

Neural Networks

Simple ANNs



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Topics

- Perceptron
 - Basics
 - Training
 - Test
 - Example
- Adaline
 - Basics
 - Differences

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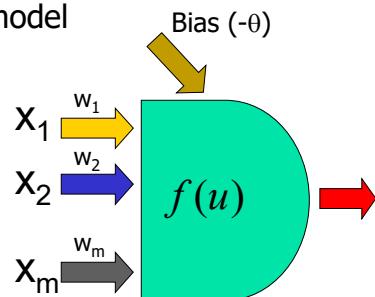
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Perceptron

- First ANN implementation
 - Rosemblat, 1958
 - McCulloch-Pitts neuron model
- Training
 - Supervised
 - Error correction
 - $w_i(t) = w_i(t-1) + \Delta w_i$
 - $\Delta w_i = \eta x_i \delta$
 - $\Delta w_i = \eta x_i (y - f(\mu))$
- Convergence theorem

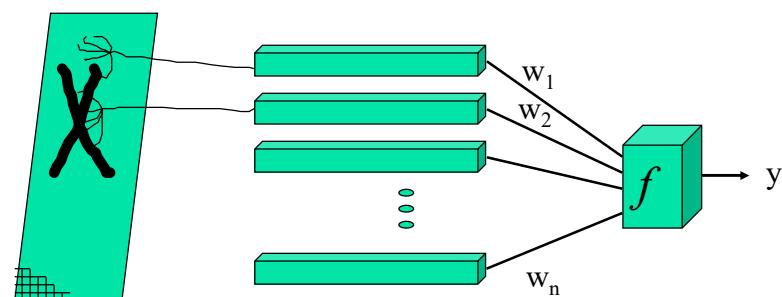


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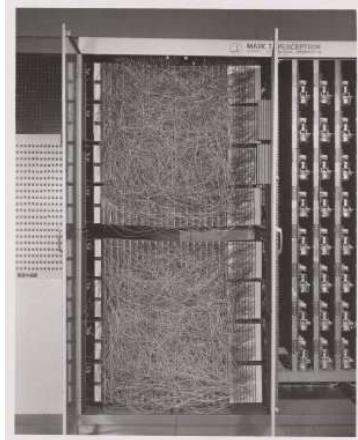
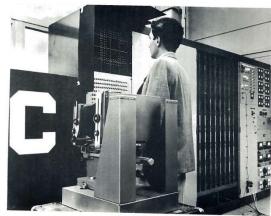
Perceptron architecture



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Perceptron implementation

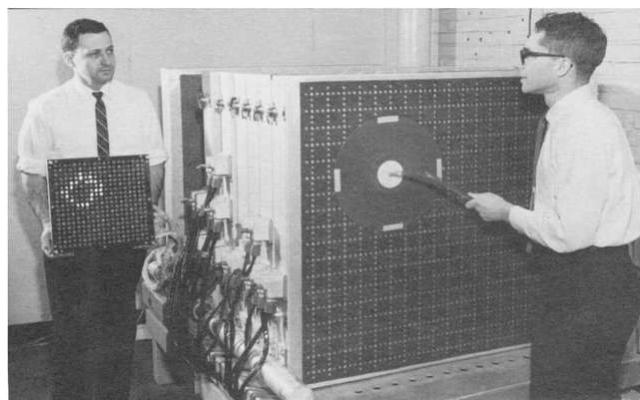
- First implementation:
 - Mark I Perceptron
 - Cornell Aeronautical Laboratory, USA



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Starting the implementation



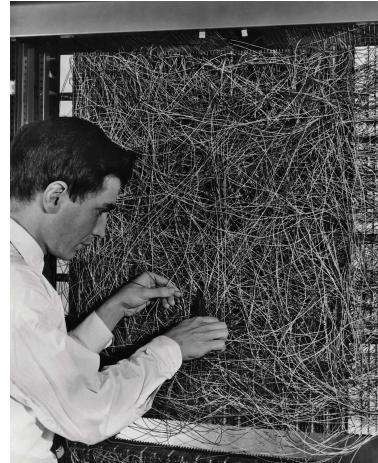
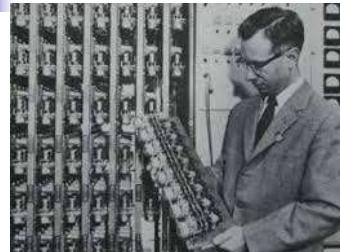
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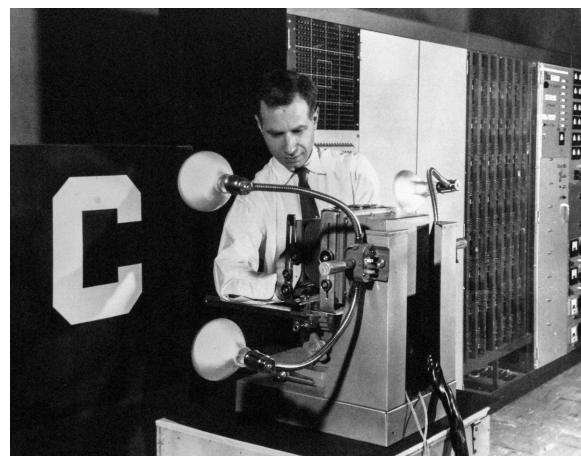
Preparing the Perceptron



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Concluding Perceptron

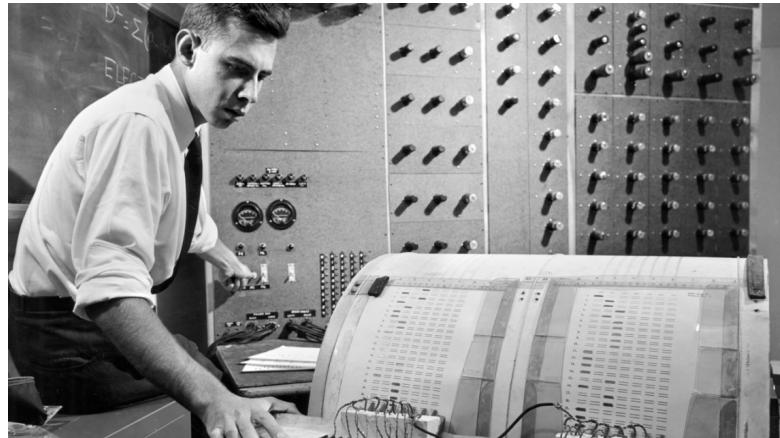


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Perceptron working



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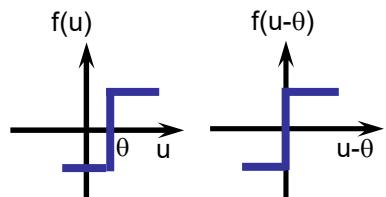
Perceptron

- Answer / network output
 - Applies threshold activation function on total input sum received by a neuron

$$u = \sum_{i=1}^m x_i w_i$$

$$f(u) = \begin{cases} +1 & \text{if } u \geq \theta \\ -1 & \text{if } u < \theta \end{cases}$$

$$net = \sum_{i=0}^m x_i w_i$$

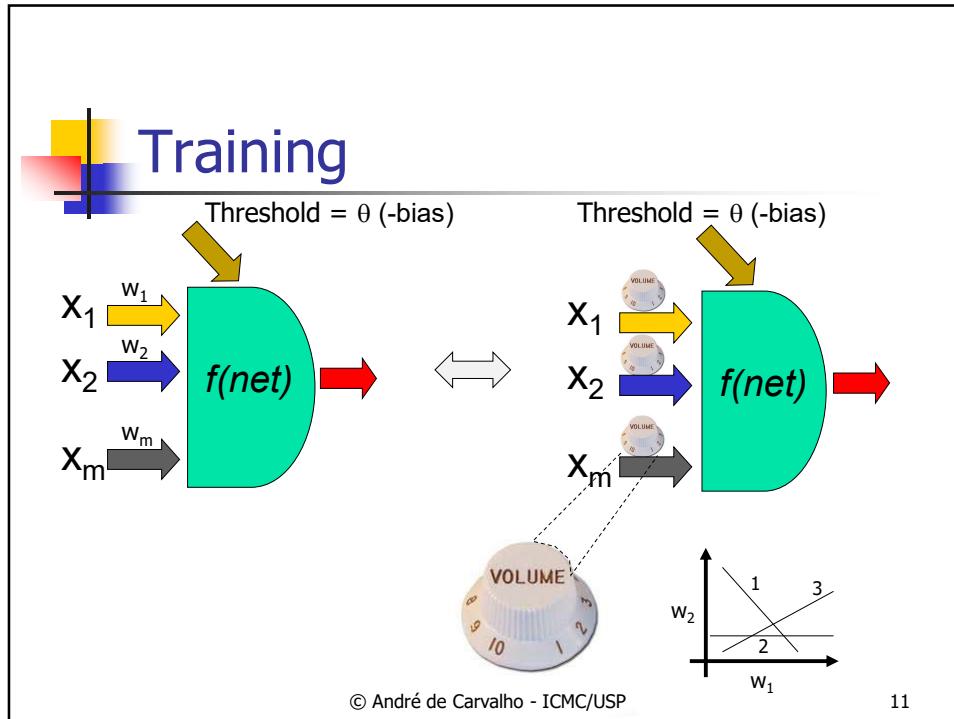


$$\begin{aligned} f(u-\theta) &= \text{sinal}(u-\theta) \\ f(net) &= f(u-\theta) \end{aligned}$$

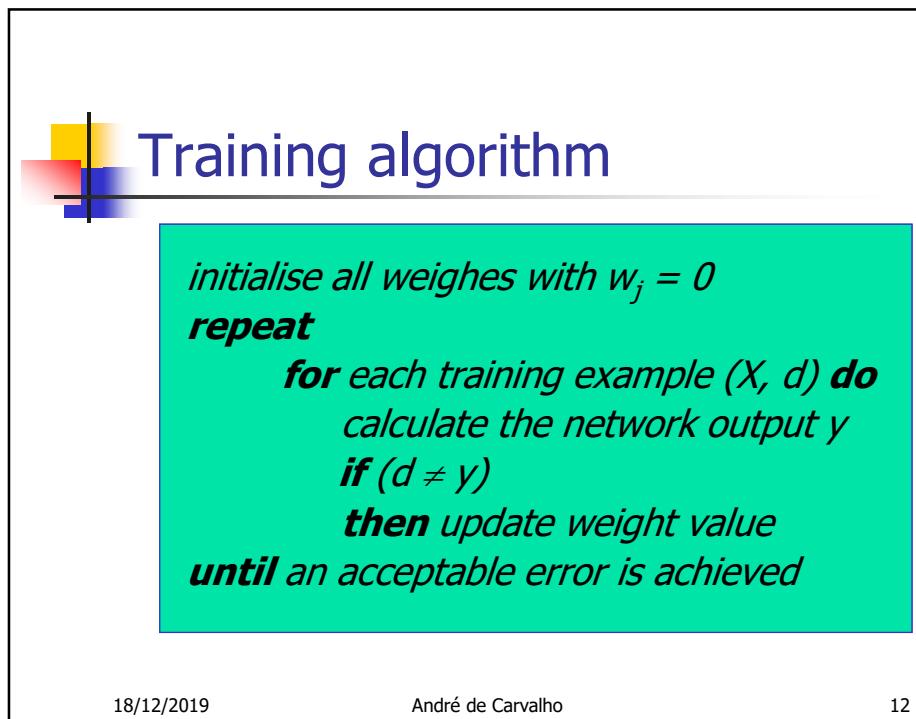
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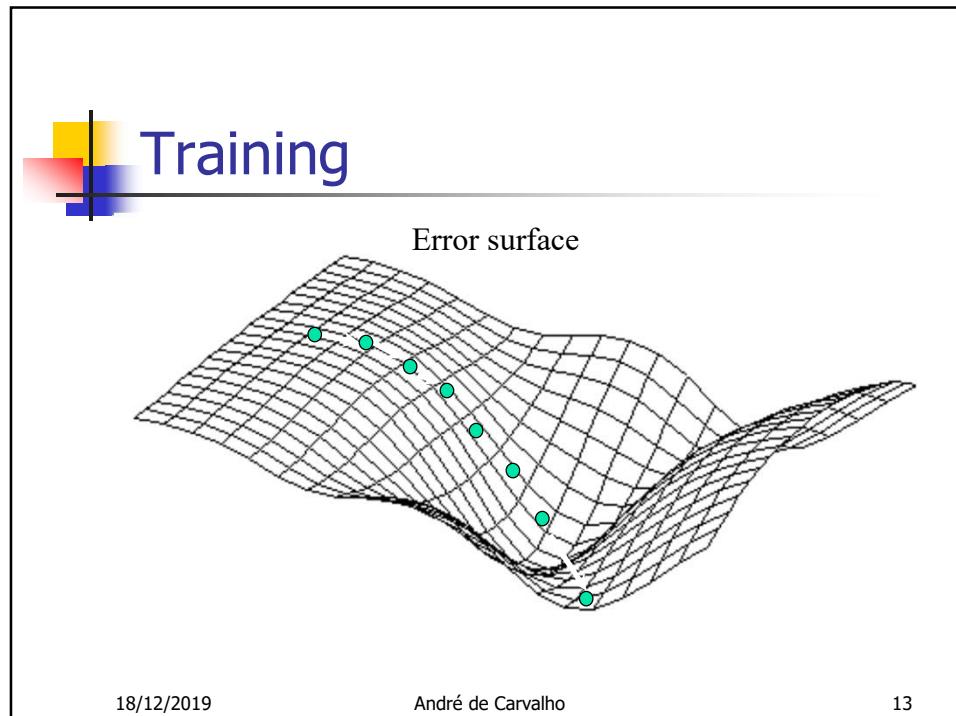
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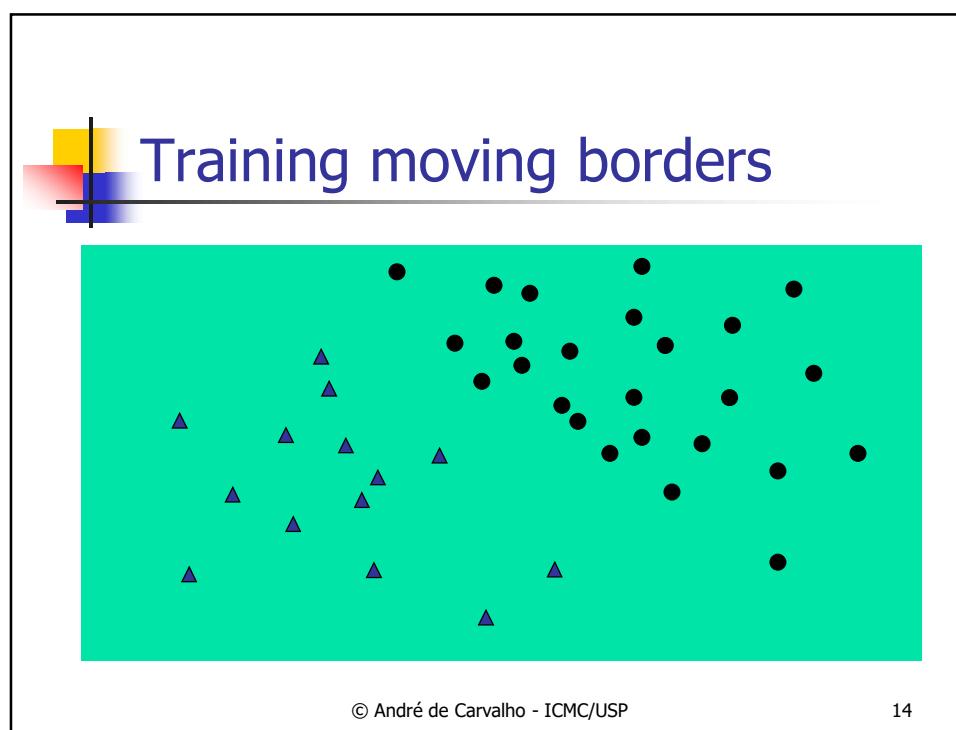
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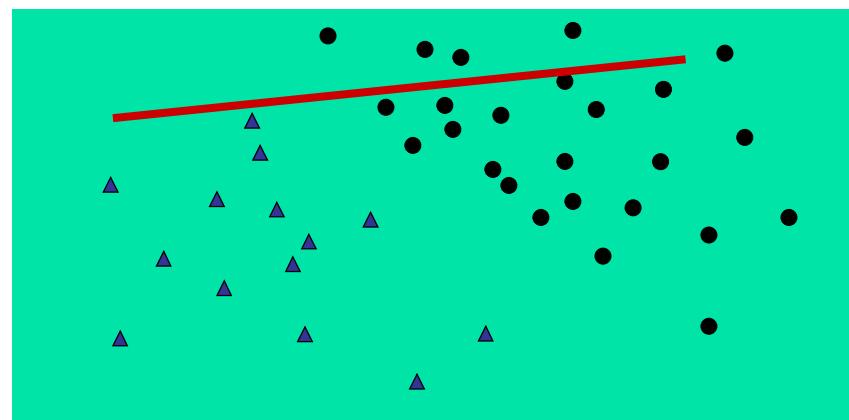


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Training moving borders

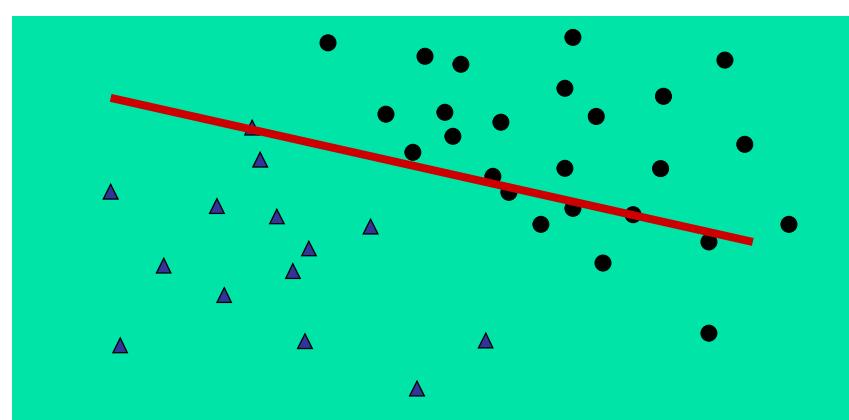


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Training moving borders

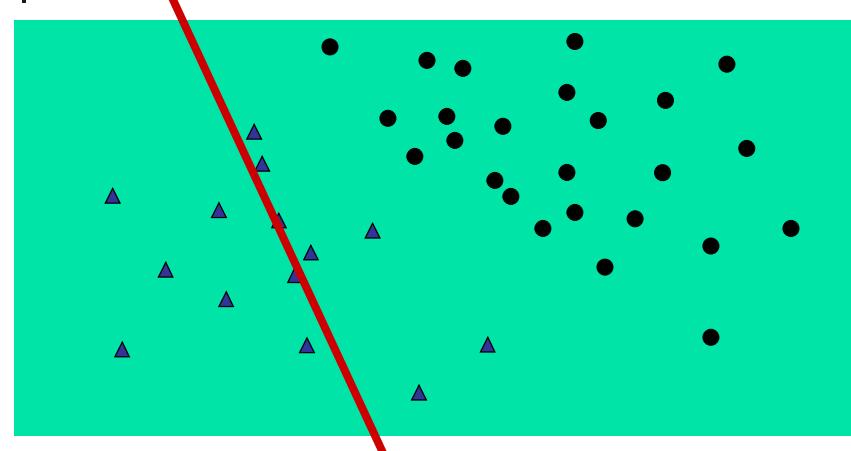


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Training moving borders

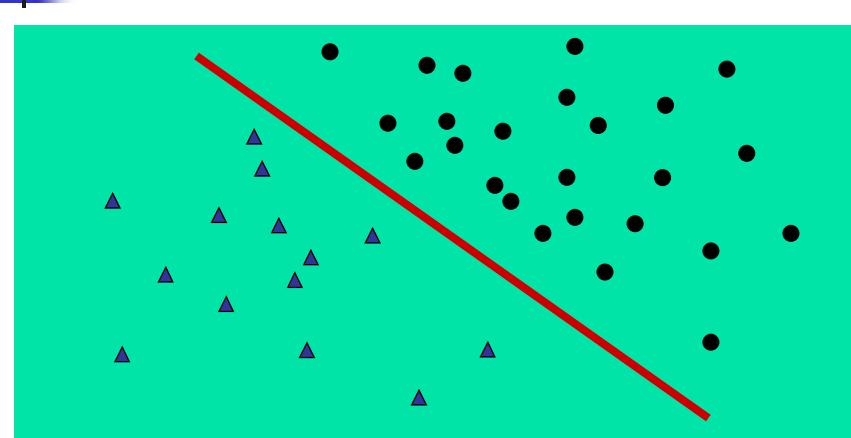


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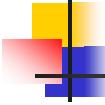
Training moving borders



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Test

```

for each test example  $X$  do
    present  $X$  to the network input
    calculate network output  $y$ 
    if ( $y = -1$ )
        then  $X \in$  class A
    else  $X \in$  class B

```

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Example

- Given a Perceptron network with:
 - Three input terminals, using the following initial weights $w_0 = 0,4$, $w_1 = -0,6$ e $w_2 = 0,6$, and threshold $\theta = 0,5$:
 - Teach the networks with the training dataset (001, -1) and (110, +1)
 - Using as learning rate $\eta = 0,4$
 - Define the class for the samples: 111, 000, 100 e 011

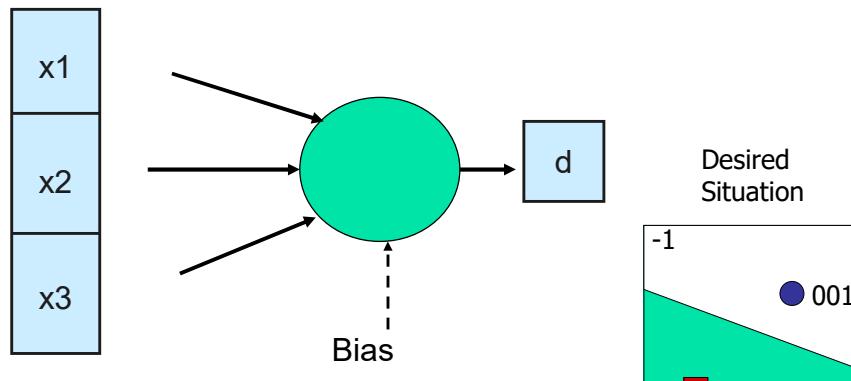
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Example



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Example: item a)

a) Train the network

a.1) For the input pattern 001 $(d = -1)$

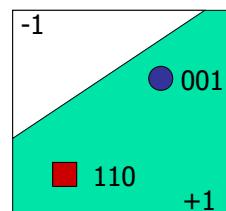
Step 1: define the network output

$$u = 0(0.4) + 0(-0.6) + 1(0.6) - 1(0.5) = 0.1 \\ y = u = +1 \text{ (since } 0.1 \geq 0\text{)}$$

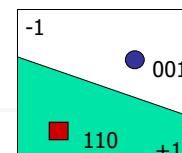
Step 2: adjust weights ($d \neq y$)

$$w_0 = 0.4 + 0.4(0)(-1 - (+1)) = 0.4 \\ w_1 = -0.6 + 0.4(0)(-1 - (+1)) = -0.6 \\ w_2 = 0.6 + 0.4(1)(-1 - (+1)) = -0.2 \\ w_3 = 0.5 + 0.4(-1)(-1 - (+1)) = 1.3$$

Current Situation



Desired Situation

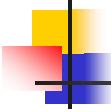


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 **Example: item a)**

a) Train the network

a.2) For the input pattern 110 ($d = +1$)

Step 1: define the network output

$$u = 1(0.4) + 1(-0.6) + 0(-0.2) -1(1.3) = -1.5$$

$$y = u = -1 \text{ (since } -1.5 < 0\text{)}$$

Step 2: adjust weights ($d \neq y$)

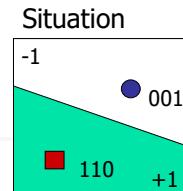
$$w_0 = 0.4 + 0.4(1)(1 - (-1)) = 1.2$$

$$w_1 = -0.6 + 0.4(1)(1 - (-1)) = 0.2$$

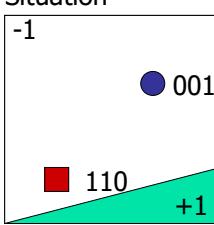
$$w_2 = -0.2 + 0.4(0)(1 - (-1)) = -0.2$$

$$w_3 = 1.3 + 0.4(-1)(1 - (-1)) = 0.5$$

Desired Situation



Current Situation



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 **Example: item a)**

a) Train the network

a.3) For the input pattern 001 ($d = -1$)

Step 1: define the network output

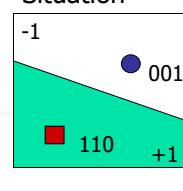
$$u = 0(1.2) + 0(0.2) + 1(-0.2) -1(0.5) = -0.7$$

$$y = u = -1 \text{ (since } -0.7 < 0\text{)}$$

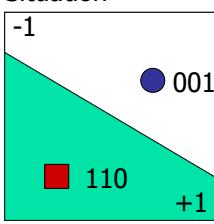
Step 2: adjust weights ($d = y$)

Since $d = y$, there is no need to adjust the weights

Desired Situation



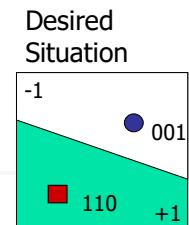
Current Situation



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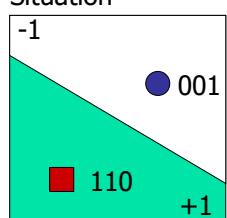
Example: item a)



a) Train the network

a.4) For the input pattern 110 (d = +1)

Current Situation



Step 1: define the network output

$$u = 1(1.2) + 1(0.2) + 0(-0.2) -1(0.5) = +0.7$$

$$y = u = +1 \text{ (since } 0.7 > 0\text{)}$$

Step 2: adjust weights (d = y)

Since d = y, there is no need to adjust the weights

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Example: item b)

b) Test the network

b.1) For the input pattern 111

$$u = 1(1.2) + 1(0.2) + 1(-0.2) -1(0.5) = 0.7$$

$$y = u = 1 \text{ (since } 0.7 \geq 0\text{)} \Rightarrow \text{class 1}$$

b.2) For the input pattern 000

$$u = 0(1.2) + 0(0.2) + 0(-0.2) -1(0.5) = -0.5$$

$$y = u = -1 \text{ (since } -0.5 < 0\text{)} \Rightarrow \text{class 0}$$

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Example: item b)

b) Test the network

b.3) For the input pattern 100

$$u = 1(1.2) + 0(0.2) + 0(-0.2) + 1(-0.5) = 0.7$$

$y = u = 1$ (since $0.7 \geq 0$) \Rightarrow class 1

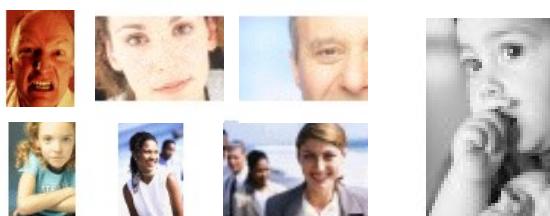
b.4) For the input pattern 011

$$u = 0(1.2) + 1(0.2) + 1(-0.2) - 1(0.5) = -0.5$$

$y = u = -1$ (since $-0.5 < 0$) \Rightarrow class 0

Example 2

- Distinguish male face images from female face images



Example 2

- Distinguish male face images from female face images
 - Use images directly
 - Matrix of pixels
 - Use features extracted from the image
 - Distance between components from the face (Ex. eyes)
 - Texture
 - Moustache, Hair, Beard

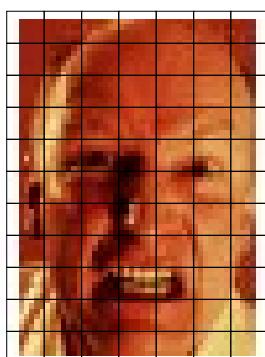
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Example 2



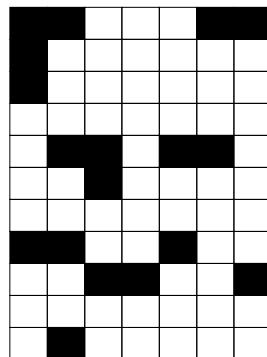
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Example 2



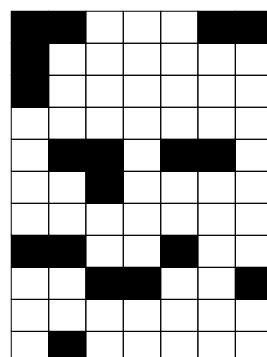
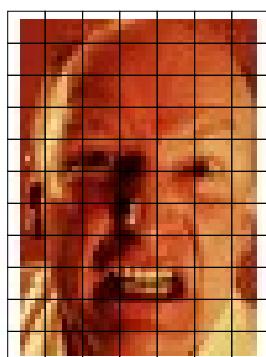
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Example 2



```
1 1 0 0 0 1 1  
1 0 0 0 0 0 0  
1 0 0 0 0 0 0  
0 0 0 0 0 0 0  
0 1 1 0 1 1 0  
0 0 1 0 0 0 0  
0 0 0 0 0 0 0  
1 1 0 0 1 0 0  
0 0 1 1 0 0 1  
0 0 0 0 0 0 0  
0 1 0 0 0 0 0
```



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Example 3

- Consider the following patients

Name	Fever	Dizzy	Spots	Pain	Diagnosis
John	yes	yes	small	yes	ill
Peter	no	no	large	no	healthy
Mary	yes	yes	small	no	healthy
Joe	yes	no	large	yes	ill
Ann	yes	no	small	yes	healthy
Lyn	no	no	large	yes	ill

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Example 3

- Consider the following patients

Fever	Dizzy	Spots	Pain	Diagnosis
1	1	0	1	1
0	0	1	0	0
1	1	0	0	0
1	0	1	1	1
1	0	0	1	0
0	0	1	1	1

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Example 3

- Train a Perceptron network to distinguish:
 - Potentially healthy patients
 - Potentially ill patients
- Test the network for the following new cases
 - (Louis, no, no, small, yes)
 - (Laura, yes, yes, large, yes)

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Adaline

- Problem with Perceptron:
 - Weight adjustment does not take into account the true distance between
 - Produced output and desired output
- Adaline network
 - Proposed by Widrow and Hoff in 1960
 - Also based on McCulloch-Pitts nodes

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Adaline

- Training

- Supervised

- Error correction (LMS, delta rule)

- $\Delta w_{ij} = \eta x_i(d_j - y_j) \quad (d \neq y)$

- $\Delta w_{ij} = 0 \quad (d = y)$

- Gradual weight adjustment

- Takes into account the distance between the desired output (d) and the produced output (y)

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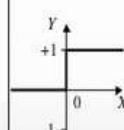
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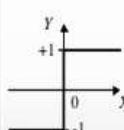
Activation functions

Step function



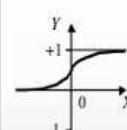
$$y^{step} = \begin{cases} 1, & \text{if } X \geq 0 \\ 0, & \text{if } X < 0 \end{cases}$$

Sign function



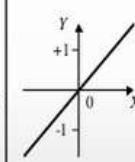
$$y^{sign} = \begin{cases} +1, & \text{if } X \geq 0 \\ -1, & \text{if } X < 0 \end{cases}$$

Sigmoid function



$$y^{sigmoid} = \frac{1}{1+e^{-X}}$$

Linear function

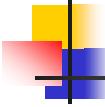


$$y^{linear} = X$$

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Quiz 1

- What is the main difference between Perceptron and Adaline?
 - A) Learning rule
 - B) Architecture
 - C) Activation function
 - D) Learning paradigm

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A bit of history

- (1969) Minsky & Papert analysed the Perceptron network and pointed out its limitations
 - Could only deal with linear separable problems
 - Not with XOR and parity
 - Largely reduced the research activity in ANNs

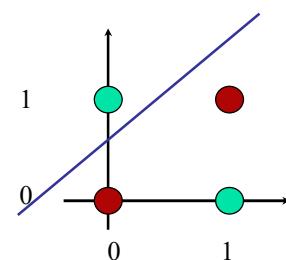
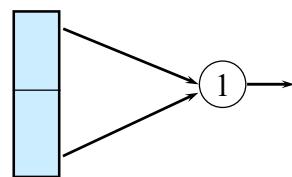
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Perceptron limitation

$$\begin{array}{l}
 0, 0 \rightarrow 0 \\
 0, 1 \rightarrow 1 \\
 1, 0 \rightarrow 1 \\
 1, 1 \rightarrow 0
 \end{array}$$



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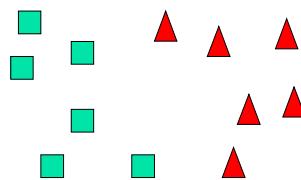
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Perceptron

- Linearly separable patterns



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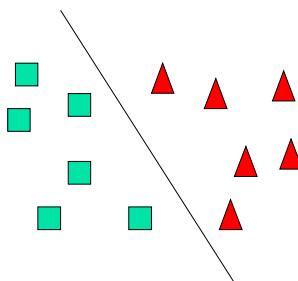
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Perceptron

- Linearly separable patterns



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Perceptron limitation

- One-layer networks can only deal with linearly separable problems
- A large number of important application problems are non-linearly separable
- Many problems have more than 2 classes
 - Multiclass problems

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Quiz 2

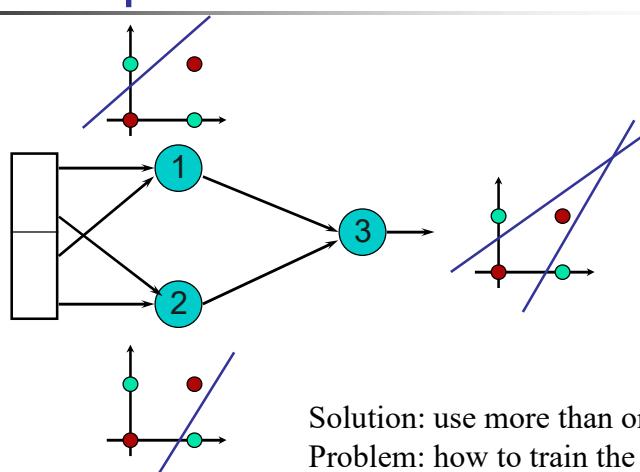
- What is the main difference between Perceptron and Adaline?
 - A) Learning rule
 - B) Architecture
 - C) Activation function
 - D) Learning paradigm

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Perceptron limitation



Solution: use more than one layer
 Problem: how to train the first layers

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MLP Neural Networks

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