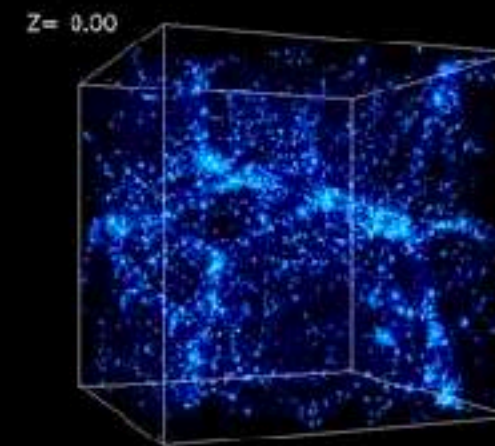
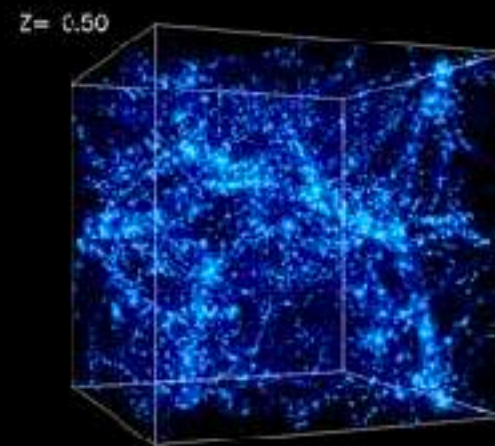
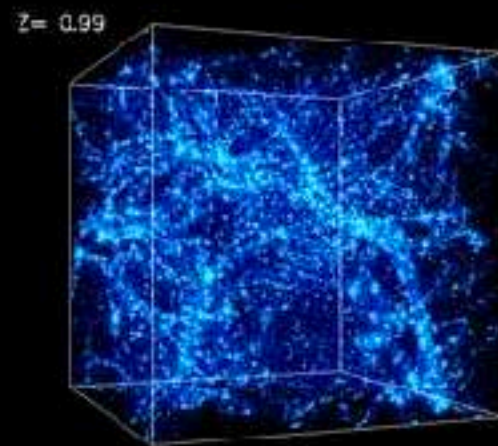
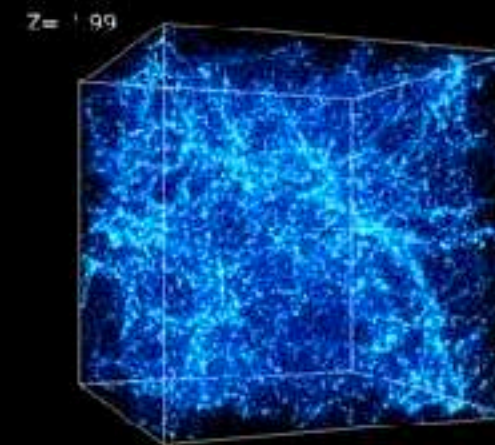
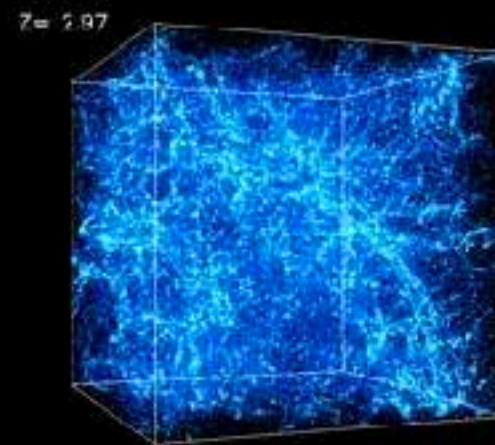
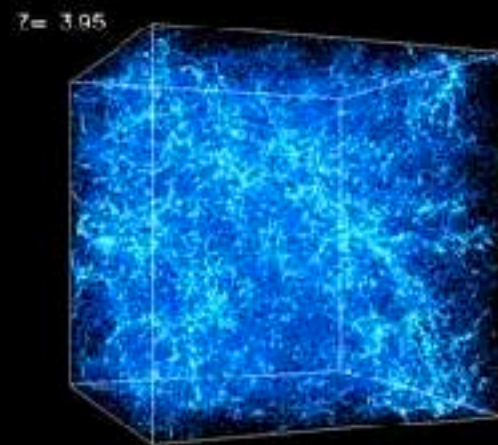
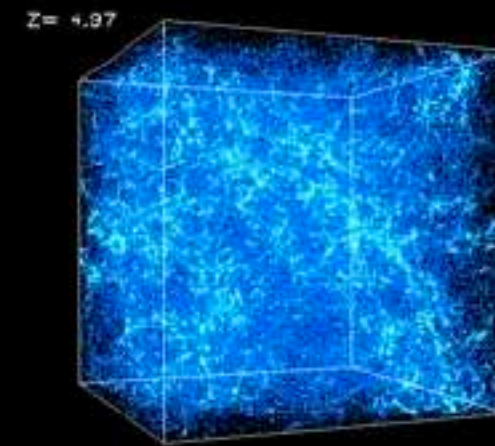
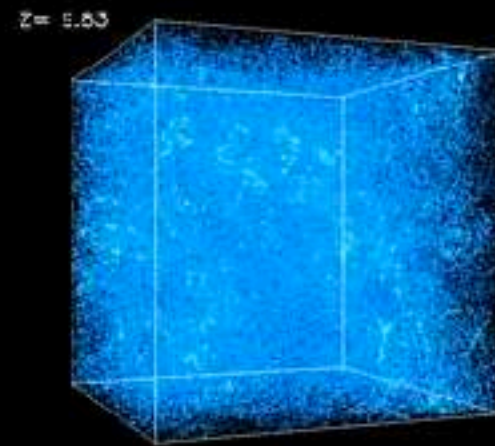
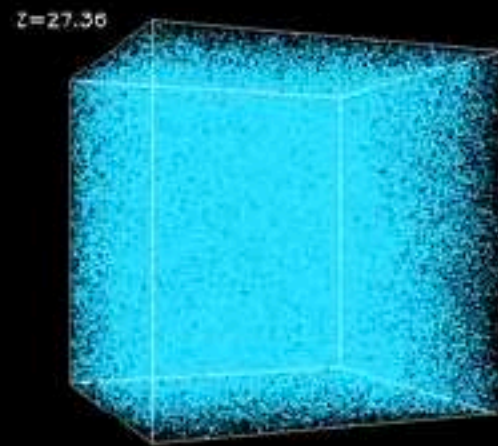
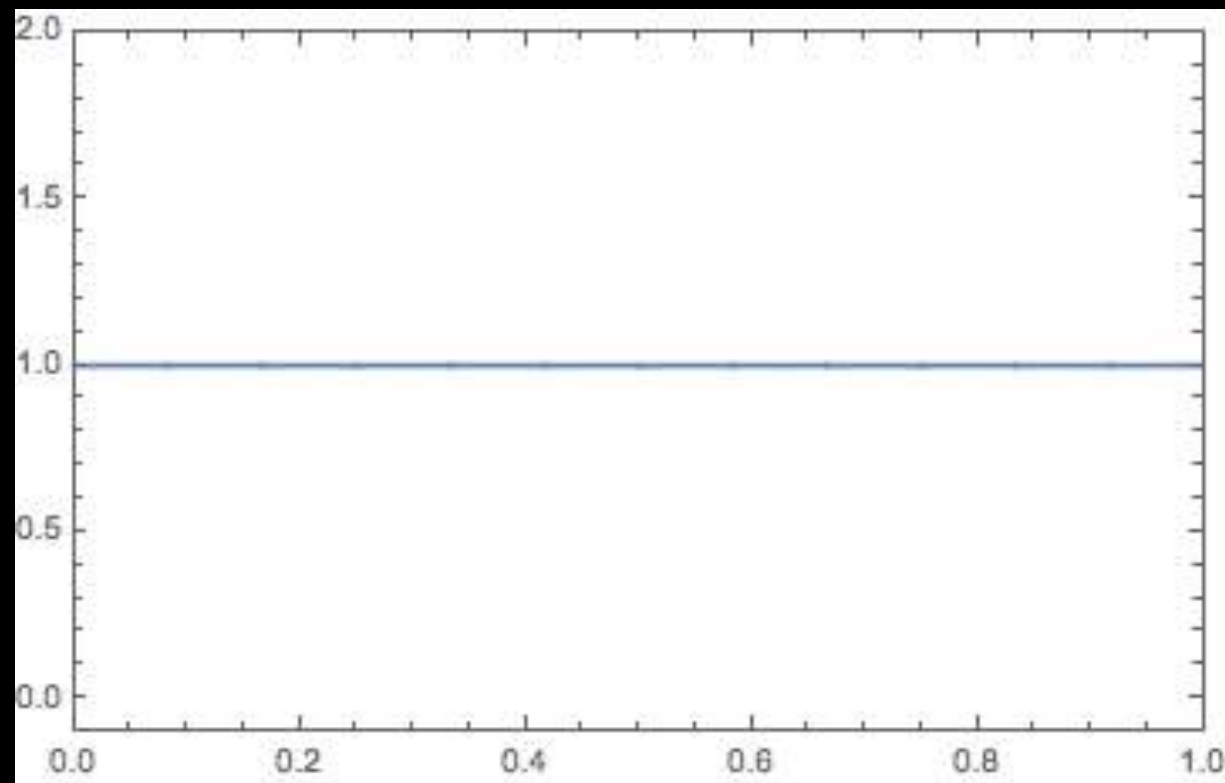


# THE VISIBLE AND THE INVISIBLE WEBS

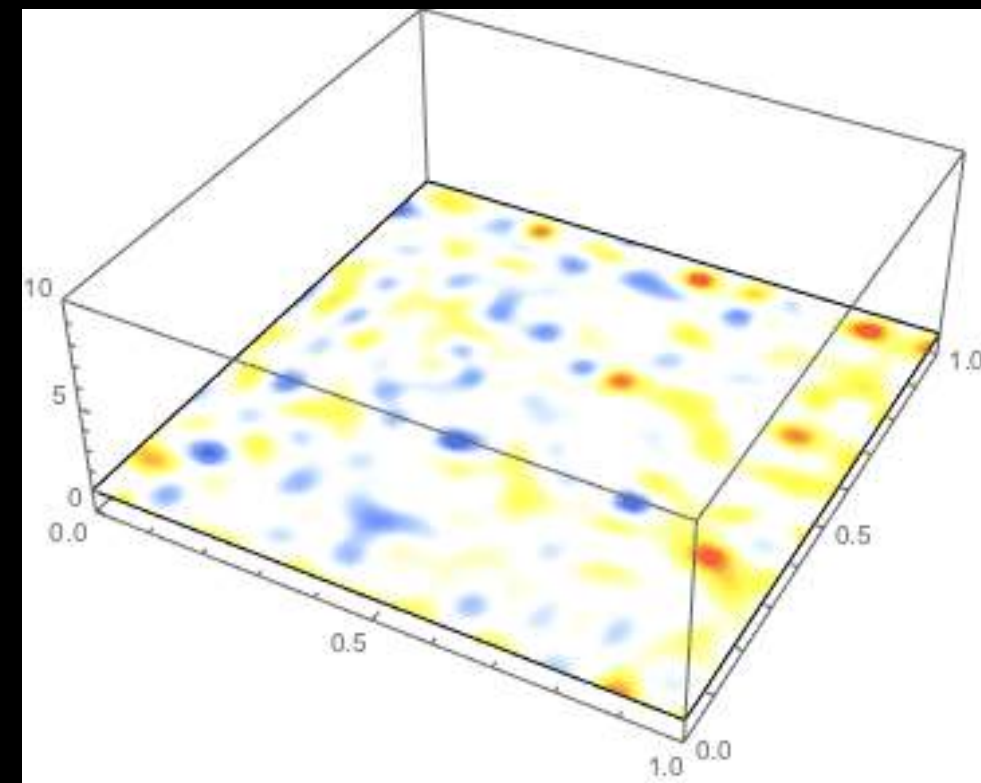


# THE VISIBLE AND THE INVISIBLE WEBS

1D



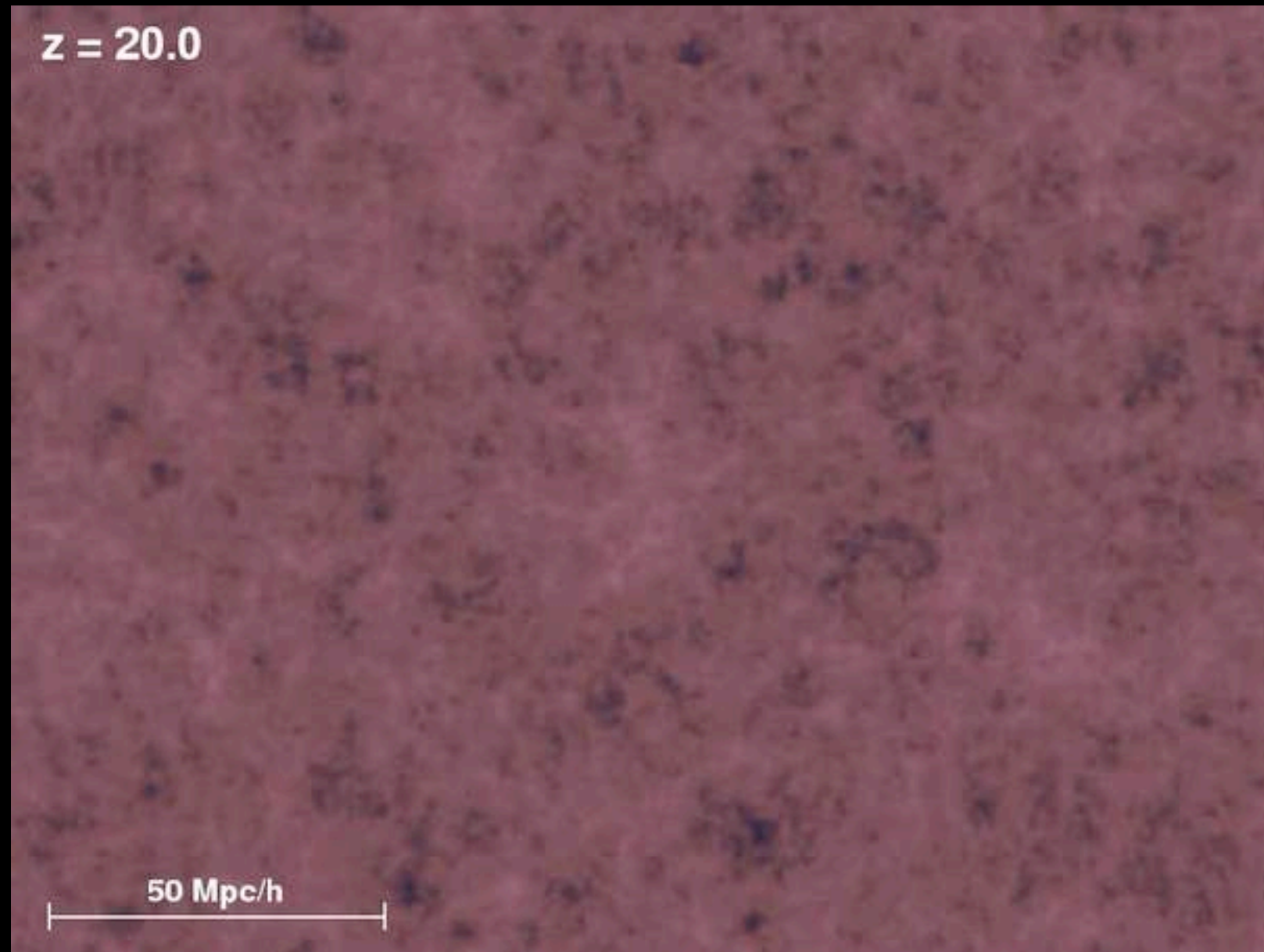
2D



Initially, density fluctuations are very small ( $\delta\rho/\rho \sim 10^{-4}$ ), and in this linear regime, structure formation proceeds at a moderate pace

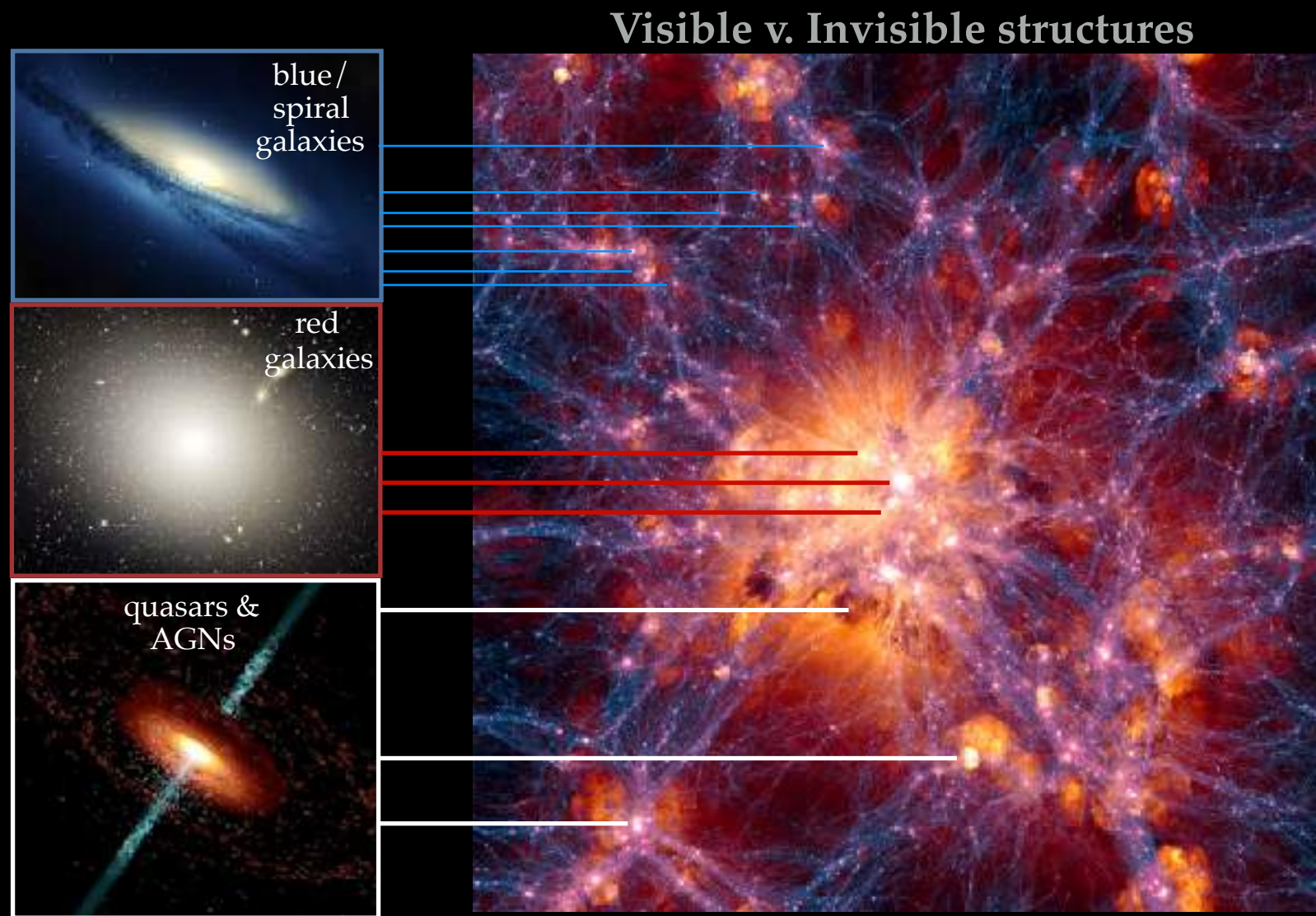


# THE VISIBLE AND THE INVISIBLE WEBS



However, soon the linear regime fails to describe the growing concentration of matter in the initially overdense regions. Gravity is a relentless force *driving inequality* in the Universe.

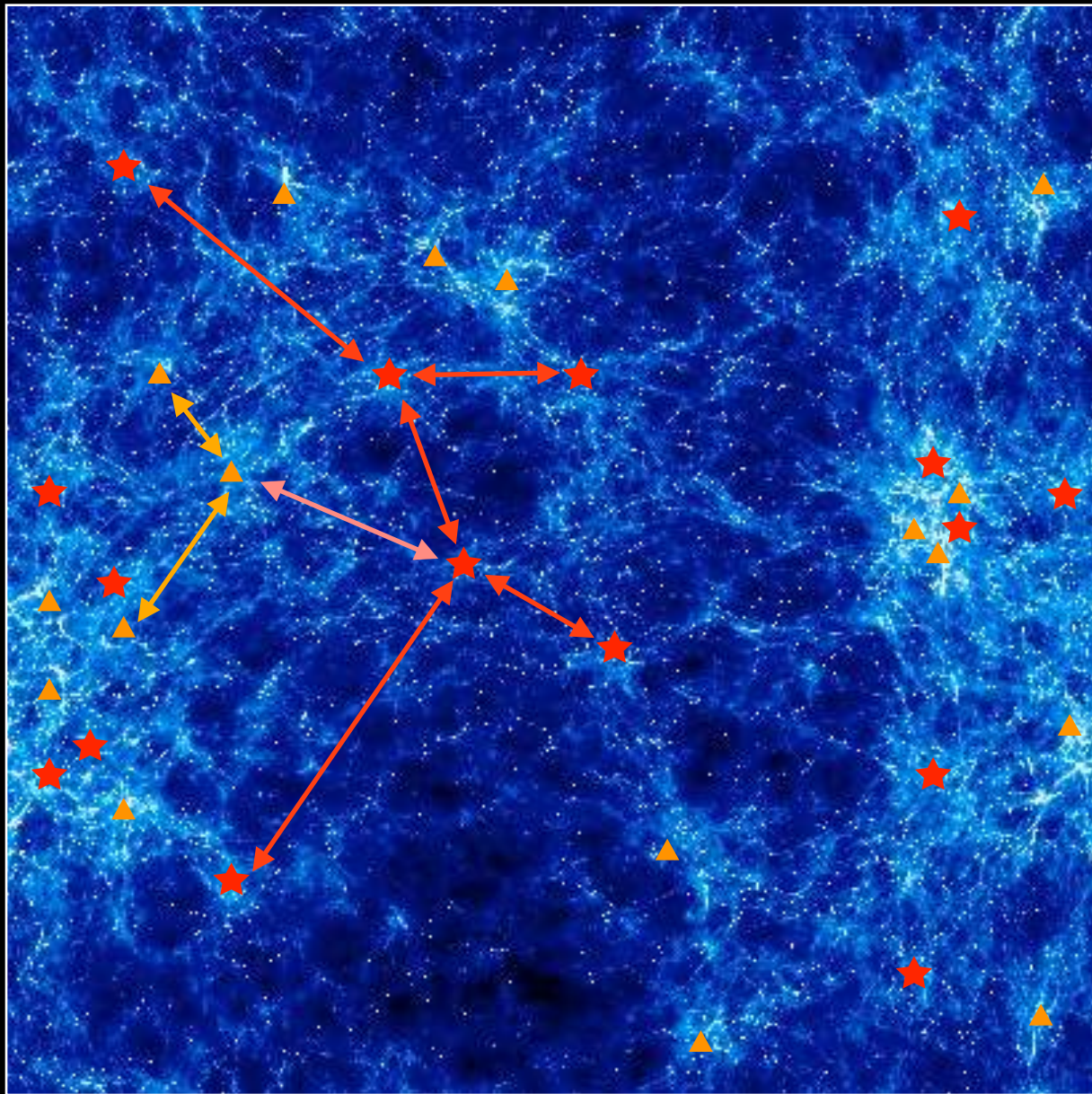
# THE VISIBLE AND THE INVISIBLE WEBS



Dark matter is 5-6x more abundant than baryonic matter, therefore it often determines the gravitational wells where we also find luminous baryons— galaxies of all kinds, quasars, gas clouds, etc.



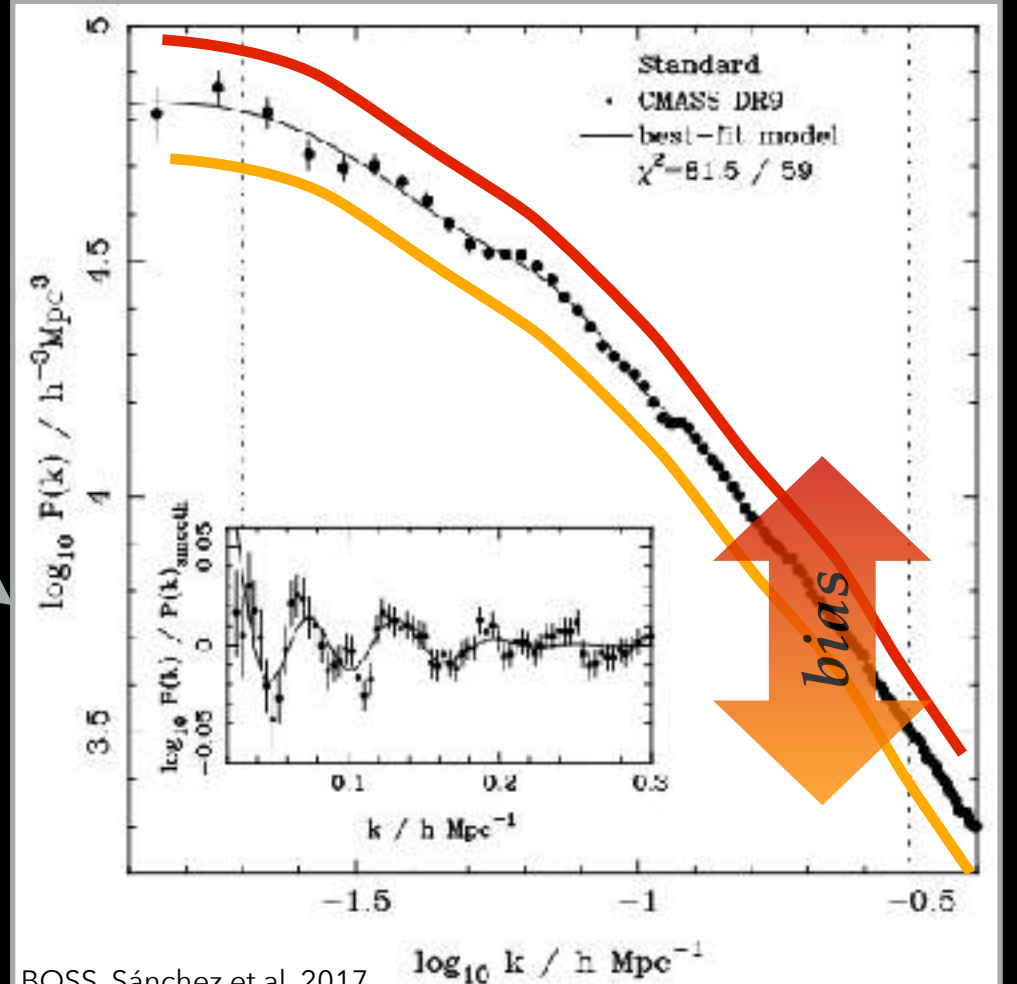
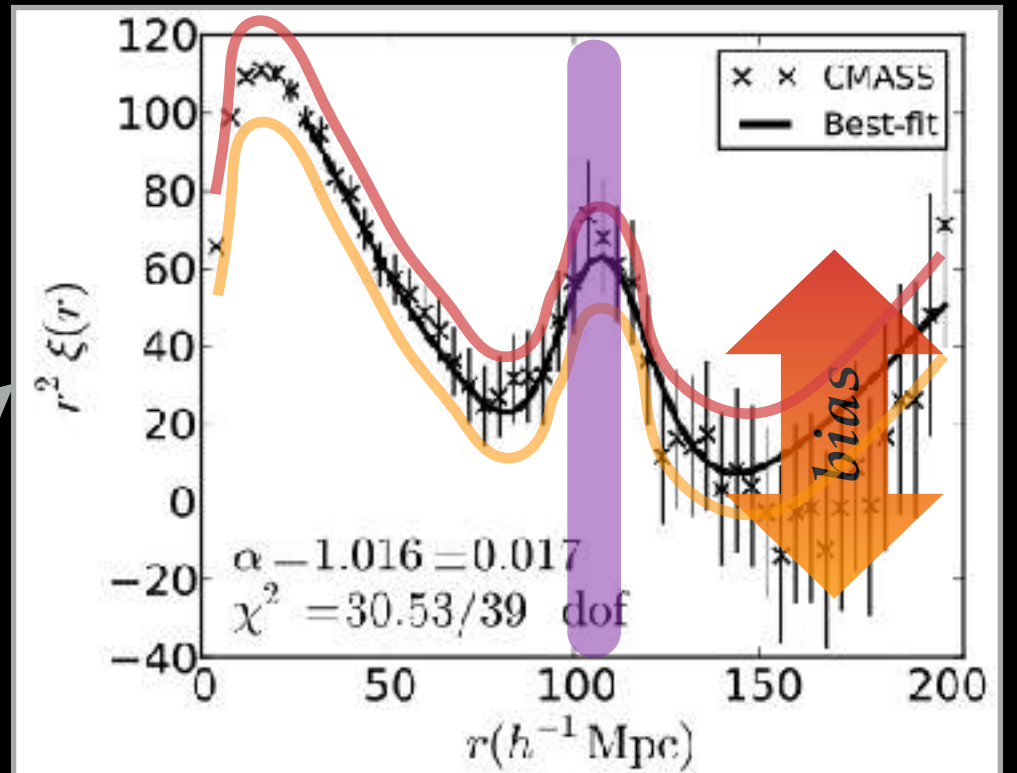
# THE CLUSTERING OF MATTER



Clustering  
in position  
space

Clustering  
in Fourier  
space

Galaxies serve as *tracers* of the dense regions of the Universe, where we find more matter. Although their *absolute* positions are irrelevant, their *relative positions* tells us about *clustering*

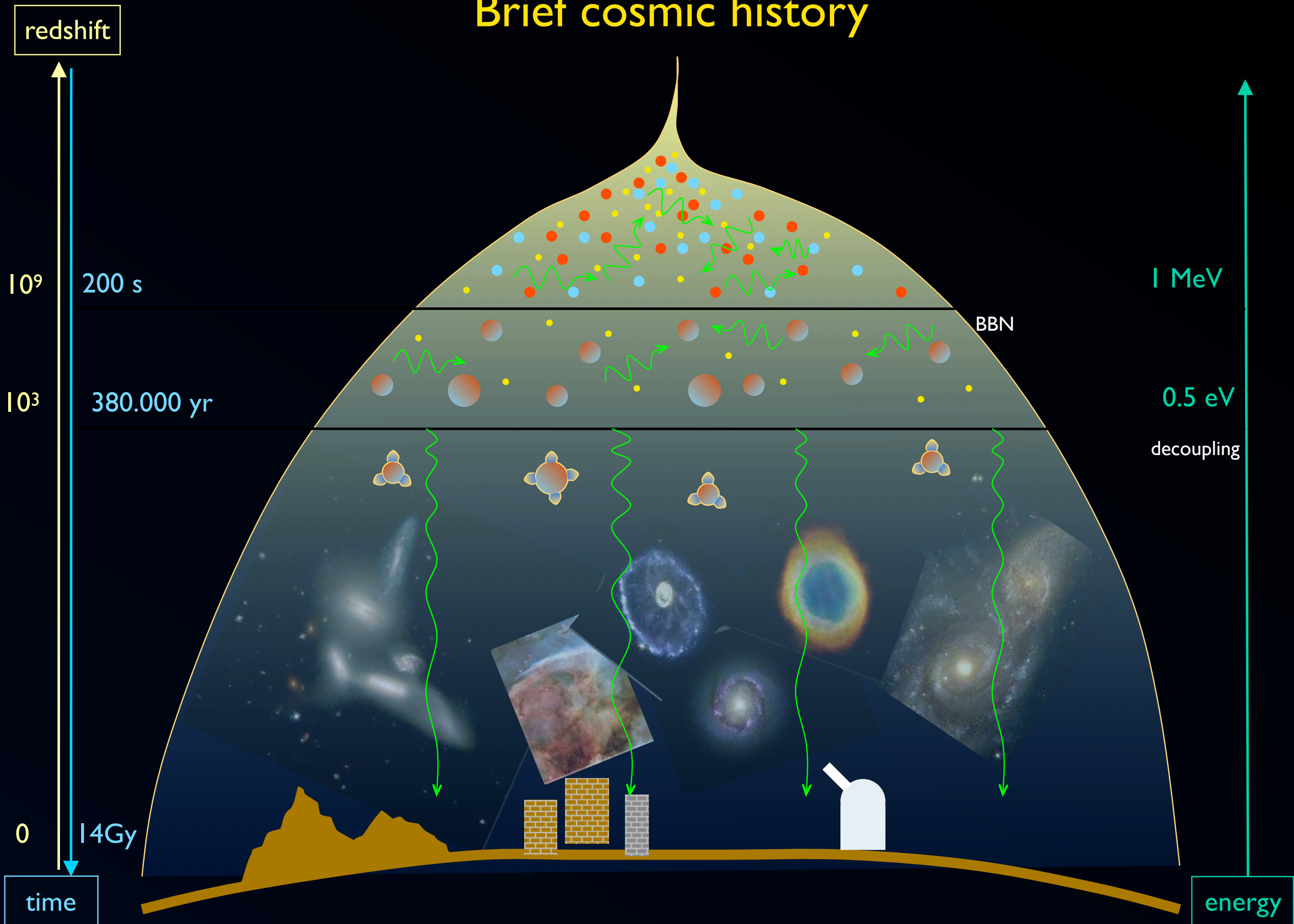


To the blackboard!

Brief review of  
Cosmic Microwave Background Radiation  
and  
Baryon Acoustic Oscillations



# Brief cosmic history

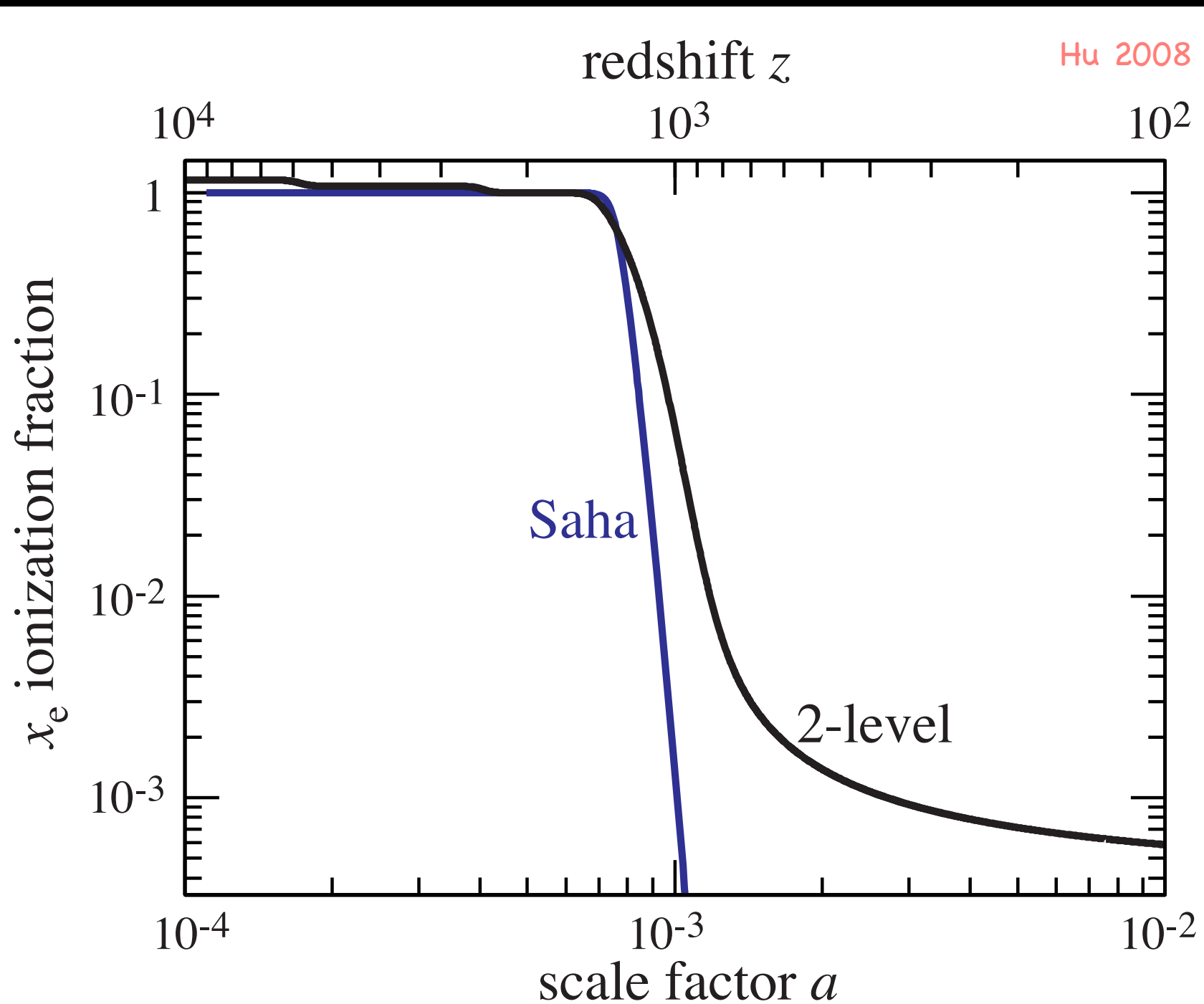




# Recombination: the Saha equation and full recombination

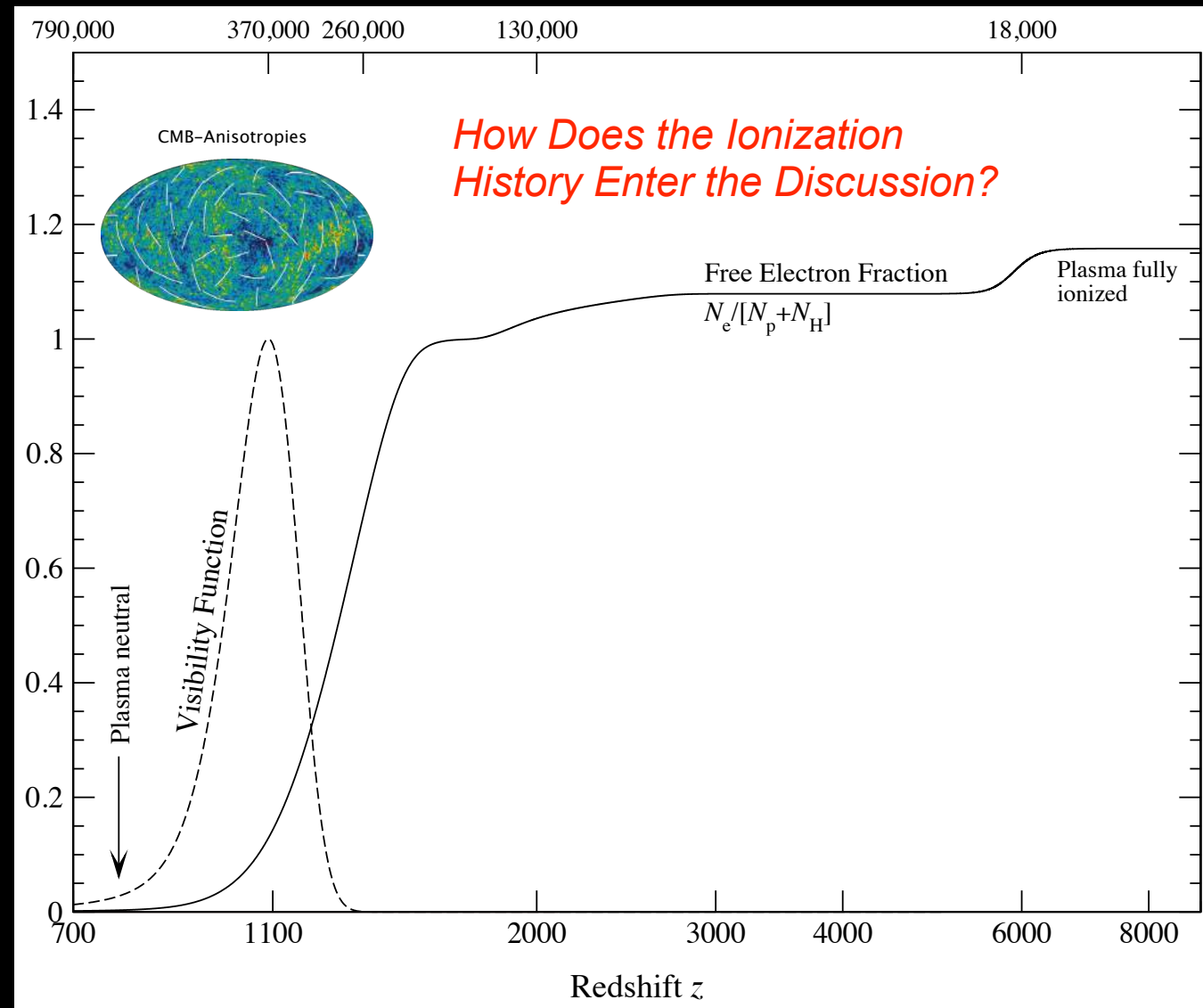
Number of free (ionized) electrons and ionized fraction::

$$n_e = (1 - Y)X_e n_b = x_e \times 1.12 \times 10^{-5} \Omega_b h^2 (1 + z)^3 \text{cm}^{-3}$$



This probability per unit length that a photon is scattered by some time  $t$ , but not afterwards, is called the **visibility function**:

$$g(\eta) = \mu'(\eta)e^{-\mu(\eta)} = \sigma_T X_e(\eta)n_b(\eta)a(\eta) \times \exp \left[ \int_0^\eta d\eta' \sigma_T X_e(\eta')n_b(\eta')a(\eta') \right]$$

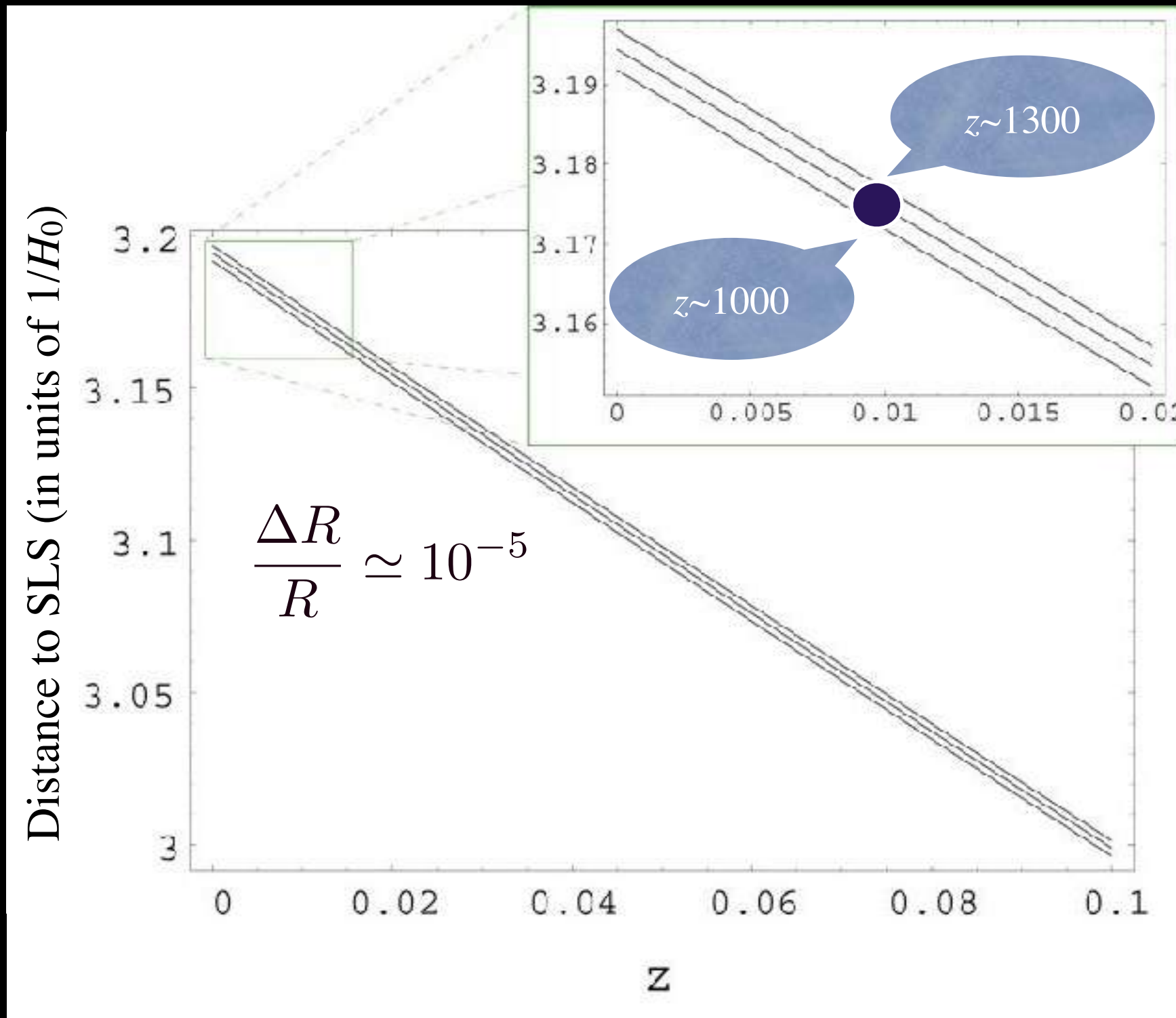


Peak probability:

$$z_* \approx 1089 \left( \frac{\Omega_m h^2}{0.14} \right)^{0.0105} \left( \frac{\Omega_b h^2}{0.024} \right)^{-0.028}$$

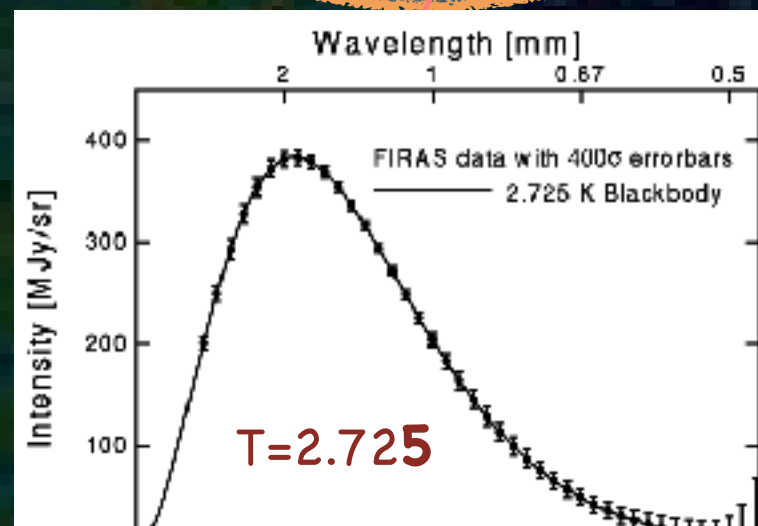
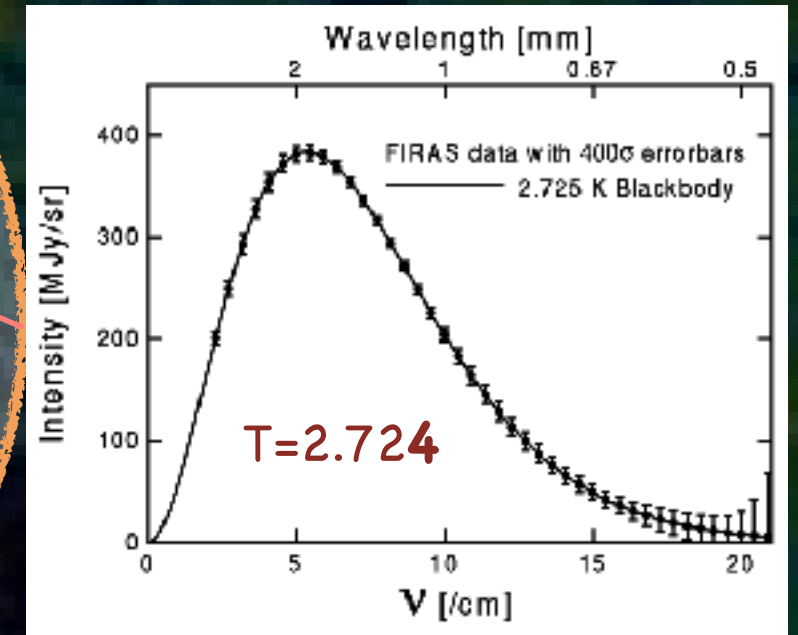
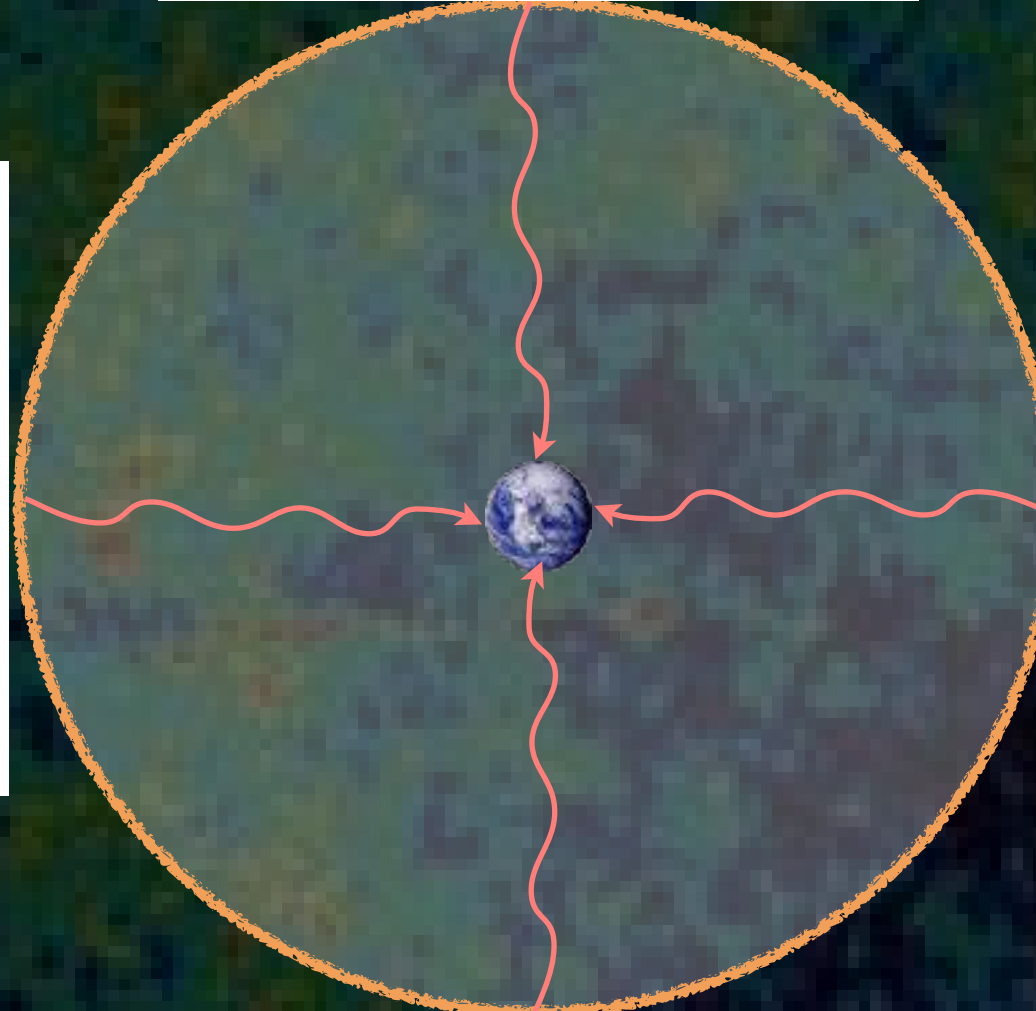
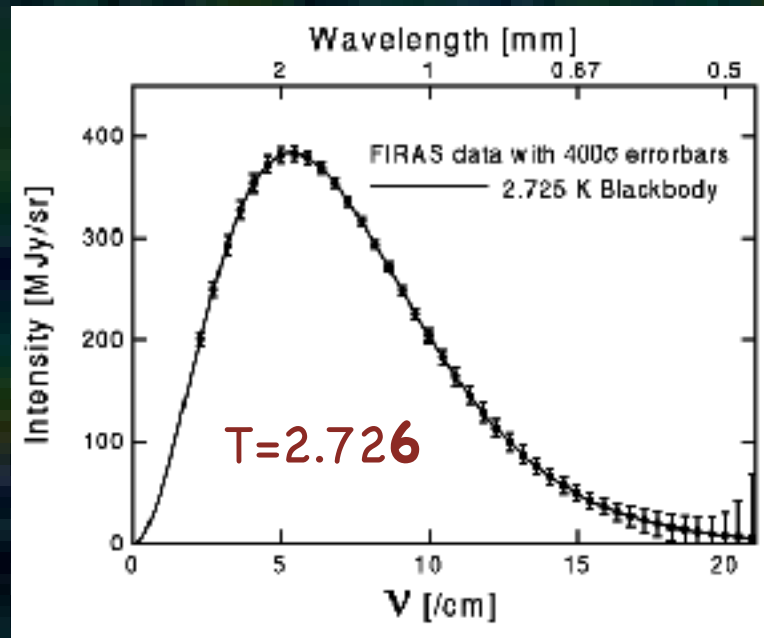
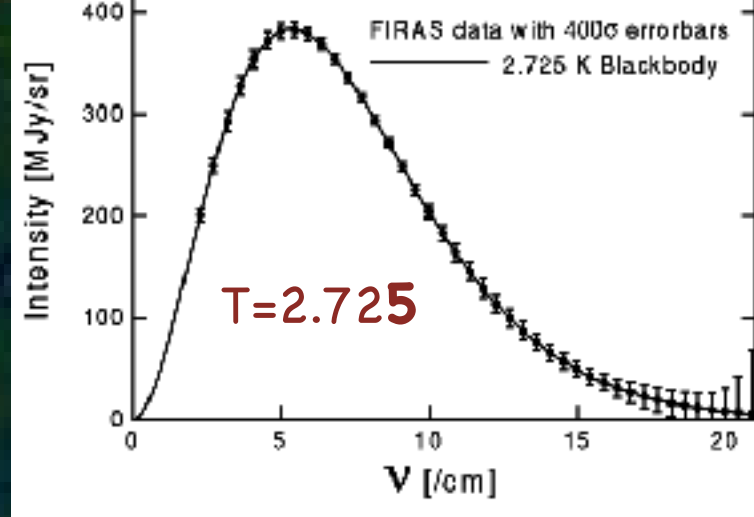
Hu 2005

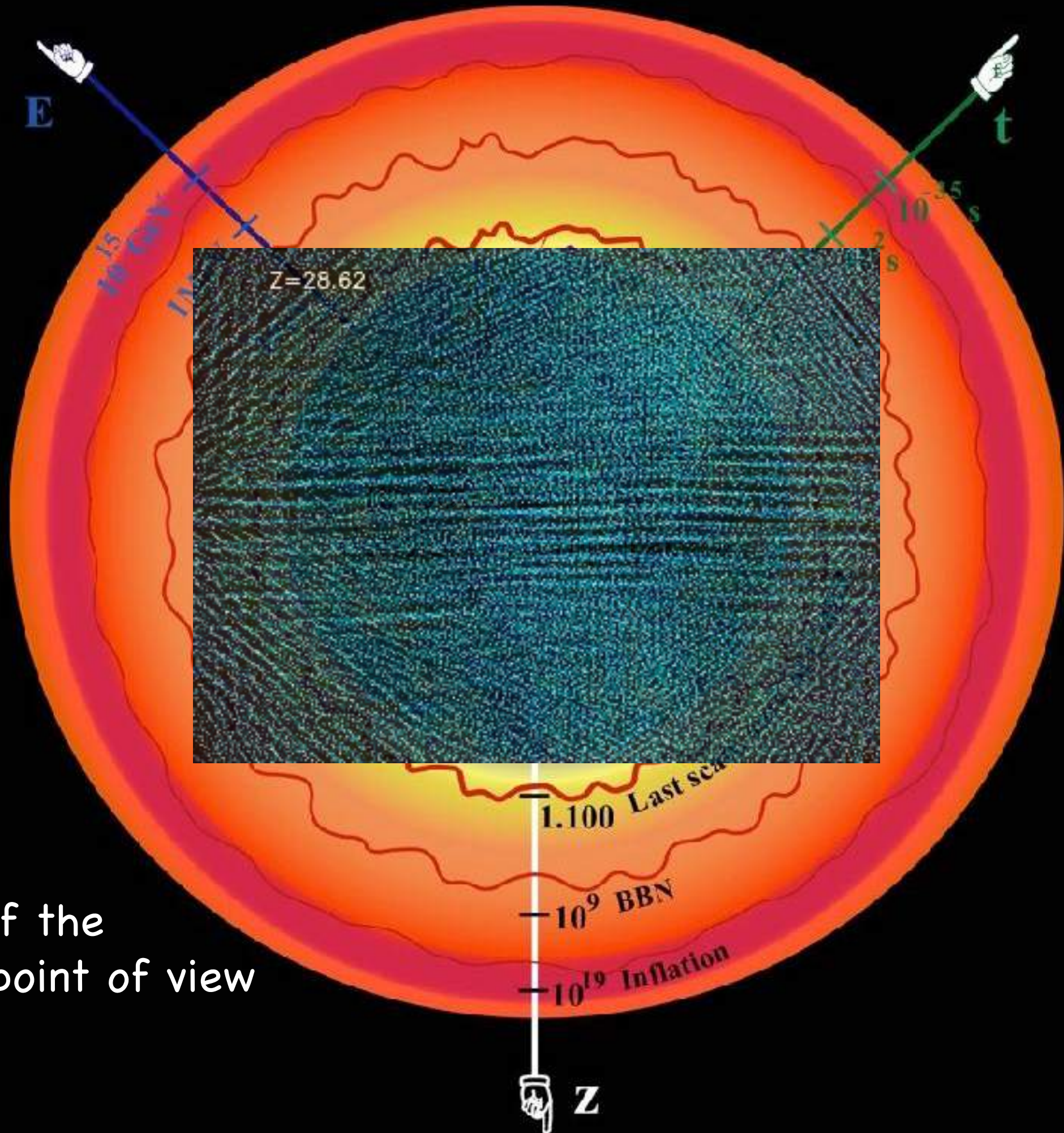
# Width of the Surface of Last Scattering, as observed today:



- The CMB is really a snapshot of an "instant": a picture of a spherical shell of radius  $R_{SLS}$ , when the Universe was 400,000 yrs old







Causal description of the Universe, from our point of view



# Illustris simulation



Time since the Big Bang: 10.8 billion years

ILLUSTRIS

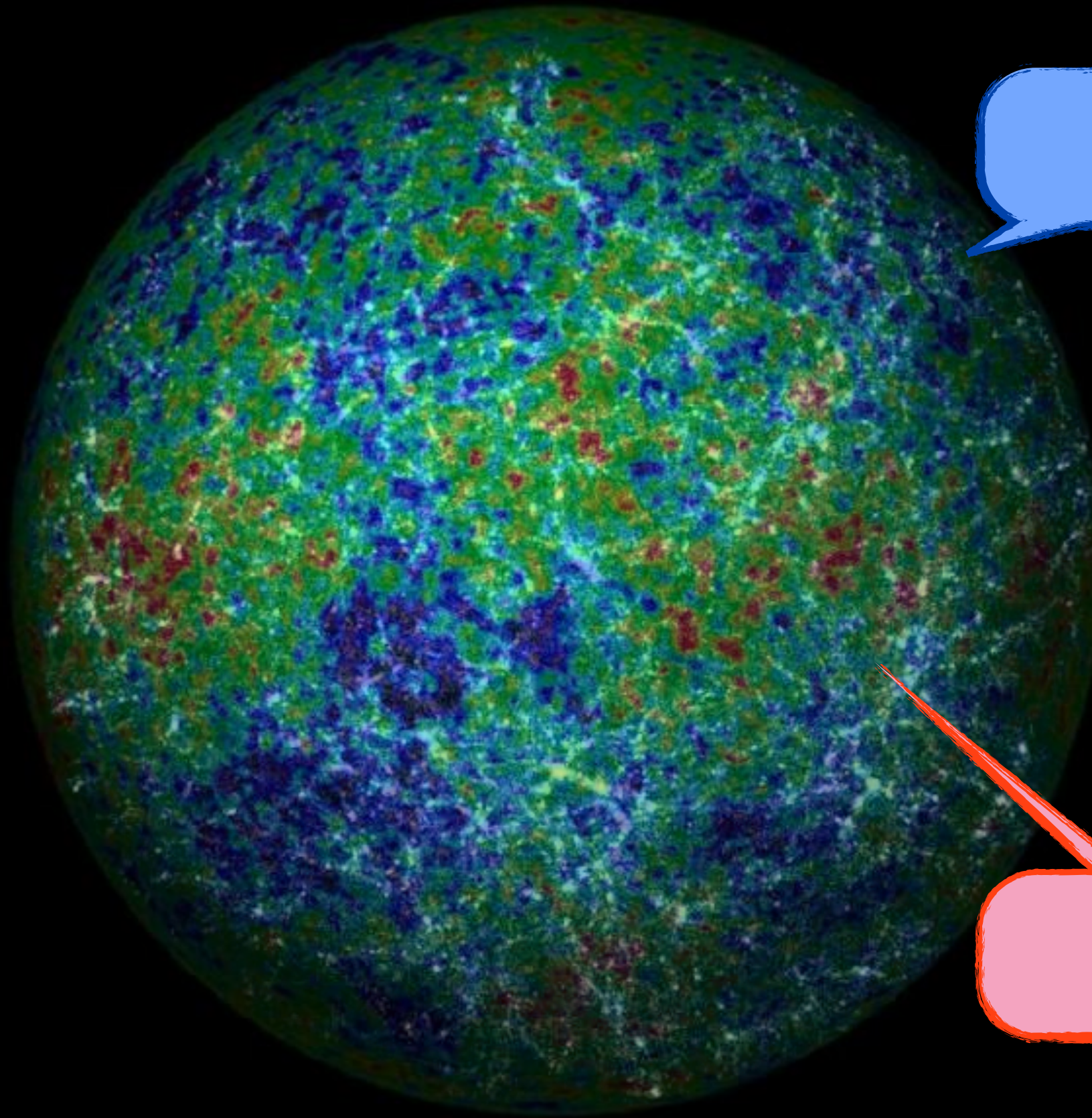
Time since the Big Bang: 10.8 billion years

ILLUSTRIS



# Cosmic Microwave Background:

initial conditions to build the structures of the Universe

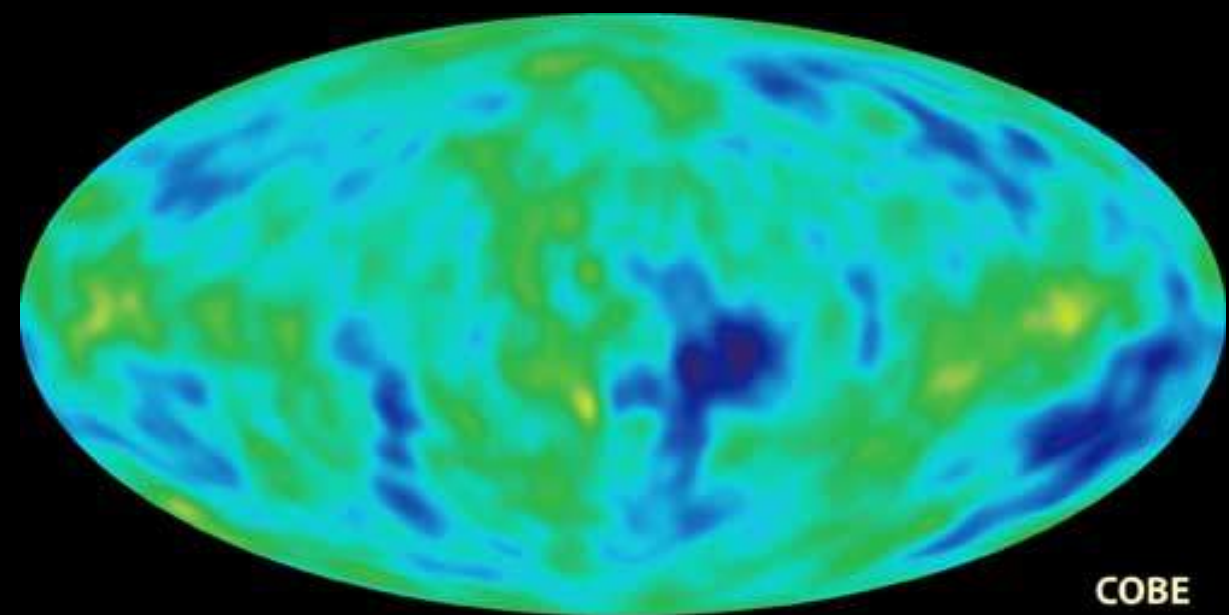


$T \sim 2.7292$  K

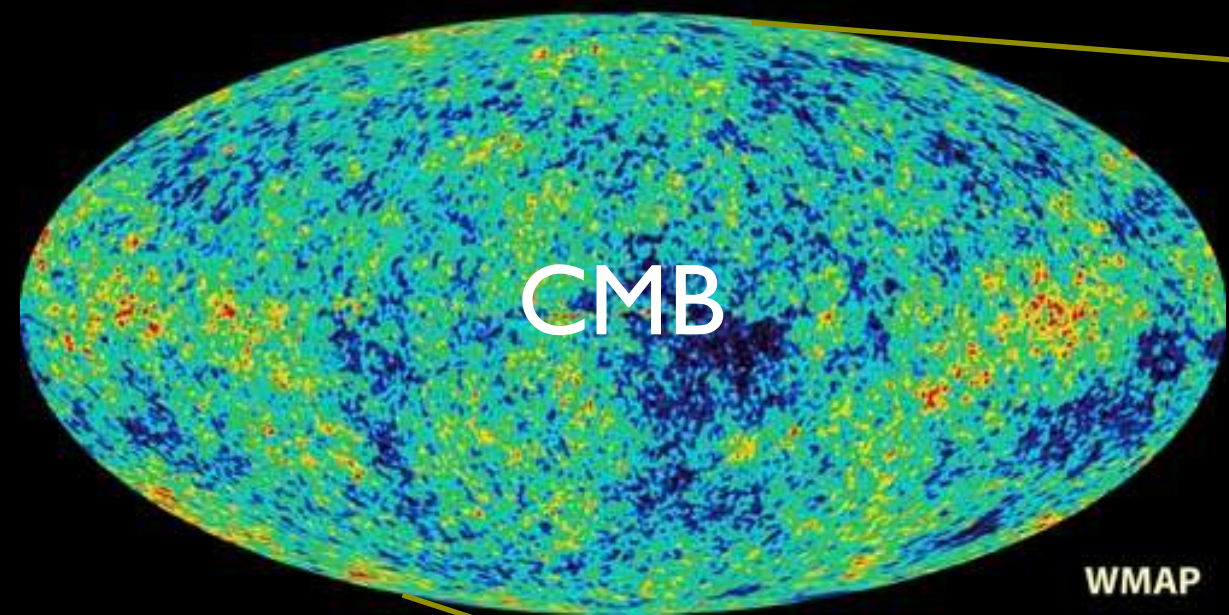
$\Delta T/T \sim 10^{-5}$

$T \sim 2.7298$  K



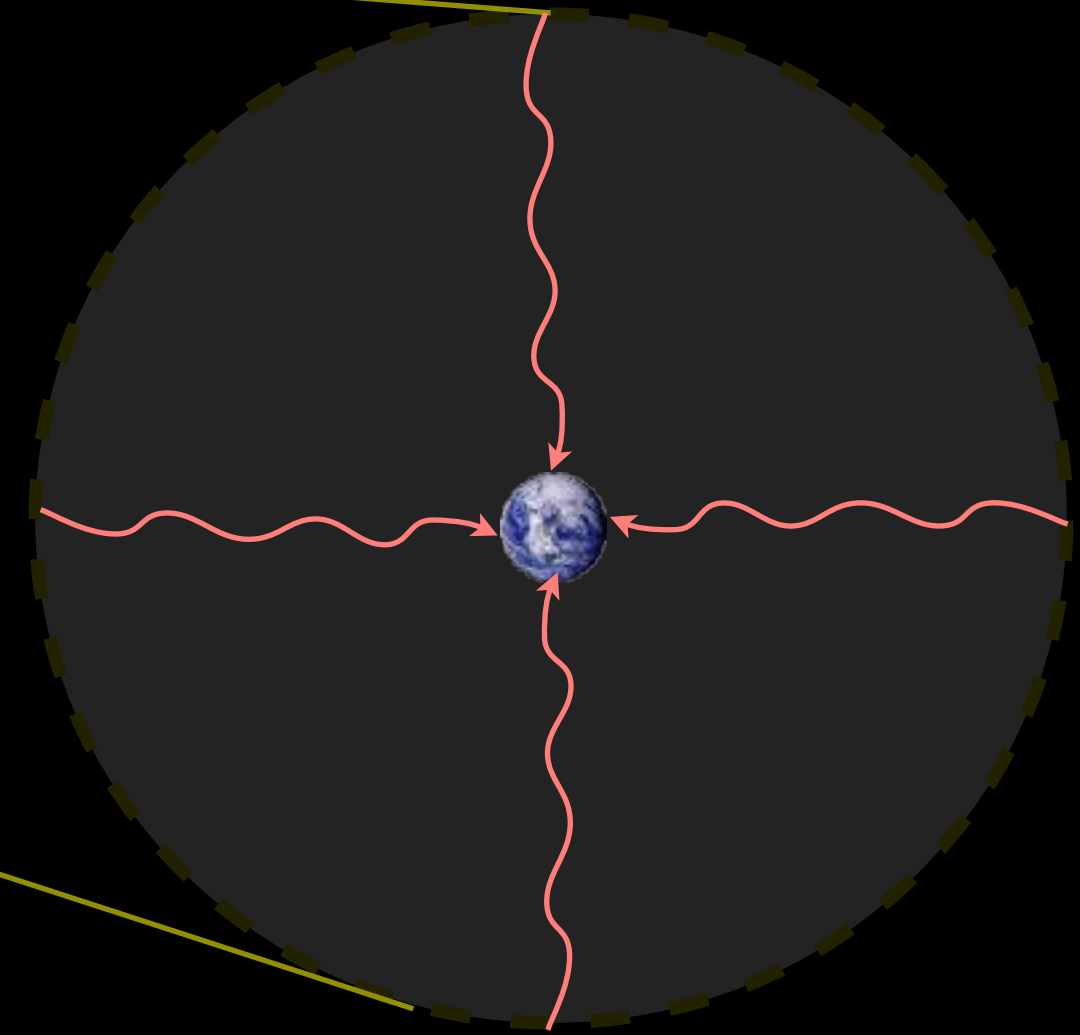


COBE



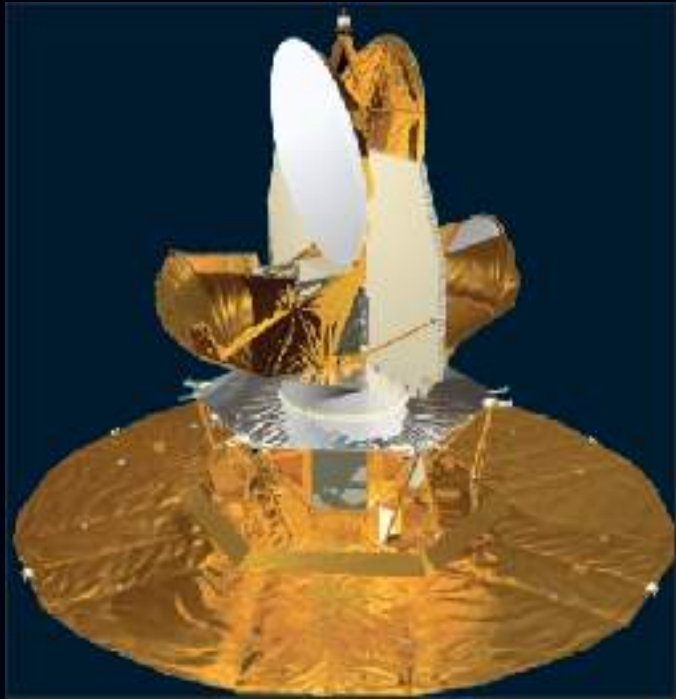
CMB

WMAP

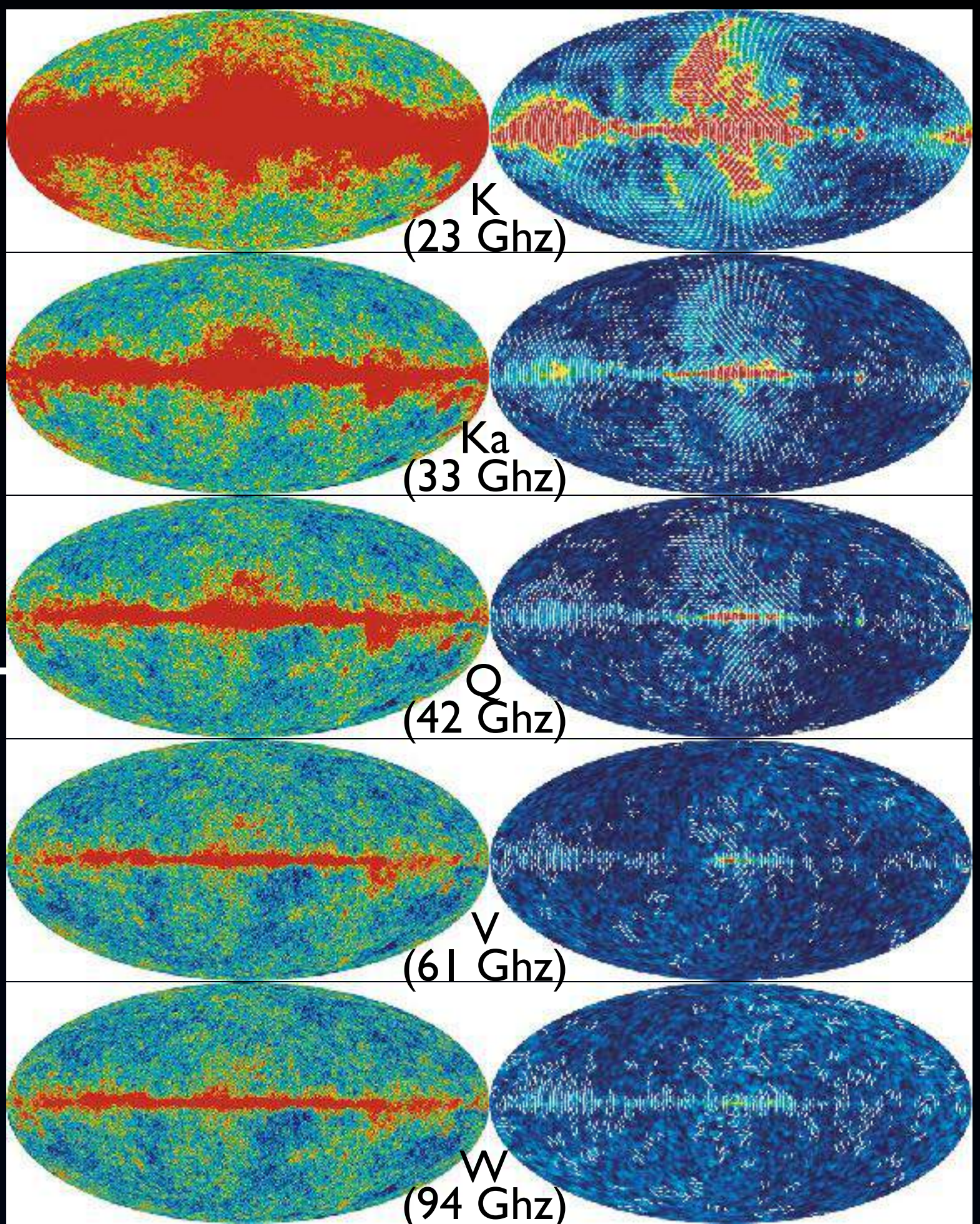




# WMAP: 2003-2012



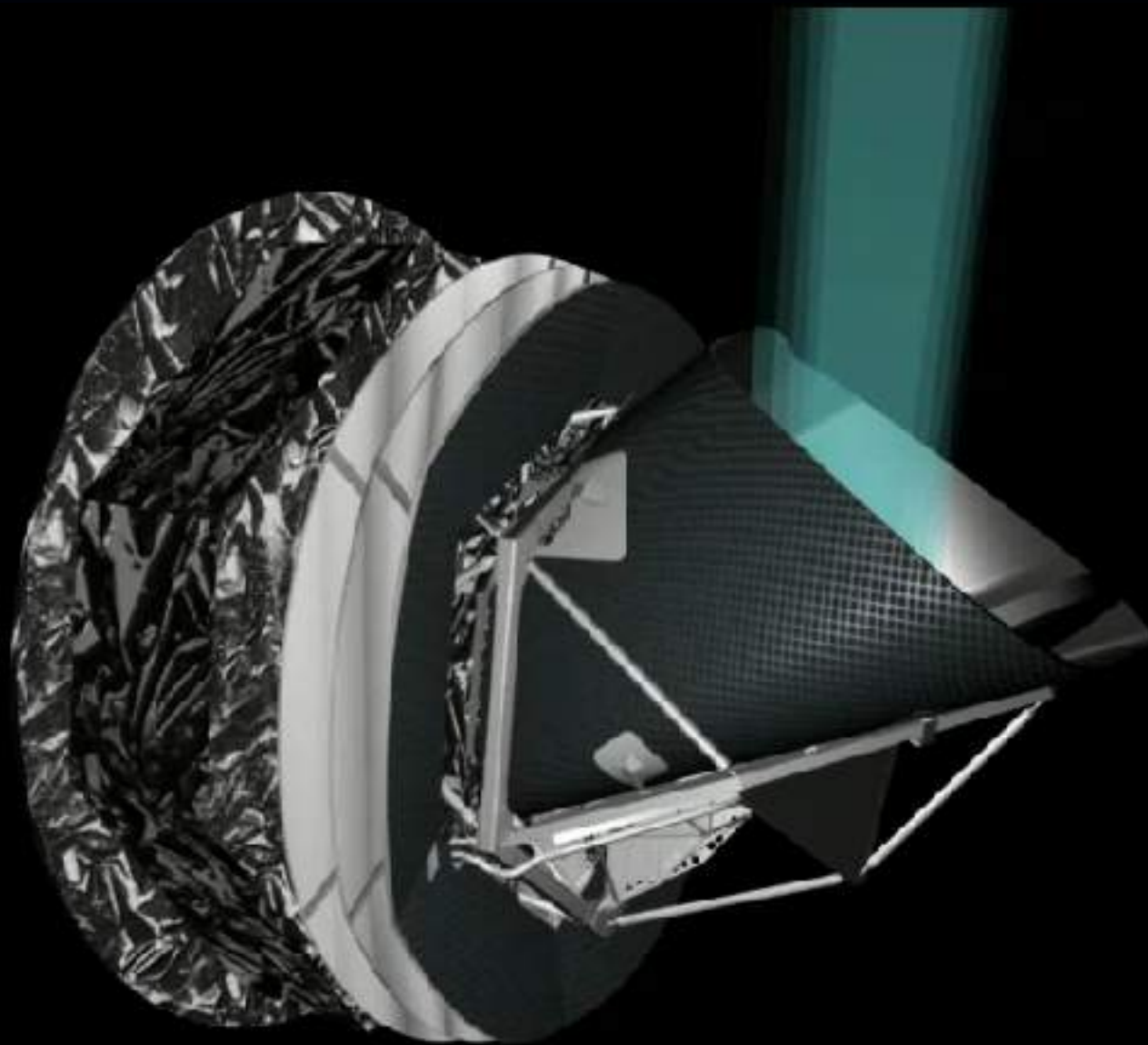
Temperature



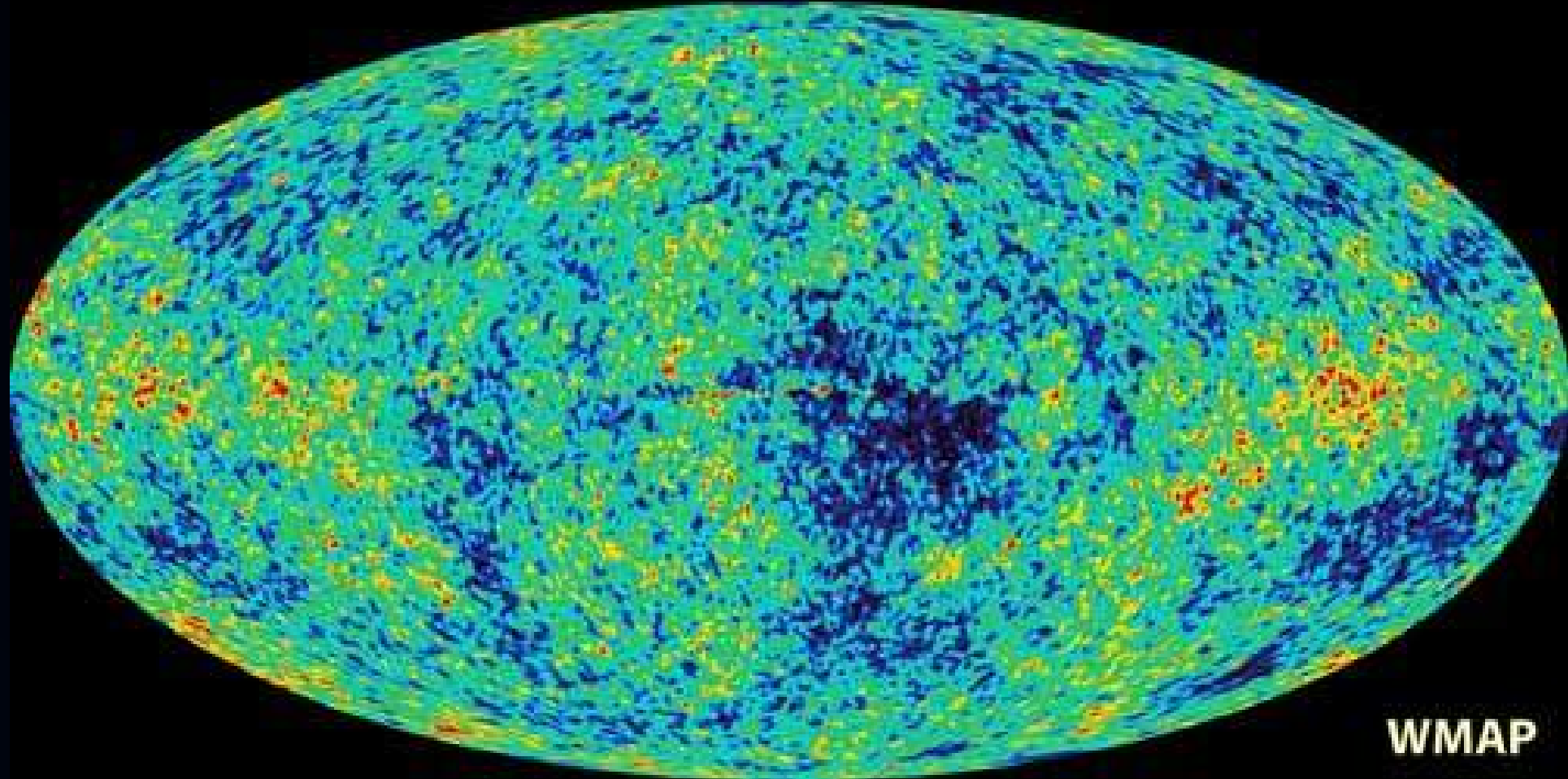
Polarization



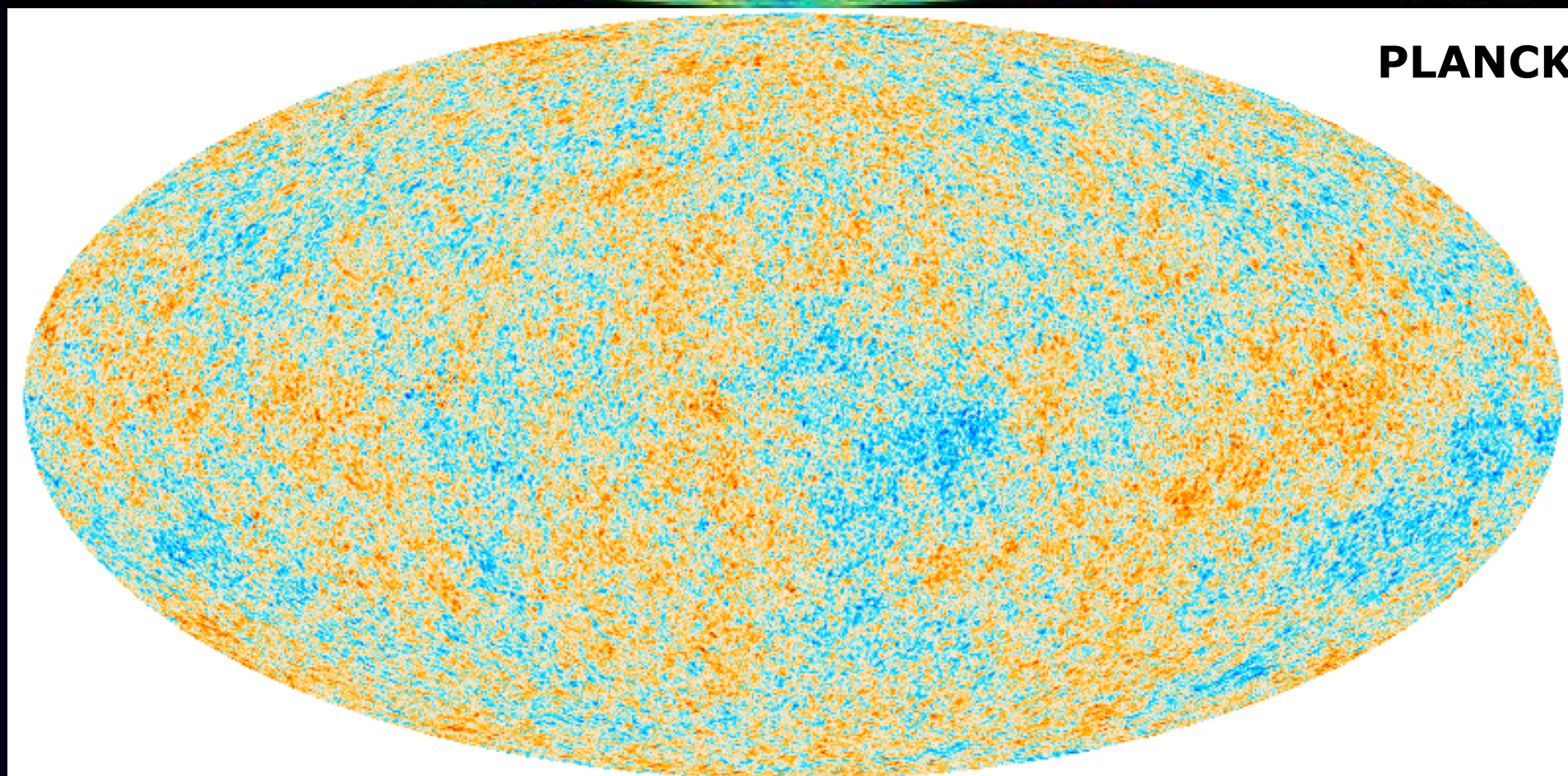
# PLANCK







WMAP

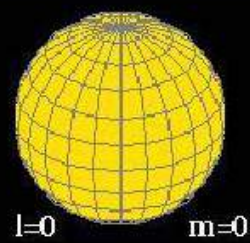
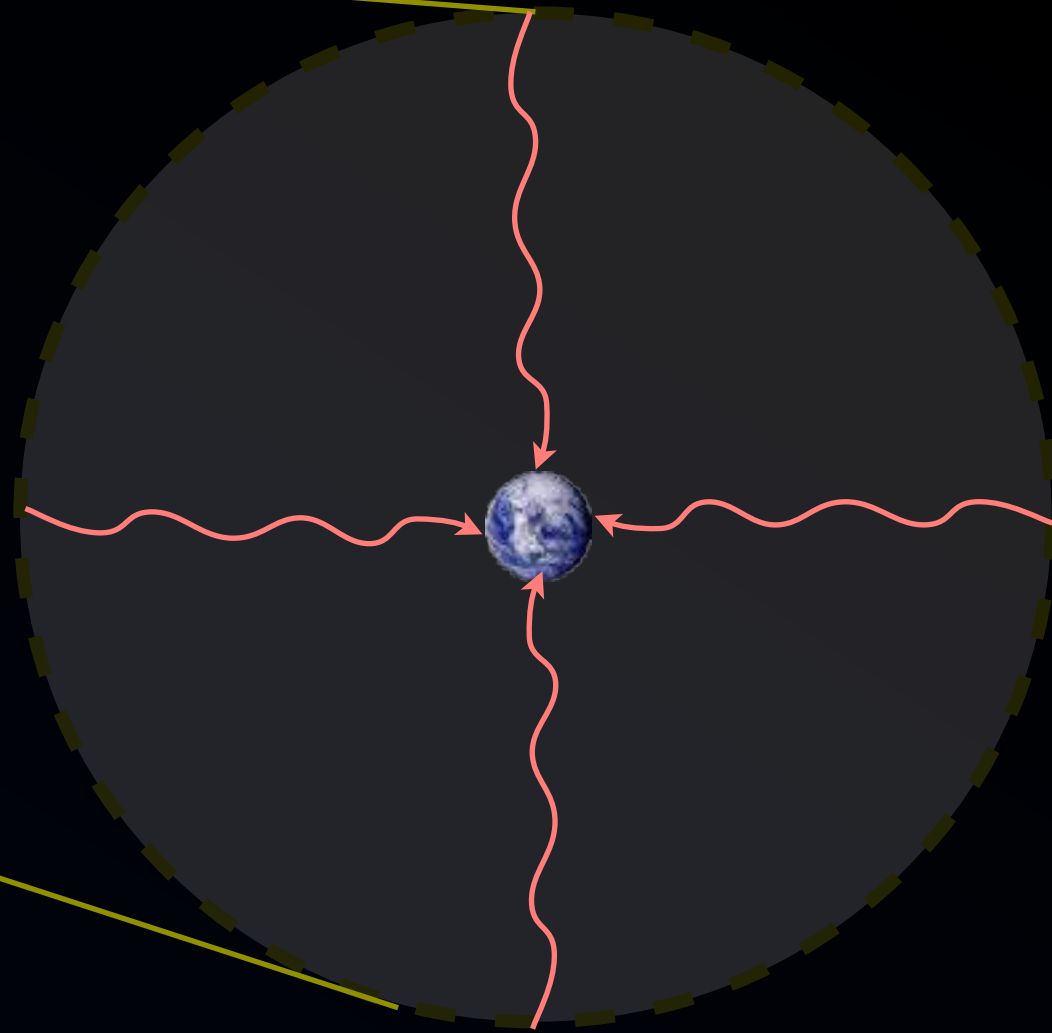


PLANCK

-500  500  $\mu\text{K}_{\text{CMB}}$

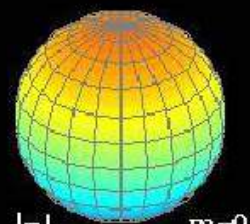


Cosmic  
microwave  
background

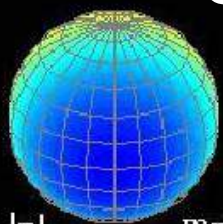


l=0 m=0

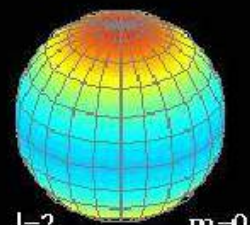
$T(\theta, \varphi)$ :  
spherical harmonic  
decomposition



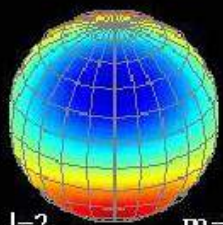
l=1 m=0



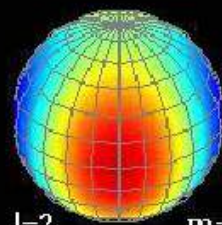
l=1 m=1



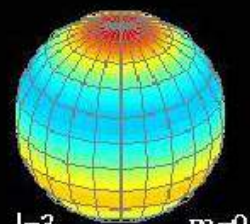
l=2 m=0



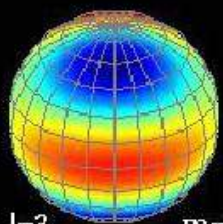
l=2 m=1



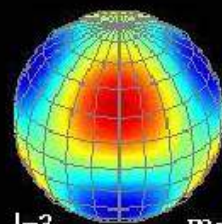
l=2 m=2



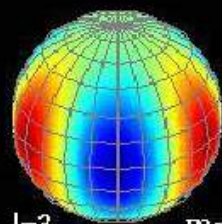
l=3 m=0



l=3 m=1



l=3 m=2



l=3 m=3

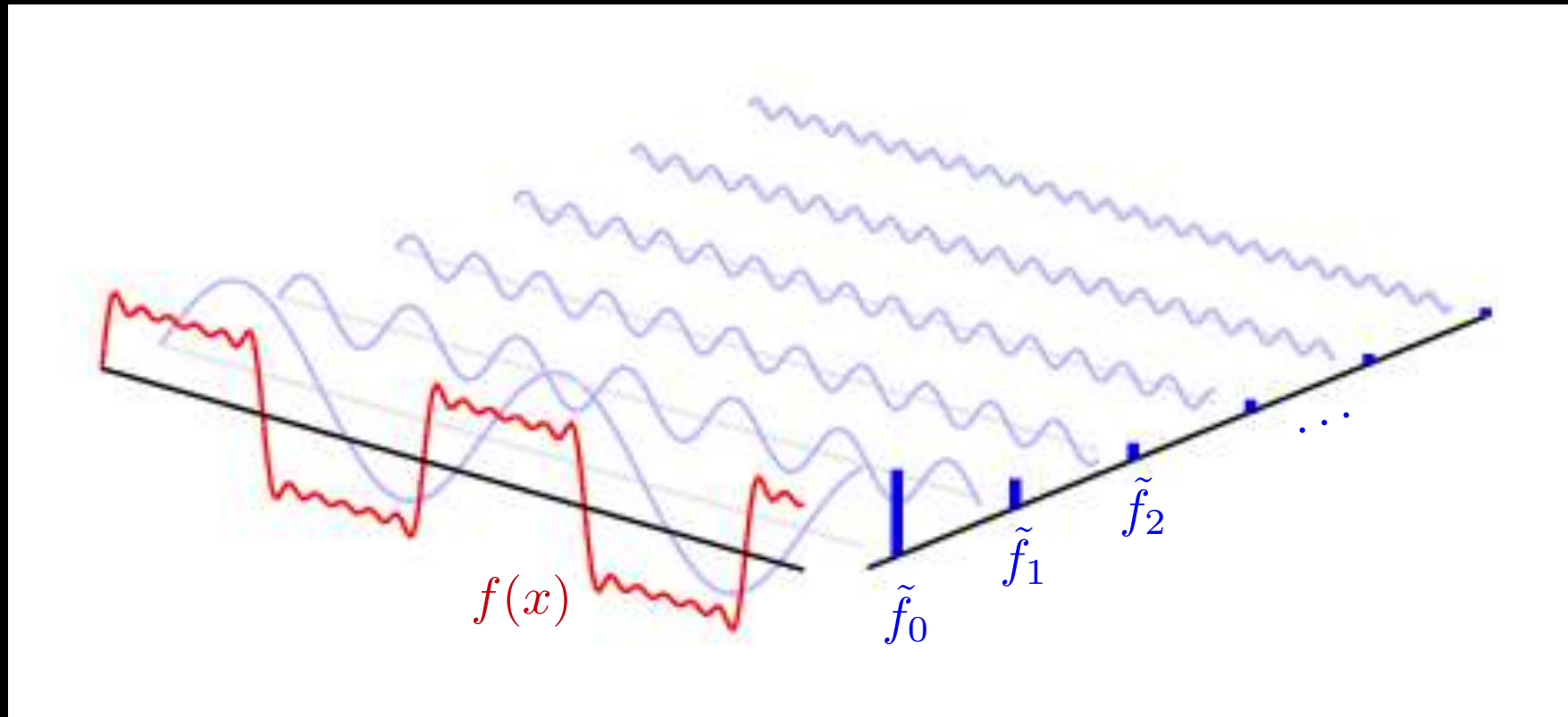
$$\delta T(\theta, \varphi) = \sum_{\ell, m} a_{\ell m} Y_{\ell}^m(\theta, \varphi)$$

$$C_{\ell} = \frac{1}{2\ell + 1} \sum_{m=-\ell}^{\ell} |a_{\ell m}|^2$$



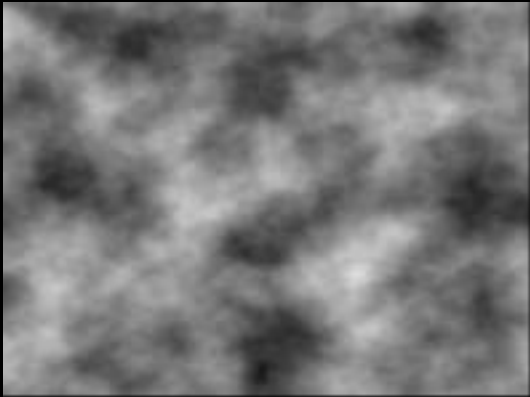
# Spherical Harmonics and Fourier Transform

Decomposition into Fourier modes (*Fourier Transform*)

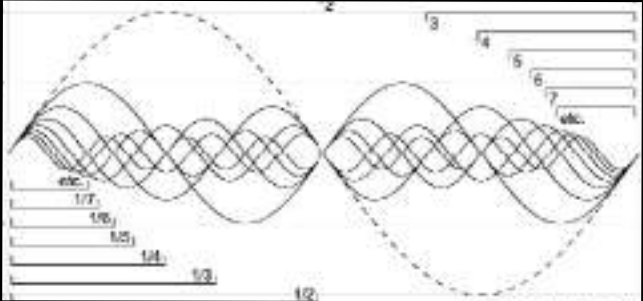


$$f(x) = \sum_k \tilde{f}_k e^{ikx}$$

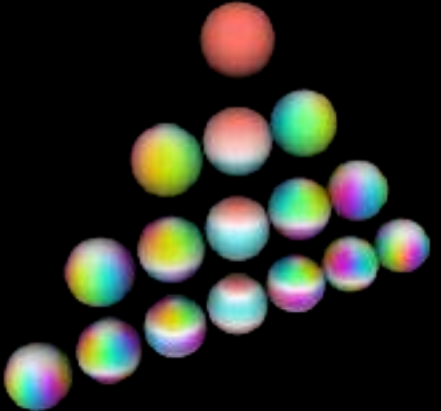
# Spherical Harmonics and Fourier Transform



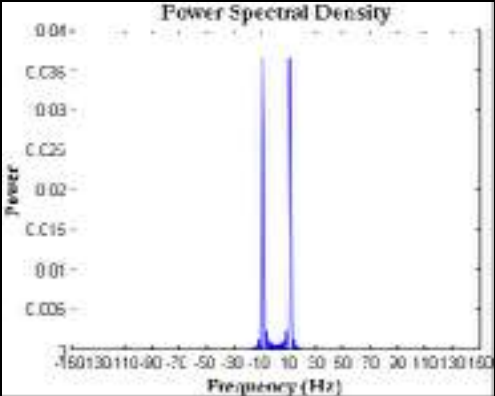
$$f(x, y) \longleftrightarrow f(\theta, \phi)$$



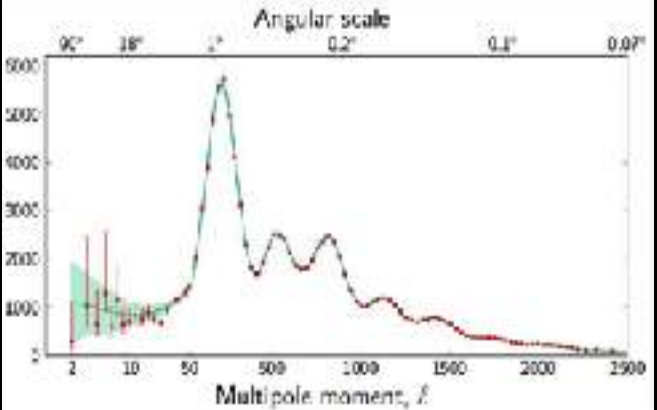
$$e^{i(k_x x + k_y y)} \longleftrightarrow Y_{\ell m}(\theta, \phi)$$



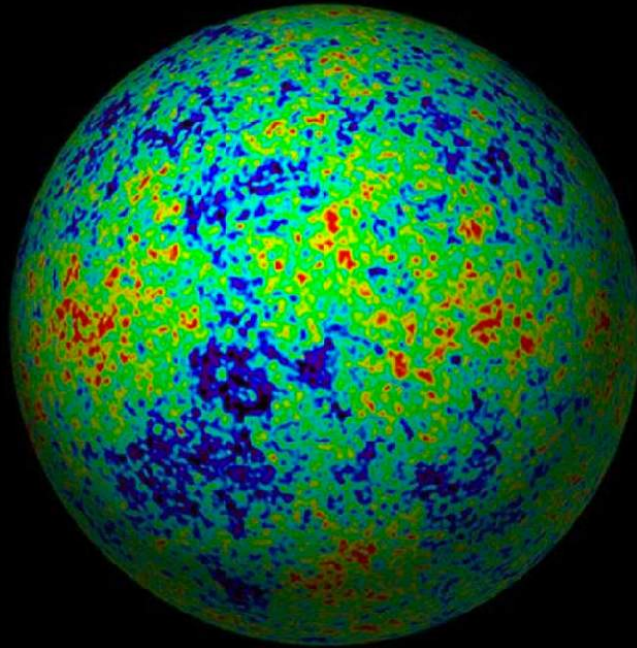
$$f(x, y) = \sum_{\vec{k}} \tilde{f}_{\vec{k}} e^{i(k_x x + k_y y)} \longleftrightarrow f(\theta, \phi) = \sum_{m=-\ell}^{\ell} \sum_{\ell=0}^{\infty} a_{\ell m} Y_{\ell m}(\theta, \phi)$$



$$P_k = |\tilde{f}_{\vec{k}}|^2 \longleftrightarrow C_\ell = \langle |a_{\ell m}|^2 \rangle$$



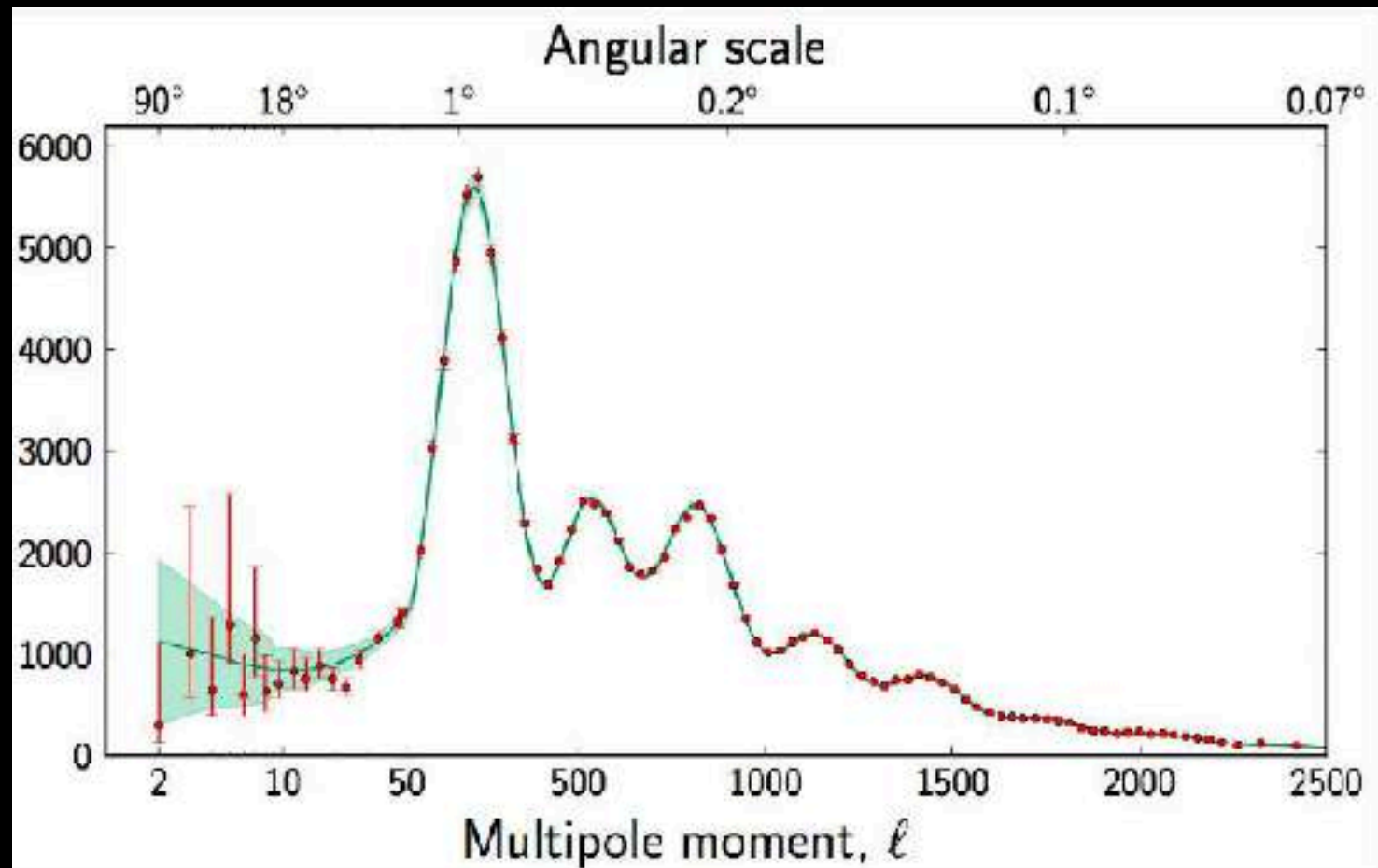
# Angular power spectrum of the CMB



NASA, WMAP

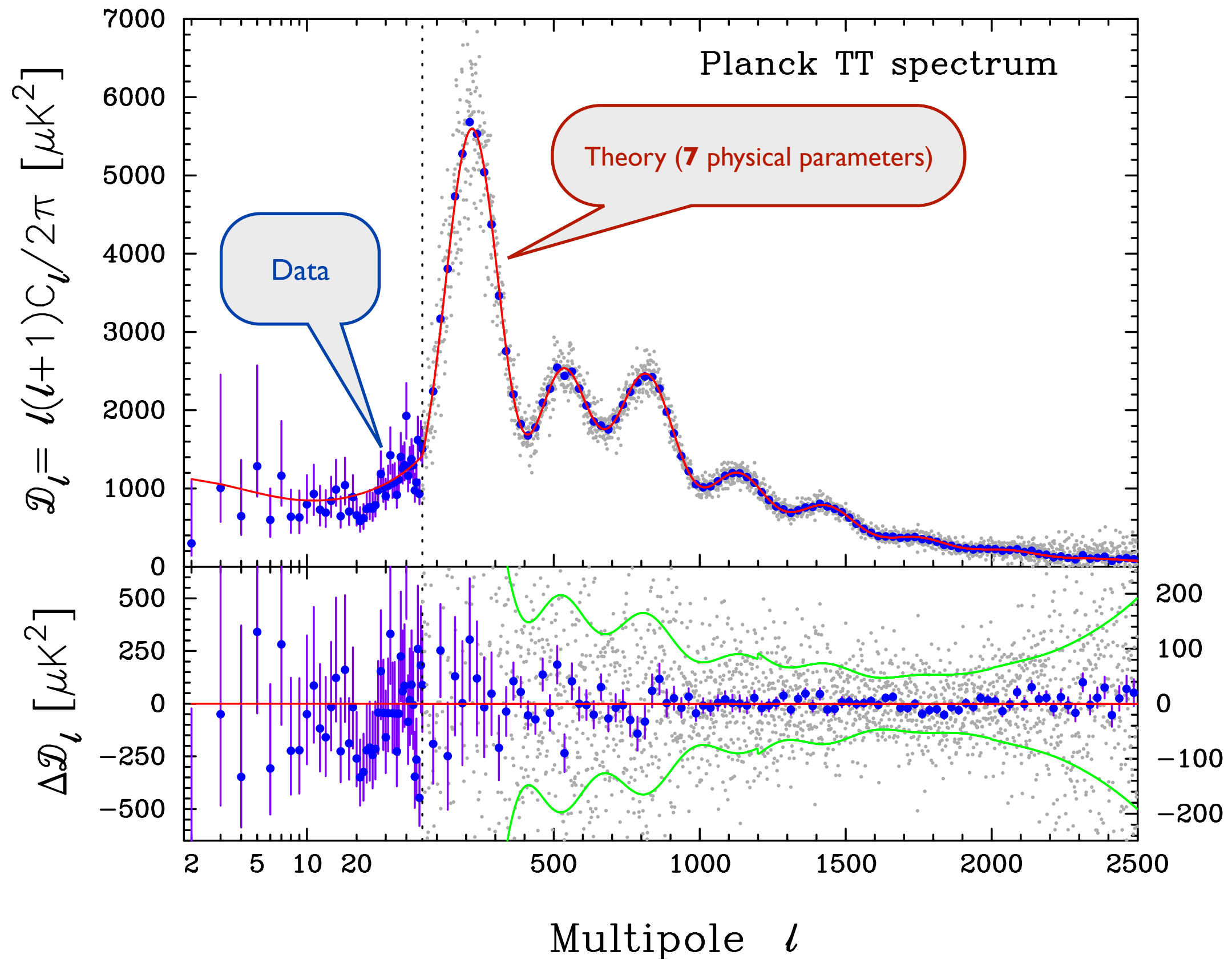
$$f(\theta, \phi) = \sum_{m=-\ell}^{\ell} \sum_{\ell=0}^{\infty} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$C_{\ell} = \langle |a_{\ell m}|^2 \rangle$$





# Theory v. data (temperature)

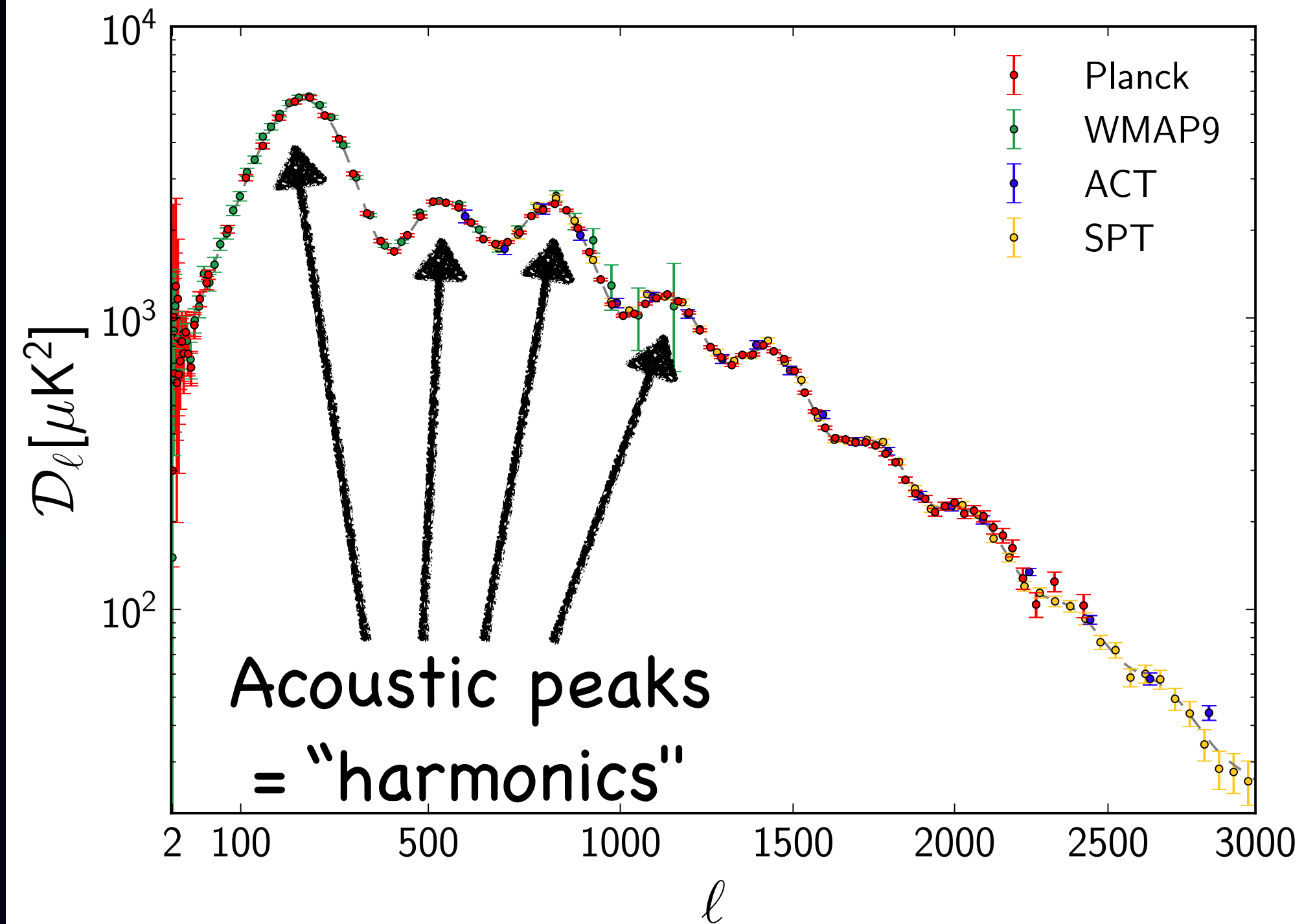


# CMB: “Precision cosmology”

Parameter	<i>Planck</i> (CMB+lensing)		<i>Planck</i> +WP+highL+BAO	
	Best fit	68 % limits	Best fit	68 % limits
$\Omega_b h^2$ . . . . .	0.022242	$0.02217 \pm 0.00033$	0.022161	$0.02214 \pm 0.00024$
$\Omega_c h^2$ . . . . .	0.11805	$0.1186 \pm 0.0031$	0.11889	$0.1187 \pm 0.0017$
$100\theta_{MC}$ . . . . .	1.04150	$1.04141 \pm 0.00067$	1.04148	$1.04147 \pm 0.00056$
$\tau$ . . . . .	0.0949	$0.089 \pm 0.032$	0.0952	$0.092 \pm 0.013$
$n_s$ . . . . .	0.9675	$0.9635 \pm 0.0094$	0.9611	$0.9608 \pm 0.0054$
$\ln(10^{10} A_s)$ . . . . .	3.098	$3.085 \pm 0.057$	3.0973	$3.091 \pm 0.025$
$\Omega_\Lambda$ . . . . .	0.6964	$0.693 \pm 0.019$	0.6914	$0.692 \pm 0.010$
$\sigma_8$ . . . . .	0.8285	$0.823 \pm 0.018$	0.8288	$0.826 \pm 0.012$
$z_{re}$ . . . . .	11.45	$10.8^{+3.1}_{-2.5}$	11.52	$11.3 \pm 1.1$
$H_0$ . . . . .	68.14	$67.9 \pm 1.5$	67.77	$67.80 \pm 0.77$
Age/Gyr . . . . .	13.784	$13.796 \pm 0.058$	13.7965	$13.798 \pm 0.037$
$100\theta_*$ . . . . .	1.04164	$1.04156 \pm 0.00066$	1.04163	$1.04162 \pm 0.00056$
$r_{drag}$ . . . . .	147.74	$147.70 \pm 0.63$	147.611	$147.68 \pm 0.45$
$r_{drag}/D_V(0.57)$ . . . . .	0.07207	$0.0719 \pm 0.0011$		



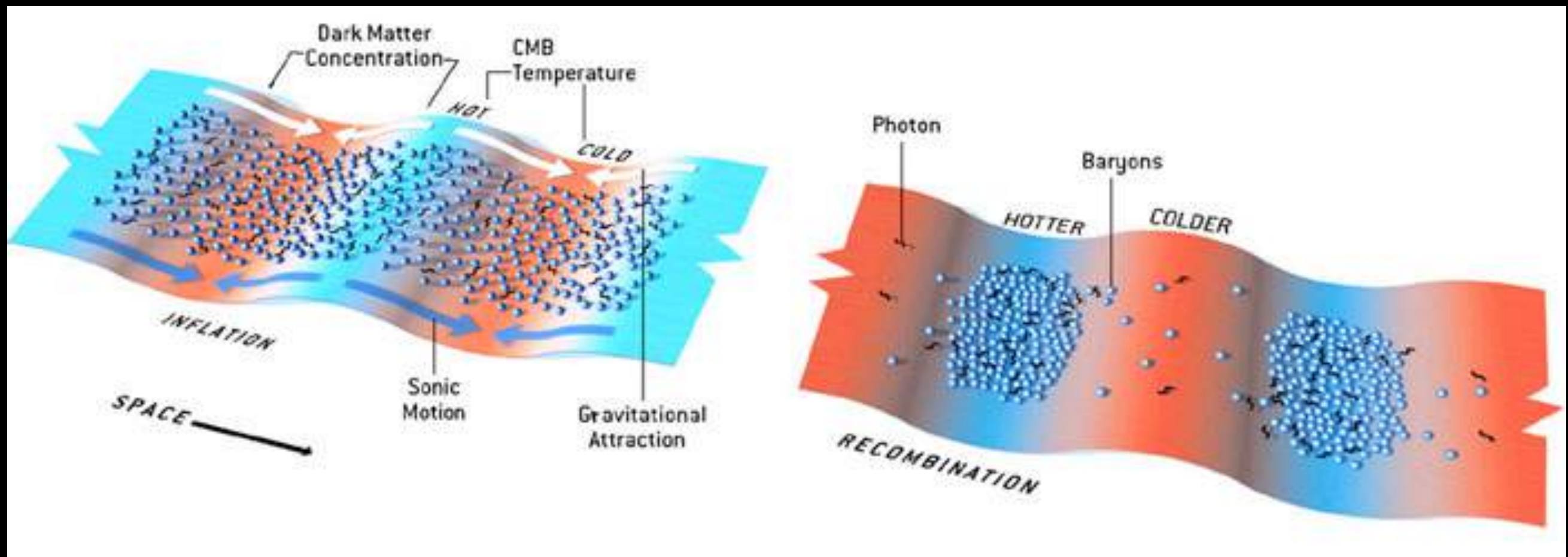
# Acoustic waves of radiation, baryonic matter (and dark matter)



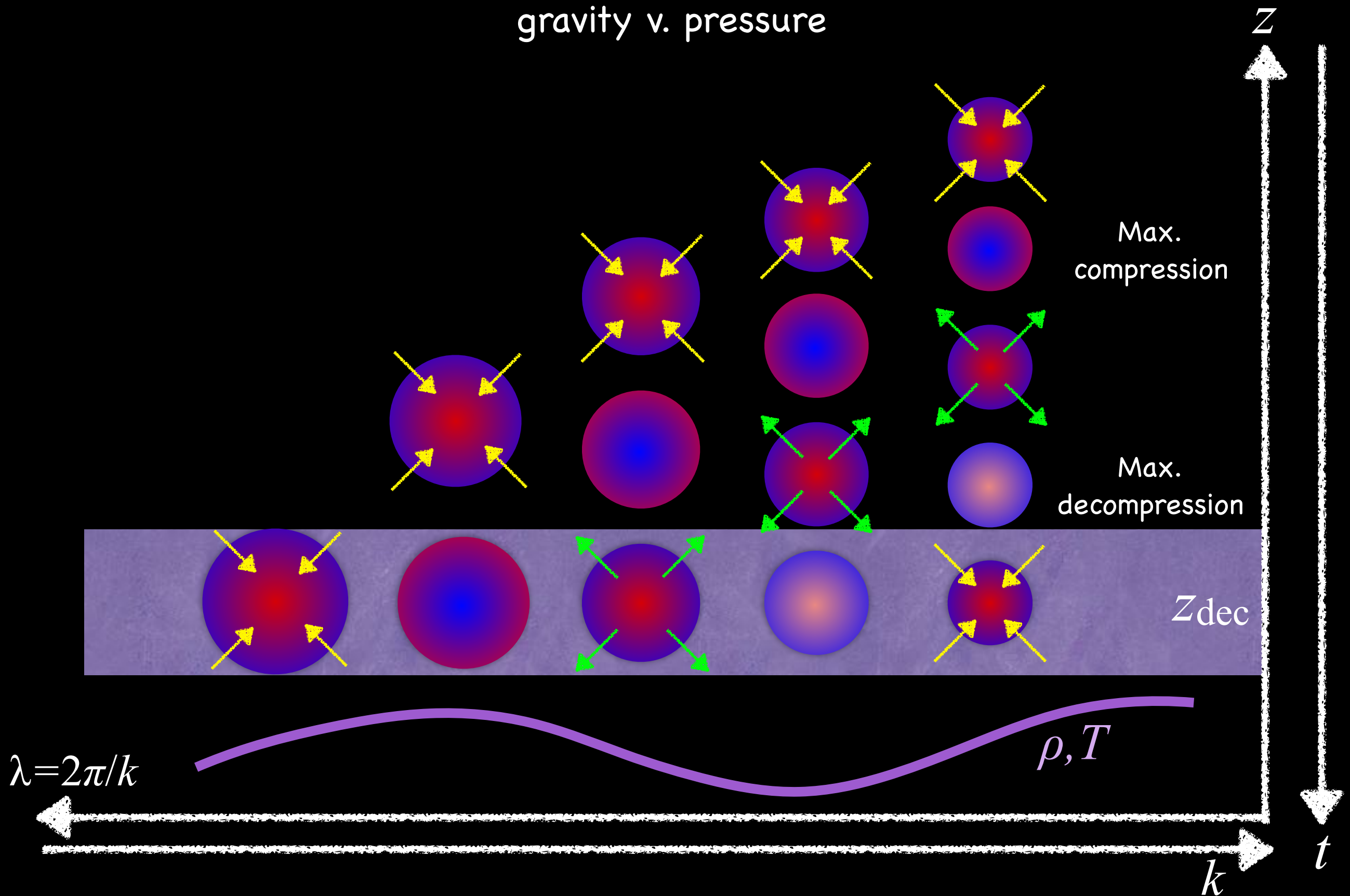
**Physics of the CMB:  
pressure waves  
("acoustic waves")**



# Physical processes around decoupling: pressure waves (“acoustic waves”)



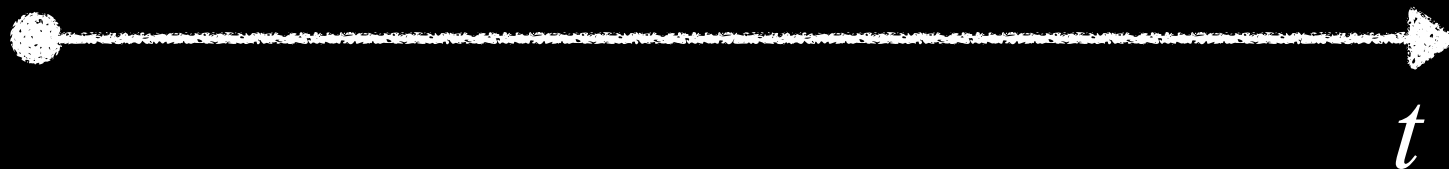
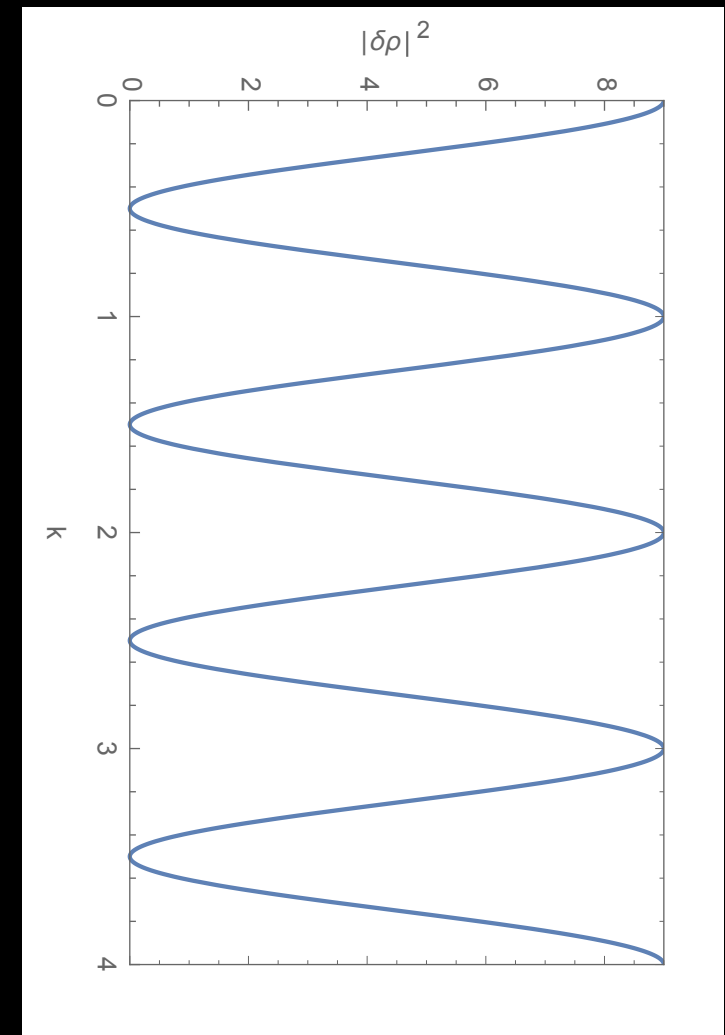
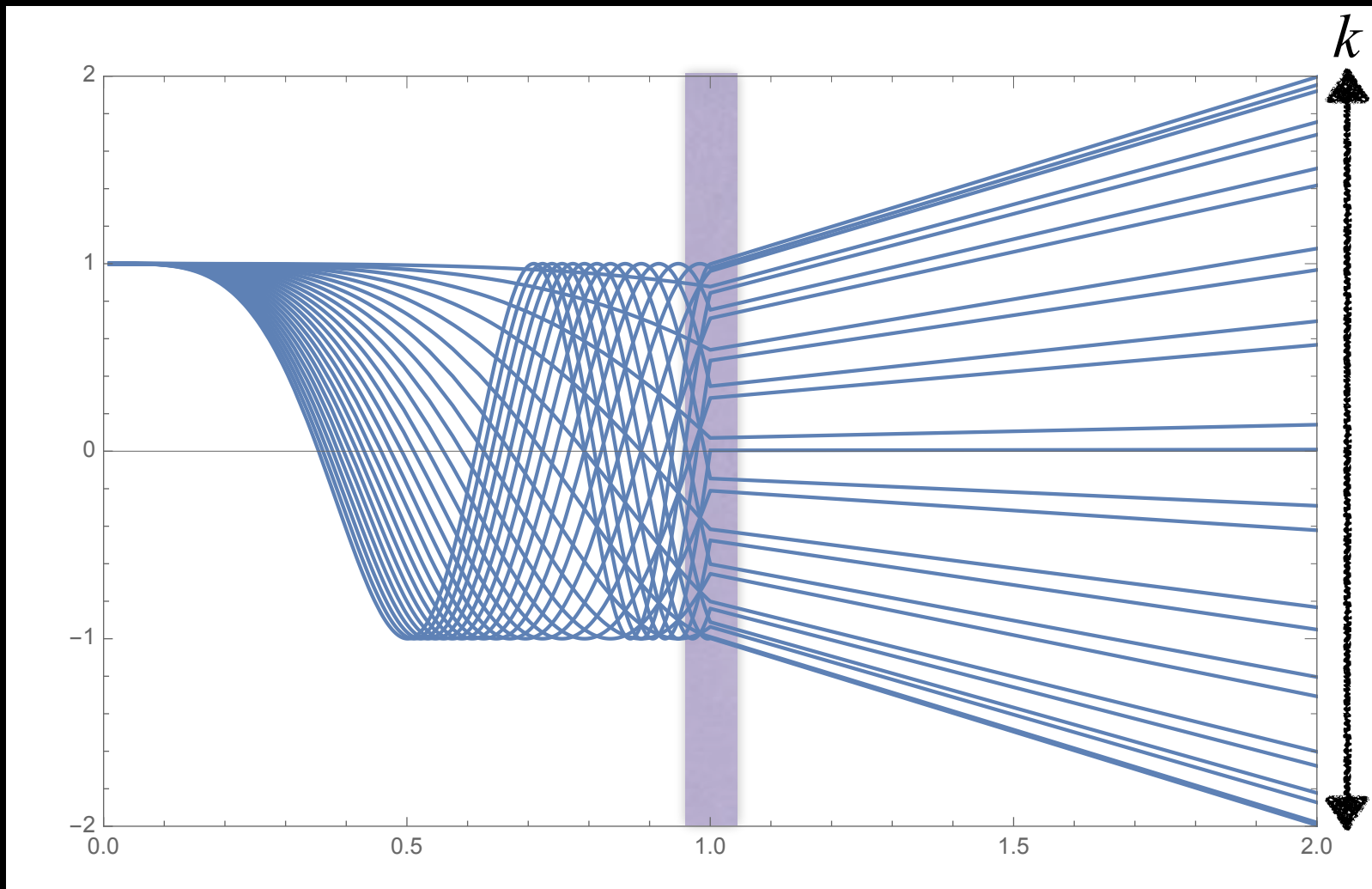
Acoustic waves of the photon+baryon+dark matter fluid:  
gravity v. pressure





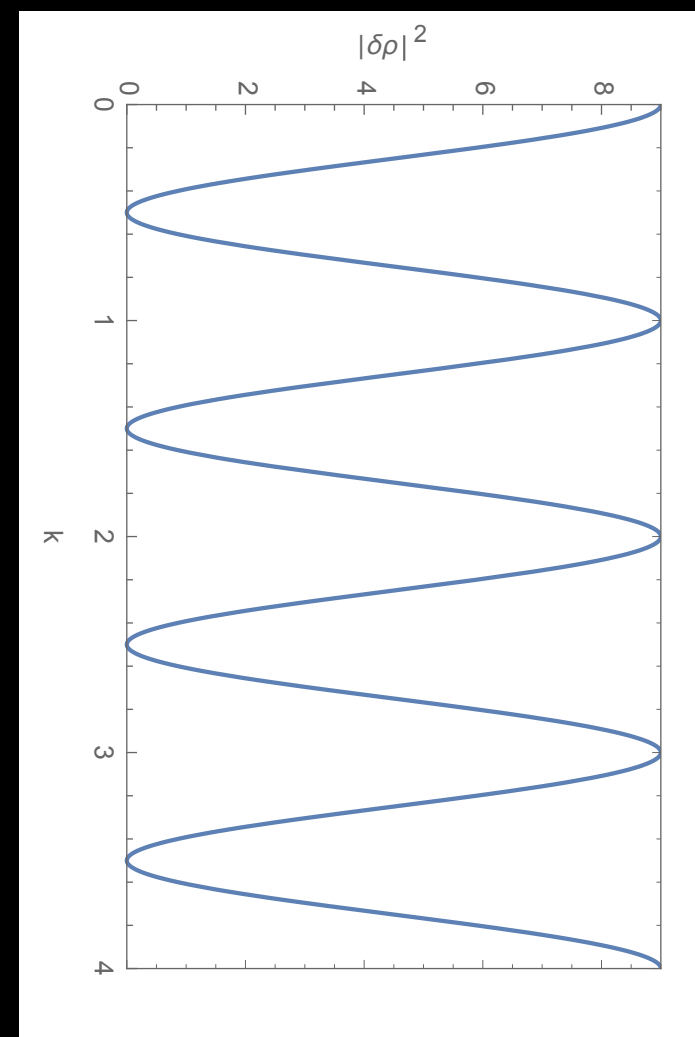
When the photons decouple from matter, the density fluctuations (of baryons + DM, mostly) lose the pressure support and start evolving only according to gravity – growing with the scale factor:

$$\delta \sim a$$



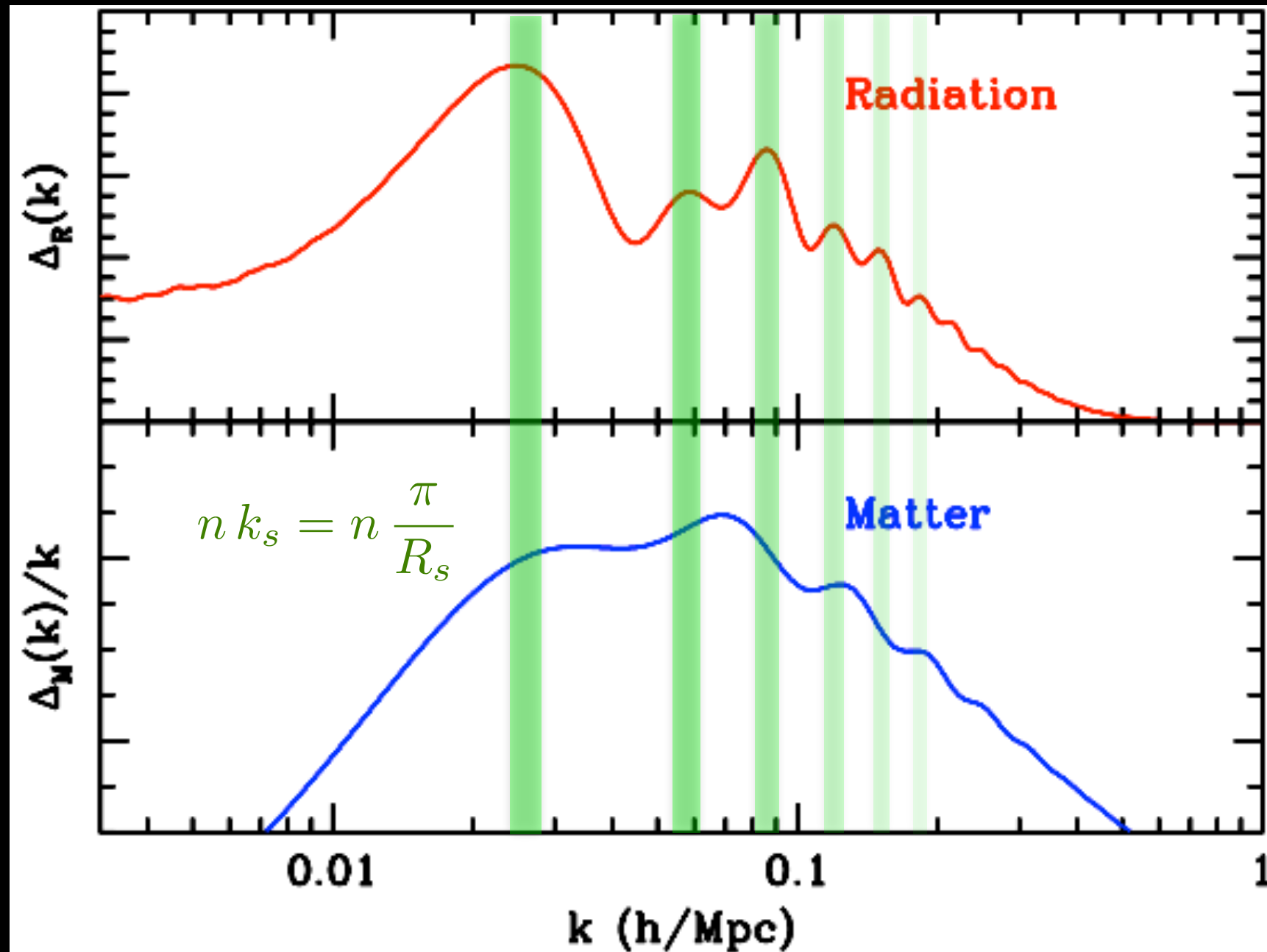
When the photons decouple from matter, the density fluctuations (of baryons + DM, mostly) lose the pressure support and start evolving only according to gravity – growing with the scale factor:

$$\delta \sim a$$



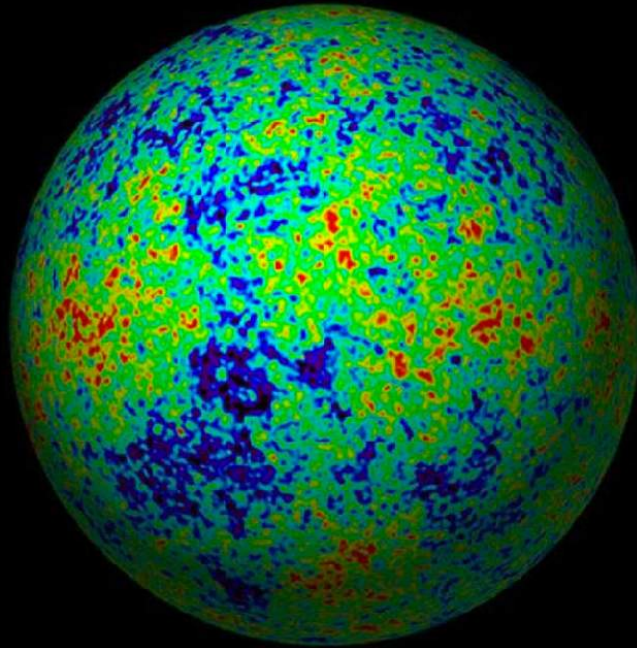


# Acoustic waves of radiation, baryons and dark matter



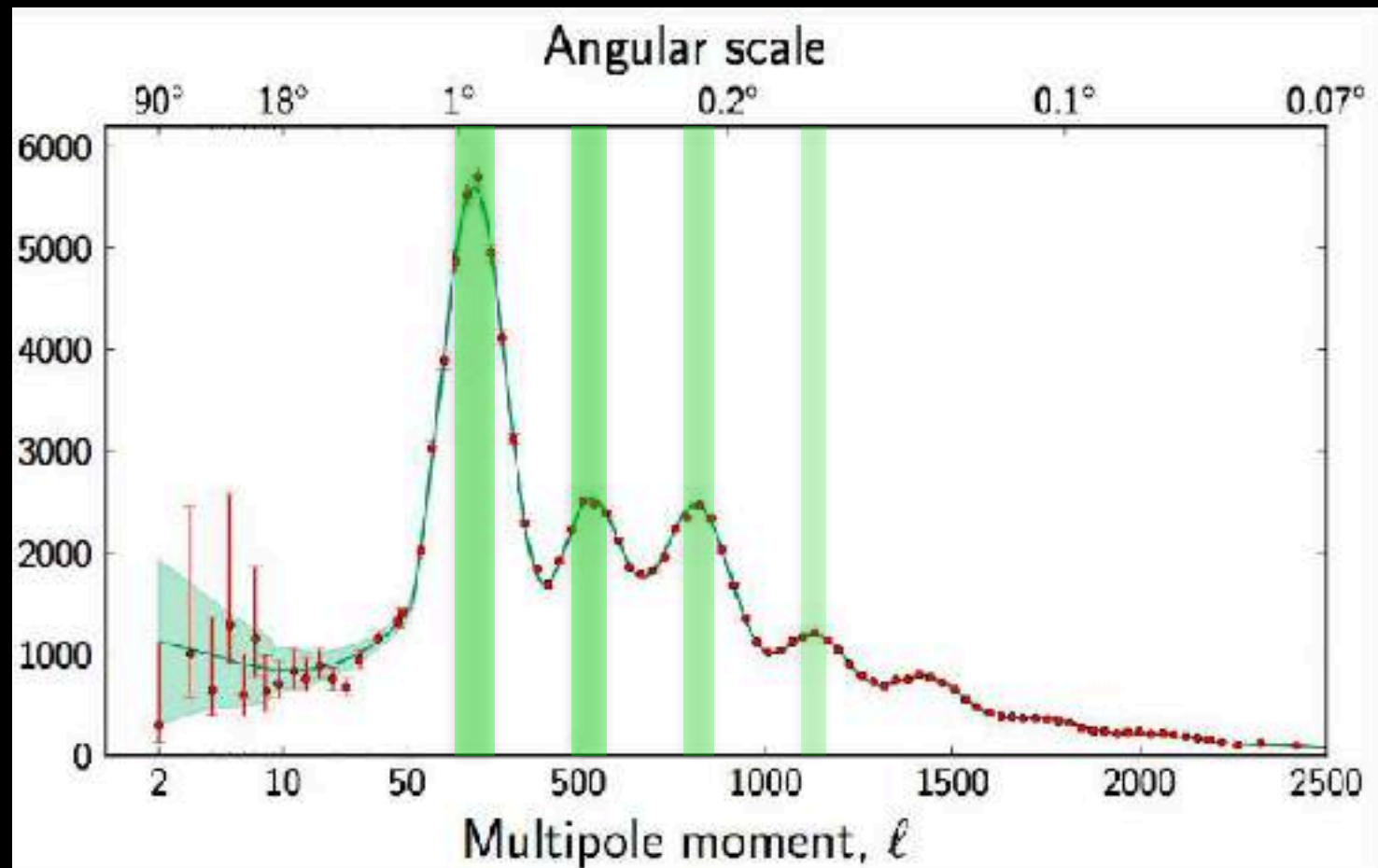
$$R_s = \int_0^{t_{dec}} dt \frac{c_s}{a(t)} = \int_0^{a_{dec}} da \frac{c_s}{H(a) a^2} = \int_{z_{dec}}^{\infty} dz \frac{c_s}{H(z)}$$

# Angular power spectrum of the CMB



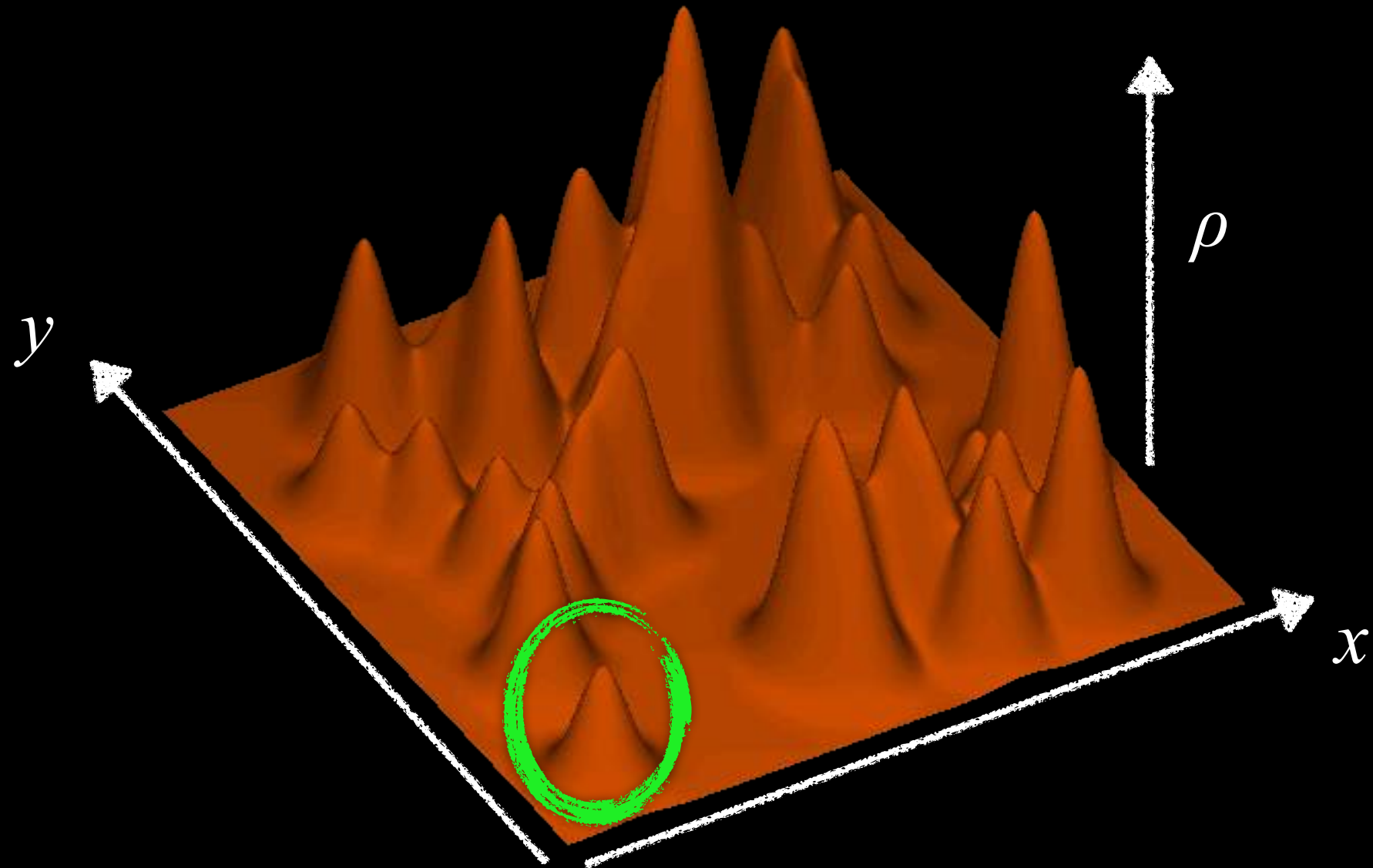
$$f(\theta, \phi) = \sum_{m=-\ell}^{\ell} \sum_{\ell=0}^{\infty} a_{\ell m} Y_{\ell m}(\theta, \phi)$$

$$C_{\ell} = \langle |a_{\ell m}|^2 \rangle$$





In matter the effect is subtle, when we observe a more realistic distribution of matter (below, a 2D section of a 3D distribution)



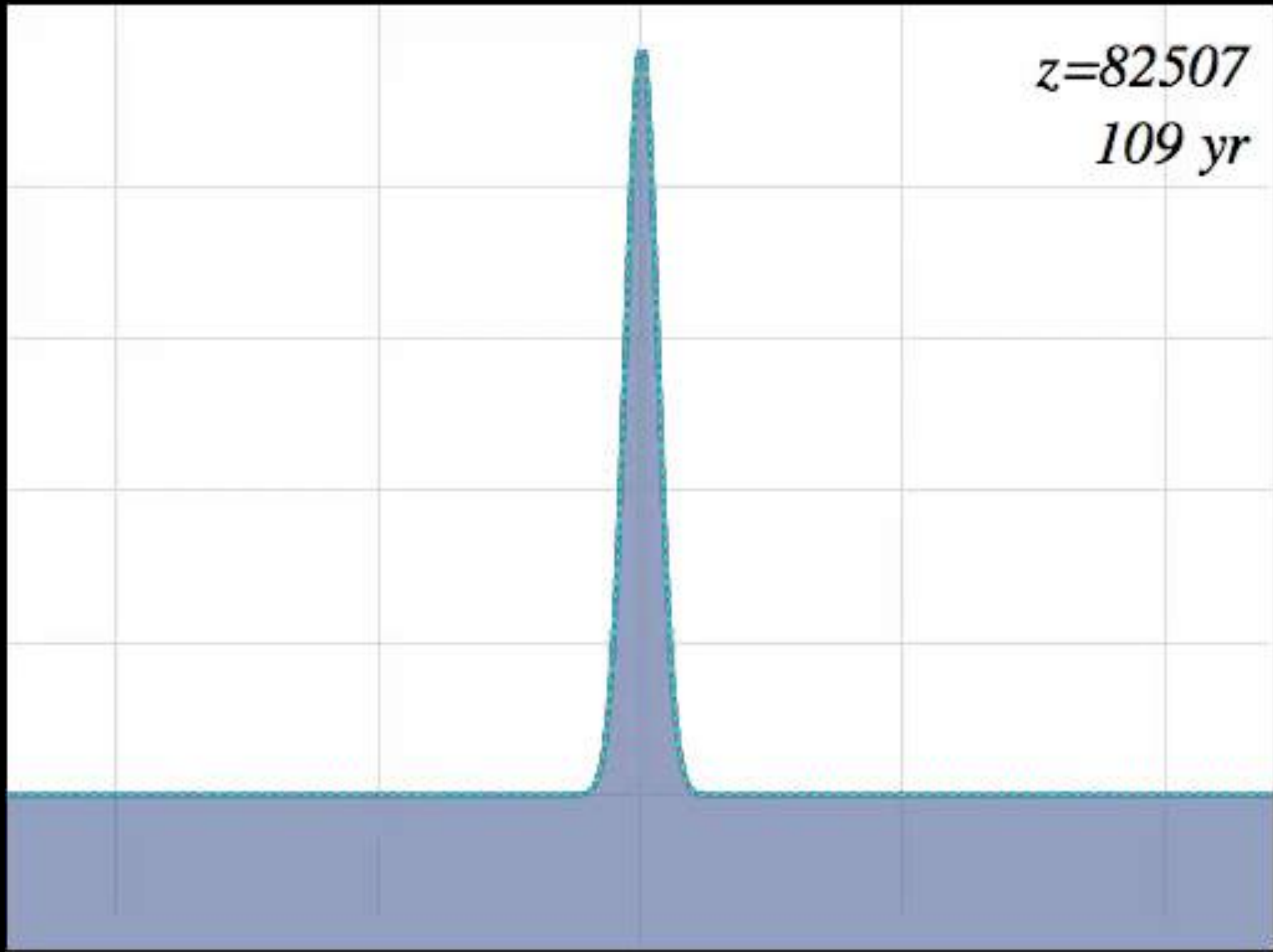
$z=82507$   
109 yr

Dark Matter

Baryons

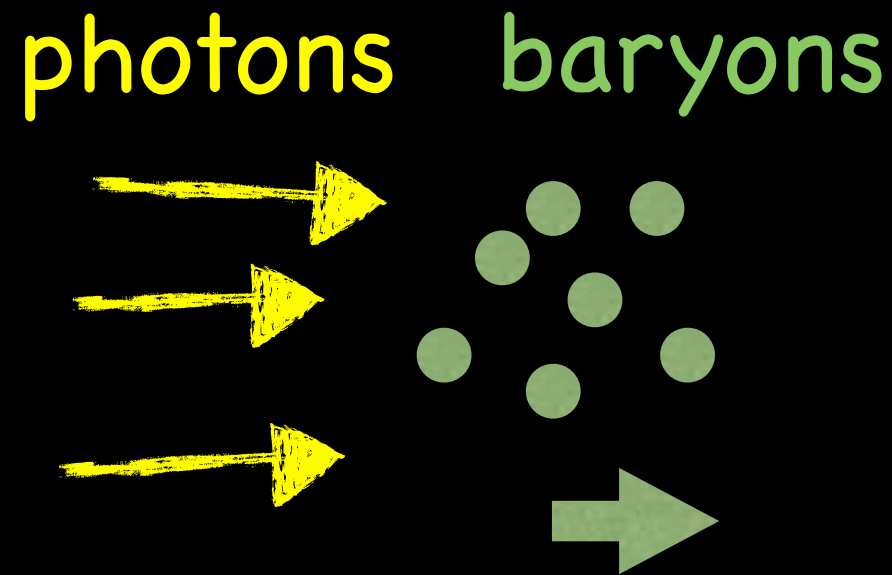
Neutrinos

Photons





Let's add some more substance, by taking into account the additional inertia that the baryons impose on photons due to scattering ("baryon drag")



This drag is proportional to the baryon/photon ratio

$$R_b \equiv \frac{(\rho_b + p_b)v_b}{(\rho_r + p_r)v_r} = \frac{\rho_b}{\rho_r + \frac{1}{3}\rho_r} = \frac{\rho_b}{\frac{4}{3}\rho_r} \simeq 31.5 \Omega_b h^2 \frac{10^3}{z}$$

The sound speed of this medium then becomes:

$$c_s^2(z) = \frac{1}{3} \frac{1}{1 + R_b(z)}$$

## Acoustic horizon at decoupling:

Observations:  
WMAP, Planck

$$z_{dec} \simeq 1090.5 \pm 1 \quad \longleftrightarrow \quad R_s(z_{dec}) = (146.8 \pm 1.8) \text{ Mpc}$$

## Acoustic horizon at "baryon drag"

Since we have  $\sim 10^9$  photons for each baryon (!!!), even after decoupling, even if the photons are not so affected by the baryons, the baryons do feel the drag of radiation, as it moves away from over-dense ("hot") regions and into under-dense ("cold") ones.

This drag ends shortly **after** decoupling:

Uncertainty in the  
prediction based on  
WMAP, Planck

$$z_{drag} \simeq 1020.5 \pm 1.6 \quad \longleftrightarrow \quad R_s(z_{drag}) = (153.3 \pm 2) \text{ Mpc}$$

This acoustic horizon, which can be predicted with **high accuracy** by observations of the CMB, shows up in the present **matter distribution**

