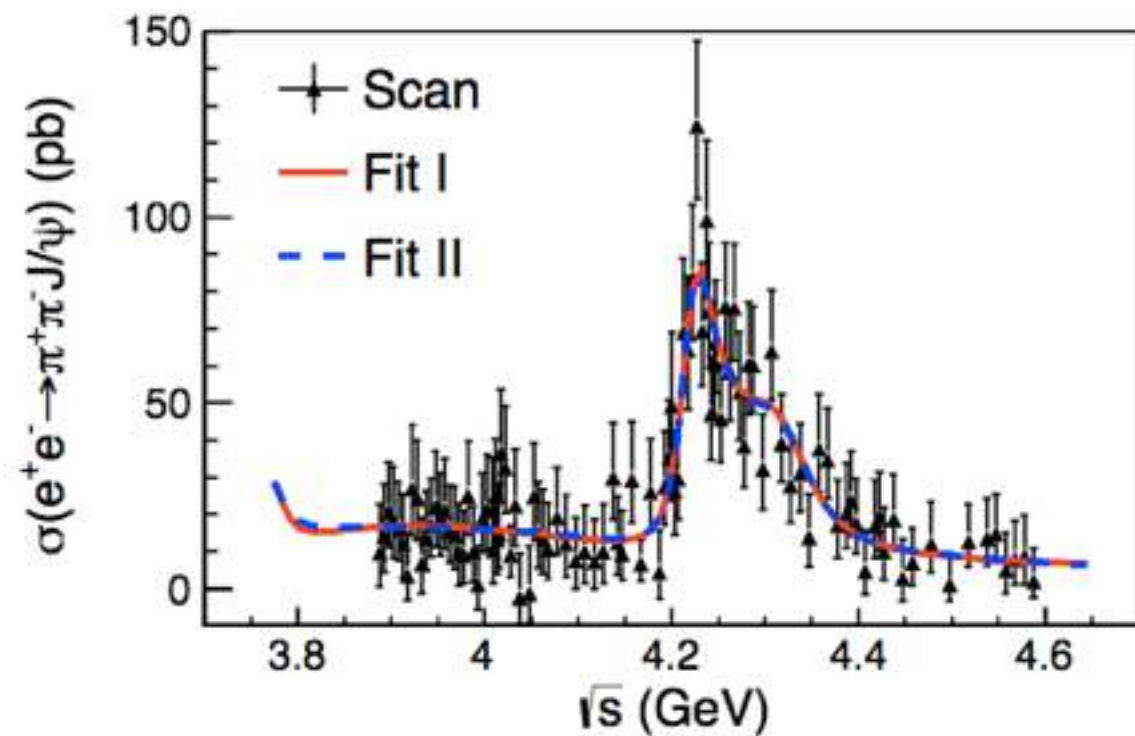


FIG. 3. The likelihood contours in the mass and width planes for $Y(4220)$ (*left panel*) and $Y(4390)$ (*right panel*). The filled areas are up to 3σ likelihood contours and the dots with error bars are the locations of Y or ψ states. The parameters of $Y(4260)^{\text{PDG}}$ are taken from the PDG average [3] and $Y(4260)^{\text{BESIII}}$ from the measurement of $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ at BESIII [35].



arXiv:1611.01317 $\Rightarrow e^+e^- \rightarrow \pi^+\pi^- J/\psi$

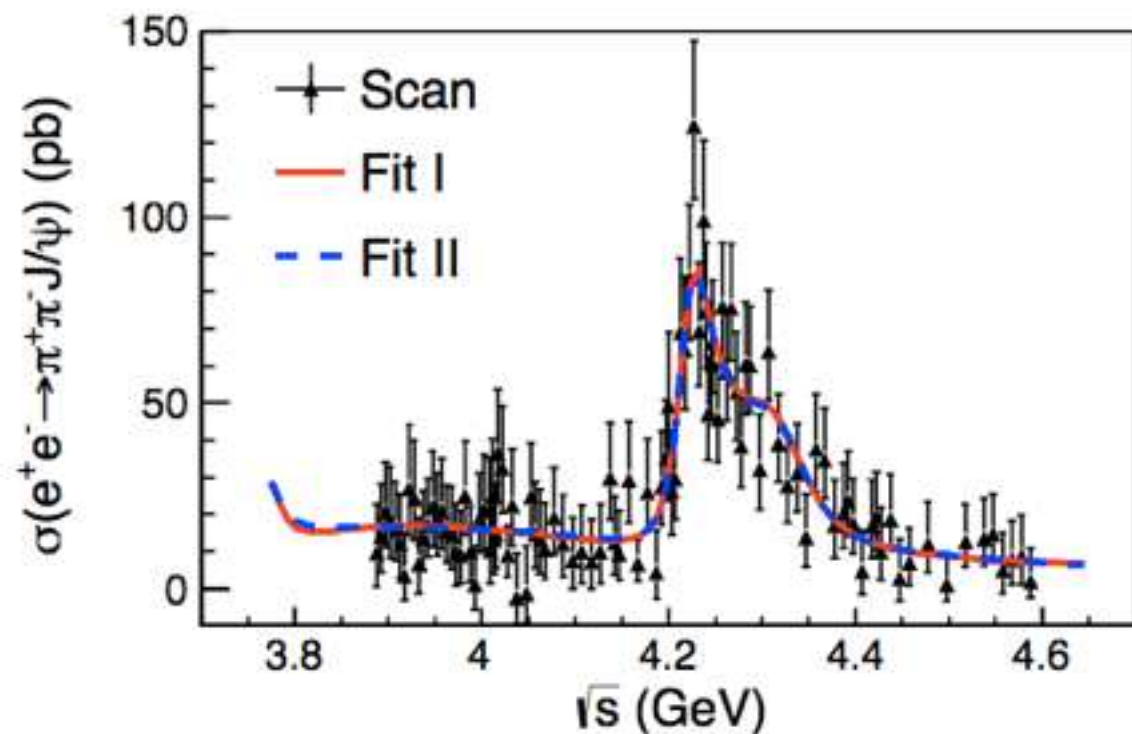
$$M = (4222.0 \pm 3.1 \pm 1.4) \text{ MeV}$$

$$\Gamma = (44.1 \pm 4.3 \pm 2.0) \text{ MeV}, 10\sigma$$

$$M = (4320.0 \pm 10.4 \pm 7) \text{ MeV}$$

$$\Gamma = (101.4 \pm 23.2 \pm 10.2) \text{ MeV}, 7.6\sigma$$

Consistent with the $Y(4260)$ and $Y(4360)$ (first time in this channel)



$$\text{arXiv:1611.01317} \Rightarrow e^+e^- \rightarrow \pi^+\pi^- J/\psi$$

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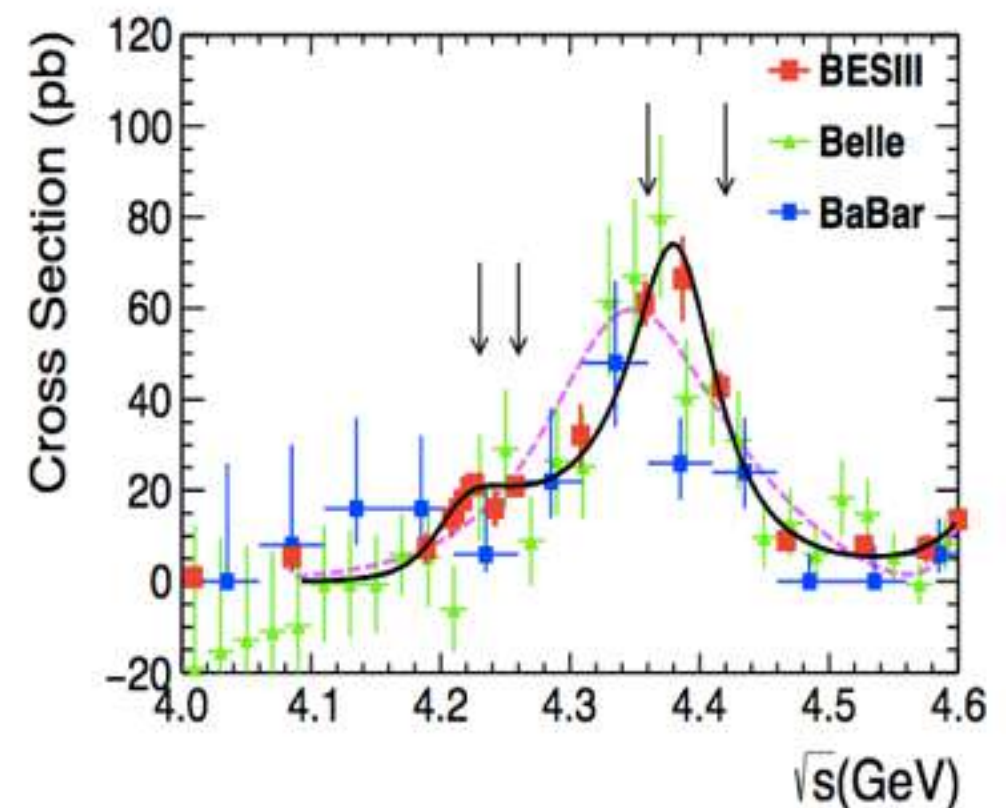
$$\text{arXiv:1703.08787} \Rightarrow e^+e^- \rightarrow \pi^+\pi^- \psi(2S)$$

$$M = (4209.5 \pm 7.4 \pm 1.4) \text{ MeV}$$

$$\Gamma = (80.1 \pm 24.6 \pm 2.9) \text{ MeV}, 5.8\sigma$$

$$M = (4383.8 \pm 4.2 \pm 0.8) \text{ MeV}$$

$$\Gamma = (84.2 \pm 12.5 \pm 2.1) \text{ MeV}, 10\sigma$$



Consistent with the $Y(4220)$ and $Y(4390)$ observed in $e^+e^- \rightarrow \pi^+\pi^- h_c$

arXiv:1808.02847 $\Rightarrow e^+e^- \rightarrow \pi^+ D^0 D^{*-}$

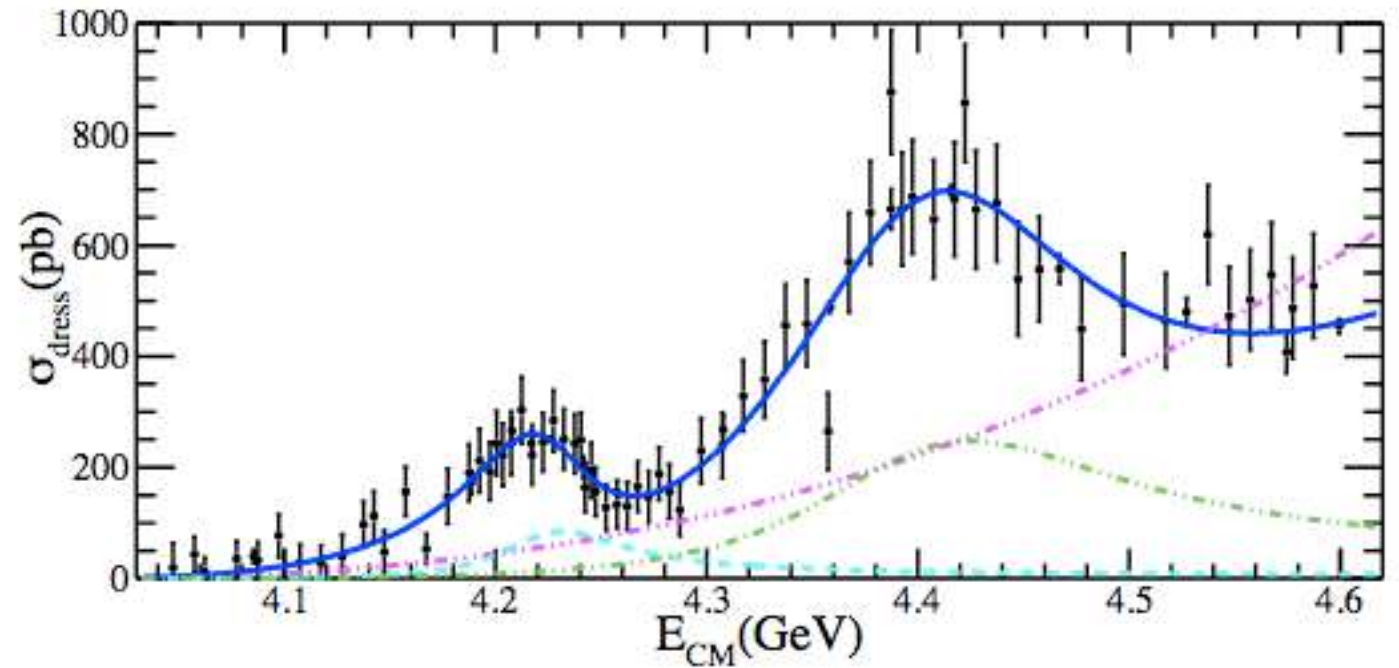
$M = (4224.8 \pm 5.6) \text{ MeV}$

$\Gamma = (72.3 \pm 9.1) \text{ MeV}$

$M = (4400.1 \pm 9.3) \text{ MeV}$

$\Gamma = (181.7 \pm 16.9) \text{ MeV}$

lower mass resonance in good agreement with the $Y(4220)$



$$\text{arXiv:1808.02847} \Rightarrow e^+ e^- \rightarrow \pi^+ D^0 D^{*-}$$

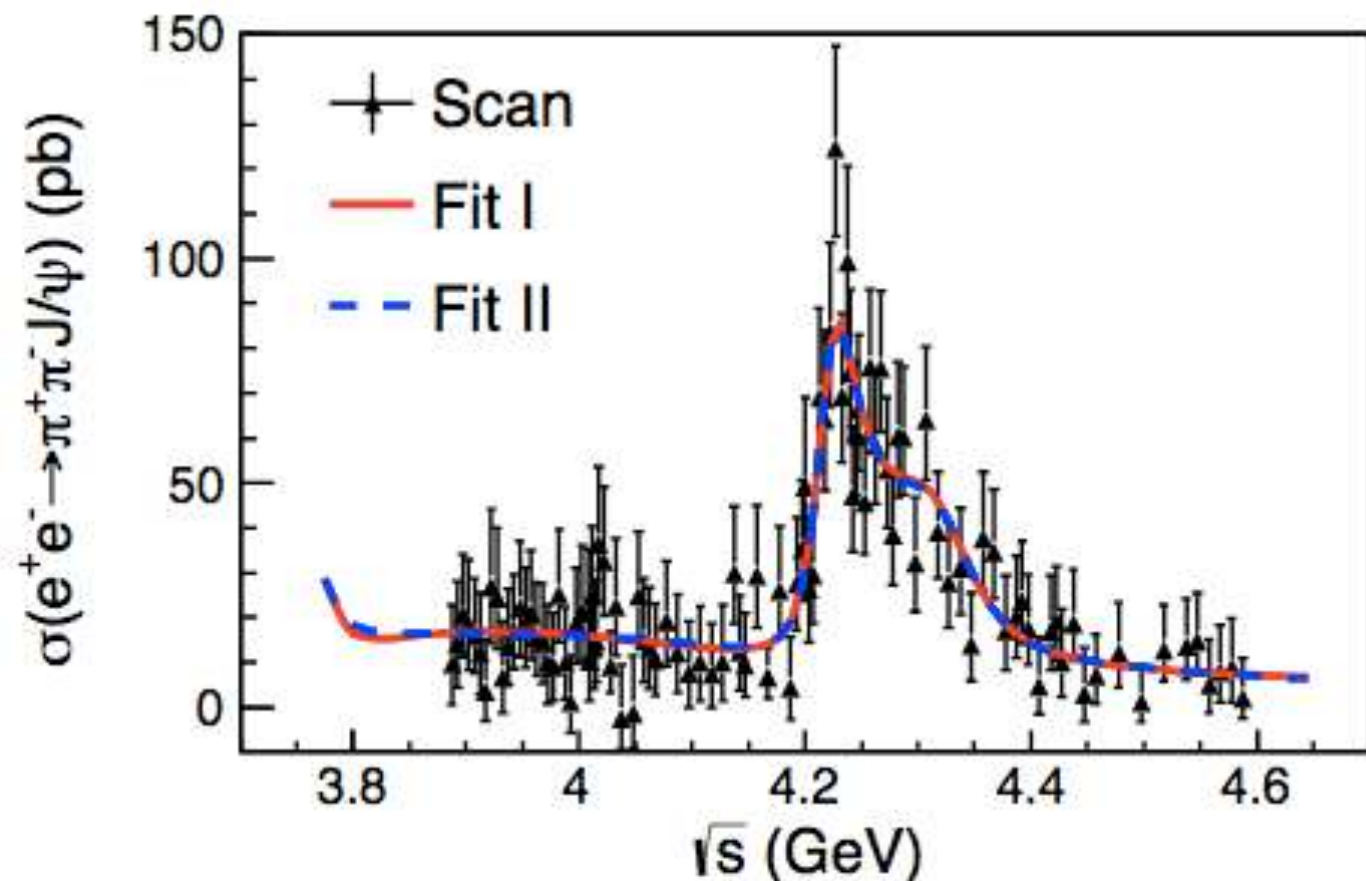
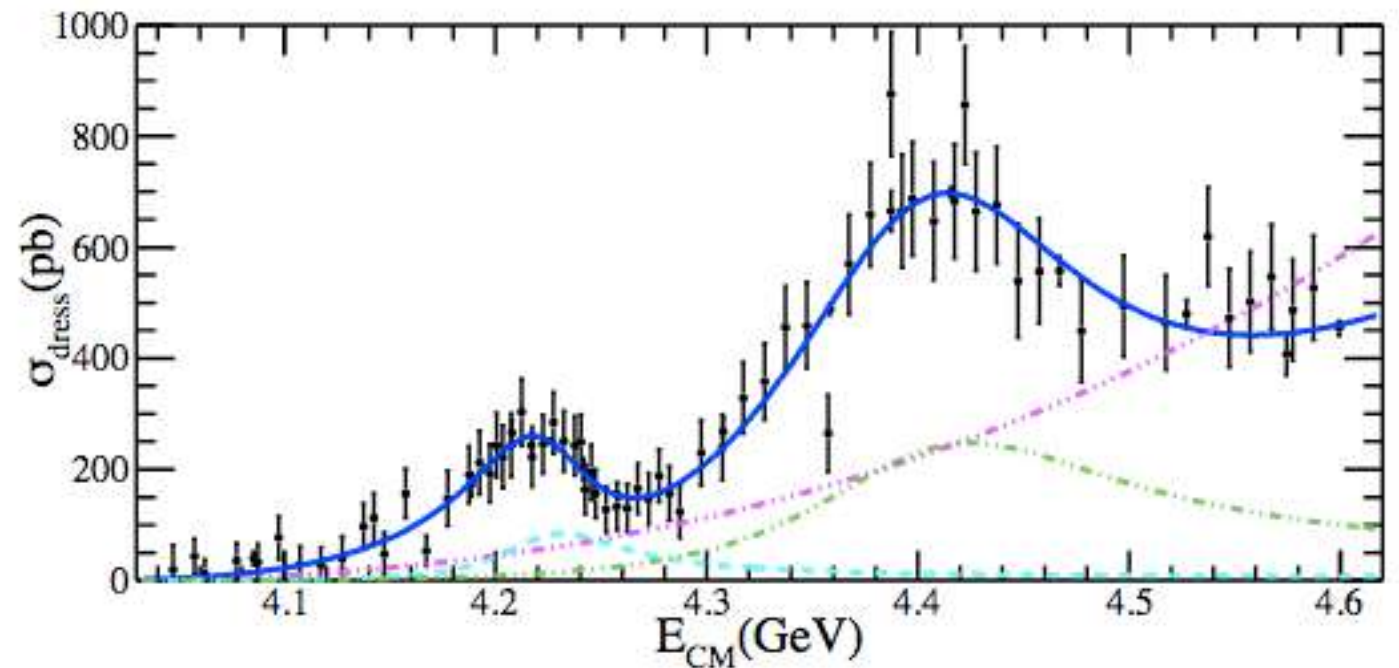
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$$M = (4400.1 \pm 9.3) \text{ MeV}$$

$$\Gamma = (181.7 \pm 16.9) \text{ MeV}$$

lower mass resonance in good agreement with the $Y(4220)$



BESIII data indicate that the structure $Y(4260)$ actually consists of two resonances with masses 4220 and 4320 MeV, observed in the $e^+ e^- \rightarrow \pi^+ \pi^- J/\psi$, with the $Y(4220)$ being its main component

QCD sum rules calculation for $Y(J^{PC} = 1^{--})$

tetraquark current (Albuquerque, MN, arXiv:0804.4817)

$$j^Y = [cs]_{S=1} [\bar{c}\bar{s}]_{S=0} + [cs]_{S=0} [\bar{c}\bar{s}]_{S=1}$$

$m_Y = (4.65 \pm 0.10)$ GeV in good agreement with $Y(4660)$

molecular current (Albuquerque, MN, Silva, arXiv:1110.2113)

$$j^Y = D_0 \bar{D}^* + \bar{D}_0 D^*$$

$m_Y = (4.96 \pm 0.11)$ GeV not compatible with $Y(4260)$

$$\text{other currents} \left\{ \begin{array}{l} D_s^* \bar{D}_{s0} \Rightarrow m = (5.12 \pm 0.10) \text{ GeV} \\ D \bar{D}_1 \Rightarrow m = (4.12 \pm 0.09) \text{ GeV} \\ [cq]_{S=0} [\bar{c}\bar{q}]_{S=1} \Rightarrow m = (4.49 \pm 0.11) \text{ GeV} \end{array} \right.$$

QCD sum rules calculation for $Y(J^{PC} = 1^{--})$

tetraquark current (Albuquerque, MN, arXiv:0804.4817)

$$j^Y = [cs]_{S=1}[\bar{c}\bar{s}]_{S=0} + [cs]_{S=0}[\bar{c}\bar{s}]_{S=1}$$

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$$\text{other currents} \left\{ \begin{array}{l} D_s^*\bar{D}_{s0} \Rightarrow m = (5.12 \pm 0.10) \text{ GeV} \\ D\bar{D}_1 \Rightarrow m = (4.12 \pm 0.09) \text{ GeV} \\ [cq]_{S=0}[\bar{c}\bar{q}]_{S=1} \Rightarrow m = (4.49 \pm 0.11) \text{ GeV} \end{array} \right.$$

none of them compatible with $Y(4260)$

$\Upsilon(4260)$ as a mixed charmonium 4-quark state

Dias, Albuquerque, MN, Zanetti: PRD86 (12)

$$j_\mu(x) = \sin(\theta) j_\mu^{(4)}(x) + \cos(\theta) j_\mu^{(2)}(x)$$
$$j_\mu^{(2)} = \frac{1}{\sqrt{2}} \langle \bar{q}q \rangle \bar{c}_a(x) \gamma_\mu c_a(x)$$
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$$52.5^\circ \leq \theta \leq 53.5^\circ \longleftrightarrow m_Y = (4.26 \pm 0.13) \text{ GeV}$$

$Y(4260)$ as a mixed charmonium 4-quark state

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$$52.5^\circ \leq \theta \leq 53.5^\circ \longleftrightarrow m_Y = (4.26 \pm 0.13) \text{ GeV}$$

$$\Gamma(Y \rightarrow J/\psi \pi\pi) = (4.1 \pm 0.6) \text{ MeV} \quad \text{much smaller than the total experimental width: } \Gamma^{exp} = (55 \pm 19) \text{ MeV}$$



possible indication that the main decay channel is in D mesons \Rightarrow
the $Y(4220)$ is indeed the main component of the $Y(4260)$!

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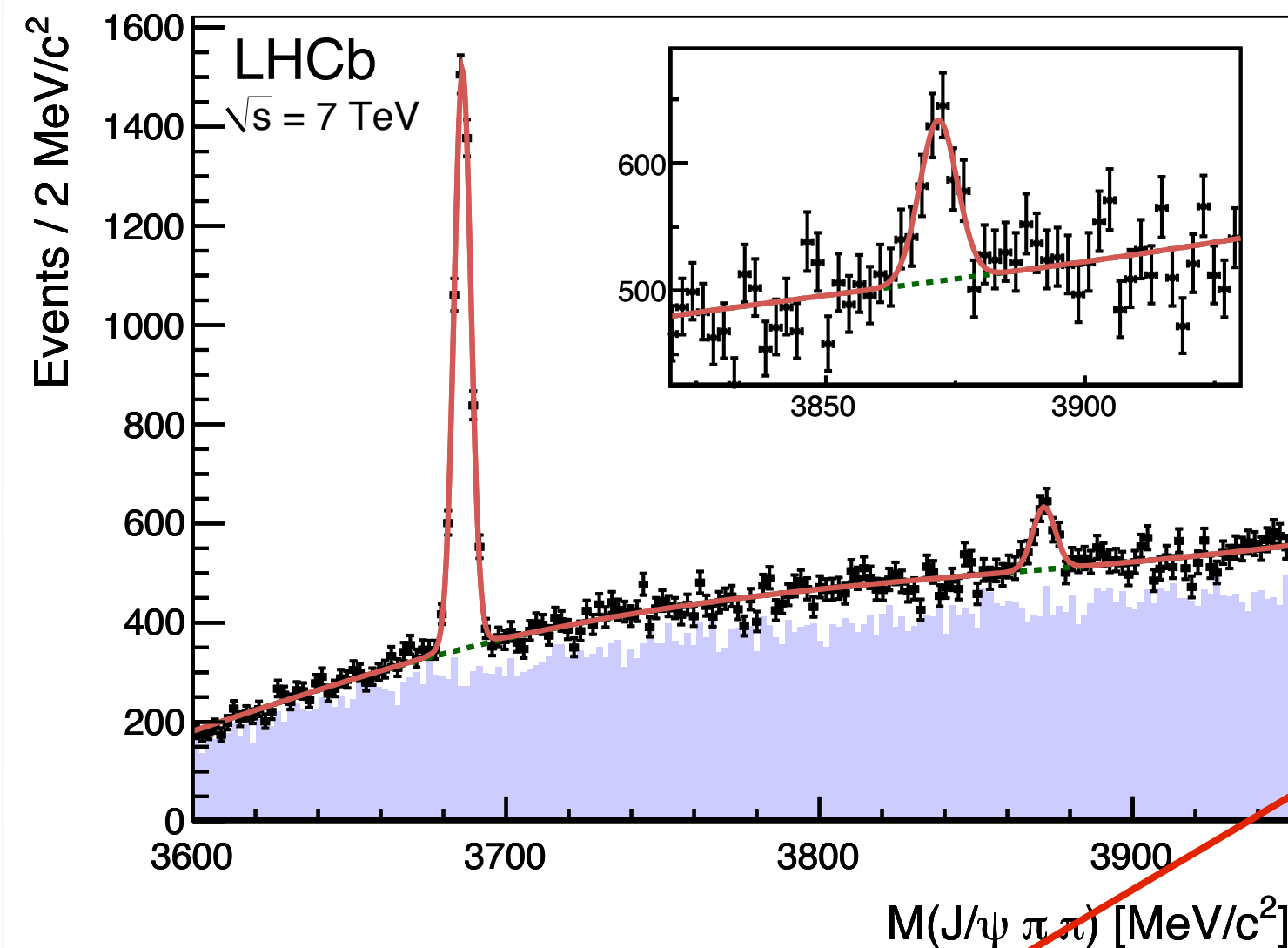
possible indication that the main decay channel is in D mesons \Rightarrow
the $Y(4220)$ is indeed the main component of the $Y(4260)$!

production in B meson decay: $\mathcal{B}(B \rightarrow Y(4260)K) = (1.34 \pm 0.47) \times 10^{-6}$
compatible with the experimental limit: $\mathcal{B}^{exp} < 2.9 \times 10^{-5}$

X(3872) @ KEK (PRL91(2003))

very narrow state observed in the decay: $B^\pm \rightarrow K^\pm (J/\psi \pi^+ \pi^-)$

best studied charmonium exotic candidate



$$M_X = (3871.69 \pm 0.17) \text{ MeV}$$

$$\Gamma < 1.2 \text{ MeV}$$



$c\bar{c}$ spec. for $J^{PC} = 1^{++}$ (Barnes & Godfrey, PRD69 (2004))

$2 \ ^3P_1$ (3990)
 $3 \ ^3P_1$ (4290)

$$\frac{X \rightarrow J/\psi \pi^+ \pi^- \pi^0}{X \rightarrow J/\psi \pi^+ \pi^-} = 0.8 \pm 0.3 \Rightarrow \text{strong isospin and G parity violation}$$

$$M(D^{*0} \bar{D}^0) = (3871 \pm 1)$$

X(3872): molecular $(D^{*0} \bar{D}^0 + \bar{D}^{*0} D^0)$ state (Swanson, Close, Voloshin, Wong ...)

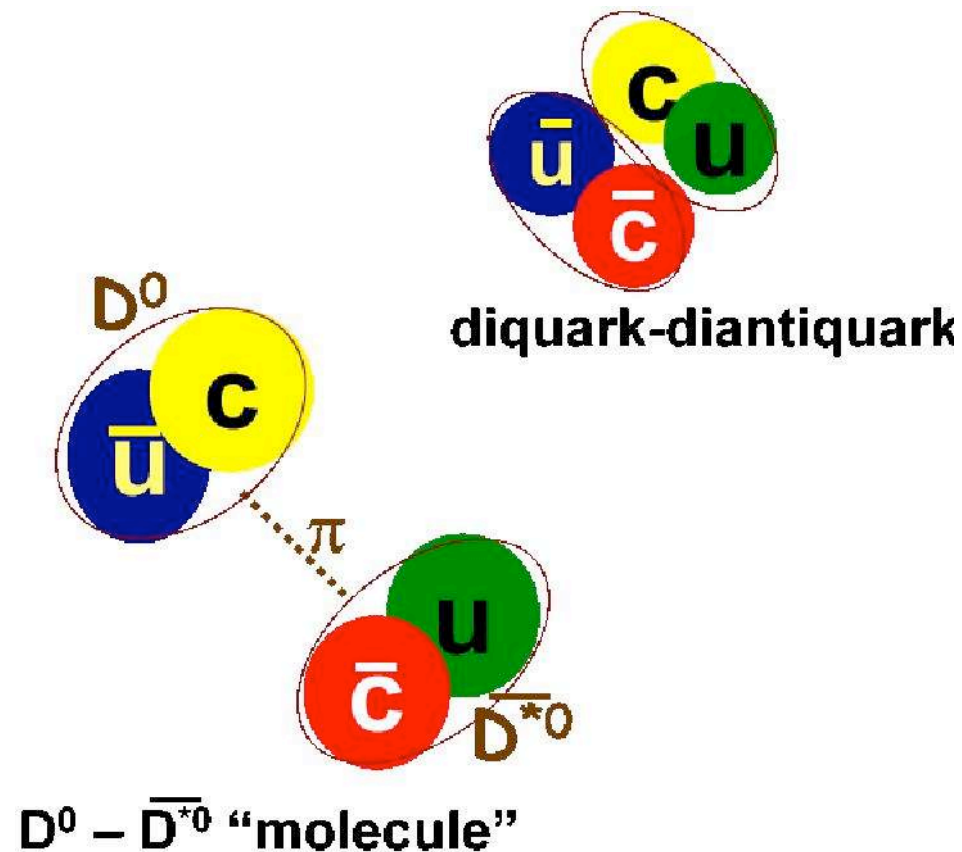
Maiani et al. (PRD71 (05)) tetraquark $J^{PC} = 1^{++}$ state

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molecular and tetraquark interpretations differ by the way quarks are organized in the state

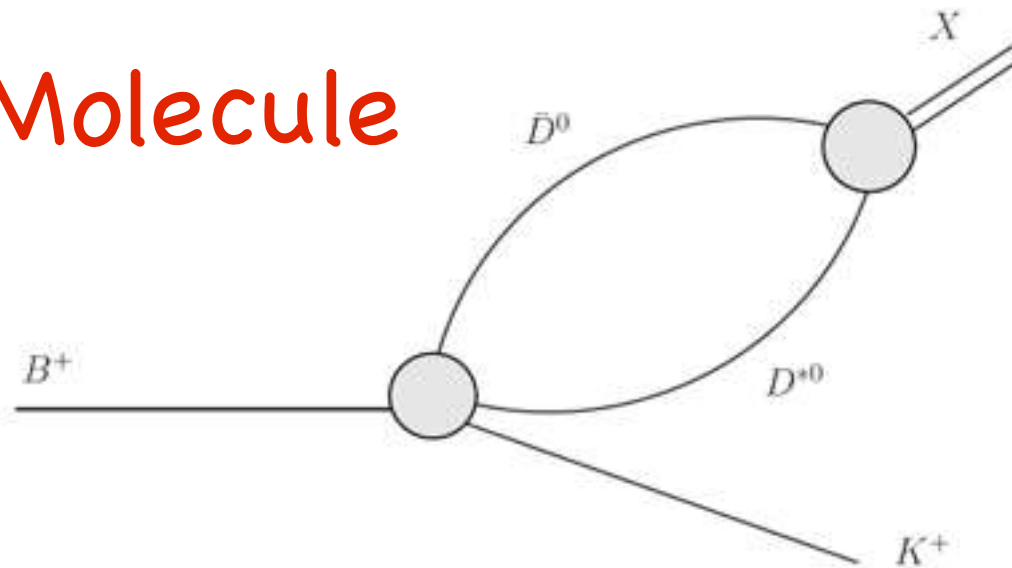
X(3872) production

B decays at B factories



$$B^{\pm} \rightarrow X(3872) K^{\pm}$$

Meson Molecule



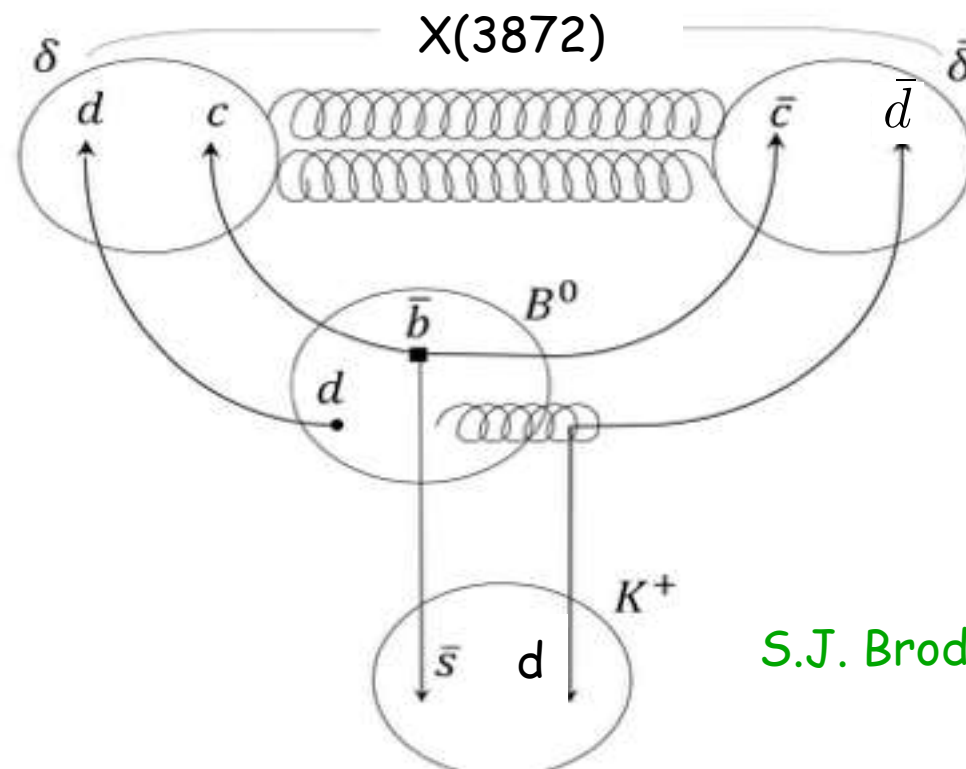
Meson coalescence

Small binding energy

Agreement with data !

E. Braaten, M. Kusunoki, hep-ph/0404161

Tetraquark



Diquark-antidiquark picture

Non-relativistic potential

Agreement with data !

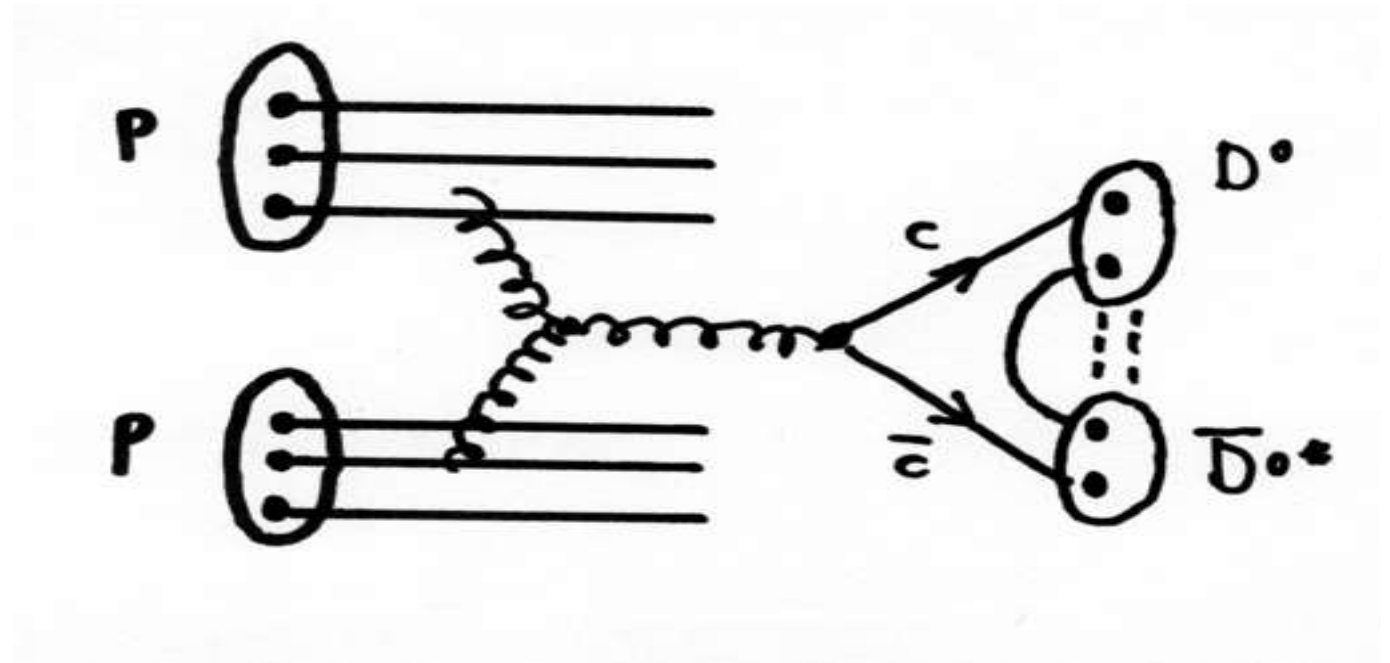
S.J. Brodsky, D.S. Hwang, R.F. Lebed, arXiv:1406.7281

Proton - (anti)Proton



$$\sigma_{\text{exp}} = 30 \text{ nb (CMS)}$$

Meson molecule



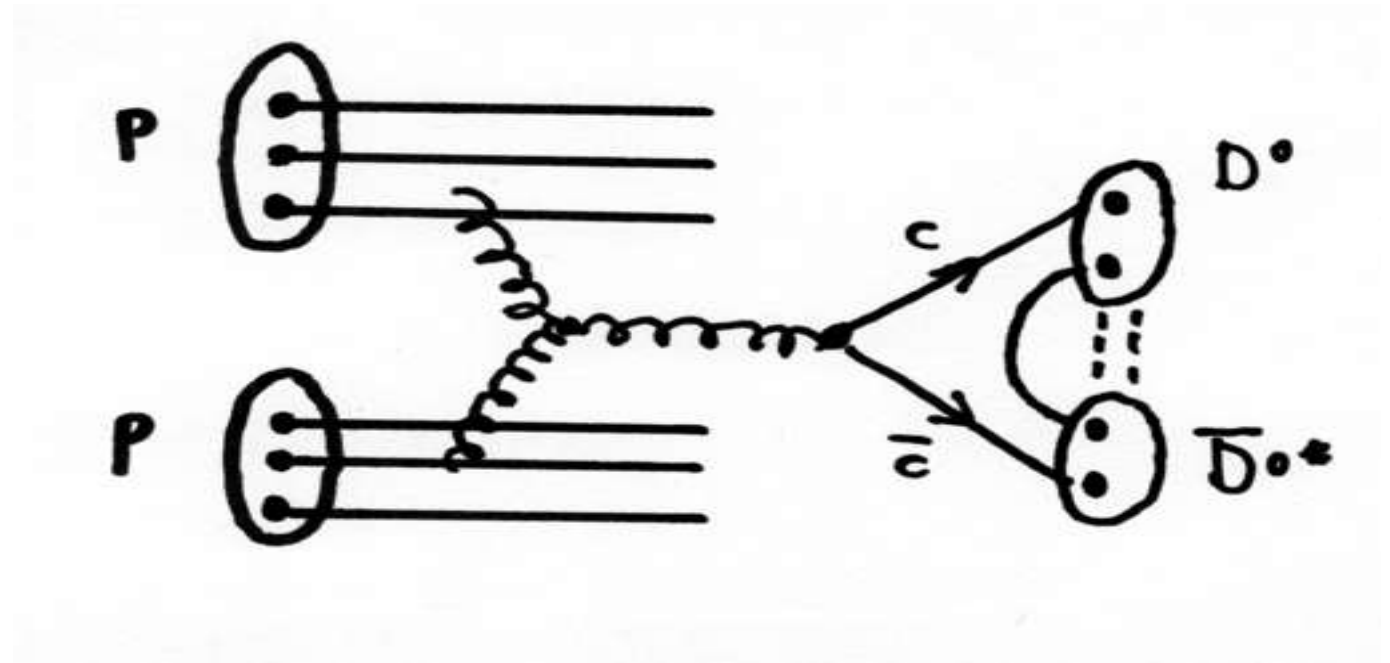
How can a molecule, with small binding energy, be produced in high energy collision with large cross section?

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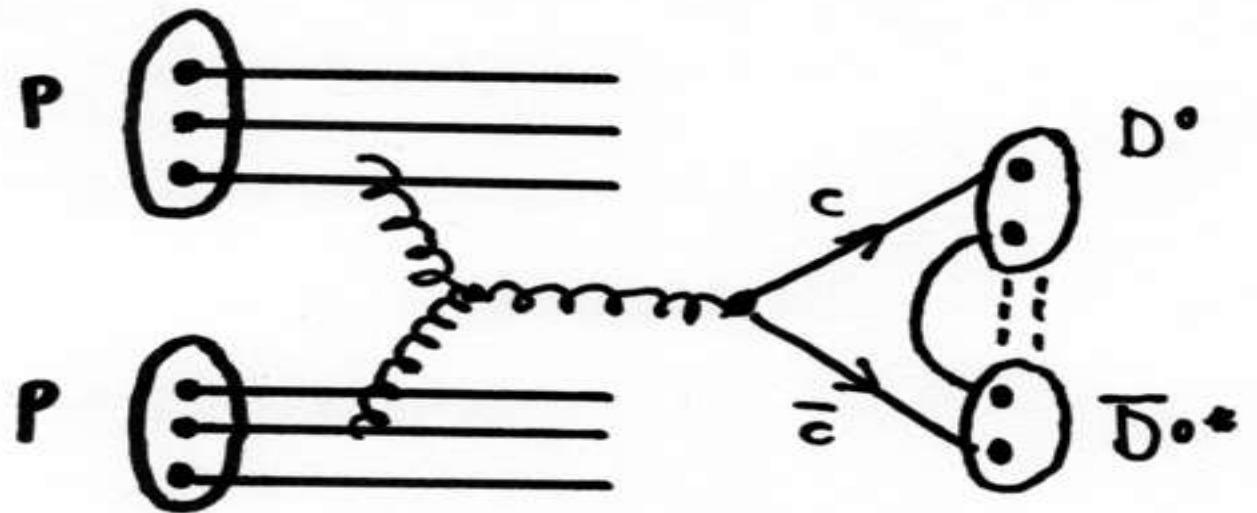
theoretical estimates + MC \rightarrow production cross section smaller by factor 300! (Bignamini et. al., PRL103(09)162001) Problem for molecular approach

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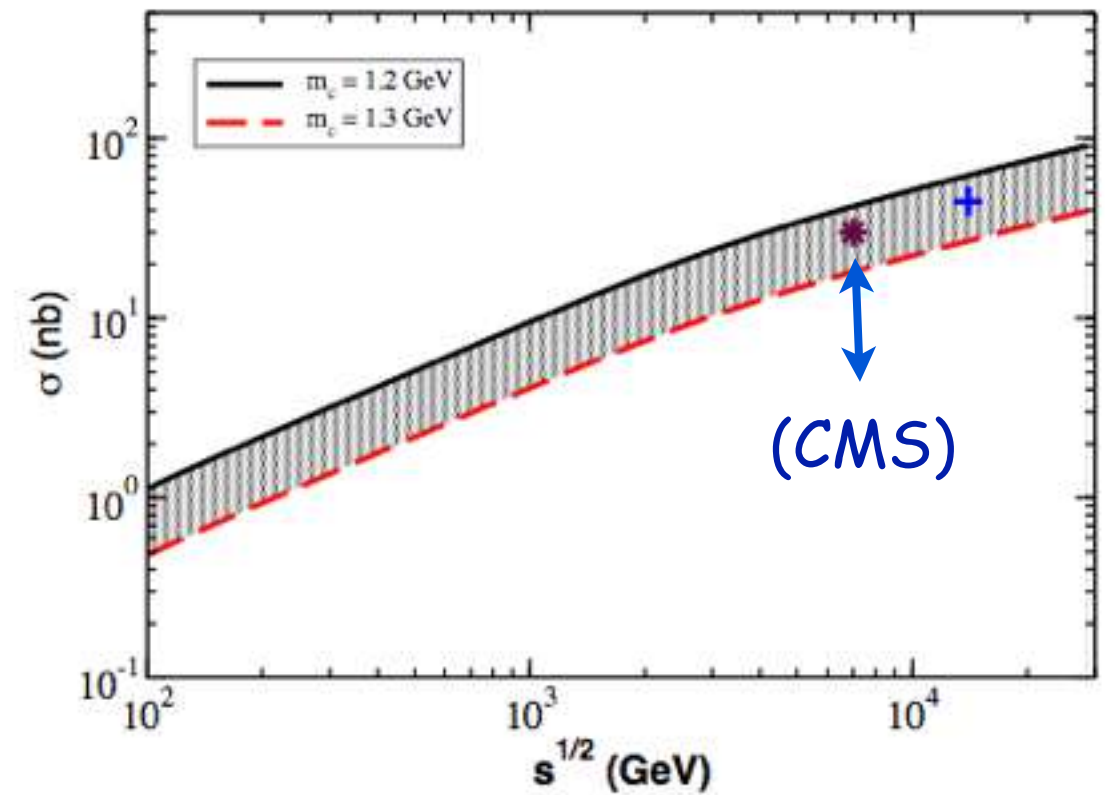
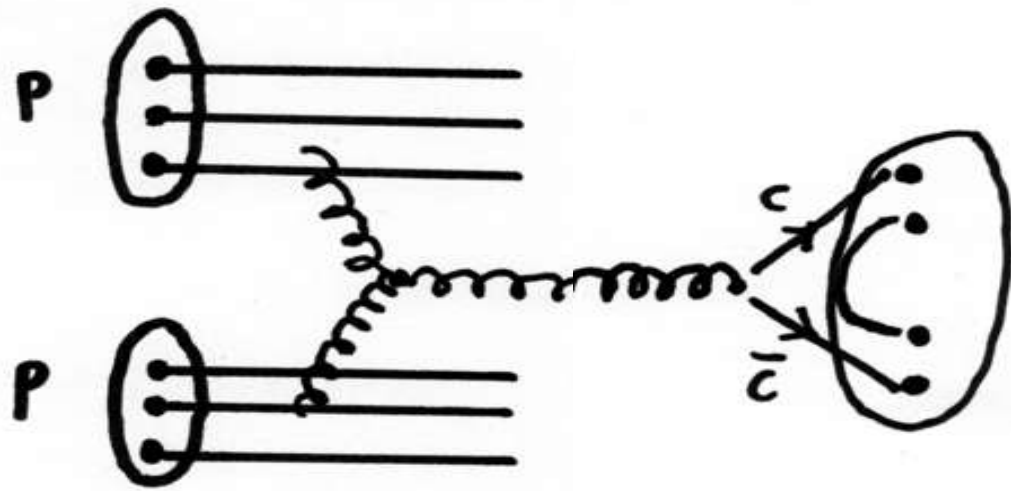


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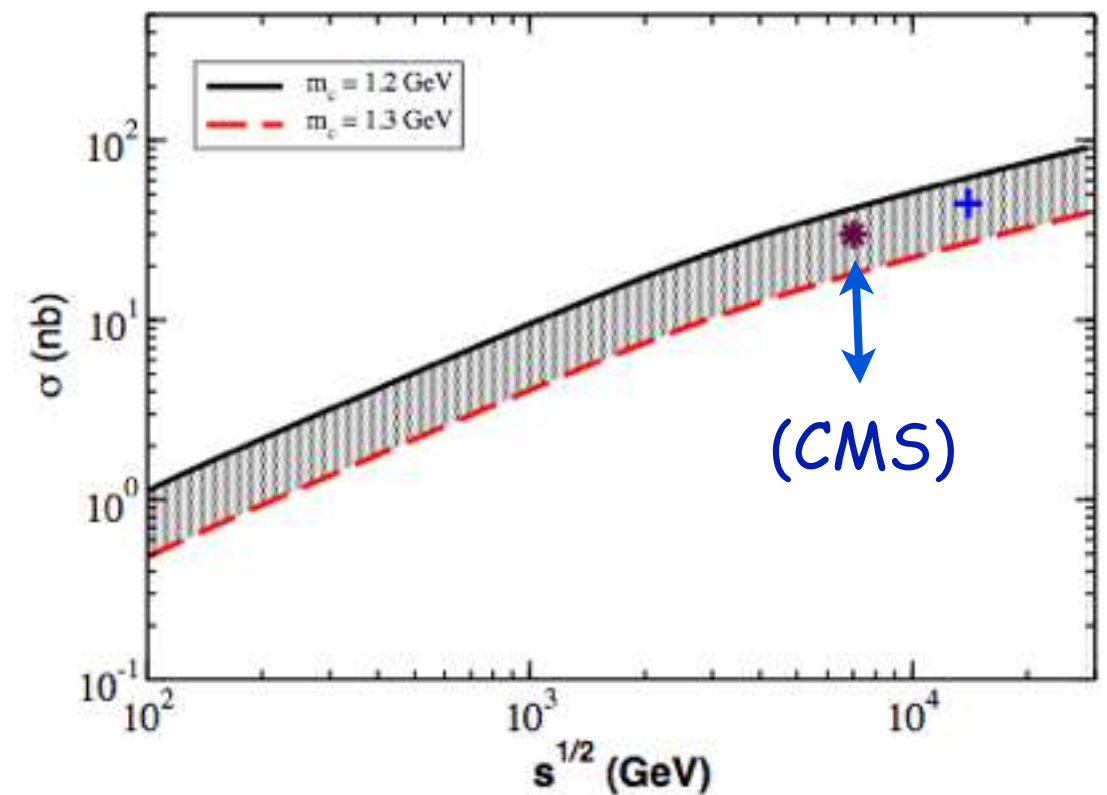
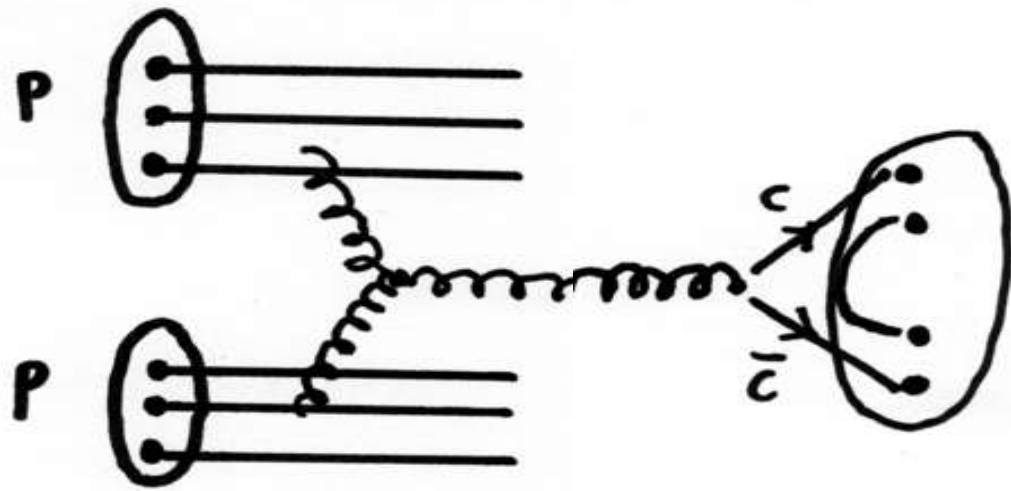
NRQCD plus production from rescattering of $D\bar{D}^*$ created at a point: molecular approach can describe the CDF data ! E Braaten, L-P He, K Ingles, arXiv:1811.08876

Tetraquark

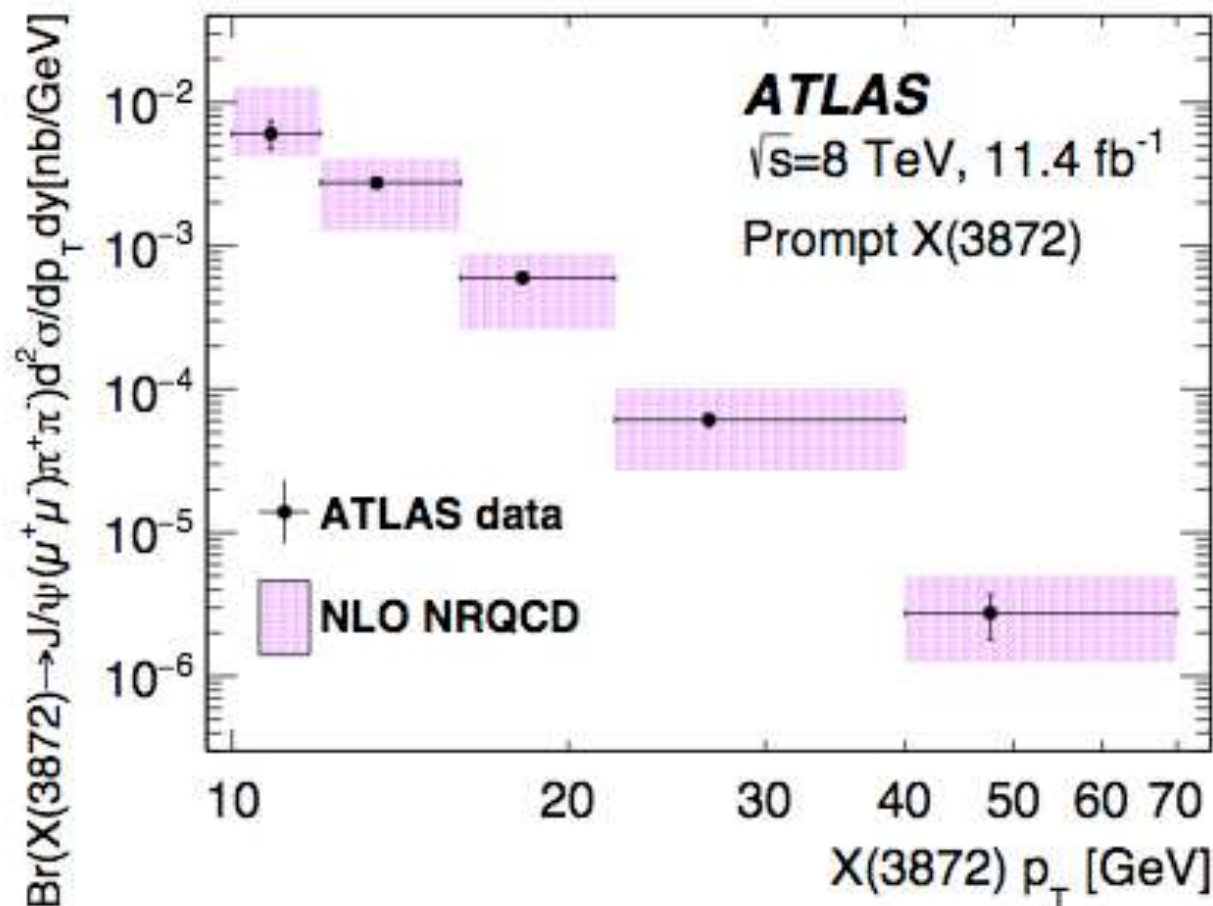


double parton scattering with parameters fixed to reproduce CMS data (Carvalho et al., arXiv:1511.05209)

Tetraquark



double parton scattering with parameters fixed to reproduce CMS data (Carvalho et al., arXiv:1511.05209)



The $X(3872)$ is modeled as a mixture of a $\chi_{c1}(2P)$ and a $\bar{D}^0 D^{*0}$ molecular state.

arXiv:1610.09303

Theoretical calculation from Meng et al., arXiv:1304.6710

QCD sum rules calculation for $X(3872)$

Matheus, Narison, MN, Richard: PRD75 (07)

$$j_\mu = \frac{i\epsilon_{abc}\epsilon_{dec}}{\sqrt{2}} [(q_a^T C \gamma_5 c_b)(\bar{q}_d \gamma_\mu C \bar{c}_e^T) + (q_a^T C \gamma_\mu c_b)(\bar{q}_d \gamma_5 C \bar{c}_e^T)]$$

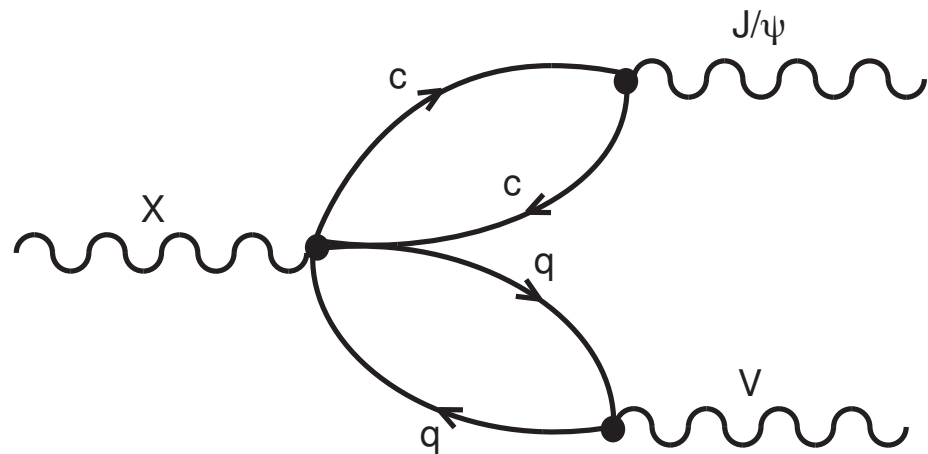
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Problem: decay width $X \rightarrow J/\psi \pi \pi \pi$
 $\sim 50 \text{ MeV}$ (Navarra, MN, PLB639 (06)272)

How to solve this problem?

X(3872) as a mixed charmonium 4-quark state

Matheus, Navarra, MN, Zanetti: PRD80 (09)

$$J_\mu^q(x) = \sin(\theta) j_\mu^{(4q)}(x) + \cos(\theta) j_\mu^{(2q)}(x)$$

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$$m_X = (3.77 \pm 0.18) \text{ GeV}$$

$$5^\circ \leq \theta \leq 13^\circ$$

Compatible with the experimental X(3872) mass

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$$\frac{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^- \pi^0)}{\mathcal{B}(X \rightarrow J/\psi \pi^+ \pi^-)} = 1.0 \pm 0.4 \pm 0.3 \rightarrow j_\mu^X(x) = \cos \alpha J_\mu^u(x) + \sin \alpha J_\mu^d(x)$$

$$\alpha \sim 20^\circ$$

Decay width $X \rightarrow J/\psi \pi^+ \pi^- \pi^0$

$$\Gamma = (9.3 \pm 6.9) \text{ MeV}, 5^\circ \leq \theta \leq 13^\circ$$

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Decay width $X \rightarrow J/\psi \gamma$

MN, Zanetti: PRD82 (10)



$$\frac{\Gamma(X \rightarrow J/\psi \gamma)}{\Gamma(X \rightarrow J/\psi \pi^+ \pi^-)} = 0.14 \pm 0.05$$

$$5^\circ \leq \theta \leq 13^\circ$$



$$\frac{\Gamma(X \rightarrow J/\psi \gamma)}{\Gamma(X \rightarrow J/\psi \pi^+ \pi^-)} = 0.19 \pm 0.13$$

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Production rate $B^+ \rightarrow X(3872)K^+$

Matheus, MN, Zanetti: PLB702 (11)

$$5^0 \leq \theta \leq 13^0 \rightarrow \mathcal{B}(B \rightarrow X(3872)K) = (1.00 \pm 0.68) \times 10^{-5}$$



$$\mathcal{B}(B^\pm \rightarrow K^\pm X(3872)) < 3.2 \times 10^{-4}$$

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$$\mathcal{B}(B^\pm \rightarrow K^\pm X(3872)) < 3.2 \times 10^{-4}$$

- $X(3872)$ is probably a mixed multiquark state with a χ_{c1} state

Conclusions

$X(3872) \rightarrow$ mixture χ_{c1} and a 4-quark state

$Z_c^+(3900) \rightarrow J^P=1^+$ tetraquark state

$Z_c^+(4430) \rightarrow$ first radial excitation of $Z_c^+(3900)$

- Z^+ states need confirmation. A bump in the spectra does not indicate, necessarily, the existence of a state

$Y(4260) \rightarrow$ mixture of charmonium and a 4-quark state

$Y(4660) \rightarrow$ tetraquark quark state $[cs][\bar{c}\bar{s}]$



Thank you!