

# Quarkonium Suppression in a Hadron Gas

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# Charmonium in the QGP

Matsui-Satz, PLB (1986)

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} e^{-r/r_D} \quad r_D < r_\psi$$

If screening radius is smaller than Bohr radius:  
Quark and antiquark do not bind !  $\rightarrow$  SUPPRESSION

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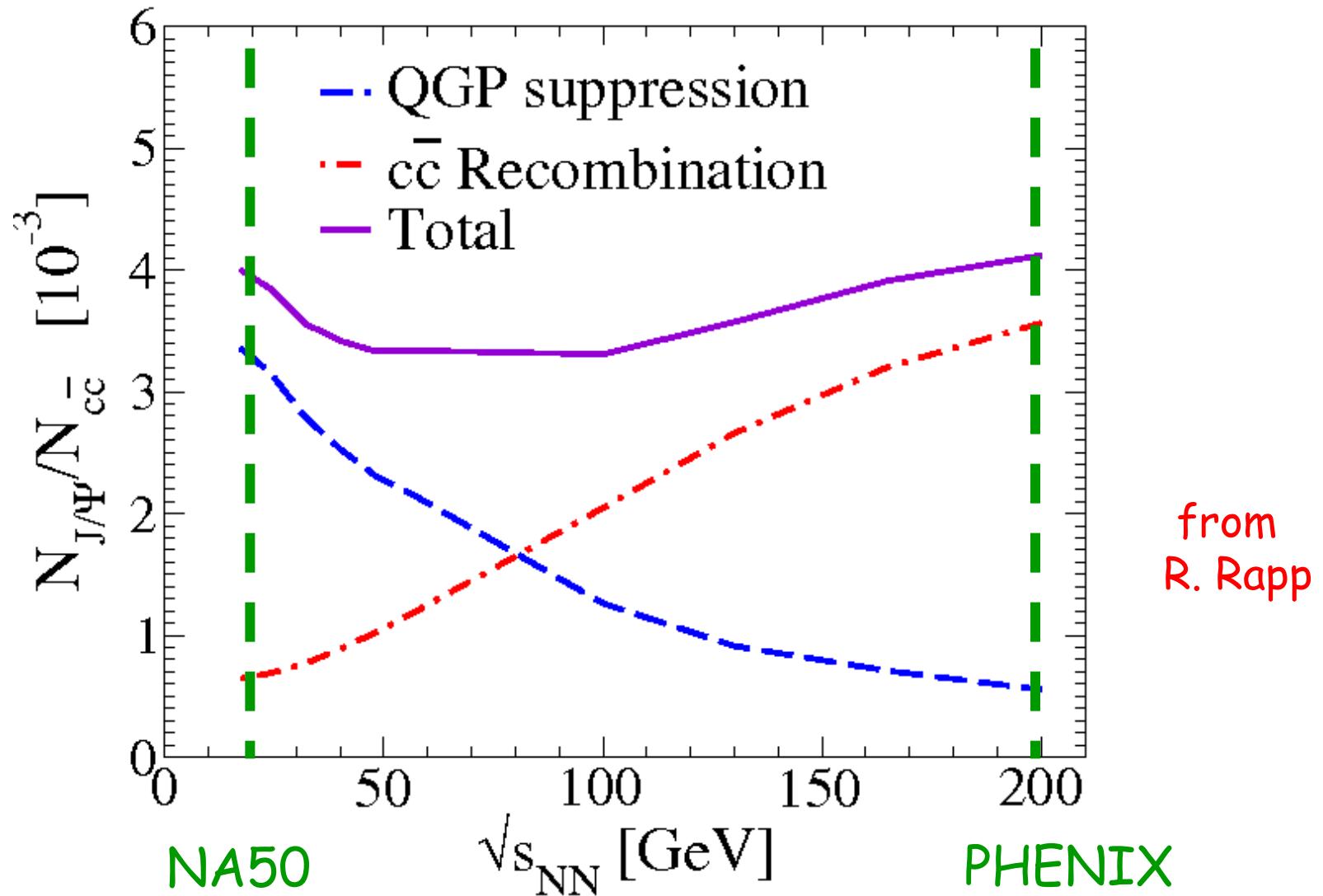
Thews-Schroedter-Rafelski, PRC (2001)

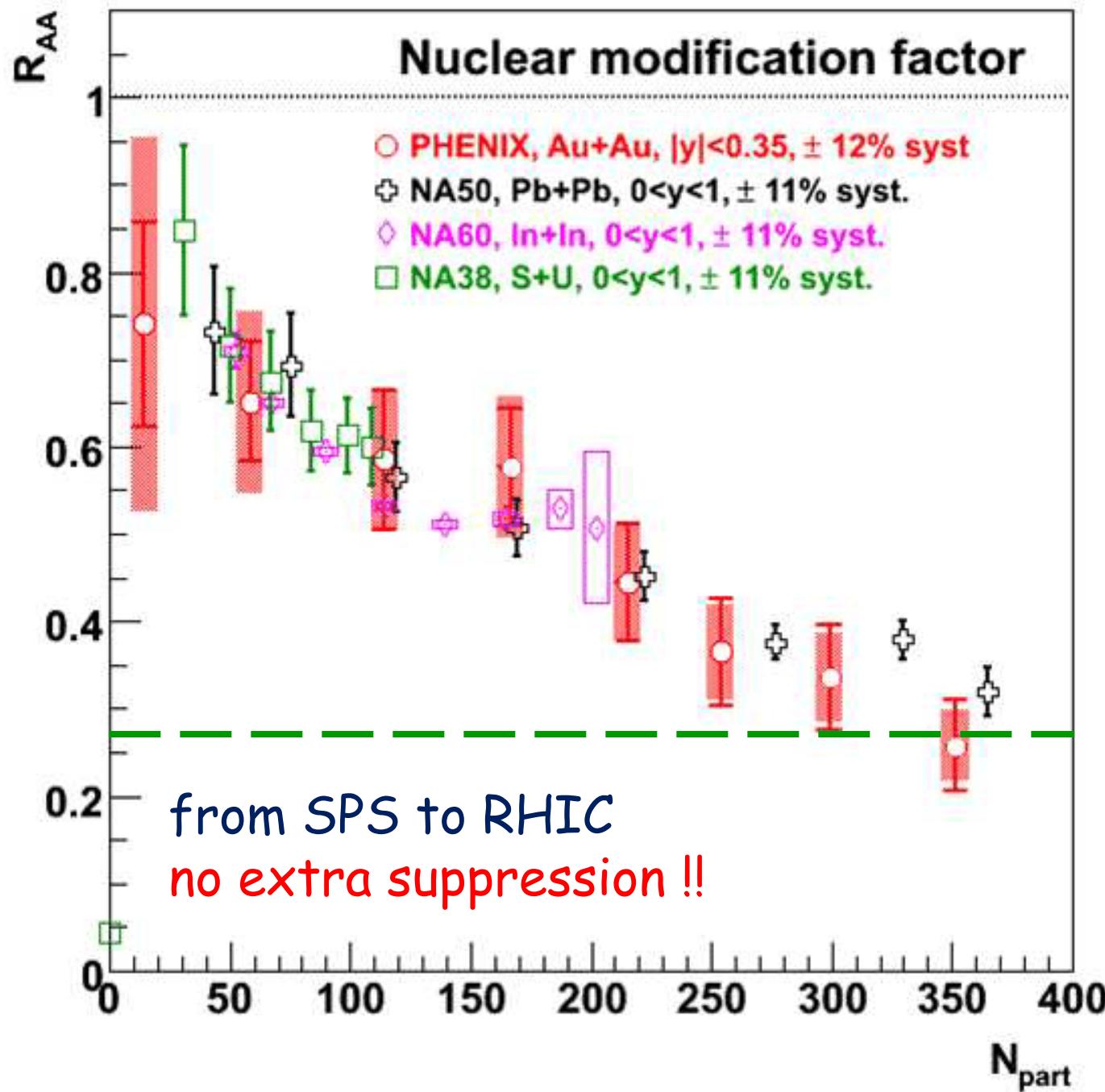
Large number of charm quarks

Quarks from different parent gluons form bound states

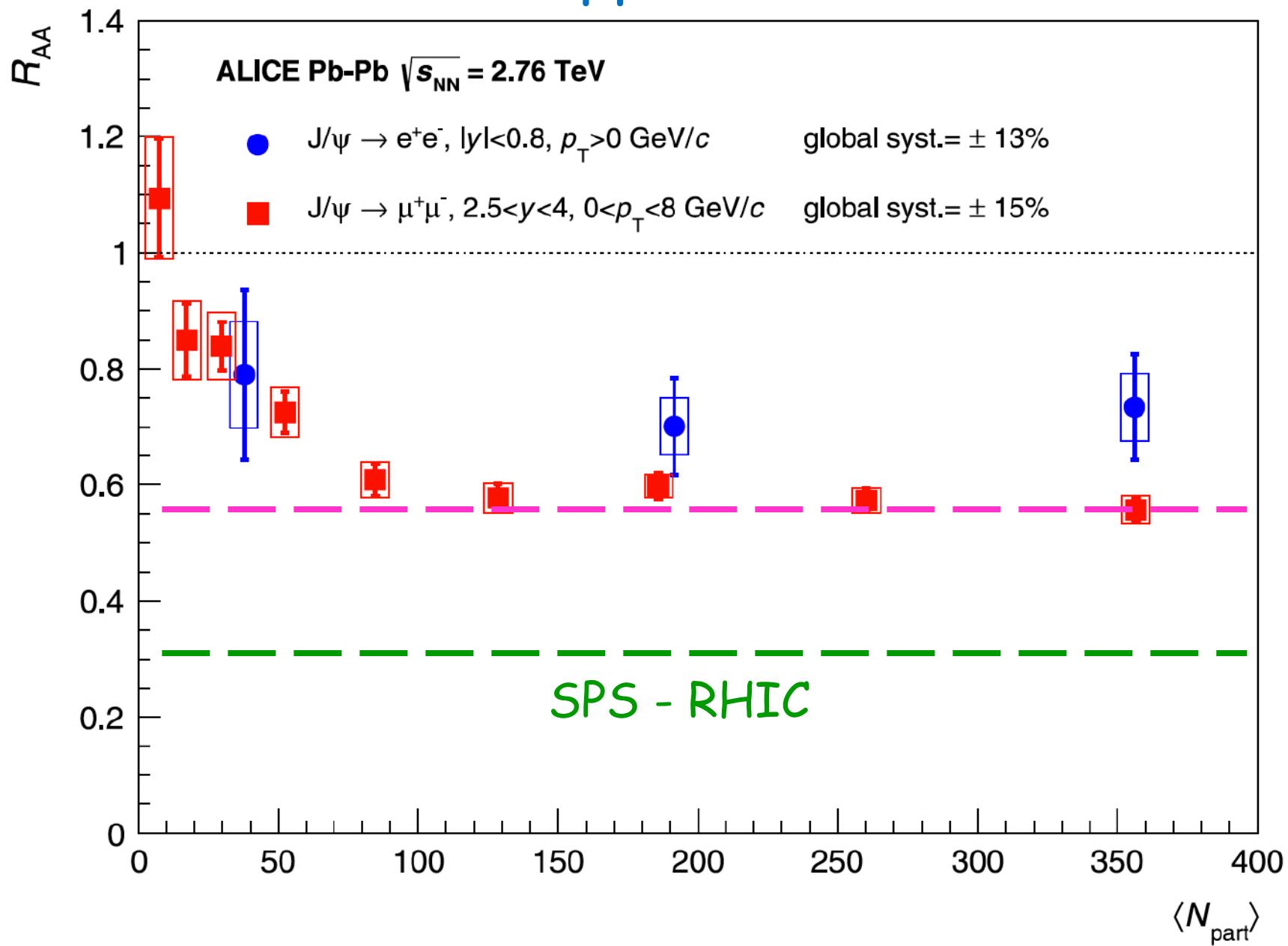
Recombination  $\rightarrow$  ENHANCEMENT

# Recombination in the QGP

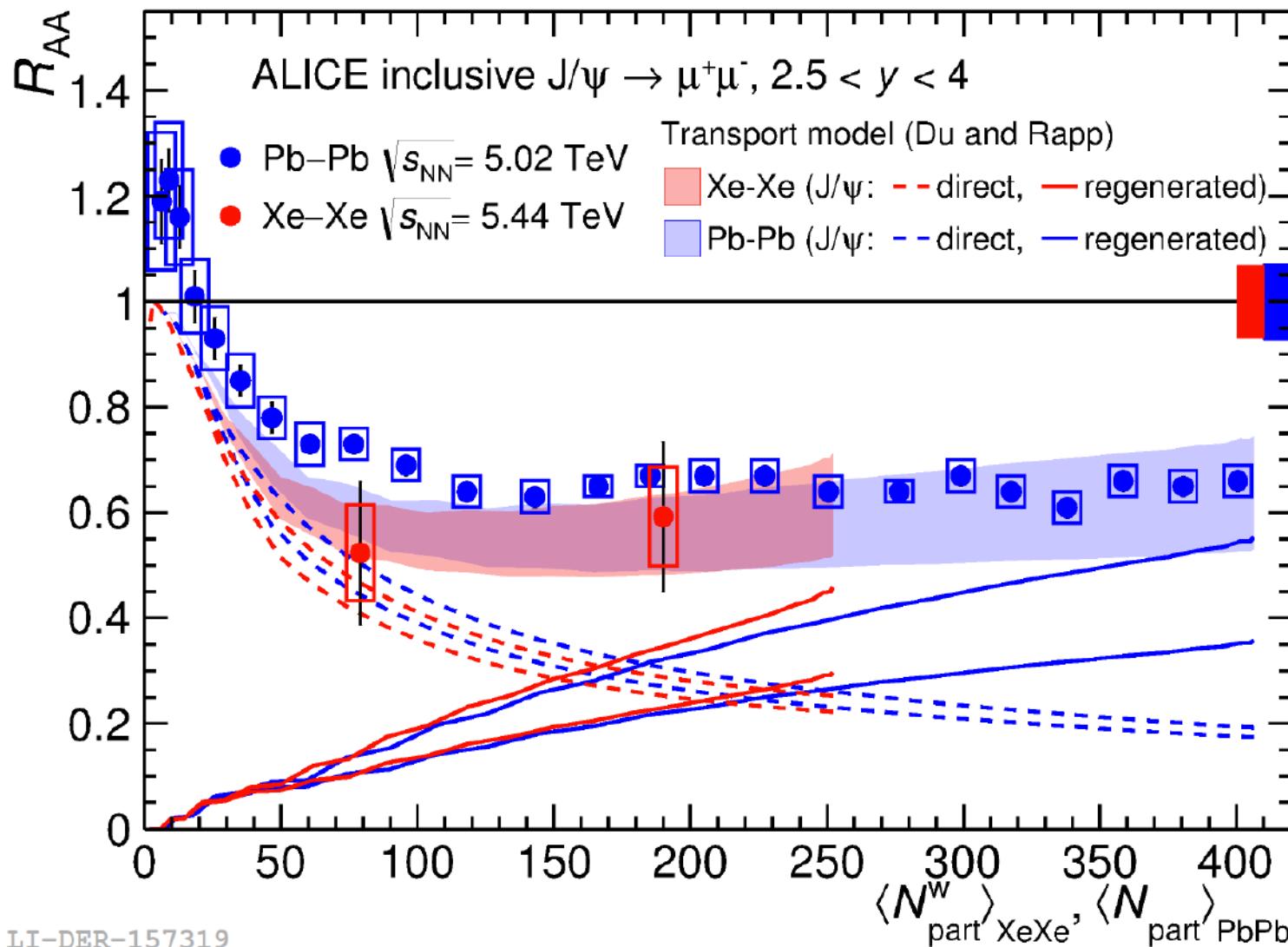




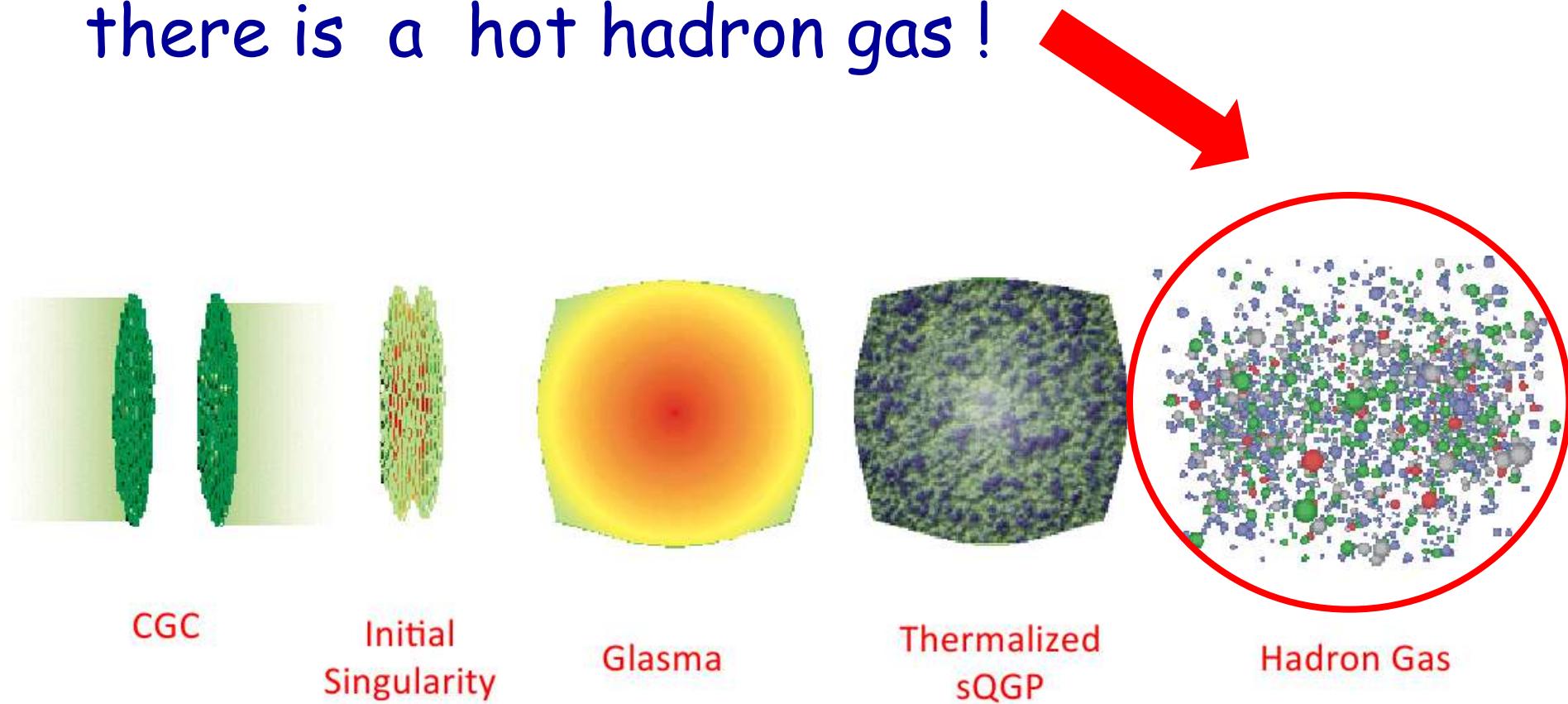
# "Unsuppression"



# "Unsuppression" is robust !

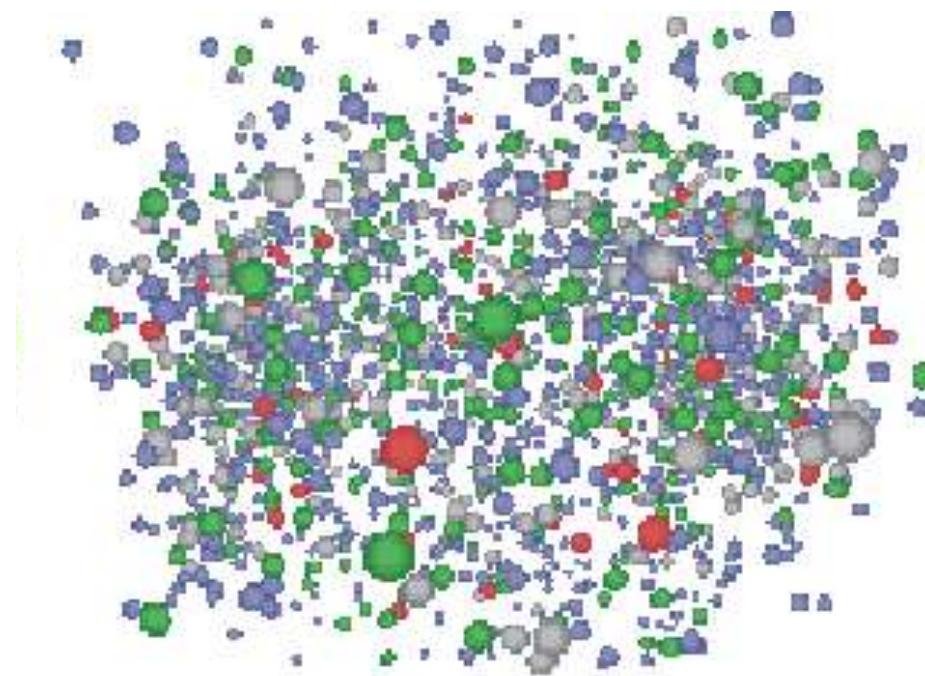


In heavy ion collisions  
there is a hot hadron gas !



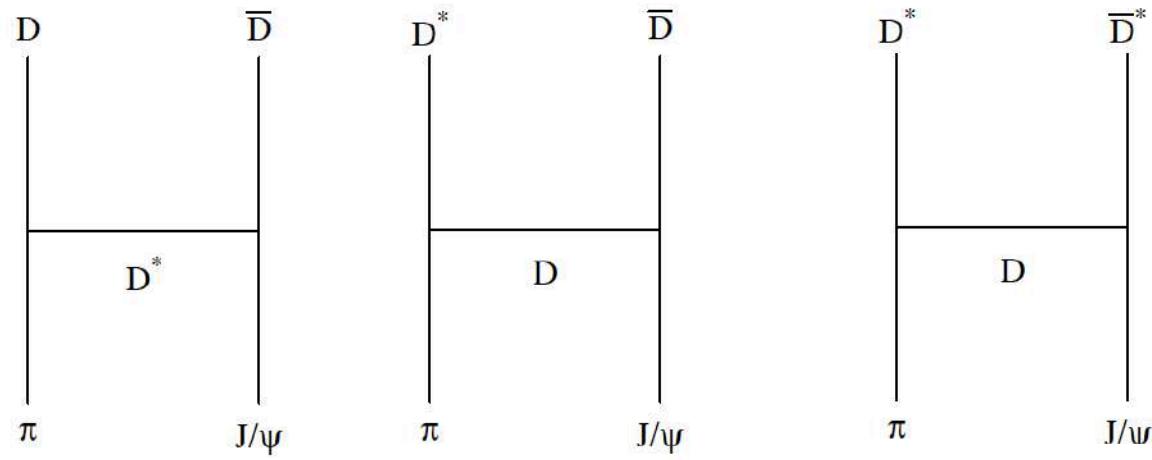
# Charmonium suppression in the HG

Abreu et al., arxiv:1712.06019



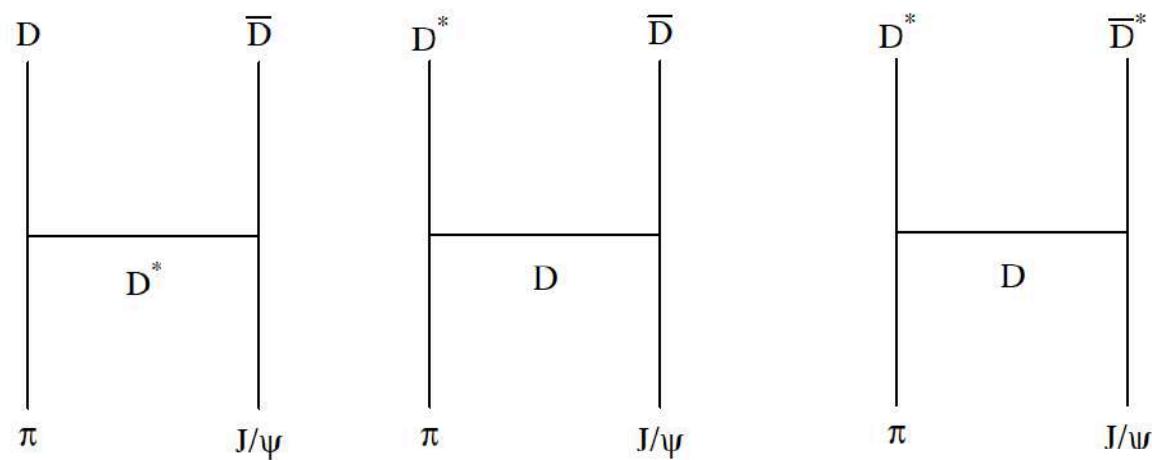
Hadron Gas

# Meson Exchange Model

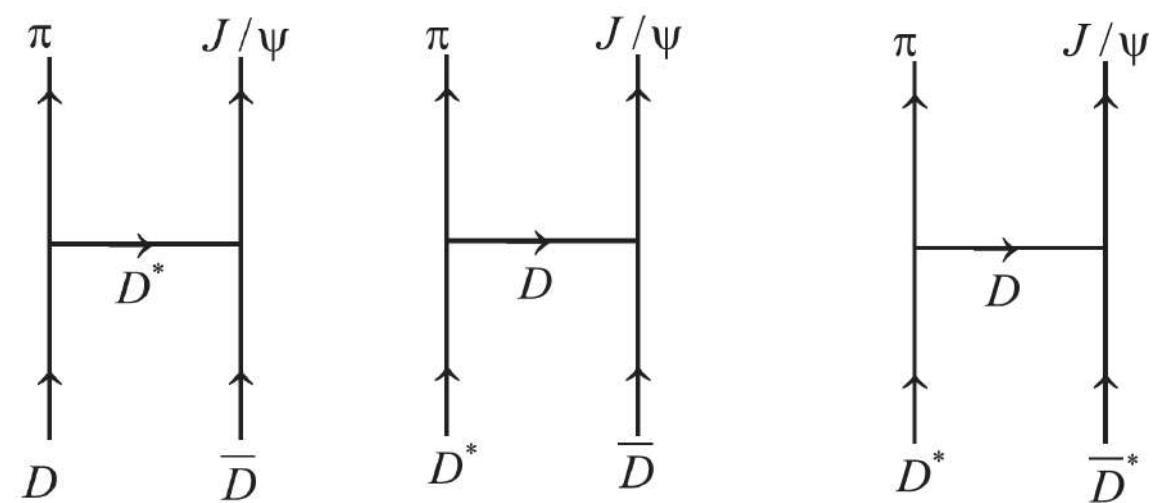


S.G. Matinyan and B. Muller,  
PRC (1998)

# Meson Exchange Model



S.G. Matinyan and B. Muller,  
PRC (1998)



Inverse processes  
can also happen

Charmonium can  
be produced !!!

F. Carvalho, F.O. Duraes, FSN and M. Nielsen, PRC (2005)

# SU(4) Effective Lagrangians

$$\begin{aligned}
 \mathcal{L}_{PPV} &= -ig_{PPV} \langle V^\mu [P, \partial_\mu P] \rangle, \\
 \mathcal{L}_{VVV} &= ig_{VVV} \langle \partial_\mu V_\nu [V^\mu, V^\nu] \rangle, \\
 \mathcal{L}_{PPVV} &= g_{PPVV} \langle PV^\mu [V_\mu, P] \rangle, \\
 \mathcal{L}_{VVVV} &= g_{VVVV} \langle V^\mu V^\nu [V_\mu, V_\nu] \rangle,
 \end{aligned}$$

$$V_\mu = \begin{pmatrix} \frac{\omega}{\sqrt{2}} + \frac{\rho^0}{\sqrt{2}} & \rho^+ & K^{*+} & \bar{D}^{*0} \\ \rho^- & \frac{\omega}{\sqrt{2}} - \frac{\rho^0}{\sqrt{2}} & K^{*0} & D^{*-} \\ K^{*-} & \bar{K}^{*0} & \phi & D_s^{*-} \\ D^{*0} & D^{*+} & D_s^{*+} & J/\psi \end{pmatrix}_\mu$$

$$P = \begin{pmatrix} \frac{\eta}{\sqrt{3}} + \frac{\eta'}{\sqrt{6}} + \frac{\pi^0}{\sqrt{2}} & \pi^+ & K^+ & \bar{D}^0 \\ \pi^- & \frac{\eta}{\sqrt{3}} + \frac{\eta'}{\sqrt{6}} - \frac{\pi^0}{\sqrt{2}} & K^0 & D^- \\ K^- & \bar{K}^0 & -\frac{\eta}{\sqrt{3}} + \sqrt{\frac{2}{3}}\eta' & D_s^- \\ D^0 & D^+ & D_s^+ & \eta_c \end{pmatrix}$$

# Anomalous Parity Terms

$$\begin{aligned}\mathcal{L}_{PVV} &= -g_{PVV} \varepsilon^{\mu\nu\alpha\beta} \langle \partial_\mu V_\nu \partial_\alpha V_\beta P \rangle, \\ \mathcal{L}_{PPPV} &= -ig_{PPPV} \varepsilon^{\mu\nu\alpha\beta} \langle V_\mu (\partial_\nu P) (\partial_\alpha P) (\partial_\beta P) \rangle, \\ \mathcal{L}_{PVVV} &= ig_{PVVV} \varepsilon^{\mu\nu\alpha\beta} [\langle V_\mu V_\nu V_\alpha \partial_\beta P \rangle \\ &\quad + \frac{1}{3} \langle V_\mu (\partial_\nu V_\alpha) V_\beta P \rangle] .\end{aligned}$$

Oh, Song, Lee, PRC (2001)

amplitudes

$$\left\{ \begin{array}{l} \mathcal{M}_1^{(\varphi)} = \sum_i \mathcal{M}_{1i}^{(\varphi)\mu} \epsilon_\mu(p_2), \quad \varphi = \pi, \rho, K, K^* \\ \mathcal{M}_2^{(\varphi)} = \sum_i \mathcal{M}_{2i}^{(\varphi)\mu\nu\lambda} \epsilon_\mu(p_2) \epsilon_\nu^*(p_3) \epsilon_\lambda^*(p_4), \\ \mathcal{M}_3^{(\varphi)} = \sum_i \mathcal{M}_{3i}^{(\varphi)\mu\nu} \epsilon_\mu(p_2) \epsilon_\nu^*(p_3), \\ \mathcal{M}_4^{(\varphi)} = \sum_i \mathcal{M}_{4i}^{(\varphi)\mu\nu} \epsilon_\mu(p_2) \epsilon_\nu^*(p_4). \end{array} \right.$$

amplitudes

$$\left\{ \begin{array}{l} \mathcal{M}_1^{(\varphi)} = \sum_i \mathcal{M}_{1i}^{(\varphi)\mu} \epsilon_\mu(p_2), \quad \varphi = \pi, \rho, K, K^* \\ \mathcal{M}_2^{(\varphi)} = \sum_i \mathcal{M}_{2i}^{(\varphi)\mu\nu\lambda} \epsilon_\mu(p_2) \epsilon_\nu^*(p_3) \epsilon_\lambda^*(p_4), \\ \mathcal{M}_3^{(\varphi)} = \sum_i \mathcal{M}_{3i}^{(\varphi)\mu\nu} \epsilon_\mu(p_2) \epsilon_\nu^*(p_3), \\ \mathcal{M}_4^{(\varphi)} = \sum_i \mathcal{M}_{4i}^{(\varphi)\mu\nu} \epsilon_\mu(p_2) \epsilon_\nu^*(p_4). \end{array} \right.$$

averaged  
amplitudes

$$\left\{ \sum_{S,I} |\mathcal{M}_r|^2 = \frac{1}{g_1 g_2} \sum_{S,I} |\mathcal{M}_r|^2 \right.$$

spin, isospin

$$g_1 = (2I_{1i,r} + 1)(2S_{1i,r} + 1), g_2 = (2I_{2i,r} + 1)(2S_{2i,r} + 1)$$

amplitudes

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cross  
sections

$$\sigma_r^{(\varphi)}(s) = \frac{1}{64\pi^2 s} \frac{|\vec{p}_f|}{|\vec{p}_i|} \int d\Omega \overline{\sum_{S,I}} |\mathcal{M}_r^{(\varphi)}(s, \theta)|^2$$

## Form factors

Account for higher order corrections and for  
the spatial structure of hadronic vertices

$$F_3 = \frac{\Lambda^2}{\Lambda^2 + \mathbf{q}^2}; \quad F_4 = \frac{\Lambda^2}{\Lambda^2 + \bar{\mathbf{q}}^2} \frac{\Lambda^2}{\Lambda^2 + \bar{\mathbf{q}}^2},$$

$$\mathbf{q} = (\mathbf{p}_1 - \mathbf{p}_3)^2$$

$$\bar{\mathbf{q}} = [(\mathbf{p}_1 - \mathbf{p}_3)^2 + (\mathbf{p}_2 - \mathbf{p}_3)^2]/2.$$

Can be calculated with QCD sum rules

Bracco, Chiapparini, FSN, Nielsen, PPNP (2012)

# Coupling constants

Directly from experiment:  $D^* \rightarrow D \pi$   $g_{D^* D \pi}$

Experiment + VDM:  $D^* \rightarrow D \gamma$   $g_{D^* D \gamma}$

Heavy quark symmetry:  $g_{D^* D^* \pi} \simeq g_{D^* D \pi}$

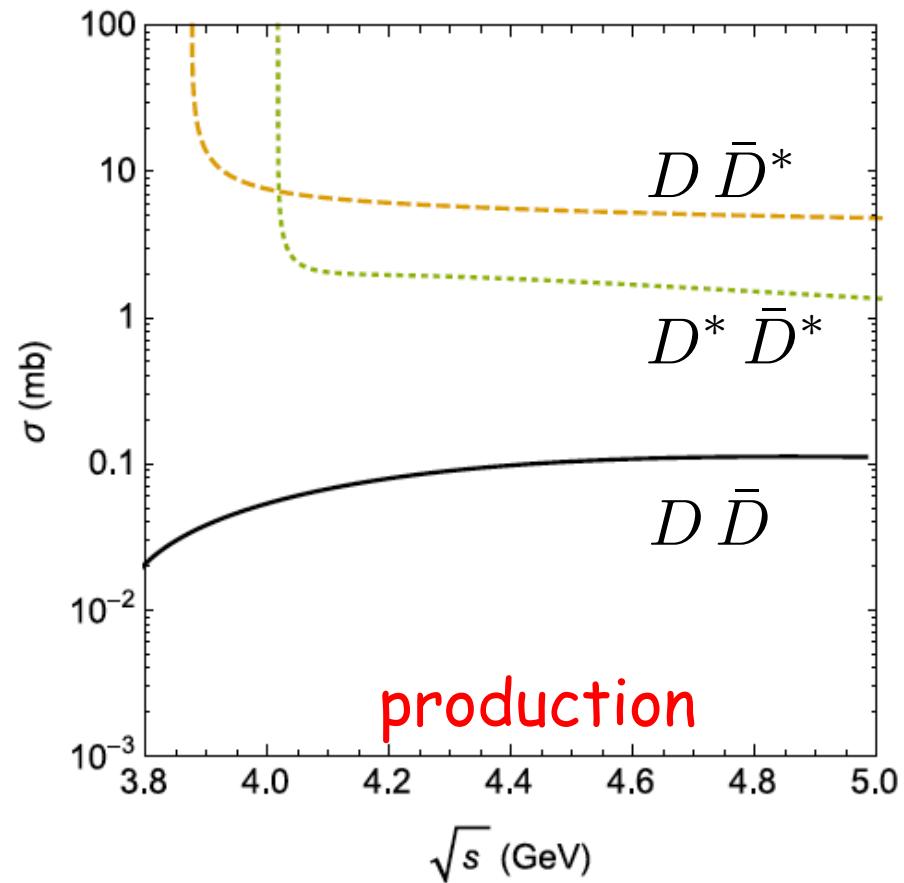
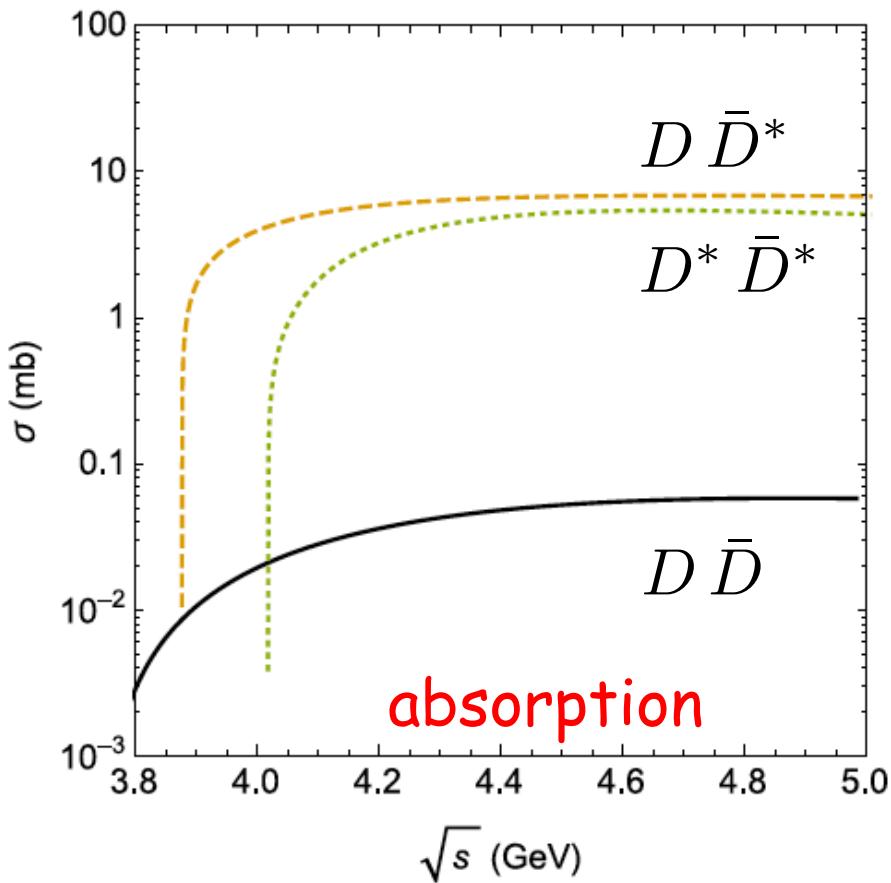
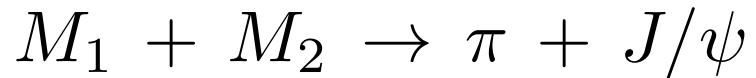
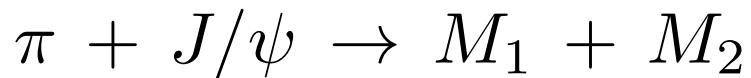
SU(4) relations

Can be calculated with QCD sum rules

Bracco, Chiapparini, FSN, Nielsen, PPNP (2012)

SU(4) relations are violated by  $\sim 30\%$   
(except for the pion :  $\sim 70\%$ )

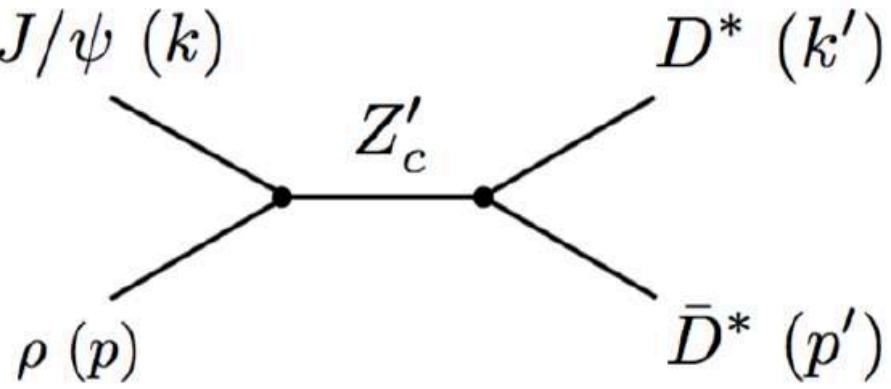
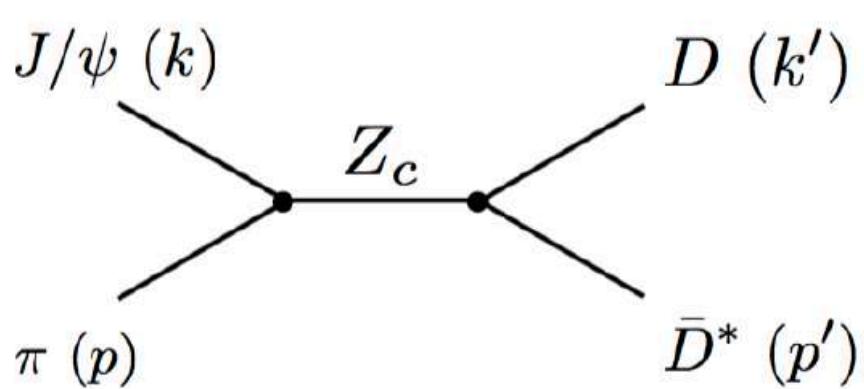
# J/Psi cross sections

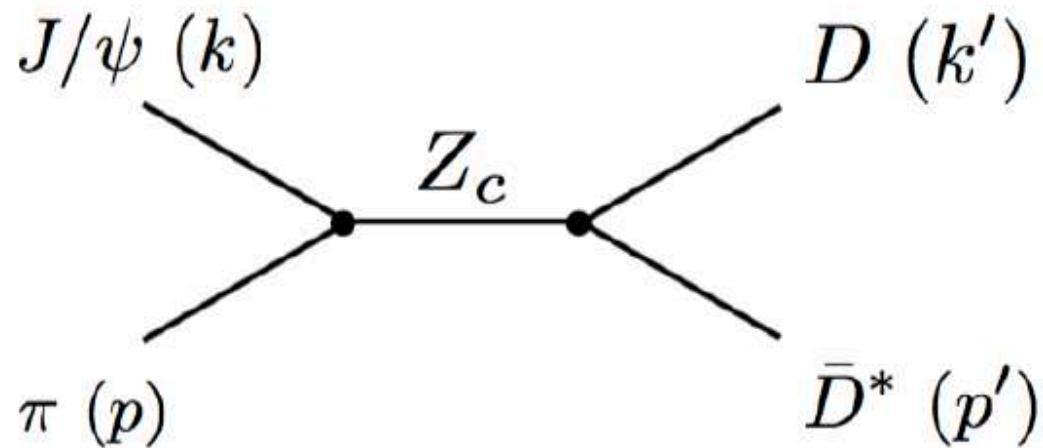


# Impact of exotic charmonium

2003  $X(3872)$  : a multiquark state  $c\bar{c}q\bar{q}$

2013  $Z_c(3900), Z_c(4025)$  : charged state  $c\bar{c}u\bar{d}$

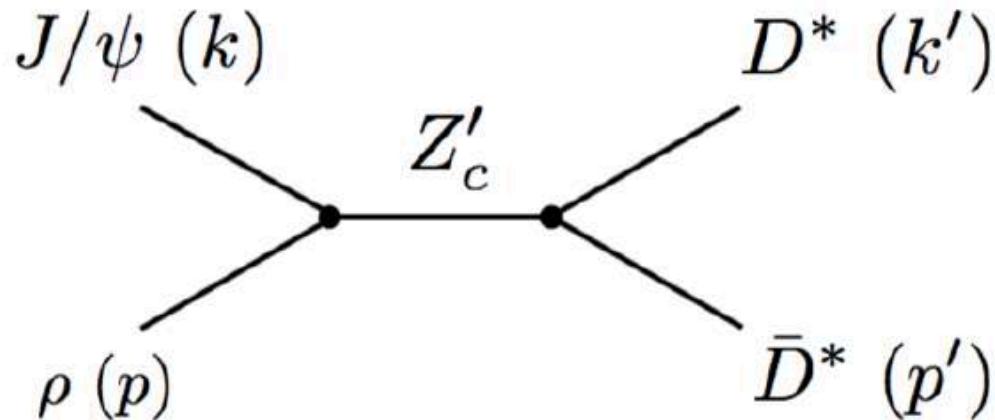




$$\begin{aligned}
 \mathcal{M}_Z &= \alpha_{J/\psi\pi} \alpha_{D\bar{D}^*} \frac{1}{s - M_Z^2 + iM_Z\Gamma_Z} \\
 &\times \left( -g^{\mu\nu} + \frac{p^\mu k'^\nu}{M_Z^2} \right) \epsilon^\mu(k) \epsilon^\nu{}^*(p') ,
 \end{aligned}$$

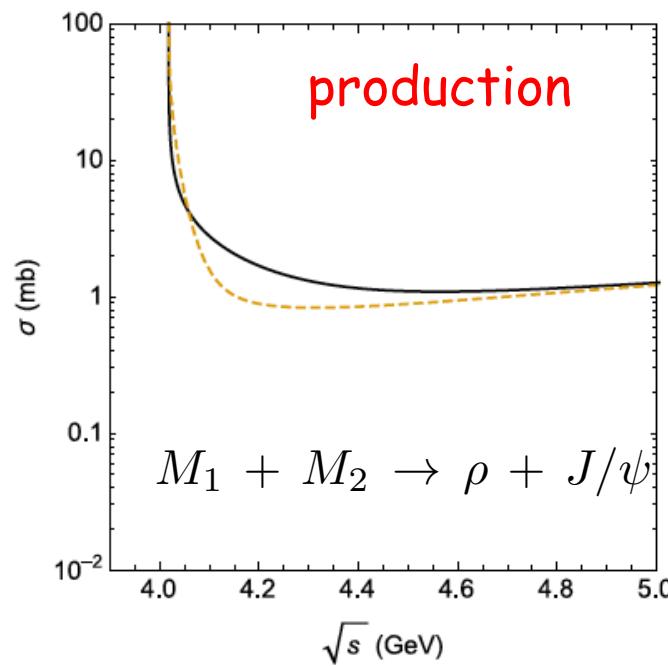
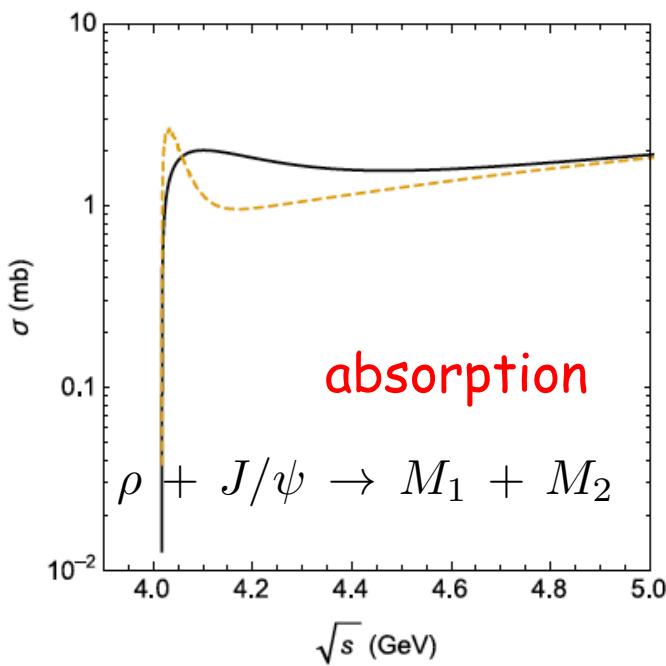
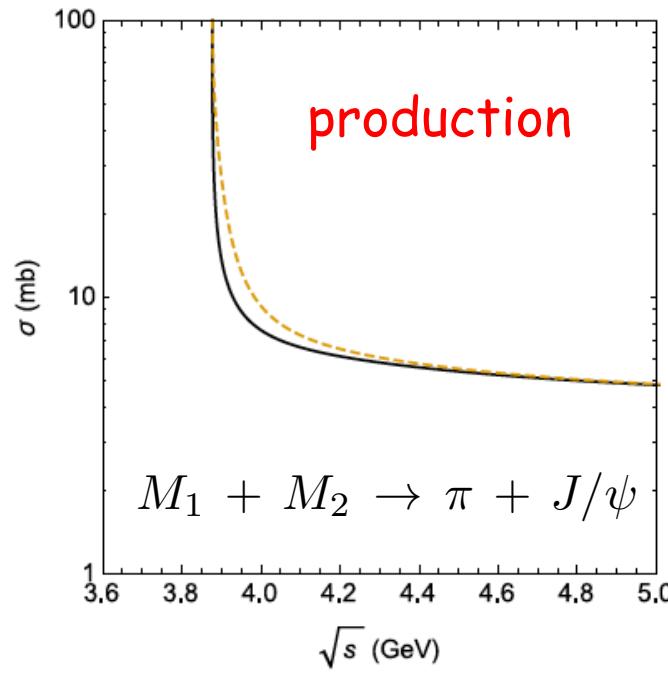
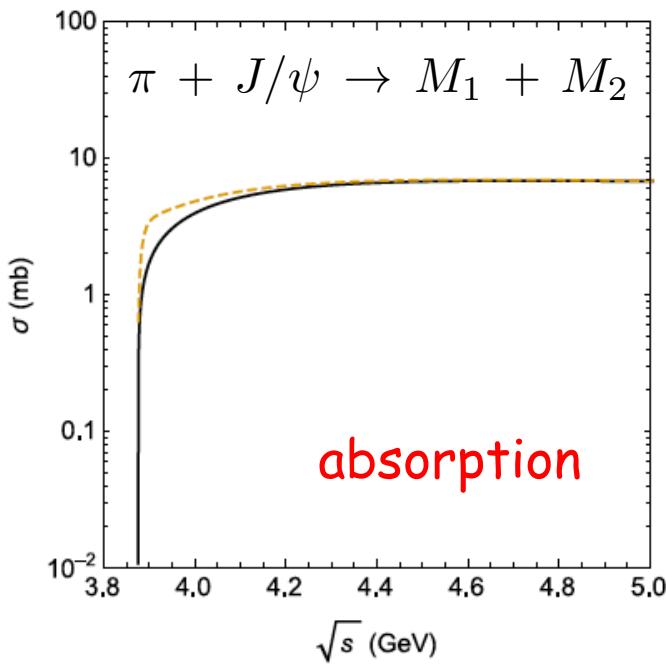
Couplings from experiment

Abreu et al., arxiv:1712.06019



$$\begin{aligned}
 \mathcal{M}_{Z'} = & \eta_{J/\psi\rho} \eta_{D^*\bar{D}^*} \frac{1}{s - M_{Z'}^2 + iM_{Z'}\Gamma_{Z'}} \\
 & \times P^{\mu\nu\alpha\beta}(q) \epsilon_\mu(k) \epsilon_\nu(p) \epsilon_\alpha^*(k') \epsilon_\beta^*(p'),
 \end{aligned}$$

Couplings from experiment  
 Abreu et al., arxiv:1712.06019



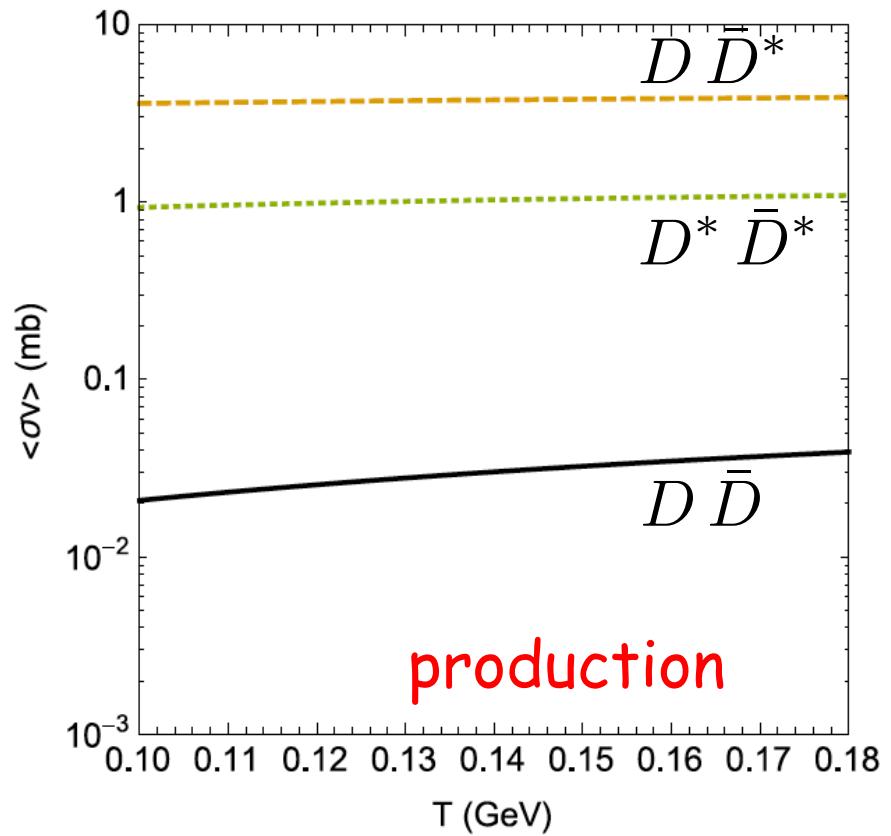
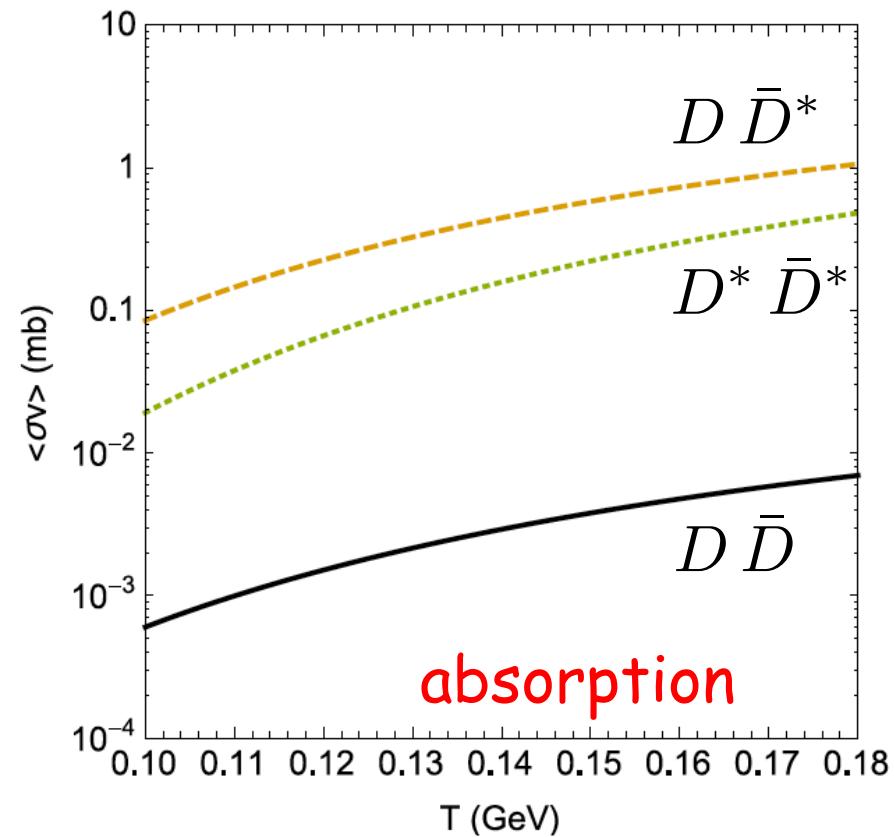
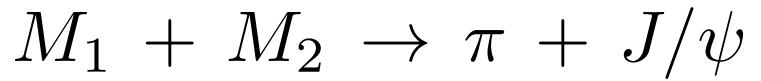
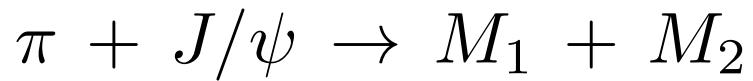
## Averaged thermal cross sections

$$\langle \sigma_{ab} v_{ab} \rangle = \frac{\int d^3 p_a d^3 p_b f_a(p_a) f_b(p_b) \sigma_{ab} v_{ab}}{\int d^3 p_a d^3 p_b f_a(p_a) f_b(p_b)}$$

$f_a(p_a)$  = Bose-Einstein distribution of meson a

$\sigma_{ab}$  = cross section of meson a + meson b

$v_{ab}$  = relative velocity of meson a and meson b



# Time evolution of charmonium multiplicity

Solve the rate equation including gain and loss terms:

gain

loss

$$\begin{aligned}
 \frac{dN_{J/\psi}(\tau)}{d\tau} = & \sum_{\varphi=\pi,\rho K,K^*} \left[ \langle \sigma_{D_{(s)}\bar{D} \rightarrow \varphi J/\psi} v_{D_{(s)}\bar{D}} \rangle n_{D_{(s)}}(\tau) N_{\bar{D}}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow D_{(s)}\bar{D}} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \right. \\
 & + \langle \sigma_{D_{(s)}^*\bar{D}^* \rightarrow \varphi J/\psi} v_{D_{(s)}^*\bar{D}^*} \rangle n_{D_{(s)}^*}(\tau) N_{\bar{D}^*}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow D_{(s)}^*\bar{D}^*} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \\
 & + \langle \sigma_{D_{(s)}^*\bar{D} \rightarrow \varphi J/\psi} v_{D_{(s)}^*\bar{D}} \rangle n_{D_{(s)}^*}(\tau) N_{\bar{D}}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow D_{(s)}^*\bar{D}} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \\
 & \left. + \langle \sigma_{D_{(s)}\bar{D}^* \rightarrow \varphi J/\psi} v_{D_{(s)}\bar{D}^*} \rangle n_{D_{(s)}}(\tau) N_{\bar{D}^*}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow D_{(s)}\bar{D}^*} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \right] \\
 & + \sum_{\varphi=\bar{\pi},\bar{\rho},\bar{K},\bar{K}^*} \left[ \langle \sigma_{\bar{D}_{(s)}D \rightarrow \varphi J/\psi} v_{\bar{D}_{(s)}D} \rangle n_{\bar{D}_{(s)}}(\tau) N_D(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow \bar{D}_{(s)}D} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \right. \\
 & + \langle \sigma_{\bar{D}_{(s)}^*D^* \rightarrow \varphi J/\psi} v_{\bar{D}_{(s)}^*D^*} \rangle n_{\bar{D}_{(s)}^*}(\tau) N_{D^*}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow \bar{D}_{(s)}^*D^*} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \\
 & + \langle \sigma_{\bar{D}_{(s)}D \rightarrow \varphi J/\psi} v_{\bar{D}_{(s)}D} \rangle n_{\bar{D}_{(s)}}(\tau) N_D(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow \bar{D}_{(s)}D} v_{\varphi J/\psi} \rangle n_{\varphi}(\tau) N_{J/\psi}(\tau) \\
 & \left. + \langle \sigma_{\bar{D}_{(s)}^*D^* \rightarrow \varphi J/\psi} v_{\bar{D}_{(s)}^*D^*} \rangle n_{\bar{D}_{(s)}^*}(\tau) N_{D^*}(\tau) - \langle \sigma_{\varphi J/\psi \rightarrow \bar{D}_{(s)}^*D^*} v_{\varphi J/\psi} \rangle \right],
 \end{aligned}$$

# Model of the fireball evolution

Cho et al ExHIC Collaboration, PPNP (2017)

$$n_i(\tau) \approx \frac{1}{2\pi^2} \gamma_i g_i m_i^2 T(\tau) K_2 \left( \frac{m_i}{T(\tau)} \right)$$

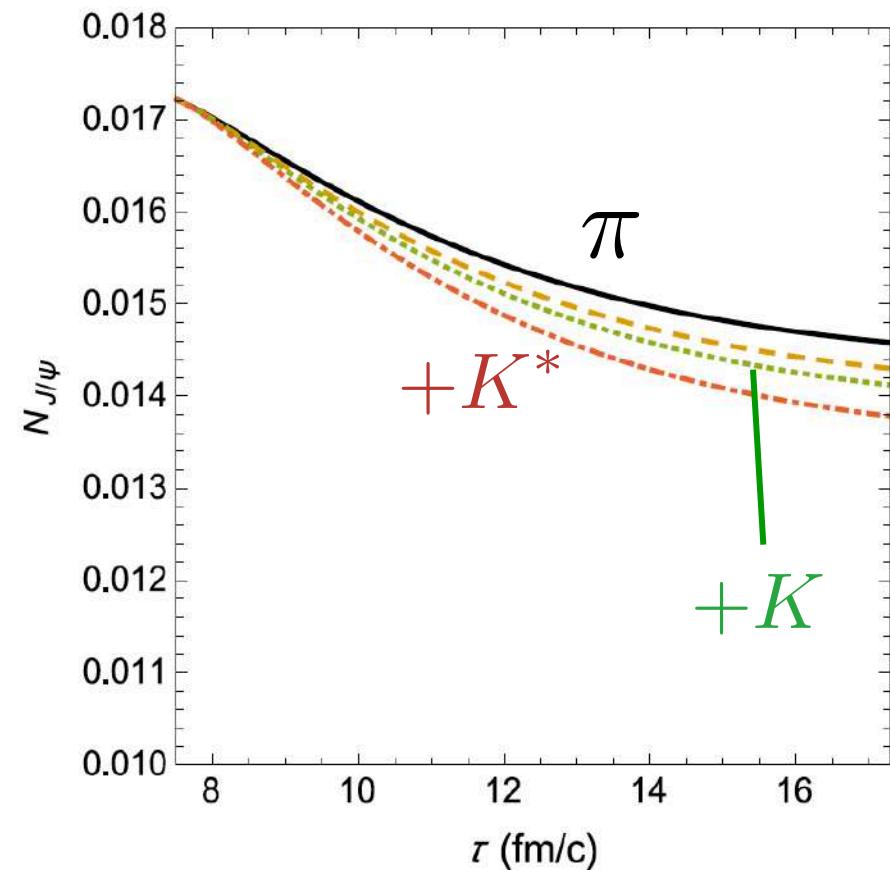
$$T(\tau) = T_C - (T_H - T_F) \left( \frac{\tau - \tau_H}{\tau_F - \tau_H} \right)^{\frac{4}{5}},$$

$$V(\tau) = \pi \left[ R_C + v_C (\tau - \tau_C) + \frac{a_C}{2} (\tau - \tau_C)^2 \right]^2 \tau_C$$

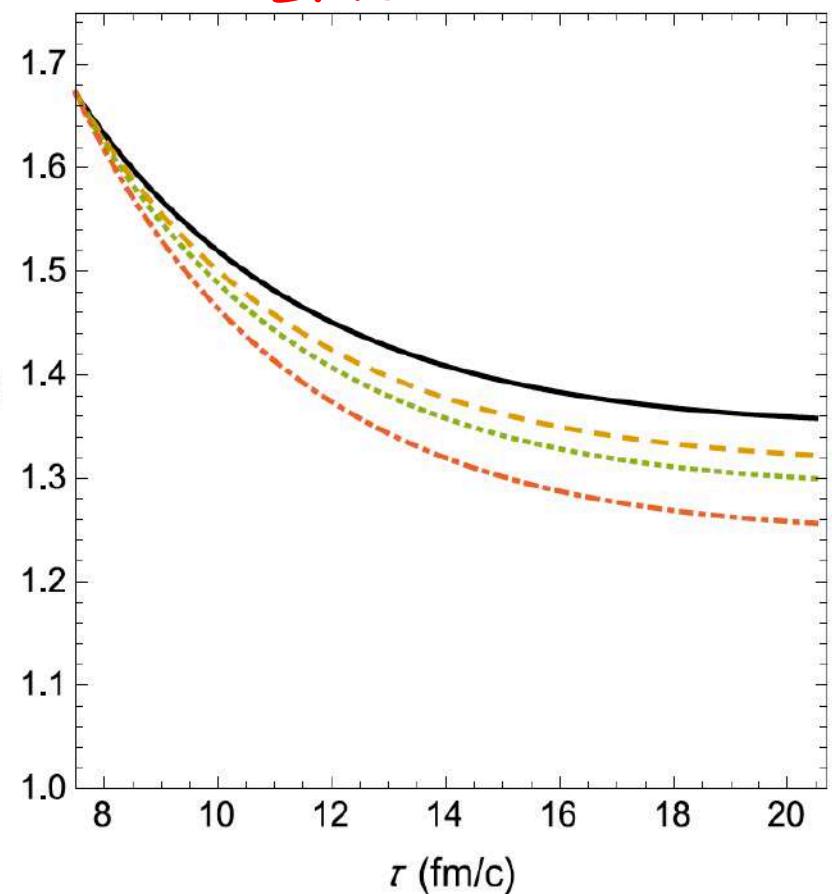
	$\sqrt{s_{NN}}$ (TeV)	$v_C$ (c)	$a_C$ ( $c^2/fm$ )	$R_C$ (fm)	$\tau_C$ (fm/c)	$\tau_H$ (fm/c)	$\tau_F$ (fm/c)	$\gamma_c$	$N_{J/\psi}$
RHIC	0.2	0.4	0.02	8	5	7.5	17.3	6.4	0.017
LHC	5	0.6	0.044	13.11	5	7.5	20.7	15.8	1.67

20-24 % reduction of the number of Psi's

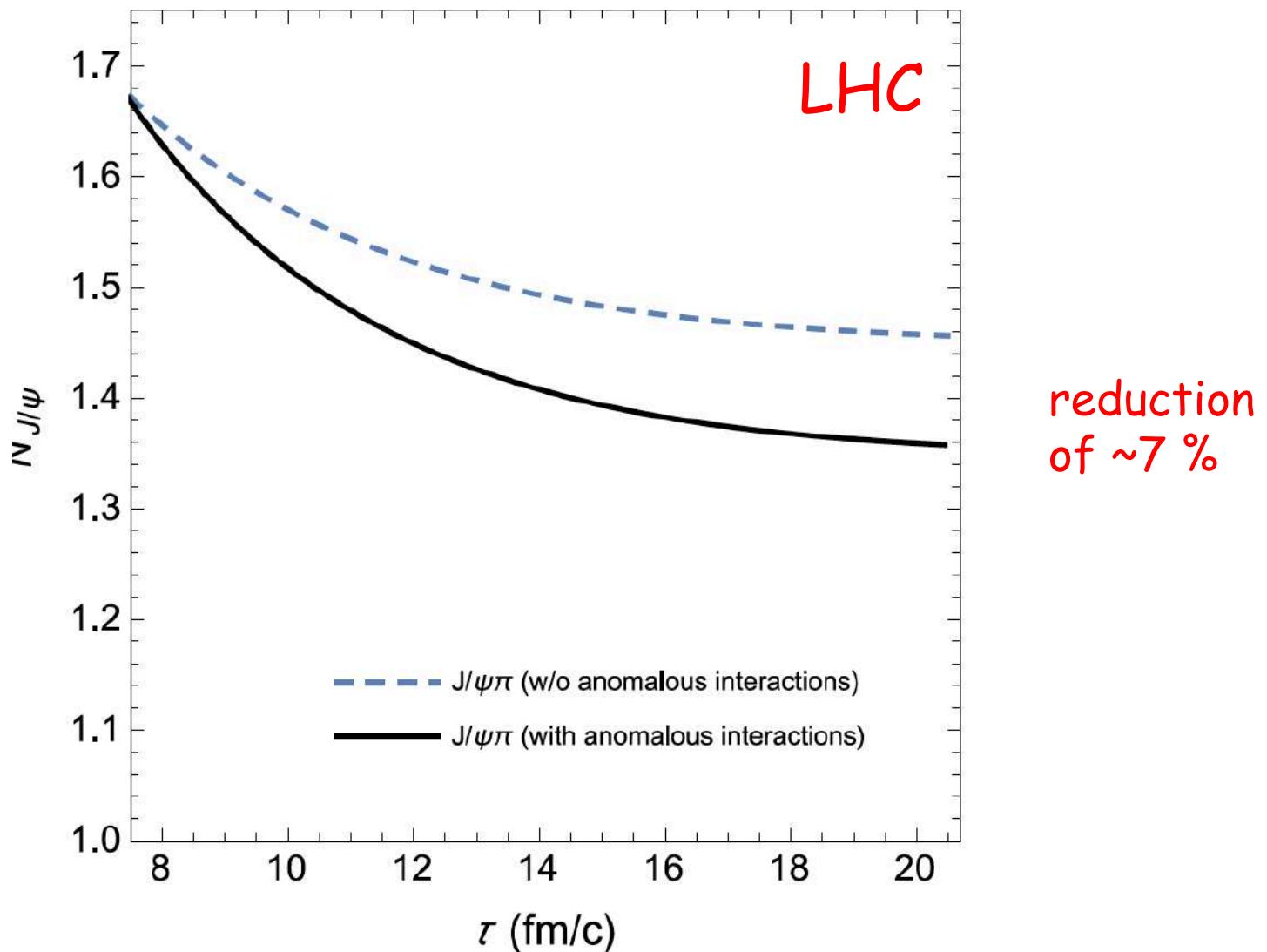
RHIC



LHC



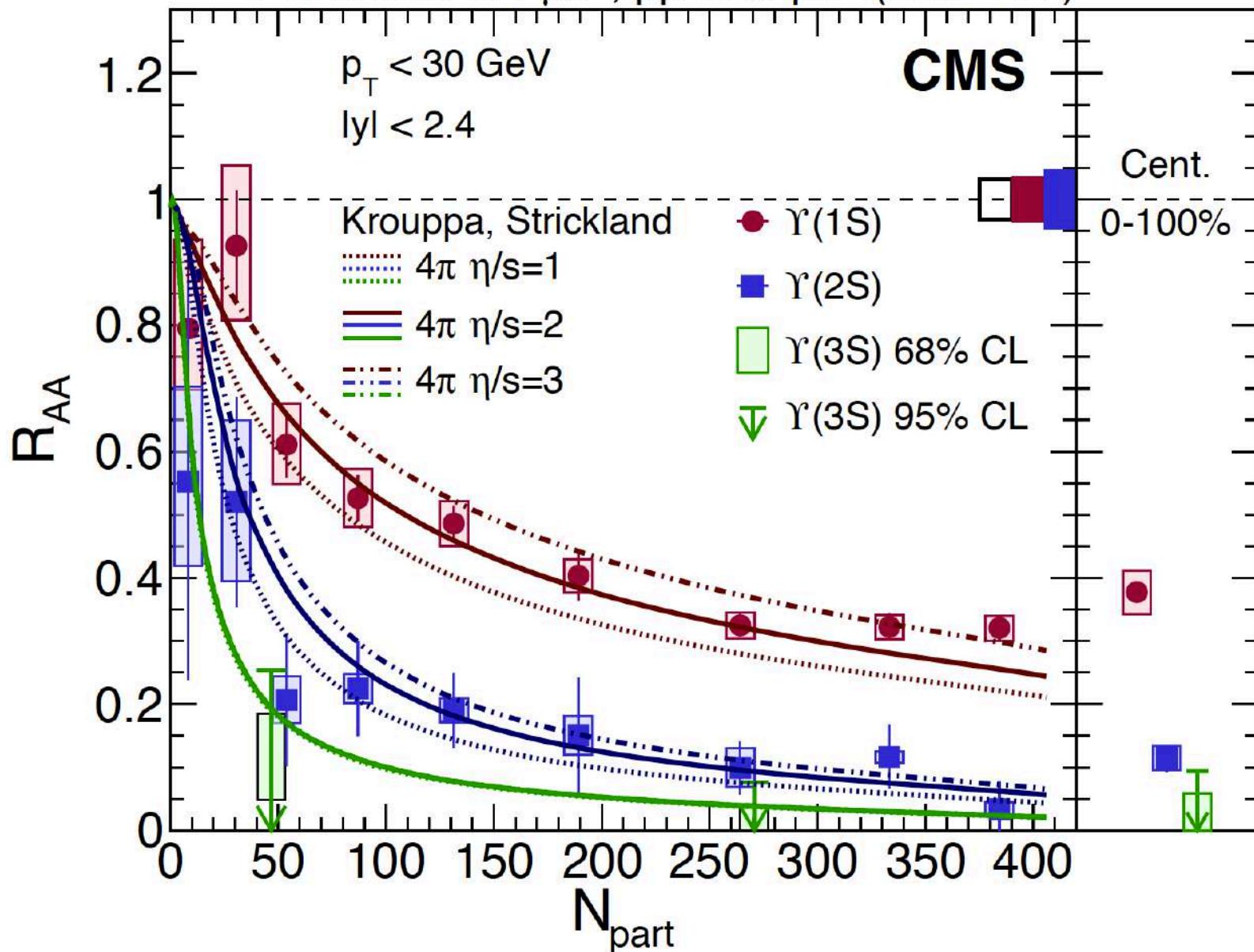
# Role of anomalous interactions



# Bottomonium

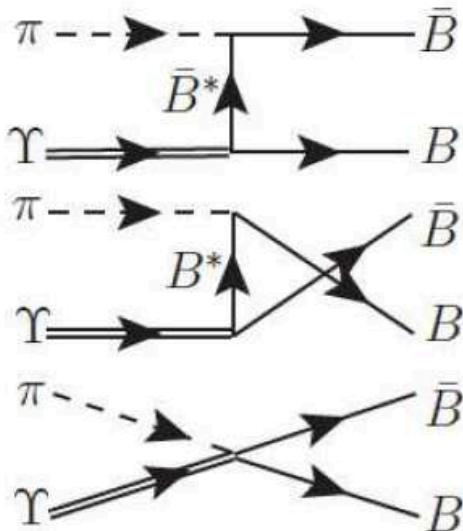
Abreu, FSN, Nielsen, arxiv:1807.05081

PbPb  $368/464 \mu\text{b}^{-1}$ , pp  $28.0 \text{ pb}^{-1}$  (5.02 TeV)

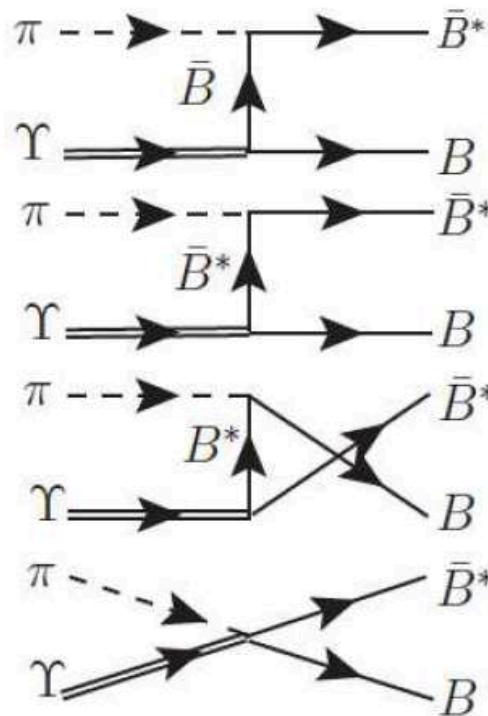


# Bottomonium in a hadron gas

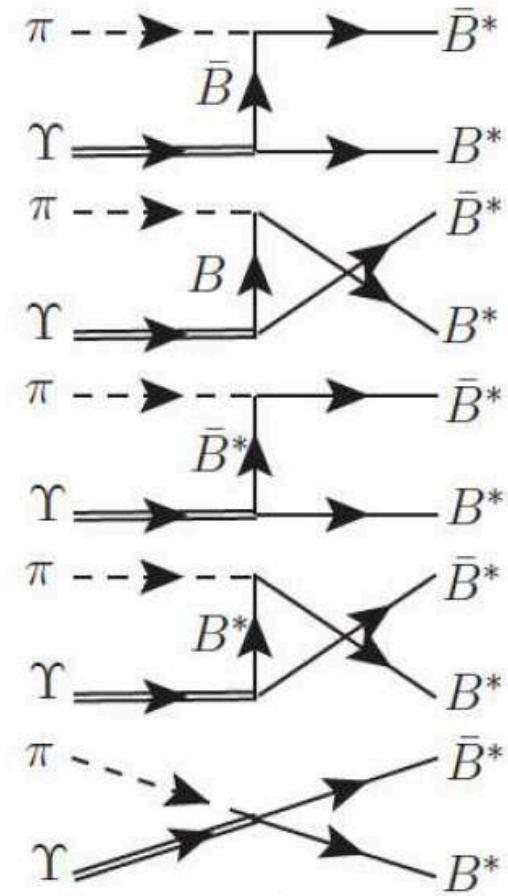
Lin,Ko, PLB (2001) : meson exchange model in SU(5)



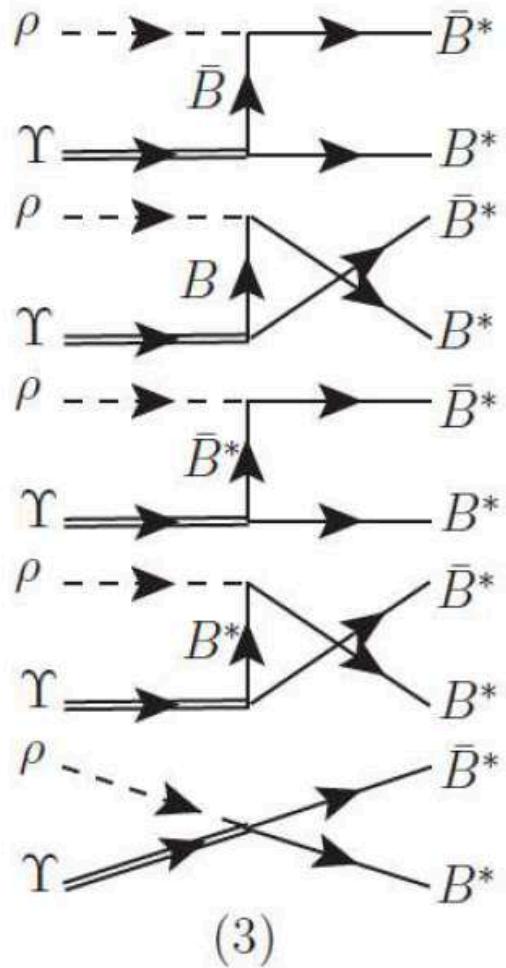
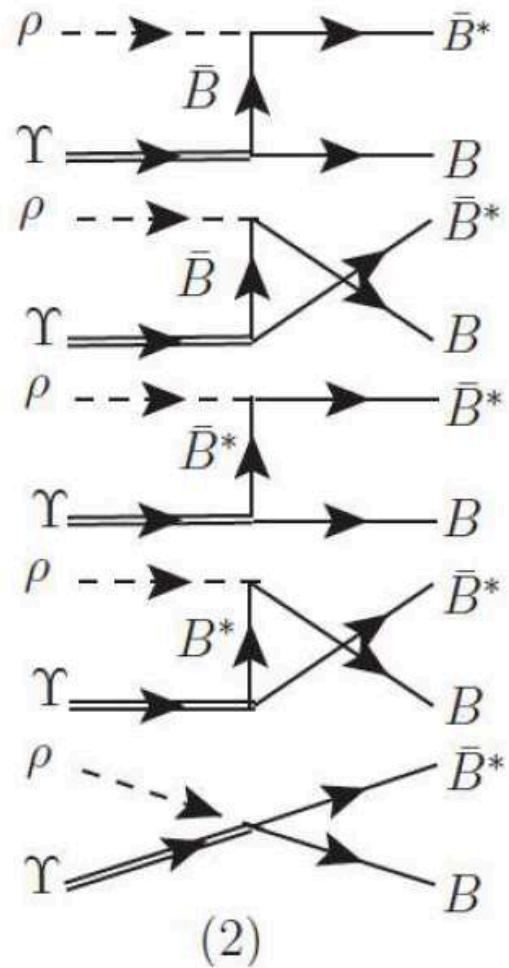
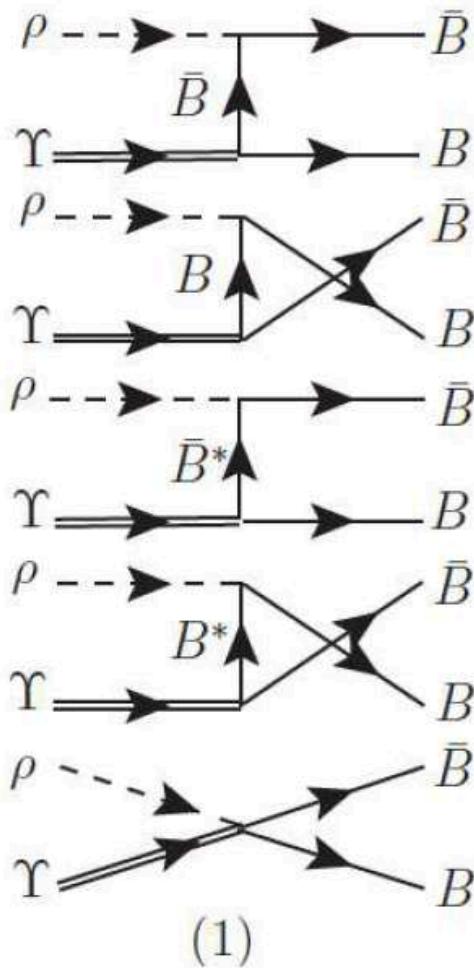
(1)



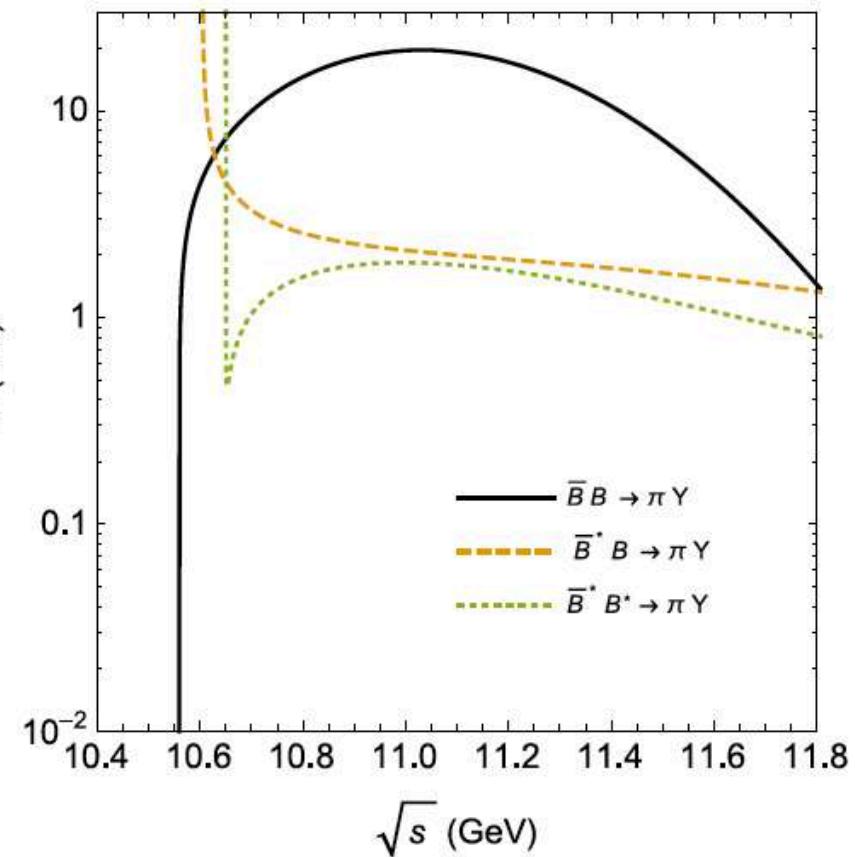
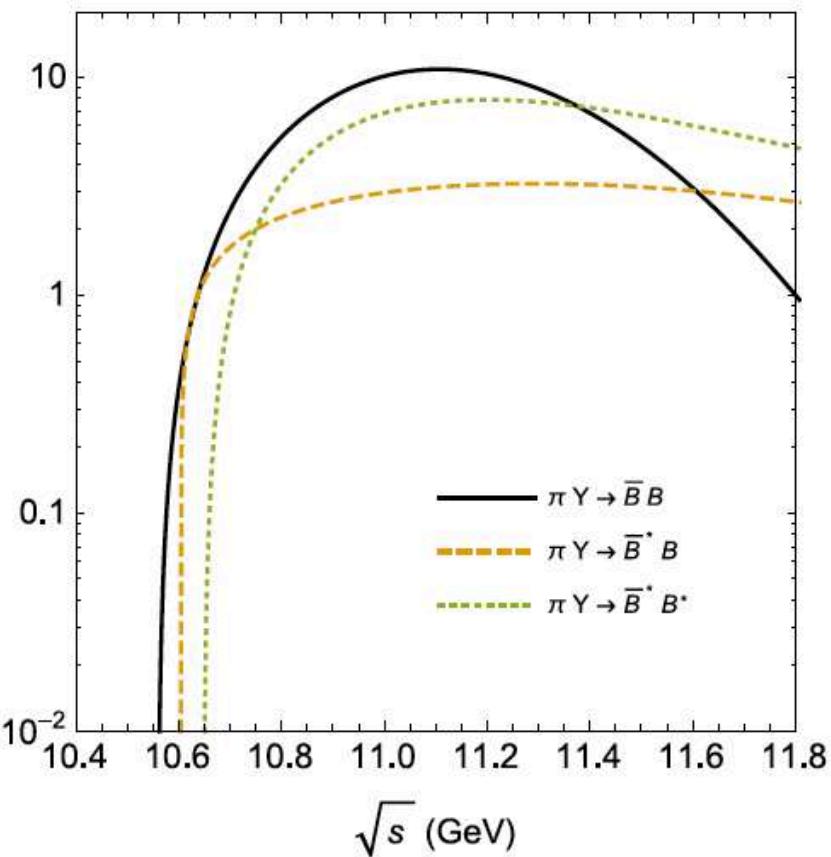
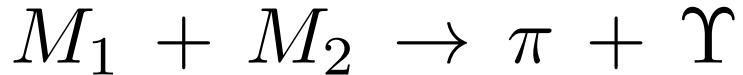
(2)



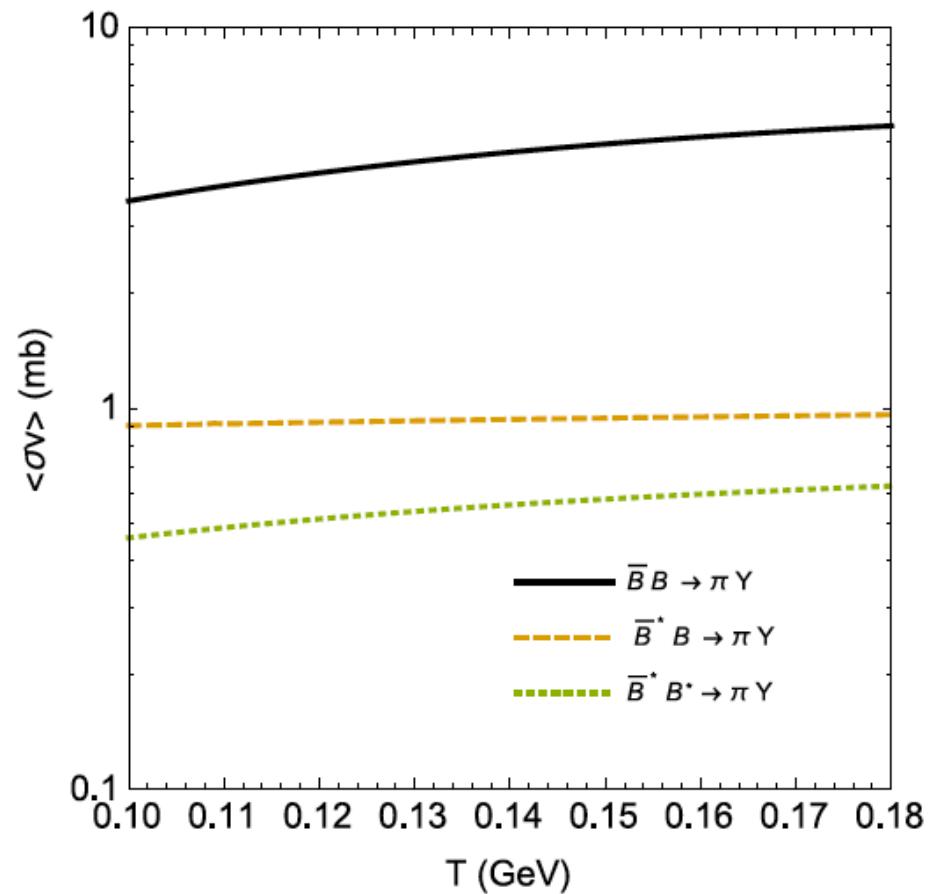
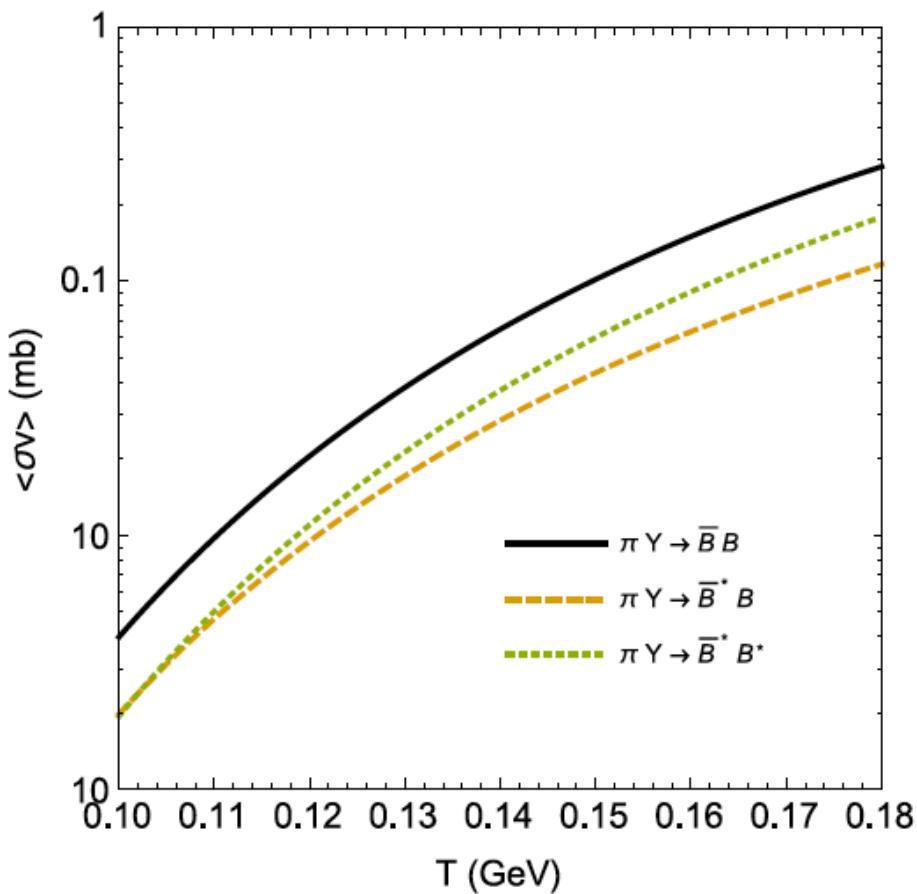
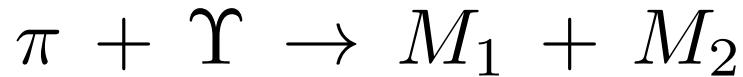
(3)



# Upsilon - pion cross sections

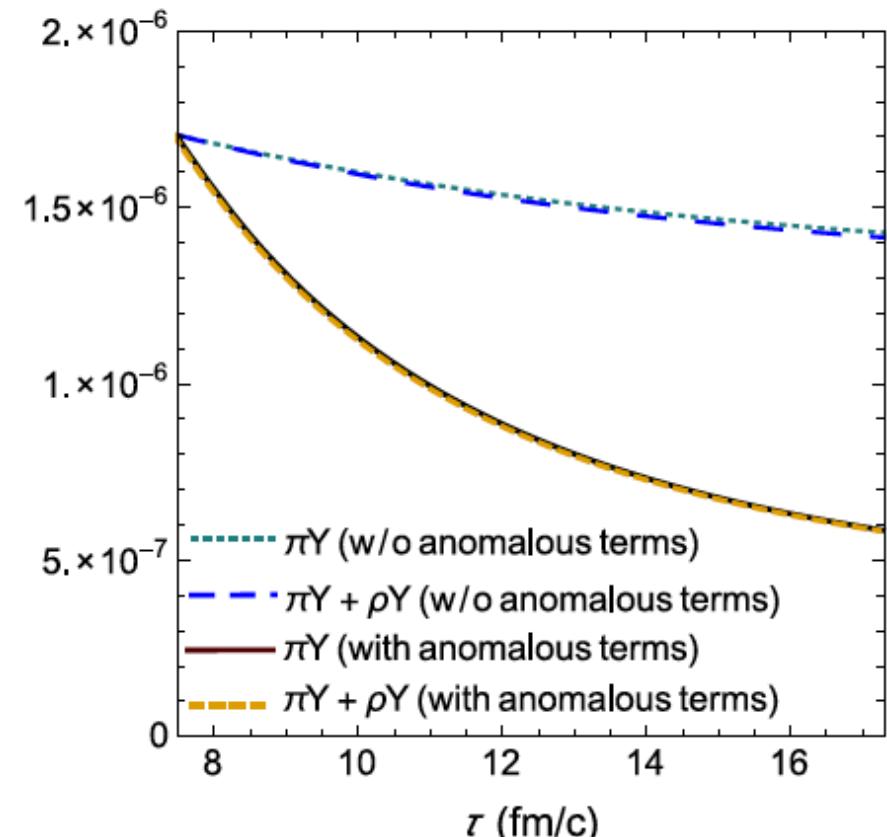


# Upsilon - pion cross sections



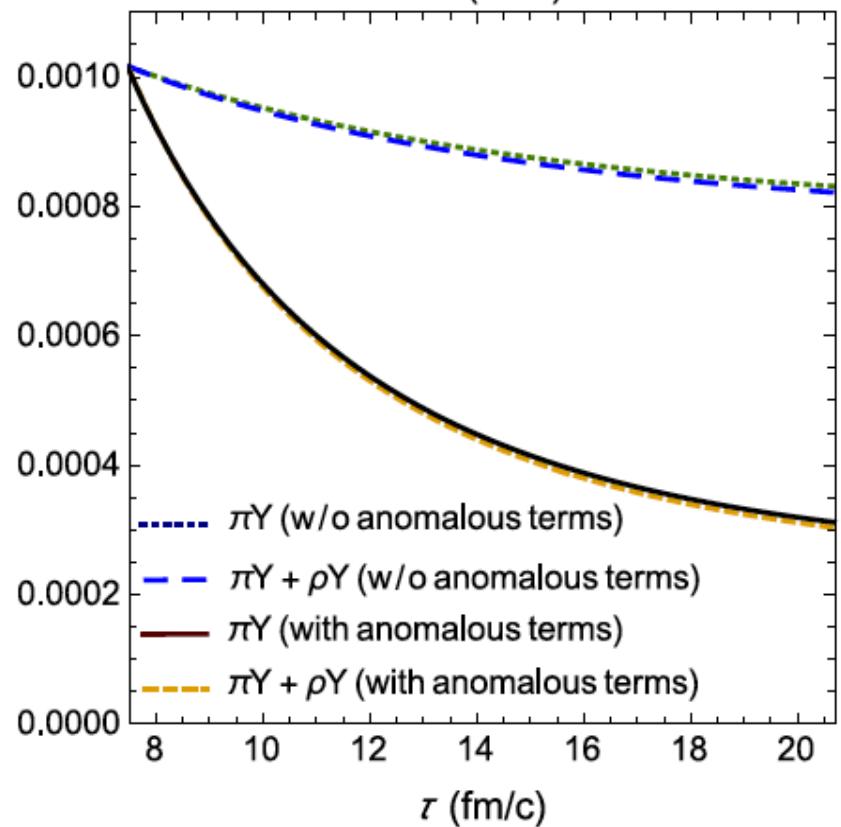
# Upsilon multiplicity and anomalous terms

RHIC



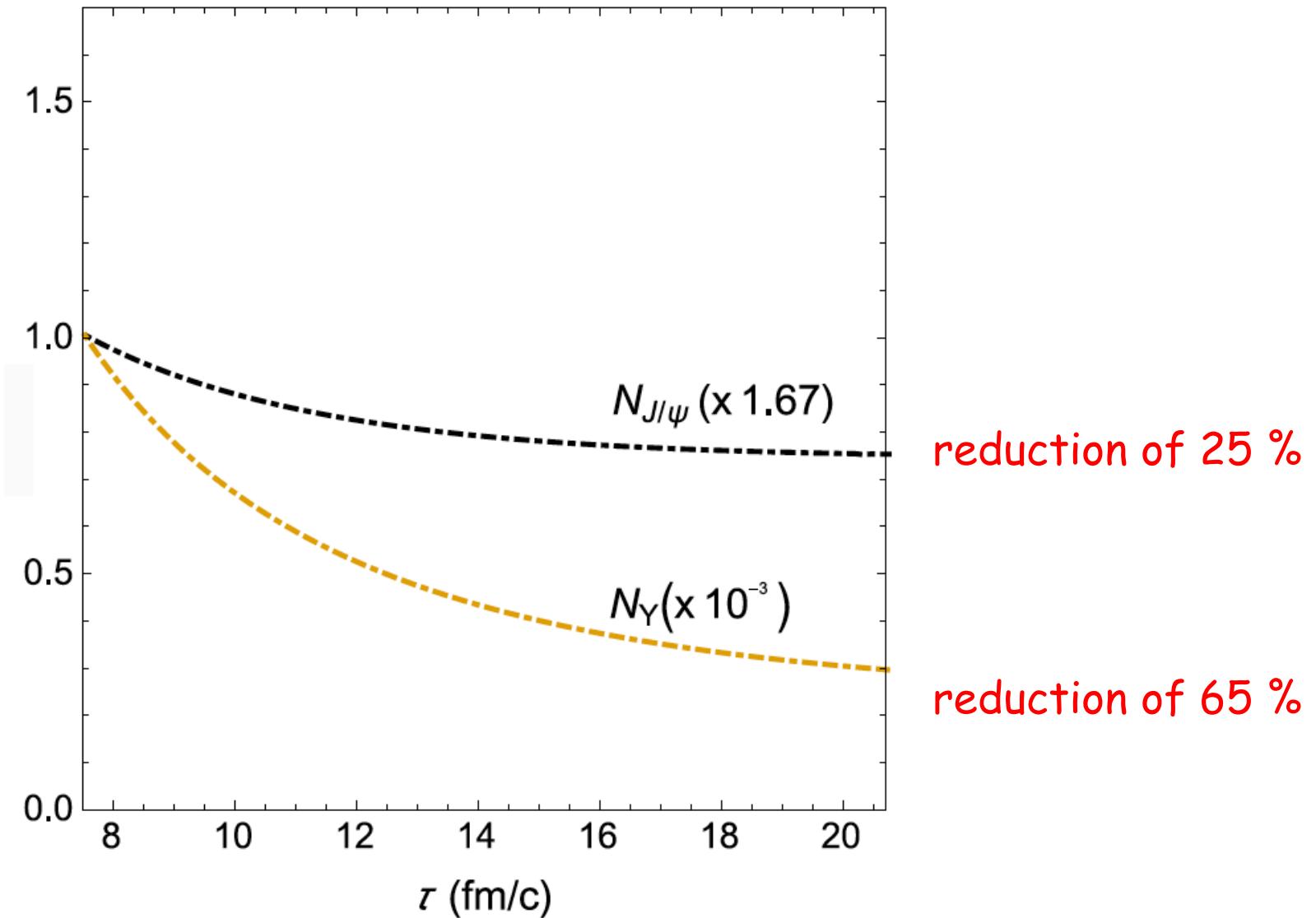
reduction of 60 %

LHC

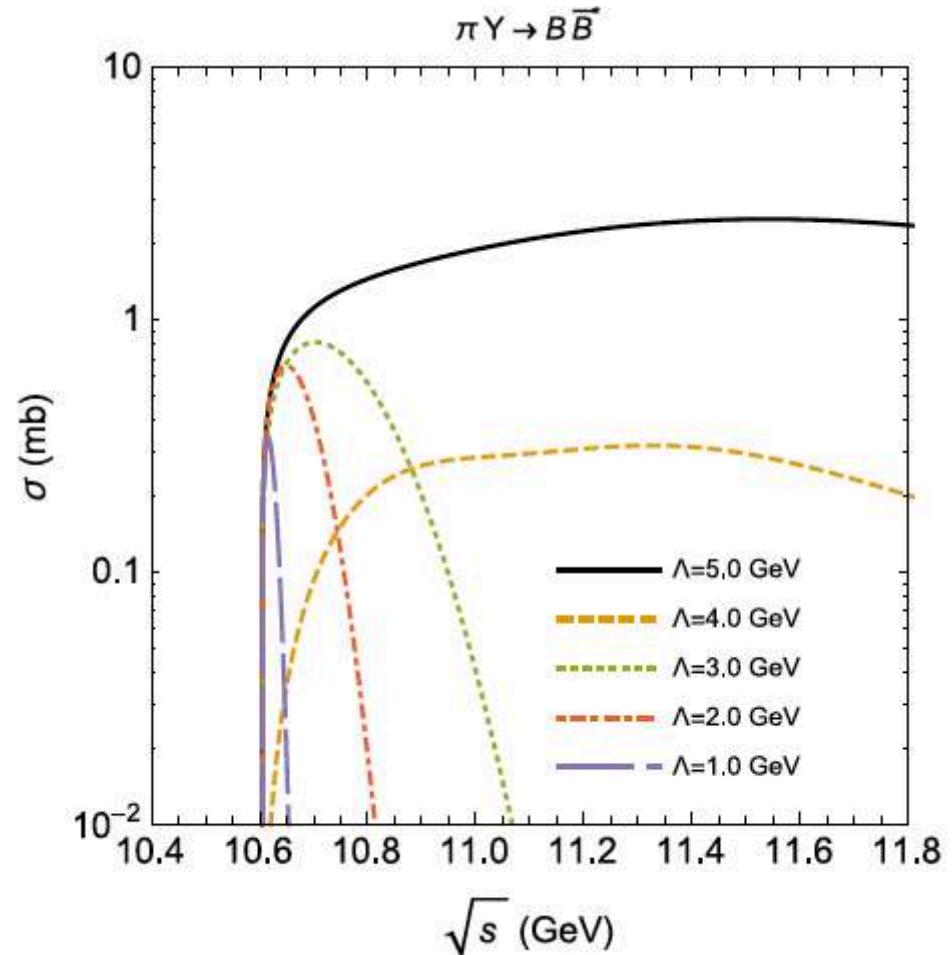
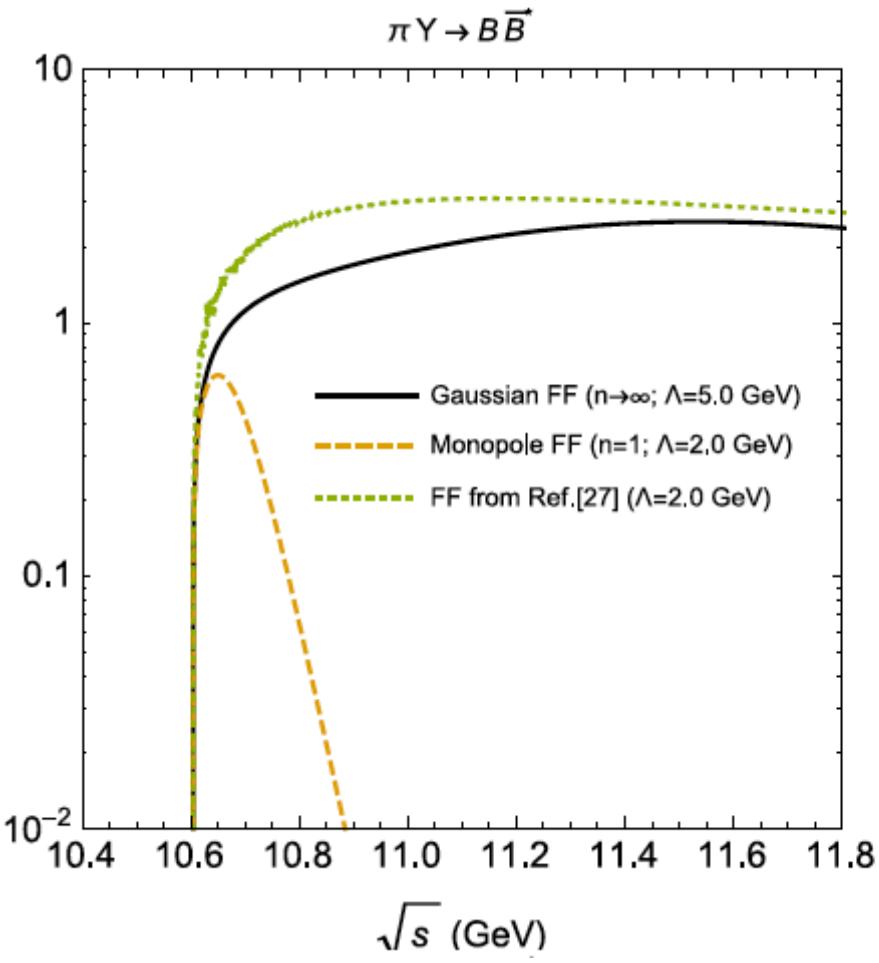


reduction of 65 %

# Charmonium X Bottomonium



# Problem: dependence on form factors



Hope: cure with QCD sum rules

# Summary

We have studied the production and absorption of heavy quarkonium in a hadron gas with an effective Lagrangian model

Role of  $\pi$ ,  $\rho$ ,  $\text{kaon}$ ,  $\text{kstar}$

Role of exotic resonances  $Z(3900)$ ,  $Z(4025)$

Role anomalous terms

Role of couplings and form factors

RHIC and LHC

Effective Lagrangian approach  
can be systematically improved with QCDSR

As in data we find suppression with:

--Weak energy dependence

--Bottom more suppressed than charm

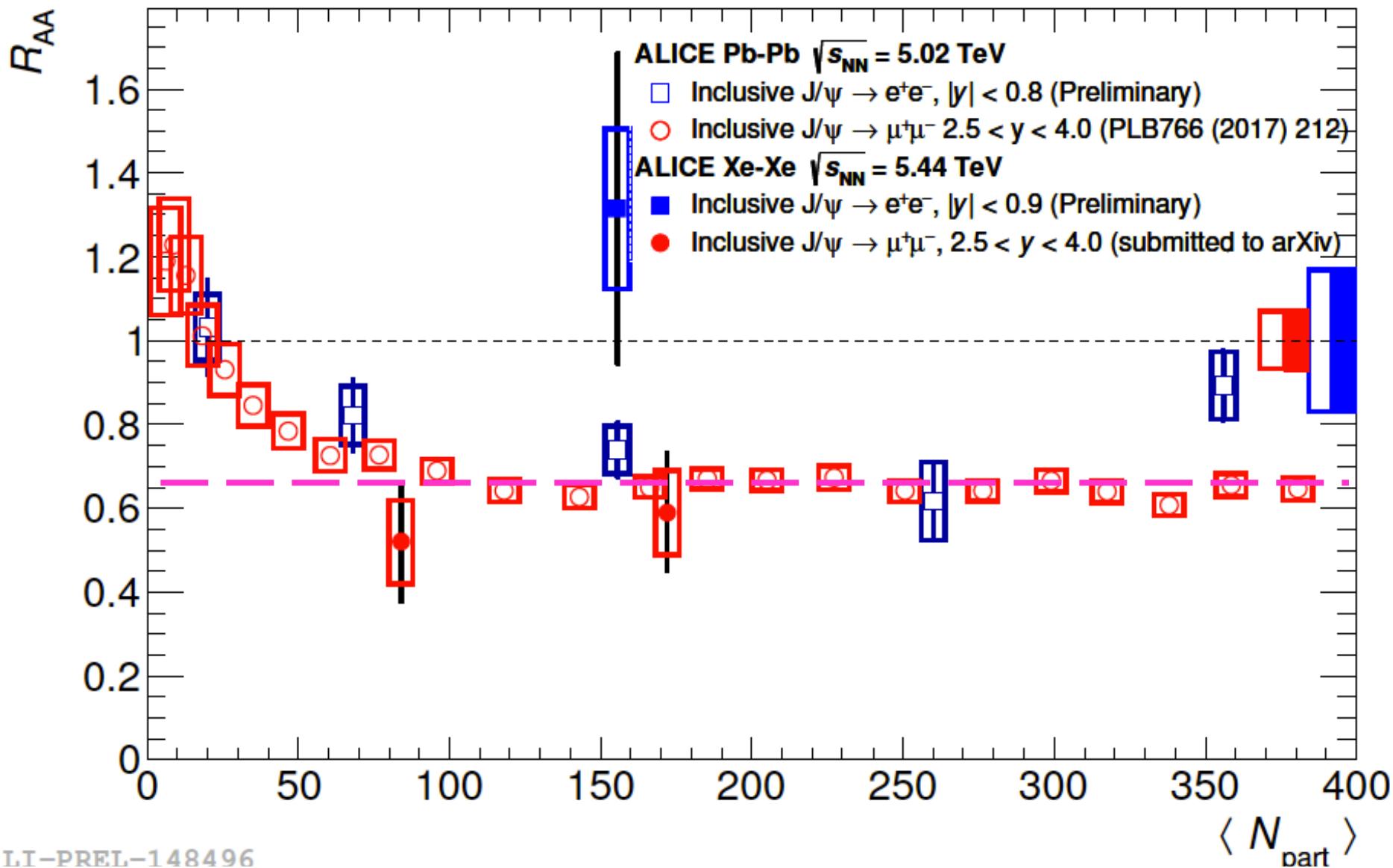
Hadronic phase is important !

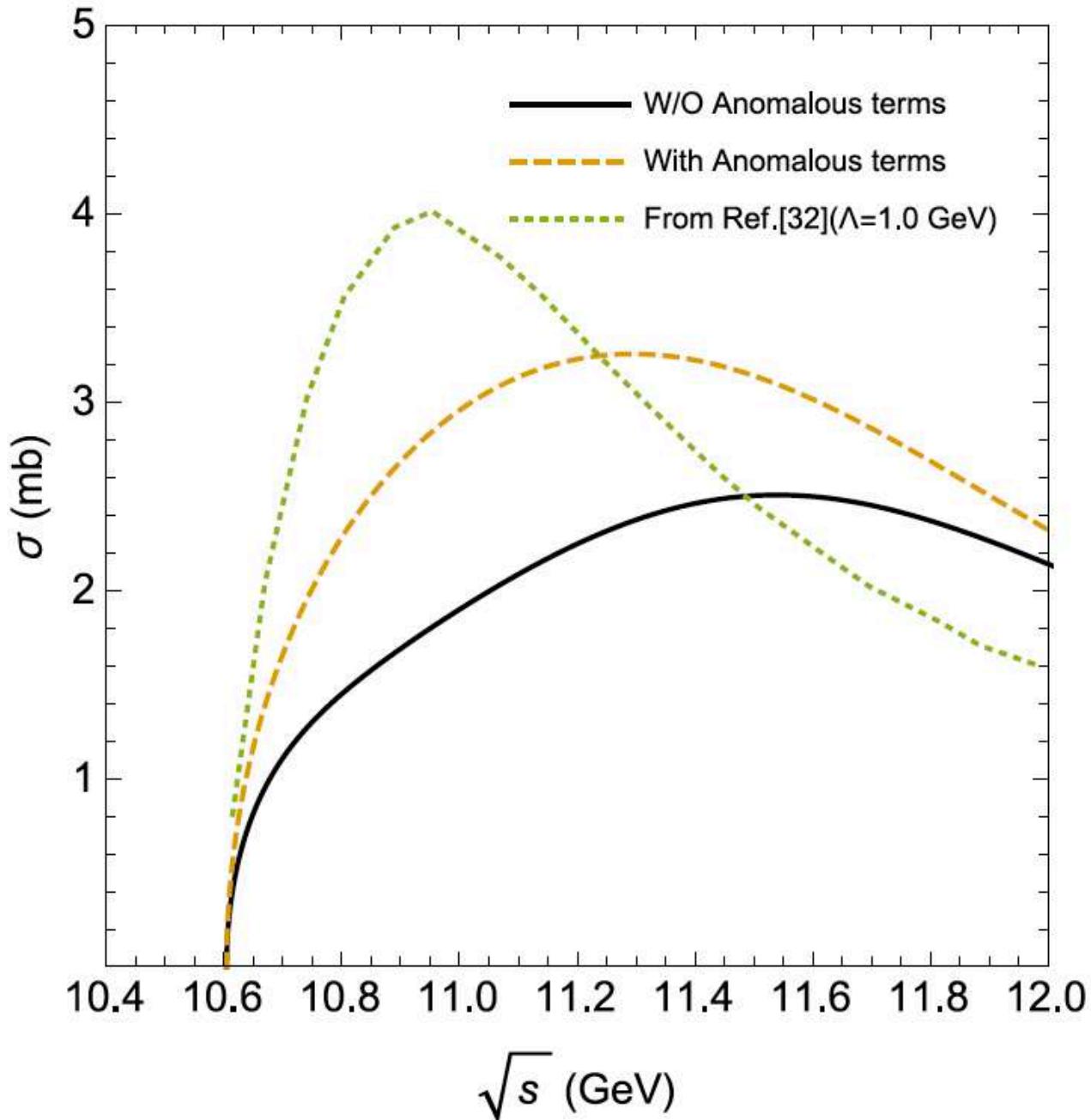
# Back-ups

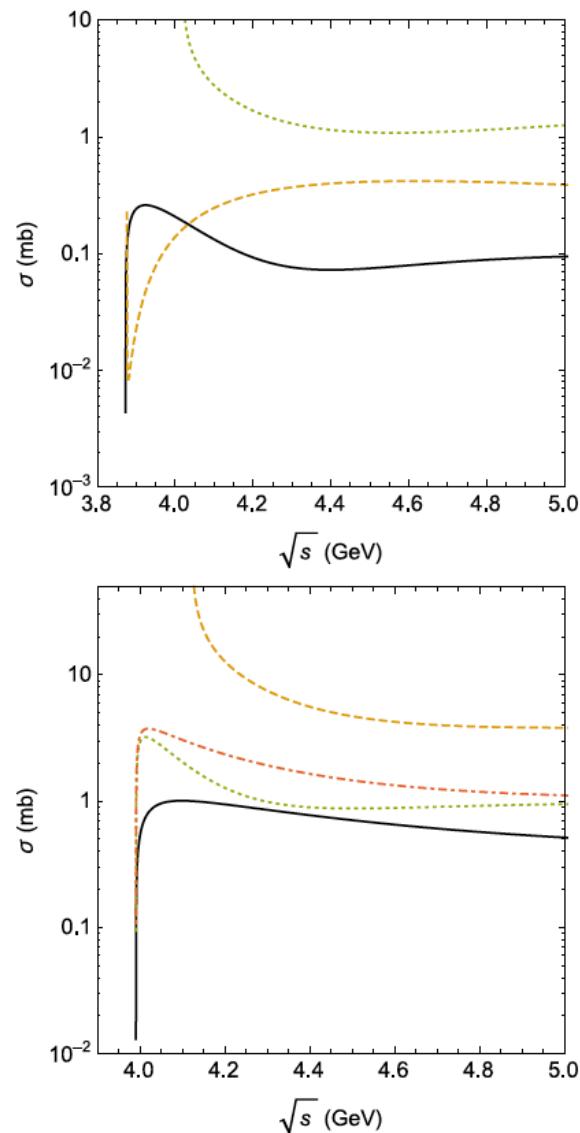
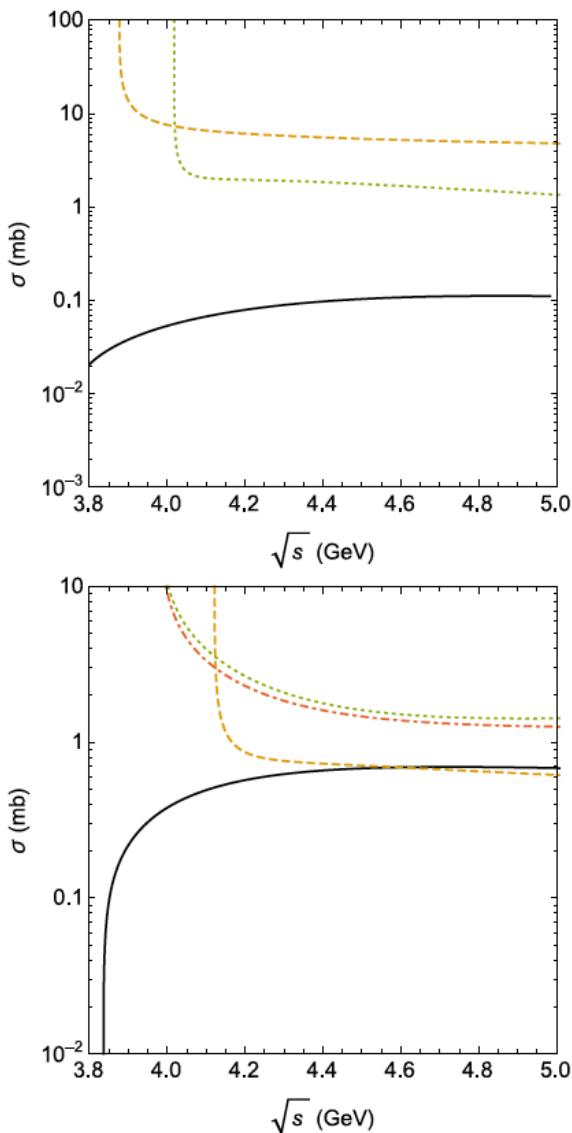
# Charmonium

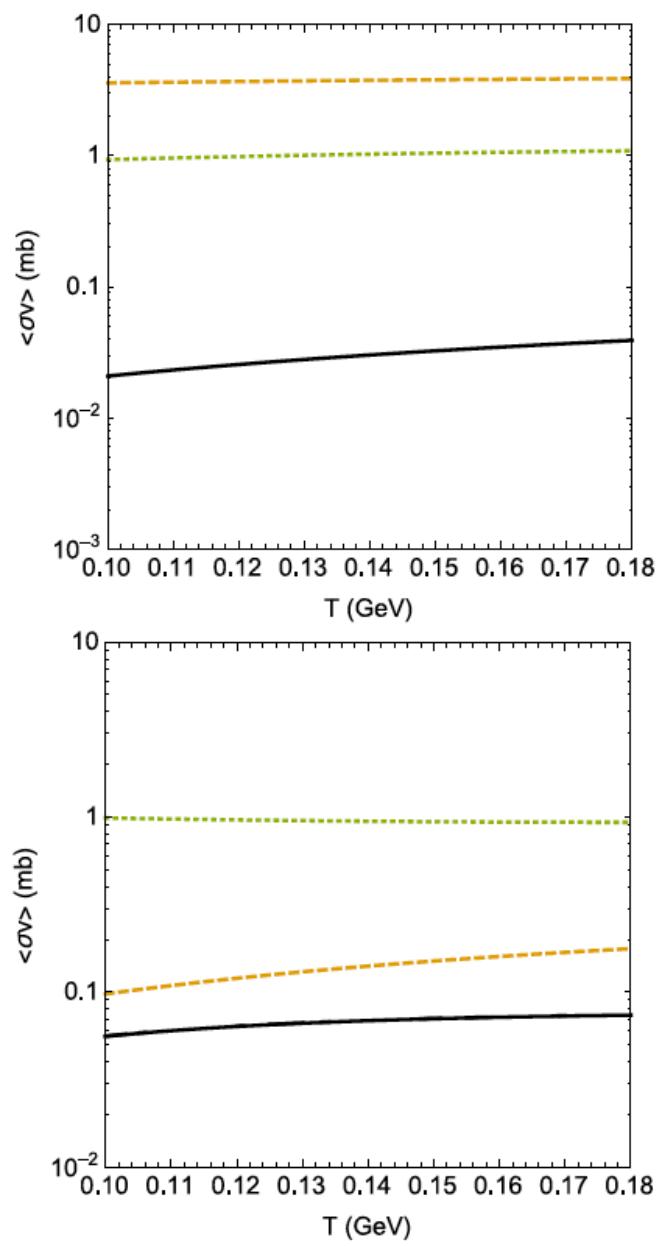
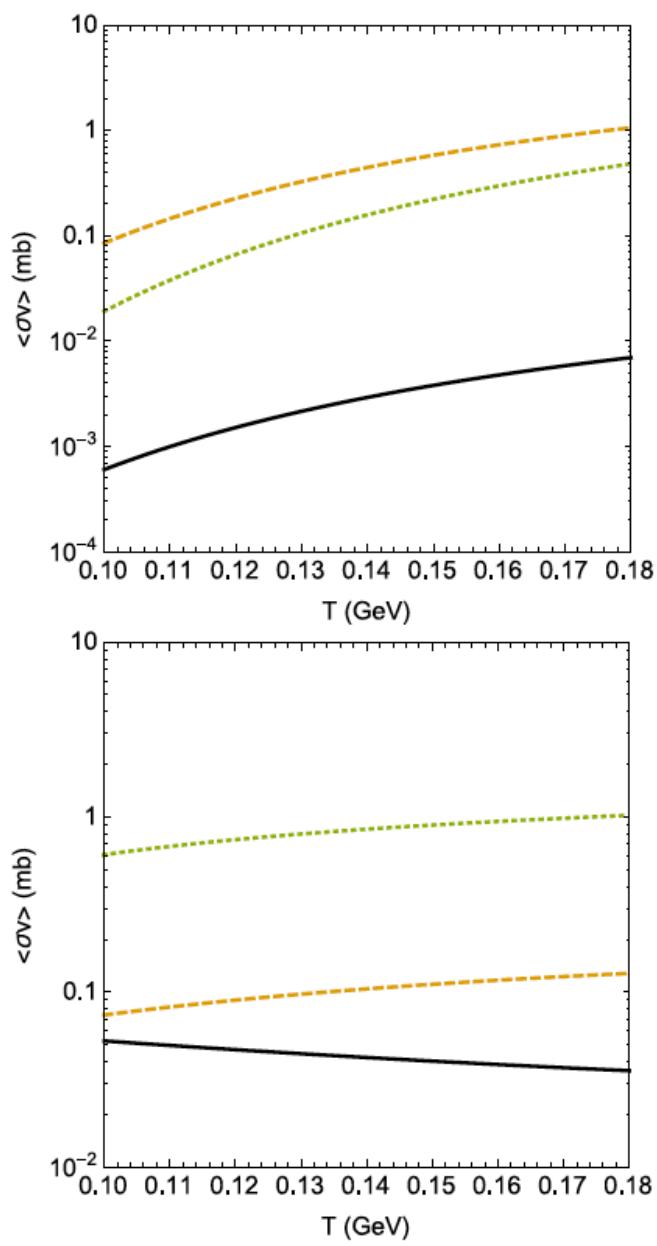
Abreu et al., arxiv:1712.06019

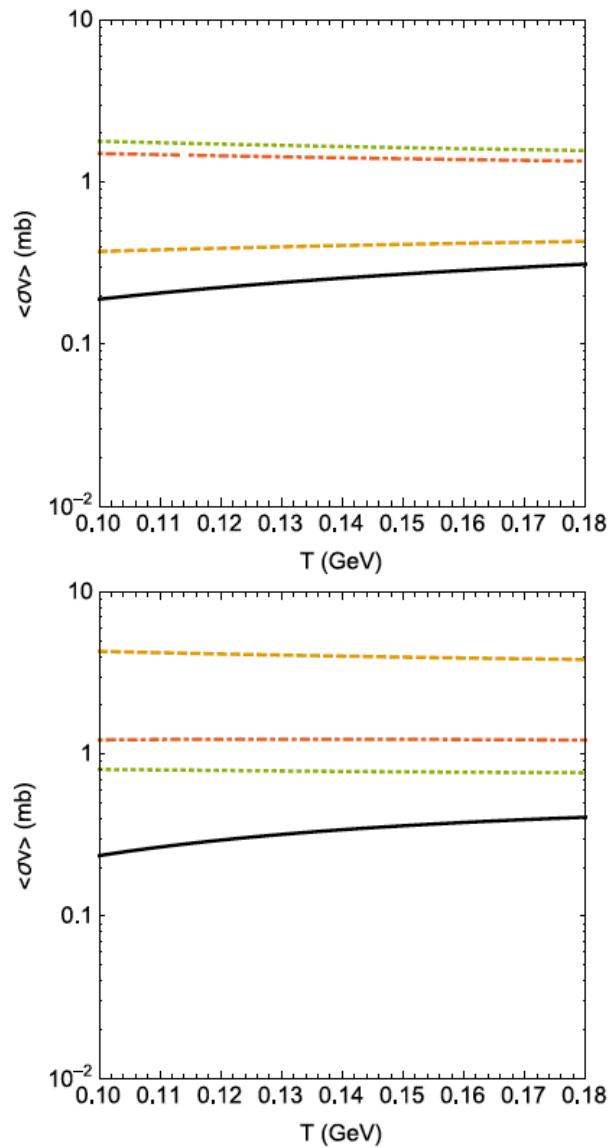
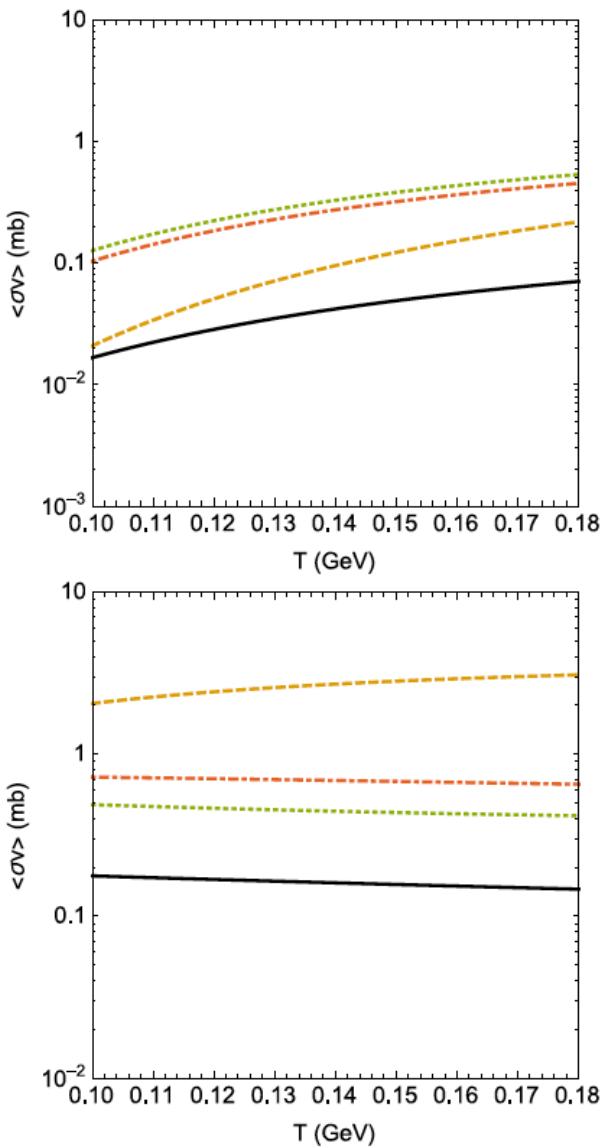
# "Unsuppression" is robust !

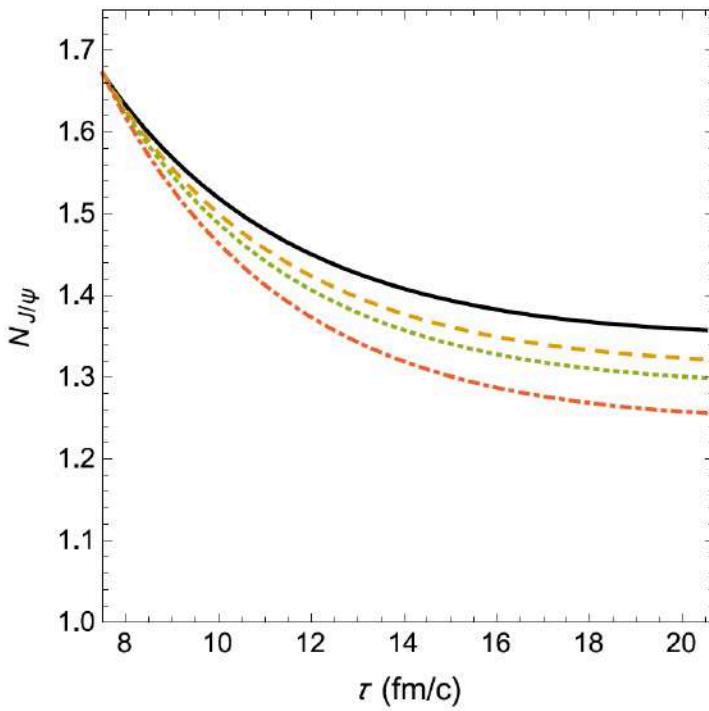
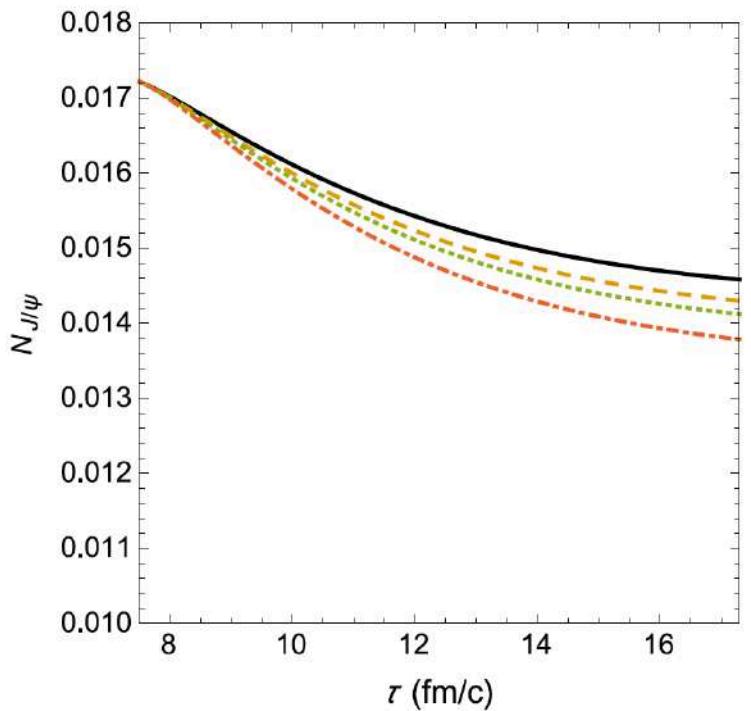


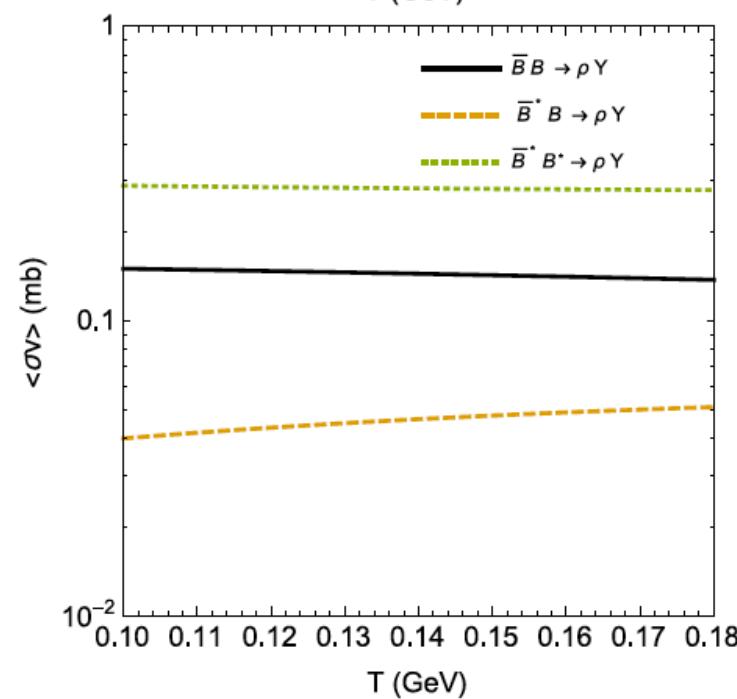
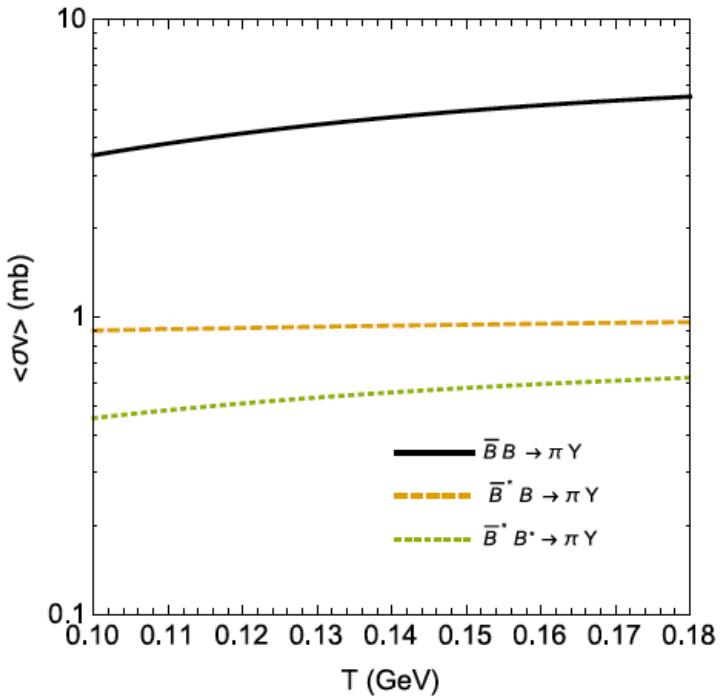
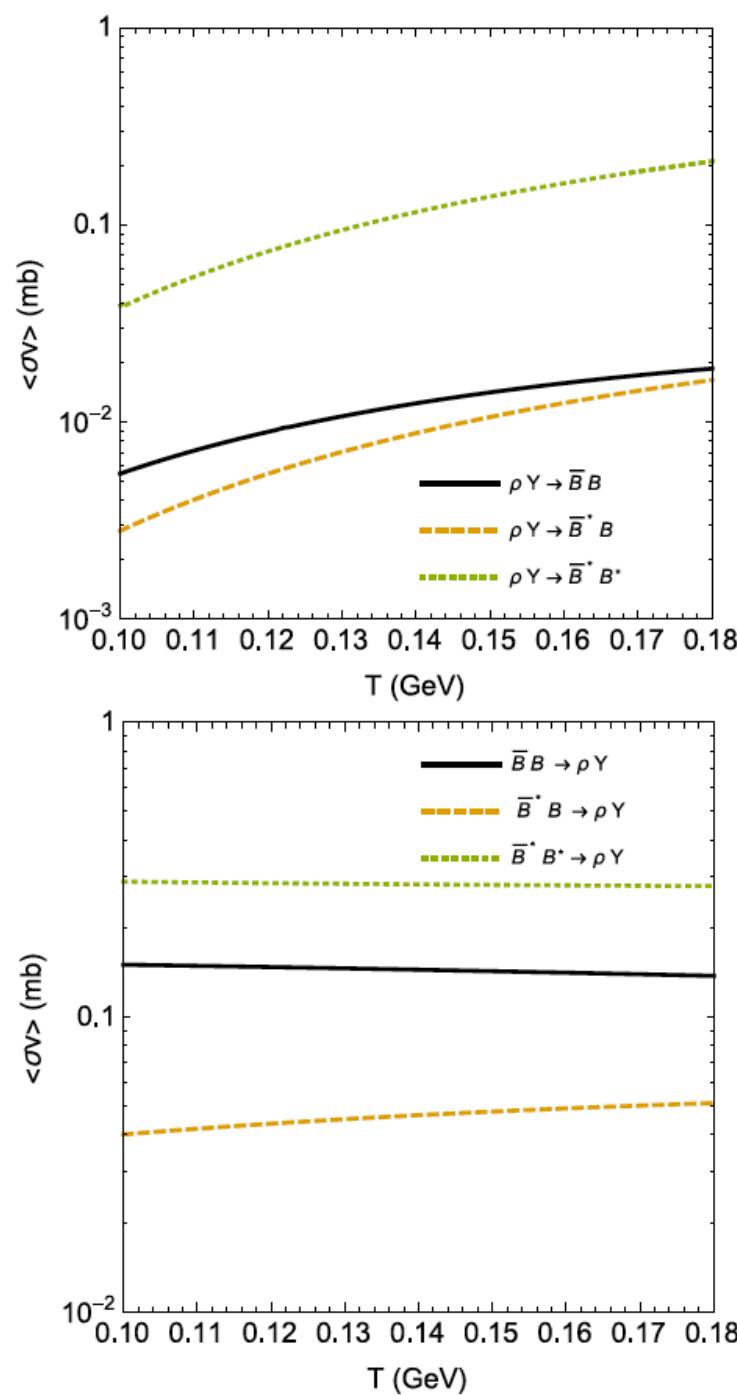
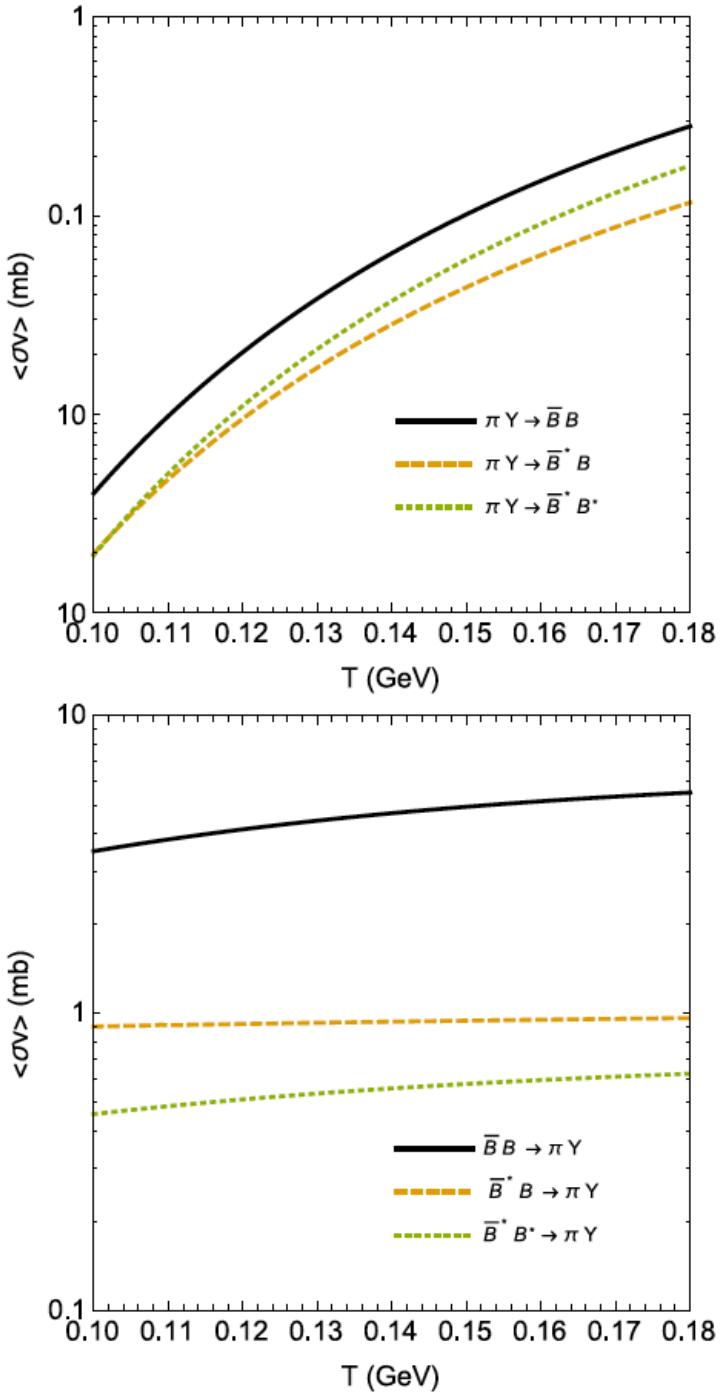
$\pi Y \rightarrow B\bar{B}^*$ 











# Quarkonium suppression in the QGP

$$T = 0$$

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + \sigma r$$

$$T > T_c$$

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r}$$

$$T > 1.5 T_c$$

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} e^{-r/r_D}$$

If screening radius is smaller than Bohr radius:

$$r_D < r_\psi$$

Quark and antiquark do not bind !

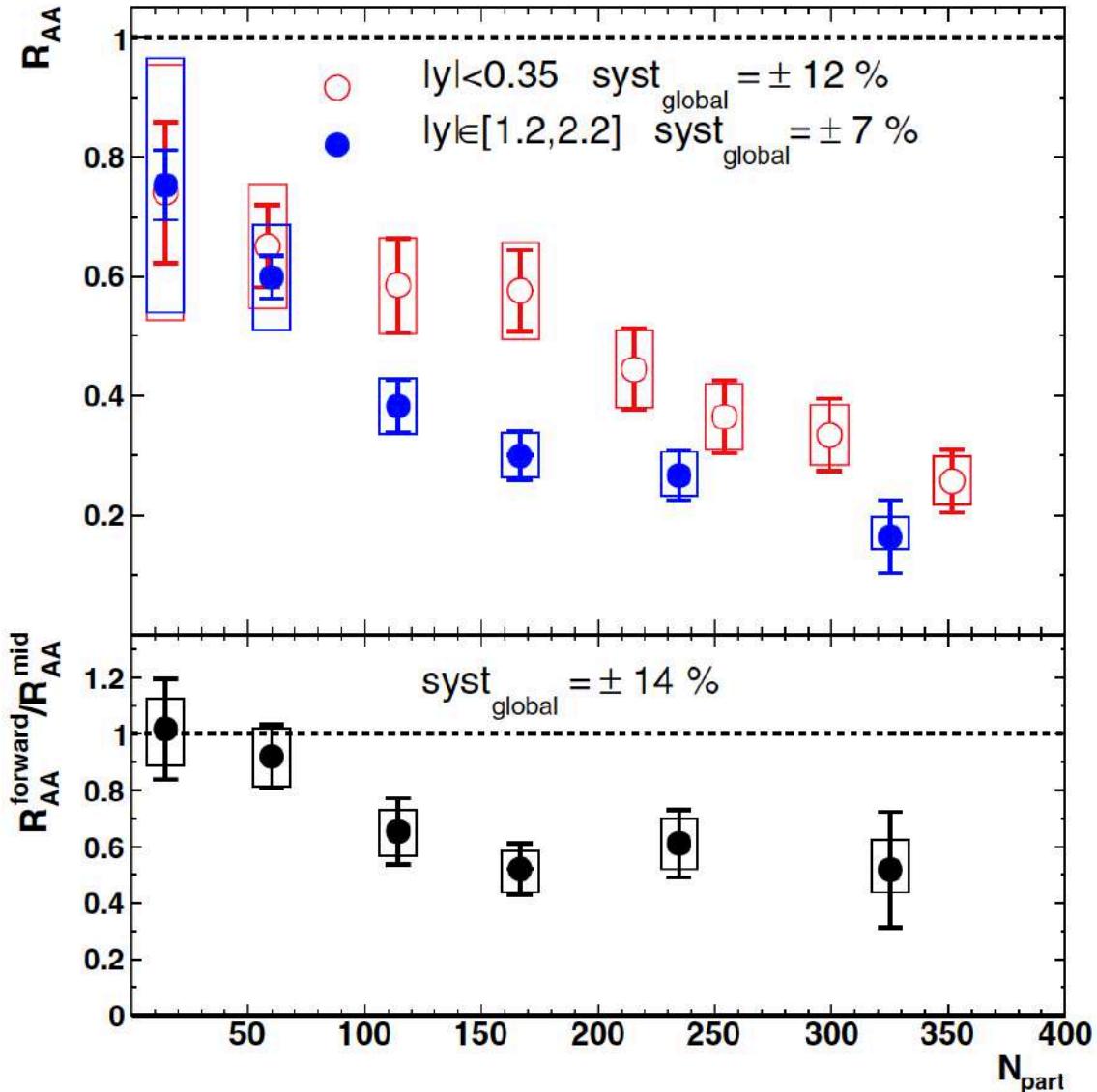
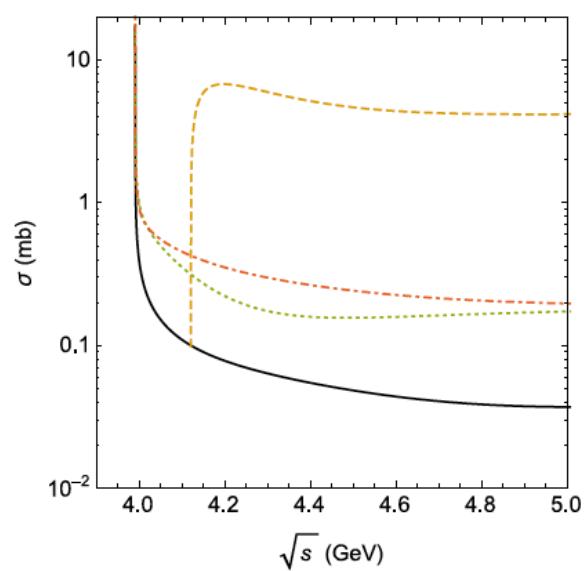
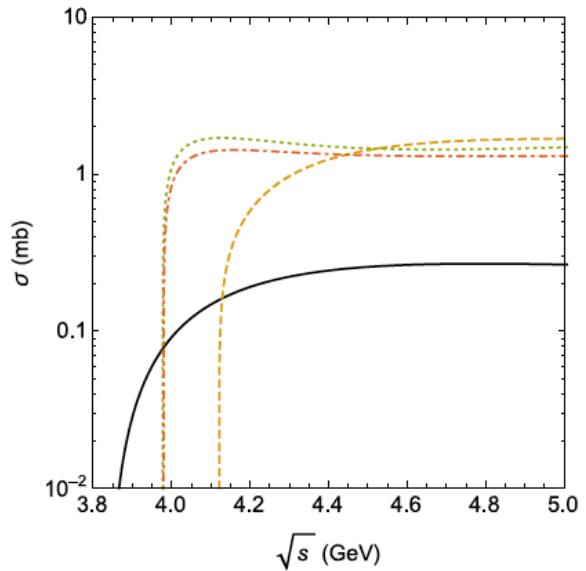
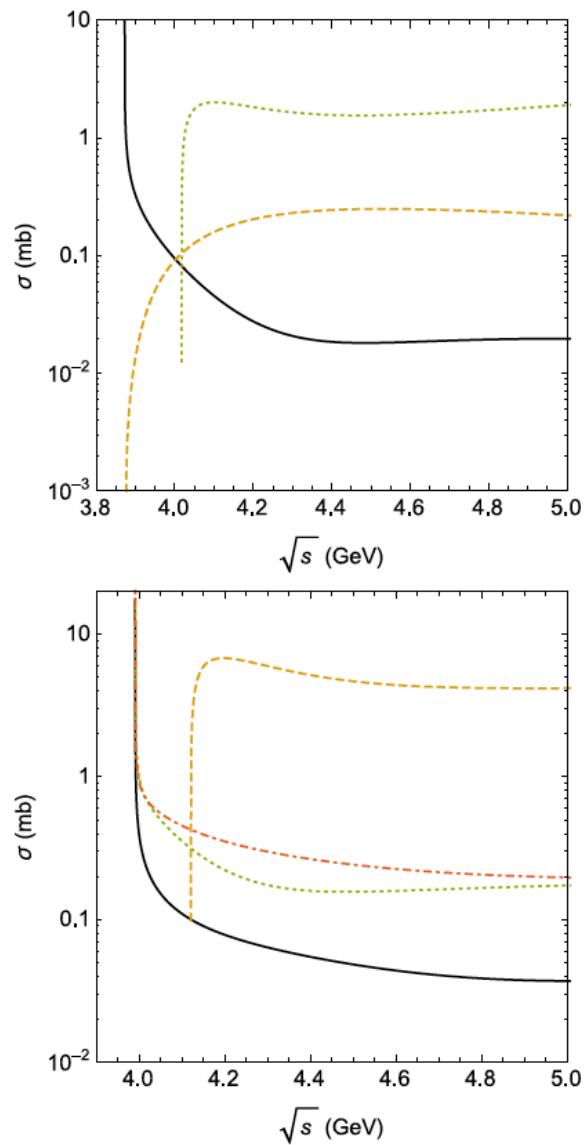
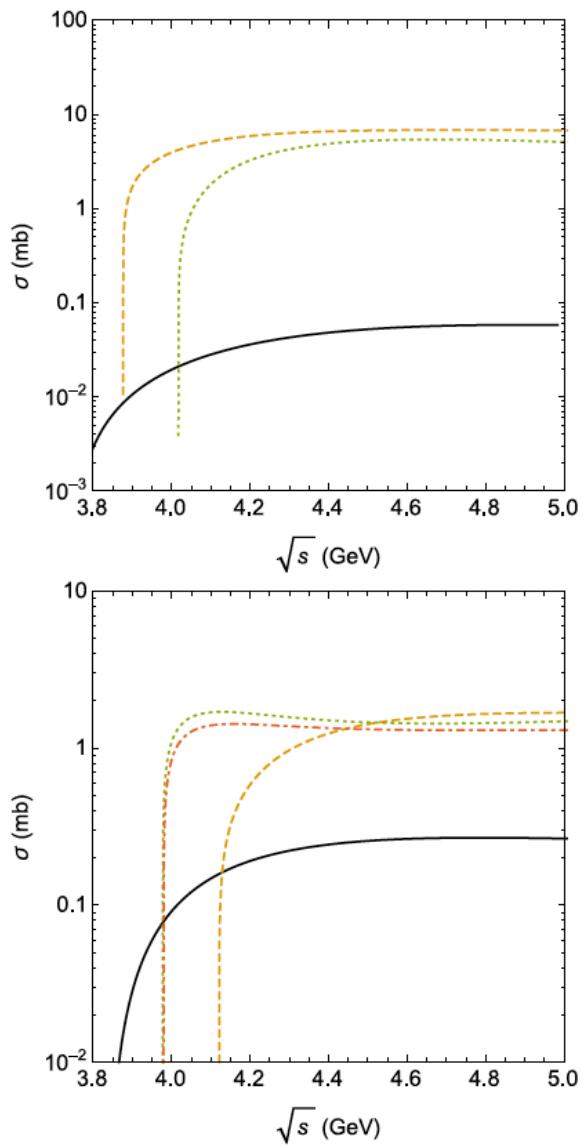
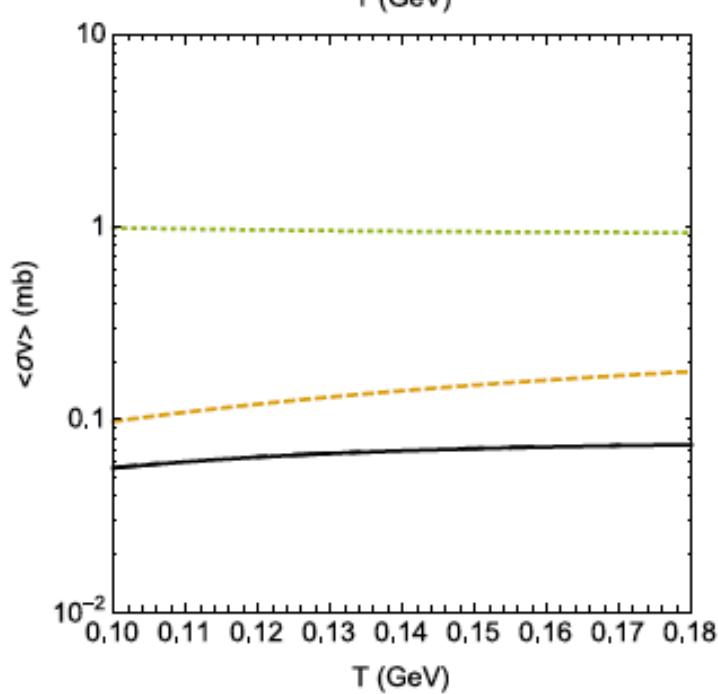
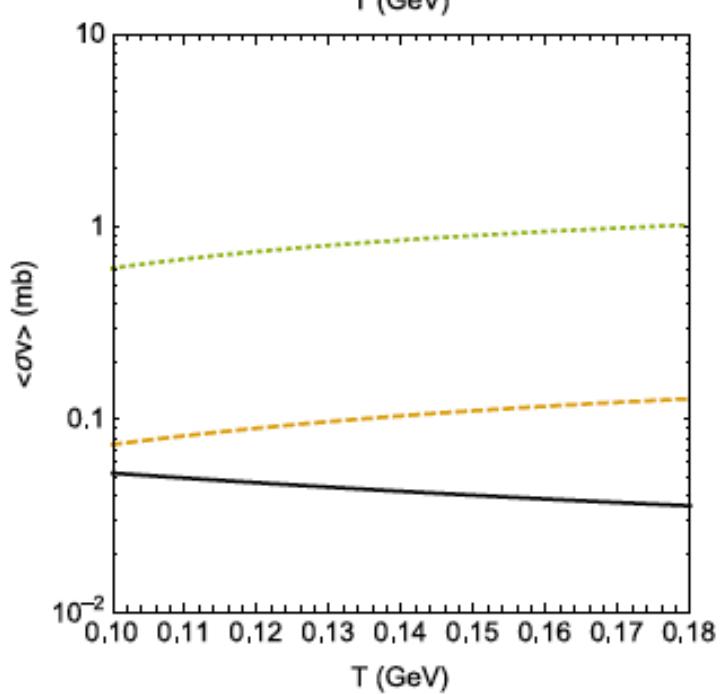
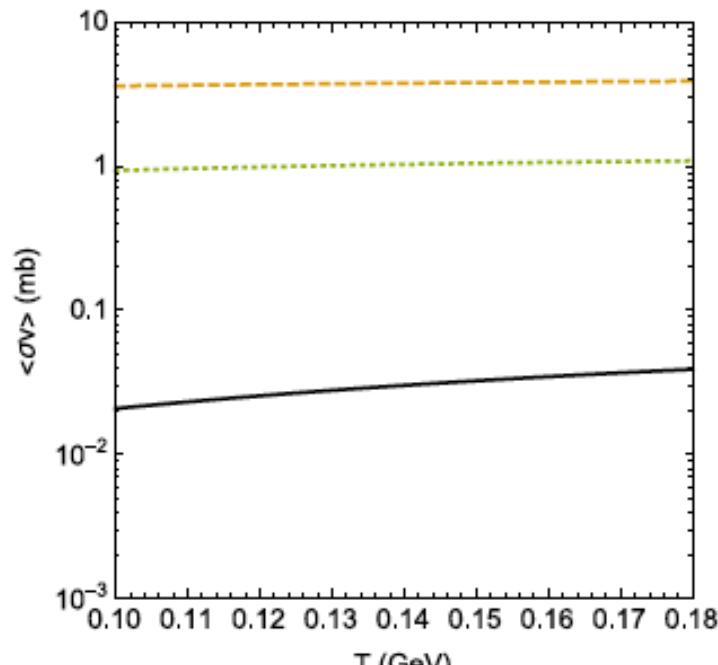
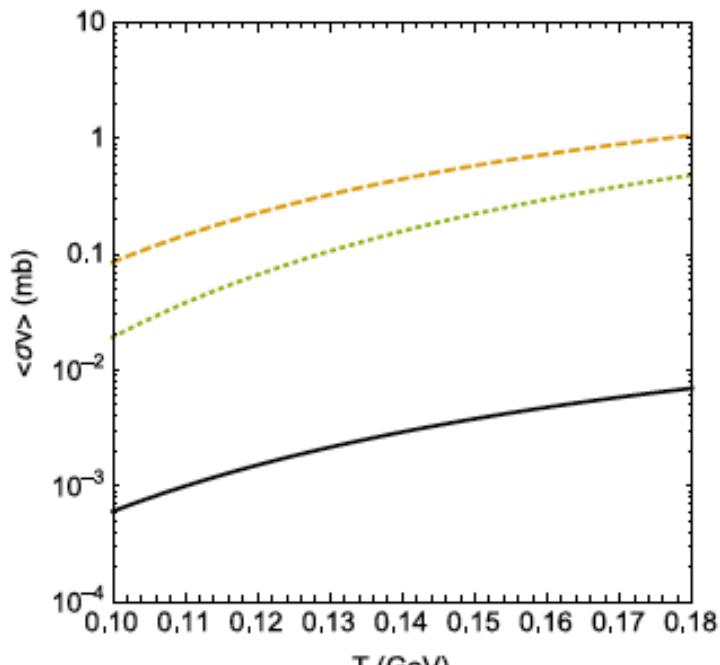
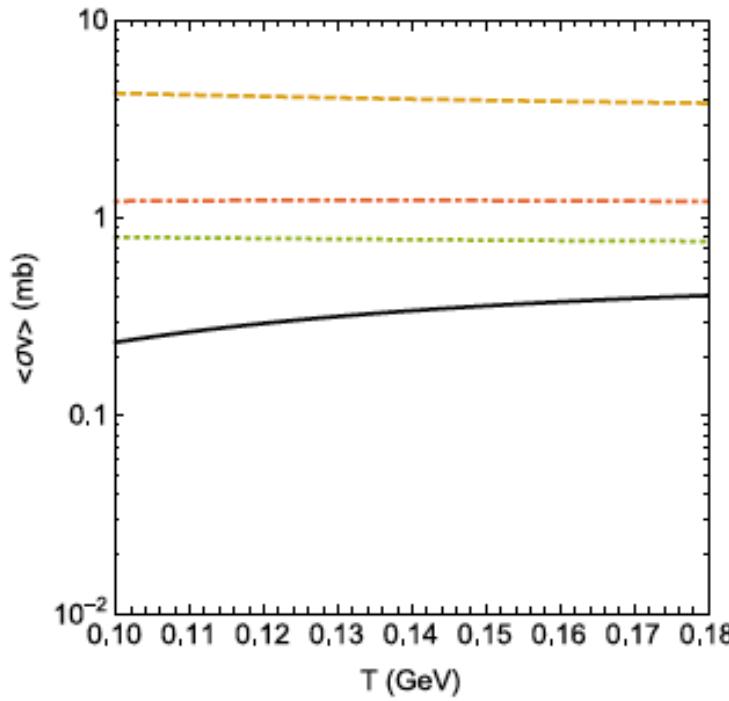
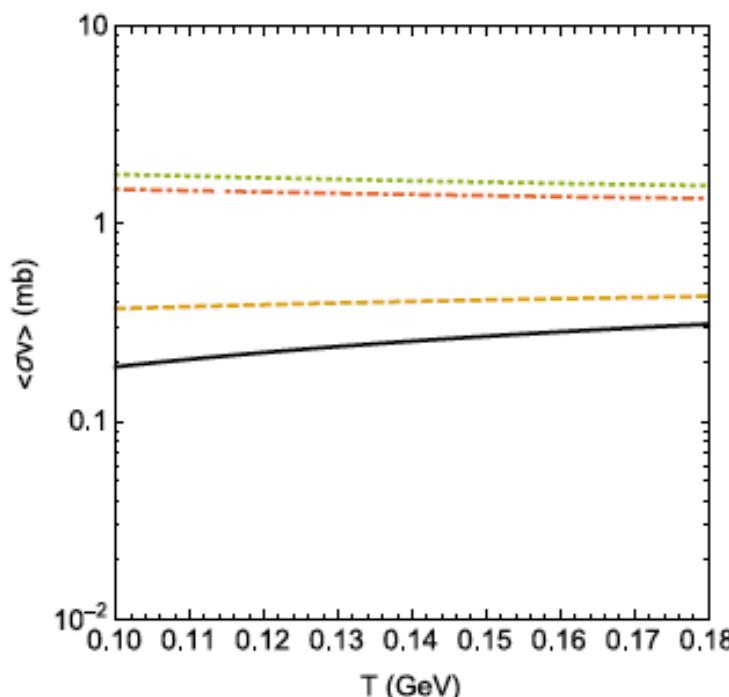
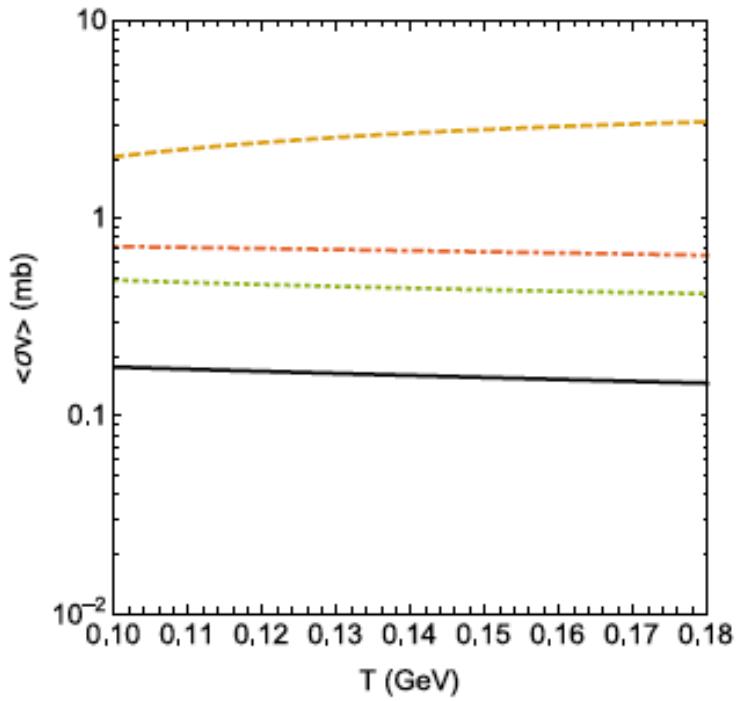
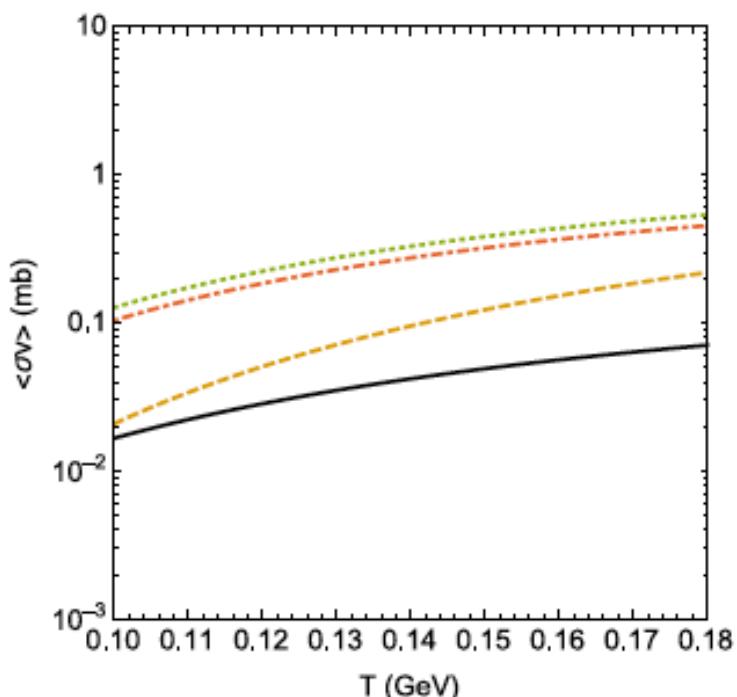
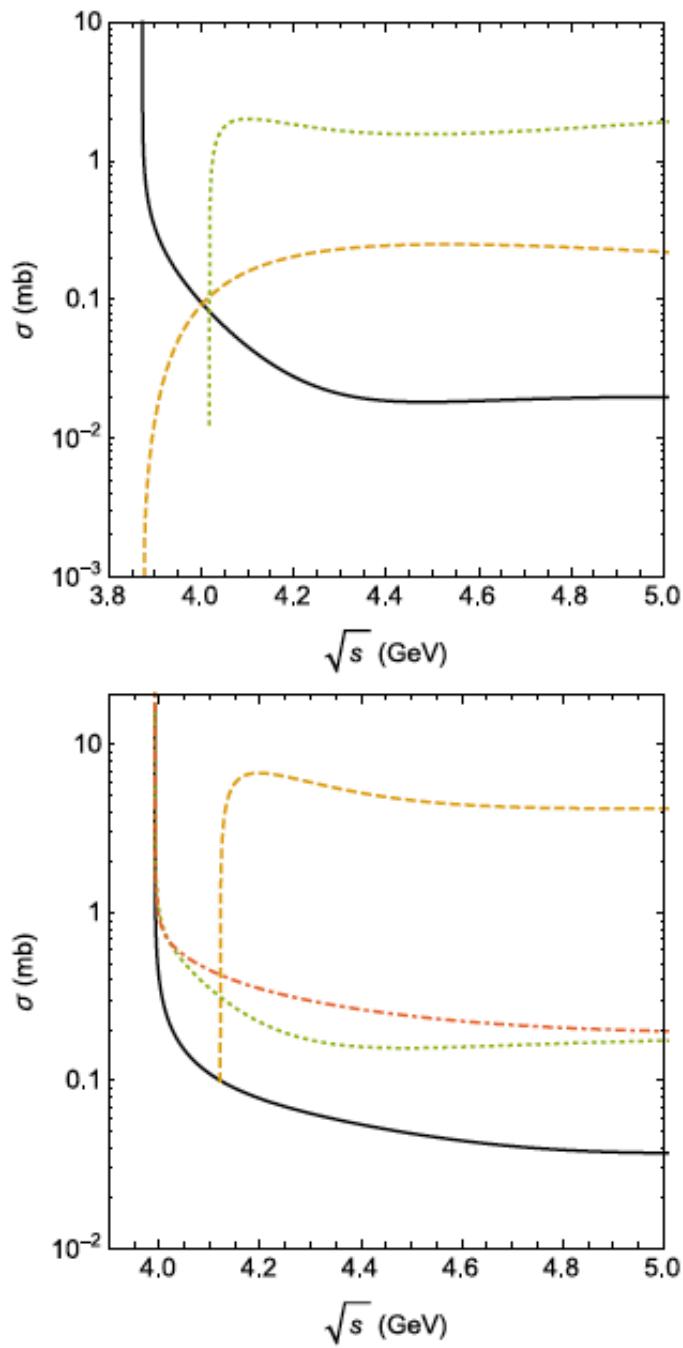
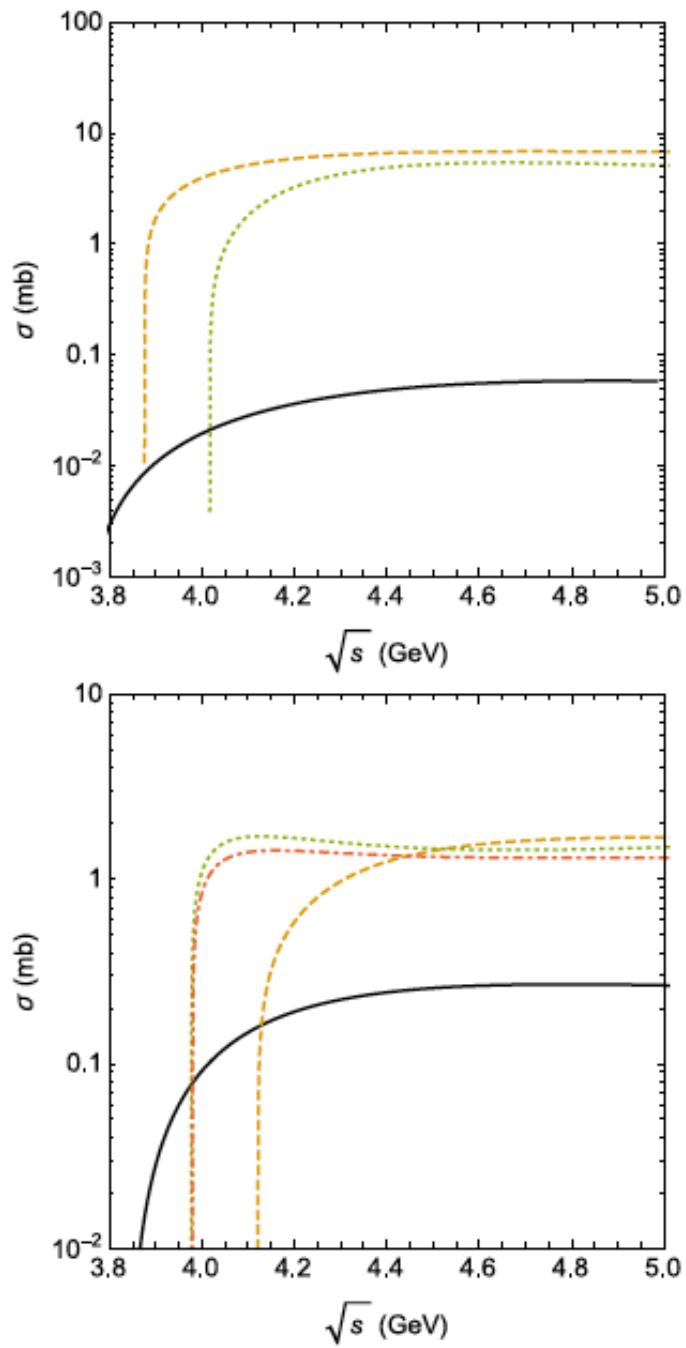


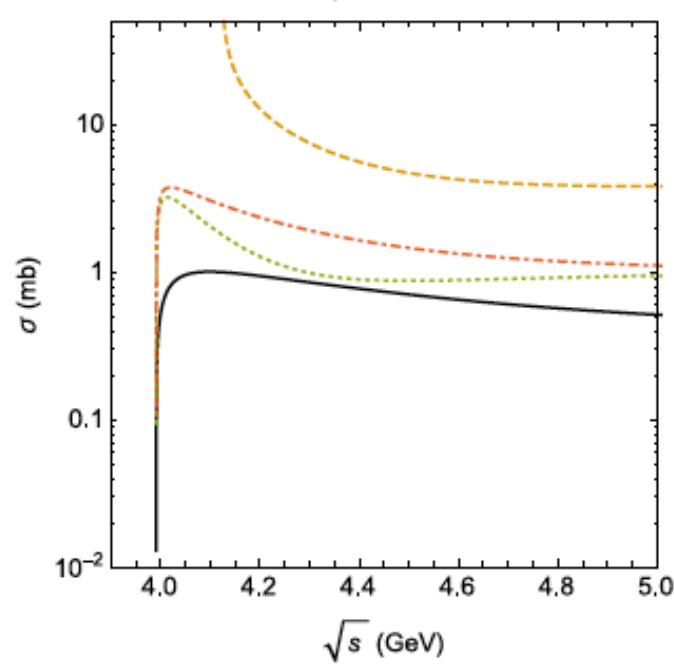
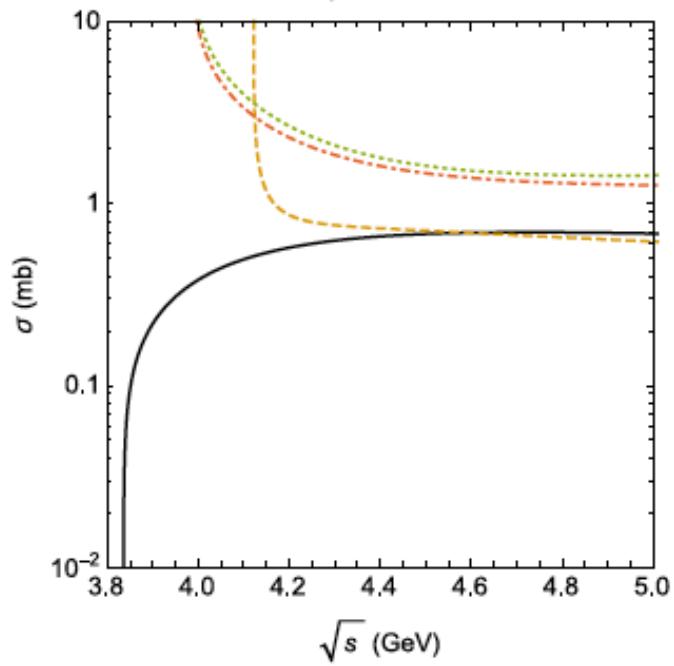
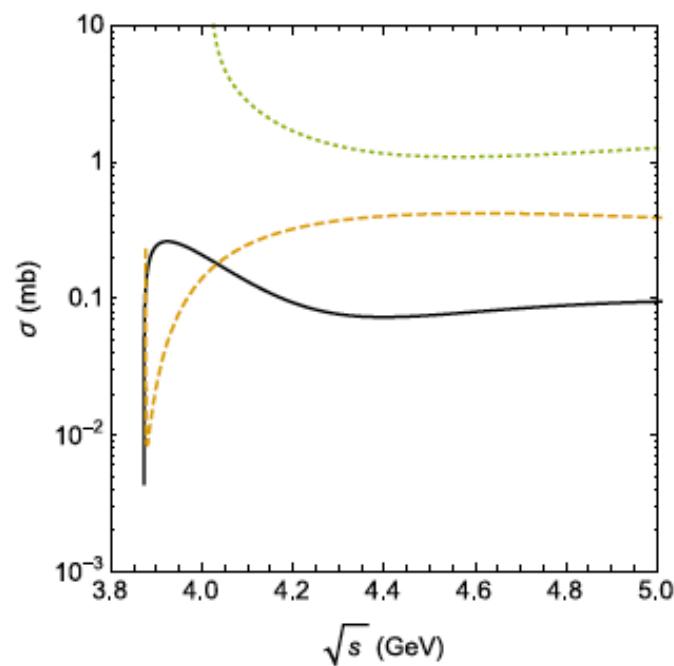
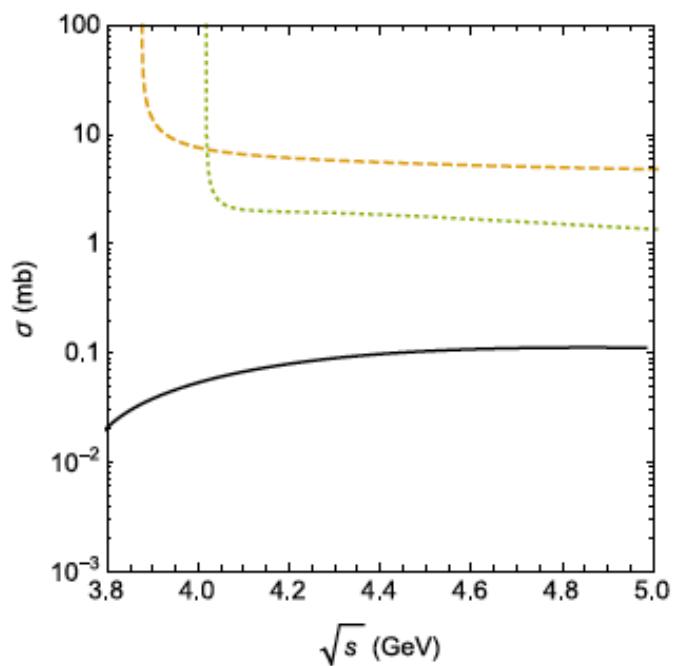
FIG. 5 (color online). (a)  $J/\psi R_{\text{AA}}$  versus  $N_{\text{part}}$  for Au + Au collisions. Mid (forward) rapidity data are shown with open (solid) circles. (b) Ratio of forward or midrapidity  $J/\psi R_{\text{AA}}$  versus  $N_{\text{part}}$ . For the two most central bins, midrapidity points

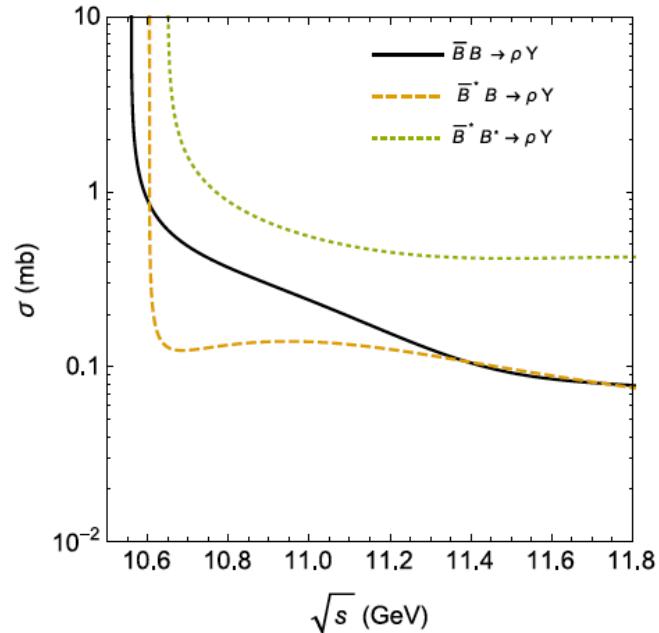
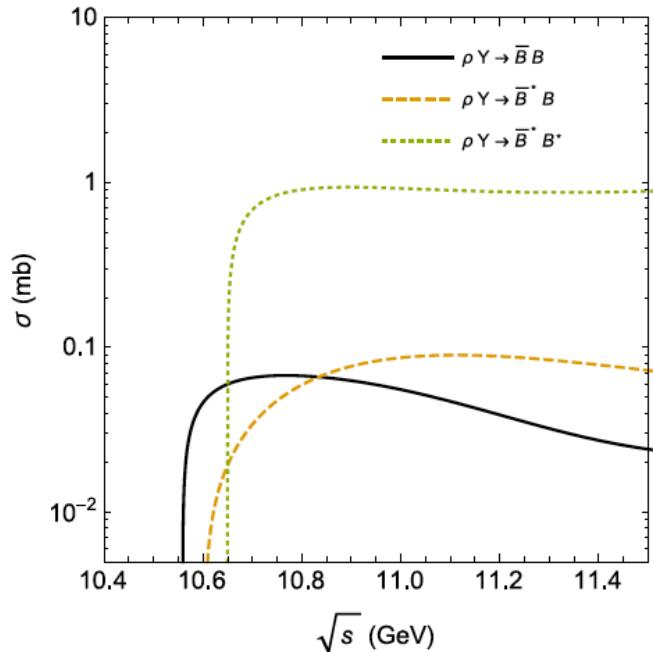
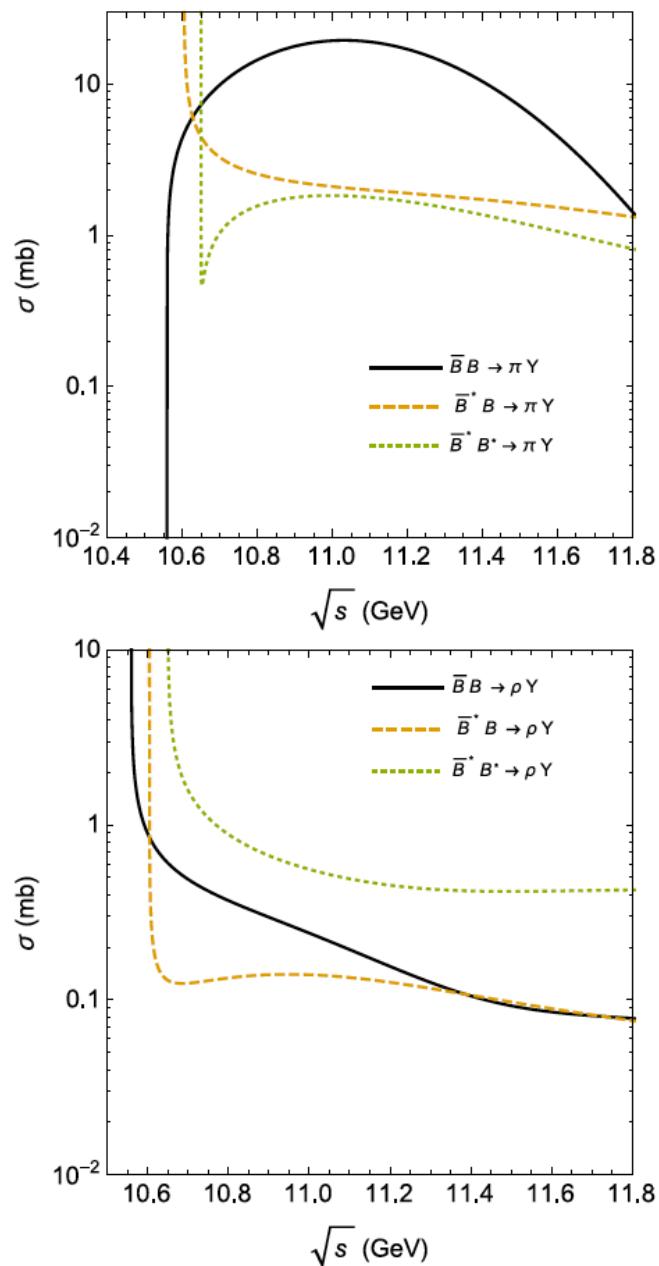
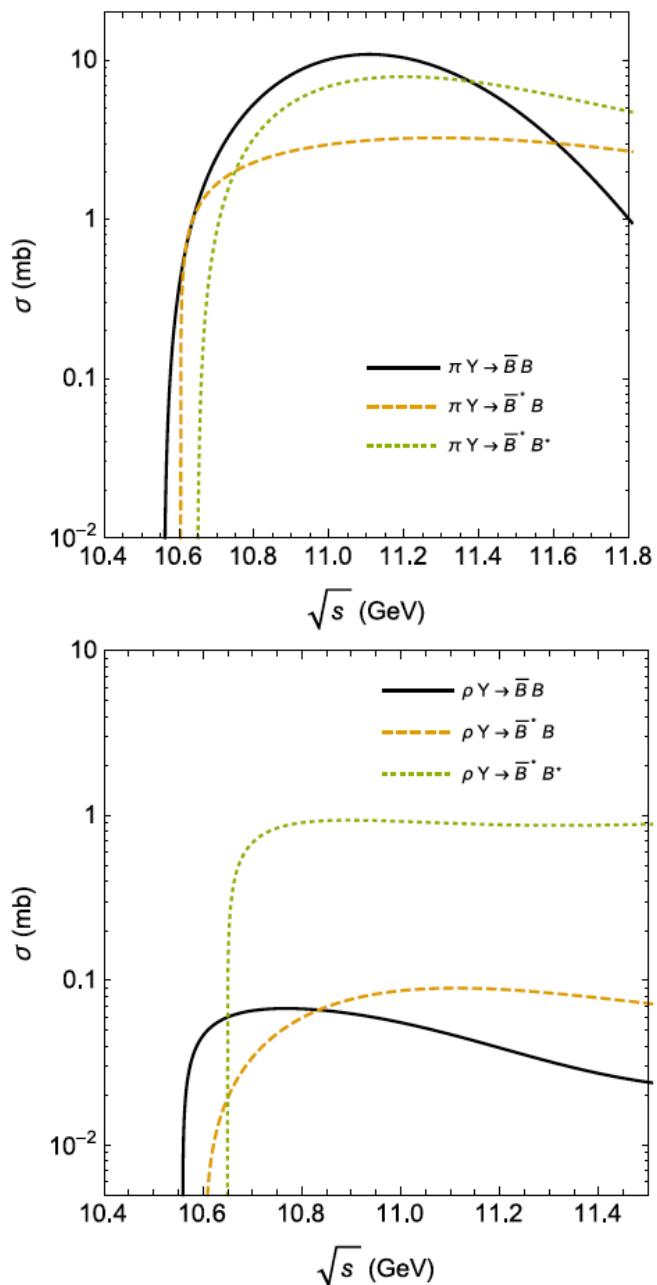


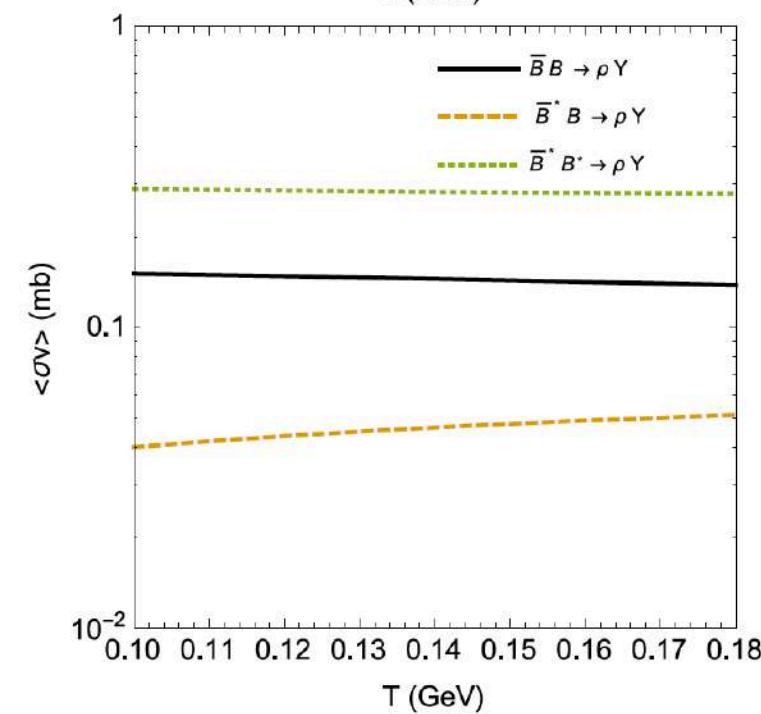
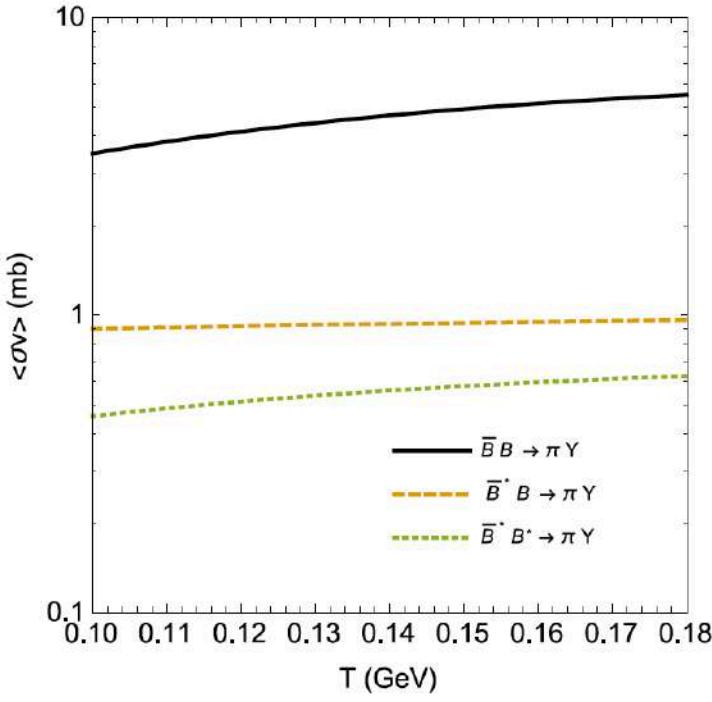
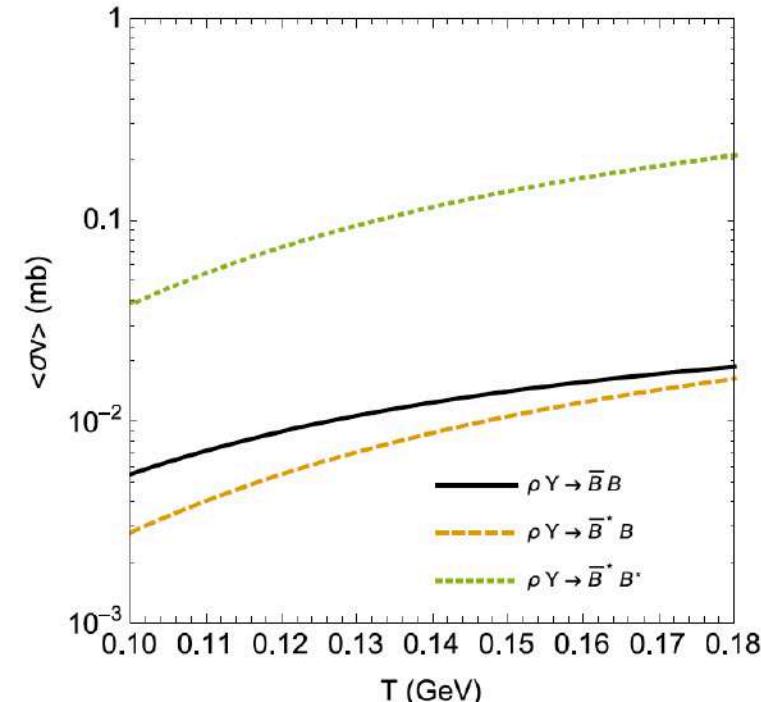
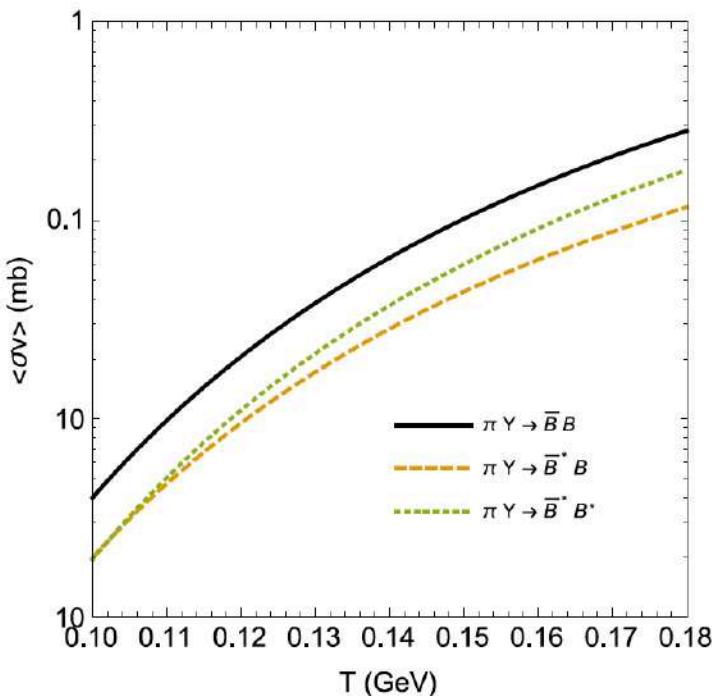




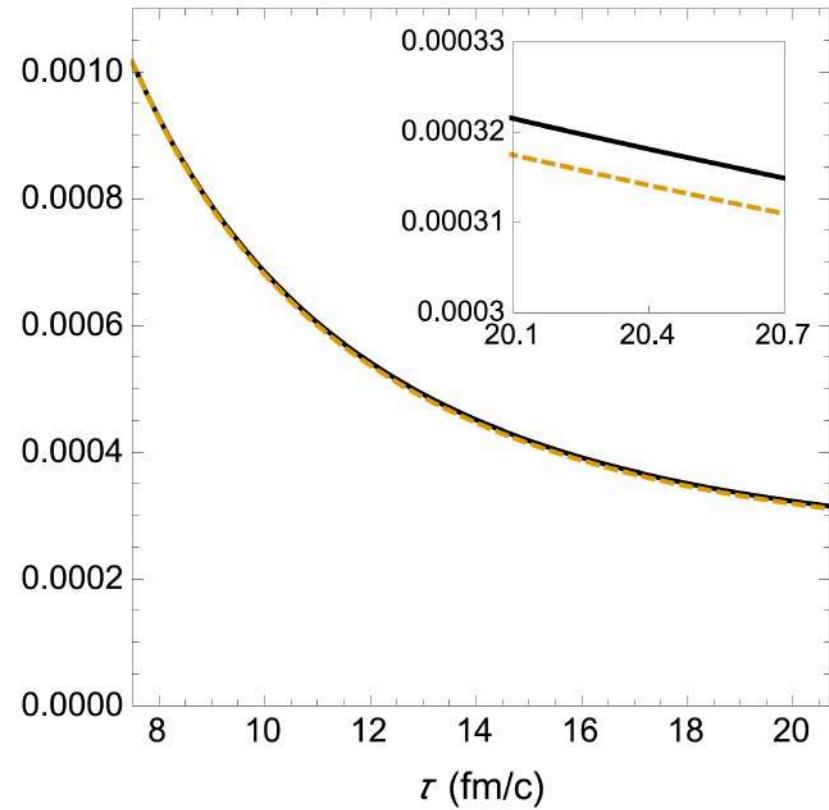
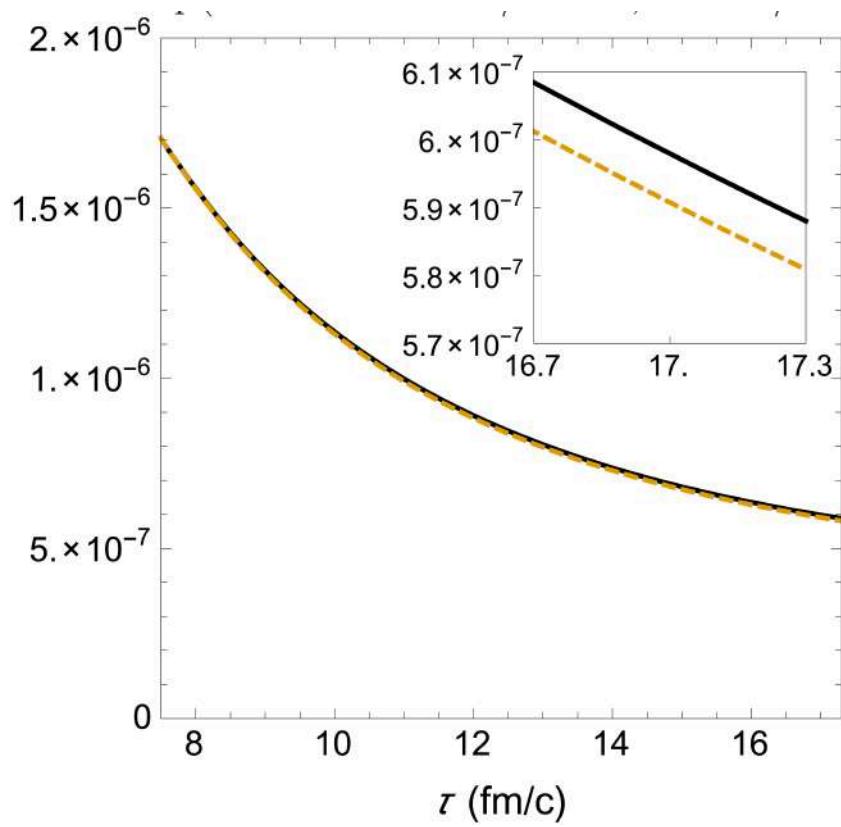






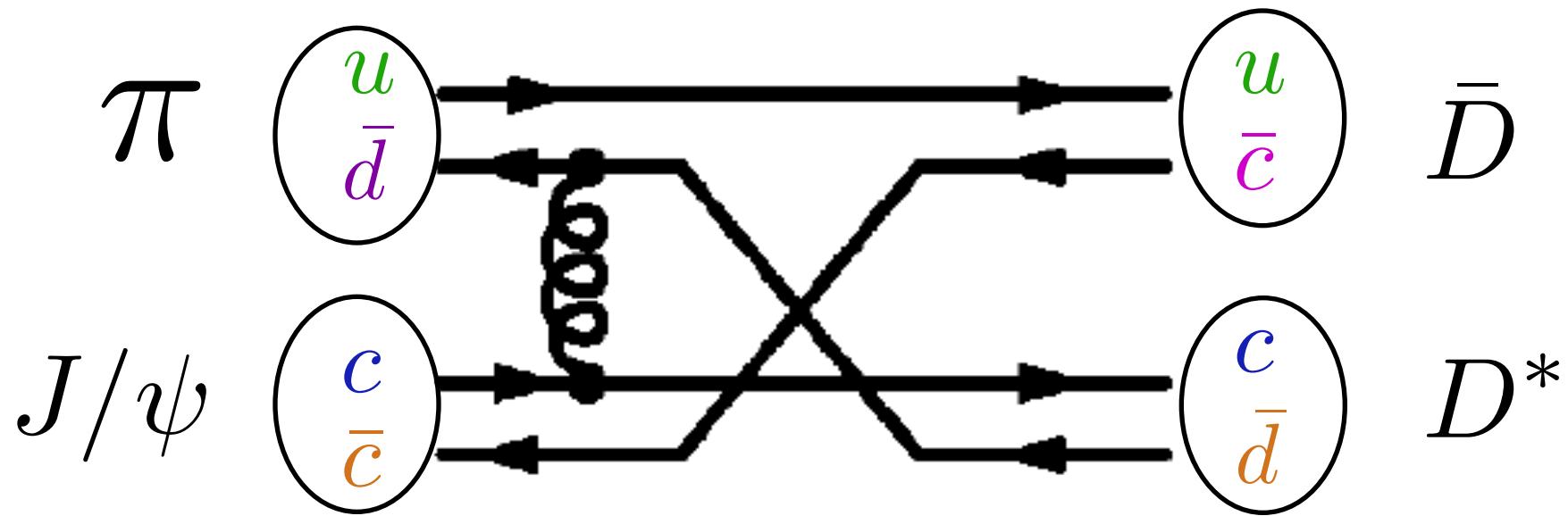
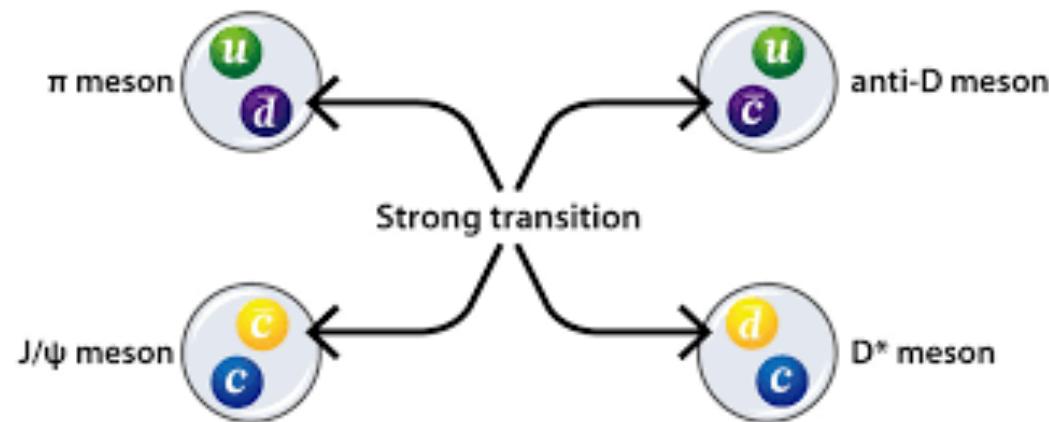


# Upsilon in a hadron gas

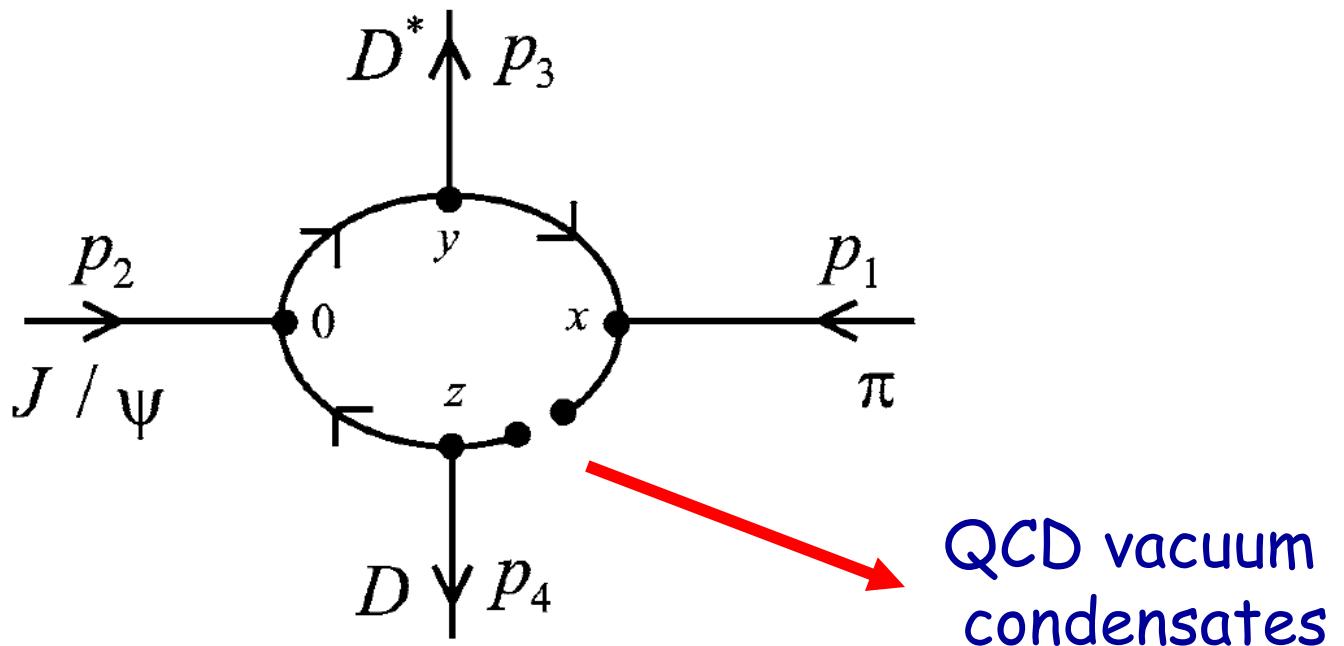


Suppression by a factor 3 in the hadron gas !

# Quark Exchange Models



# QCD Sum Rules



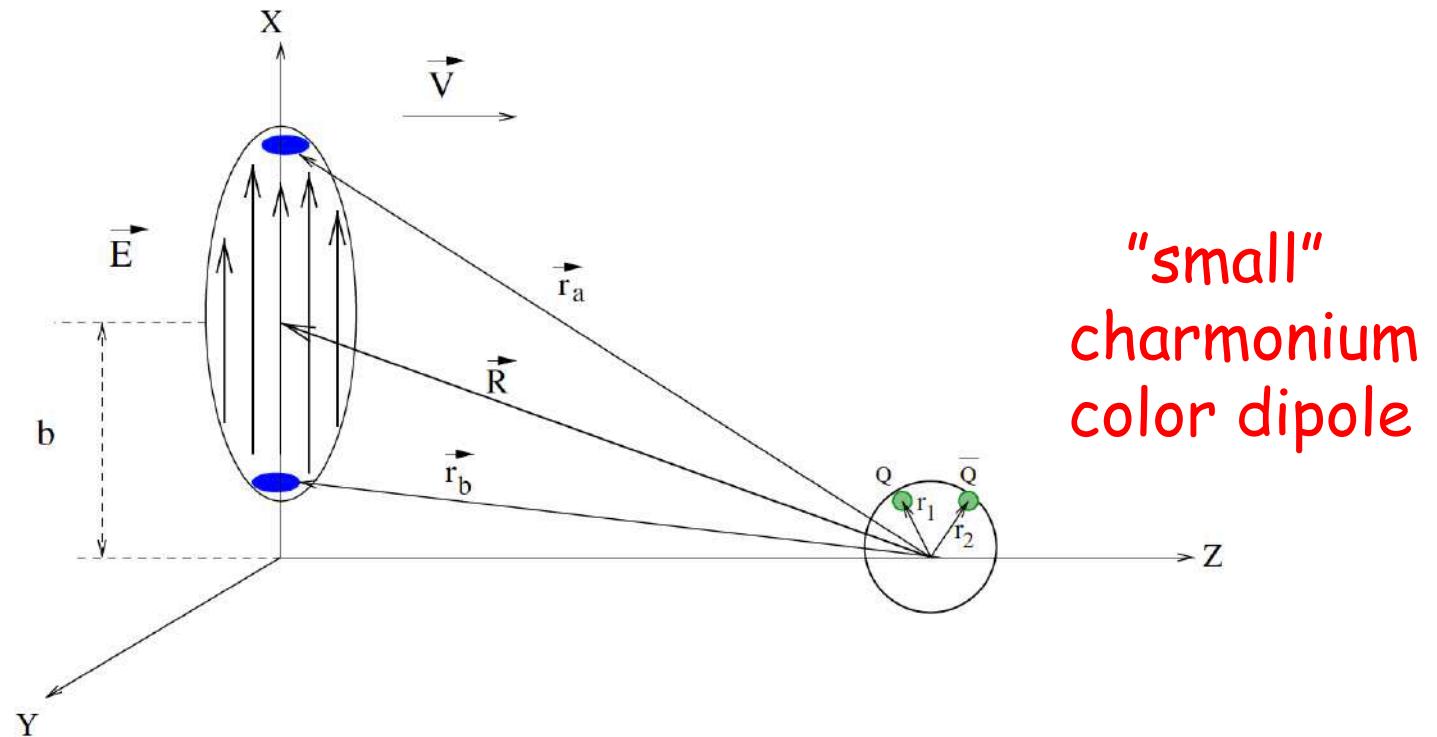
FSN, M. Nielsen, R.S. Marques de Carvalho and G. Krein, Phys. Lett. B (2002)

F.O. Duraes, S.H. Lee, FSN and M. Nielsen, Phys. Lett. B (2003)

F.O. Duraes, H. Kim, S.H. Lee, FSN and M. Nielsen, Phys. Rev. C (2003)

# Semi-classical model: dipole in a color capacitor

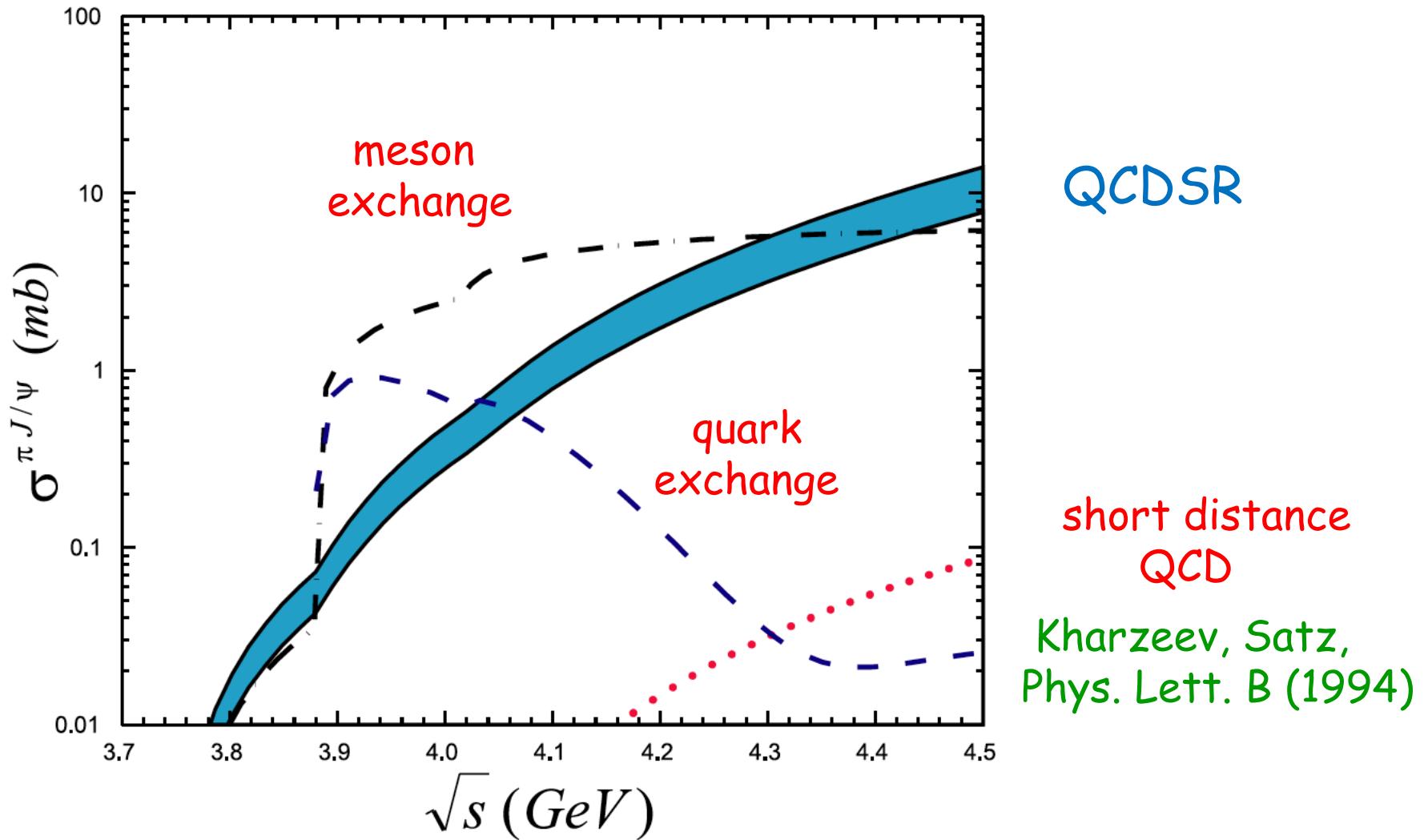
"big" pion  
capacitor



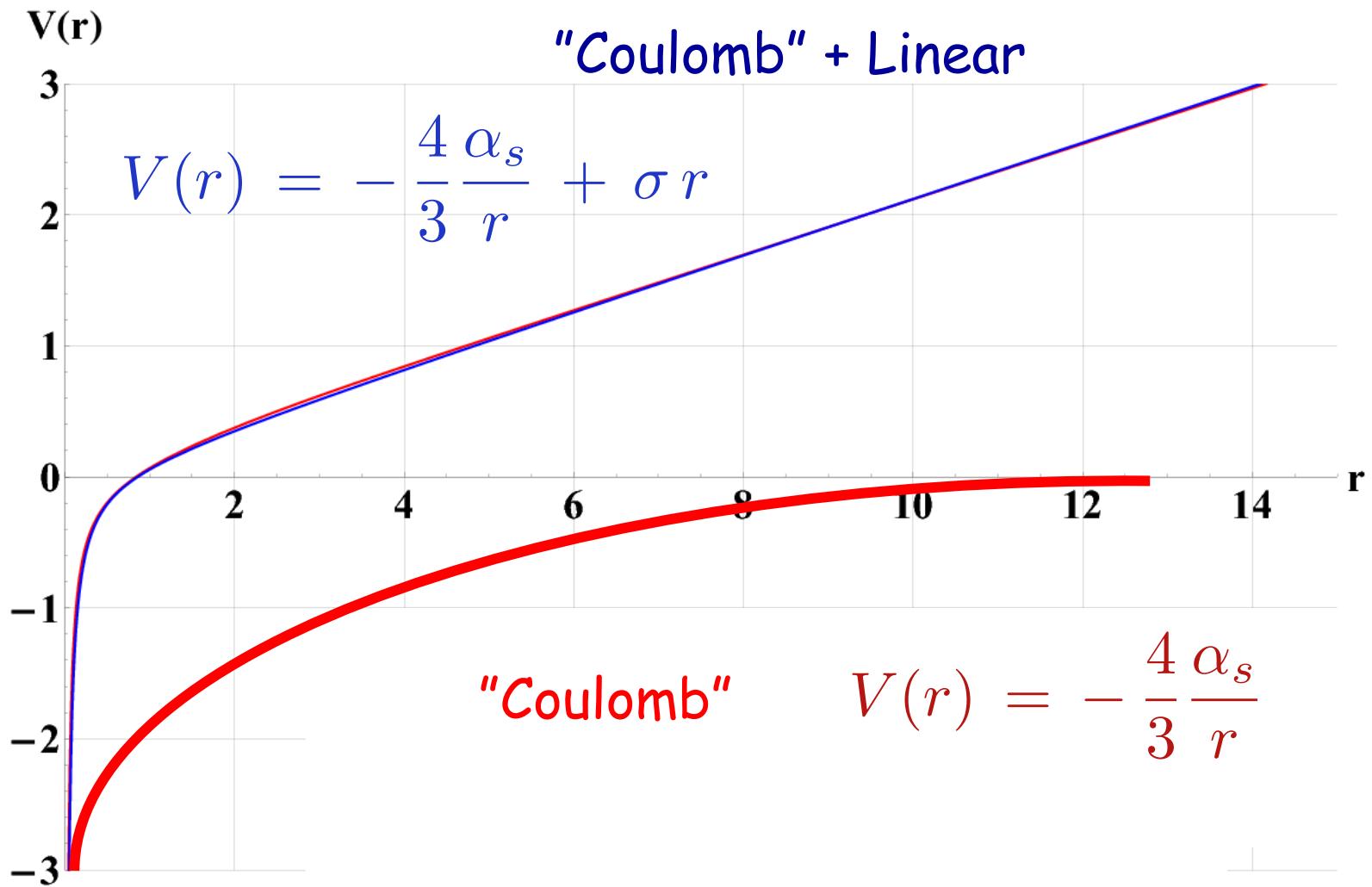
"small"  
charmonium  
color dipole

Kugeratski, FSN, Phys. Rev. C (2005)

# Results



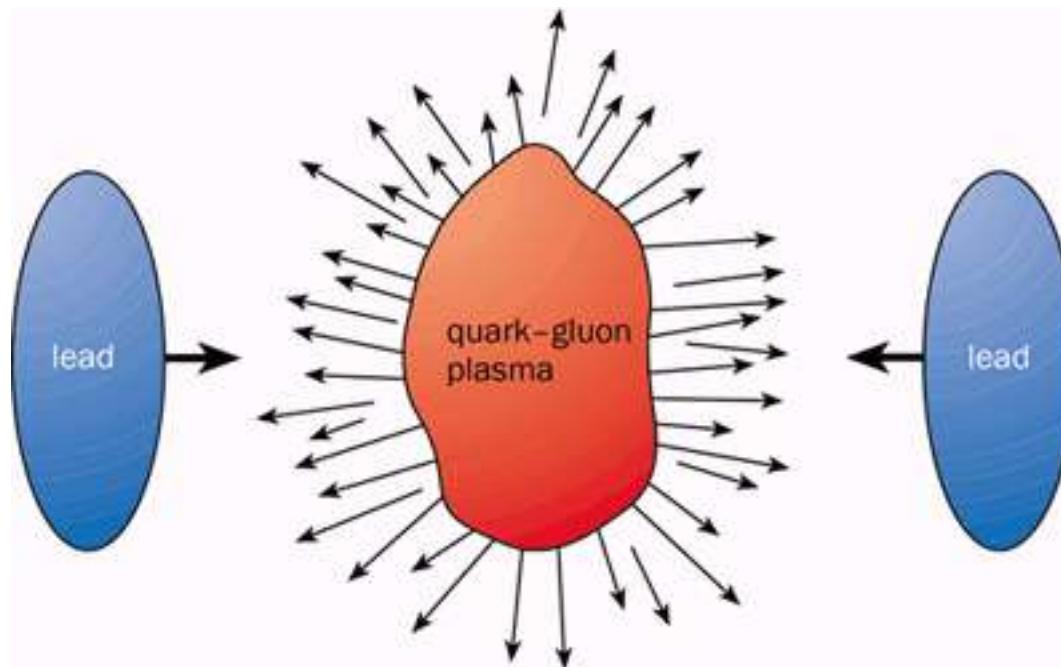
# Confinement: infinite energy to separate quarks



No confinement: they bind but can be separated

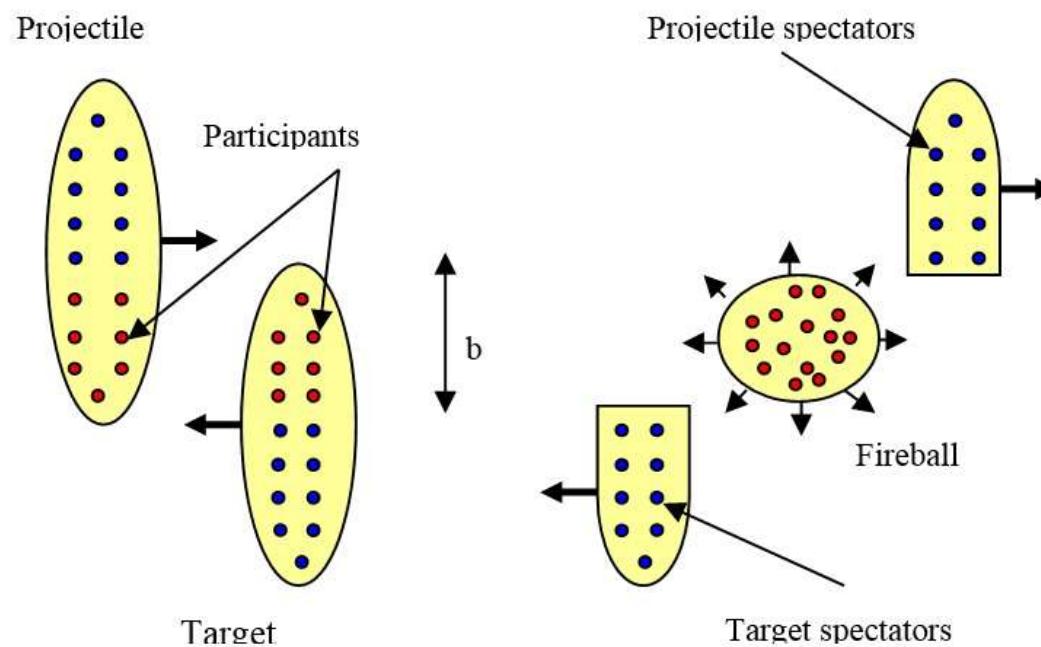
## Central Collisions

More participants  
larger  $N_{\text{part}}$

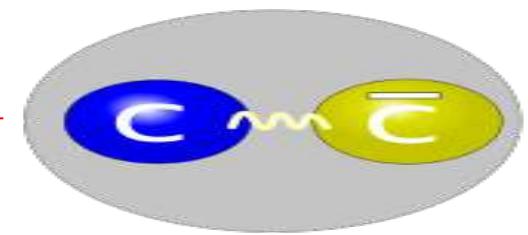
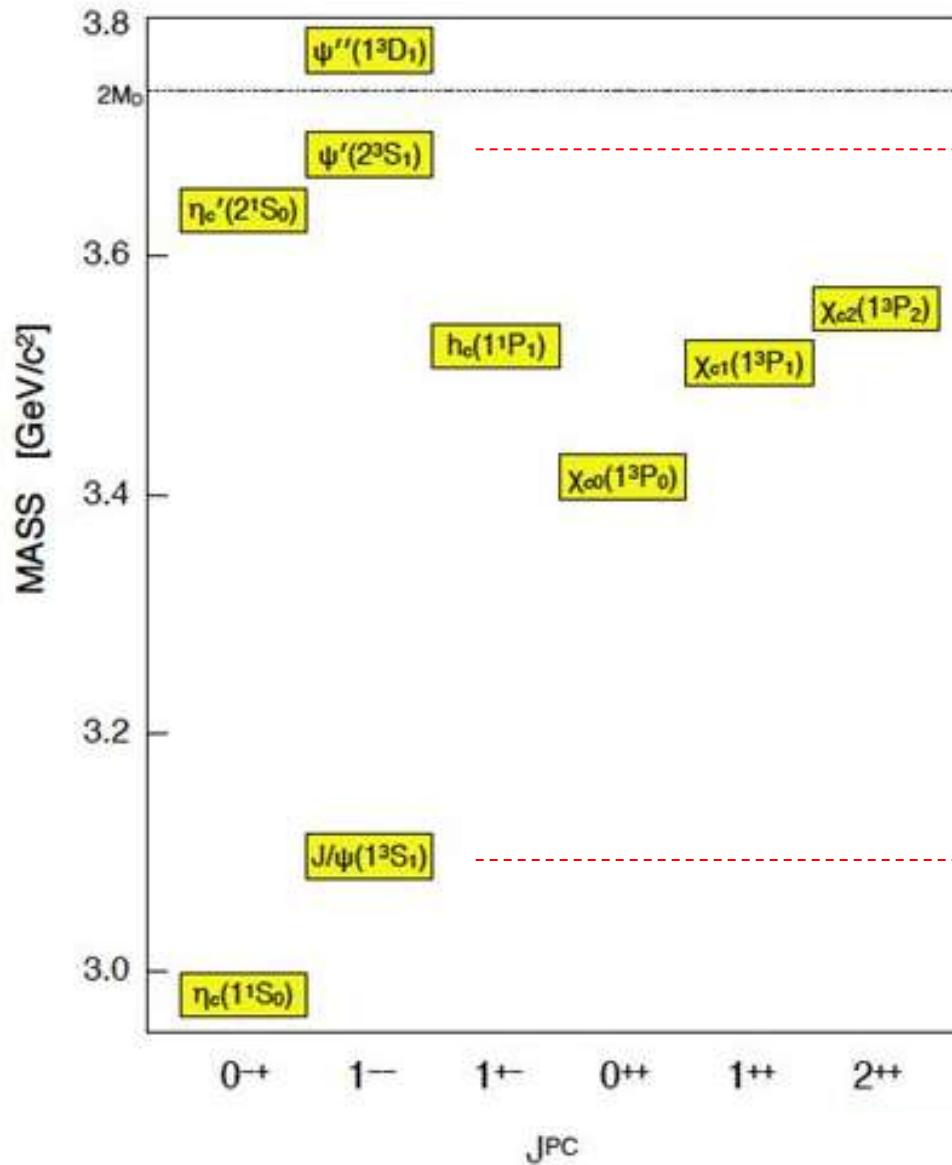


## Noncentral Collisions

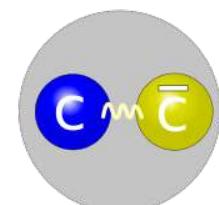
Less participants  
smaller  $N_{\text{part}}$



# Quarkonium spectrum



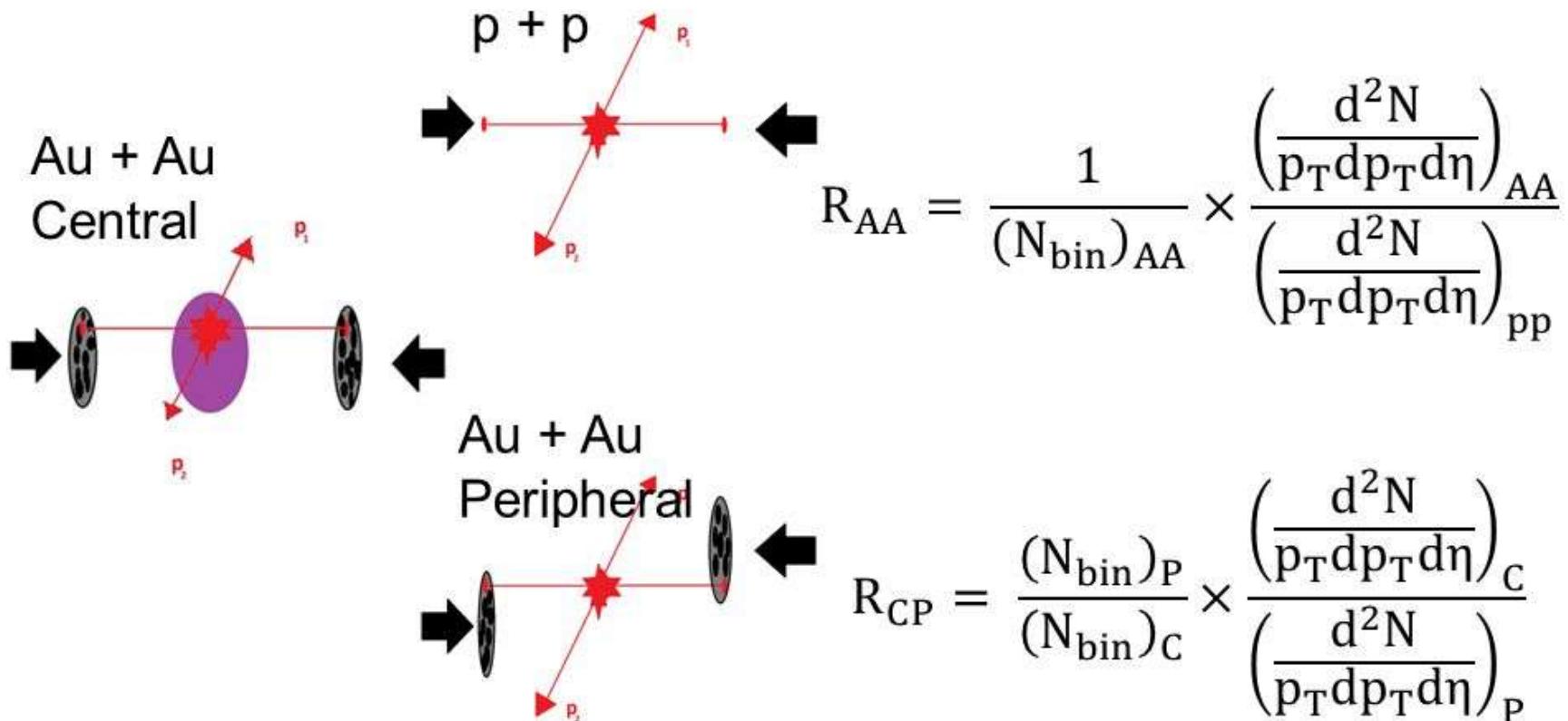
$r_{\psi'}$



$r_\psi$

# Nuclear Modification Factor

hard scatterings produce early high  $p_T$  probes



$N_{bin} \equiv$  number of binary collisions (from Glauber)

# Machines and energy per nucleon-pair

CERN - SPS

$$\sqrt{s} \simeq 20 \text{ GeV}$$

NA38, NA50, NA60

BNL - RHIC

$$\sqrt{s} \simeq 200 \text{ GeV}$$

STAR, PHENIX

CERN - LHC

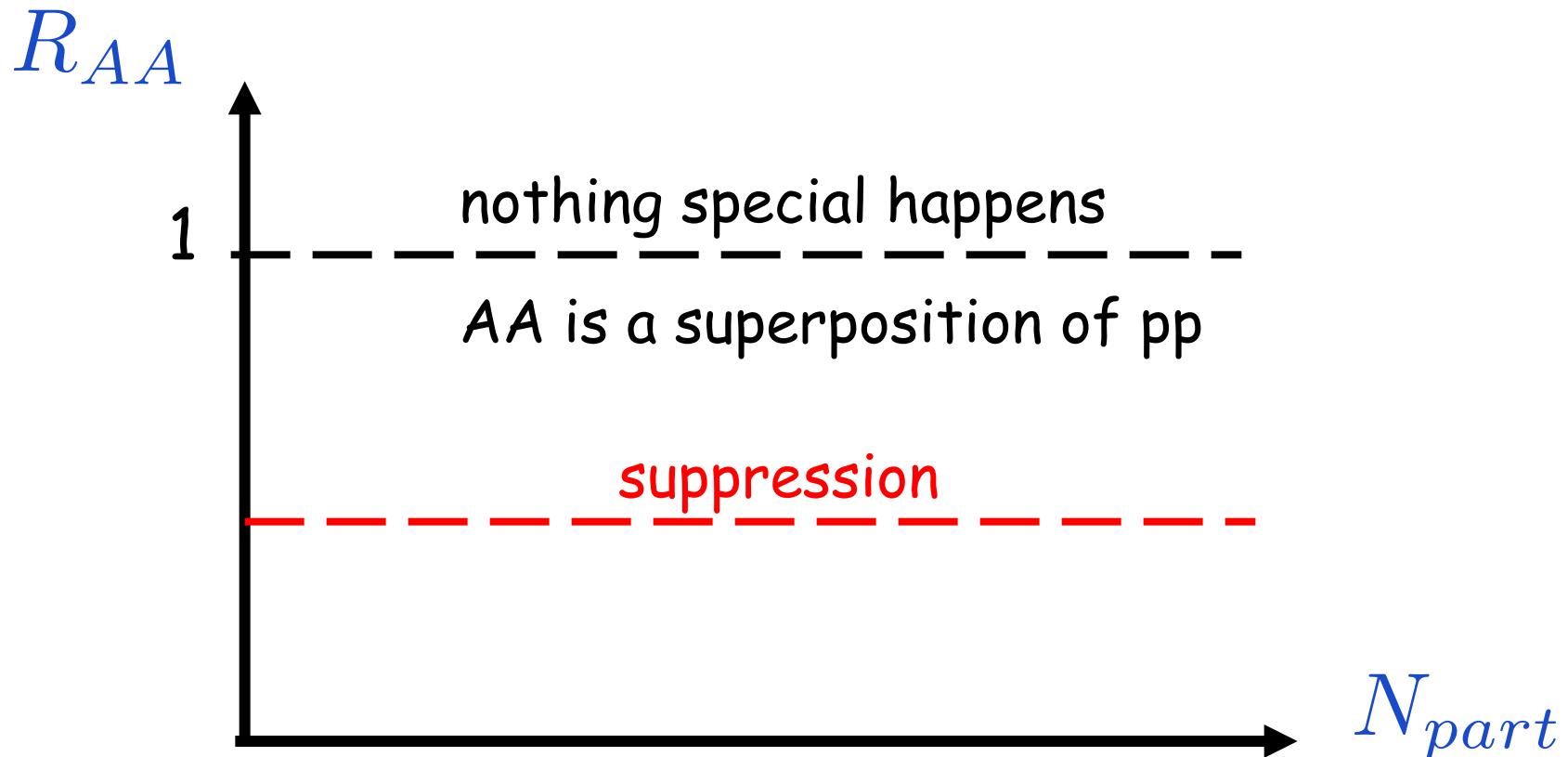
$$\sqrt{s} \simeq 2000 \text{ GeV}$$

ALICE, CMS, ATLAS

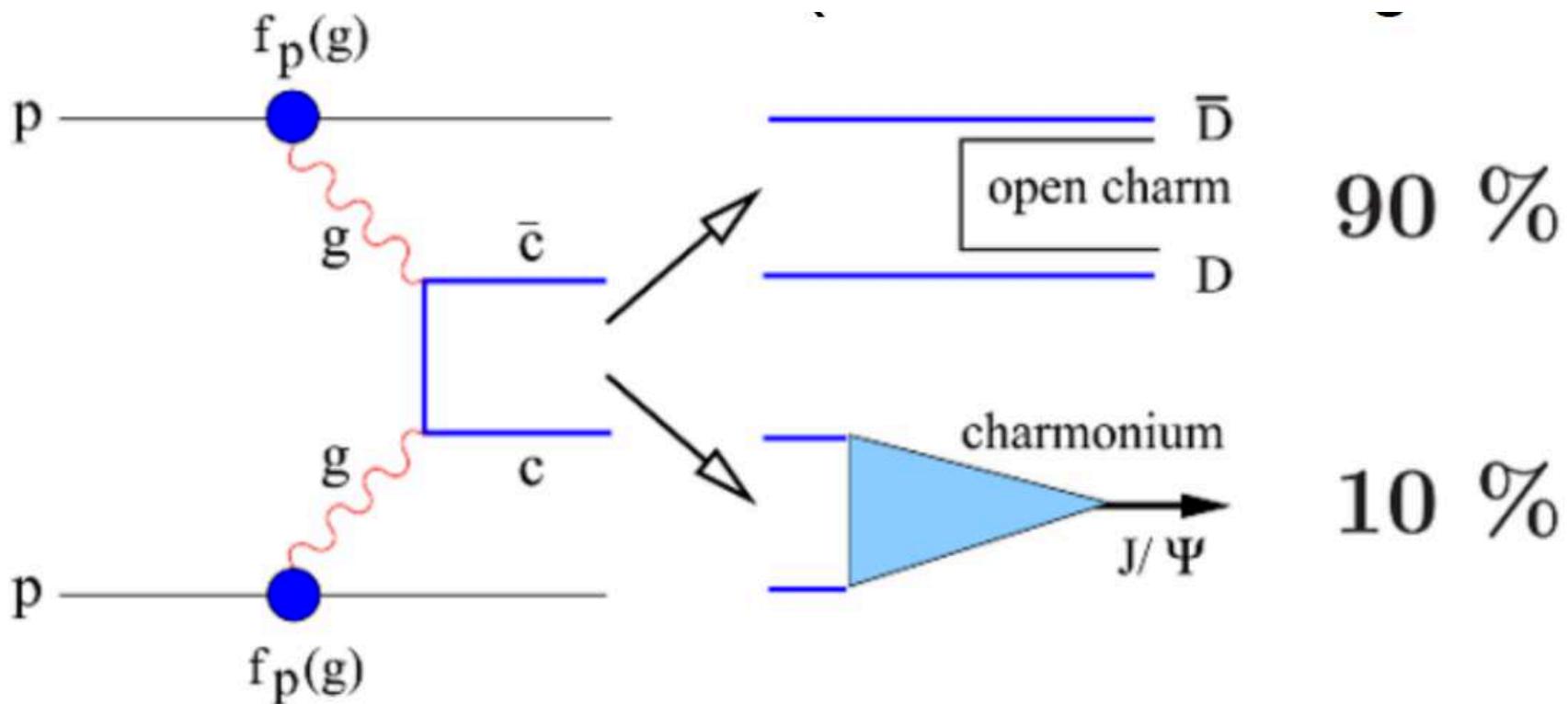
# Data on $R_{AA}$ versus $N_{part}$

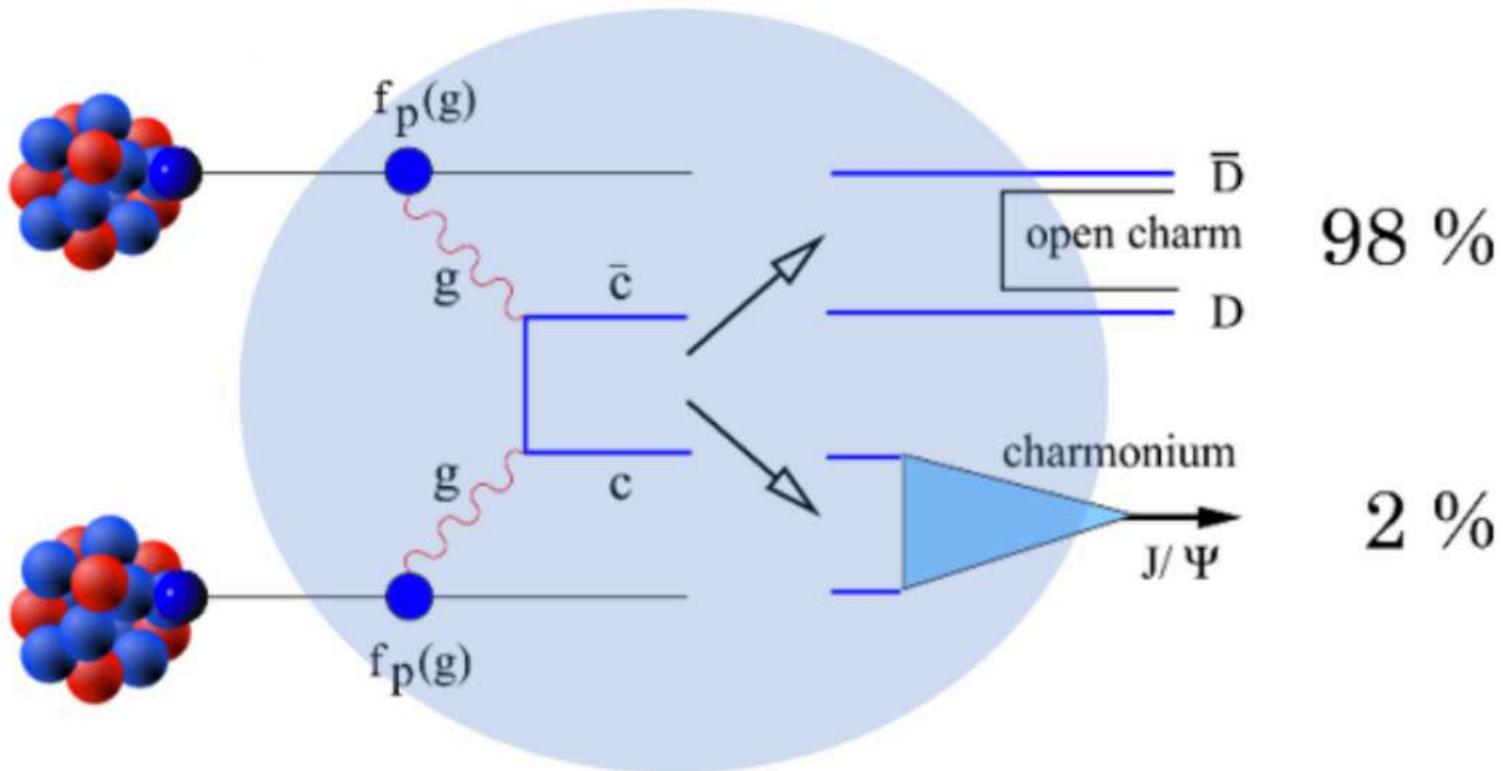
("number" of J/Psi's)

("amount" of QGP)



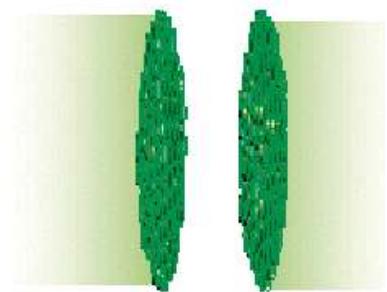
# In calculations



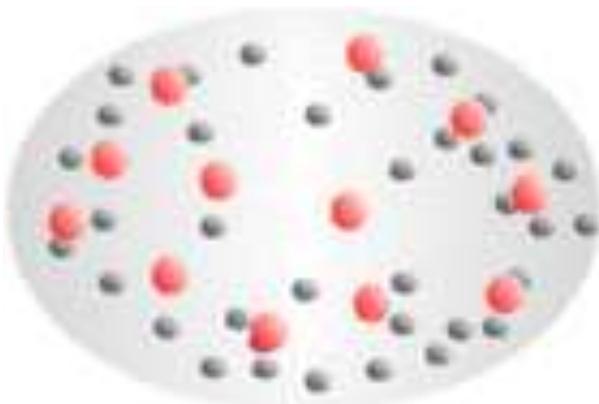


In  $A+A$  color screening reduces charmonia production → reduction of fraction of  $c\bar{c}$  pairs going into charmonia in respect to  $p+p$  at the same energy

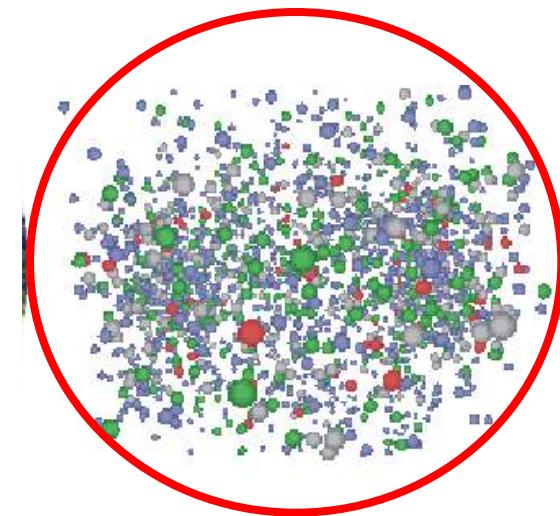
but there may be no  
quark gluon plasma ...



CGC



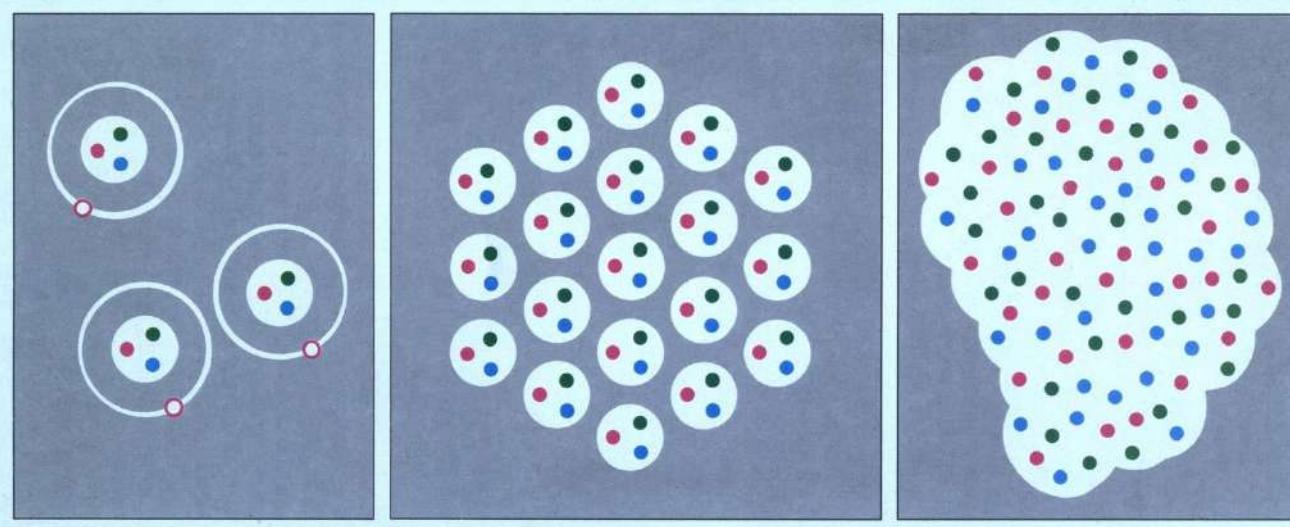
Hotter Hadron Gas



Hadron Gas

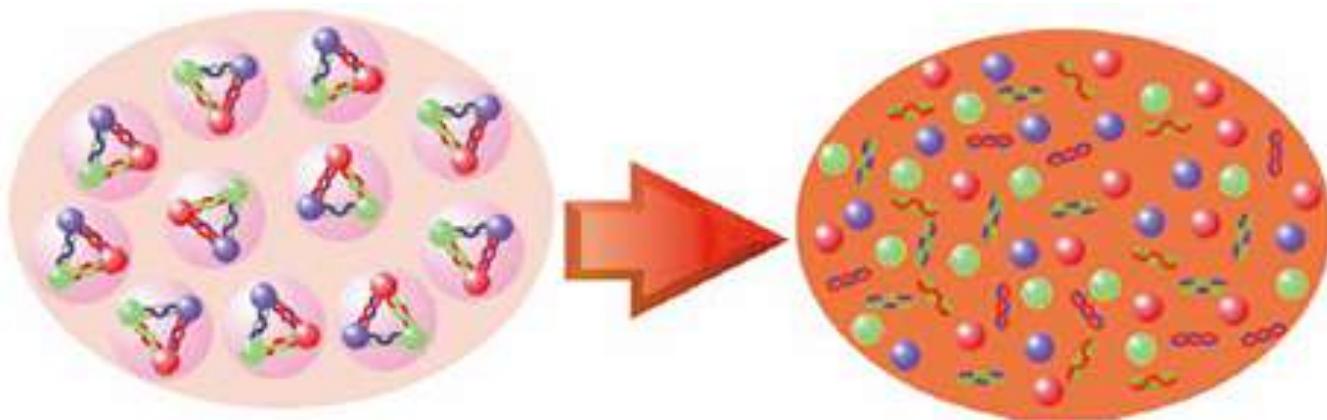
Even without QGP charmonium  
is destroyed in the hadron gas (pions) !

# We can compress matter and create a quark gluon plasma !



$T = 0$

Quarks are free  
to move everywhere



通常の核物質  
クォークが核子に閉じ込められている。

QGPの状態  
閉じ込めが破れてクォークとグルーオンが動き回っている。

$T > T_c$

Best explanation: "cocktail" with

-suppression of the primordial Psi's

and

-regeneration in the QGP

# Enhanced $J/\psi$ production in deconfined quark matter

Robert L. Thews, Martin Schroedter, and Johann Rafelski

*Department of Physics, University of Arizona, Tucson, Arizona 85721*

(Received 29 August 2000; published 23 April 2001)

Phys. Rev. C (2001)

(Non)thermal aspects of charmonium production  
and a new look at  $J/\psi$  suppression  $\star$

P. Braun-Munzinger<sup>a</sup>, J. Stachel<sup>b</sup>

Phys.. Lett. B (2000)

<sup>a</sup> *Gesellschaft für Schwerionenforschung, D 64291 Darmstadt, Germany*

<sup>b</sup> *Physikalisches Institut der Universität Heidelberg, D 69120 Heidelberg, Germany*

Received 26 July 2000; accepted 17 August 2000

Editor: J.-P. Blaizot

Thermal versus direct  $J/\Psi$  production in ultrarelativistic  
heavy-ion collisions

L. Grandchamp<sup>a,b</sup>, R. Rapp<sup>a</sup>

Phys. Lett. B (2001)

<sup>a</sup> *Department of Physics and Astronomy, State University of New York, Stony Brook, NY 11794-3800, USA*

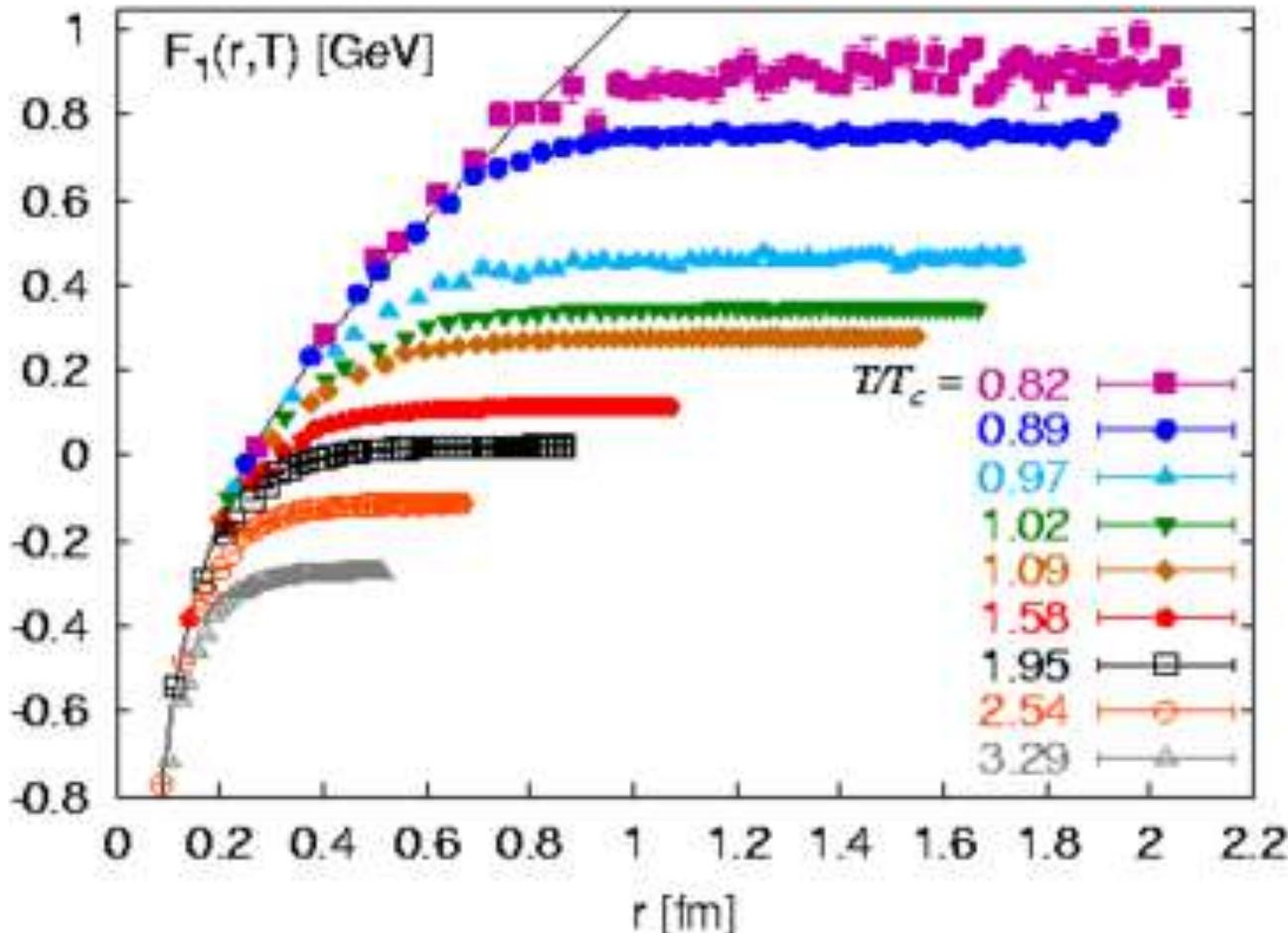
<sup>b</sup> *IPN Lyon, IN2P3-CNRS et UCBL, 43 Bd. du 11 Novembre 1918, 69622 Villeurbanne Cedex, France*

Received 29 March 2001; received in revised form 19 June 2001; accepted 15 October 2001

Editor: J.-P. Blaizot

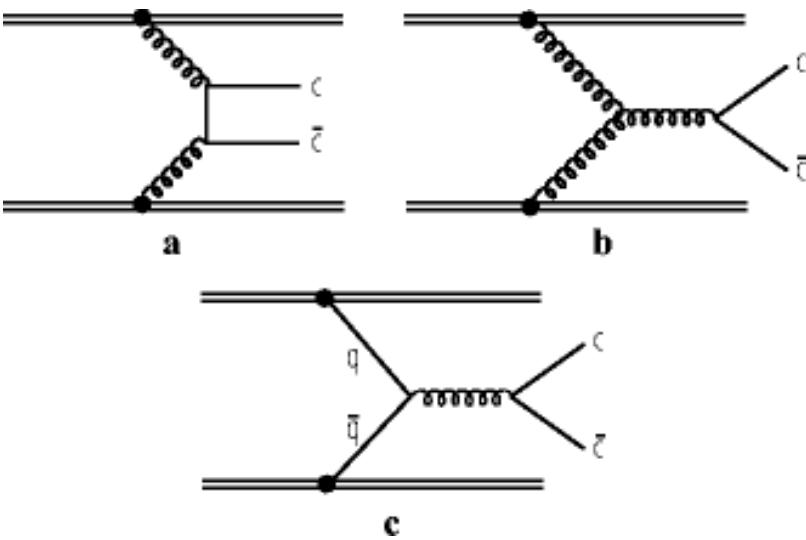
# In a thermal bath

## Deconfinement: quarks can be free

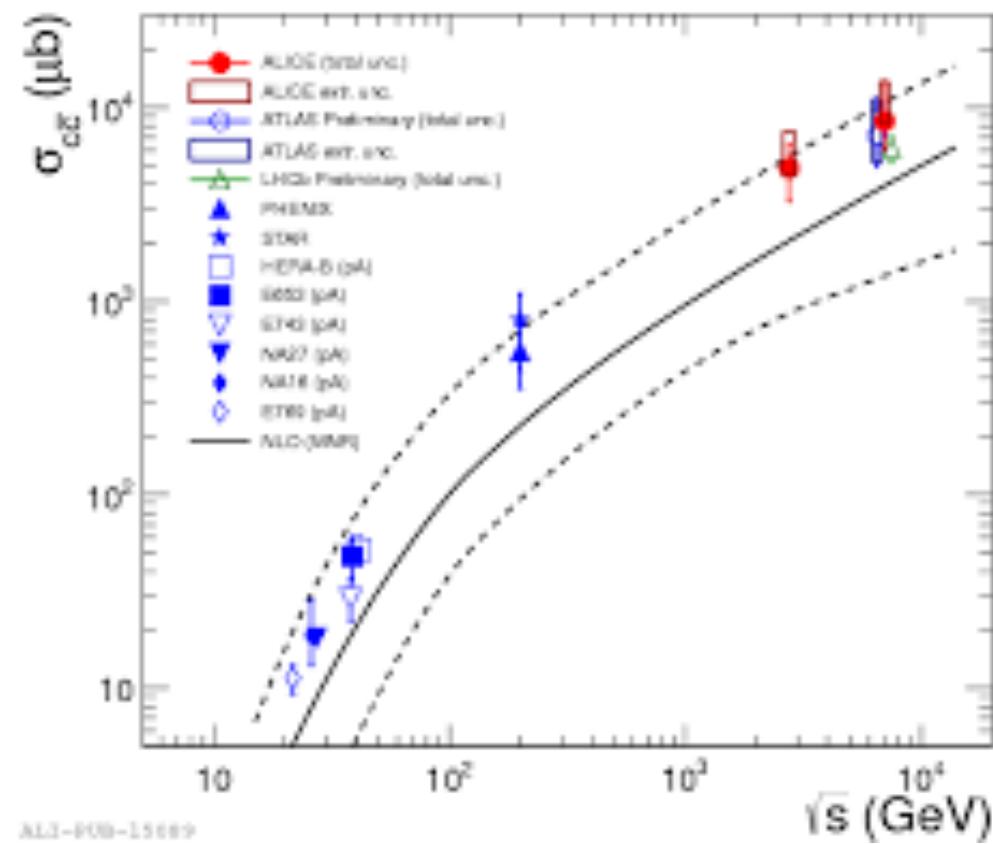


A real  
calculation in  
Lattice QCD

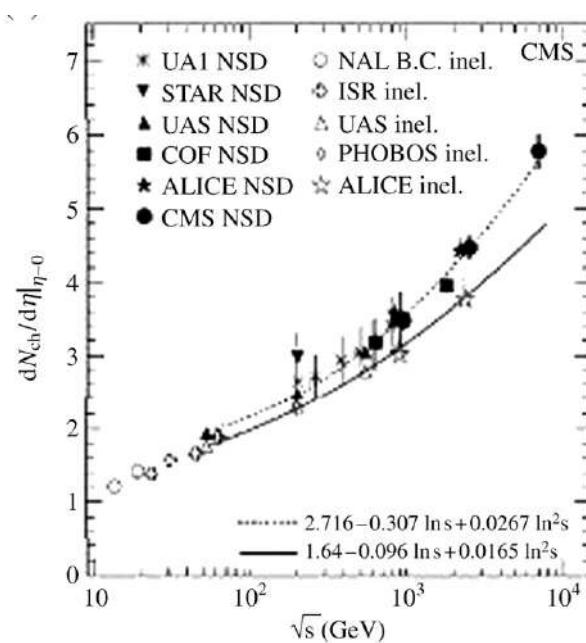
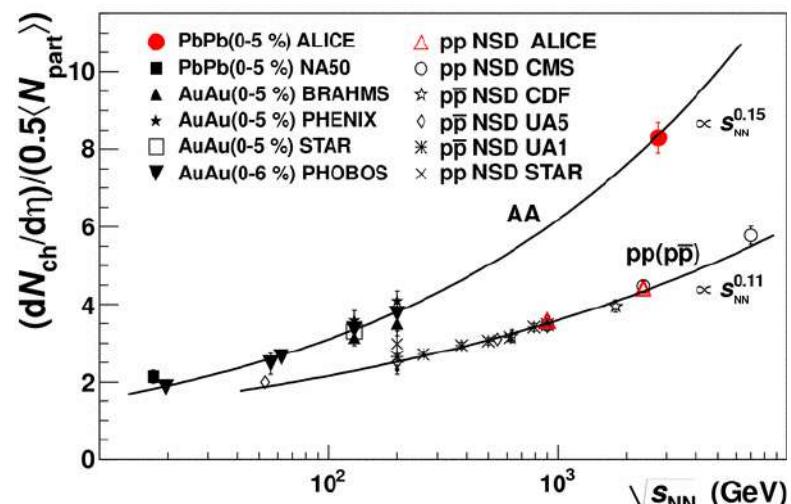
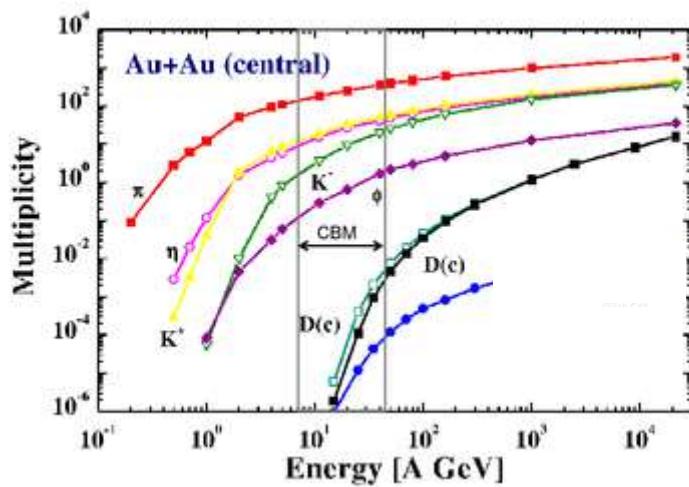
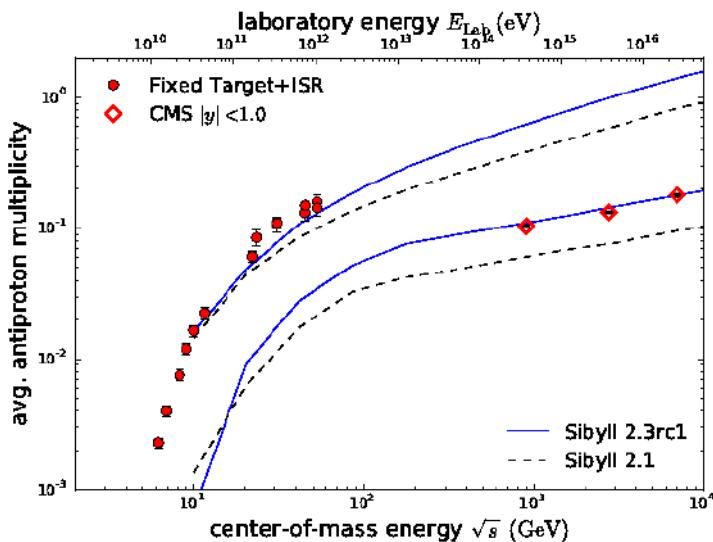
# Charmonium production in proton-proton collisions



Higher energies  
more charmonium !



# In general: more energy, more particles



# Sequential melting

Screening length  $\lambda_D$  vs.  $T$ :

