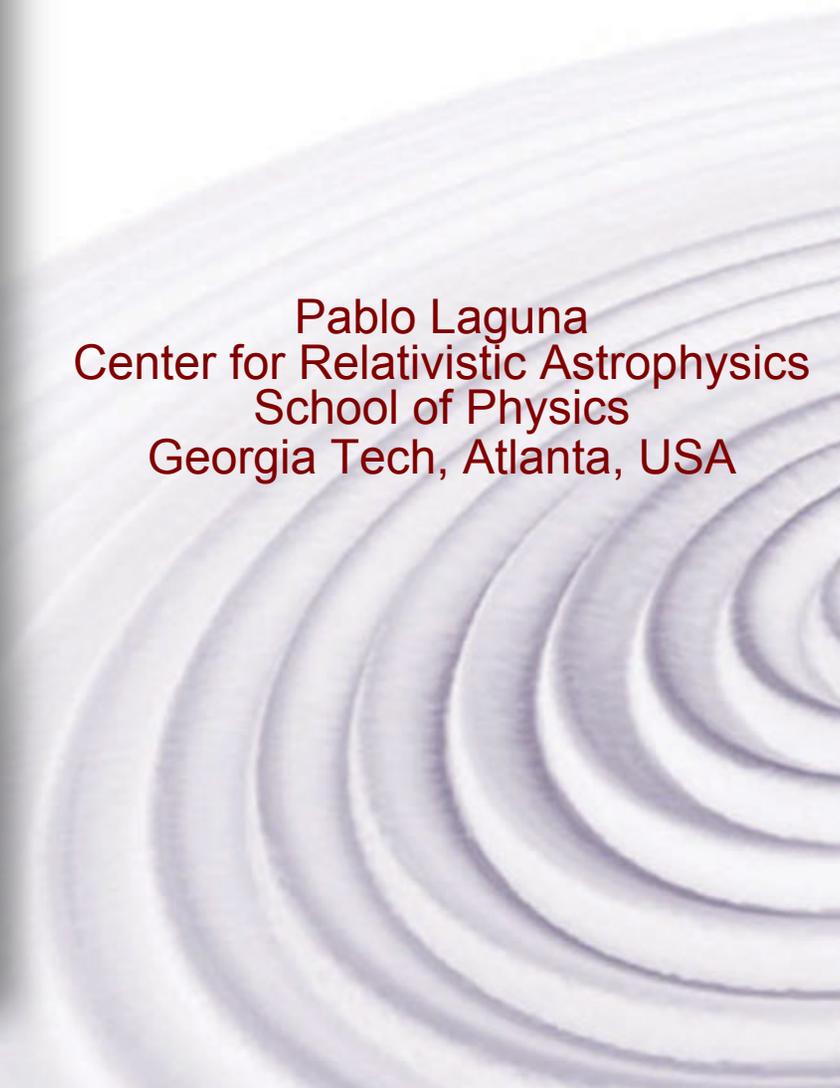


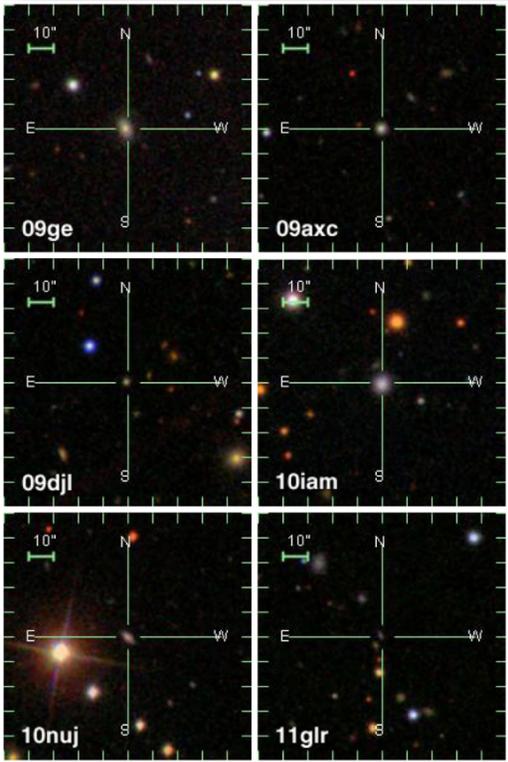
Pablo Laguna  
Center for Relativistic Astrophysics  
School of Physics  
Georgia Tech, Atlanta, USA



The background of the right side of the slide is a grayscale image of concentric, overlapping ripples, representing gravitational waves.

# The Transient Sky

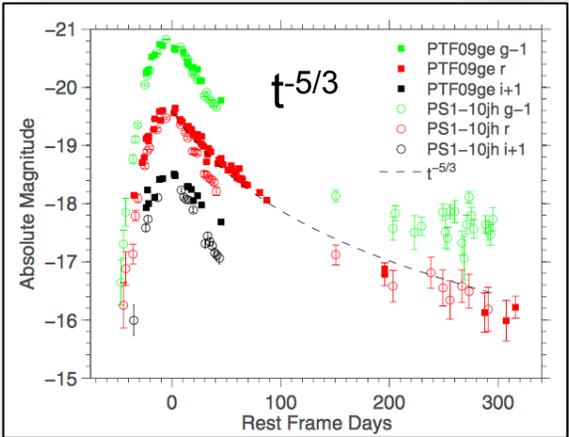
SN, GRBs, AGN or TDEs?



Arcavi et al. 2014, ApJ, 793, 38



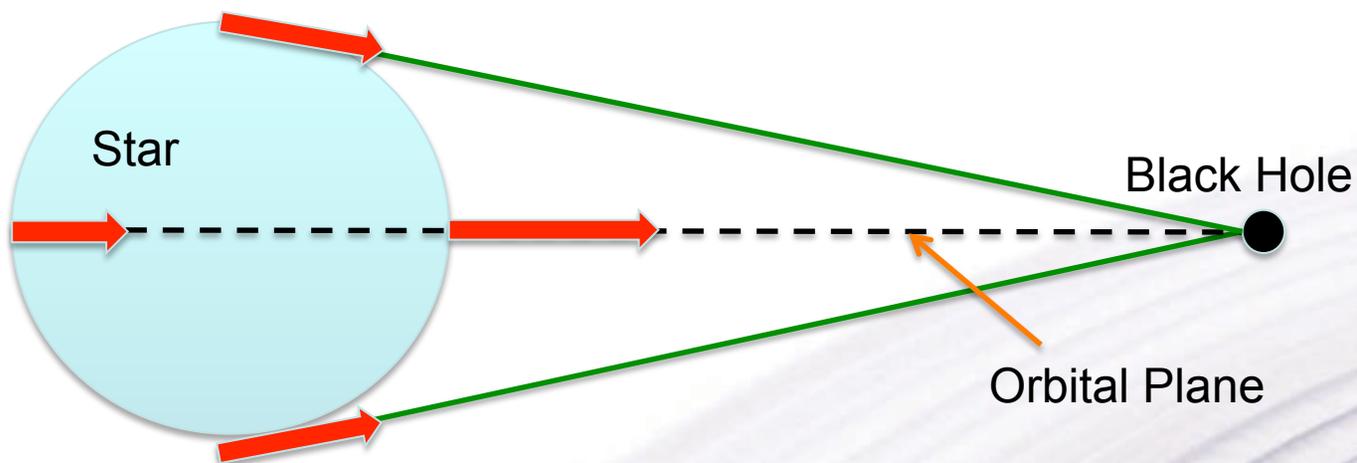
van Velzen et al. 2011, ApJ, 741, 73



If TDEs, we will learn about

- Demographics of MBHs in quiescent galaxies
- Constraints on low mass galaxies hosting MBHs
- Growth of MBHs by accreting gas at super-Eddington rates
- Stellar dynamics in the neighborhood of MBH

# Tidal Forces



$$\frac{GmM_*}{R_*^2} = \frac{GmM_h}{(R_t - R_*)^2} - \frac{GmM_h}{(R_t + R_*)^2} \approx \frac{GmM_h R_*}{R_t^3}$$

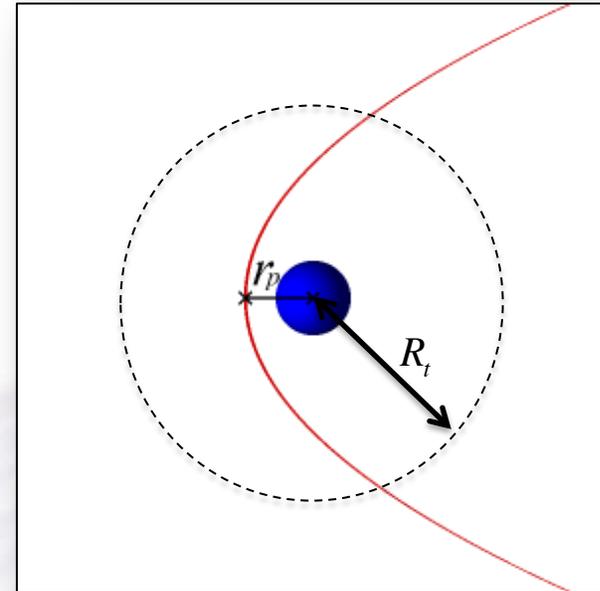
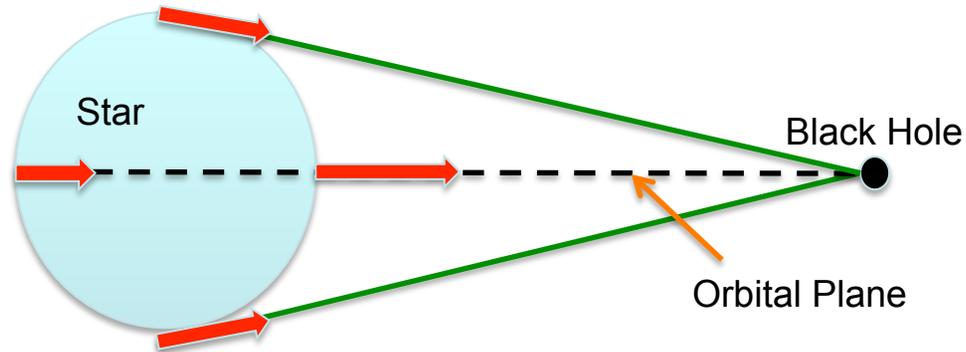
$$\frac{M_*}{R_*^2} \approx \frac{M_h R_*}{R_t^3}$$

$$R_t \approx R_* \left( \frac{M_h}{M_*} \right)^{1/3}$$

Tidal Radius

- Stretching along the orbital plane
- Compression perpendicular to the orbital plane

# Tidal Radius and Penetration Factor



$$R_t = R_* \left( \frac{M_h}{M_*} \right)^{1/3}$$

Tidal Radius

$$\beta \equiv \frac{R_t}{R_p}$$

Penetration Factor

Main Sequence

$$\frac{R_t}{M_{bh}} \approx 47 \left( \frac{R_{ms}}{R_\odot} \right) \left( \frac{M_{ms}}{M_\odot} \right)^{-1/3} \left( \frac{M_{bh}}{10^6 M_\odot} \right)^{-2/3}$$

White Dwarf

$$\frac{R_t}{M_{bh}} \approx 22 \left( \frac{R_{wd}}{0.95 R_\oplus} \right) \left( \frac{M_{wd}}{M_\odot} \right)^{-1/3} \left( \frac{M_{bh}}{10^4 M_\odot} \right)^{-2/3}$$

# Triangle of Astrophysical Relevance

Tidal Radius

$$R_t \equiv R_* \left( \frac{M_h}{M_*} \right)^{1/3}$$

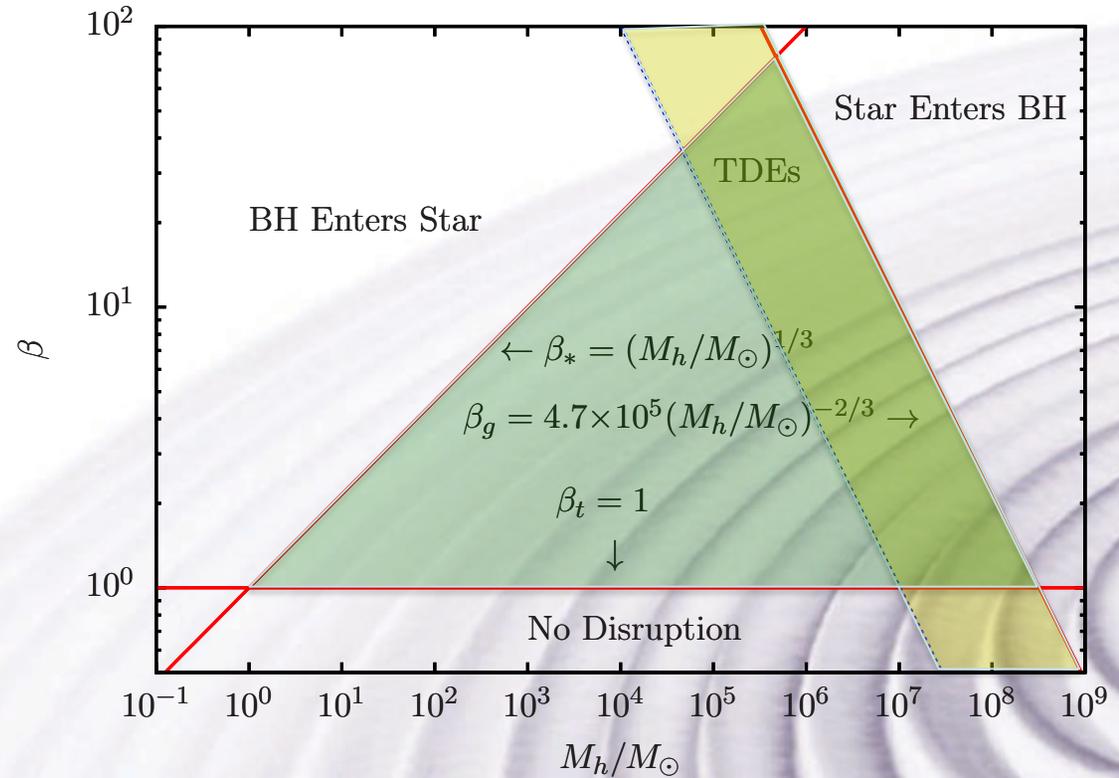
Penetration Factor

$$\beta(R_p) \equiv \frac{R_t}{R_p} = \frac{R_*}{R_p} \left( \frac{M_h}{M_*} \right)^{1/3}$$

$$\beta_t = \beta(R_t) = 1$$

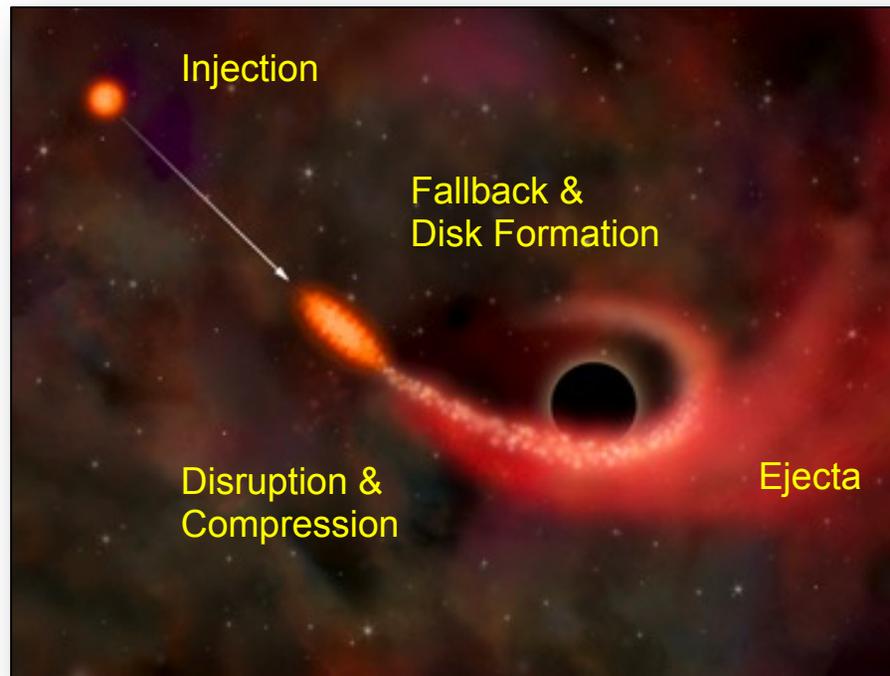
$$\beta_* = \beta(R_*) = \left( \frac{M_h}{M_*} \right)^{1/3}$$

$$\beta_g = \beta(R_g) = \frac{R_*}{GM_* / c^2} \left( \frac{M_h}{M_*} \right)^{-2/3}$$



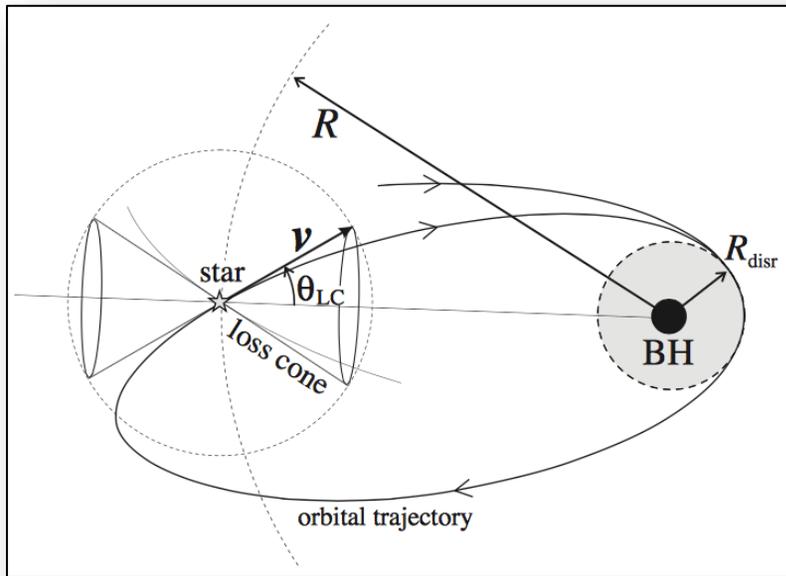
Luminet & Pichon (1989)

# The Disruption of a Star: What to Look For



- Near periapsis, the star disrupts and compresses. Detonation, multiple bounces, and gravitational waves are possible outcomes.
- Fallback material yields an accretion disk (soft x-rays), with super-Eddington outflows (optical/UV) and relativistic jets (radio/x-rays)
- Unbound material could also yield emission lines if irradiated by the disk

# TDE: The Capture



Freitag & Benz

**Loss Cone:** Set of orbital directions that leads to capture or disruption

Event rate depends on how the **Loss Cone** gets populated

Stars enter the **Loss Cone** via collisions with other stars or relaxation

Stars can also be ejected from the **Loss Cone** via collisions.

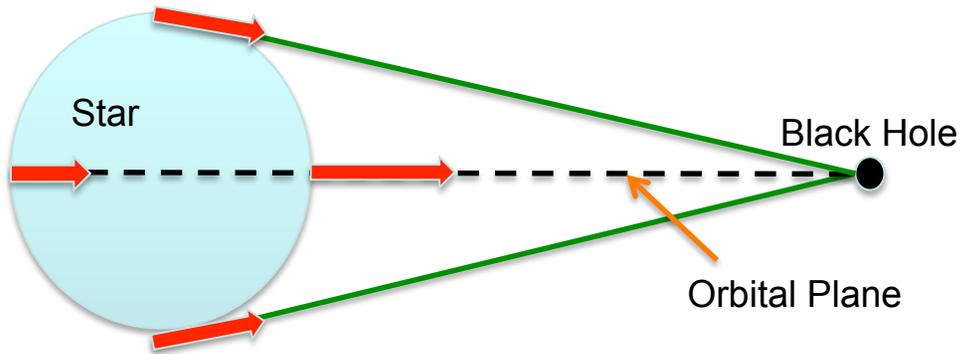
Event rate  $\sim 10^{-4} \text{ yr}^{-1}$

$$L \leq L_{LC} \approx \sqrt{2GM_h R_{LC}}$$

$$\text{If } R_{LC} \approx R_h \approx \frac{GM_h}{\sigma^2} \text{ star is captured}$$

$$\text{If } R_{LC} \approx R_t \approx R_* \left( \frac{M_h}{M_*} \right)^{1/3} \text{ star is disrupted}$$

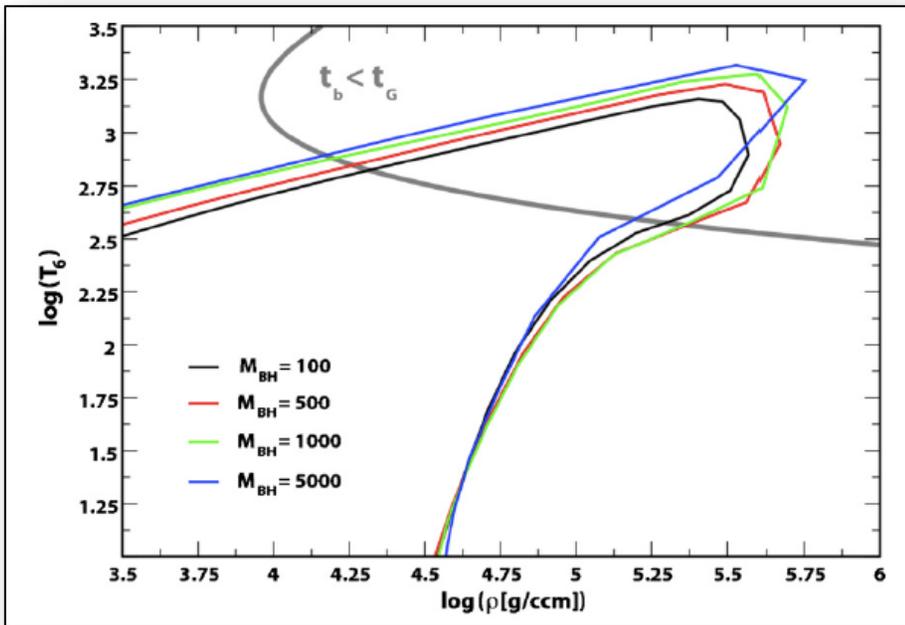
# Tidal Compression



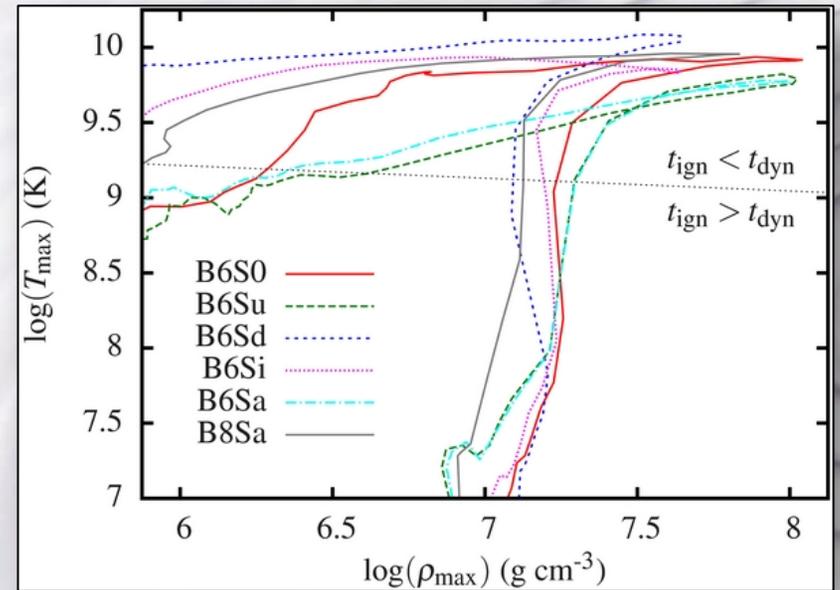
$$\rho_{max} \sim \rho_* \beta^3$$

$$T_{max} \sim T_* \beta^2$$

Carter & Luminet 1993

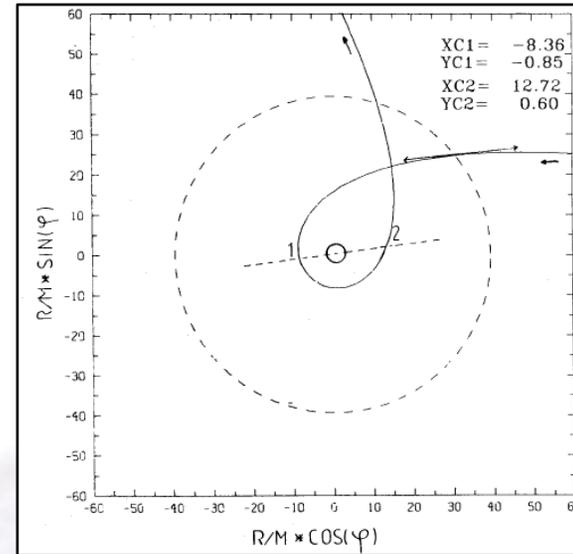
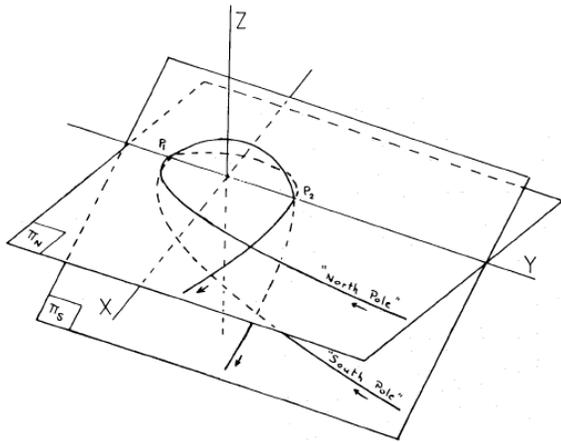


Rosswog, Ramirez-Ruiz, Hix

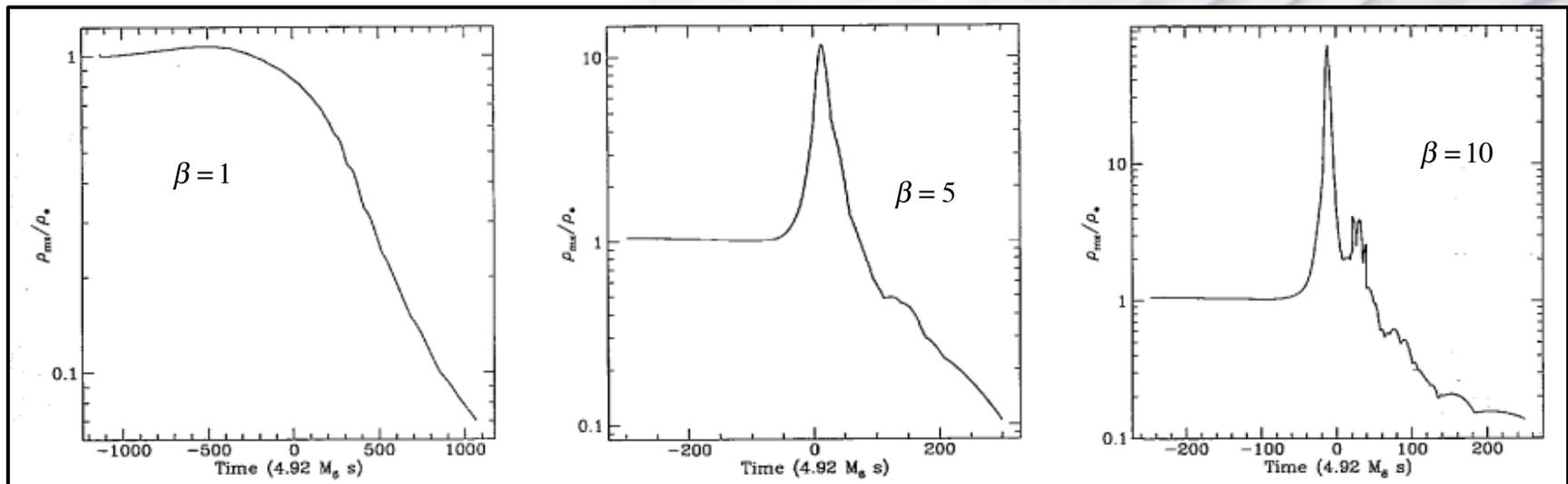


Haas, Shcherbakov, Bode, PL

# Multiple Tidal Compression



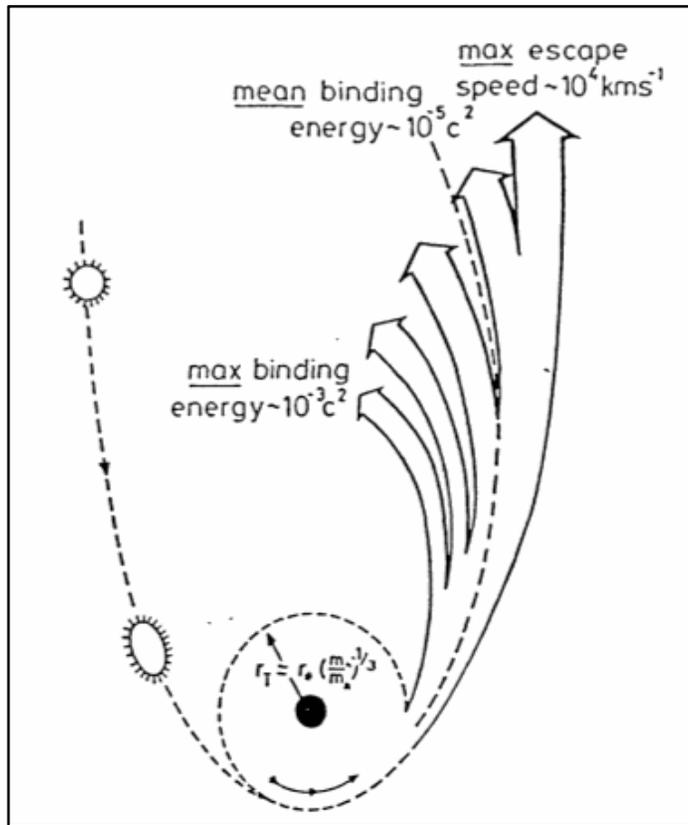
Luminet & Marck, 1985, MNRAS, 212, 57



Laguna, Miller, Zurek & Davies 1993, ApJL 410, 83

# Fallback Material

$$\dot{M} = \frac{dM}{d\epsilon} \frac{d\epsilon}{dt} \propto \frac{d\epsilon}{dt} \quad \text{if } \frac{dM}{d\epsilon} \approx \text{const}$$



Rees 1988

Recall

$$\epsilon \sim \frac{M_{bh}}{a}$$

$$P \propto a^{3/2}$$



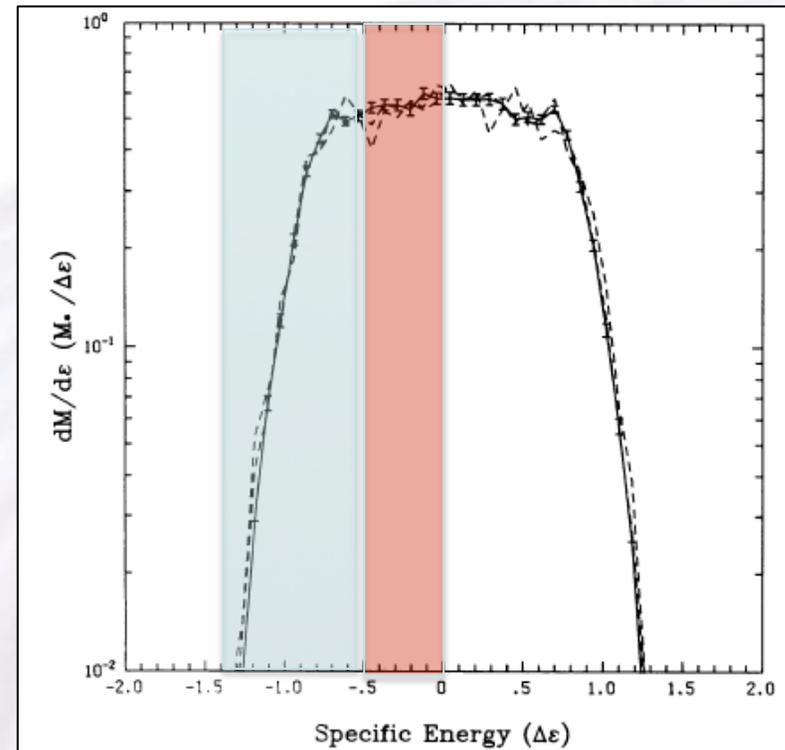
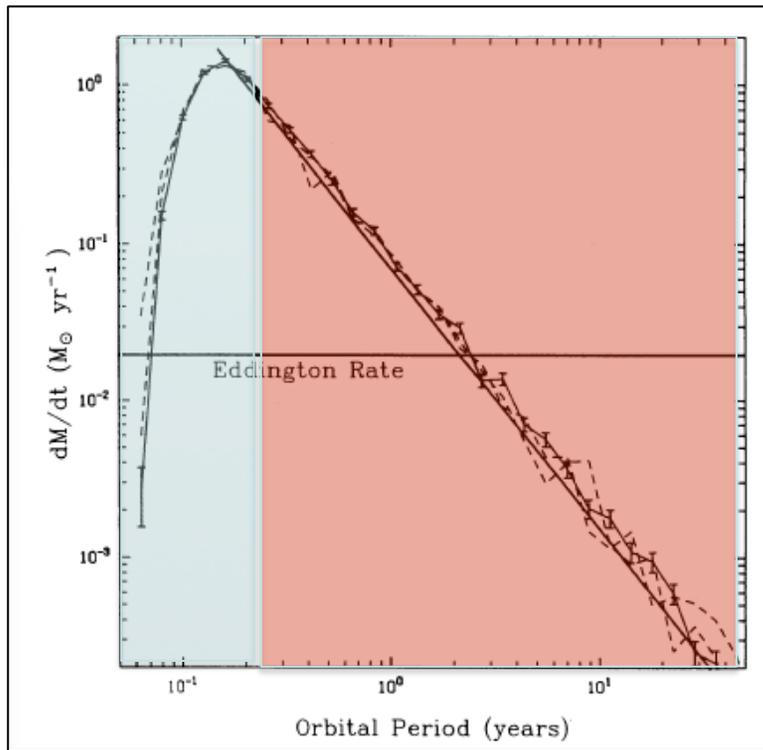
$$\epsilon \sim P^{-2/3}$$

$$\frac{d\epsilon}{dt} \propto t^{-5/3}$$

$$L \propto \dot{M} \propto t^{-5/3}$$

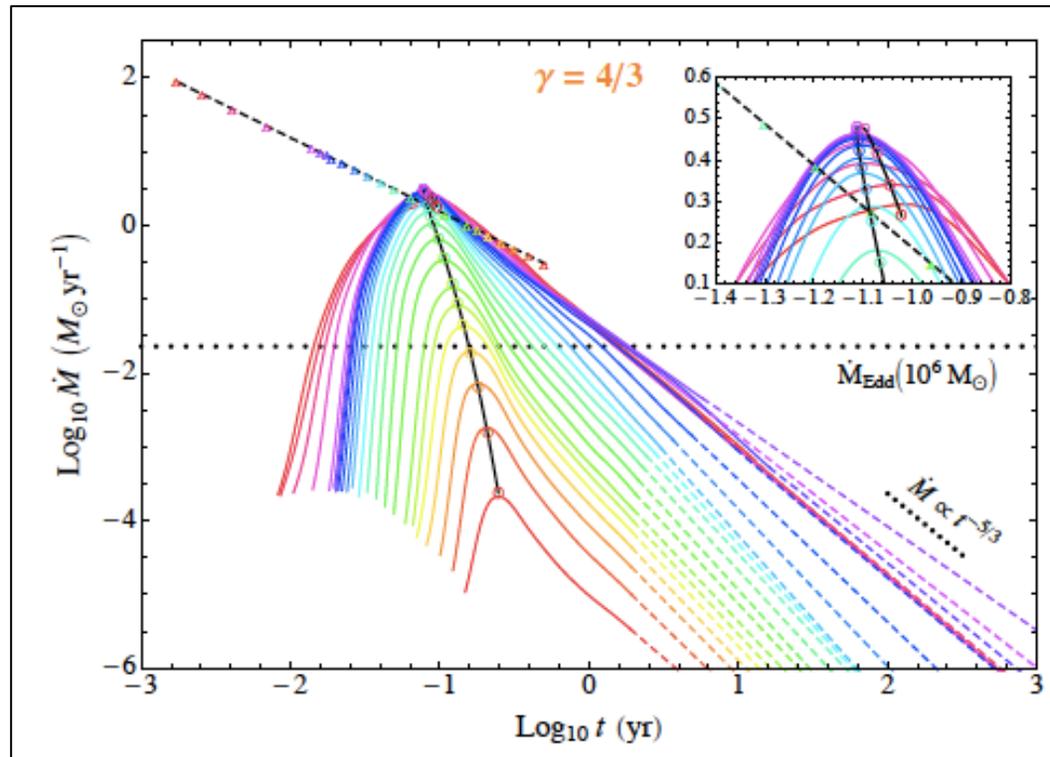
# The TDE Smoking Gun

$$L \propto \dot{M} \propto t^{-5/3}$$



Deviations from

$$\dot{M} \propto t^{-5/3}$$

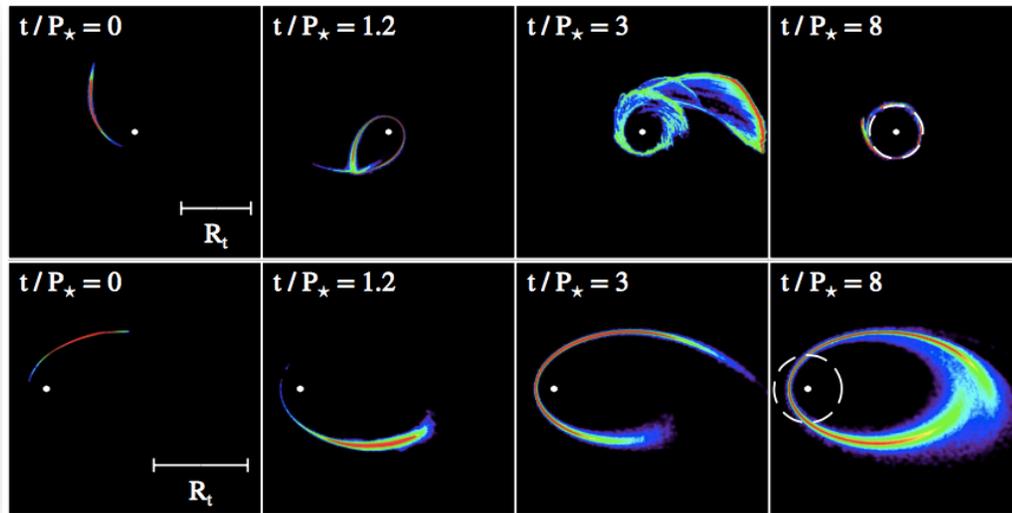


Guillochon et al

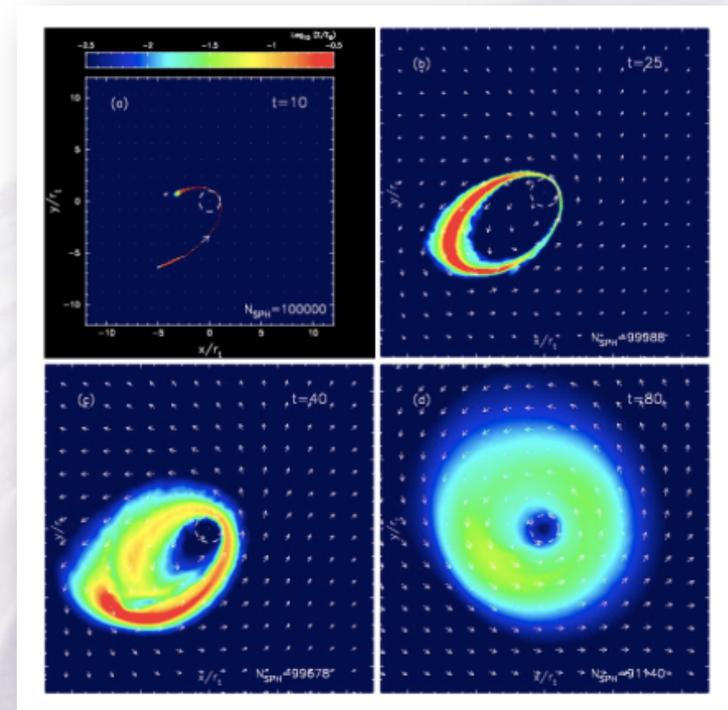
Not included:

- BH and stellar spin
- GR
- Partial disruption

# Circularization & Disk Formation

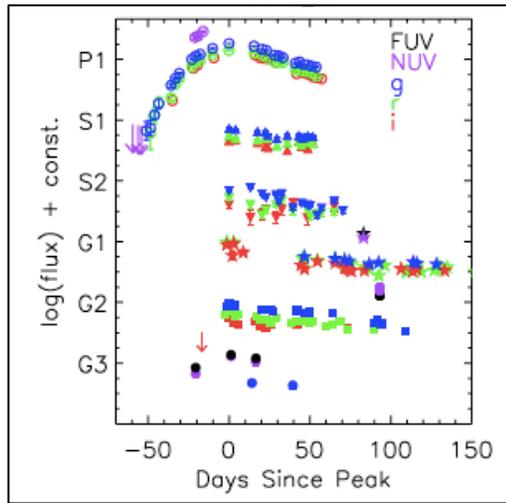


Relativistic precession could also assist in circularizing the bound debris. *Bonnerot et al*

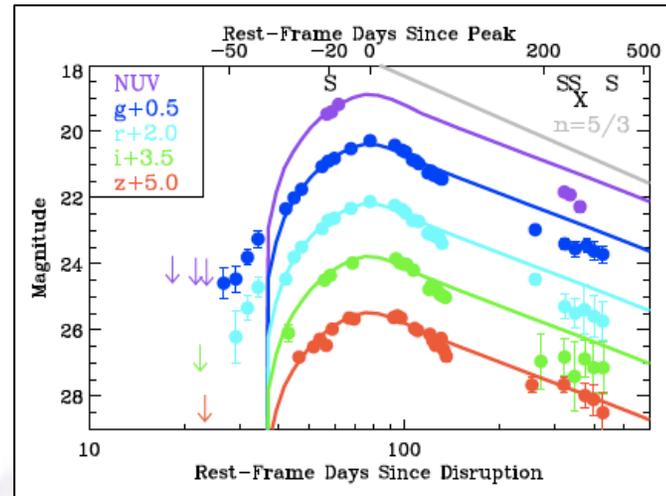


Circularization depends on the efficiency of radiative cooling. *Hayasaki, Stone & Loeb*

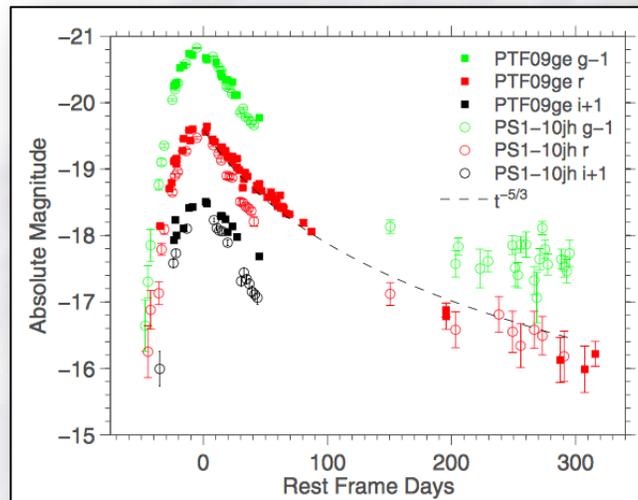
# TDE Candidates



Gezari et al

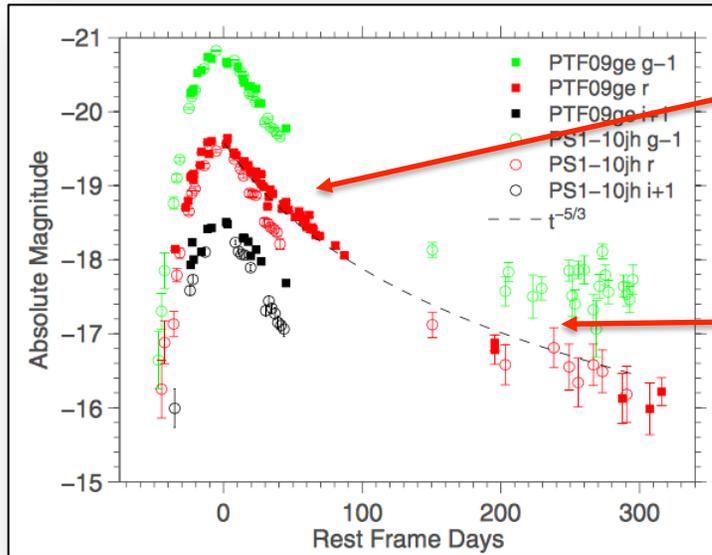


PS1-10jh



van Velzen et al. 2011, ApJ, 741, 73

# Where is the emission produced?

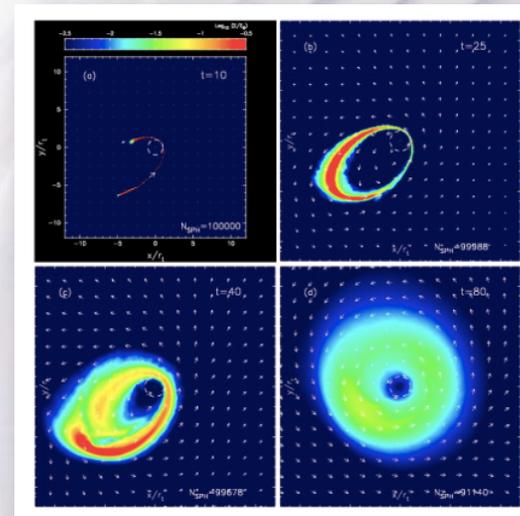
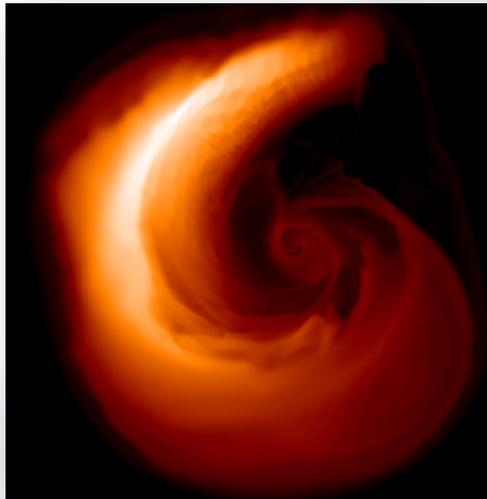


## Flare:

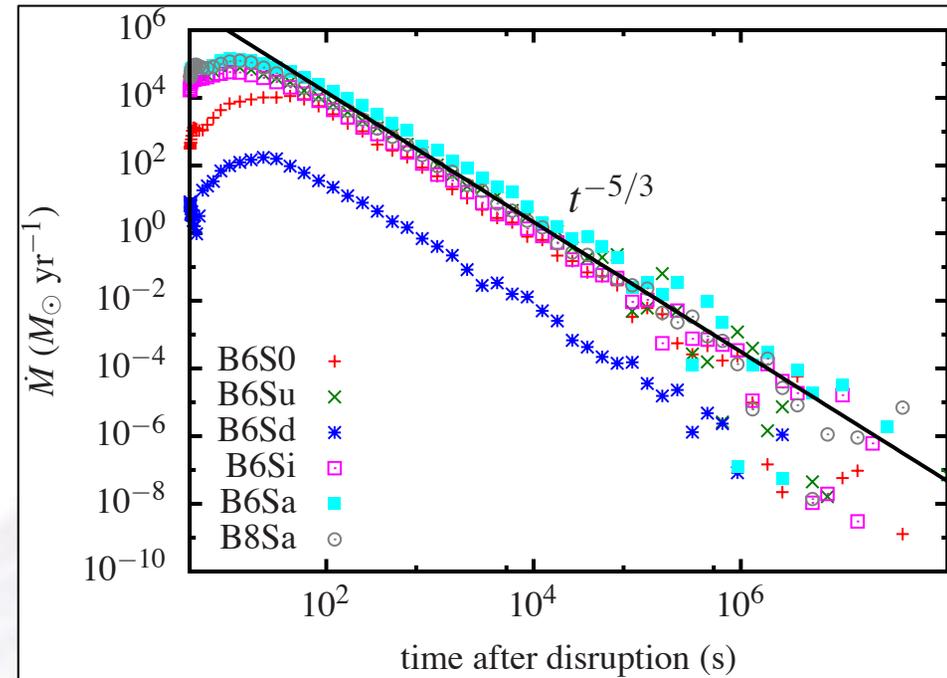
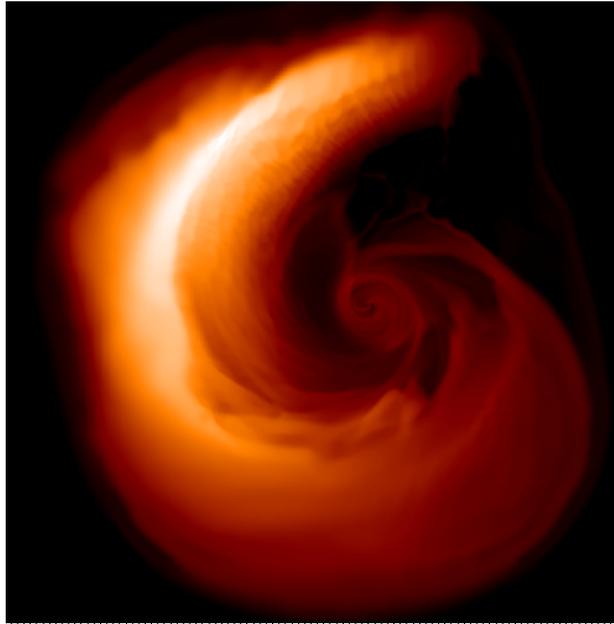
- From self-intersection
- Prompt accretion

## Power-law decay:

- From the disk?
- Direct accretion?



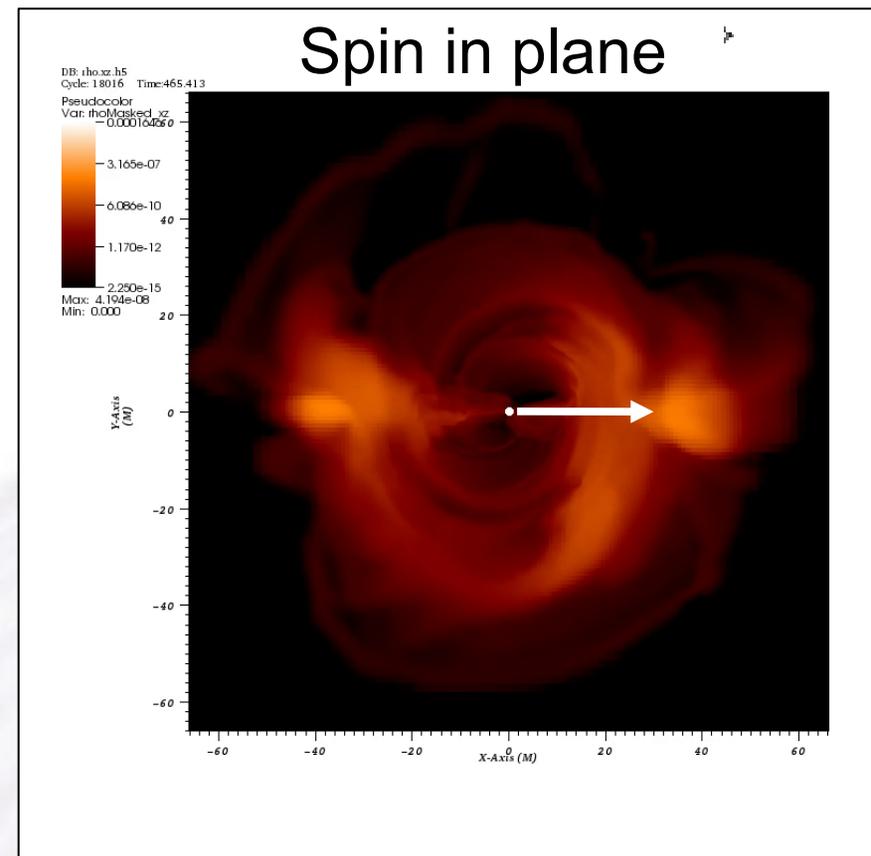
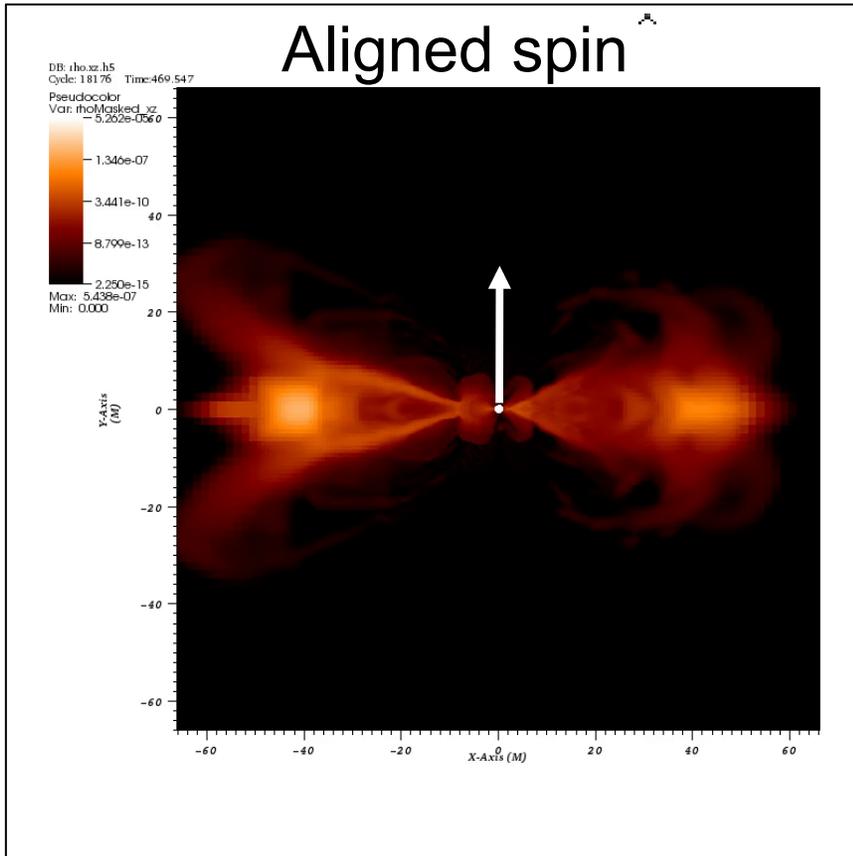
# White Dwarf TD



Haas et al 2012

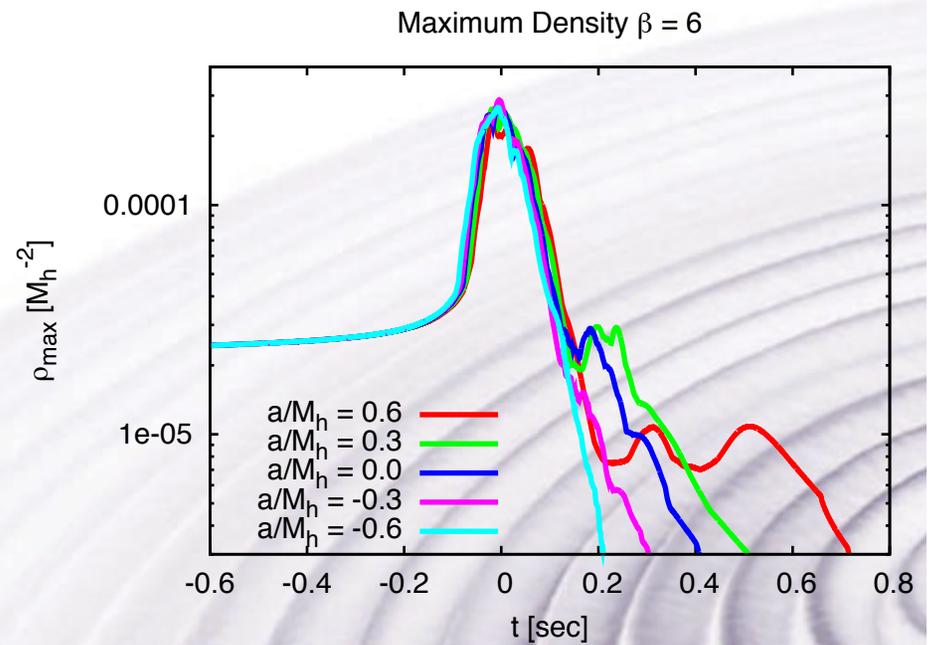
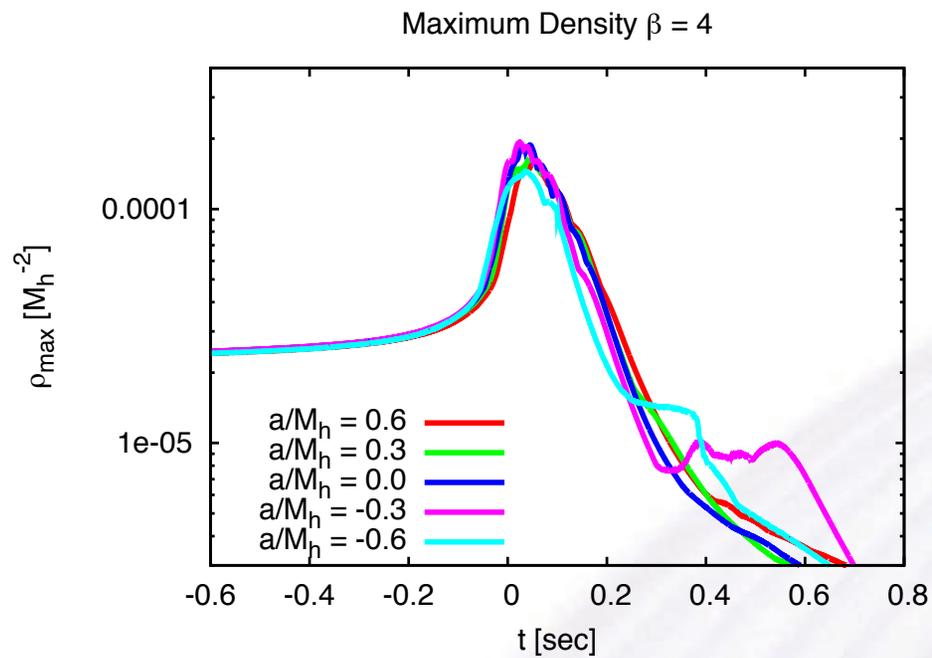
- WD disrupted by a  $1,000 M_{\text{solar}}$  BH
- Eventually fallback rate settles down to  $t^{-5/3}$
- Amplitude of accretion depends on spin and its orientation

# Effects of spin misalignment

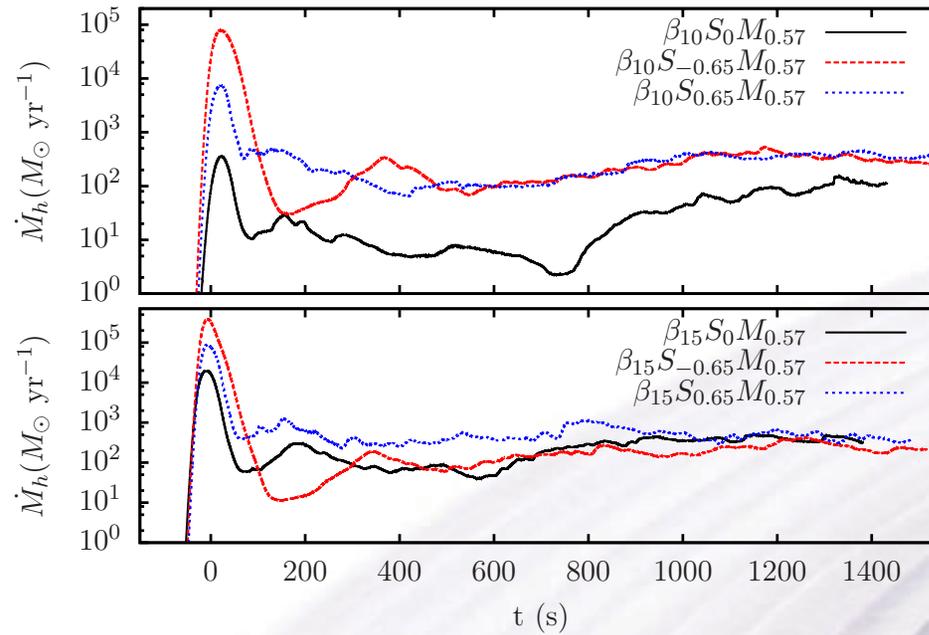


- Material is influenced by frame dragging
- Inner region obscured by debris

# Density & Temperature @ Max Compression



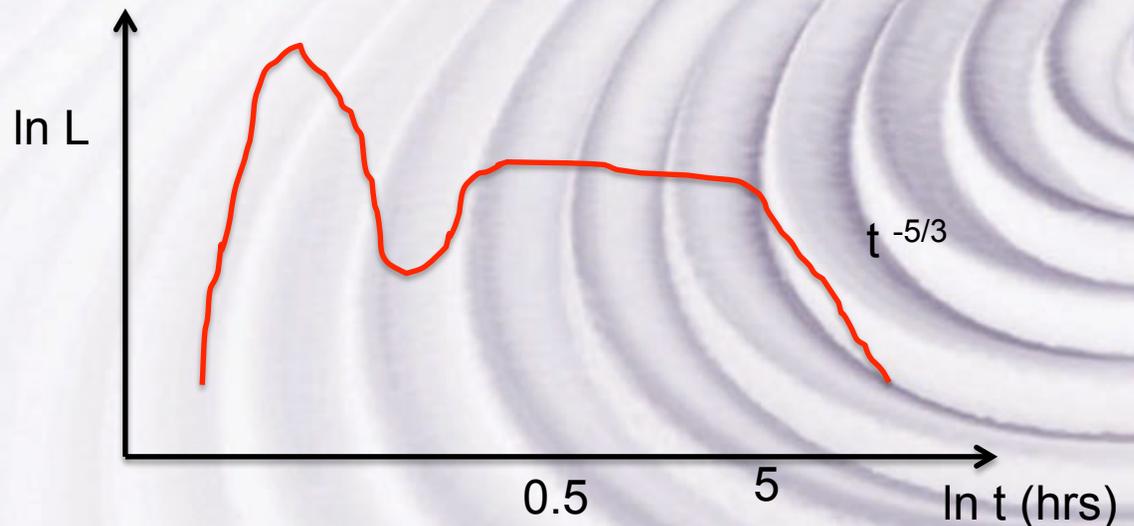
# Accretion Rates



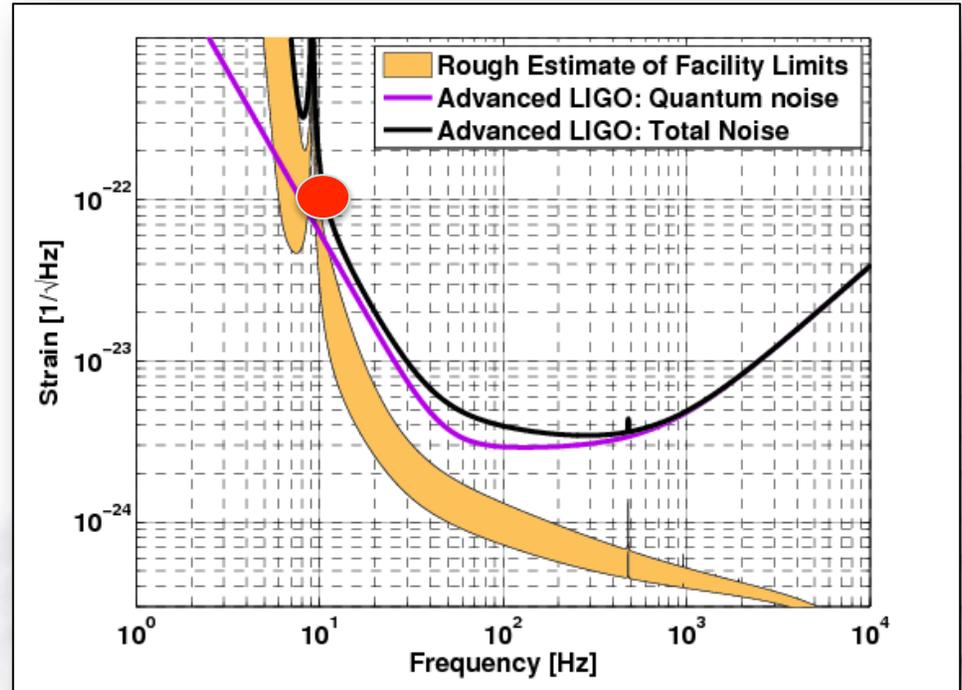
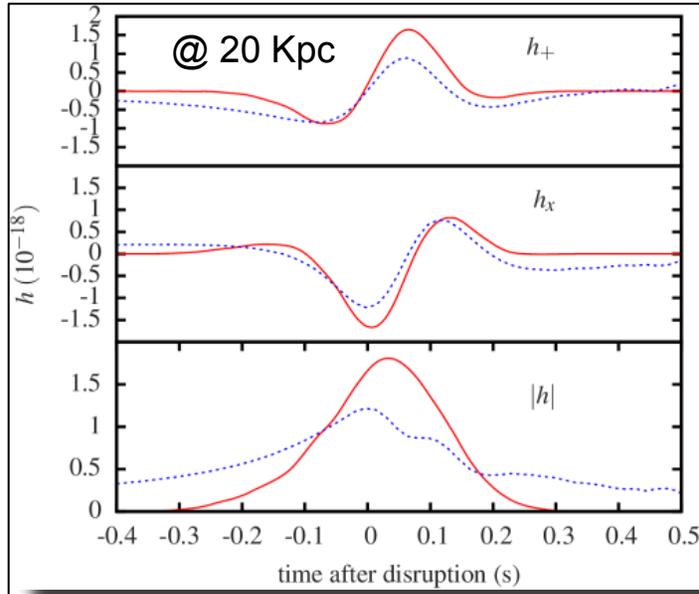
Time to swallow the bound debris:

$$T_* \approx \frac{0.5 M_\odot}{10^3 M_\odot \text{ yr}^{-1}} \sim 5 \text{ hrs}$$

Simulation time  $\sim 0.6$  hrs



# Gravitational Waves from Star-BH System

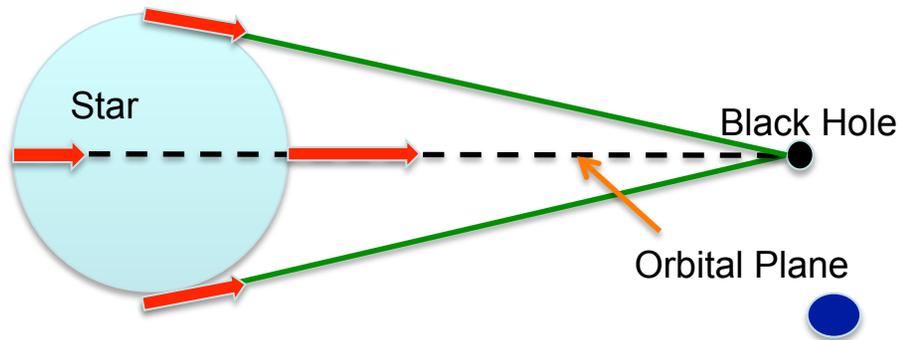


Haas, Bode, Schervakov & PL 2004

$$\begin{aligned}
 h &\sim \frac{M_* M_h}{DR_p} \sim \beta D^{-1} R_*^{-1} M_*^{4/3} M_h^{2/3} \\
 &\sim 10^{-22} \left(\frac{\beta}{10}\right) \left(\frac{D}{100 \text{ Mpc}}\right)^{-1} \left(\frac{R_{ms}}{R_\odot}\right)^{-1} \left(\frac{M_{ms}}{M_\odot}\right)^{4/3} \left(\frac{M_h}{10^6 M_\odot}\right)^{2/3} \\
 &\sim 10^{-22} \left(\frac{\beta}{10}\right) \left(\frac{D}{100 \text{ Mpc}}\right)^{-1} \left(\frac{R_{wd}}{R_\oplus}\right)^{-1} \left(\frac{M_{wd}}{M_\odot}\right)^{4/3} \left(\frac{M_h}{10^4 M_\odot}\right)^{2/3}
 \end{aligned}$$

$$\begin{aligned}
 f &\sim \left(\frac{M_{bh}}{R_p^3}\right)^{1/2} \sim \beta^{3/2} R_*^{-3/2} M_*^{1/2} \\
 &\sim 0.02 \left(\frac{\beta}{10}\right)^{3/2} \left(\frac{R_{ms}}{R_\odot}\right)^{-3/2} \left(\frac{M_{ms}}{M_\odot}\right)^{1/2} \text{ Hz} \\
 &\sim 10 \left(\frac{\beta}{10}\right)^{3/2} \left(\frac{R_{wd}}{R_\oplus}\right)^{-3/2} \left(\frac{M_{wd}}{M_\odot}\right)^{1/2} \text{ Hz}
 \end{aligned}$$

# Gravitational Waves from Star Compression

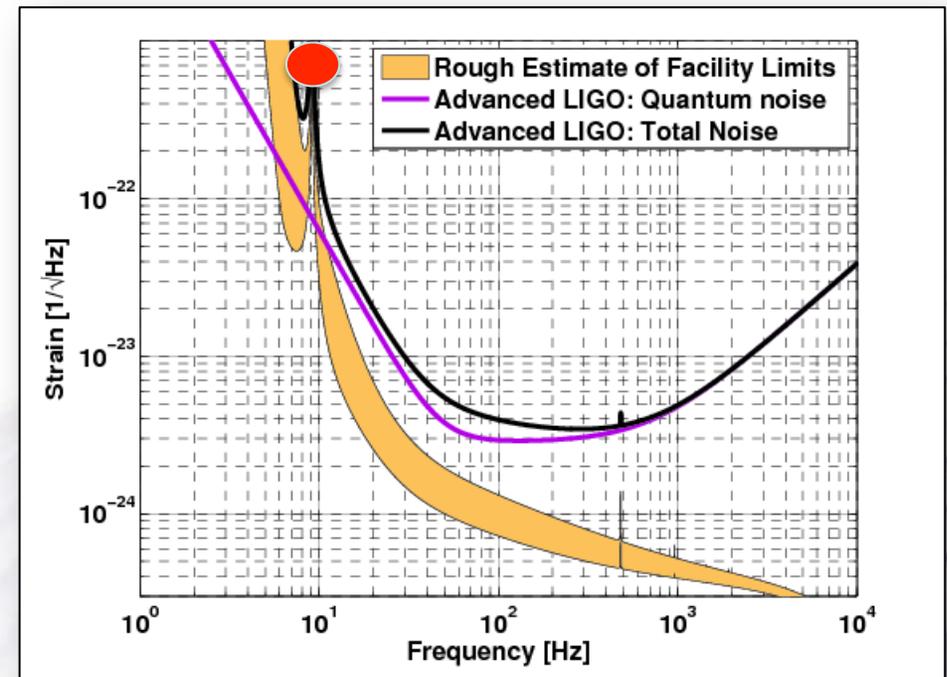


Guillichon et al 2008; Stone et al 2012

$$h \sim \frac{\beta^3 M_*^2}{D R_*}$$

$$\sim 10^{-23} \left(\frac{\beta}{10}\right)^3 \left(\frac{D}{100 \text{ Mpc}}\right)^{-1} \left(\frac{R_{ms}}{R_\odot}\right)^{-1} \left(\frac{M_{ms}}{M_\odot}\right)^2$$

$$\sim 10^{-21} \left(\frac{\beta}{10}\right)^3 \left(\frac{D}{100 \text{ Mpc}}\right)^{-1} \left(\frac{R_{wd}}{R_\oplus}\right)^{-1} \left(\frac{M_{wd}}{M_\odot}\right)^2$$



$$f \sim \beta^4 R_*^{-3/2} M_*^{1/2}$$

$$\sim 0.02 \left(\frac{\beta}{10}\right)^4 \left(\frac{R_{ms}}{R_\odot}\right)^{-3/2} \left(\frac{M_{ms}}{M_\odot}\right)^{1/2} \text{ Hz}$$

$$\sim 10 \left(\frac{\beta}{10}\right)^4 \left(\frac{R_{wd}}{R_\oplus}\right)^{-3/2} \left(\frac{M_{wd}}{M_\odot}\right)^{1/2} \text{ Hz}$$

# Summary

- For ultra-close encounters ( $R_t \sim R_g$ ), the tools of numerical relativity are needed to get the correct gas dynamics to model TDEs
- Early accretion, outflow and fallback rate will tell us about the BH's spin
- TDEs with prompt accretion will help identifying IMBH
- Magnetic fields could provided models of jetted TDEs
- TDEs of WD by IMBH could potentially be candidates for multi-messenger observations

## Questions

- What is the physics needed in TDE simulations to understand the observed luminosities beyond the estimates from accretion rates?
- Are there other ubiquitous signatures of TDEs besides the  $t^{-5/3}$  accretion rate decay.
- Jetted TDEs?