

# Light Inflation – Reconciling $\phi^4$ Inflation with Planck and Experimental Prospects

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# Outline

- 1 Minimally extending the Standard Model
- 2  $\phi^4$  inflation after Planck
  - Minimally coupled inflation
  - Non-minimally coupled inflation
- 3 Coupling to the SM and cosmological constraints
  - The full model
  - Constraints from reheating and radiative corrections
- 4 Anything interesting in the laboratory?
  - Direct inflaton search
  - Is the Higgs compatible?

# Standard Model of particle physics

Three Generations  
of Matter (Fermions) spin  $\frac{1}{2}$

|          | I   | II  | III   |                                      |                         |
|----------|---|---|---|--------------------------------------|-------------------------|
| mass →   | 2.4 MeV   | 1.27 GeV  | 171.2 GeV   | 0                                    | 0                       |
| charge → | $\frac{2}{3}$   | $\frac{2}{3}$   | $\frac{2}{3}$   | 0                                    | 0                       |
| name →   | Left <b>u</b> Right<br>up                                 | Left <b>c</b> Right<br>charm                            | Left <b>t</b> Right<br>top                              | <b>g</b><br>gluon                    |                         |
|          | 4.8 MeV   | 104 MeV   | 4.2 GeV   | 0                                    | 0                       |
|          | $-\frac{1}{3}$  | $-\frac{1}{3}$  | $-\frac{1}{3}$  | 0                                    | 0                       |
| Quarks   | Left <b>d</b> Right<br>down                               | Left <b>s</b> Right<br>strange                          | Left <b>b</b> Right<br>bottom                           | <b><math>\gamma</math></b><br>photon |                         |
|          | 0 eV  | 0 eV  | 0 eV  | 91.2 GeV                             | $>114$ GeV              |
|          | 0   | 0   | 0   | 0                                    | 0                       |
|          | Left <b><math>\nu_e</math></b> Right<br>electron neutrino | Left <b><math>\nu_\mu</math></b> Right<br>muon neutrino | Left <b><math>\nu_\tau</math></b> Right<br>tau neutrino | <b>Z<sup>0</sup></b><br>weak force   | <b>H</b><br>Higgs boson |
|          | 0.511 MeV   | 105.7 MeV   | 1.777 GeV   | 80.4 GeV                             |                         |
|          | -1  | -1  | -1  | $\pm 1$                              |                         |
| Leptons  | Left <b>e</b> Right<br>electron                           | Left <b><math>\mu</math></b> Right<br>muon              | Left <b><math>\tau</math></b> Right<br>tau              | <b>W<sup>±</sup></b><br>weak force   | spin 0                  |

Bosons (Forces) spin 1

# Standard Model and nothing else above up to Planck scale?

- No heavy particles/scales
  - no physical high scale quadratic contributions to the Higgs boson mass
  - hierarchy problem is not that scary (however, the gravity should be generous enough not to give quadratically divergent contributions)
  - Processes at the highest energy (inflation) may be directly related to the low energy properties

# Standard Model – extended for inflation

Some models that minimally expand the SM and have inflation

- Higgs inflation
  - very direct relation of inflation and SM, some subtleties with the UV properties
- $R^2$  inflation
  - purely gravitational solution, nothing interesting for the particle physics
- Light inflaton with non-minimal coupling
  - this talk, solution on the particle physics side

Note – the whole Universe evolution should be fully described within the model!

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# “Standard” chaotic inflation

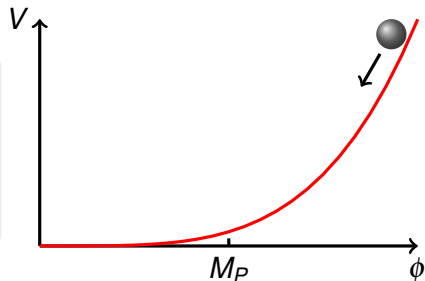
## Scalar part of the action

$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\beta}{4} \phi^4 \right\}$$

Required to get  
 $\delta T/T \sim 10^{-5}$

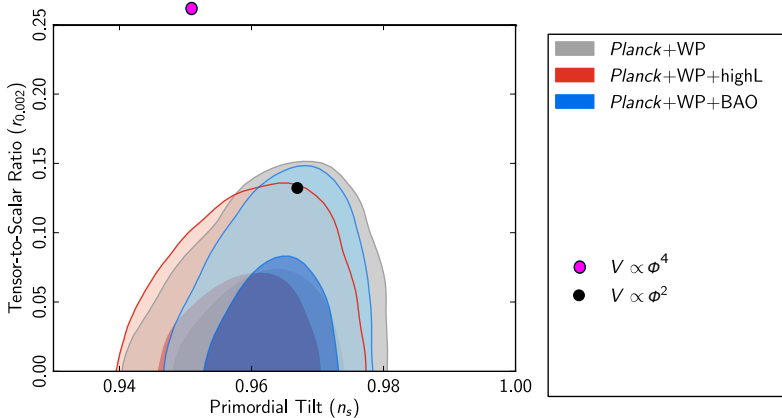
$$\beta \sim 10^{-13}$$

$$m \sim 10^{13} \text{ GeV}$$



Fields  $\gtrsim M_P$ , energy  $\sim \lambda^{1/4} M_P$ .

# Planck results disfavor plain $\phi^4$





# Non-minimal coupling to gravity leads to good inflation

## Scalar action with non-minimal coupling

$$S = \int d^4x \sqrt{-g} \left\{ -\frac{M_P^2}{2} R - \frac{\xi}{2} \phi^2 R + \frac{\partial_\mu \phi \partial^\mu \phi}{2} - \frac{\lambda}{4} \phi^4 \right\}$$

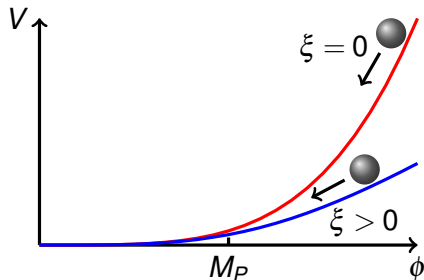
Conformal transformation to the Einstein frame

$$\hat{g}_{\mu\nu} = \sqrt{1 + \frac{\xi \phi^2}{M_P^2}} g_{\mu\nu},$$

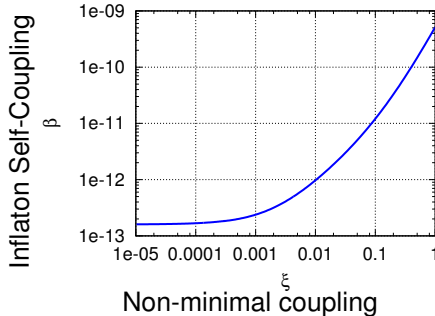
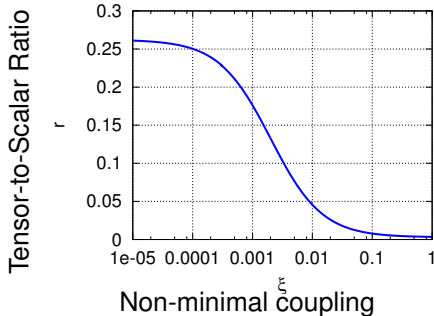
flattens the potential

$$V(\phi) \rightarrow \hat{V}(\phi) = \frac{V(\phi)}{(1 + \xi \phi^2 / M_P^2)^2}$$

(Change of the field  $\frac{d\chi}{d\phi} = \sqrt{\frac{1 + (\xi + 6\xi^2)\phi^2 / M_P^2}{(1 + \xi \phi^2 / M_P^2)^2}}$  is also needed)



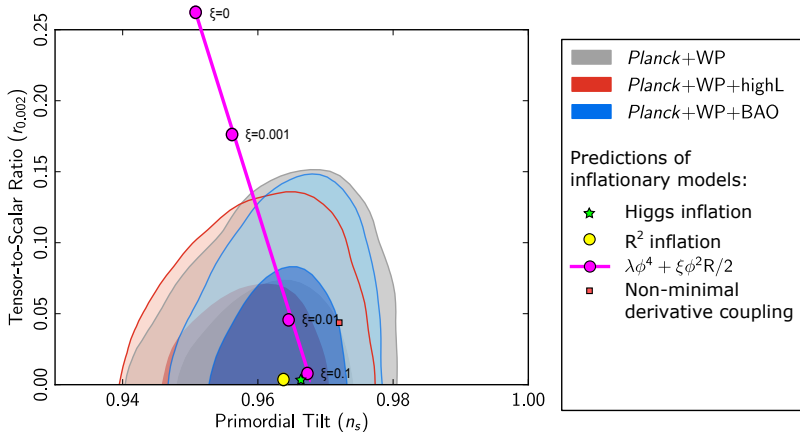
# The tensor perturbations are suppressed, inflaton self-coupling $\beta$ is increased



For each  $\xi$  the self-coupling  $\beta$  is fixed by  $\delta T/T \simeq 10^{-5}$  requirement.

[Tsujiikawa, Gumjudpai'04, FB'08, Okada, Rehman, Shafi'10]

# Inflationary predictions are ok for $\xi \gtrsim 0.003$



# SM + Light Inflaton coupled in the Higgs sector only

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \alpha H^\dagger H \phi^2 + \frac{\beta}{4} \phi^4 + \frac{\xi}{2} \phi^2 R$$

Standard Model
Interaction
Inflationary sector

Inflaton mass depends on interaction strength:  $m_\chi = m_h \sqrt{\beta/2\alpha}$

Specifically: the Higgs-inflaton scalar potential is

$$V(H, \phi) = \lambda \left( H^\dagger H - \frac{\alpha}{\lambda} \phi^2 \right)^2 + \frac{\beta}{4} \phi^4 - \frac{1}{2} \mu^2 \phi^2 + V_0$$

We assumed here, that the scale invariance is broken *in the inflaton sector only*

[Shaposhnikov, Tkachev'06, Anisimov, Bartocci, FB'09, FB, Gorbunov'10,13]

# All constants of the model are bound from cosmology

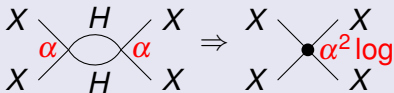
CMB normalization sets

$\beta(\xi)$

$$\beta = \frac{3\pi^2 \Delta_{\mathcal{R}}^2}{2} \frac{(1+6\xi)(1+6\xi+8(N+1)\xi)}{(1+8(N+1)\xi)(N+1)^3}$$

$\alpha \lesssim \beta^2$  (mass lower bound)

Inflation is not spoiled by the radiative corrections



CMB tensor modes bound  $\xi$

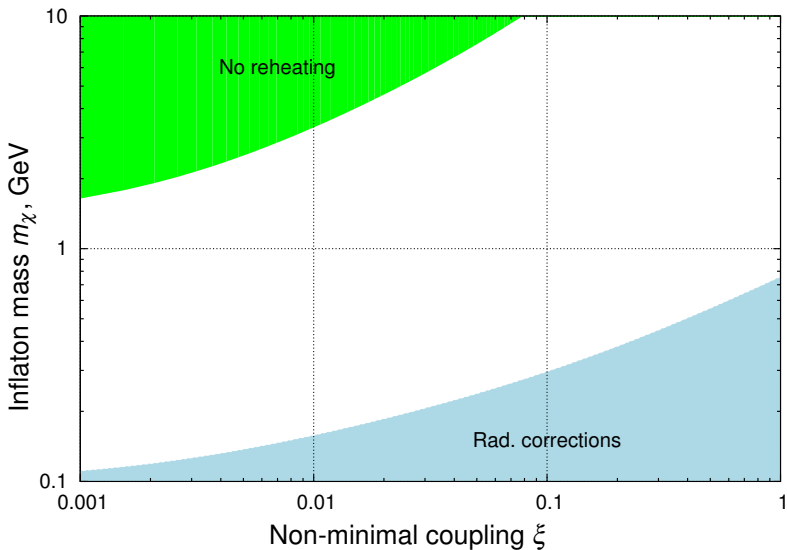
$$r = \frac{16(1+6\xi)}{(N+1)(1+8(N+1)\xi)} \lesssim 0.15$$

$\alpha > 10^{-7}$  (mass upper bound)

Sufficient reheating

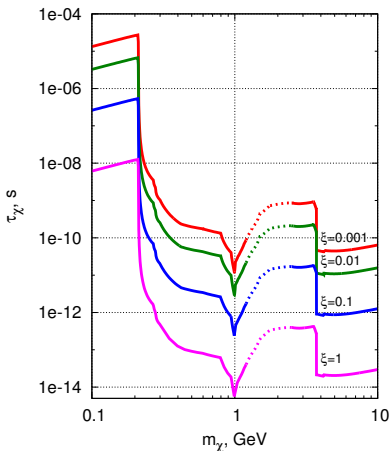
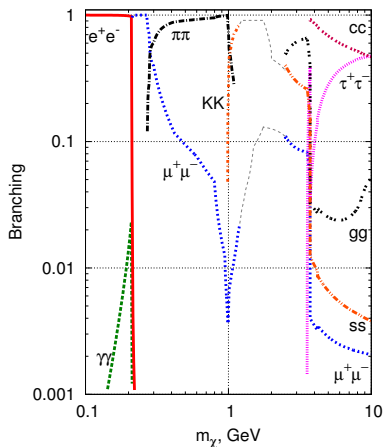
- After inflation: empty & cold
- Needed: hot,  
 $T_r \gtrsim 150$  GeV (to get baryogenesis)

# The Inflaton mass is bounded from cosmology



# Inflaton decays and lifetime

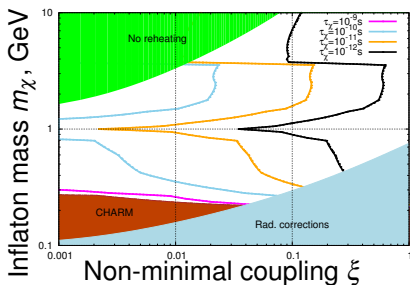
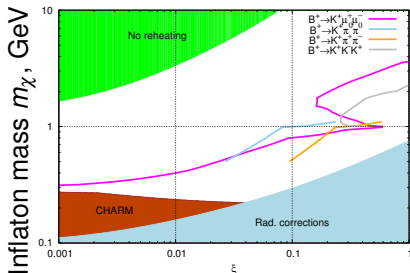
Coupled to everything proportional particle mass



Created in meson decays:

$$\text{Br}(B \rightarrow \chi X_s) \simeq 10^{-6} \frac{\beta(\xi)}{1.5 \times 10^{-13}} \frac{300 \text{ MeV}^2}{m_\chi}$$

# Experimental searches are possible



Behaves as light “Higgs” boson, suppressed by  $\theta = \sqrt{2\beta} v / m_\chi$

- Created in meson decays
- Decays:  $KK$ ,  $\pi\pi$ ,  $\mu\mu$ ,  $ee$ , ...
- Interacts with media: extremely weakly

Search (LHCb, Belle)

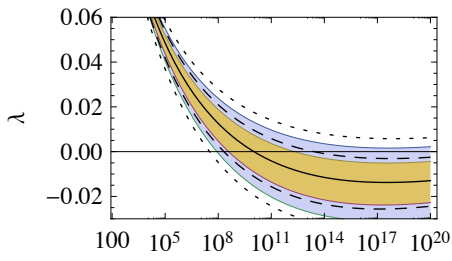
- Events with offset vertices in B decays
- Peaks in Dalitz plot of three body B decays



## Another prediction: The Higgs boson can not be light

Inflation proceeds along  $H^\dagger H = \frac{\alpha}{\lambda} X^2 \Rightarrow H$  is large at inflation

- The Higgs self-coupling  $\lambda$ : must be positive up to inflationary scales



Higgs mass  
 $m_H = 125.3 \text{ GeV}$

yScale  $\mu$ , GeV

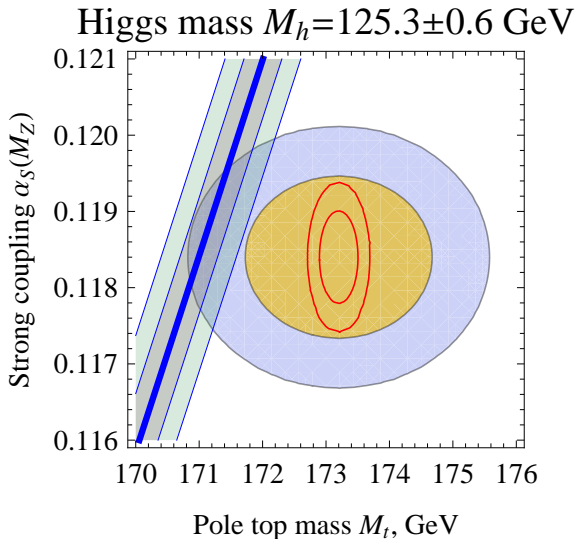
Current experimental value:  $m_H = 125.7 \pm 0.4 \text{ GeV}$  (CMS)

Mass for  $\lambda(\mu) = \beta_\lambda(\mu) = 0$

$$M_{\min} = \left[ 129.5 + \frac{M_t - 173.2 \text{ GeV}}{0.9 \text{ GeV}} \times 1.8 - \frac{\alpha_s - 0.1184}{0.0007} \times 0.6 \pm 2 \right] \text{ GeV}$$

[FB, Kalmykov, Kniehl, Shaposhnikov'12, Degraasi et.al'12]

# Critical Higgs mass is compatible with $M_t$ and $\alpha_s$



# Conclusions 1: Cosmology

- Single field quartic inflation with *small* non-minimal coupling is perfectly ok with the current CMB observations

## Conclusions 2: Cosmology and Particle Physics

- An example of a model minimally extending SM without any heavy scales: a singlet scalar field with non-minimal coupling
- Cosmological observations constrain the inflaton mass to be light (in GeV range) – interesting for particle physics!
- Further study
  - Detection of tensor modes is especially interesting to constrain the theory
  - The inflaton can be searched in low energy experiments – rare B decays
    - Offset vertices in B decays
    - Peaks in B three body decay Dalitz plot
  - Higgs mass bounds – top quark mass measurement is needed!

# Backup slides

# Dark matter – add $\nu$ MSM and stir

Three Generations  
of Matter (Fermions) spin  $\frac{1}{2}$

|         | I                            | II                         | III                        |                              |
|---------|------------------------------|----------------------------|----------------------------|------------------------------|
| mass    | 2.4 MeV                      | 1.27 GeV                   | 171.2 GeV                  |                              |
| charge  | $\frac{2}{3}$                | $\frac{2}{3}$              | $\frac{2}{3}$              | 0                            |
| name    | u<br>up                      | c<br>charm                 | t<br>top                   | g<br>gluon                   |
| Quarks  |                              |                            |                            | 0                            |
|         | d<br>down                    | s<br>strange               | b<br>bottom                | $\gamma$<br>photon           |
|         |                              |                            |                            | 91.2 GeV                     |
|         | $\nu_e$<br>electron neutrino | $\nu_\mu$<br>muon neutrino | $\nu_\tau$<br>tau neutrino | Z <sup>0</sup><br>weak force |
|         | $N_1$<br>sterile neutrino    | $N_2$<br>sterile neutrino  | $N_3$<br>sterile neutrino  | >114 GeV                     |
| Leptons |                              |                            |                            | H<br>Higgs boson             |
|         | e<br>electron                | $\mu$<br>muon              | $\tau$<br>tau              | spin 0                       |
|         |                              |                            |                            | 80.4 GeV                     |
|         |                              |                            |                            | W <sup>±</sup><br>weak force |

Bosons (Forces) spin 1

## Role of sterile neutrinos

$N_1$  (Warm) Dark Matter,  $M_1 \sim 1\text{--}50$  keV

$N_{2,3}$  Baryogenesis,  $M_{2,3} \sim \dots$  GeV

Dark matter – add  $\nu$ MSM and stirA  $\nu$ MSM inspired model with inflation  $\chi$ 

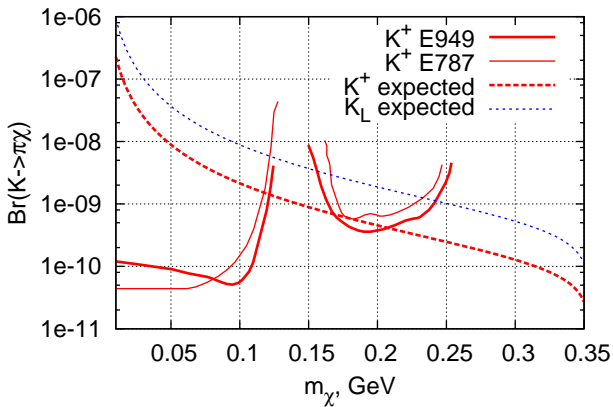
$$\mathcal{L} = (\mathcal{L}_{SM} + \bar{N}_I i \partial_\mu \gamma^\mu N_I - F_{\alpha I} \bar{L}_\alpha N_I \Phi - \frac{f_I}{2} \bar{N}_I^c N_I X + \text{h.c.}) + \frac{1}{2} (\partial_\mu X)^2 - V(\Phi, X)$$

$$\Omega_N = \frac{1.6 f(m_\chi)}{S} \cdot \frac{\beta}{1.5 \times 10^{-13}} \cdot \left( \frac{M_1}{10 \text{keV}} \right)^3 \cdot \left( \frac{100 \text{ MeV}}{m_\chi} \right)^3,$$

DM sterile neutrino mass is related to the inflaton mass

$$M_1 \simeq 13 \cdot \left( \frac{m_\chi}{300 \text{ MeV}} \right) \left( \frac{S}{4} \right)^{1/3} \cdot \left( \frac{0.9}{f(m_\chi)} \right)^{1/3} \text{ keV}.$$

# Production: bound from $K^+ \rightarrow \pi^+ + \text{nothing}$

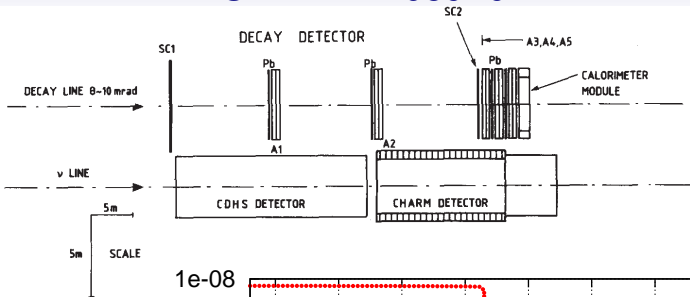


Excluded:  $m_\chi \lesssim 120$  MeV

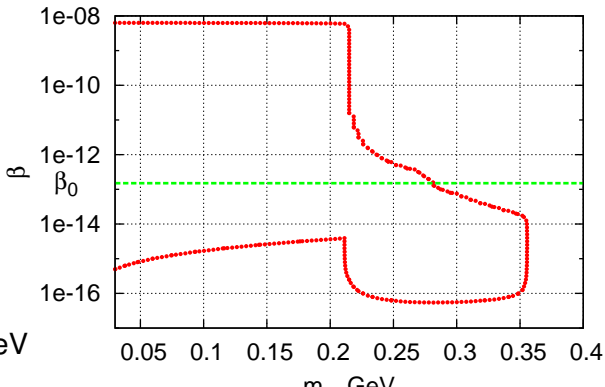
Disfavoured:  $170 \text{ MeV} \lesssim m_\chi \lesssim 205 \text{ MeV}$



## CHARM – bound



Search  
for  
decays of  
some-  
thing into  
 $\gamma\gamma$ ,  $e^+e^-$ ,  
 $\mu^+\mu^- \Rightarrow$   
 $m_\chi < 270 \text{ MeV}$



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