# Five Lectures on Dark Matter

**First Lecture** 

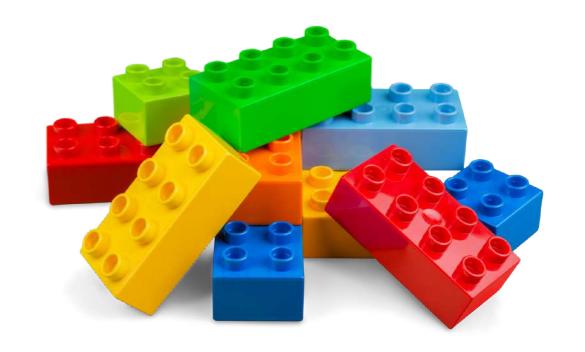




Francesco D'Eramo

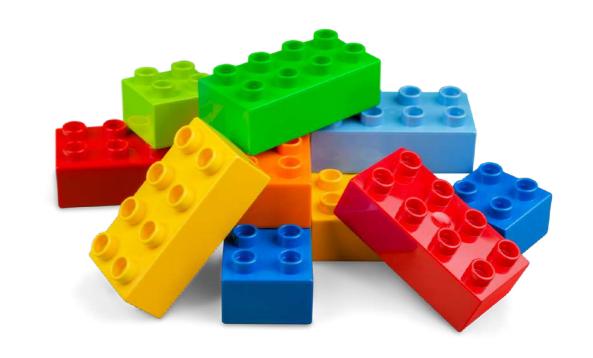
# The Big Question

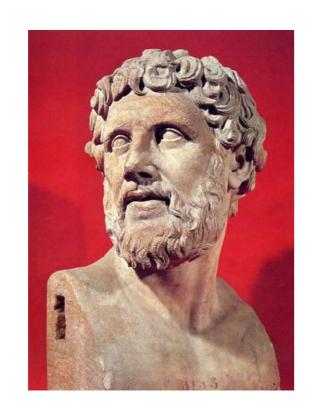
What are the building blocks of our Universe?



# The Big Question

What are the building blocks of our Universe?

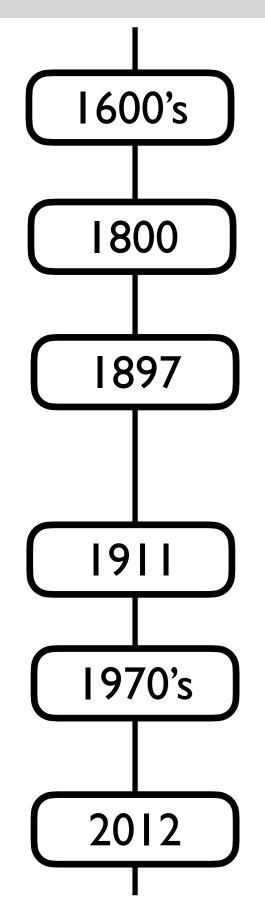




Atomic theory by Democritus (400 BC)

This question has been around for a while!

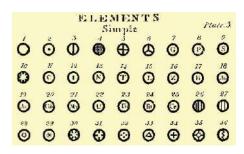
# **A Very Slow Progress**





Scientific method by G. Galilei

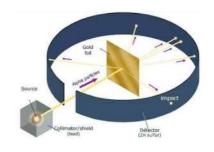
Experimental evidence for atoms by J. Dalton





Electron discovery by J. J. Thomson (atom not invisible!)

Discovery of the nucleus by E. Rutherford

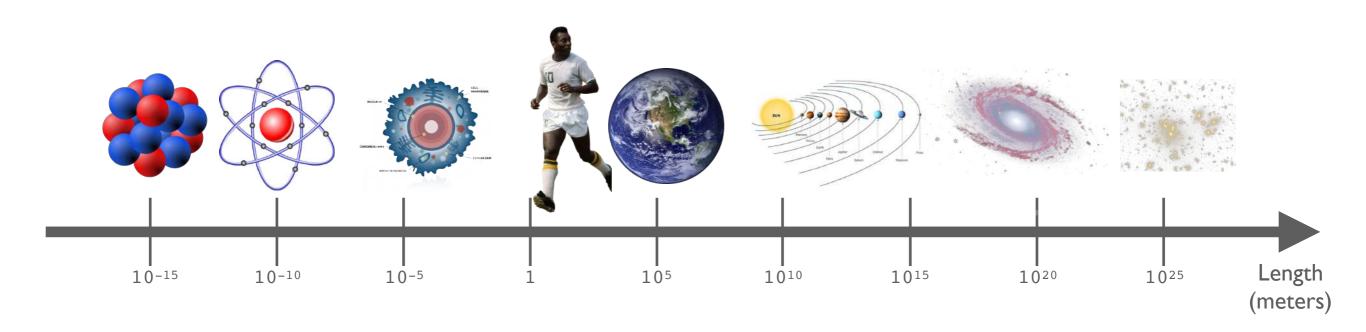


Zoo of elementary particles and the Standard Model

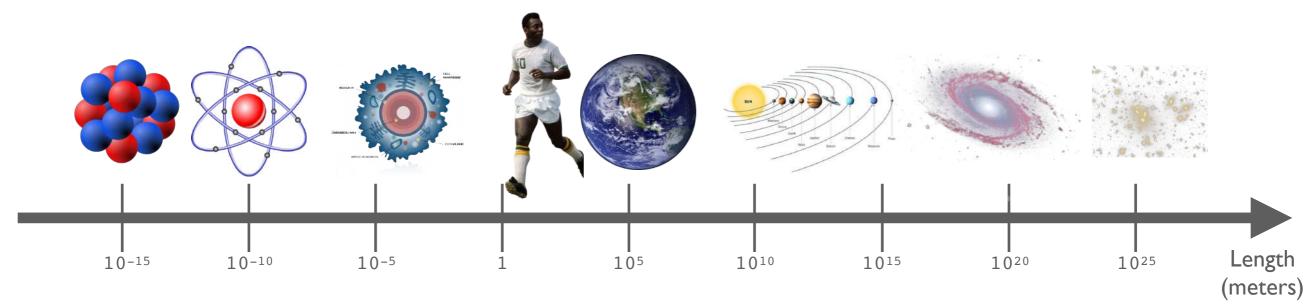


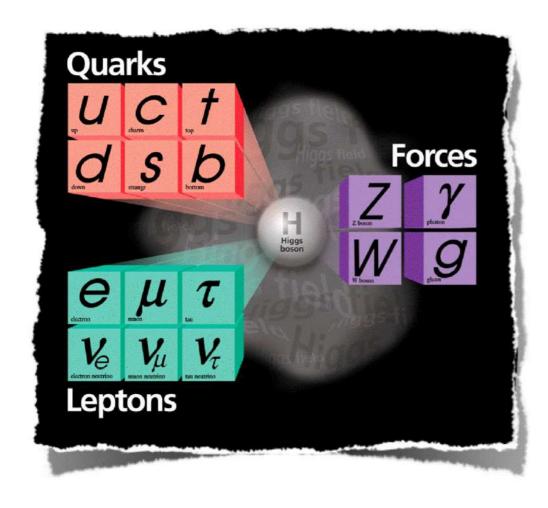
Higgs boson discovery (Standard Model is complete!)

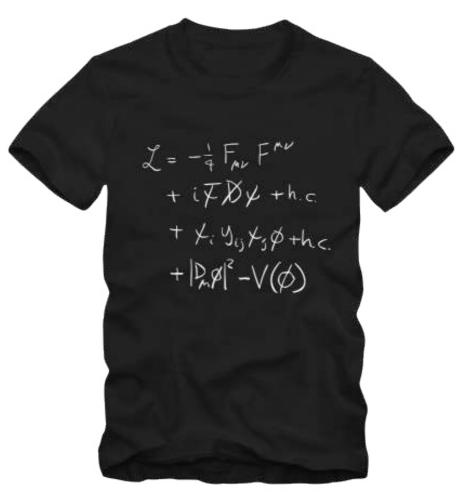
# A Magnificent Unified Description



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#### Is the Game Over?

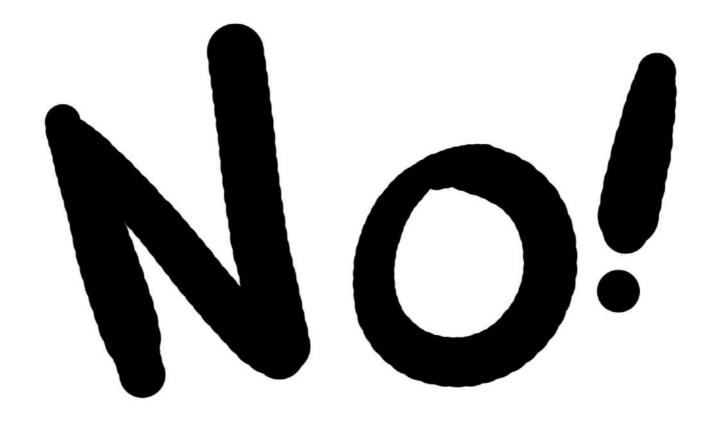
Have we finally found an answer to the question asked by Democritus more than 2000 years ago?

Can we declare victory?

#### Is the Game Over?

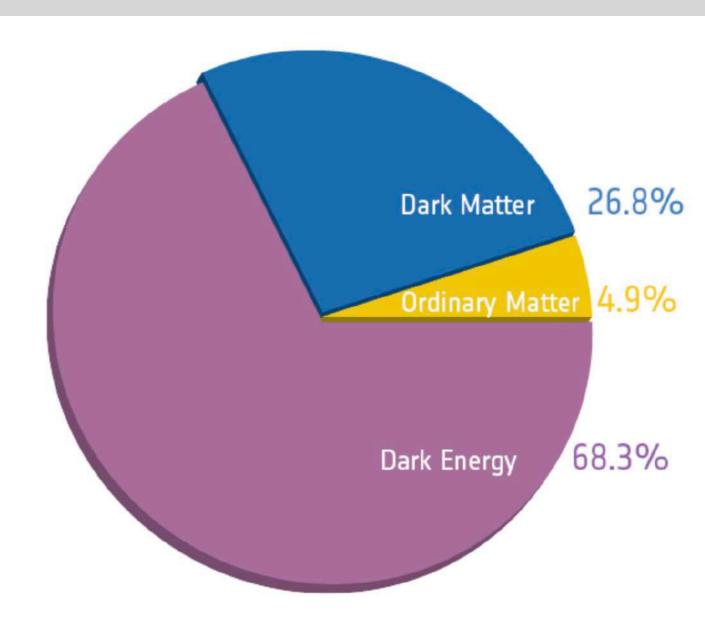
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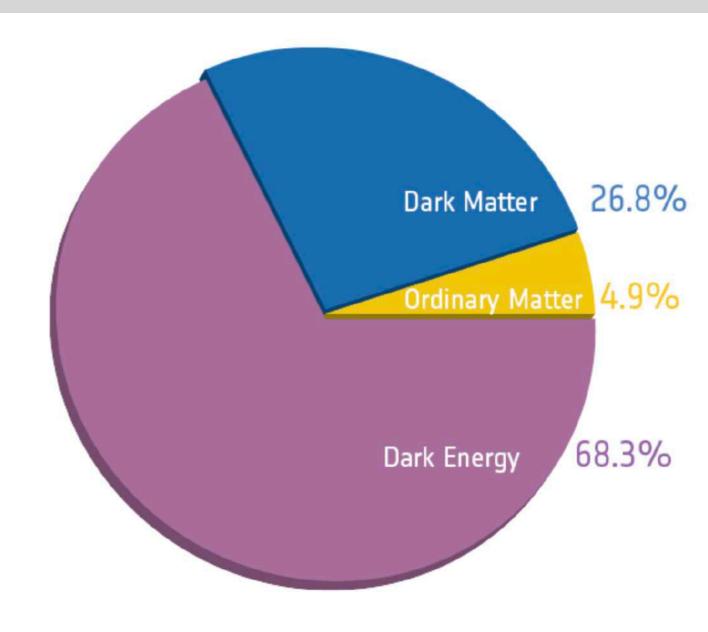
#### **Dark Matter**

Standard Model matter: approximately 5% of the current energy budget



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In this five lectures we deal with dark matter

We will review its evidence, theories and experimental searches

# Looking at the Invisible?

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Observe very carefully the motion of visible objects

Using laws of gravity we find the gravitational potential  $\Phi$ 



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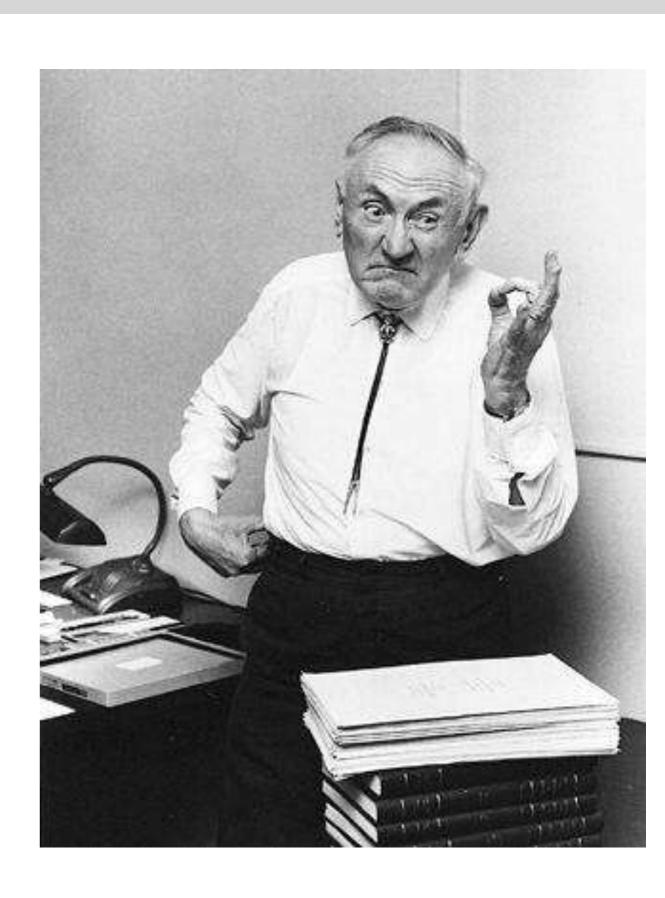
Infer <u>total</u> amount of matter (visible and invisible)

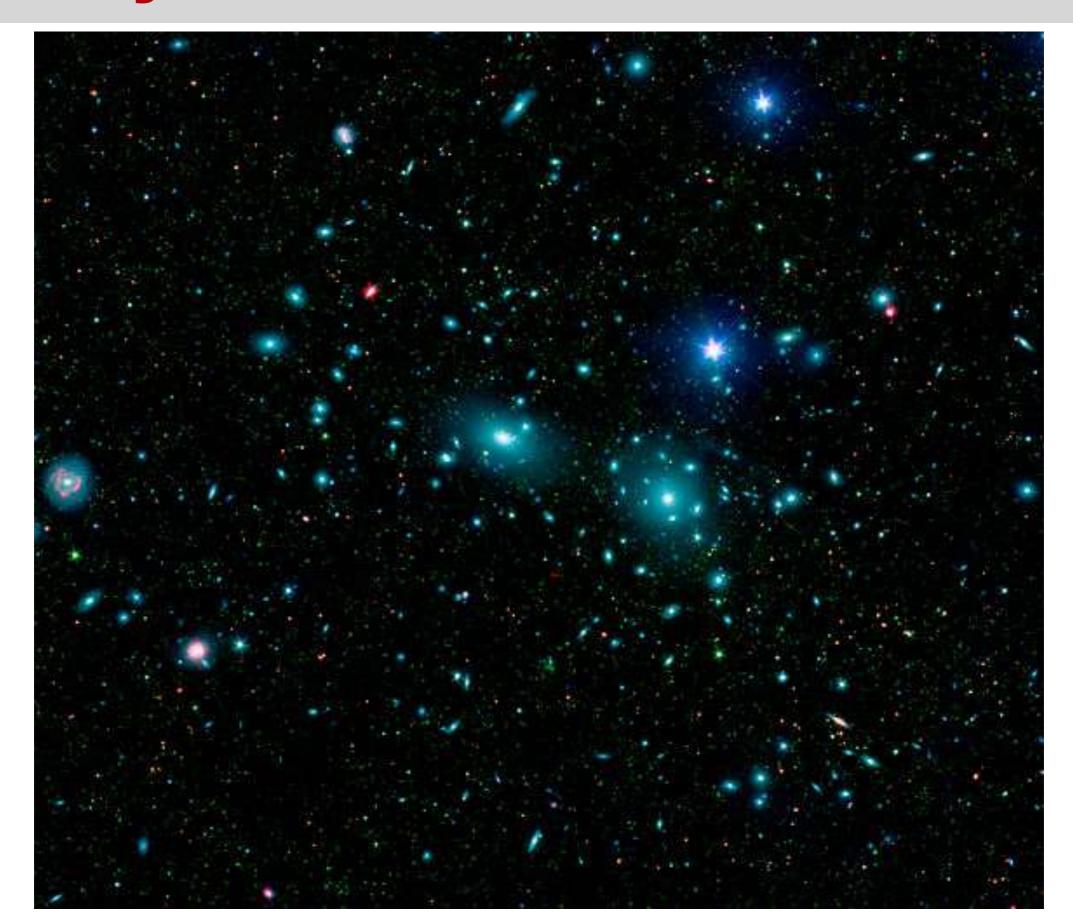
$$\nabla^2 \Phi = -4\pi G_N \rho$$

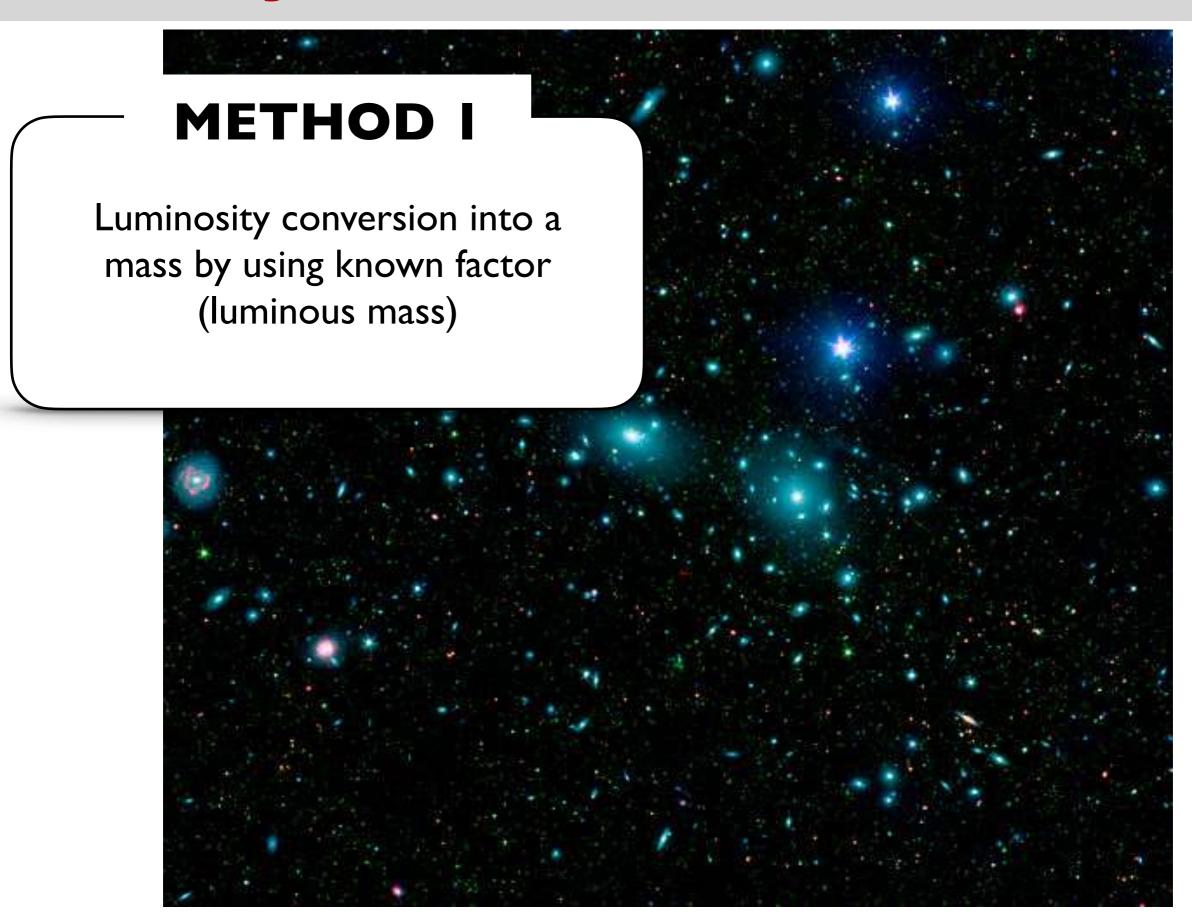
#### Fritz Zwicky (1930's)

Careful observation of galaxies within the Coma Cluster

Two independent measurement of the cluster mass... surprise!







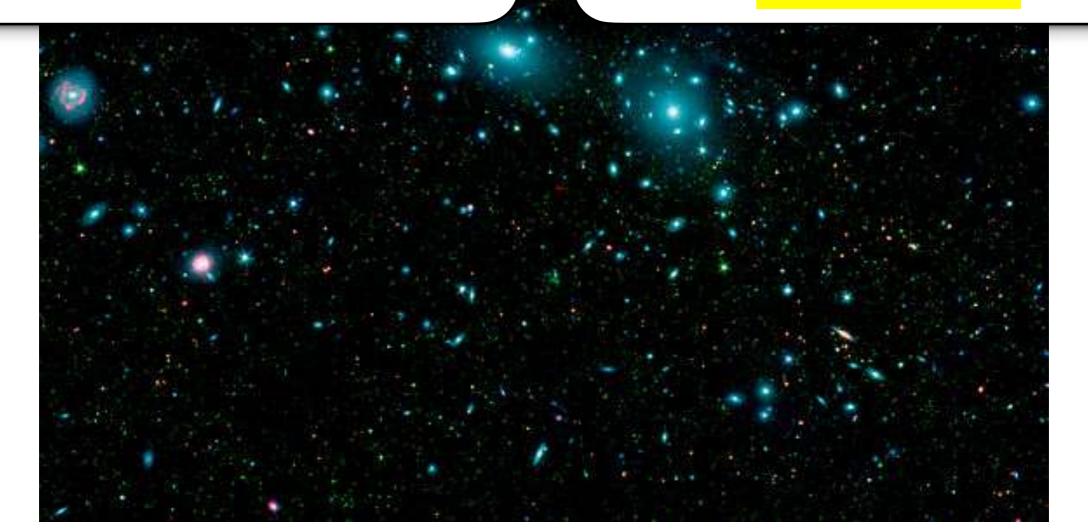
#### **METHOD I**

Luminosity conversion into a mass by using known factor (luminous mass)

#### METHOD II

Observation of galaxy velocities and derivation of the potential (gravitational mass)

PROBLEM I



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PROBLEM I

#### Mass deficit!

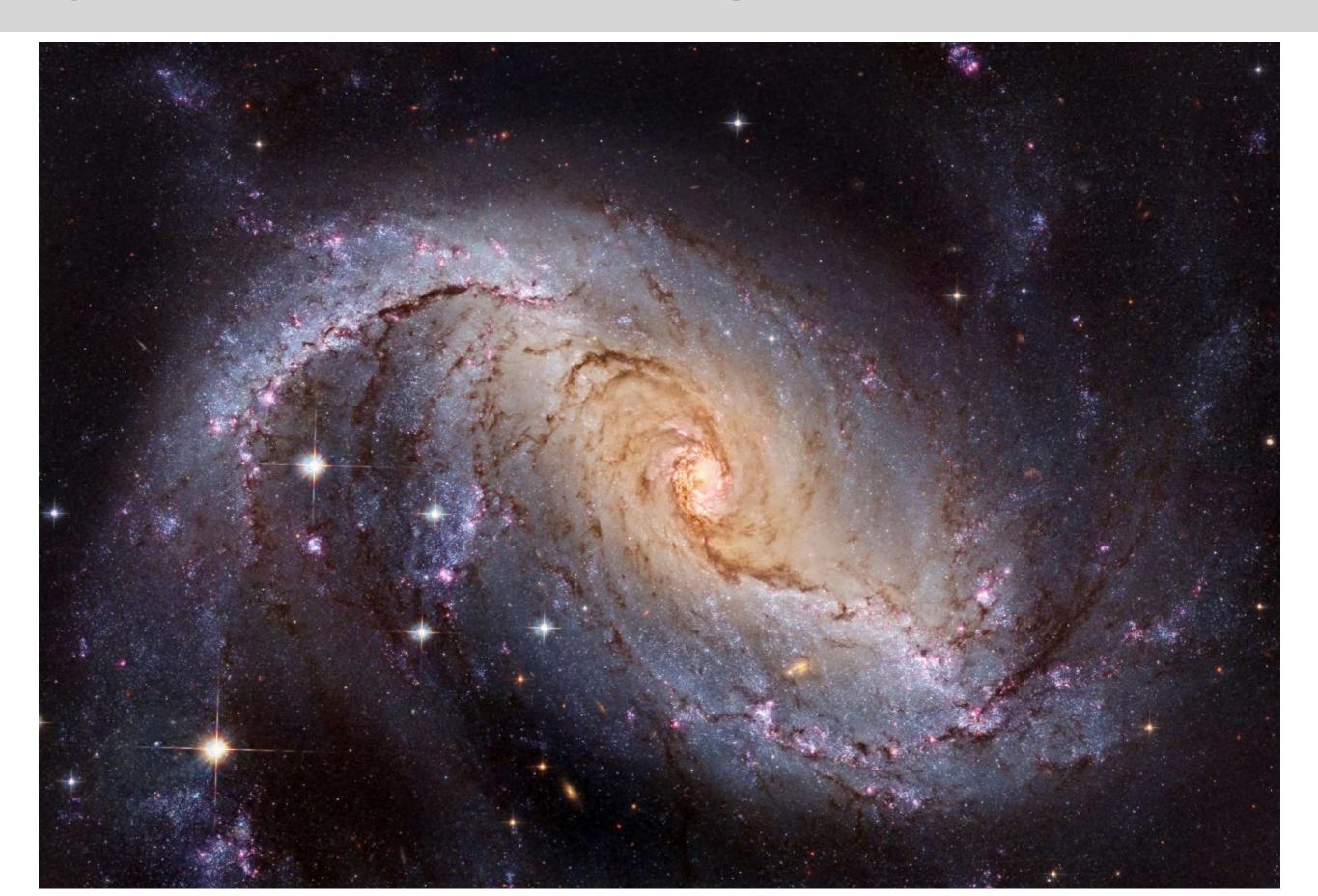
$$M_{\mathrm{Coma}}^{(grav)} \gg M_{\mathrm{Coma}}^{(vis)}$$

Vera Rubin (1970's)

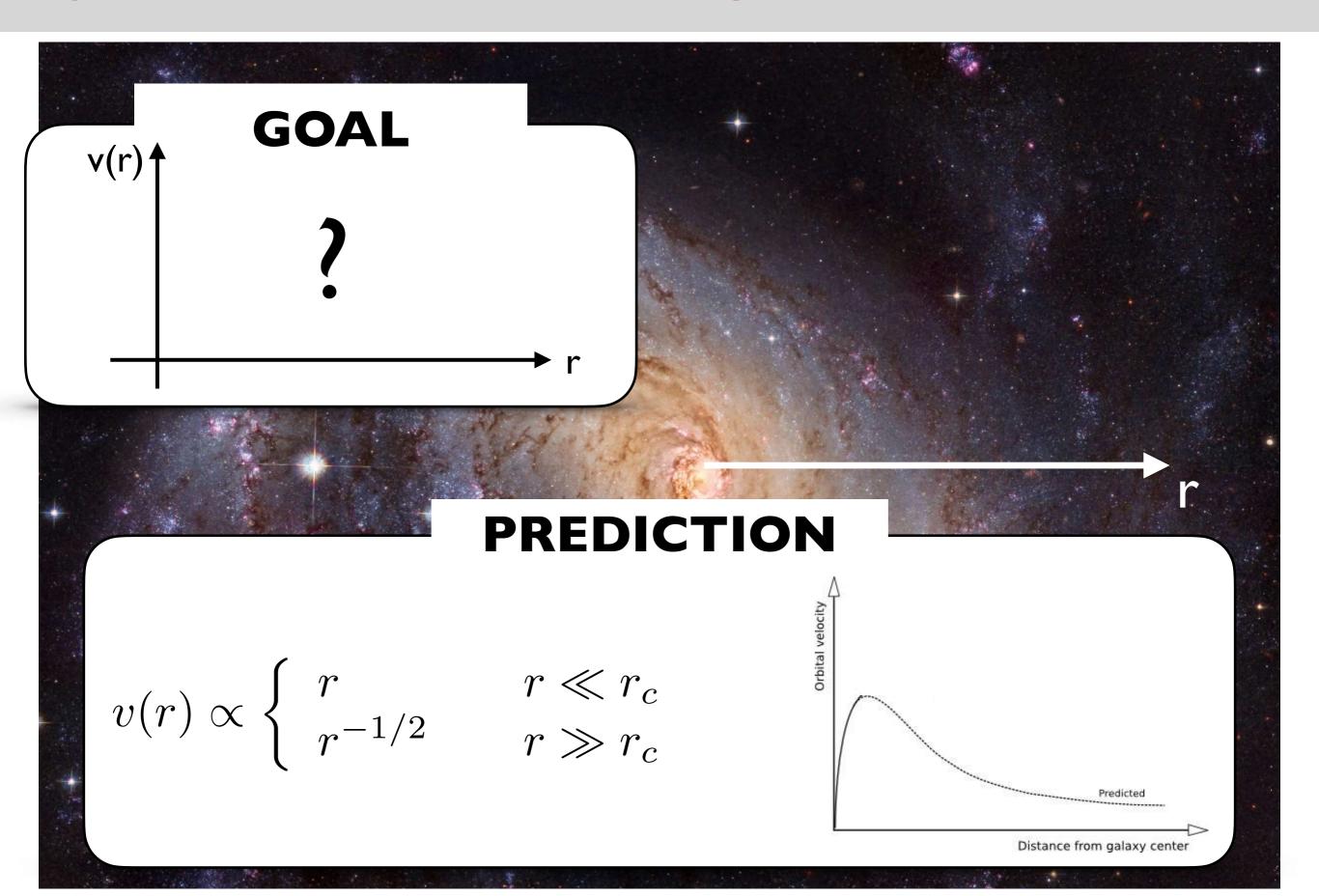
Careful observation of stellar motion within spiral galaxies

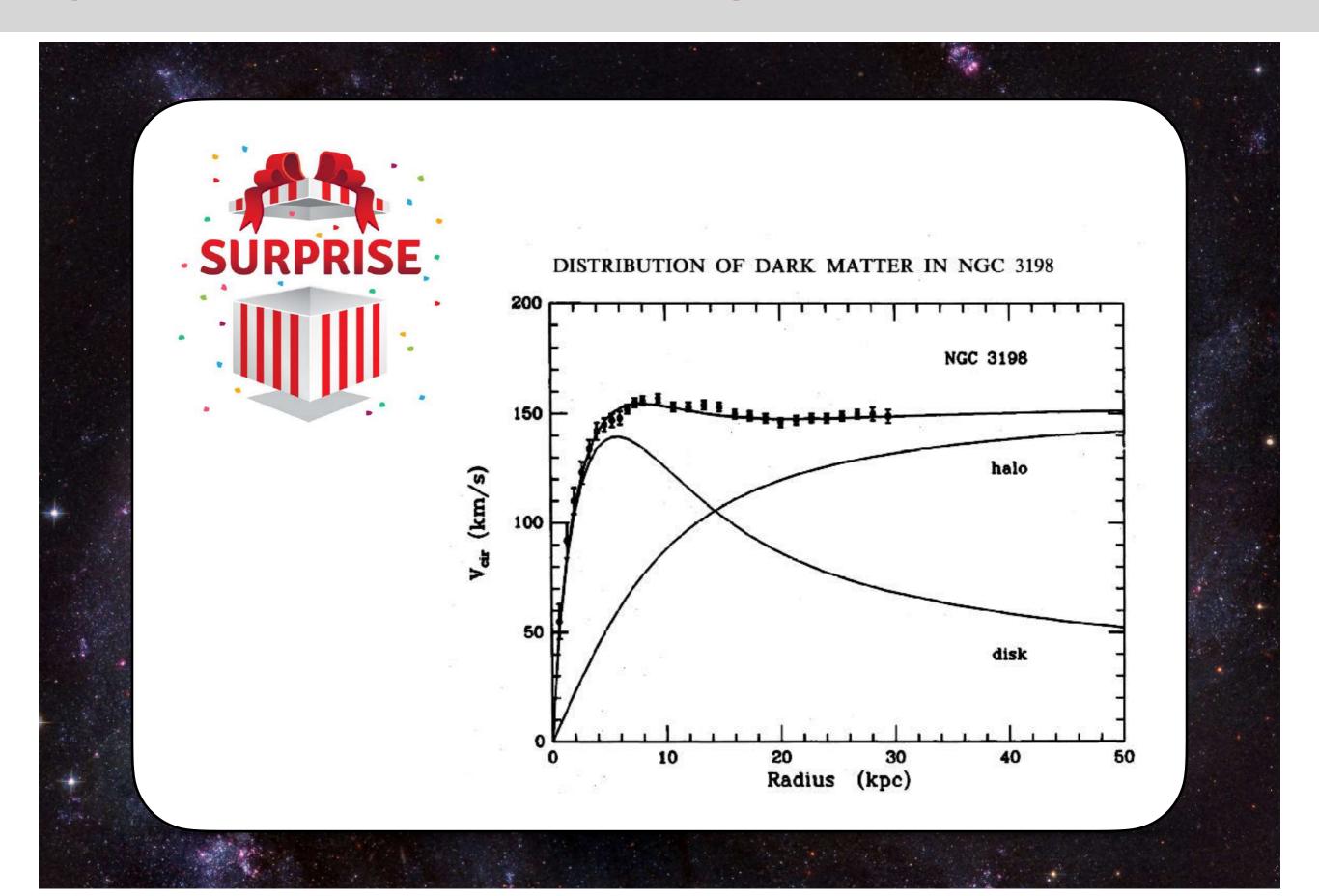
Comparison with expectation based on visible mass... surprise!



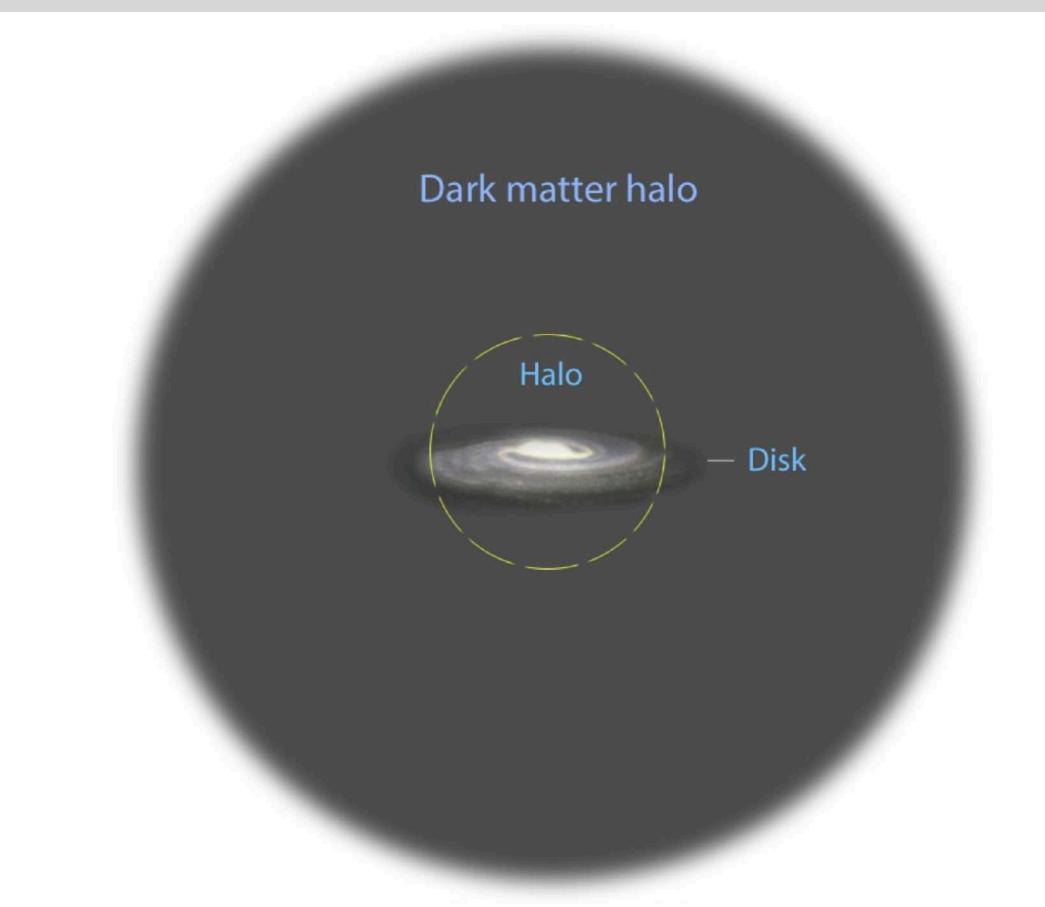






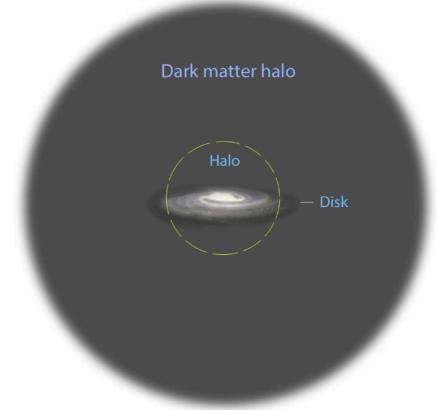


### **A Dark Matter Halo**



#### **A Dark Matter Halo**

$$m \frac{v^2(r)}{r} = \frac{G_N M(r) m}{r^2} \quad \Rightarrow \quad \rho_{\text{halo}} \propto r^{-2}$$



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#### N-body simulations

Isothermal: 
$$\rho_{\rm DM}^{\rm isothermal}(r) = \frac{\rho_0}{1 + (r/r_c)^2}$$

NFW: 
$$\rho_{\rm DM}^{\rm NFW}(r) = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}$$

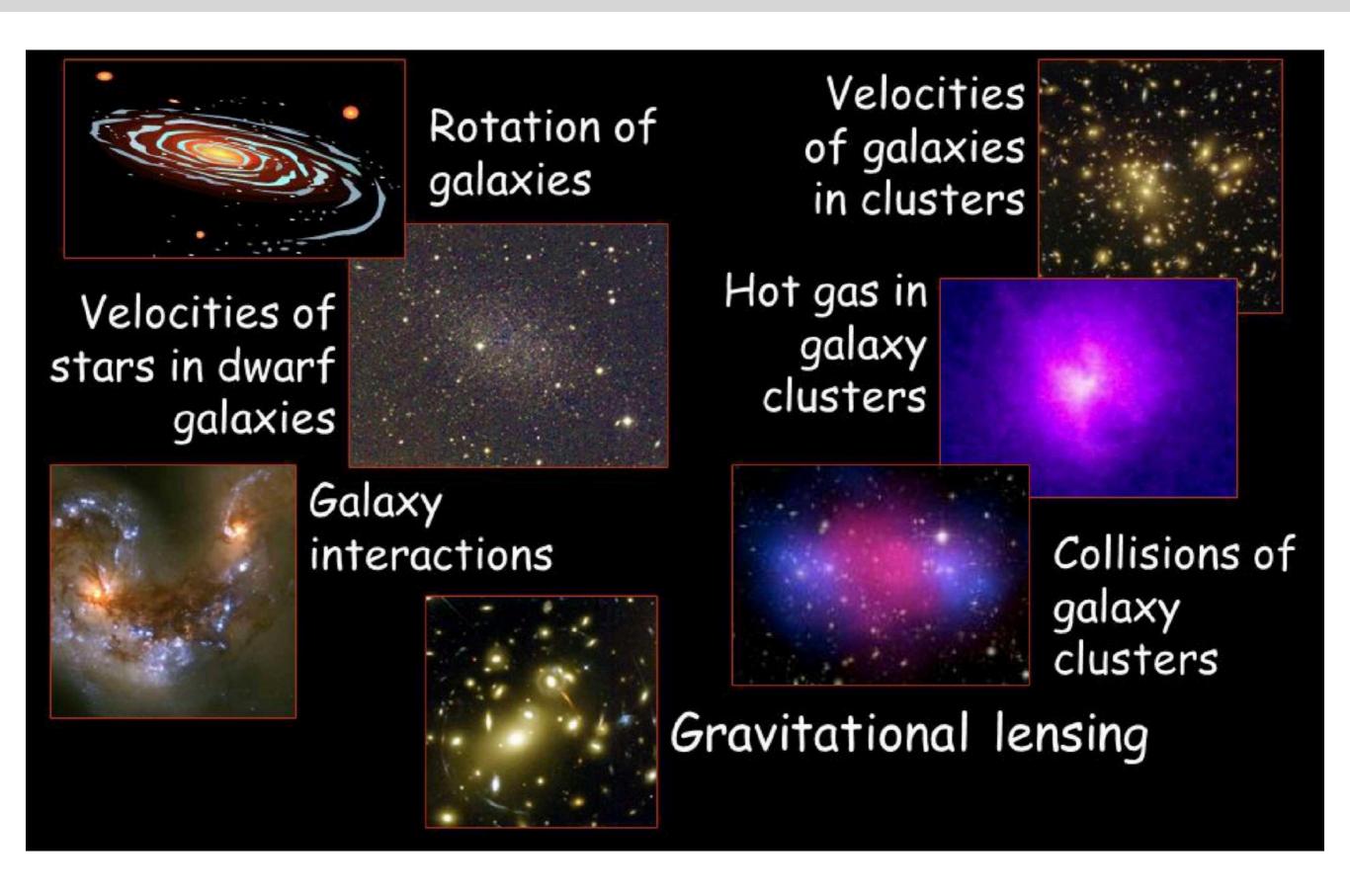
Einasto: 
$$\rho_{\rm DM}^{\rm Einasto}(r) = \rho_E \exp\left[-\frac{2}{\alpha}(r/r_E)^{\alpha} - 1\right]$$

Halo density profile for the Milky Way very important for indirect searches (later)

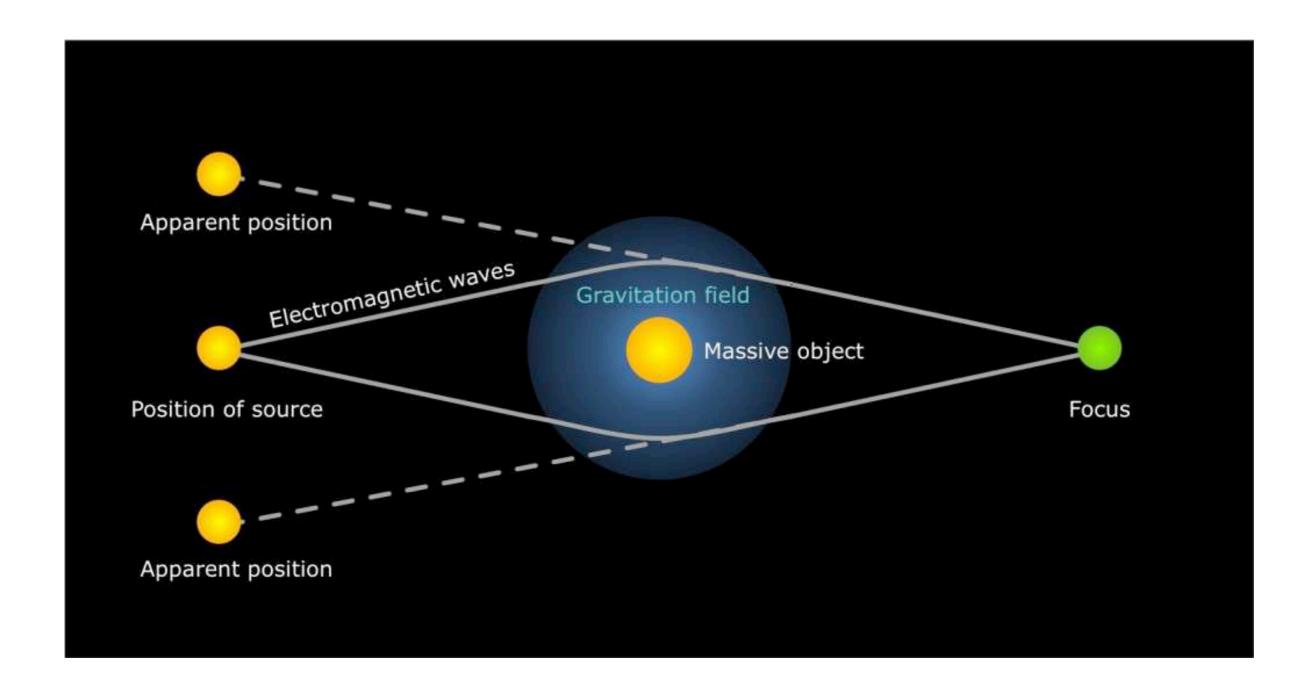
#### Dark matter halo



#### Firm evidence over decades



# **Gravitational Lensing**

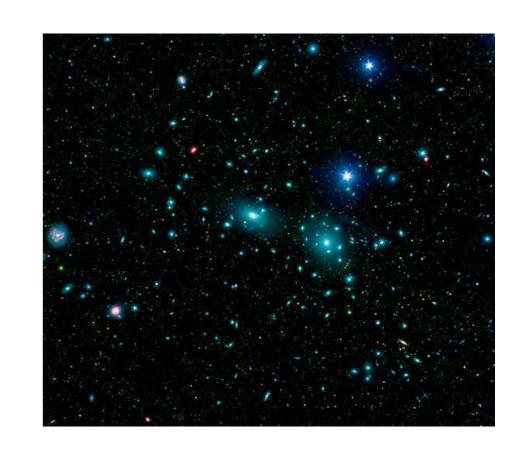


We can find evidence for dark matter even beyond the visible galactic disk

## Hot gas in galaxy clusters

Clusters are filled with hot gas that does not fall within galaxies

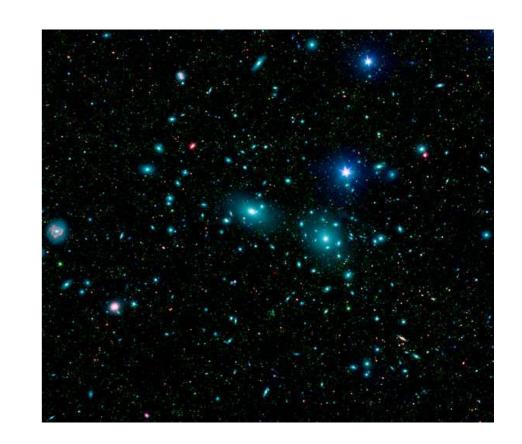
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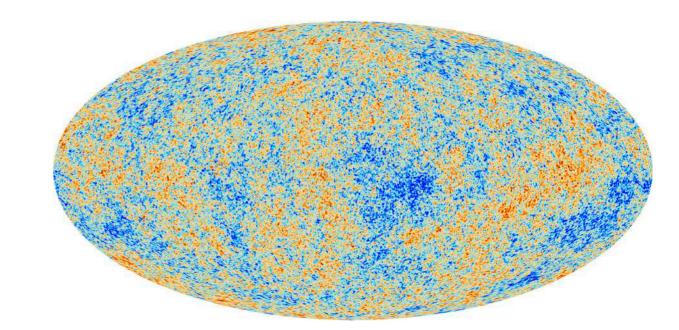


$$\left(\frac{dp(r)}{dr} = -\frac{G_N M(r)\rho(r)}{r^2}\right)$$

Hydrostatic equilibrium: we can infer the distribution of gravitational mass

# Cosmic Microwave Background

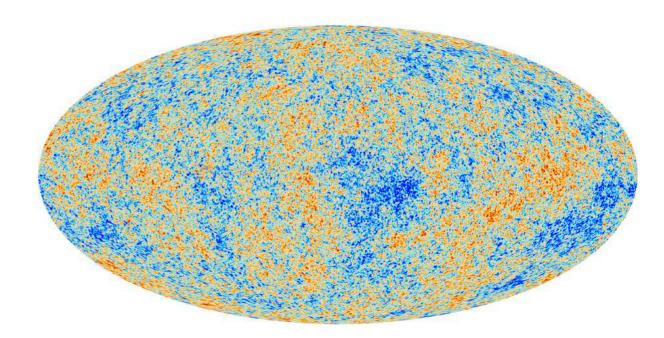
Universe 380,000 yrs old, Temperature 0.3 eV, Tiny density fluctuations



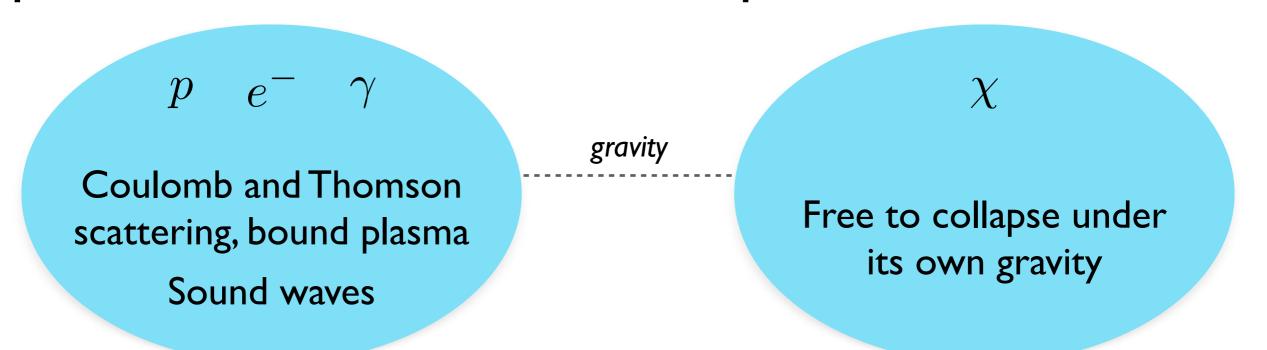
Species present @ CMB formation: photons, neutrinos, electrons, protons, dark matter

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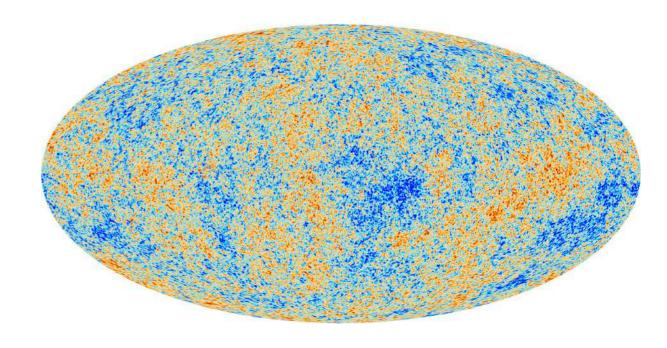


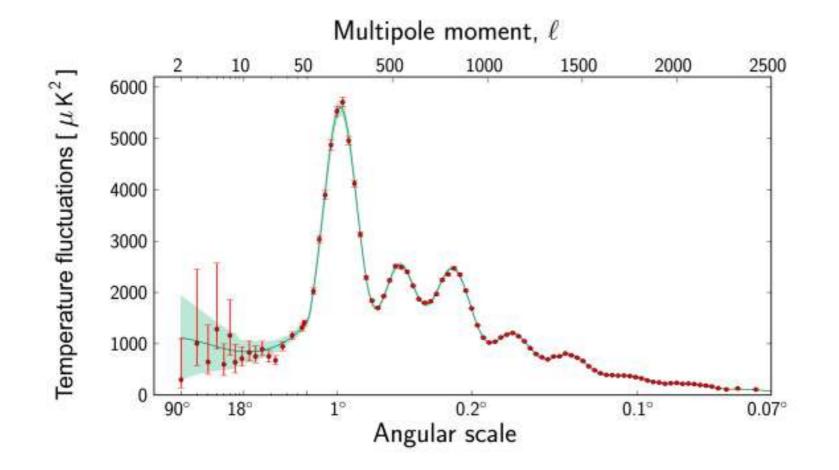
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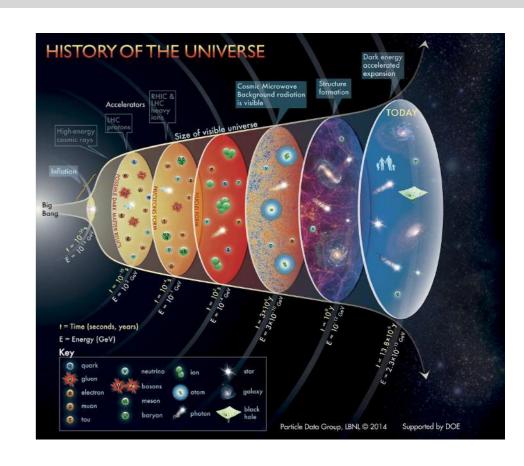


$$\rho_{\rm DM} \simeq 5 \, \rho_B$$

Dark matter must be non-baryonic!

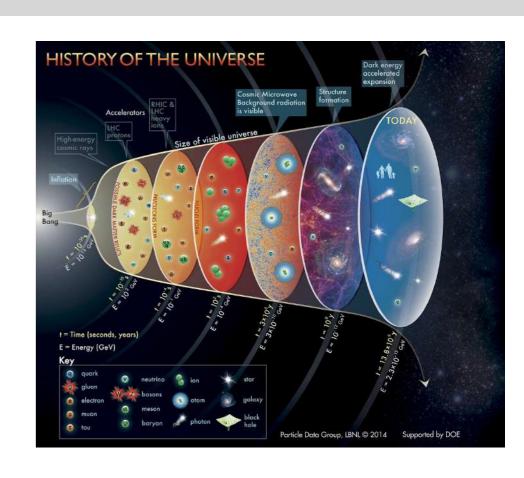
#### **Structure Formation**

How did we go from a highly homogeneous and isotropic universe to galaxies and clusters?



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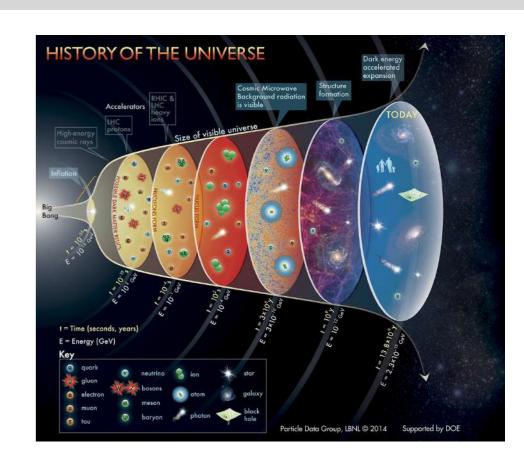


#### **GRAVITATIONAL COLLAPSE**

$$\frac{\delta \rho}{\rho} \propto \begin{cases} \ln(a) & \text{RD} \\ a & \text{MD} \end{cases}$$

#### **Structure Formation**

How did we go from a highly homogeneous and isotropic universe to galaxies and clusters?

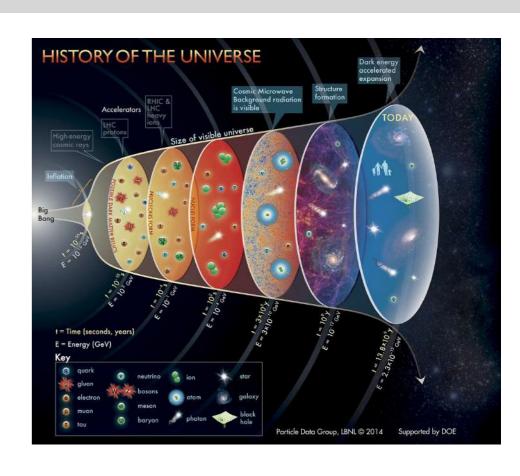


#### **BARYONS ONLY**

$$\left. \frac{\delta \rho}{\rho} \right|_{\text{today}} \simeq \left. \frac{\delta \rho}{\rho} \right|_{\text{CMB}} \frac{a_0}{a_{\text{rec}}} \simeq 10^{-5} \times 10^3 \simeq 10^{-2}$$

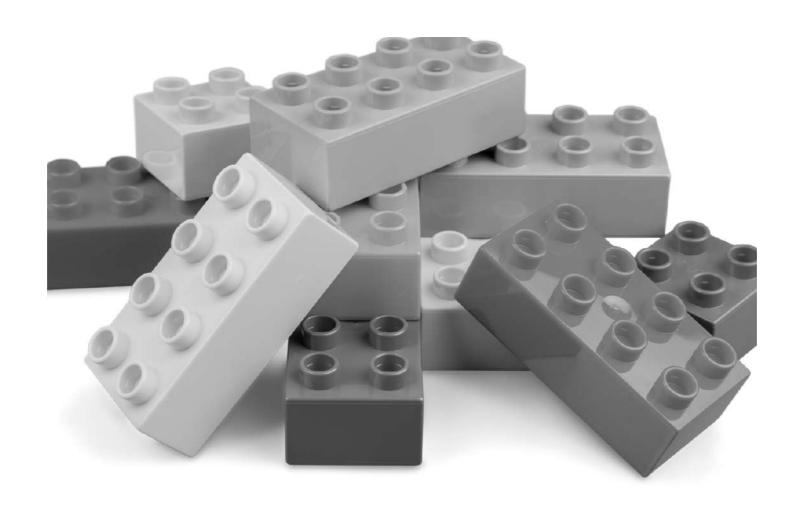
### **Structure Formation**

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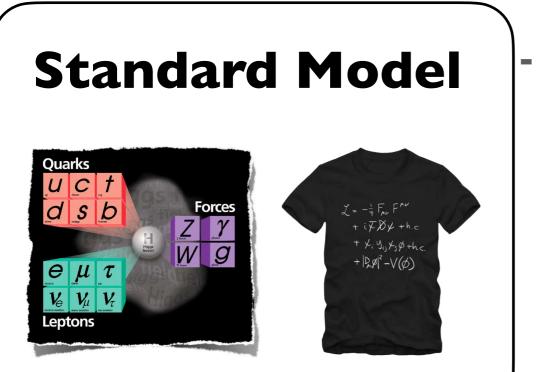


Structure formation can reach the non-linear regime only if there is dark matter!

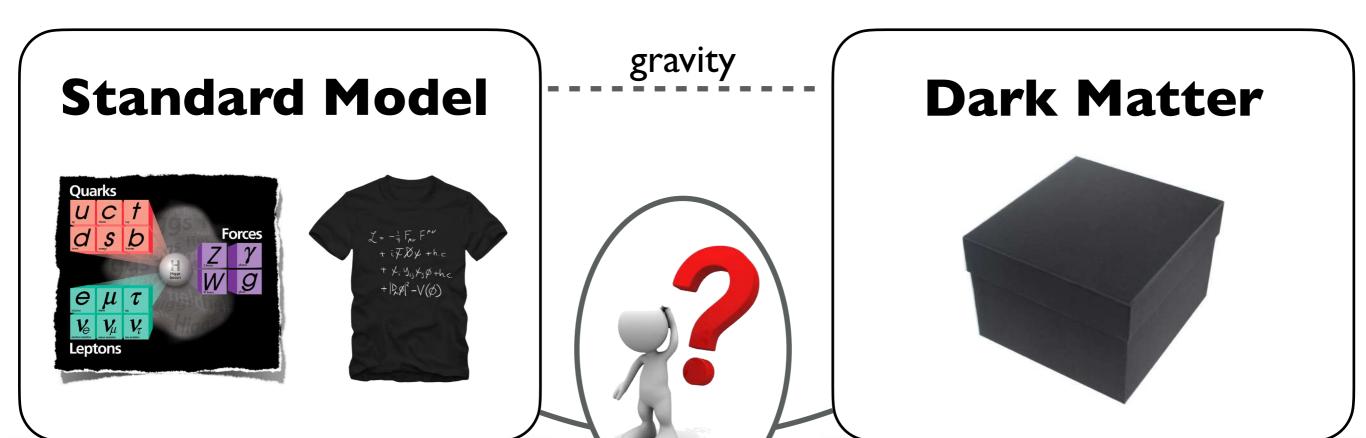
What is the dark matter made of?

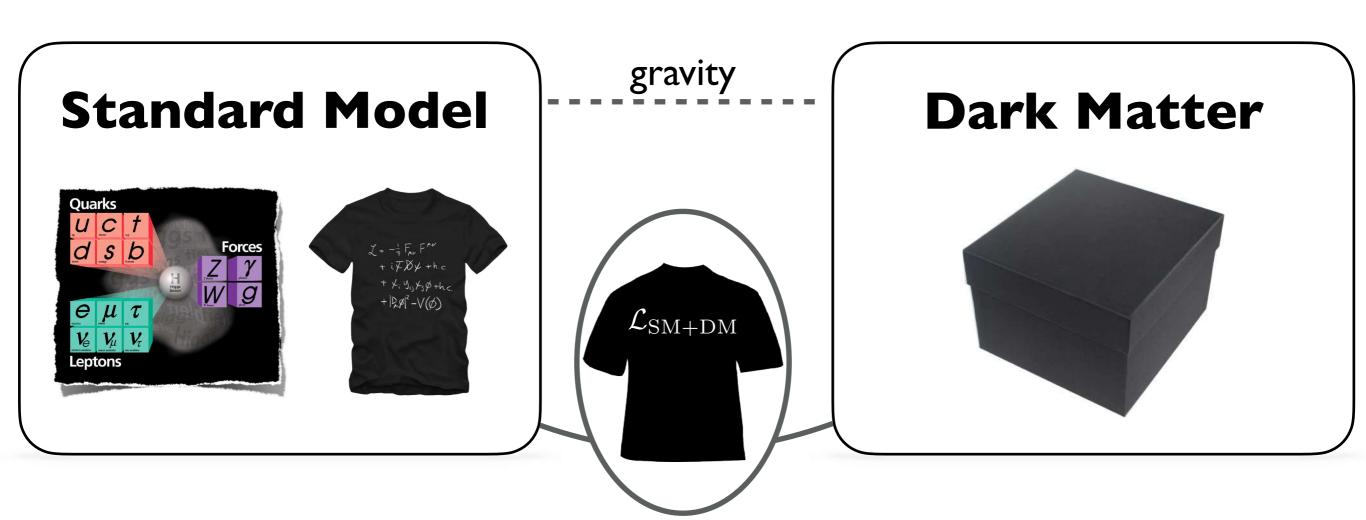


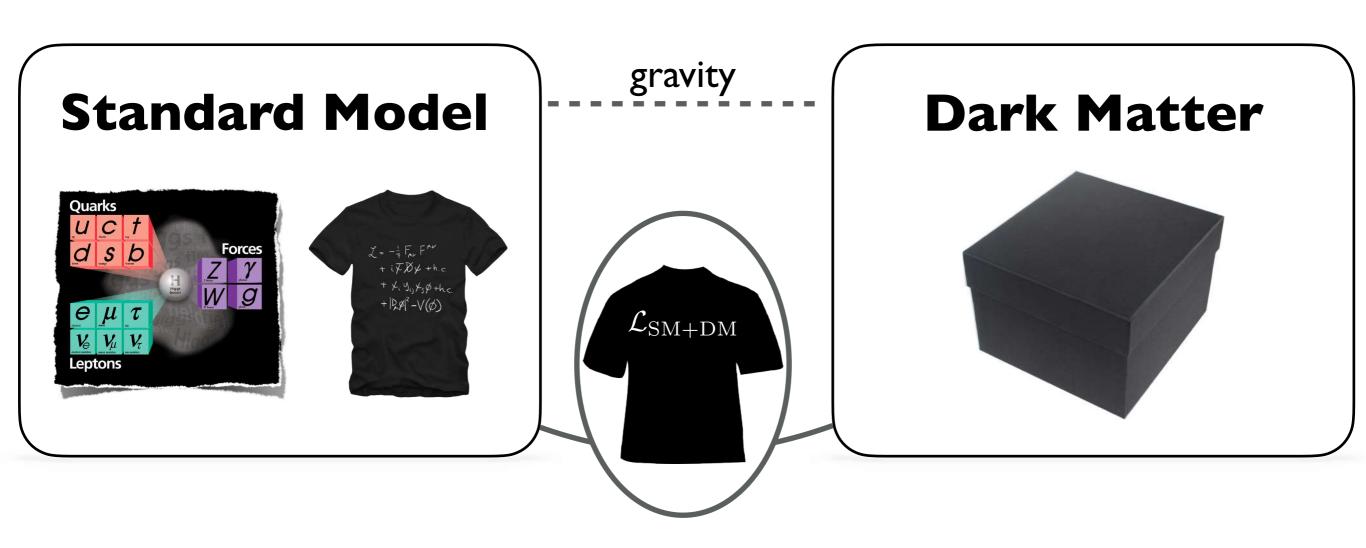
gravity











In these lectures I will tell you about possible ideas that could end up in that t-shirt

We cannot put anything we want: solid bounds from dark matter searches

#### **RELIC DENSITY**

$$\Omega_{DM}(t_0)h^2 = \frac{\rho_{DM}}{\rho_{\text{crit}}/h^2} = 0.1198 \pm 0.0012$$

#### **RELIC DENSITY**

$$\xi_{DM} = \frac{\rho_{DM}}{s(t_0)} = \frac{m_{DM}n_{DM}}{s(t_0)} = m_{DM}Y_{DM} \simeq 4.35 \times 10^{-10} \,\text{GeV}$$

Reproduce the relic density

#### **MASS BOUNDS**

### BOSON DM:

de Broglie wavelength smaller than dwarf galaxies size

$$\lambda_{DM} = \frac{h}{p} \simeq \left(\frac{1 \,\text{eV}}{m_{DM}}\right) \, 2.3 \times 10^{-3} \,\text{m}$$

$$m_{DM} \gtrsim 10^{-22} \, \text{eV}$$

Reproduce the relic density

#### **MASS BOUNDS**

### **FERMION DM:**

Tremaine-Gunn bound (Pauli exclusion principle)

$$m_{\rm DM} \gtrsim \left(\frac{9\pi}{4\sqrt{2}g} \frac{1}{\sqrt{MG^3R^3}}\right)^{1/4}$$
  
  $\gtrsim (10 - 100) \,\mathrm{eV}$ 

PROBLEM 2

Reproduce the relic density

"Statistical" bounds on the mass

#### **CHARGE NEUTRAL**

Searches for DM-electron bound states

$$q_{\rm DM} \simeq \begin{cases} 10^{-6} & m_{\rm DM} = 10 \,\text{GeV} \\ 10^{-4} & m_{\rm DM} = 10 \,\text{TeV} \end{cases}$$

Reproduce the relic density

"Statistical" bounds on the mass

Charge neutrality

#### COLDNESS

Cosmological structures study:

DM particles must have been non-relativistic when the universe had a temperature T ~ I keV

This excludes hot relics (next lecture)

Reproduce the relic density

"Statistical" bounds on the mass

Charge neutrality

Cold relics

#### **Self-Interactions**

$$\frac{\sigma_{\rm self}}{m} \lesssim 1 \frac{\rm cm^2}{\rm g}$$



Reproduce the relic density

"Statistical" bounds on the mass

Charge neutrality

Cold relics

#### **Self-Interactions**

$$\frac{\sigma_{\text{self}}}{m} \lesssim 10^{-24} \text{cm}^2 \, \text{TeV}^{-1}$$



Reproduce the relic density

"Statistical" bounds on the mass

Charge neutrality

Cold relics

Not too-much self-interacting

### **Stability**

Invisible decays alter expansion history  $\tau_{\rm DM} \gtrsim 5 \times 10^{18}\,{\rm sec}$ 

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Visible decays impact CMB spectra

$$\tau_{\rm DM} \gtrsim 10^{25-29} \, {\rm sec}$$

$$\tau_H \simeq 4 \times 10^{17} \,\mathrm{sec}$$

Reproduce the relic density

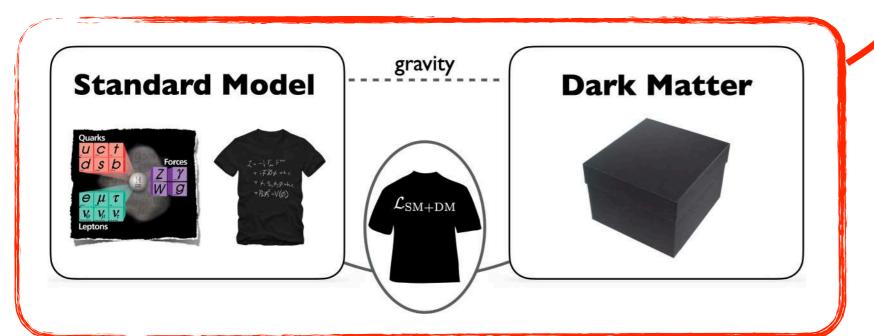
"Statistical" bounds on the mass

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Not too-much self-interacting

**Enough long-lived** 



We will see plausible options this week