

# COSMOLOGICAL BACKGROUNDS of GRAVITATIONAL WAVES

## 3rd Lecture

**Daniel G. Figueroa**  
**IFIC, VALENCIA**

# Gravitational Waves as a probe of the early Universe

## OUTLINE

1) GW definition ✓

2) GWs from Inflation

3) GWs from Preheating

4) GWs from Phase Transitions

5) GWs from Cosmic Defects

**Early  
Universe**

**3rd lecture**

# Gravitational Waves as a probe of the early Universe

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1) GW definition ✓

2) GWs from Inflation

3) GWs from **Preheating**

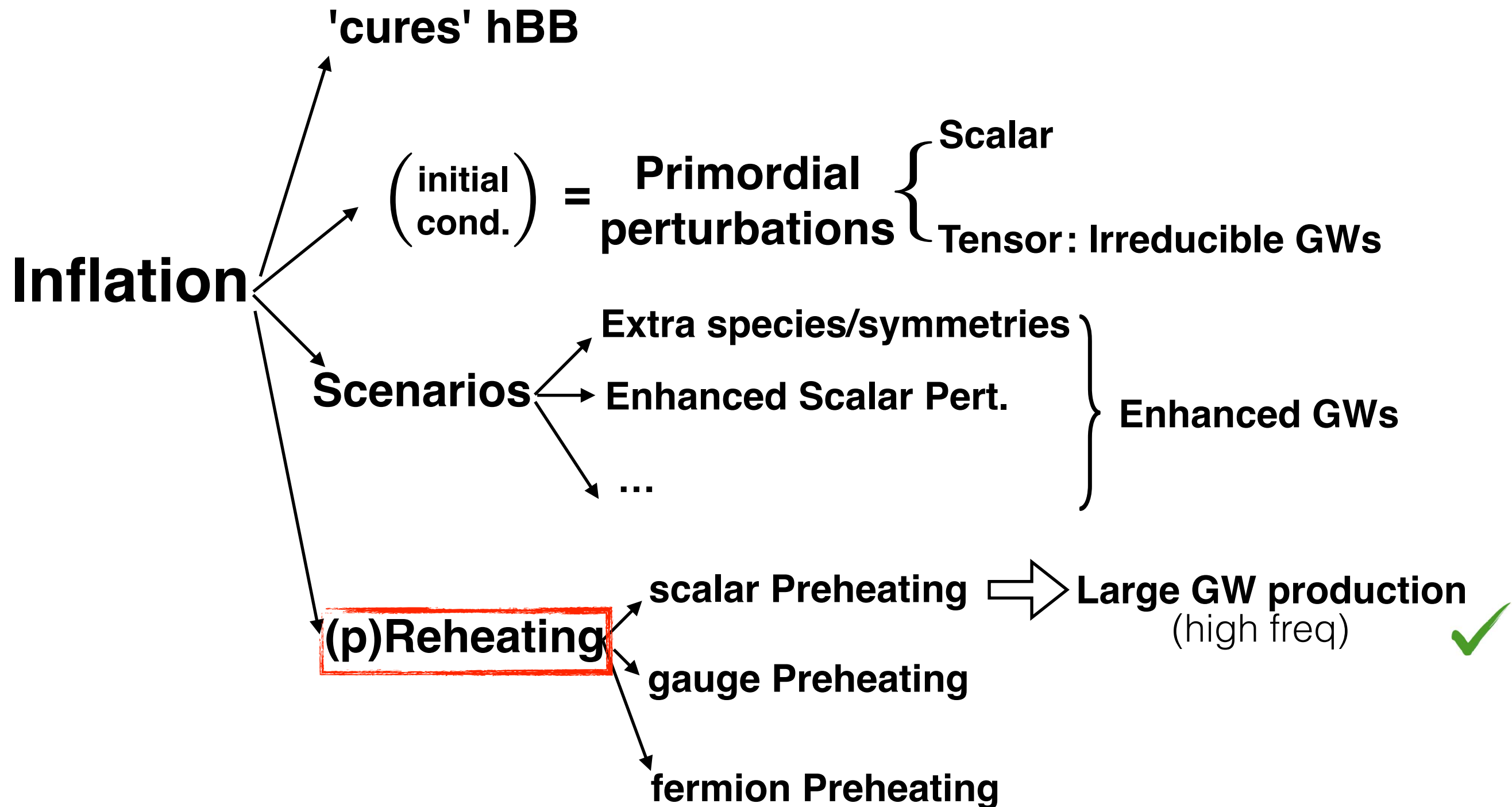
**4) GWs from Phase Transitions**

5) GWs from Cosmic Defects

**Early  
Universe**

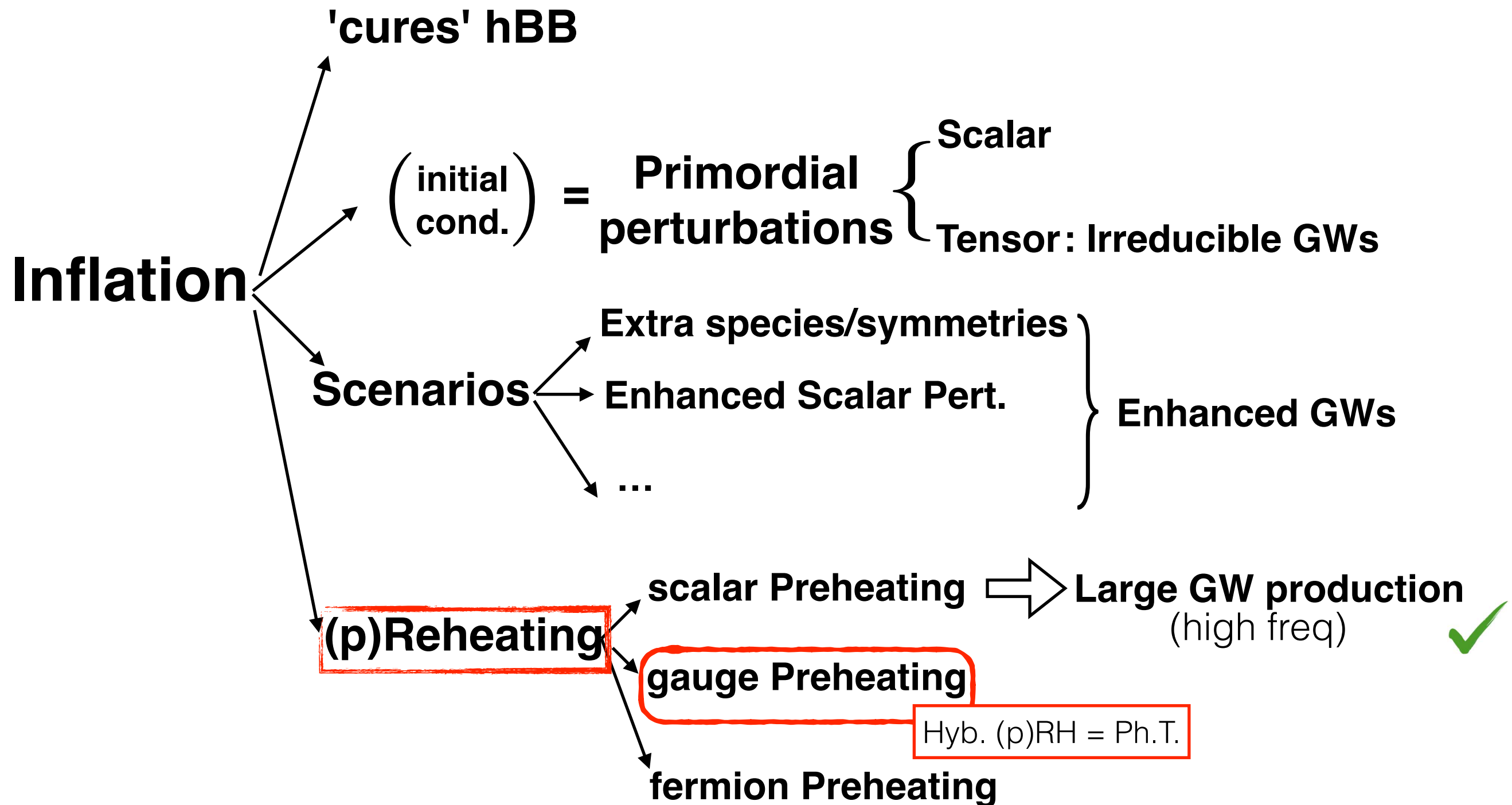
**3rd lecture**

# INFLATIONARY COSMOLOGY





# INFLATIONARY COSMOLOGY



# GAUGE (P)REHEATING

Hybrid Preheating = Higgs+Inflaton model

$$\left. \begin{array}{l} \text{Inflaton: } \ddot{\phi}(t) + (\mu^2 + g^2|\chi|^2)\phi(t) = 0 \\ \text{Higgs: } \ddot{\chi}_k + \left(k^2 + m^2 \left(\frac{\phi^2}{\phi_c^2} - 1\right) + \lambda|\chi|^2\right)\chi_k = 0 \end{array} \right\} \quad \begin{array}{l} m = \sqrt{\lambda}v \\ \phi_c \equiv m/g \end{array}$$

# GAUGE (P)REHEATING

Hybrid Preheating = Higgs+Inflaton model

inflaton mass                      coupling

**Inflaton:**  $\ddot{\phi}(t) + (\mu^2 + g^2|\chi|^2)\phi(t) = 0$

**Higgs:**  $\ddot{\chi}_k + \left(k^2 + m^2 \left(\frac{\phi^2}{\phi_c^2} - 1\right) + \lambda|\chi|^2\right)\chi_k = 0$

Self-coupling                      V.E.V.

$m = \sqrt{\lambda}v$

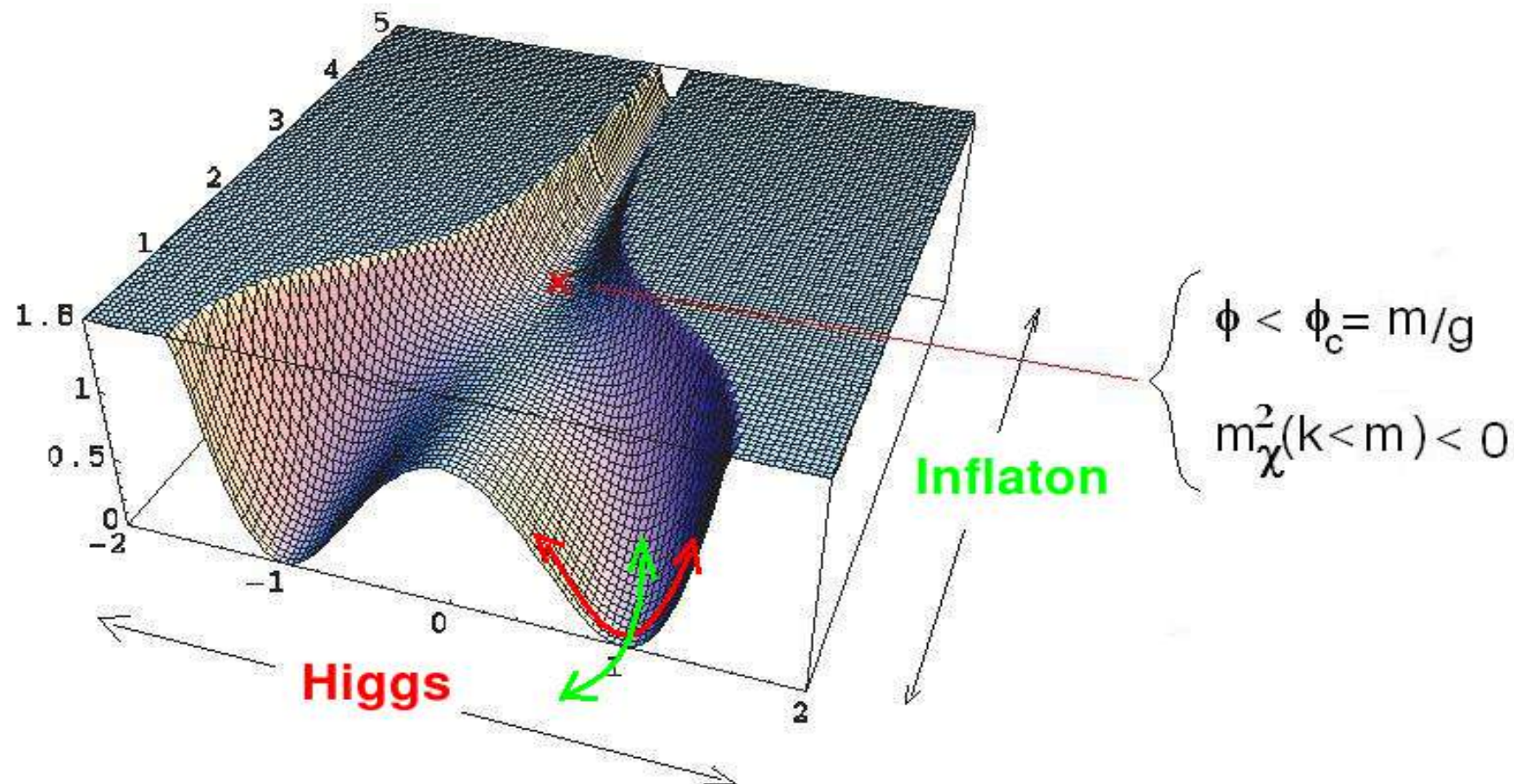
$\phi_c \equiv m/g$                       Critical value

# GAUGE (P)REHEATING

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Hybrid Preheating = Phase Transition



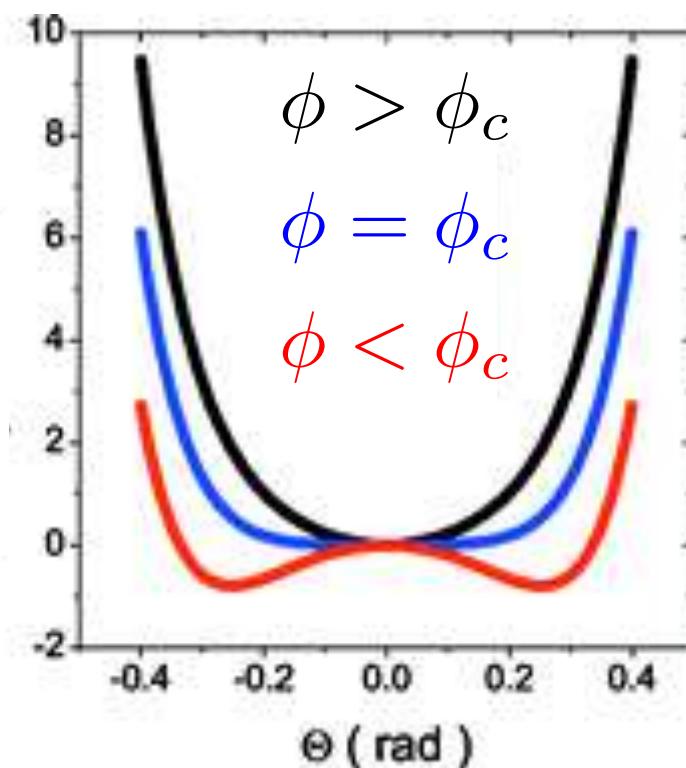
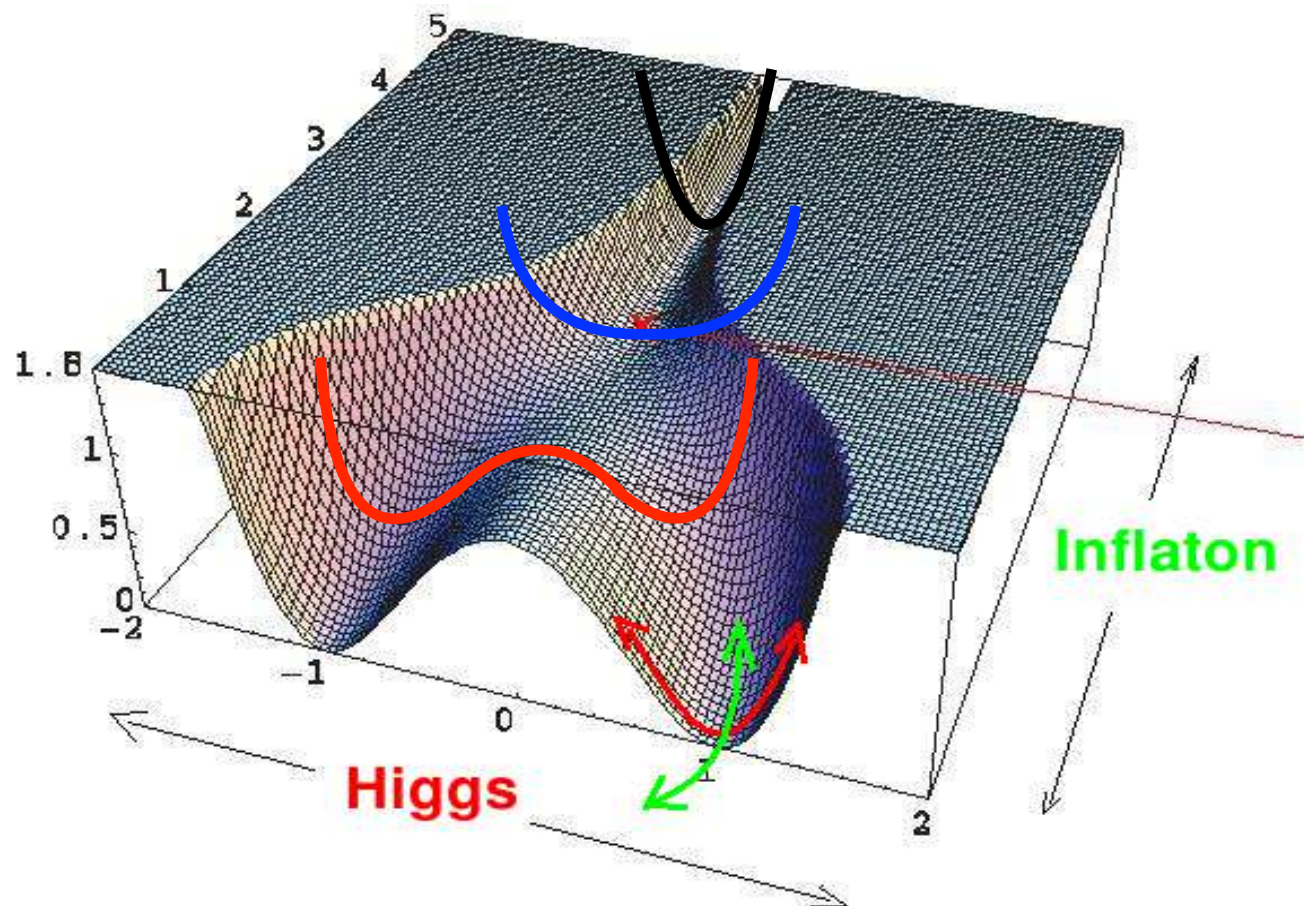


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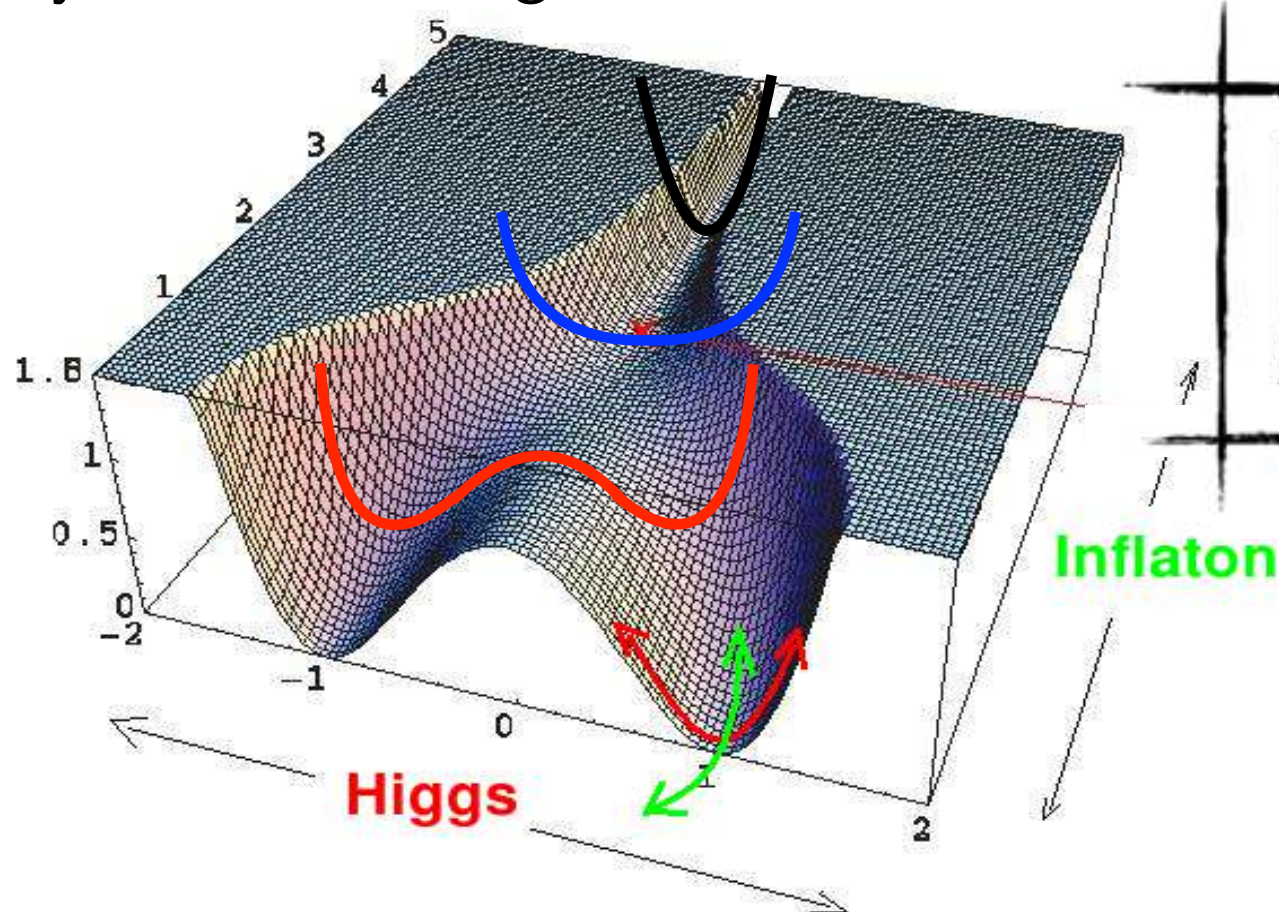


# GAUGE (P)REHEATING

Hybrid Preheating = Higgs+Inflaton model

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Hybrid Preheating = Phase Transition



**It is a Phase transition !  
by Tachyonic Instability**

$$\langle \chi \rangle = 0 \rightarrow \langle \chi \rangle = v$$

# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

$$L = -\frac{1}{4}F_{\mu\nu}^a F_a^{\mu\nu} + \text{Tr}[(D_\mu \Phi)^\dagger D^\mu \Phi] + \frac{1}{2}(\partial_\mu \chi)^2 - V(\Phi, \chi)$$

$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$$

$$D_\mu = \partial_\mu - ieA_\mu$$

$$V(\phi, \chi) = \frac{\lambda}{4}(\phi^2 - v^2)^2 + \frac{g^2}{2}\phi^2\chi^2 + \frac{1}{2}m^2\chi^2$$

Just to confuse you a little bit:      now  $\begin{cases} \chi : \text{inflaton} \\ \Phi = \frac{\phi}{\sqrt{2}} : \text{Higgs} \end{cases}$



# GAUGE (P)REHEATING

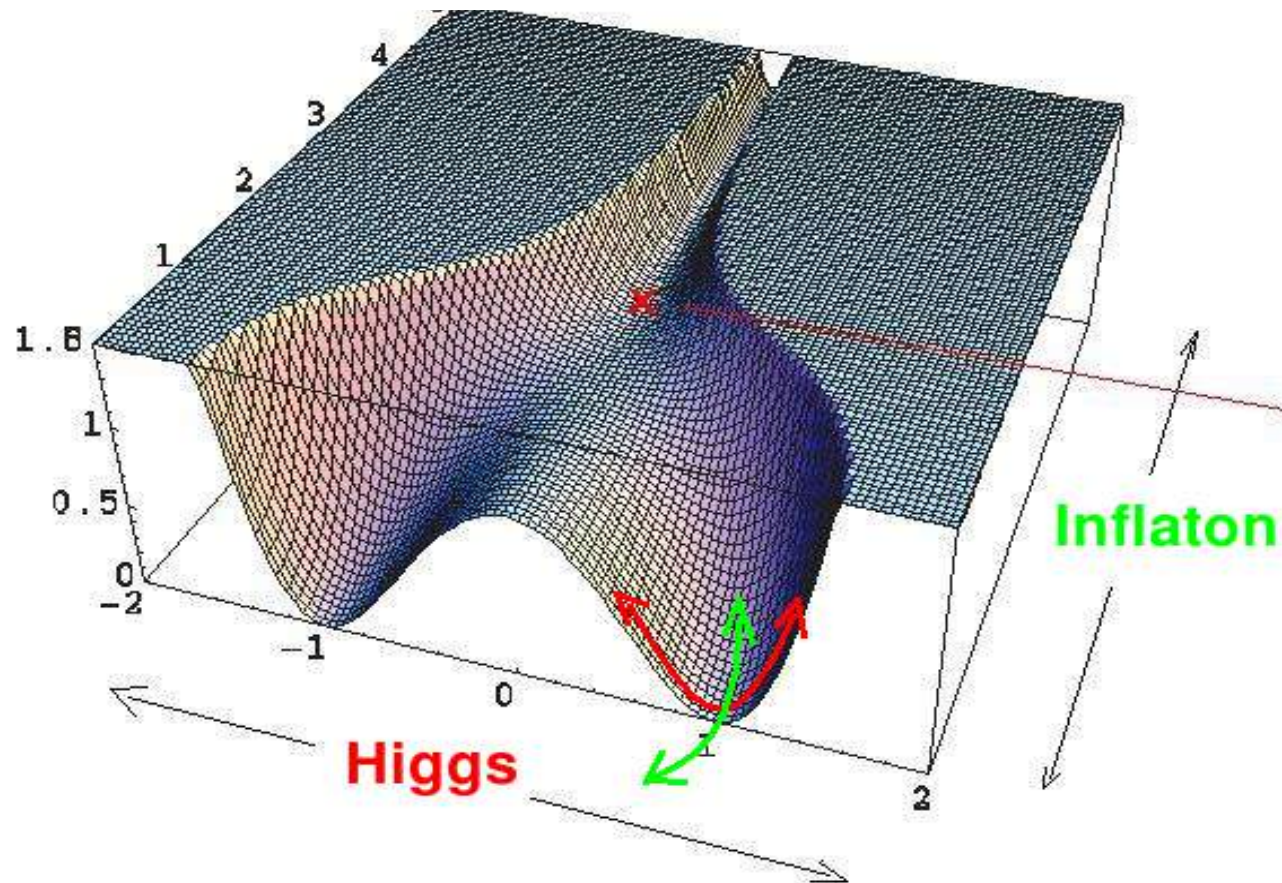
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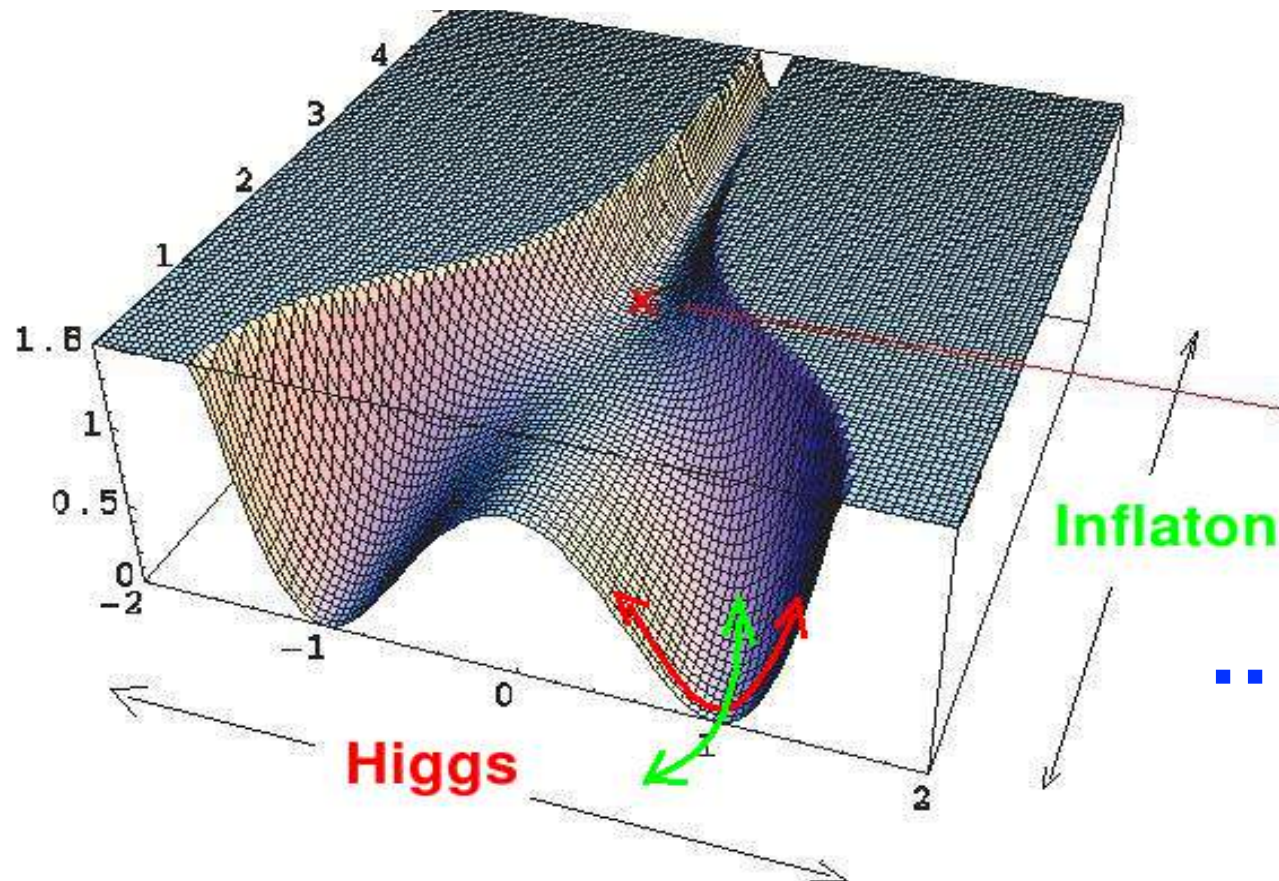
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... now there  
are gauge field(s) !

... so you excite the Higgs,  
you excite Gauge flds !



# GAUGE (P)REHEATING

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EOM:  $\begin{cases} \text{Minkowski,} \\ \text{Temporal Gauge (A}_0=0\text{)} \end{cases}$

$$\ddot{\varphi} - D_i D_i \varphi + V_{,\varphi^*} = 0$$

$$\ddot{A}_i - \partial_j \partial_j A_i + \partial_i \partial_j A_j = 2e^2 \text{Im} [\varphi^* D_i \varphi]$$

$$\partial_i \dot{A}_i = 2e^2 \text{Im} [\varphi^* \dot{\varphi}] .$$

→ SCALARS eom

→ VECTORS eom

→ GAUSS law

# GAUGE (P)REHEATING

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SCALARS eom

VECTORS eom

GAUSS law

GW EOM

$$\ddot{h}_{ij} - \partial_k \partial_k h_{ij} = 16\pi G \Pi_{ij}^{\text{TT}}$$

$$\Pi_{ij}^{\text{TT}} = [\partial_i \chi \partial_j \chi + 2 \text{Re} [D_i \varphi (D_j \varphi)^*] - B_i B_j - E_i E_j]^{\text{TT}}$$

# GAUGE (P)REHEATING

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COVARIANT

MAGNETIC

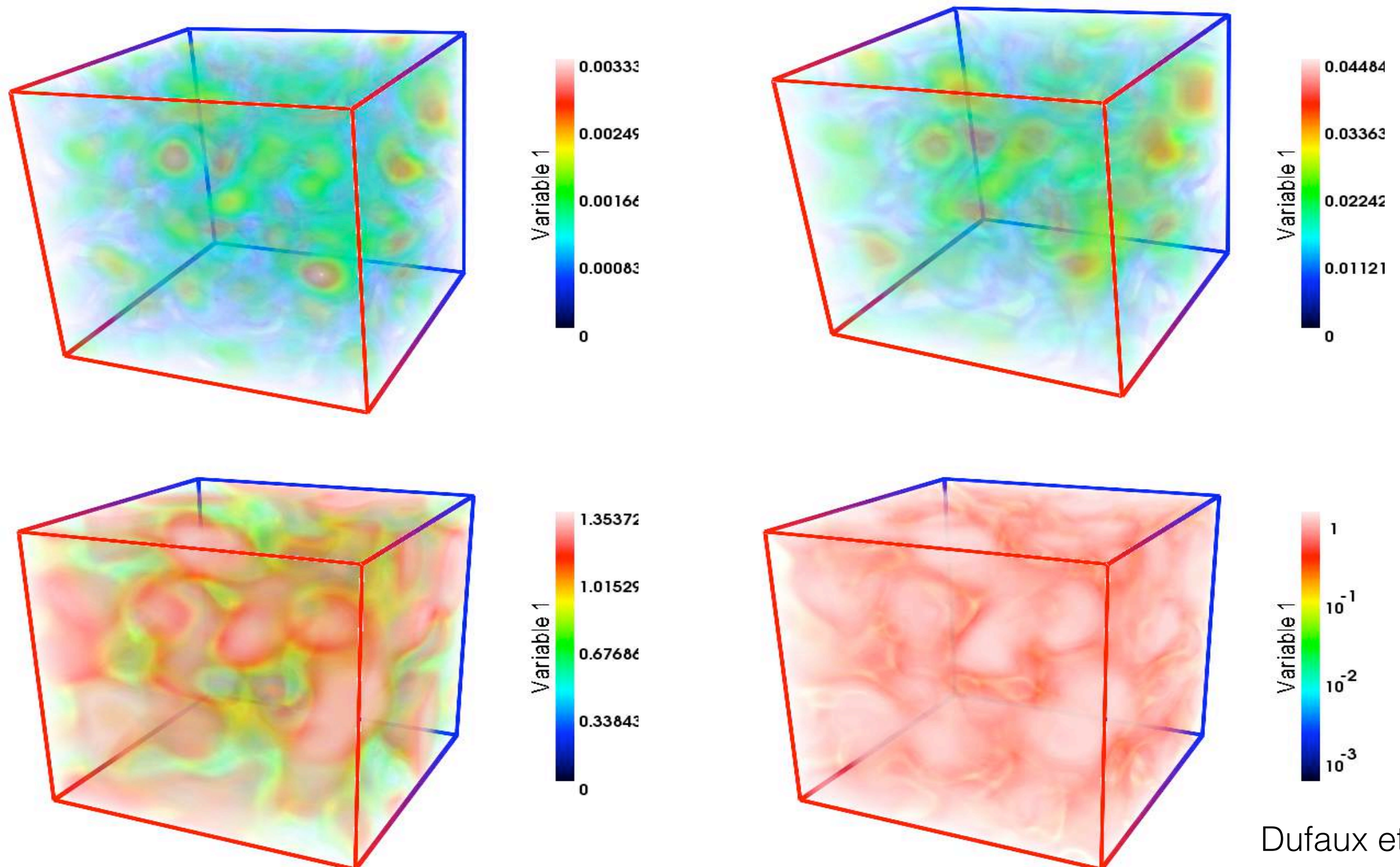
ELECTRIC



# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

DYNAMICS OF THE **HIGGS**:  $m_t = 5.5 \rightarrow m_t = 23$

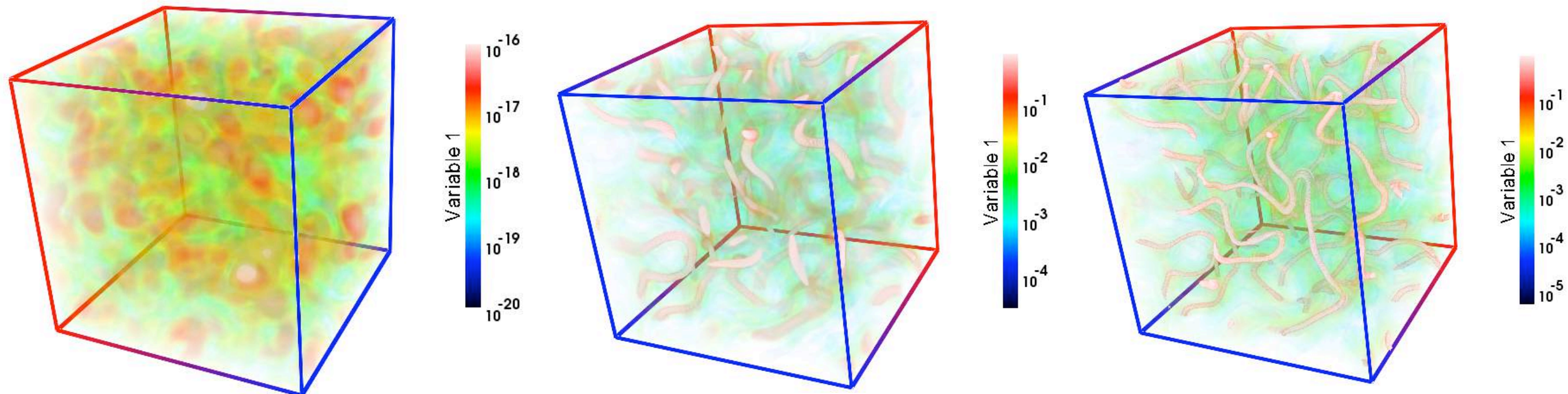




# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

DYNAMICS OF THE MAGNETIC FIELD:  $m_t = 5.5 \rightarrow m_t = 17$



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**What's going on !?**

**Cosmic Strings are formed**

# GAUGE (P)REHEATING

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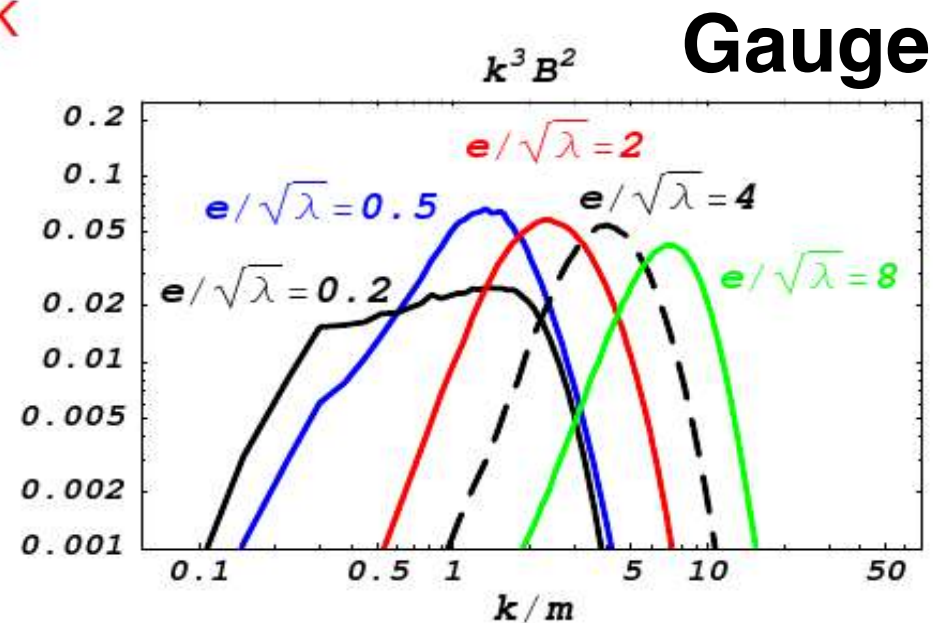
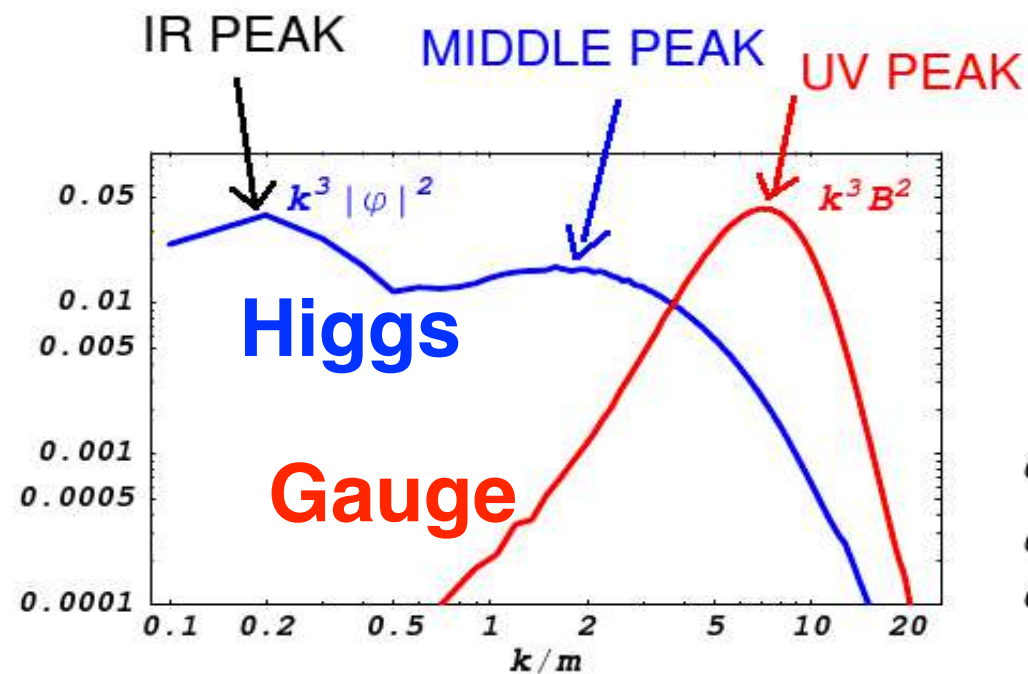
**Cosmic Strings are formed**

(Topological Defects  $\longrightarrow$  last 1/2 Lecture)

# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

SCALARS AND VECTORS' SPECTRA:

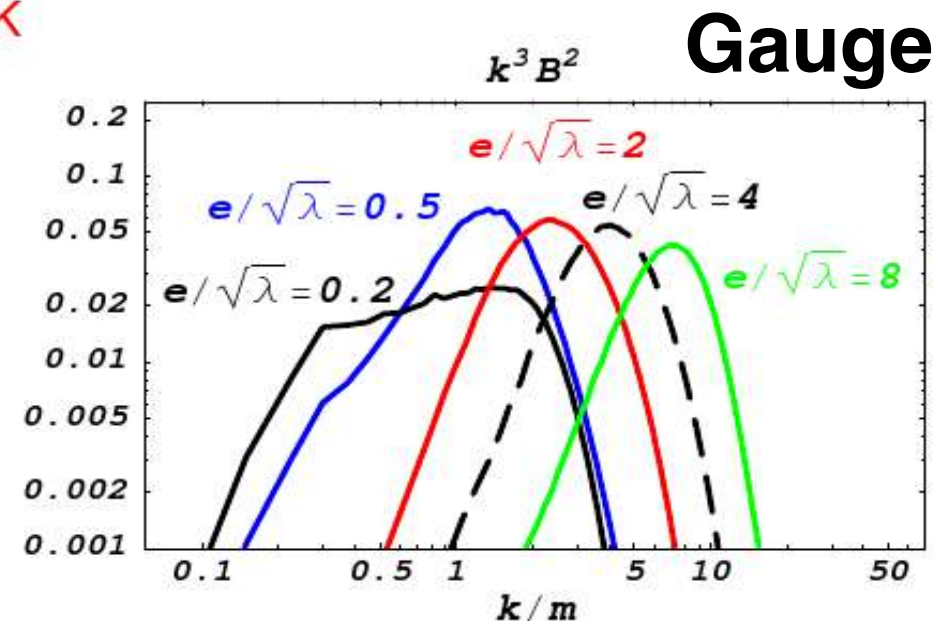
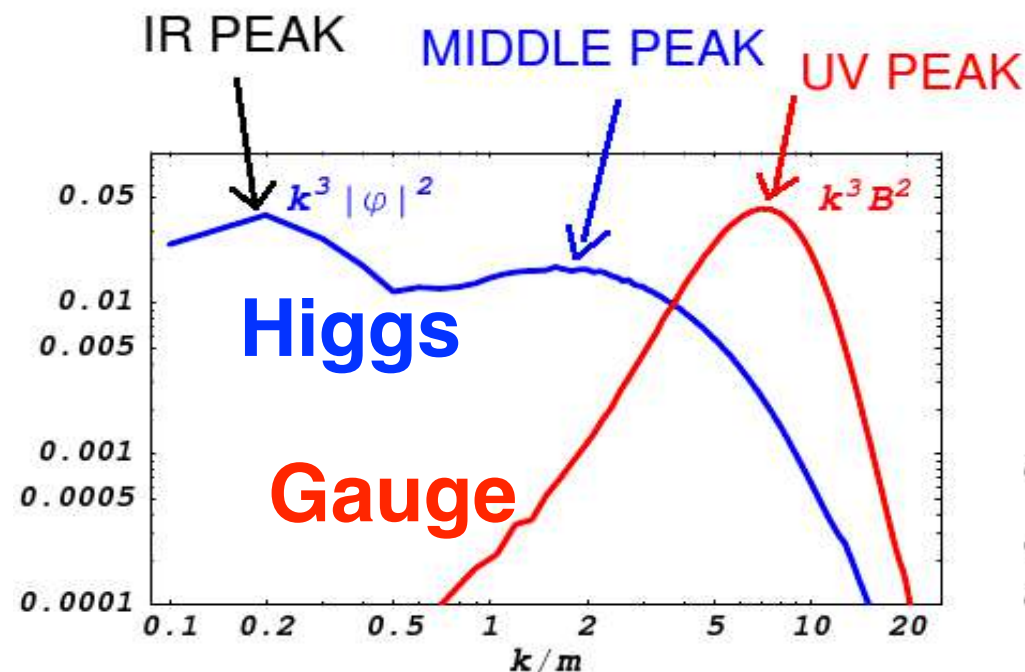




# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

SCALARS AND VECTORS' SPECTRA:



PARAMETERS ABELIAN-HIGGS Model:  $m \equiv \sqrt{\lambda}v$ ,  $\lambda/g^2$ ,  $e/\sqrt{\lambda}$ ,  $V_c$

MIDDLE PEAK:  $\left\{ \begin{array}{l} \text{Higgs mass} \\ (\text{Inflaton Velocity})^{1/3} \end{array} \right\} \rightarrow \text{Tachyonic Scale, Bubbles' Size}$

IR PEAK : Inflaton Velocity, Higgs+Inflaton Couplings (Dufaux et al 2009)

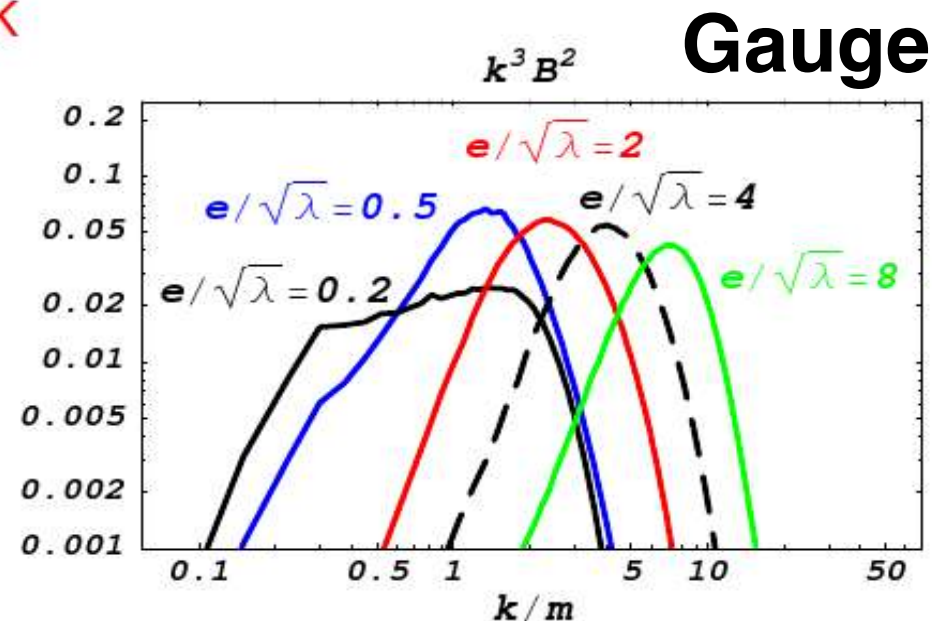
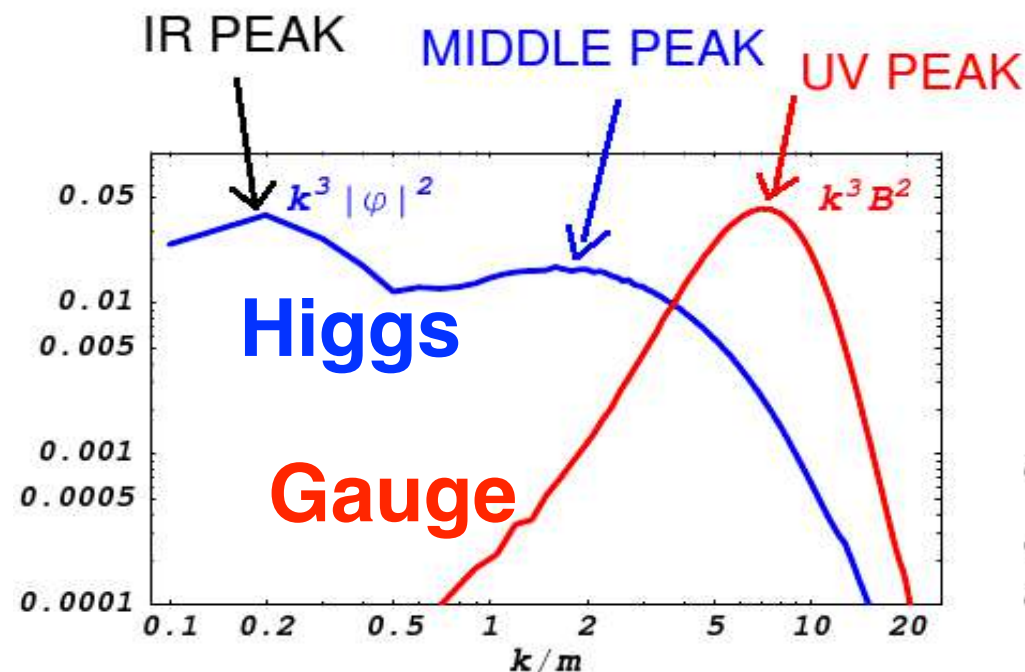
UV PEAK: Vector mass / Higgs Mass



# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

SCALARS AND VECTORS' SPECTRA:



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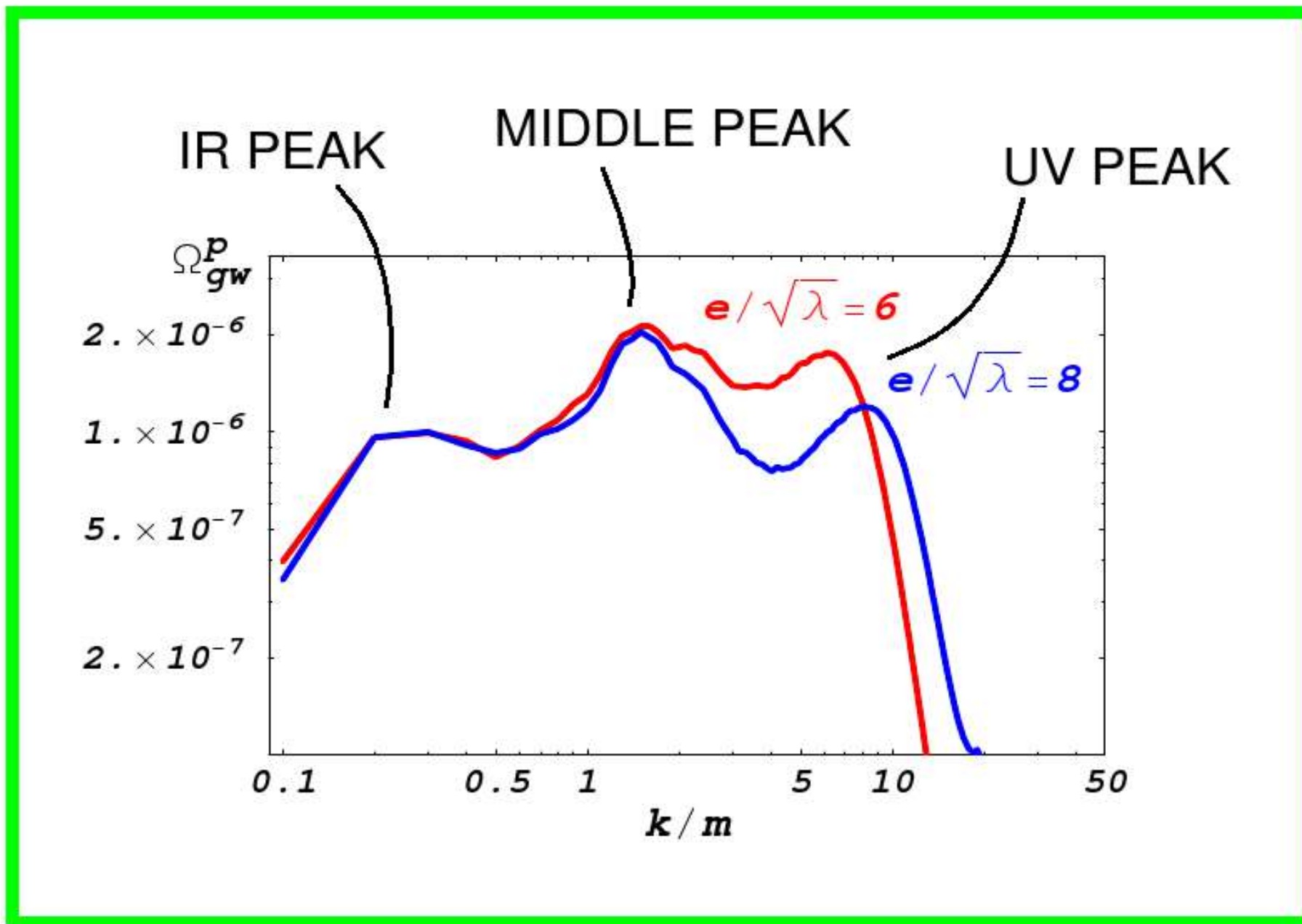
IR PEAK : Inflaton Velocity, Higgs+Inflaton Couplings (Dufaux et al 2009)

UV PEAK: Vector mass / Higgs Mass

# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

GRAVITATIONAL WAVES SPECTRA:



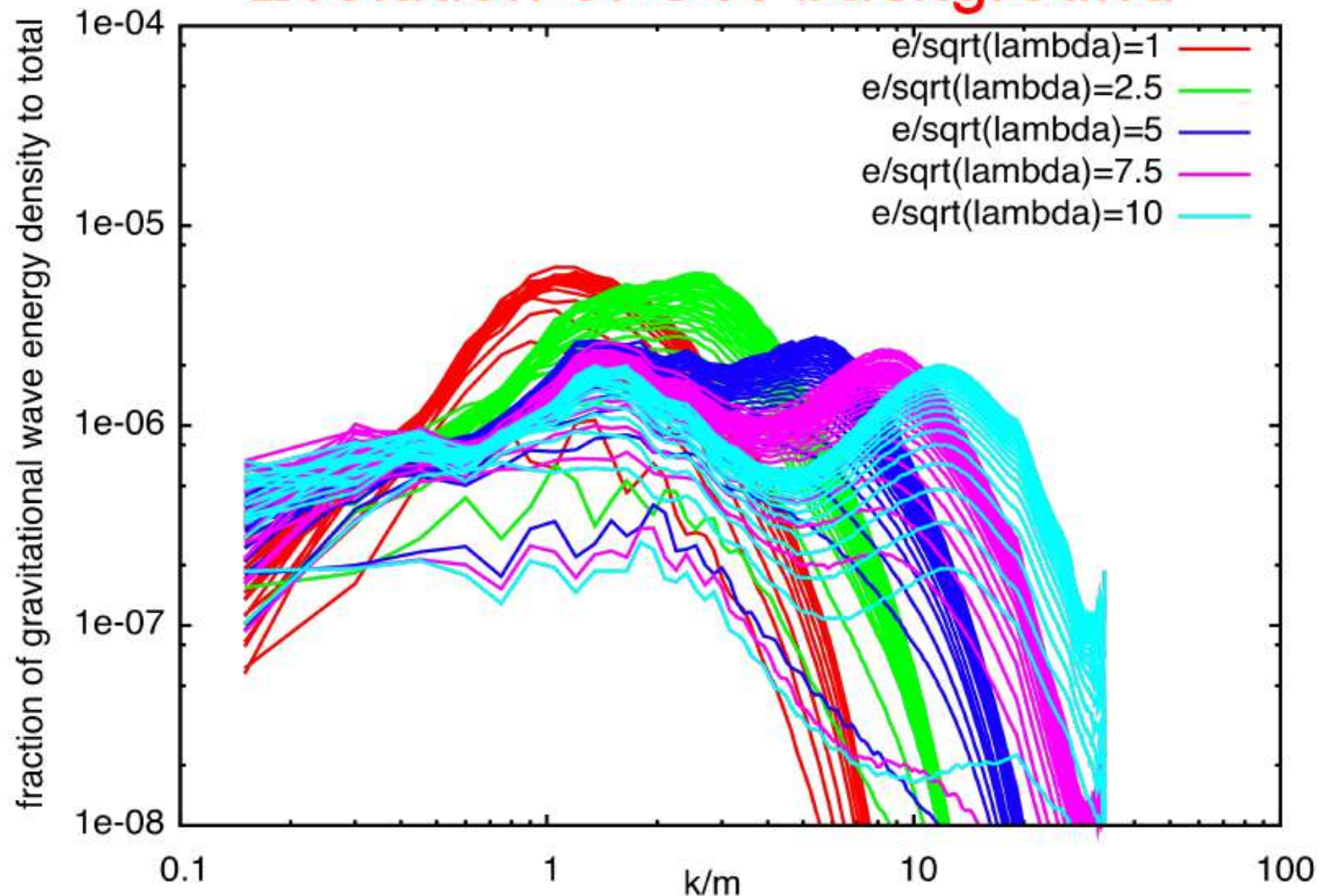


# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

### GRAVITATIONAL WAVES SPECTRA:

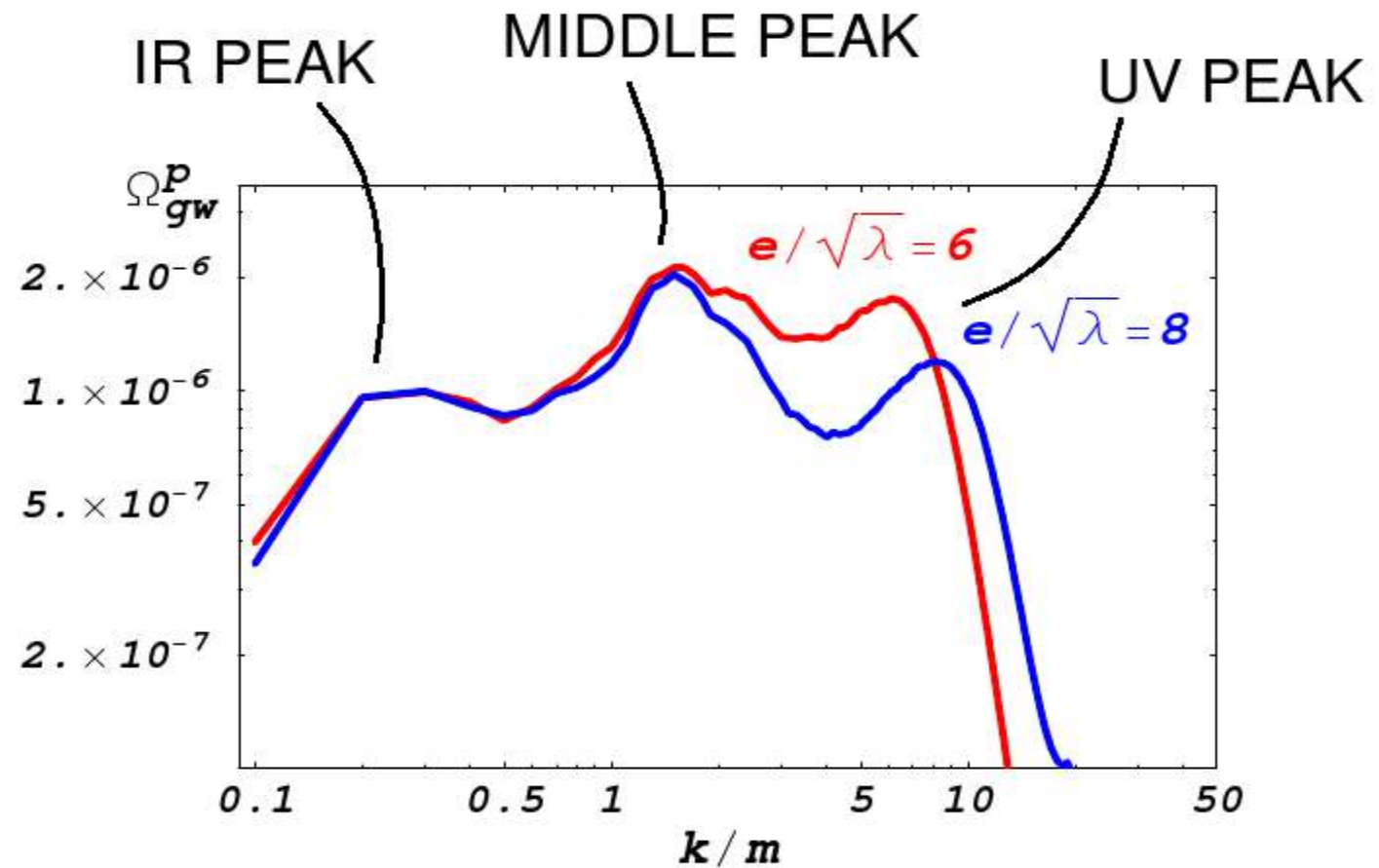
### Evolution of GW background



# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

**Several Peaks !**  
(particle physics  
spectroscopy)



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## The Abelian-Higgs+Inflaton model

**Several Peaks !**  
(particle physics  
spectroscopy)

$$\Omega_{\text{GW}}^{(o)} \sim 10^{-11},$$

**Large amplitude(s) !**



# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

**Several Peaks !**  
(particle physics  
spectroscopy)

$$\Omega_{\text{GW}}^{(o)} \sim 10^{-11}, \quad @ \quad f_o \sim 10^8 - 10^9 \text{ Hz}$$

**Large amplitude(s) ! ... but at high Frequency !**

# GAUGE (P)REHEATING

## The Abelian-Higgs+Inflaton model

**Several Peaks !**  
(particle physics  
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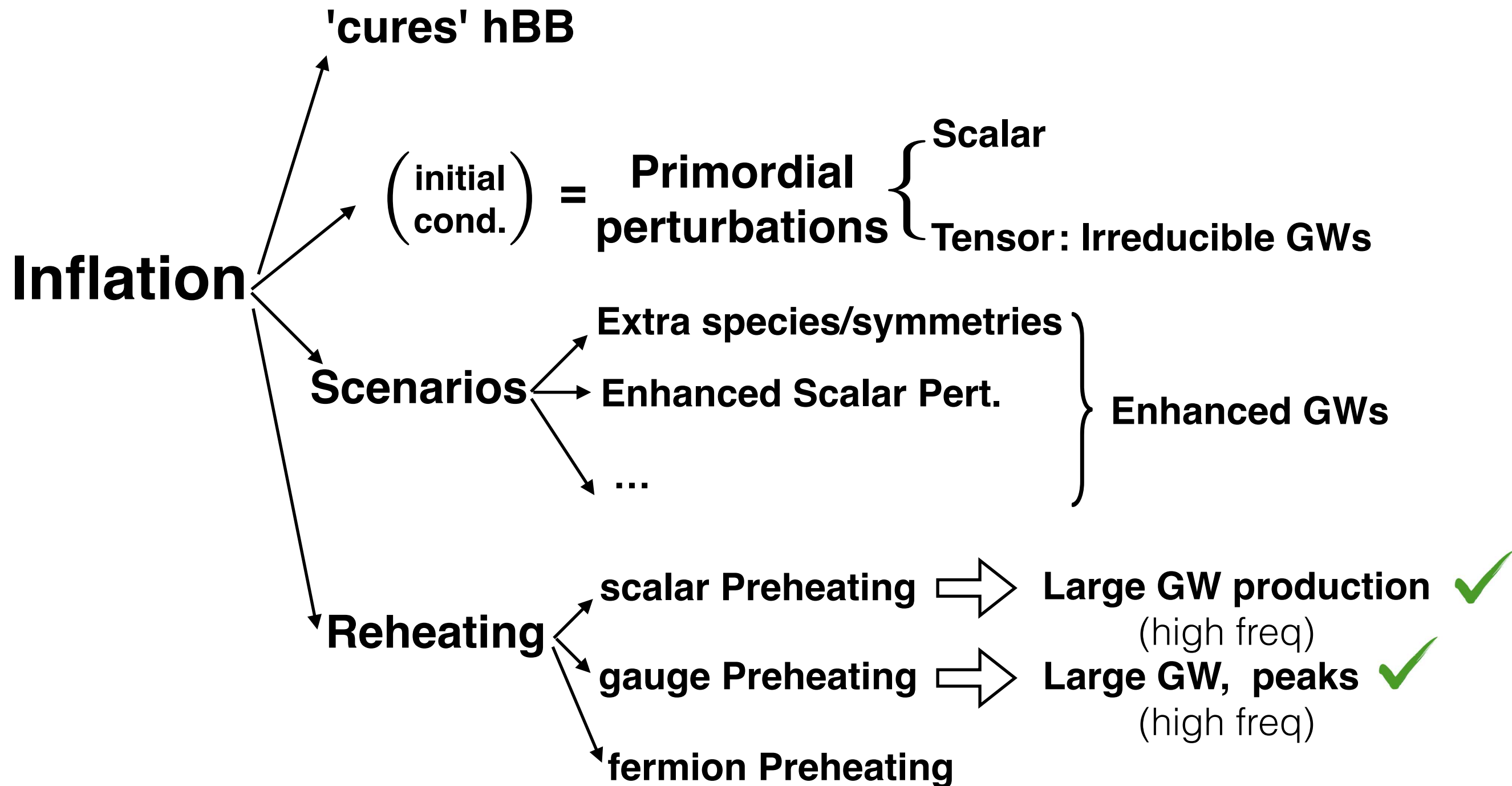
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**Large amplitude(s) ! ... but at high Frequency !**

**Very unfortunate... no high frequency detectors !**

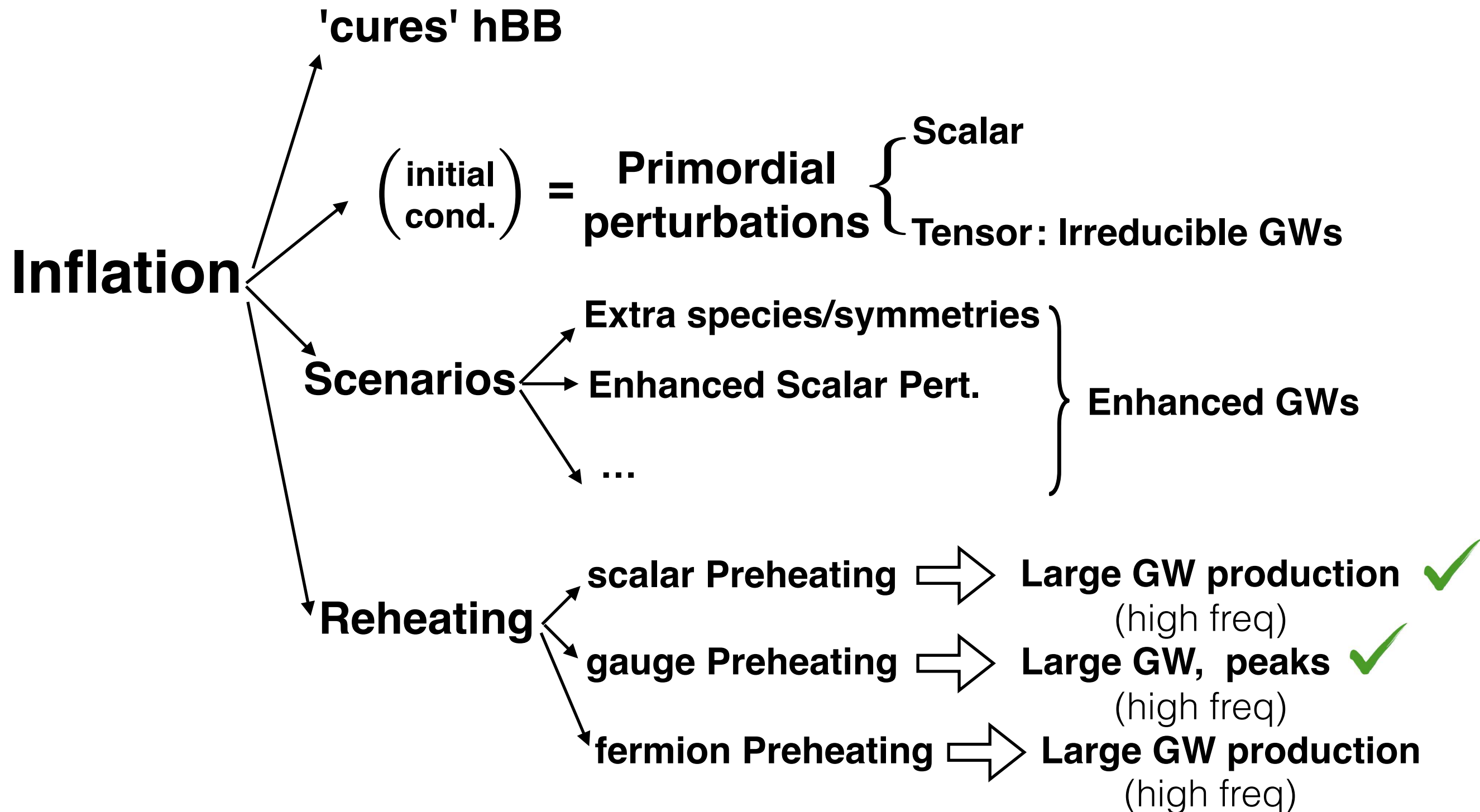


# INFLATIONARY COSMOLOGY

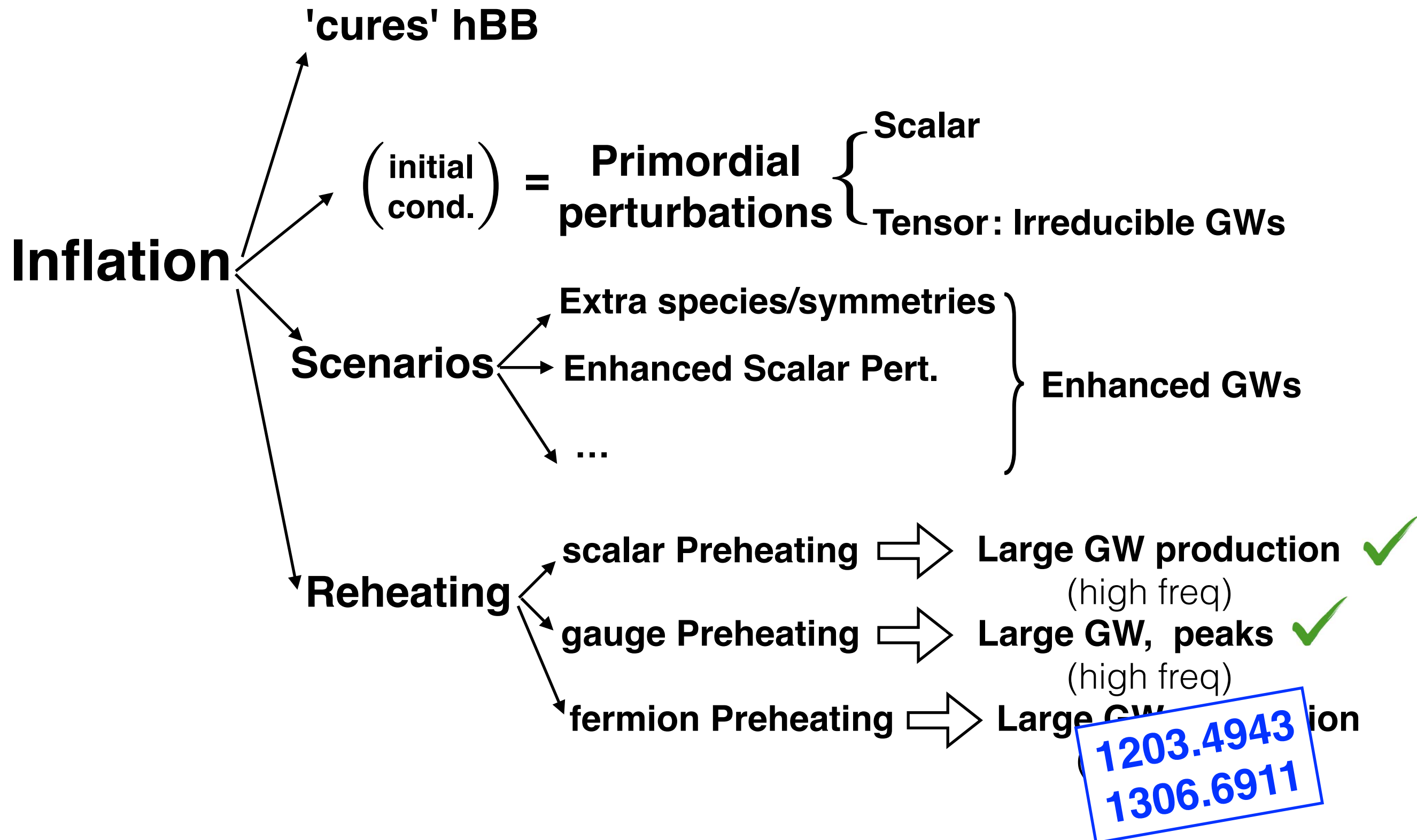




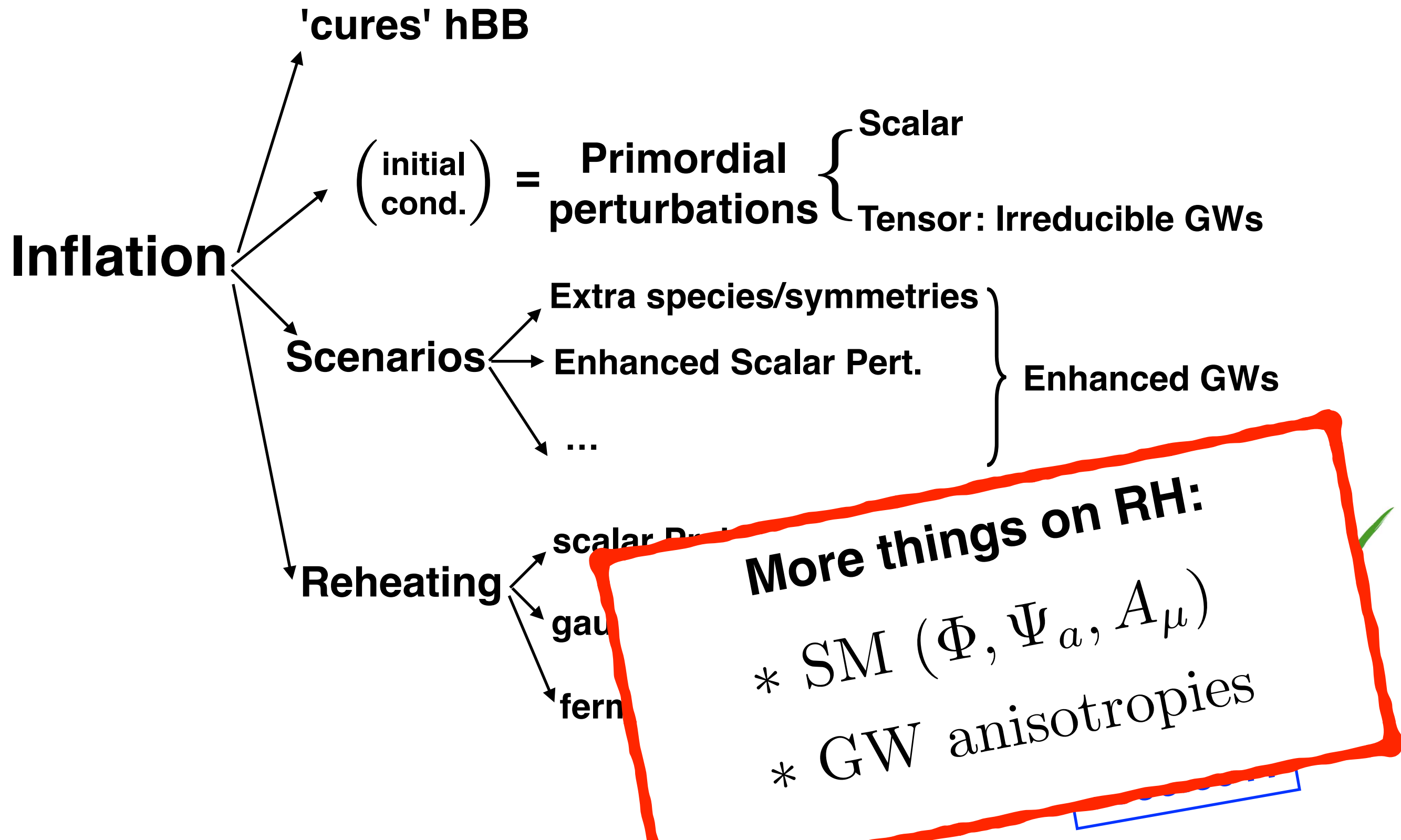
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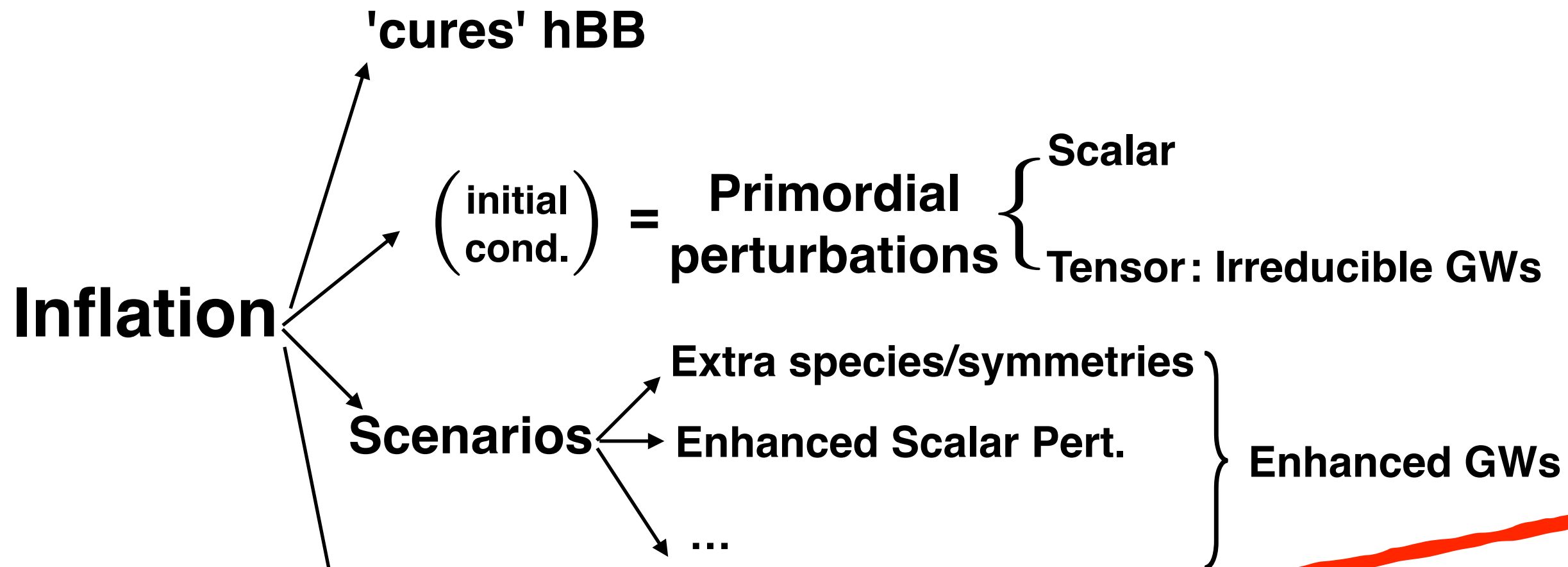


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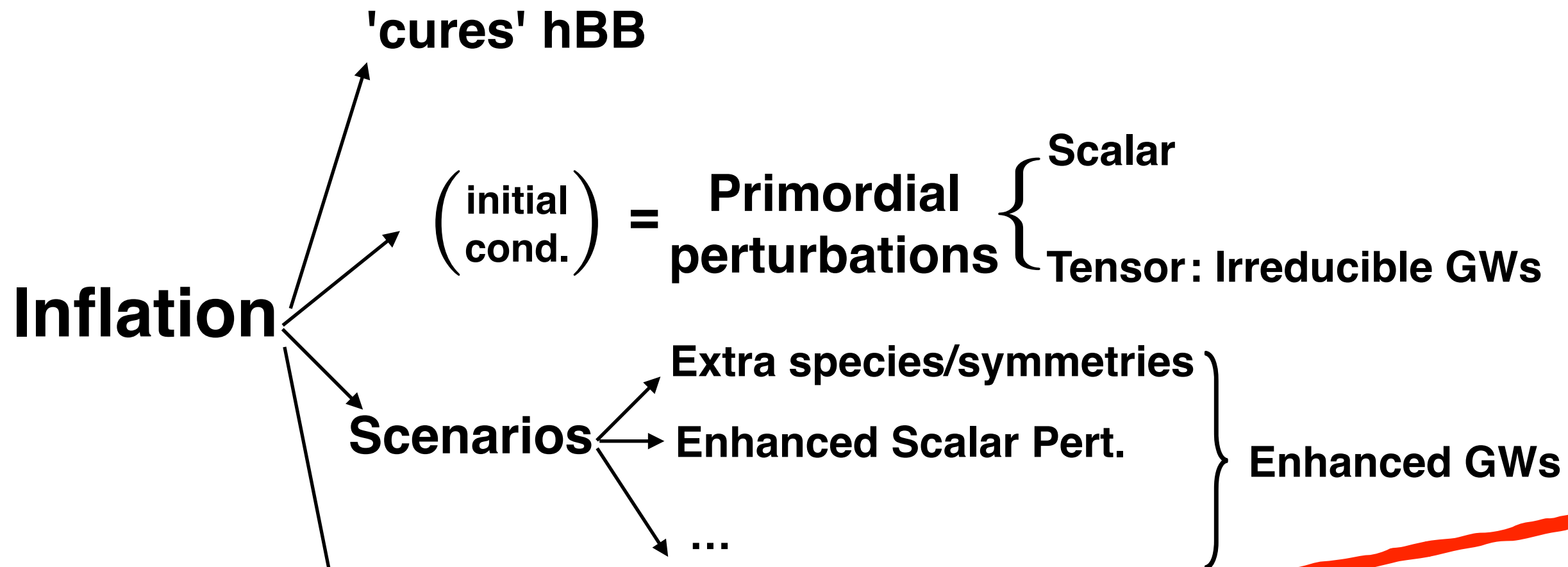
**More things on RH:**

**0812.3622 + 0812.4624**

\*  $\Delta_{\text{SW}}(\vec{k})$

\* GW anisotropies

# INFLATIONARY COSMOLOGY



**More things on RH:**

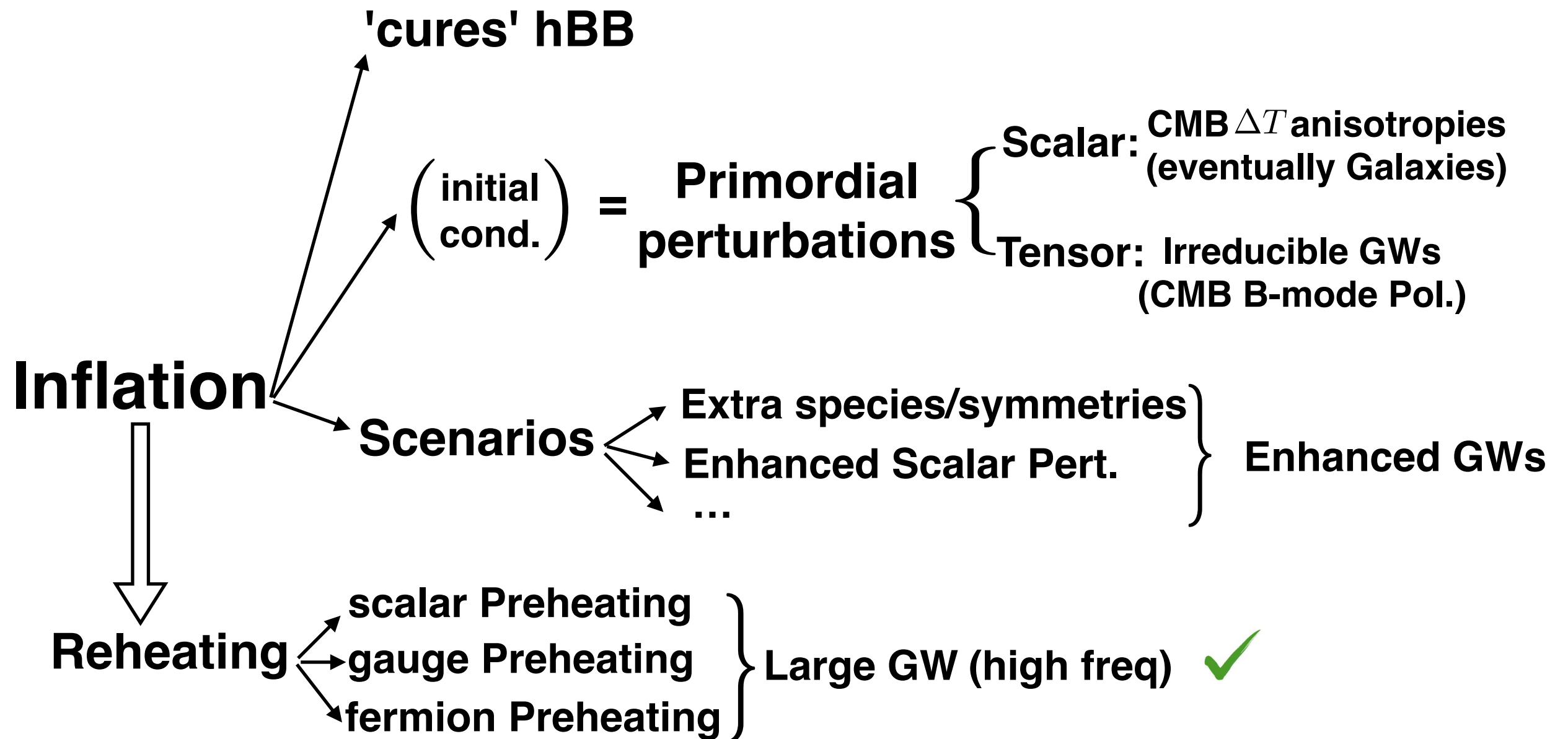
**0812.3622 + 0812.4624**

**1304.2657 + 1309.1148**

\*  $\Delta_{\text{Lensing}}^2$

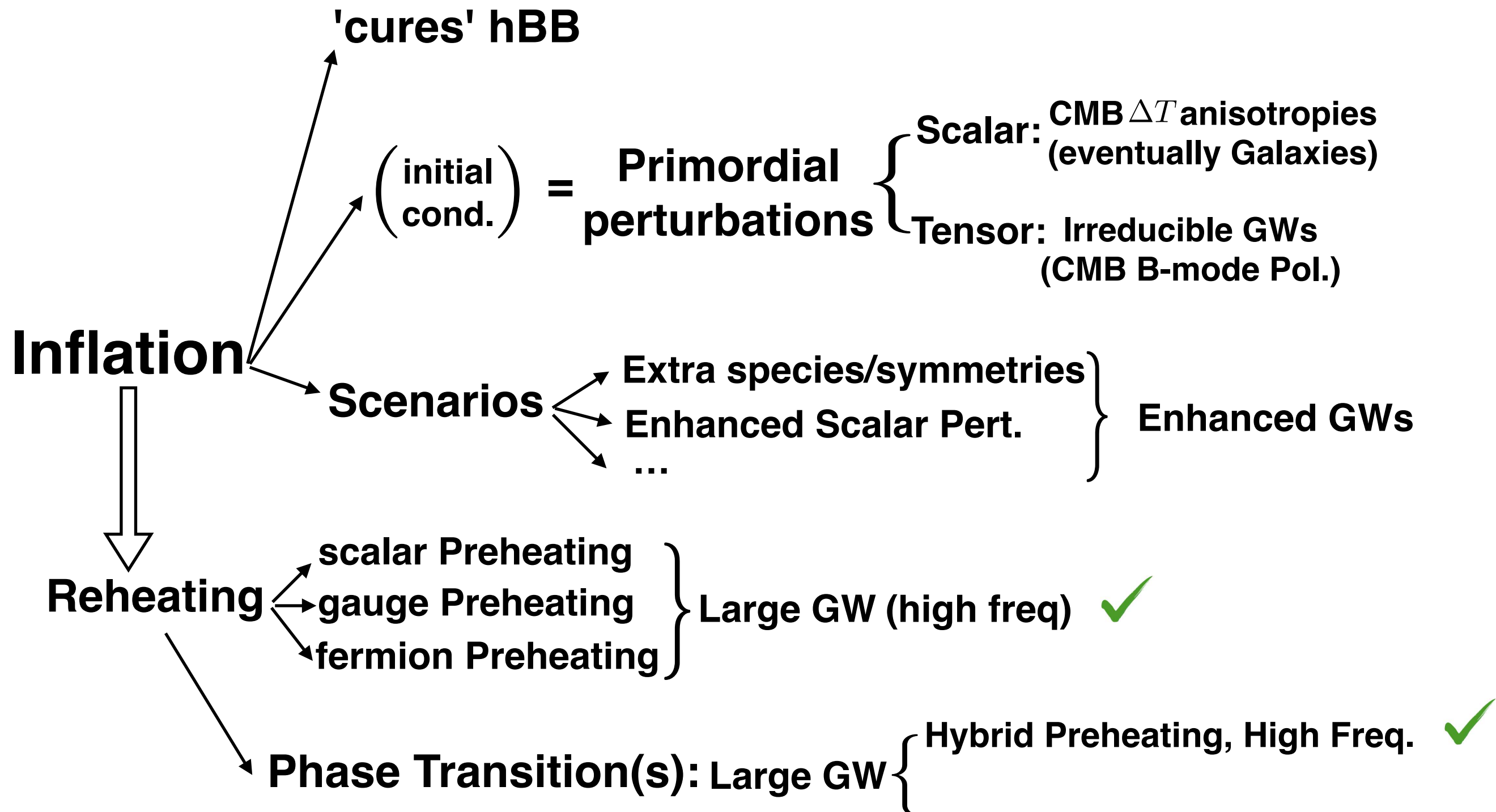
\*  $\Delta_{\text{GW}}^2$

# EARLY UNIVERSE

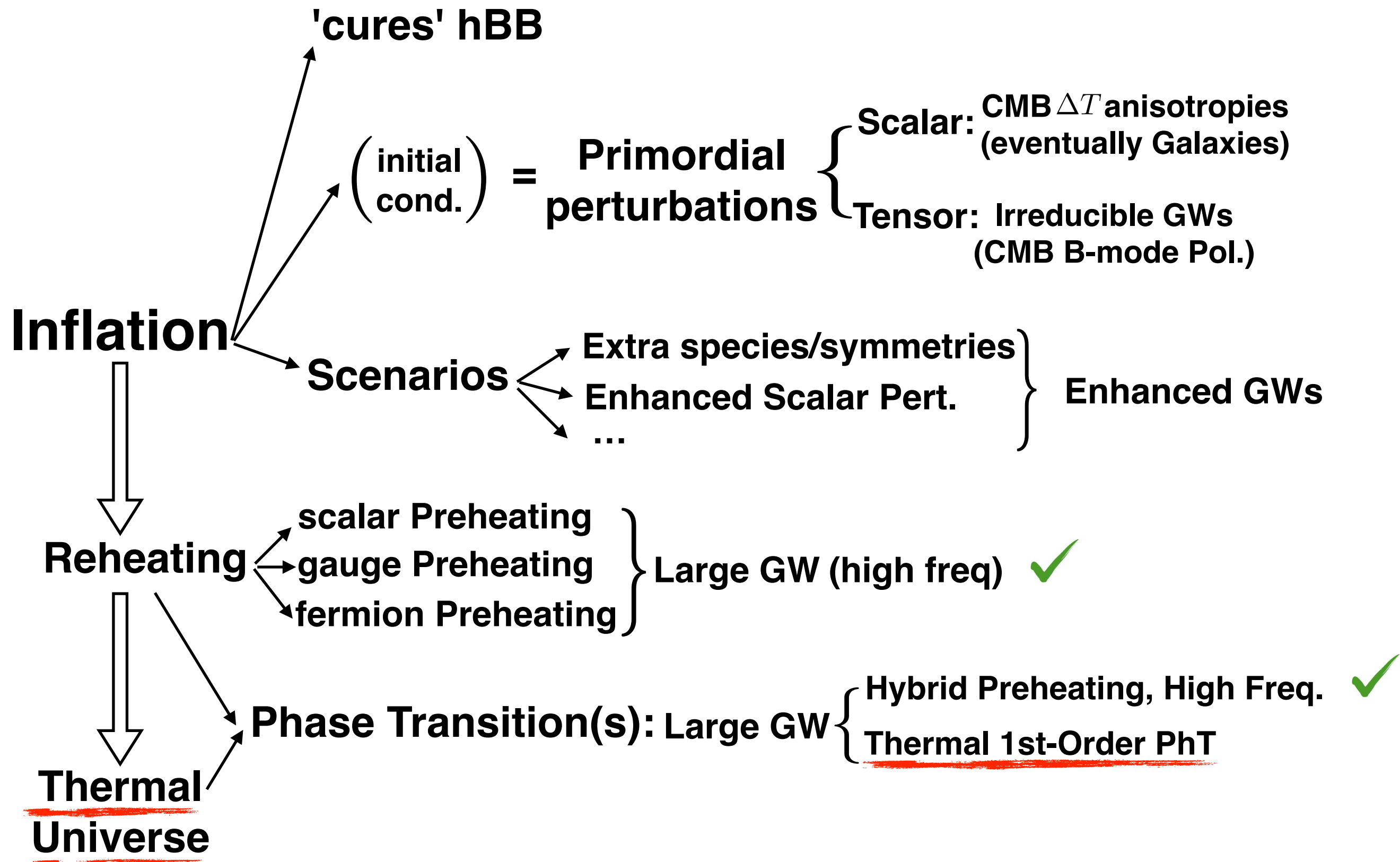




# EARLY UNIVERSE



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# OUTLINE

1st lecture

0) Gravitational Waves (GWs)

2nd lecture

1) GWs from Inflation

2) GWs from Preheating

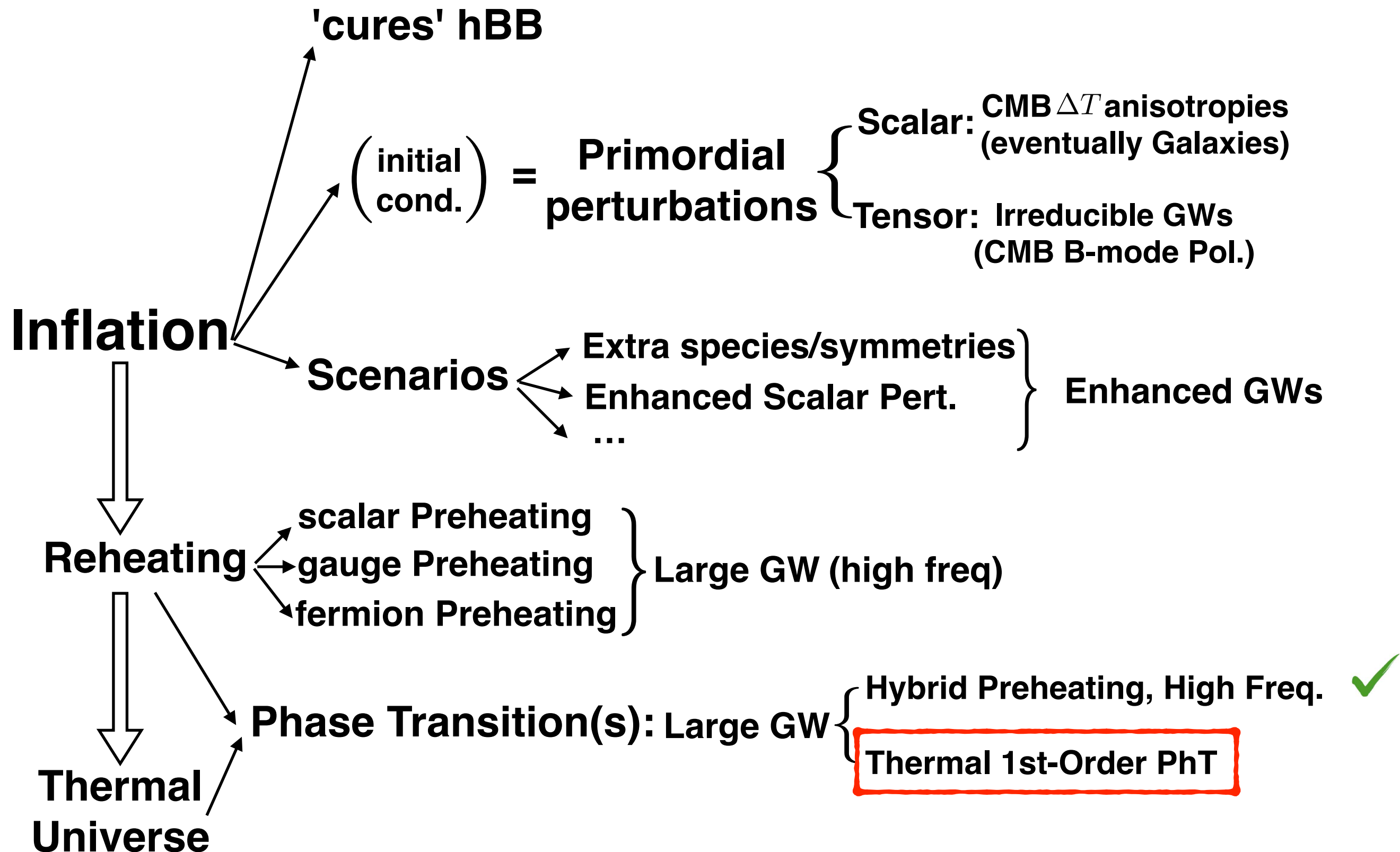
3) GWs from Phase Transitions

4) GWs from Cosmic Defects

3rd lecture



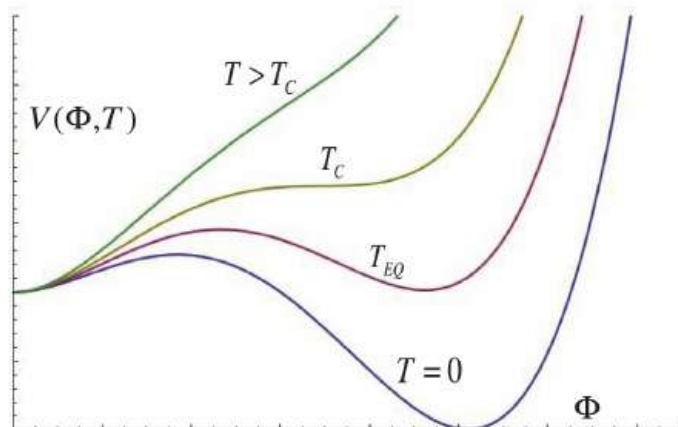
# EARLY UNIVERSE



# First order phase transitions

Universe expands, temperature decreases: phase transition triggered !

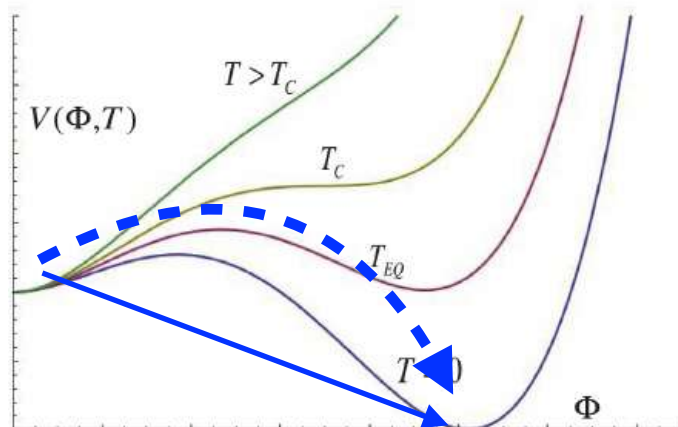
\* Potential barrier separates **true** and **false** vacua



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Universe expands, temperature decreases: phase transition triggered !

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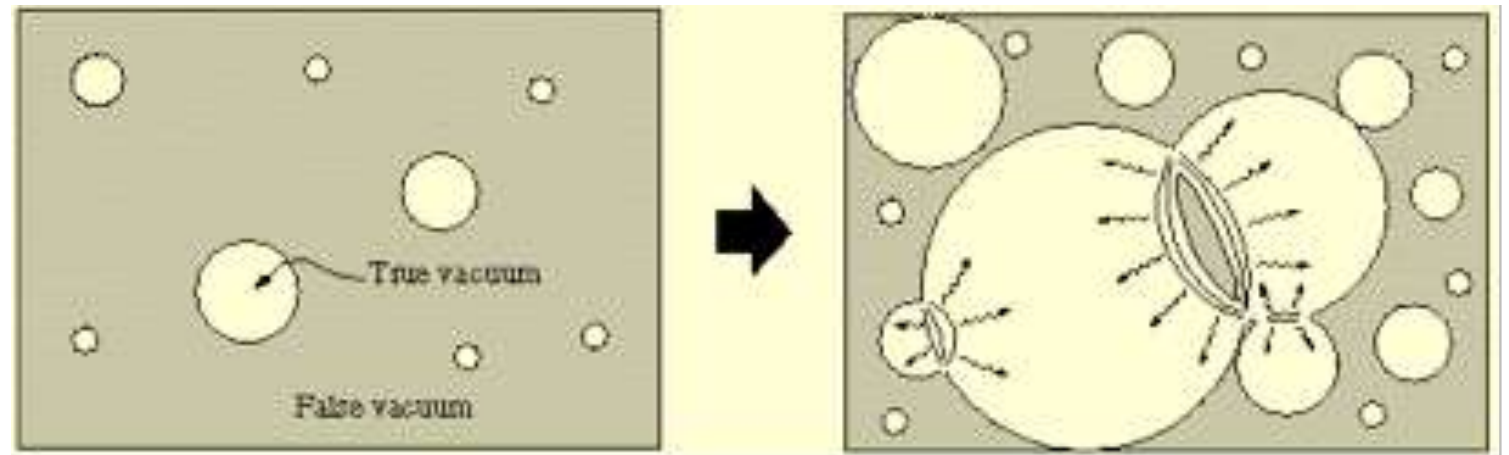
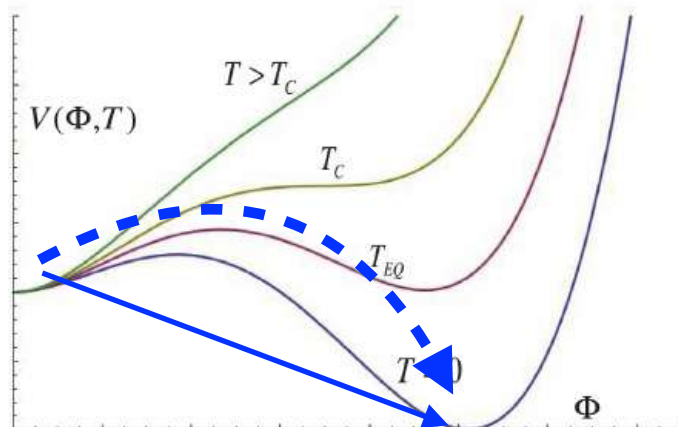


# First order phase transitions

Universe expands, temperature decreases: phase transition triggered !

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**bubble nucleation**



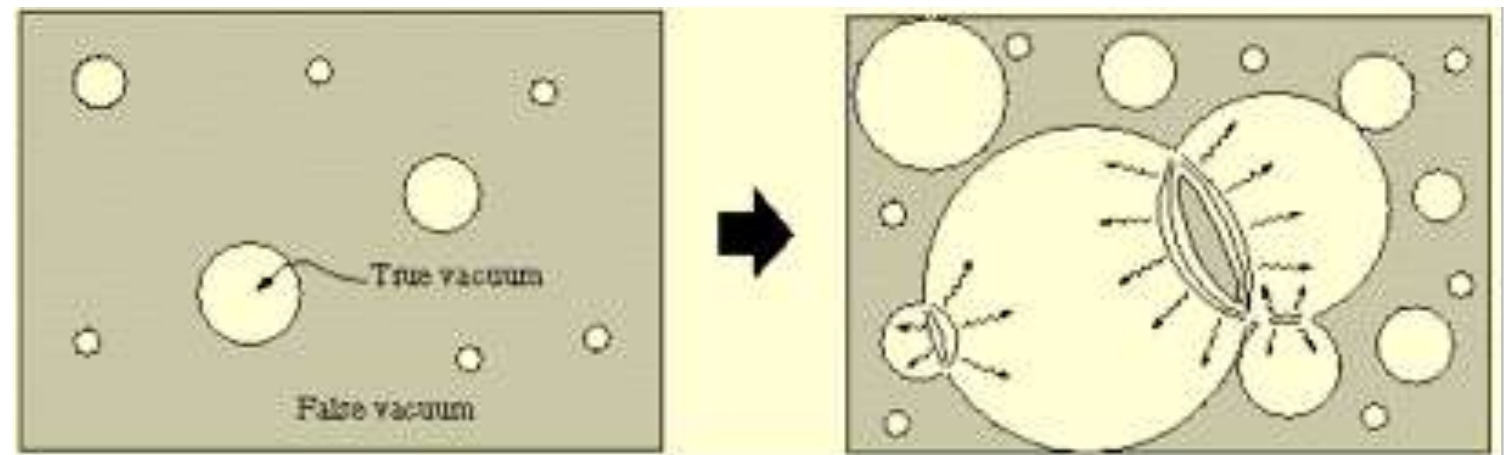
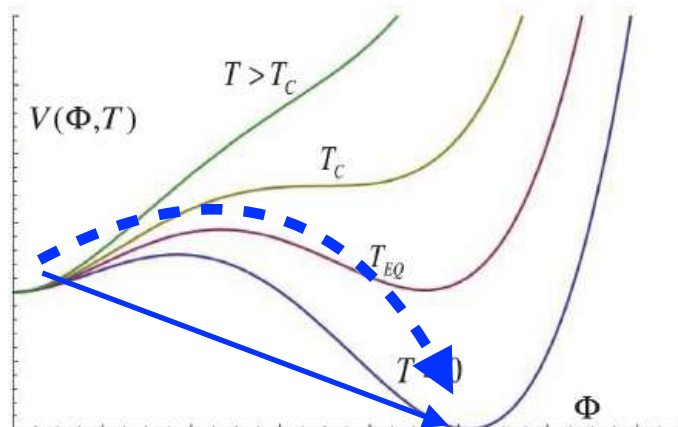


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## bubble nucleation



**GW**

**source:**  $\Pi_{ij}$  tensor  
anisotropic stress

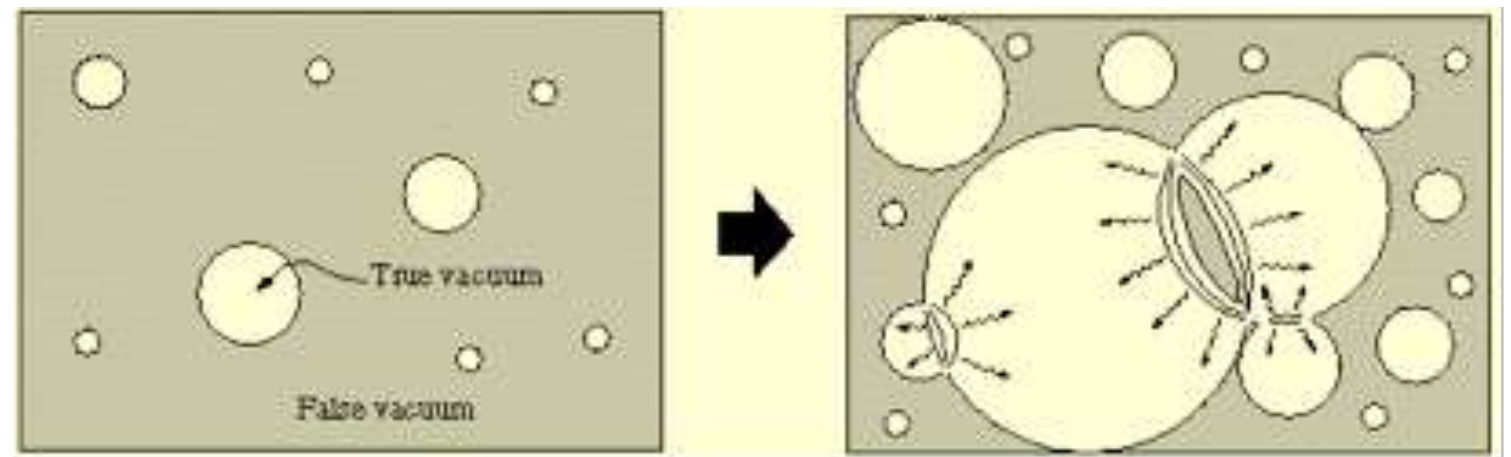
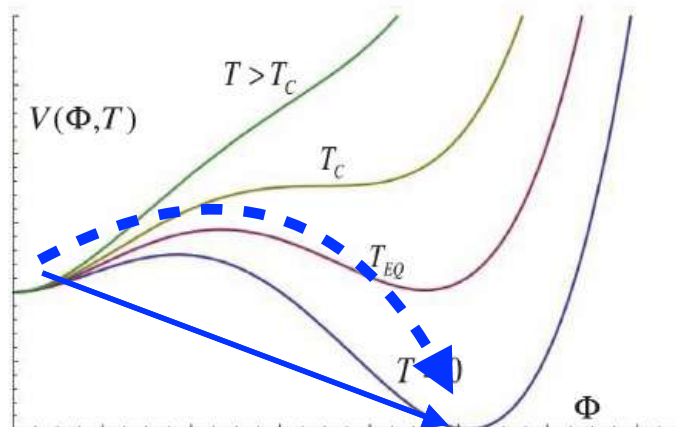
- collisions of bubble walls
- sound waves and turbulence in the fluid
- primordial magnetic fields (MHD turbulence)

# First order phase transitions

Universe expands, temperature decreases: phase transition triggered !

\* Potential barrier separates **true** and **false** vacua

**bubble nucleation**



**GW**

**source:**  $\Pi_{ij}$  tensor  
anisotropic stress

$$\Pi_{ij} \sim \partial_i \phi \partial_j \phi$$

$$\Pi_{ij} \sim \gamma^2 (\rho + p) v_i v_j$$

$$\Pi_{ij} \sim \frac{(E^2 + B^2)}{3} - E^i E^j - B^i B^j$$

# GWs from first order phase transitions

\* **GW causal source**: cannot 'operate' beyond the **horizon**

$$f_* = \frac{H(T_*)}{\epsilon_*}$$

$$\epsilon_* \leq 1$$

parameter characterising source

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parameter characterising source

Hubble rate }  
↕  
temperature

@ Today      @ Emission time

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$$



# GWs from first order phase transitions

\* **GW causal source**: cannot 'operate' beyond the **horizon**

$$f_* = \frac{H(T_*)}{\epsilon_*}$$

$$\epsilon_* \leq 1$$

parameter characterising source

Hubble rate  $\updownarrow$  temperature

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz} \simeq \text{mHz}$$

@ Today      @ Emission time

for

$$\epsilon_* \simeq 10^{-2}$$

$$T_* \simeq 1 \text{ TeV}$$

# GWs from first order phase transitions

\* **GW causal source**: cannot 'operate' beyond the **horizon**

$$f_* = \frac{H(T_*)}{\epsilon_*}$$

$$\epsilon_* \leq 1$$

parameter characterising source

Hubble rate  $\updownarrow$  temperature

$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$

$\uparrow$  @ Today       $\uparrow$  @ Emission time

$\simeq \text{mHz}$       **LISA Freq !**

for

$$\epsilon_* \simeq 10^{-2}$$

$$T_* \simeq 1 \text{ TeV}$$

$\sim$  **EW scale !**

# What is $\epsilon$ in 1st Order PhT's?

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$$

GW generation  $\longleftrightarrow$  bubbles properties

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$$\left. \begin{array}{l} \beta^{-1} : \text{duration of PhT} \\ v_b \leq 1 : \text{speed of bubble walls} \end{array} \right] \rightarrow R_* = v_b \beta^{-1} \quad \begin{array}{l} \text{size of bubbles} \\ \text{at collision} \end{array}$$



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$$\epsilon \simeq \frac{H_*}{\beta}, \quad H_* R_*$$

**BUBBLE COLLISION**

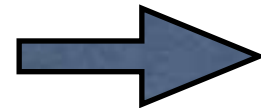
**SOUND WAVES AND  
MDH TURBULENCE**

# Parameters determining the GW spectrum

Freq.  
(today)

$$f_c = f_* \frac{a_*}{a_0} = \frac{2 \cdot 10^{-5}}{\epsilon_*} \frac{T_*}{1 \text{ TeV}} \text{ Hz}$$

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Parameter List  
(not independent)

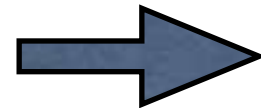
$$\frac{\beta}{H_*}, \quad v_b, \quad T_*$$

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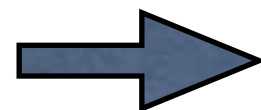


Parameter List  
(not independent)

$$\frac{\beta}{H_*}, \quad v_b, \quad T_*$$

Amplitude  
(today)

$$\Omega_{\text{GW}} \sim \Omega_{\text{rad}} \epsilon_*^2 \left( \frac{\rho_s^*}{\rho_{\text{tot}}^*} \right)^2$$



$$\frac{\rho_s^*}{\rho_{\text{tot}}^*} = \frac{\kappa \alpha}{1 + \alpha}$$

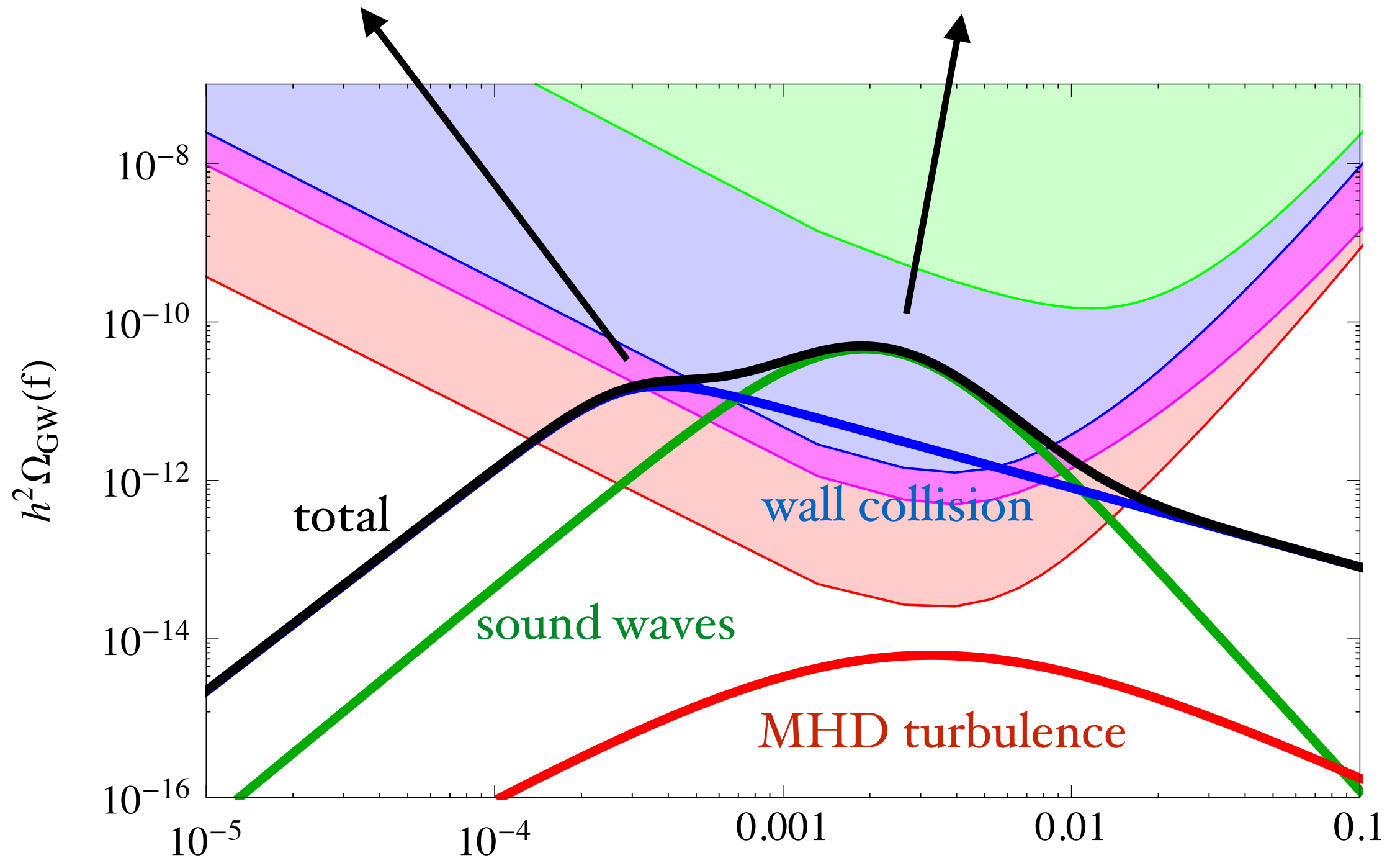
$$\alpha = \frac{\rho_{\text{vac}}}{\rho_{\text{rad}}^*}$$

$$\kappa = \frac{\rho_{\text{kin}}}{\rho_{\text{vac}}}$$

## Example of spectrum

peak of bubble collisions  $\beta$

peak of fluid-related processes  $1/R_*$



Caprini et al,  
arXiv:1512.06239

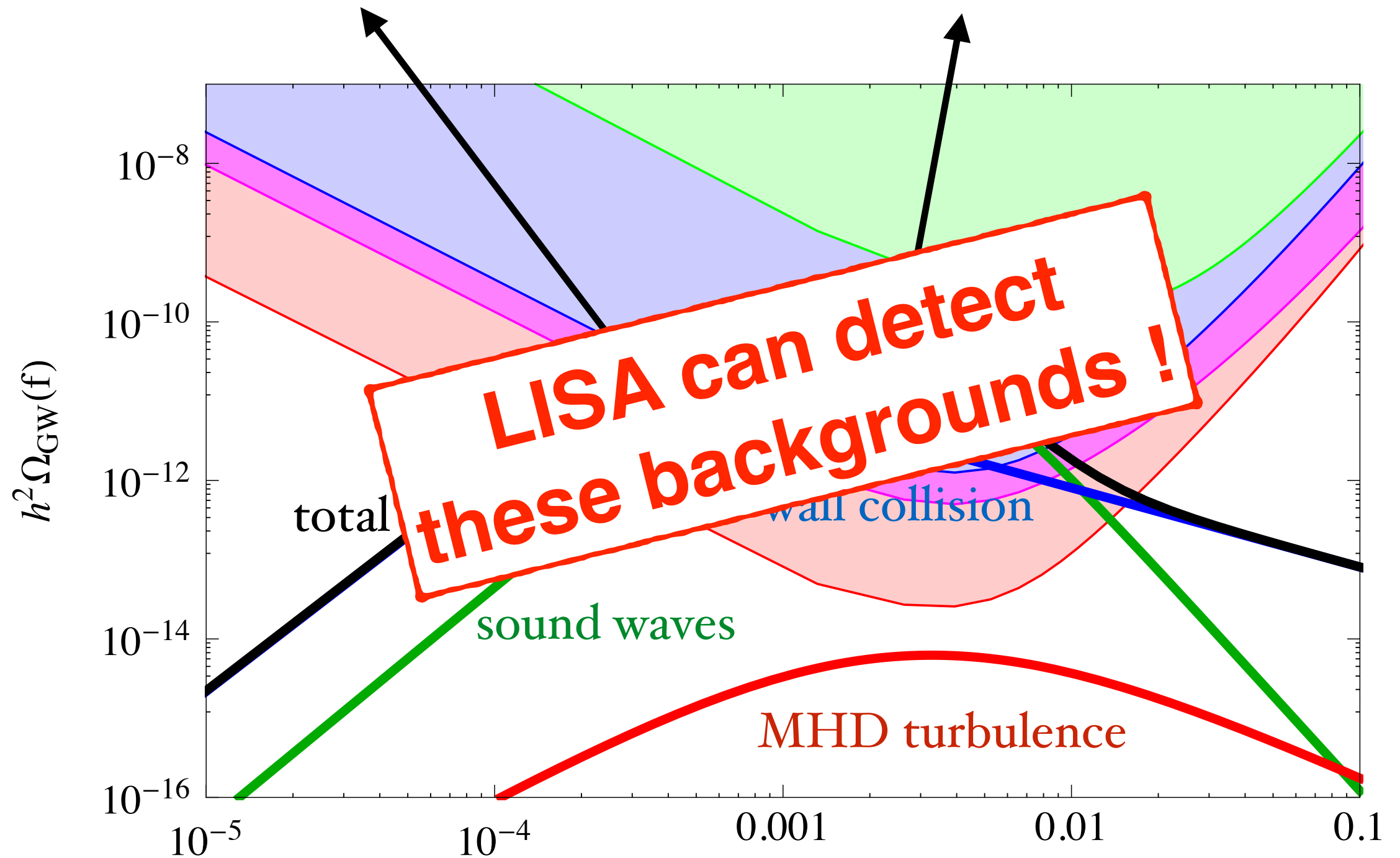
$f$  [Hz]

Caprini et al,  
arXiv:1910.13125



## Example of spectrum

peak of bubble collisions  $\beta$       peak of fluid-related processes  $1/R_*$



Caprini et al,  
arXiv:1512.06239

Caprini et al,  
arXiv:1910.13125

# Models for EWPT and beyond

- **LISA** sensitive to energy scale **10 GeV - 100 TeV !**  
(mHZ)
- **LISA can probe the EWPT in BSM models ...**
  - singlet extensions of MSSM (Huber et al 2015)
  - direct coupling of Higgs to scalars (Kozackuz et al 2013)
  - SM + dimension six operator (Grojean et al 2004)
- **... and beyond the EWPT**
  - Dark sector: provides DM candidate and confining PT (Schwaller 2015)
  - Warped extra dimensions : PT from the dilaton/radion stabilisation in RS-like models (Randall and Servant 2015)

# Evaluation of the signal

- **bubble collisions**: **analytical** and **numerical** simulations  
Huber, Konstandin '08   Cutting, Hindmarsh et al 2018, ...
- **sound waves**: **numerical** simulations of scalar field and fluid  
Hindmarsh, Weir et al 2012 - 2019,  
**analytical** Hindmarsh 2016, 2019,
- **MDH turbulence**: **analytical** evaluation  
Kosowsky et al '07, Caprini et al '09, Niksa et al '18  
**numerical** Pol et al 2019

# Evaluation of the signal

- **bubble collisions:** analytical simulations of scalar field and fluid  
Hindmarsh, Weir et al 2012 - 2019,  
analytical Hindmarsh 2016 - 2019
- **so** **Connection Particle Physics & Cosmology !**
- **M** **GW: new probe of BSM (complementary to colliders)**  
LIGO, Virgo, Niksa et al '18  
LIGO et al 2019

# Evaluation of the signal

- bubble collisions: anal

ons  
3, ...

**LISA naturally good for  
the EW PhT ( $f \sim 10^{-3}$  Hz)**

- so numerical simulations of scalar field and fluid

Hindmarsh, Weir et al 2012 - 2019,

analytical Hindmarsh 2016 - 2019

- **M GW: new probe of BSM  
(complementary to colliders)**

et al '18  
et al 2019



# Evaluation of the signal

- bubble collisions: analytical simulations

**LISA naturally good for the EW PhT** ( $f \sim 10^{-3}$  Hz)

- so numerical simulations of scalar field and fluid

Hindmarsh, Weir et al 2012 - 2019,

analytical Hindmarsh 2016 - 2019

- MHz-GHz-THz, high freq range for High-Energy phase transitions

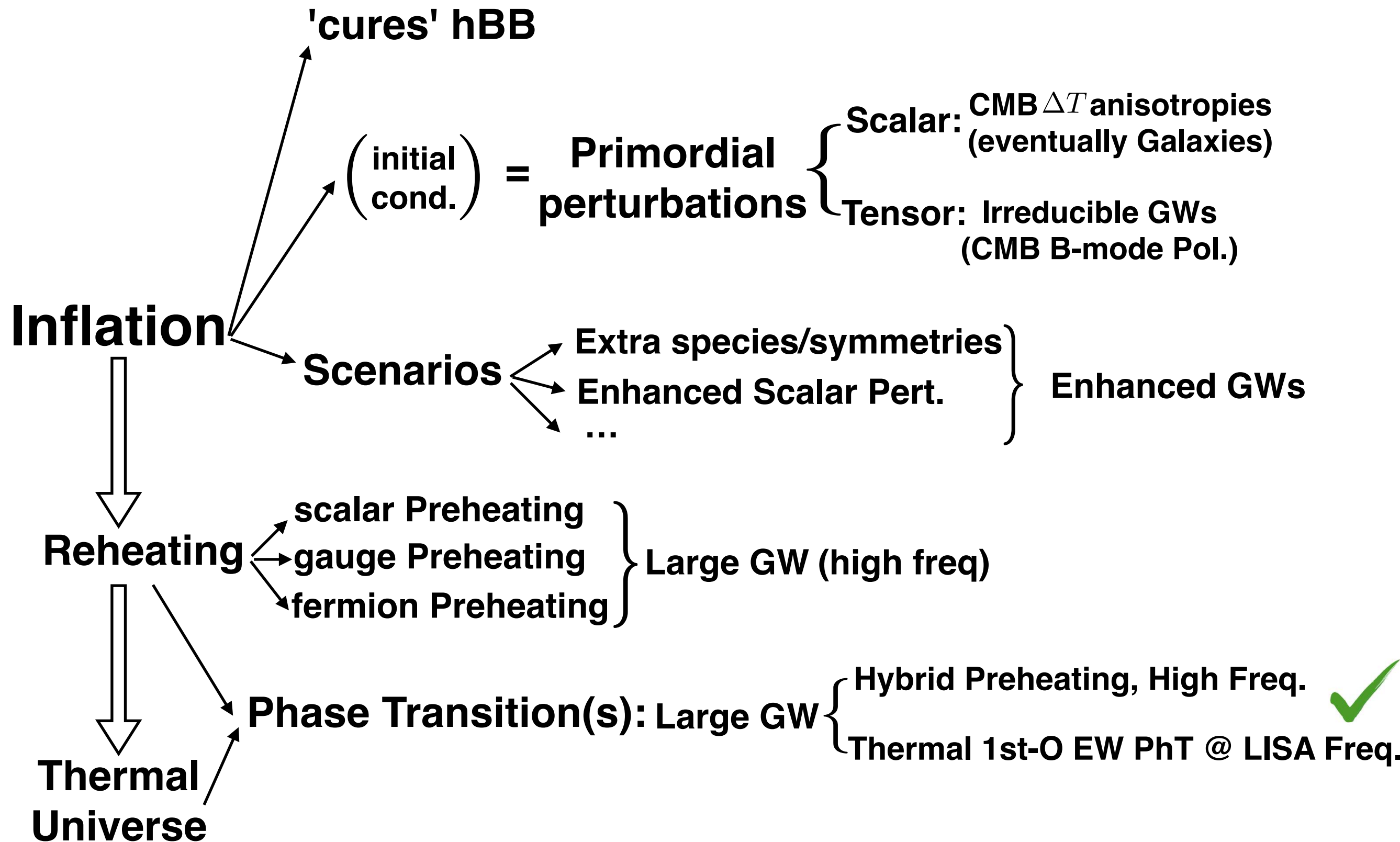
$f \sim 10^{-8} (T/\text{GeV})$  Hz

Fore et al 201

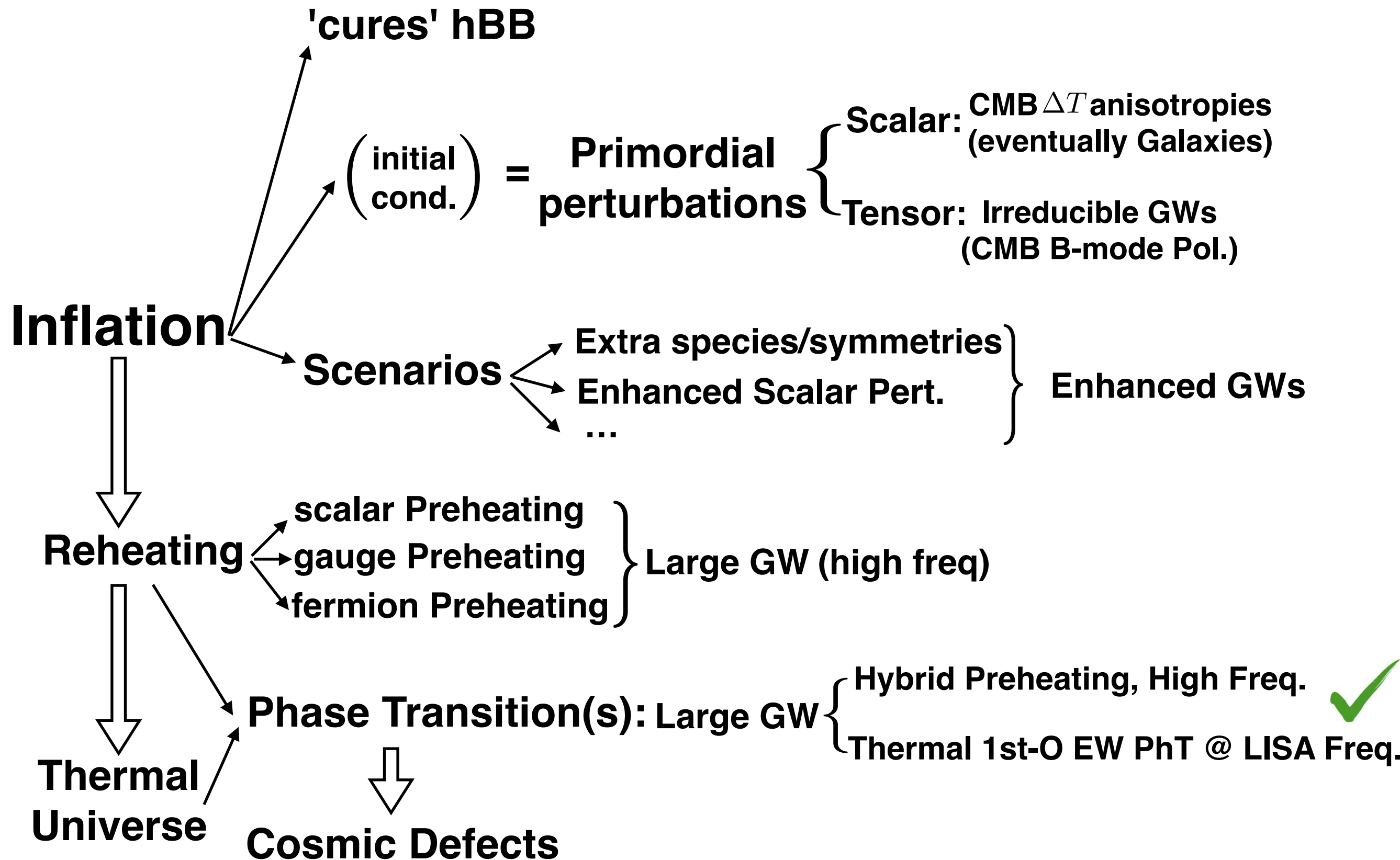
# Can we really detect a 1st-O Ph-T ?

- \* LISA can, but LHC pressures typical BSM extensions to promote EW-PhT into First Order
- \* Assuming LHC does not rule out models before, LISA can detect/constrain significant fraction of Param Space
- \* Predictions depend on many assumptions (particularly in sound waves), so is our modelling correct?
- \* Even if we detect it, then we infer  $\alpha$  and  $\beta$ , but what BSM model is behind? **not univocal !**

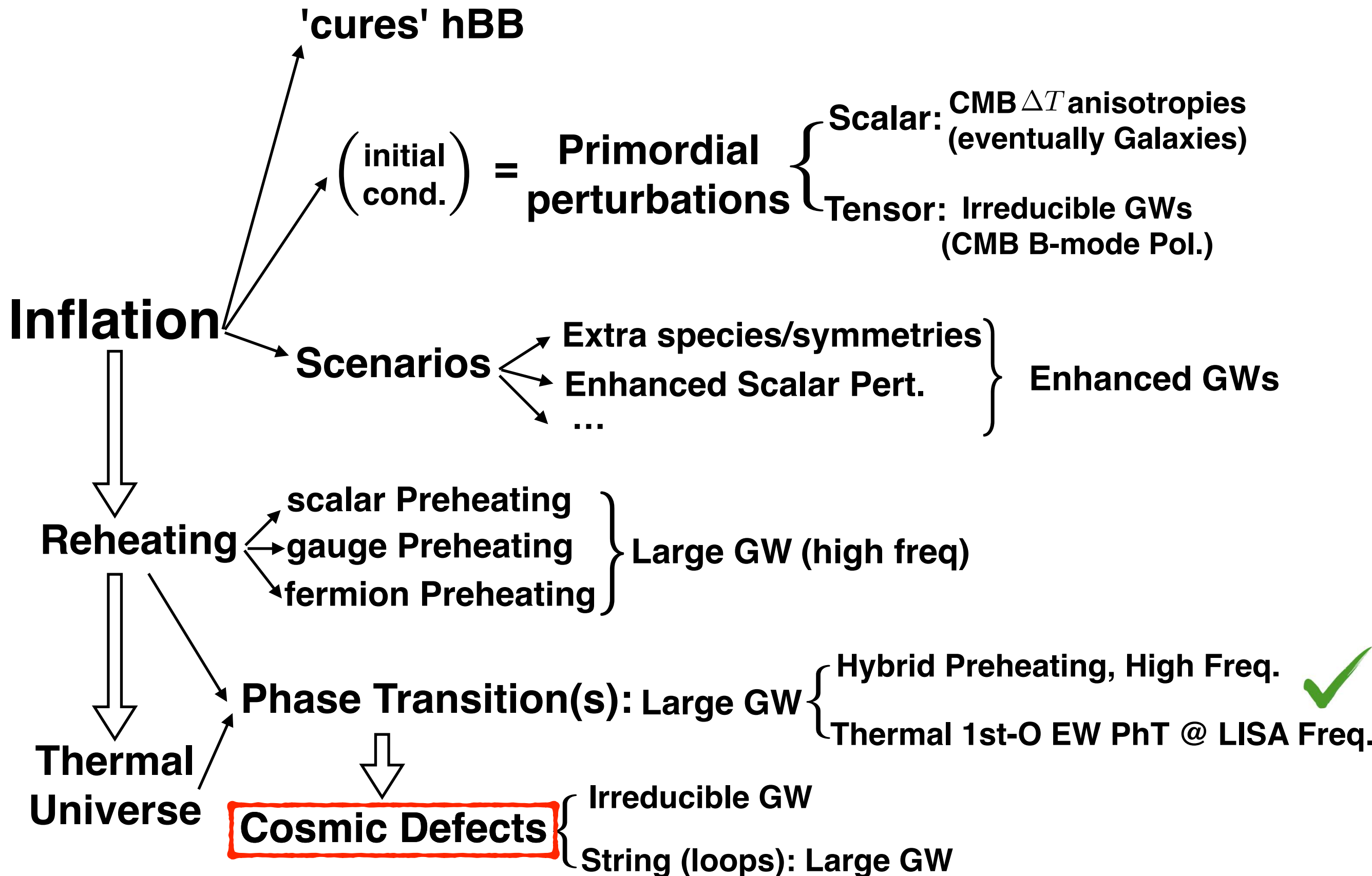
# EARLY UNIVERSE



# EARLY UNIVERSE

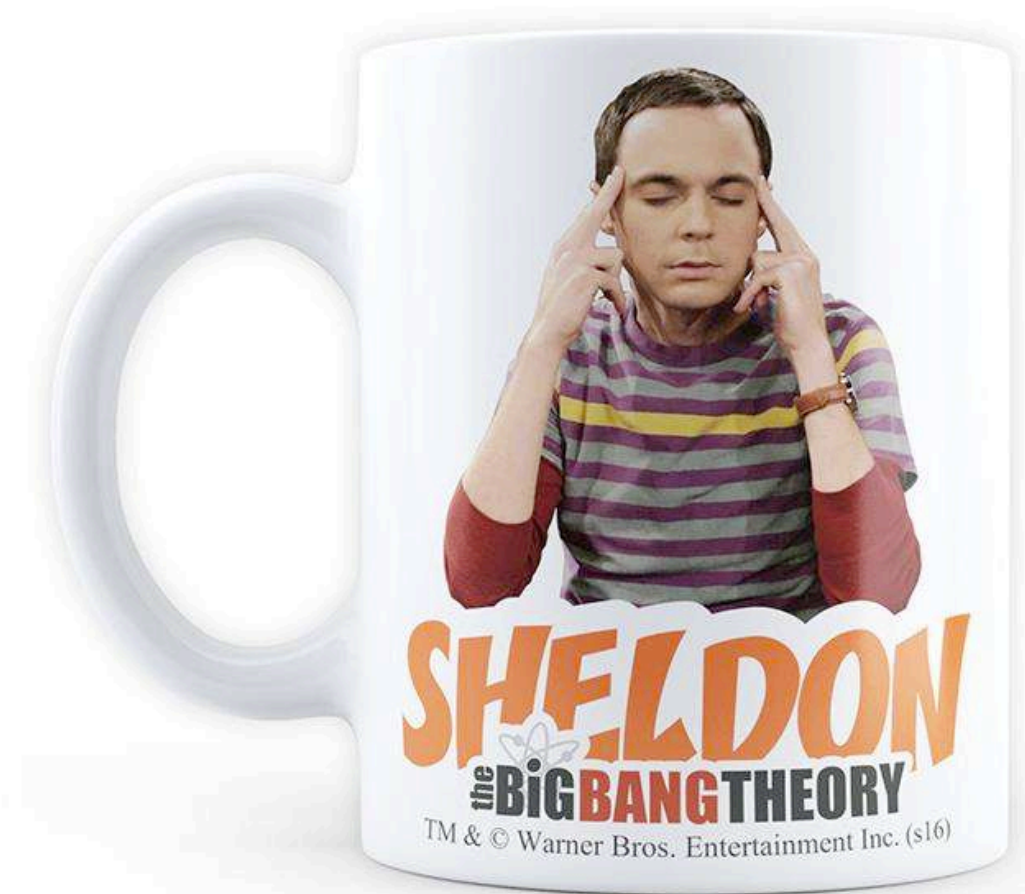


# EARLY UNIVERSE

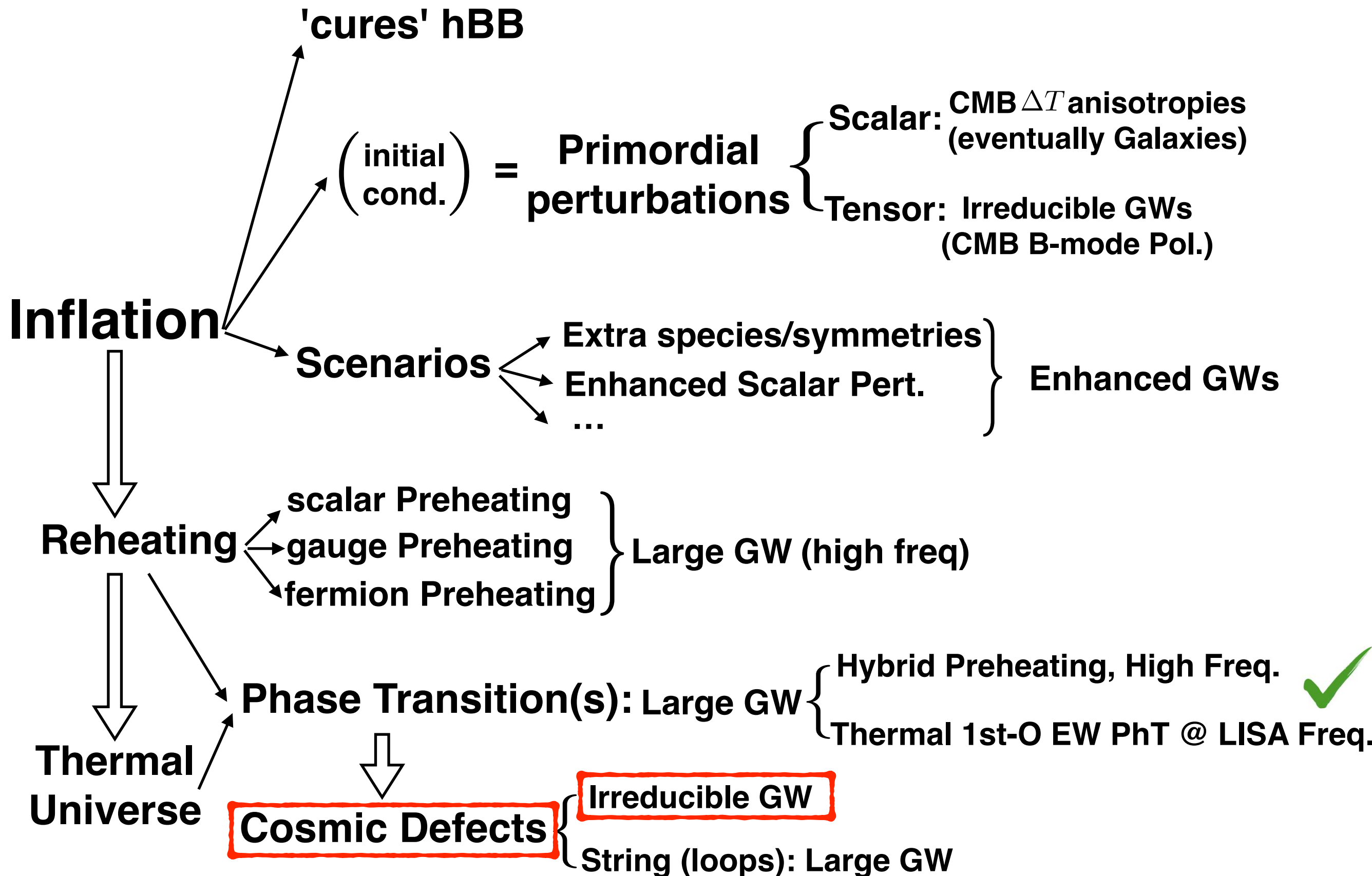




**Shall we  
coffee break ?**



# EARLY UNIVERSE



# **Cosmic Defects**

**Aftermath product of a Ph.T.**

# Introduction to Cosmic Defects

## Topology of cosmic domains and strings

T W B Kibble

Blackett Laboratory, Imperial College, Prince Consort Road, London SW7 2BZ, UK

Received 11 March 1976

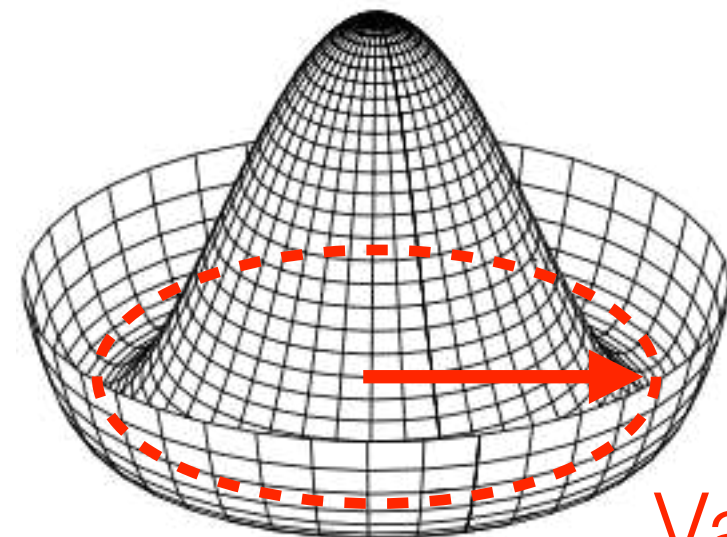
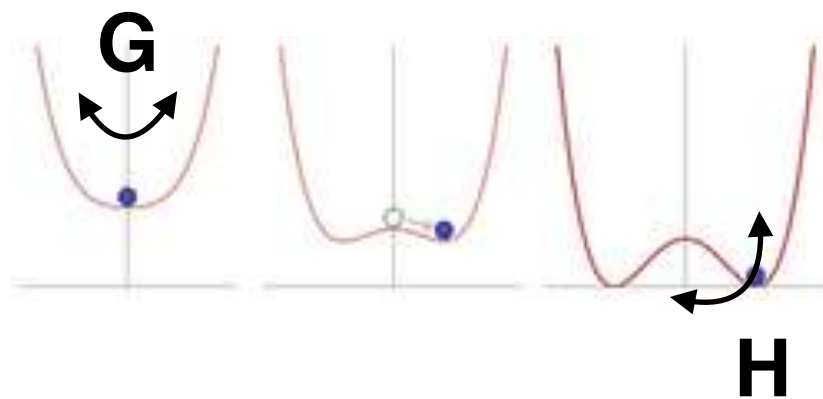
**Abstract.** The possible domain structures which can arise in the universe in a spontaneously broken gauge theory are studied. It is shown that the formation of domain walls, strings or monopoles depends on the homotopy groups of the manifold of degenerate vacua. The subsequent evolution of these structures is investigated. It is argued that while theories generating domain walls can probably be eliminated (because of their unacceptable gravitational effects), a cosmic network of strings may well have been formed and may have had important cosmological effects.

**Kibble pioneered the study of topological defect generation in the early universe.**

# Introduction to Cosmic Defects

**Kibble'76**

As recall the more general situation. In a model with symmetry group  $G$ , the vacuum expectation value  $\langle\phi\rangle$  will be restricted to lie on some orbit of  $G$ . If  $H$  is the isotropy subgroup of  $G$  at one point  $\langle\phi\rangle$ , i.e. the subgroup of transformations leaving  $\langle\phi\rangle$  unaltered, then the orbit may be identified with the coset space  $M = G/H$ . Physically  $H$  is the subgroup of unbroken symmetries, and  $M$  is the manifold of degenerate vacua. As we shall see, the topological properties of  $M$  (specifically its homotopy groups) largely determine the geometry of possible domain structures.



$$M = G/H$$

Vacuum  
Manifold

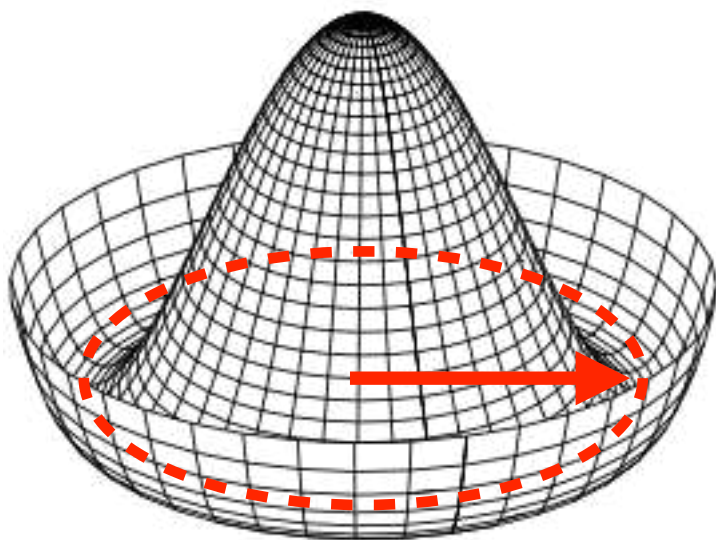


# Introduction to Cosmic Defects

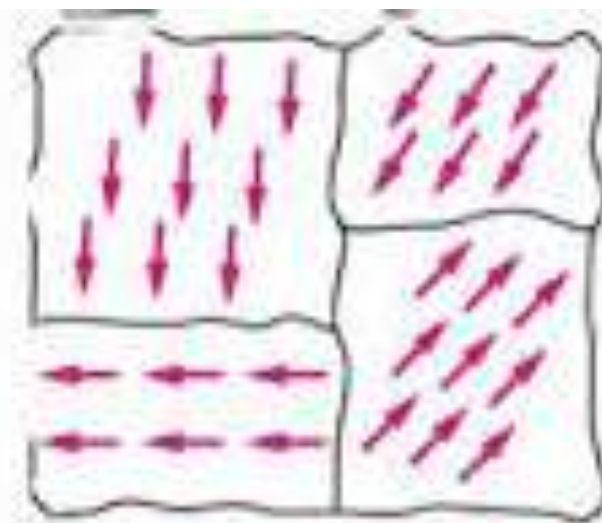
## 6. Conclusions and discussion

On this basis we showed that a domain structure can be expected to arise. The topological character of this structure depends on the homotopy groups  $\pi_k(M)$  of the manifold  $M$  of degenerate vacua. Domain walls can form if  $\pi_0(M)$  is nontrivial, i.e. if  $M$  is non-connected. If it has  $n$  connected components we find an  $n$ -phase emulsion. The formation of cosmic strings requires that  $\pi_1(M)$  be nontrivial, i.e. that  $M$  is not formed of simply connected components. Finally, 'monopoles' can form if  $\pi_2(M)$  is nontrivial.

Kibble'76



$$M = G/H$$

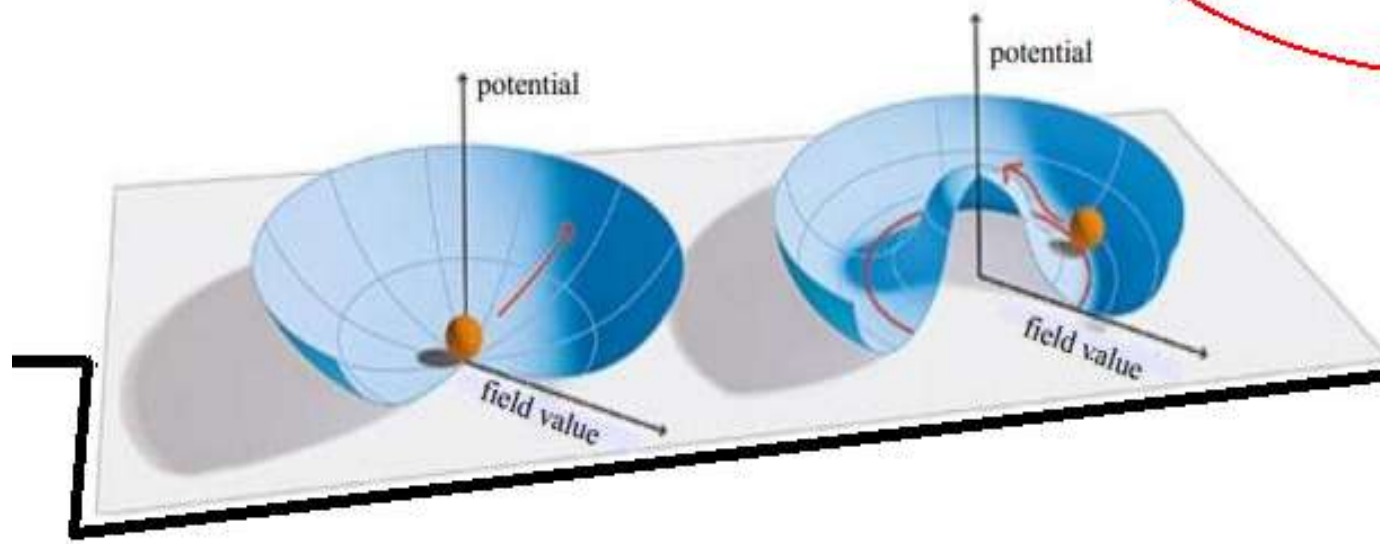


# Introduction to Cosmic Defects

$$V = \frac{\lambda}{4} (|\Phi|^2 - v^2)^2 + V_{\text{int}}(\Phi, \chi, T)$$

(1<sup>st</sup> Order, 2<sup>nd</sup> Order, Cross-Over)

$$V_{\text{int}} \sim \begin{cases} g_T^2 |\Phi|^2 T^2 & (\text{THERMAL}) \\ g^2 |\Phi|^2 \chi^2 & (\text{FIELD INT.}) \end{cases}$$

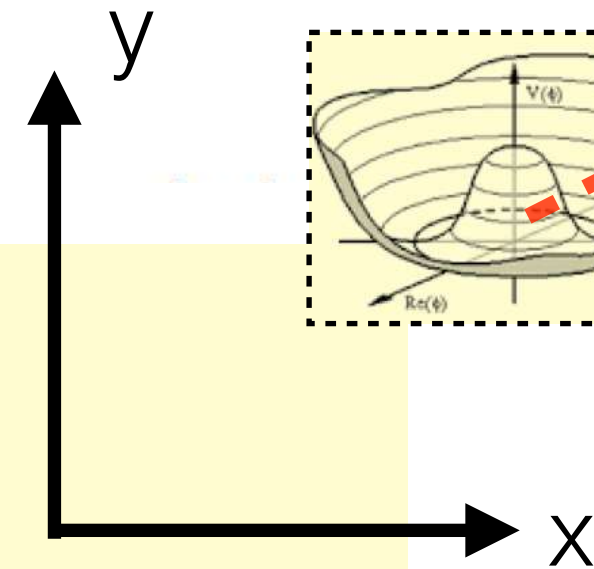
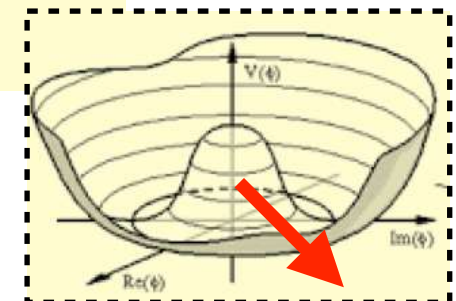
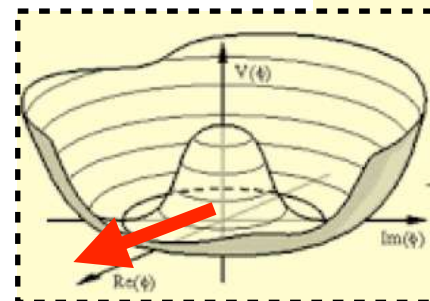
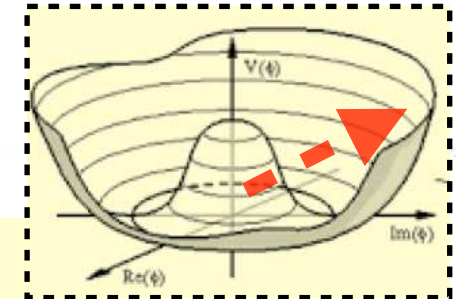
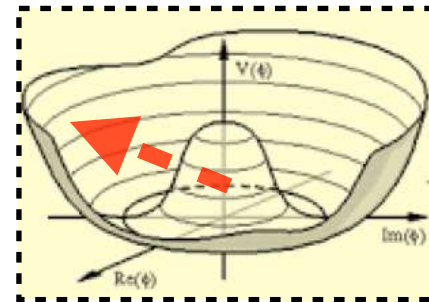
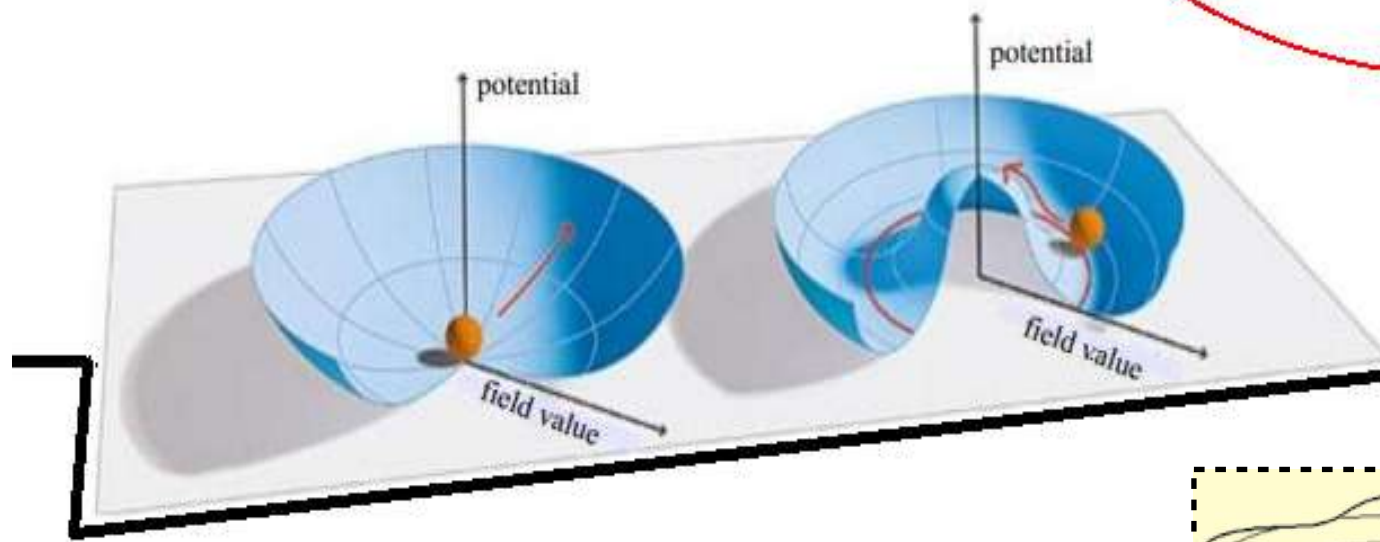


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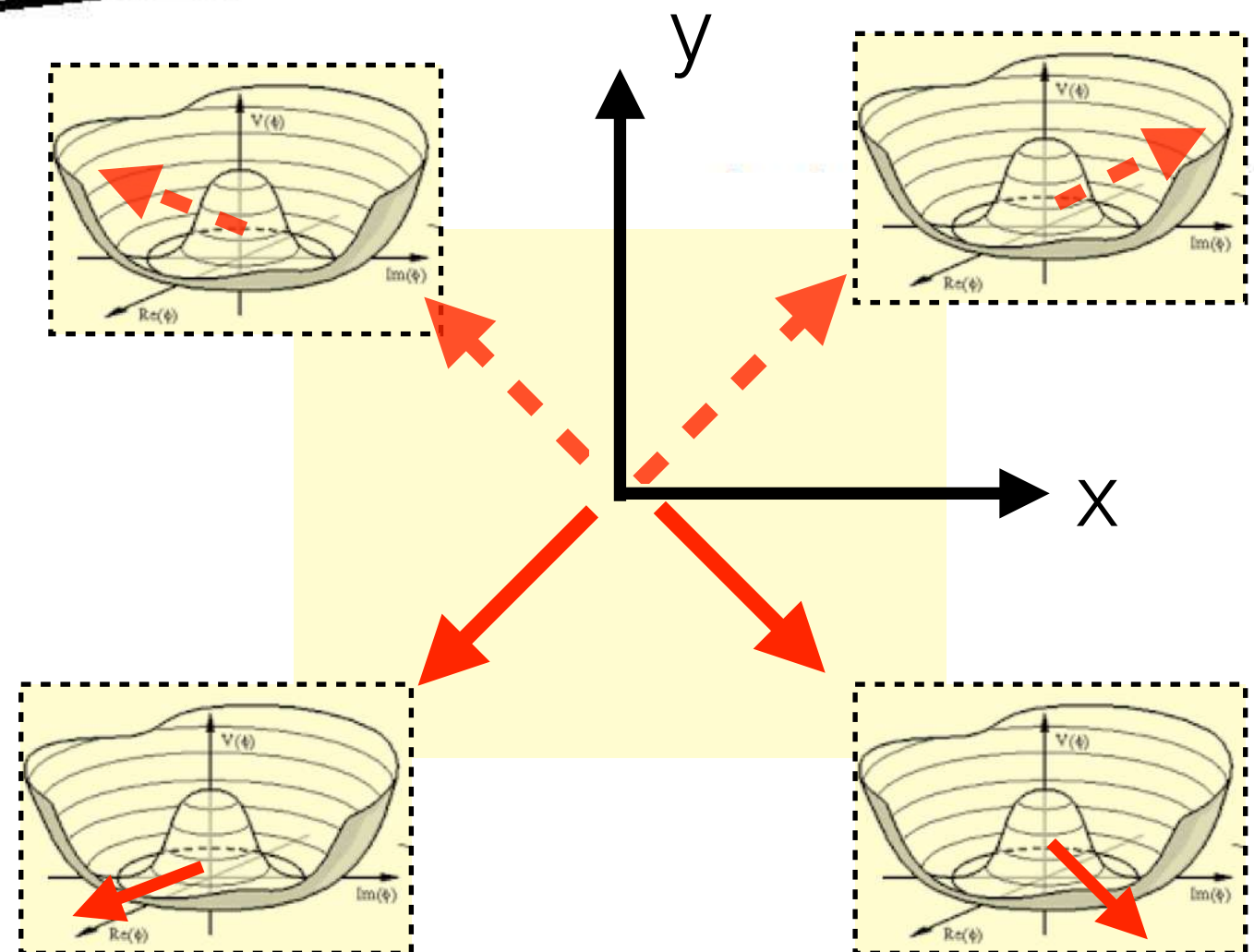
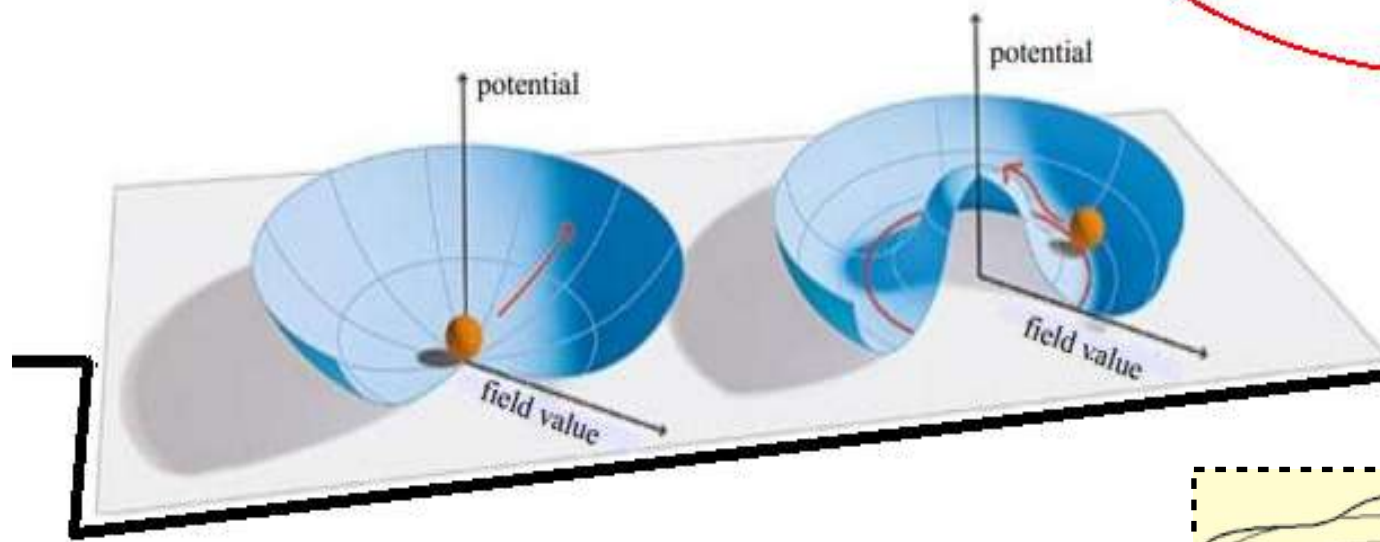


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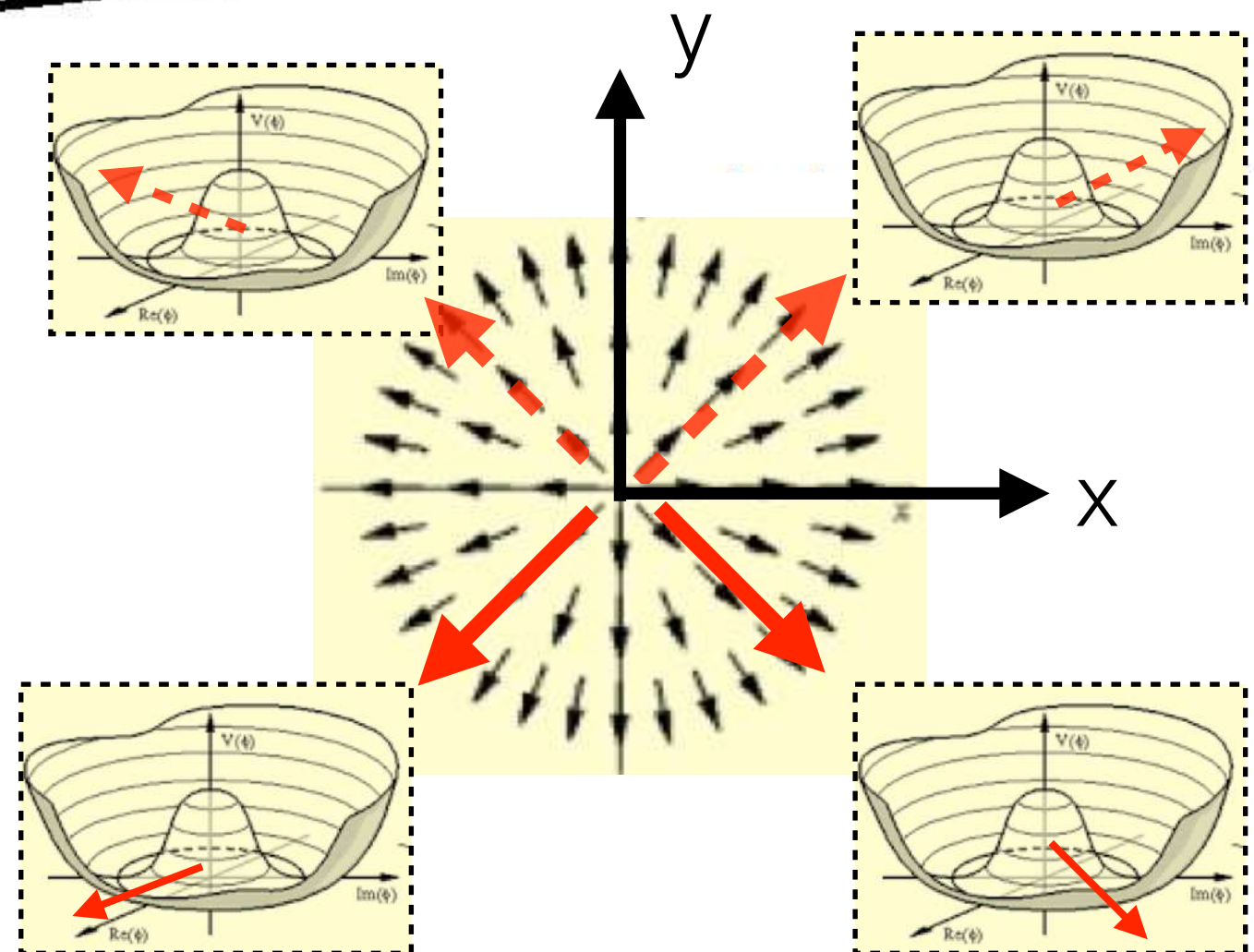
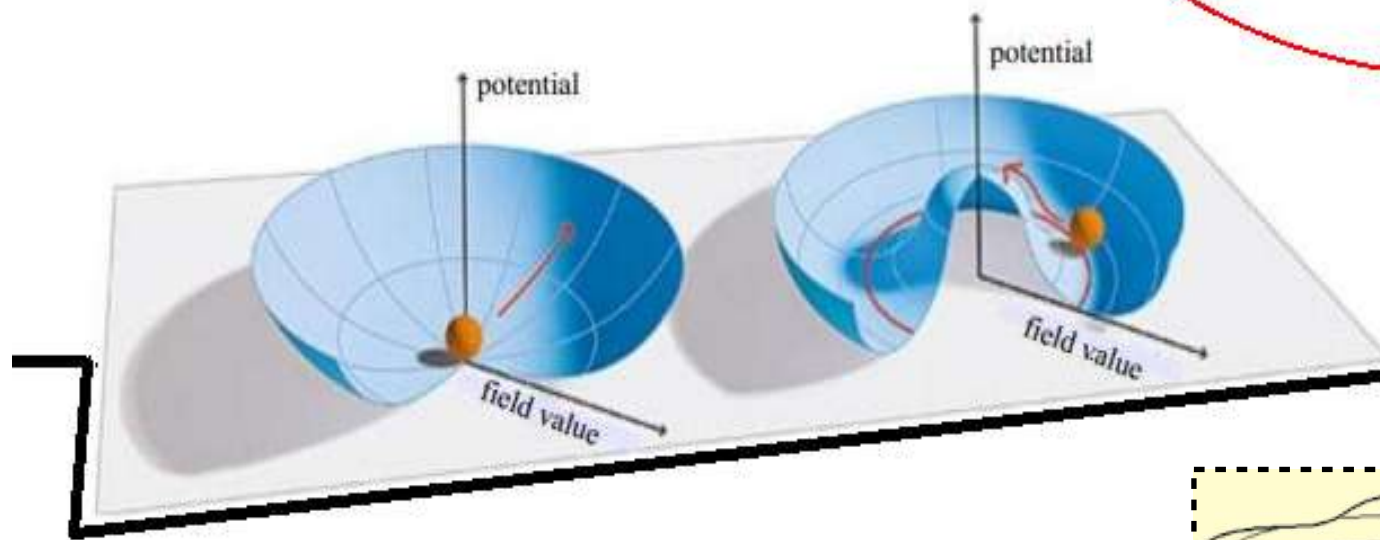


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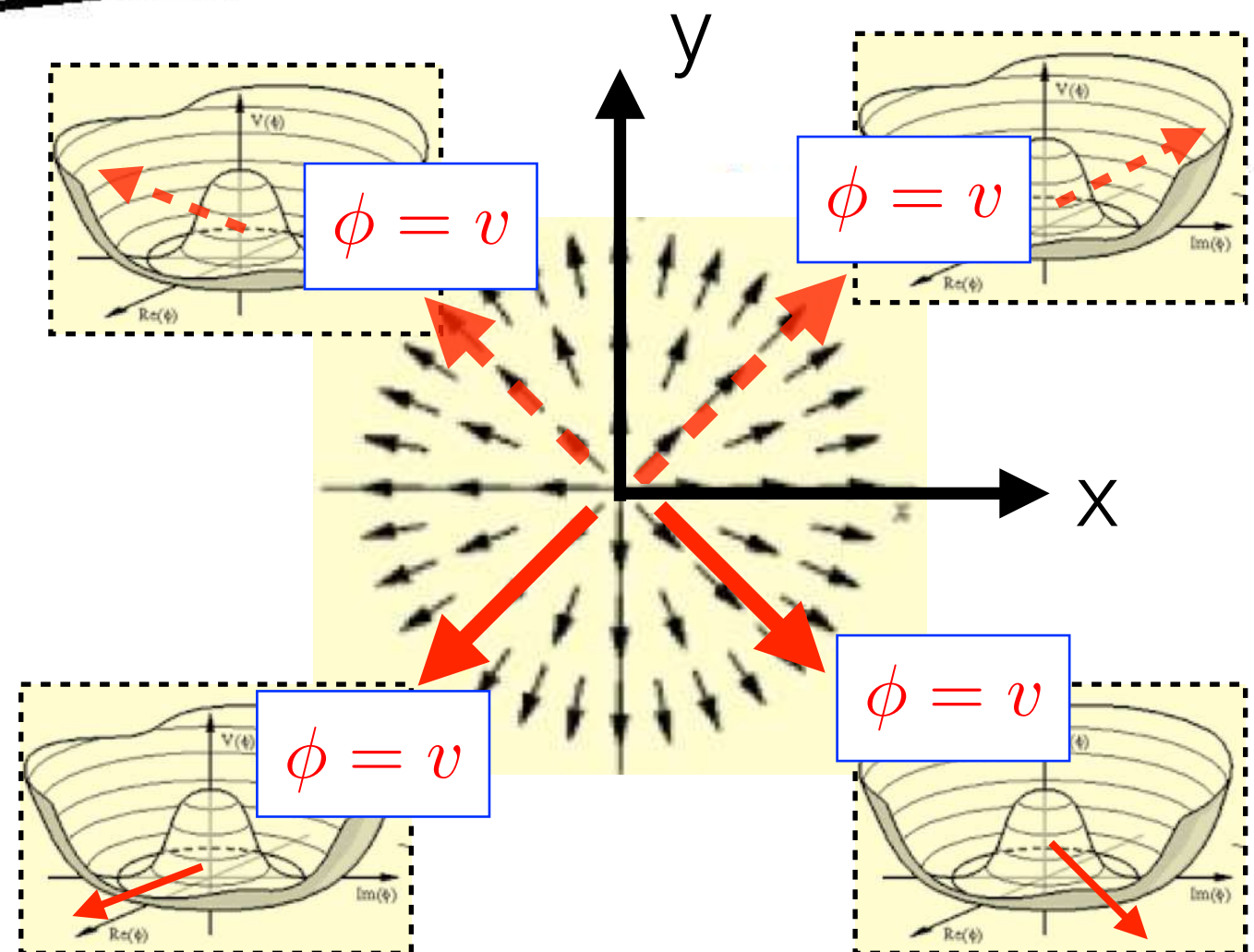
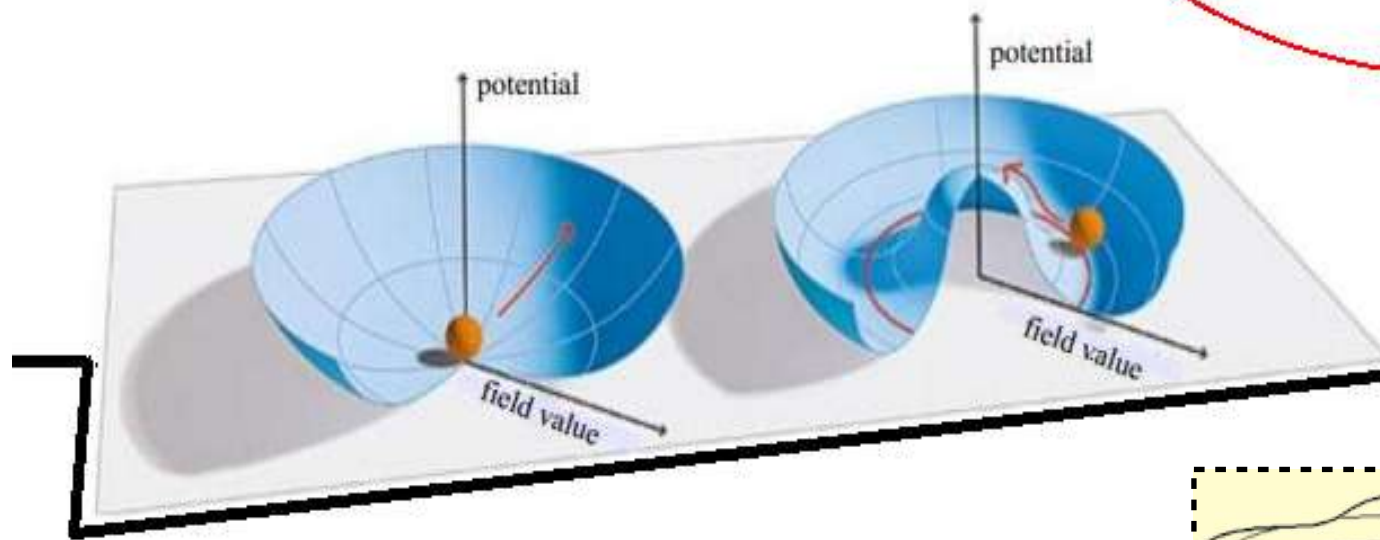


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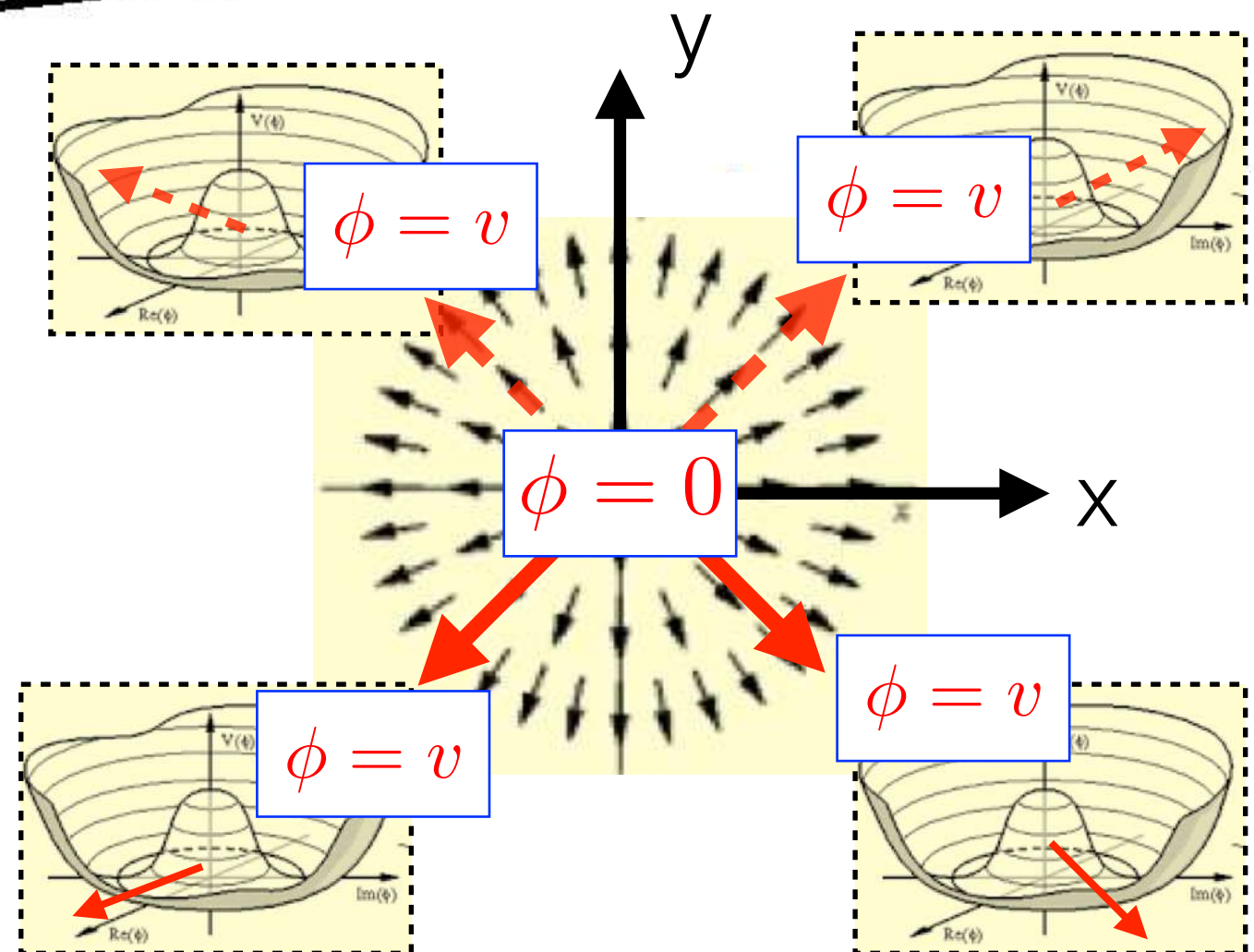
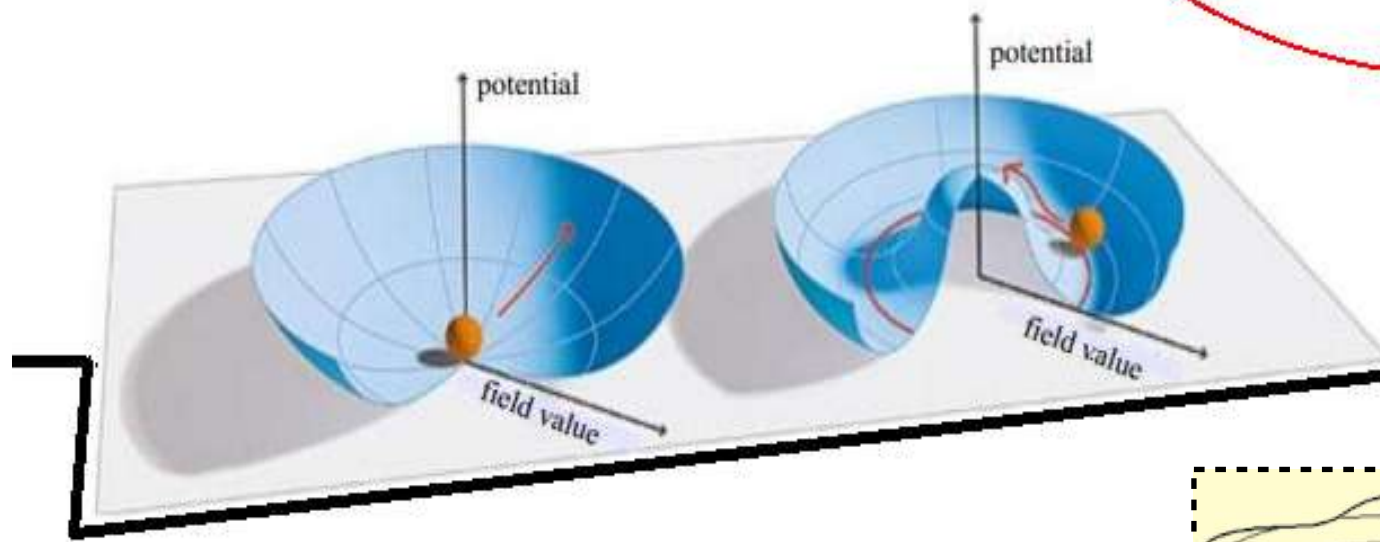


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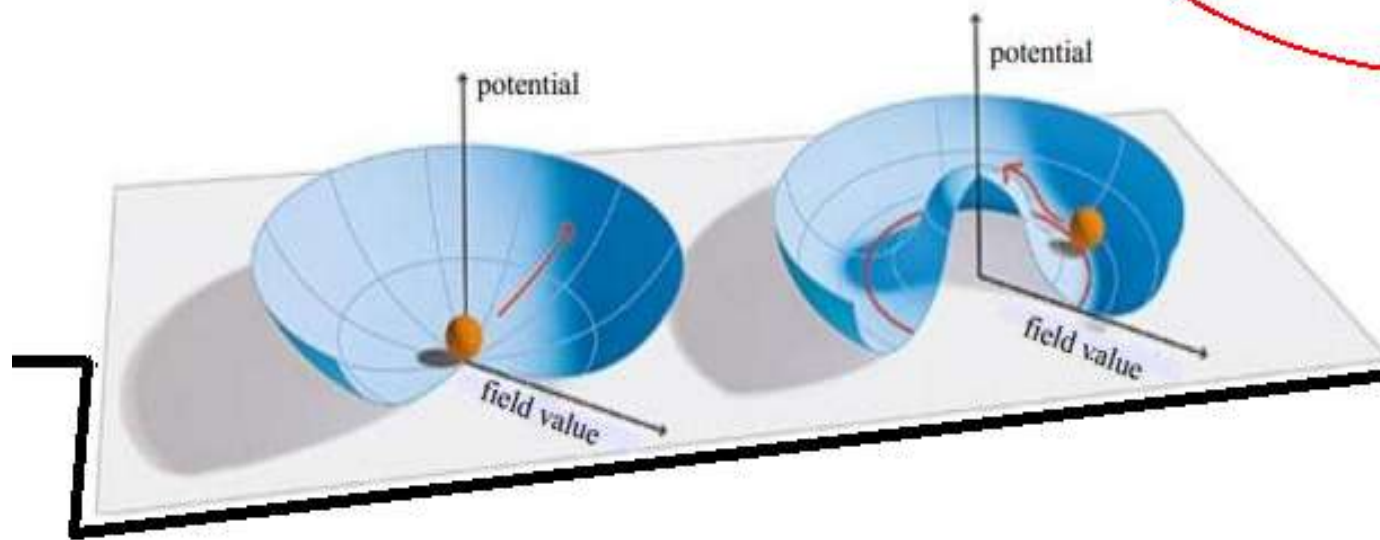


# Introduction to Cosmic Defects

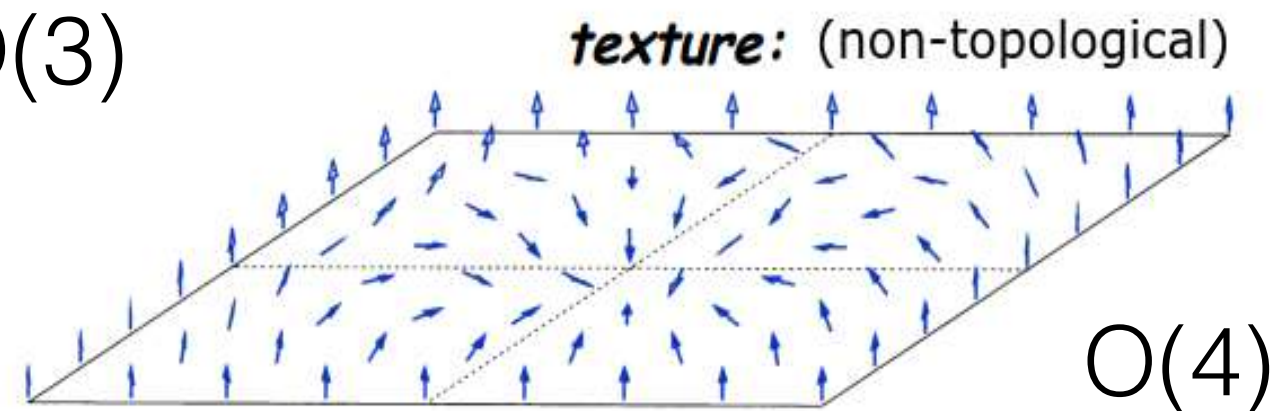
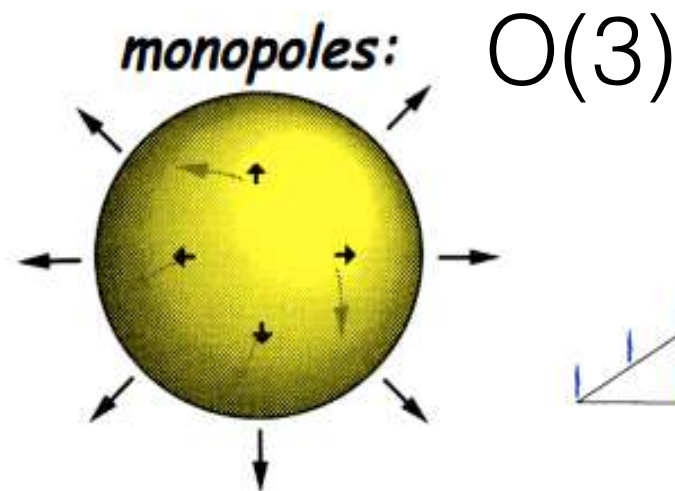
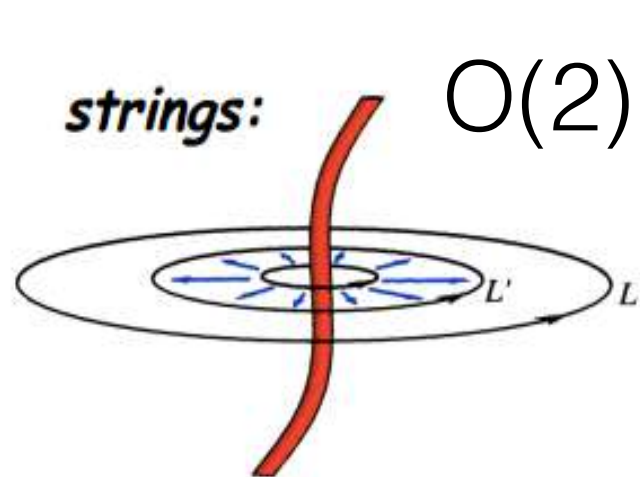
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**ZOOLOGY:**

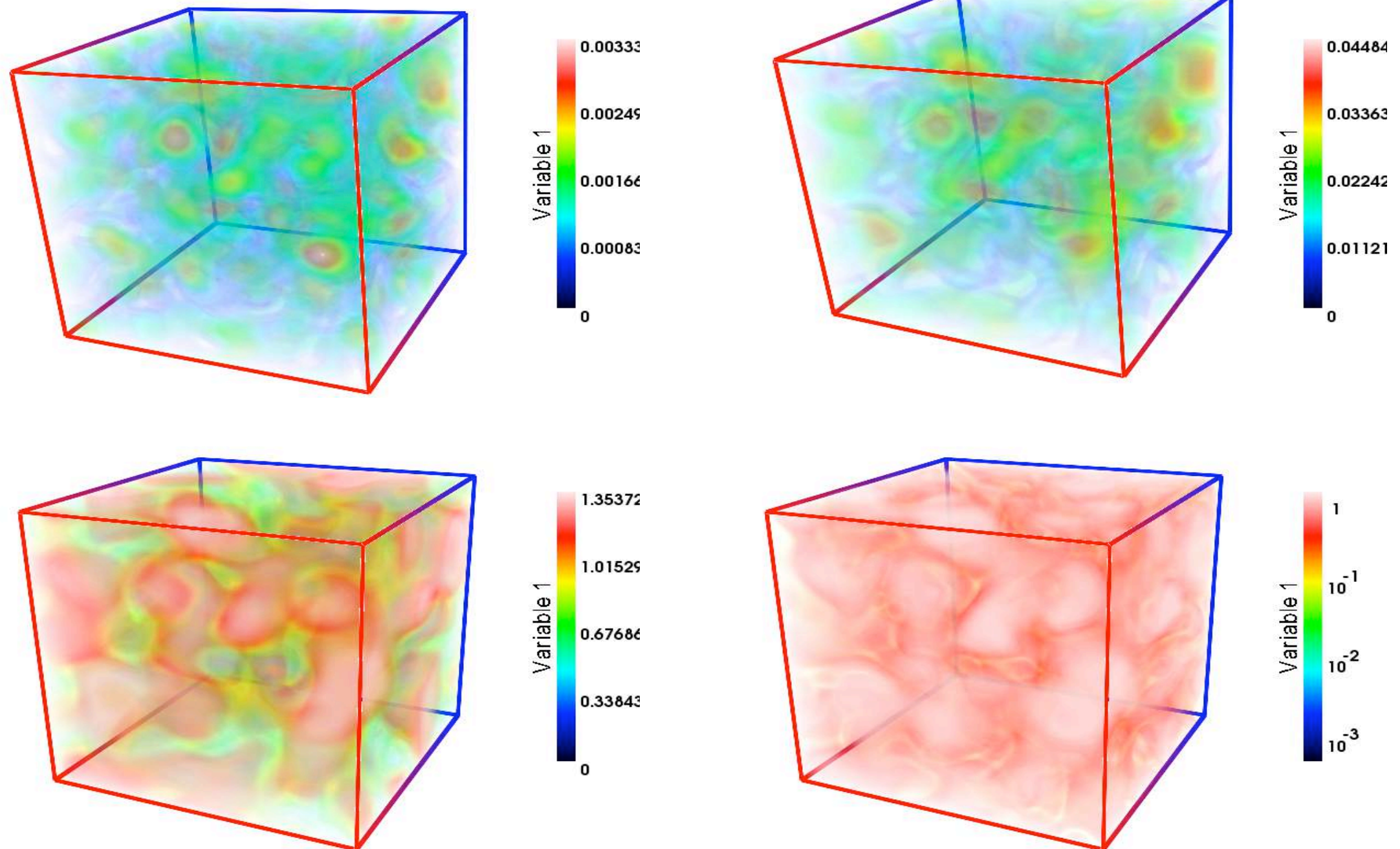


**MICRO-PHYSICS**  $\longrightarrow$  **COSMIC DEFECTS**  
 (M = G/H)

# Introduction to Cosmic Defects

## U(1) Breaking (after Hybrid Inflation)

### Higgs Dynamics

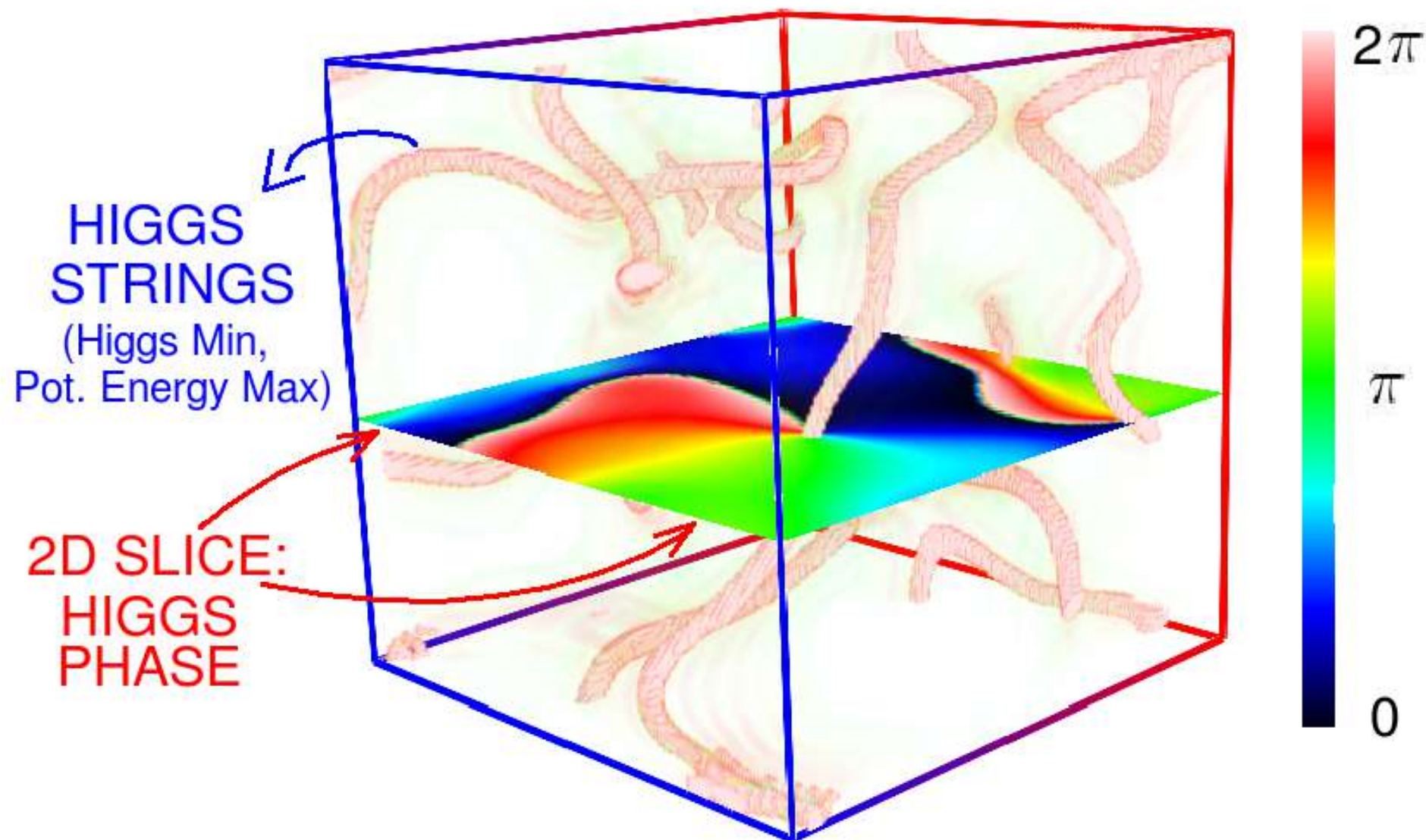




# Introduction to Cosmic Defects

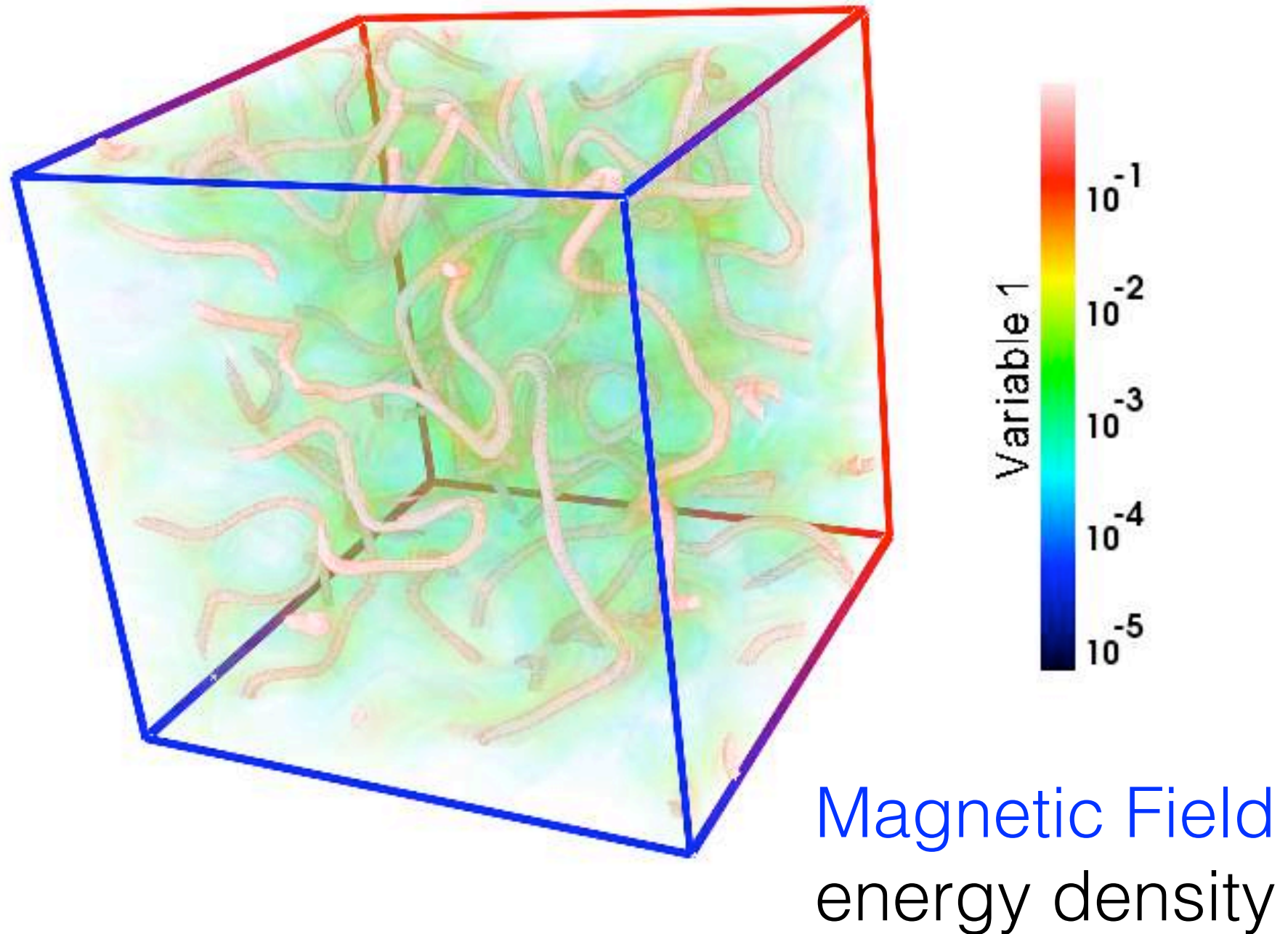
U(1) Breaking (after Hybrid Inflation)

SNAPSHOT OF THE HIGGS ( $mt = 17$ )



# Introduction to Cosmic Defects

U(1) Breaking (after Hybrid Inflation)

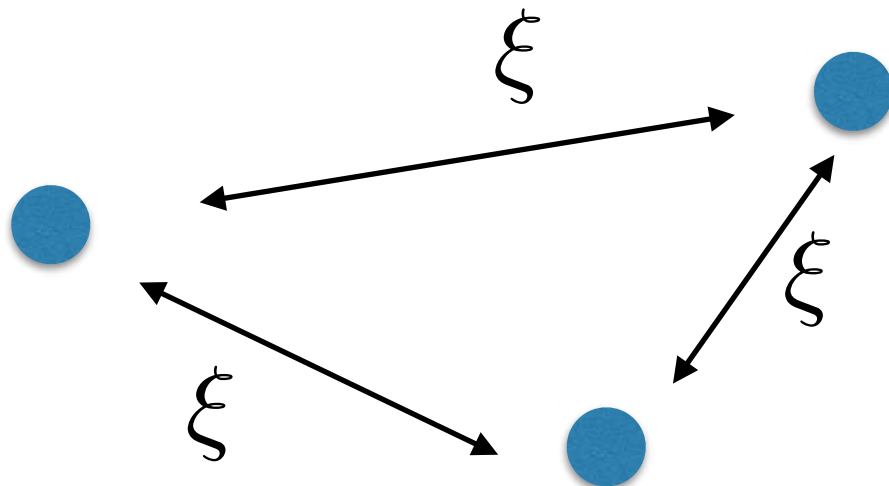




# Introduction to Cosmic Defects

DEFECTS: Aftermath of PhT  $\rightarrow$   $\left\{ \begin{array}{l} \left\{ \begin{array}{l} \text{Domain Walls} \\ \text{Cosmic Strings} \\ \text{Cosmic Monopoles} \end{array} \right. \\ \text{Non - Topological} \end{array} \right.$

CAUSALITY & MICROPHYSICS  $\Rightarrow$  Corr. Length:  $\xi(t) = \lambda(t) H^{-1}(t)$



# Introduction to Cosmic Defects

DEFECTS: Aftermath of PhT  $\rightarrow$   $\left\{ \begin{array}{l} \left\{ \begin{array}{l} \text{Domain Walls} \\ \text{Cosmic Strings} \\ \text{Cosmic Monopoles} \end{array} \right. \\ \text{Non - Topological} \end{array} \right.$

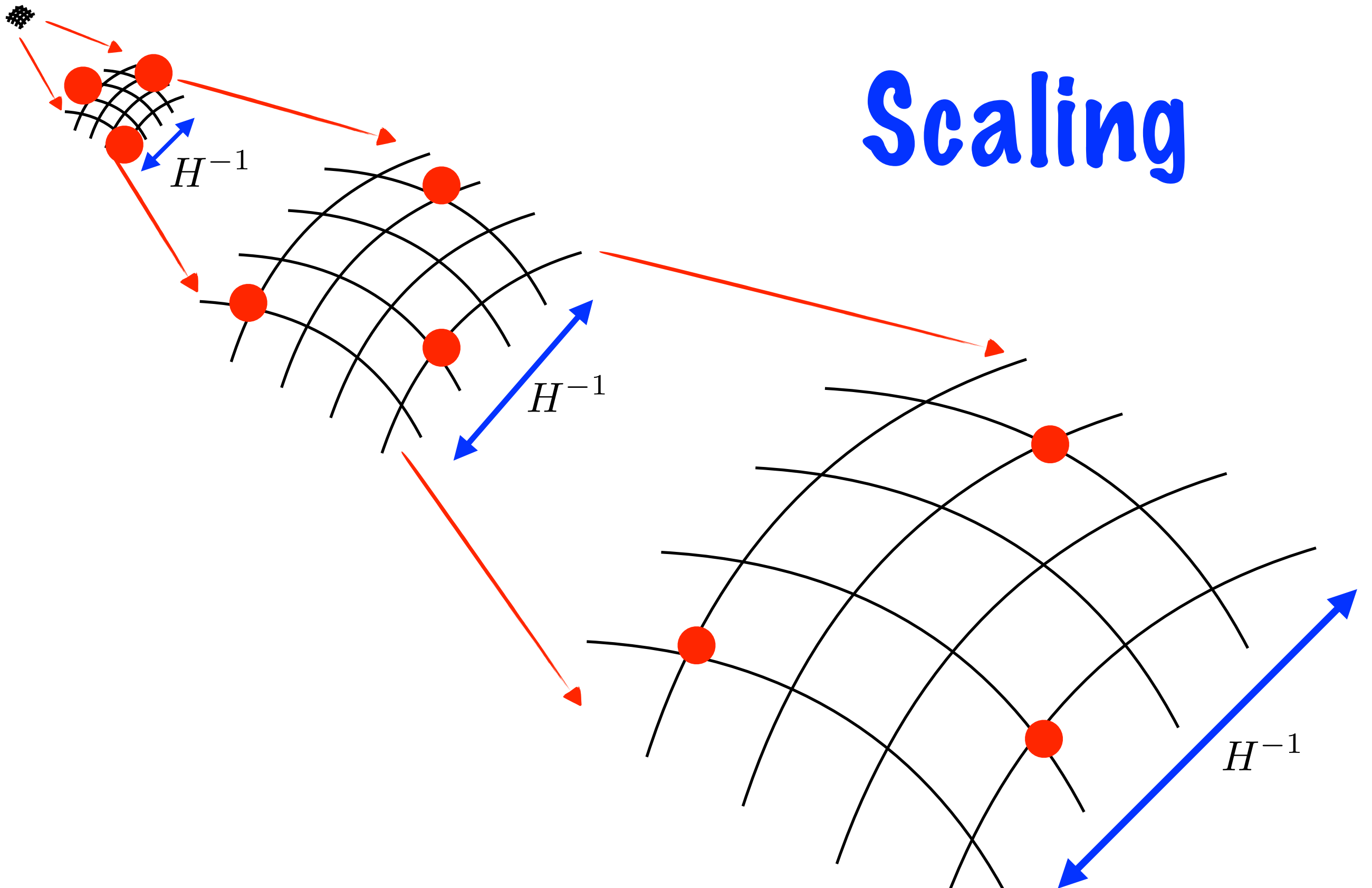
CAUSALITY & MICROPHYSICS  $\Rightarrow$  Corr. Length:  $\xi(t) = \lambda(t) H^{-1}(t)$

(Kibble' 76)

SCALING:  $\lambda(t) = \text{const.} \rightarrow \lambda \sim 1 \Rightarrow k/\mathcal{H} = kt$   
 $\swarrow \searrow$   
comoving momentum conformal time

# Cosmic Defects

Scaling



# GWs from a scaling network of cosmic defects

DEFECTS: GW Source  $\rightarrow \{T_{ij}\}^{\text{TT}} \propto \{\partial_i \phi \partial_j \phi, E_i E_j, B_i B_j\}^{\text{TT}}$

UTC:  $\langle T_{ij}^{\text{TT}}(\mathbf{k}, t) T_{ij}^{\text{TT}}(\mathbf{k}', t') \rangle = (2\pi)^3 \Pi^2(k, t_1, t_2) \delta^3(\mathbf{k} - \mathbf{k}')$

(Unequal Time Correlator)

GW spectrum:

Expansion

UTC

$$\frac{d\rho_{\text{GW}}}{d\log k}(k, t) \propto \frac{k^3}{M_p^2 a^4(t)} \int dt_1 dt_2 a(t_1) a(t_2) \cos(k(t_1 - t_2)) \Pi^2(k, t_1, t_2)$$

Comoving Conformal

# GWs from a scaling network of cosmic defects

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SCALING

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Comoving Conformal

SCALING



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Comoving Conformal

**Rad. Dom**

**SCALING**

# GWs from a scaling network of cosmic defects

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SCALING

UTC:  $\langle T_{ij}^{\text{TT}}(\mathbf{k}, t) T_{ij}^{\text{TT}}(\mathbf{k}', t') \rangle = (2\pi)^3 \frac{V^4}{\sqrt{tt'}} U(kt, kt') \delta^3(\mathbf{k} - \mathbf{k}')$

GW spectrum:

$$(x_i \equiv kt_i)$$

Expansion

UTC

$$\frac{d\rho_{\text{GW}}}{d\log k}(k, t) \propto \left(\frac{V}{M_p}\right)^4 \frac{M_p^2}{a^4(t)} \left[ \int dx_1 dx_2 \sqrt{x_1 x_2} \cos(x_1 - x_2) U(x_1, x_2) \right]$$

Rad. Dom

SCALING

# GWs from a scaling network of cosmic defects

DEFECTS: GW Source  $\rightarrow \{T_{ij}\}^{\text{TT}} \propto \{\partial_i \phi \partial_j \phi, E_i E_j, B_i B_j\}^{\text{TT}}$

SCALING

UTC:

$$\langle T_{ij}^{\text{TT}}(\mathbf{k}, t) T_{ij}^{\text{TT}}(\mathbf{k}', t') \rangle = (2\pi)^3 \frac{V^4}{\sqrt{tt'}} U(kt, kt') \delta^3(\mathbf{k} - \mathbf{k}')$$

GW spectrum:

$$(x_i \equiv kt_i)$$

Expansion

UTC

$$\frac{d\rho_{\text{GW}}}{d\log k}(k, t) \propto \left(\frac{V}{M_p}\right)^4 \frac{M_p^2}{a^4(t)} \left[ \int dx_1 dx_2 \sqrt{x_1 x_2} \cos(x_1 - x_2) U(x_1, x_2) \right]$$

Rad. Dom

SCALING

$$F_U \sim \text{Const. (Dimensionless)}$$

# GWs from a scaling network of cosmic defects

GW today:

VEV

Scaling @ RD

$$\Omega_{GW}^{(o)} \equiv \frac{1}{\rho_c^{(o)}} \left( \frac{d\rho_{GW}}{d \log k} \right)_o = \frac{32}{3} \left( \frac{V}{M_p} \right)^4 \Omega_{\text{rad}}^{(o)} F_U, \quad (\text{SCALE INV.!!})$$

Defect type

$$F_U \equiv \int_0^x dx_1 dx_2 \sqrt{x_1 x_2} \cos(x_1 - x_2) U(x_1, x_2)$$

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$$F_U \equiv \int_0^x dx_1 dx_2 \sqrt{x_1 x_2} \cos(x_1 - x_2) U(x_1, x_2)$$

$\forall$  PhT (1st, 2nd, ...),  $\forall$  Defects (top. or non-top.)



# GWs from a scaling network of cosmic defects

## Total GW Spectrum

$$h^2 \Omega_{\text{GW}}^{(\text{o})} = h^2 \Omega_{\text{rad}}^{(\text{o})} \left( \frac{V}{M_p} \right)^4 \left[ F_U^{(\text{R})} + F_U^{(\text{M})} \left( \frac{k_{\text{eq}}}{k} \right)^2 \right]$$

energy scale

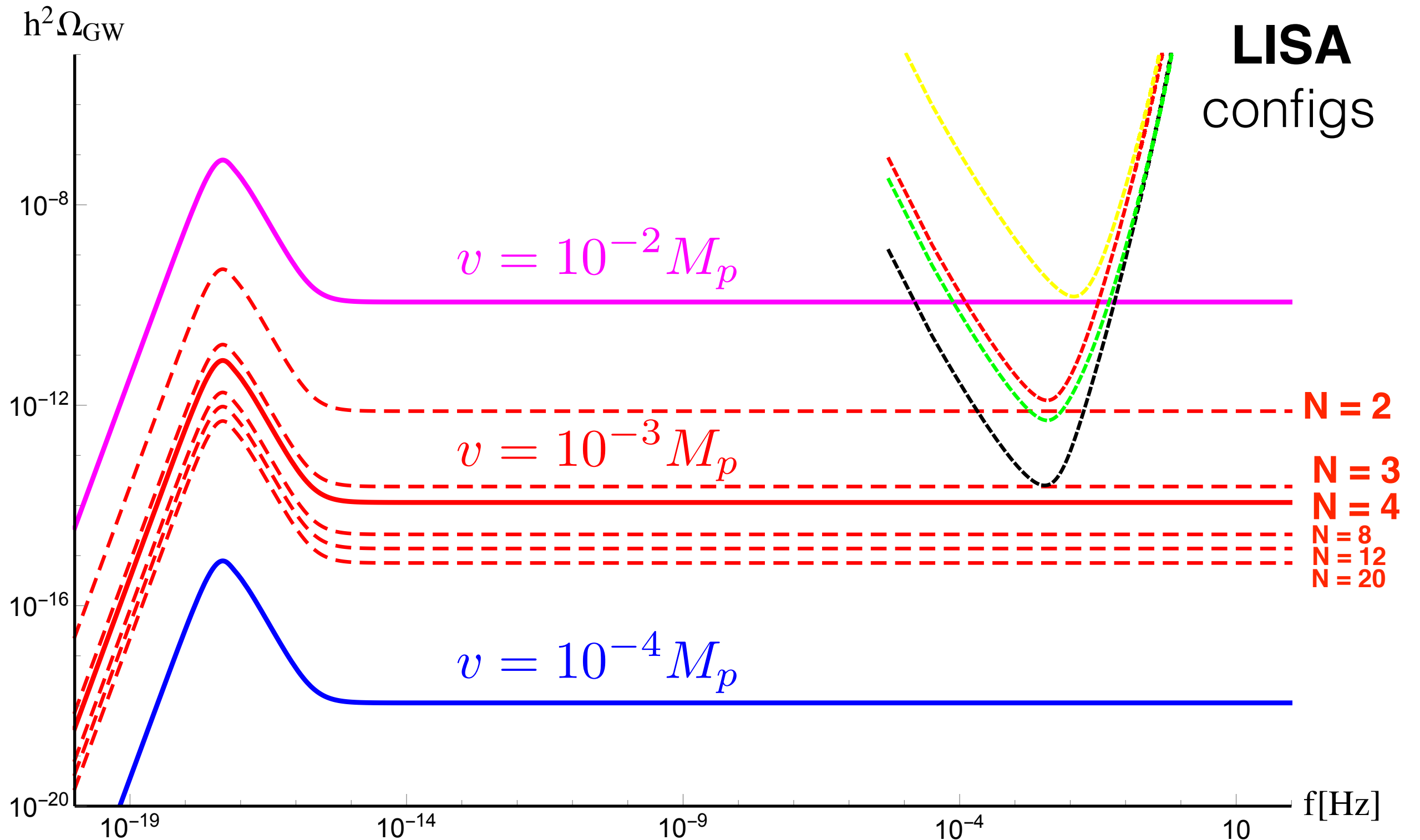
constants

**RD**  $F_U^{(\text{R})} \equiv \frac{32}{3} \int_0^x dx_1 dx_2 (x_1 x_2)^{1/2} \cos(x_1 - x_2) U_{\text{RD}}(x_1, x_2)$

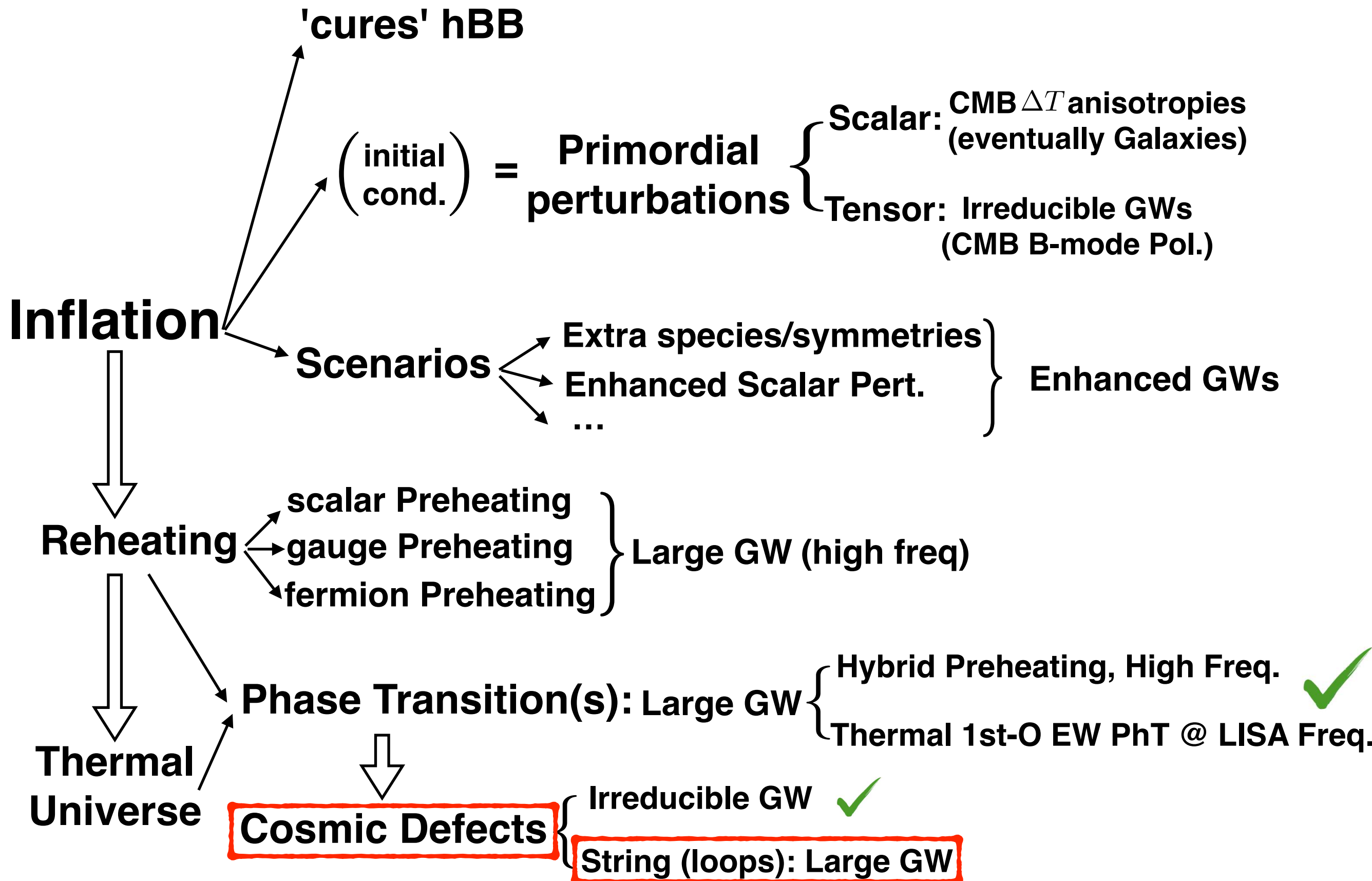
**MD**  $F_U^{(\text{M})} \equiv \frac{32}{3} \frac{(\sqrt{2} - 1)^2}{2} \int_{x_{\text{eq}}}^x dx_1 dx_2 (x_1 x_2)^{3/2} \cos(x_1 - x_2) U_{\text{MD}}(x_1, x_2)$

# More on GW from Defect Networks

$$h^2\Omega_{\text{GW}}^{(\text{o})} = h^2\Omega_{\text{rad}}^{(\text{o})} \left( \frac{V}{M_p} \right)^4 \left[ F_U^{(\text{R})} + F_U^{(\text{M})} \left( \frac{k_{\text{eq}}}{k} \right)^2 \right]$$



# EARLY UNIVERSE



# What if Defects are Cosmic Strings ?

**Extra emission of GWs !** (Vilenkin '81)

# What if Defects are Cosmic Strings ?

## Intercommutation



**Loops are formed !**



# What if Defects are Cosmic Strings ?

**Loops are formed !**

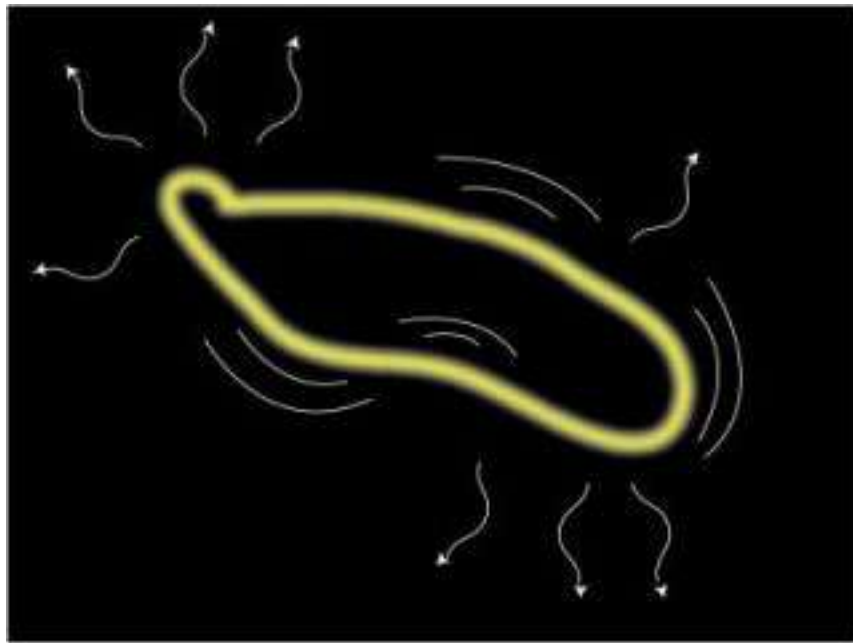


Image Credit: Google

**Gravitational Waves emitted !**  
(releasing the loops' tension)

# Cosmic Strings Network: Loop configurations

Cosmic string loop (length  $l$ ) oscillates under tension  $\mu$

➔ emits GWs in a series of harmonic modes

**Extra emission of GWs !** (Vilenkin '81)  
and many others !

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$$\frac{d\rho^{(\circ)}}{df} \equiv \Gamma G\mu^2 \int_{t_*}^{t_o} dt \left( \frac{a(t)}{a_o} \right)^3 \int_0^{\alpha/H(t)} dl l n(l, t) \mathcal{P}((a_o/a(t)) fl)$$

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expansion  
history

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expansion  
history

length      number  
density

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expansion history      length      number density      GW power emission



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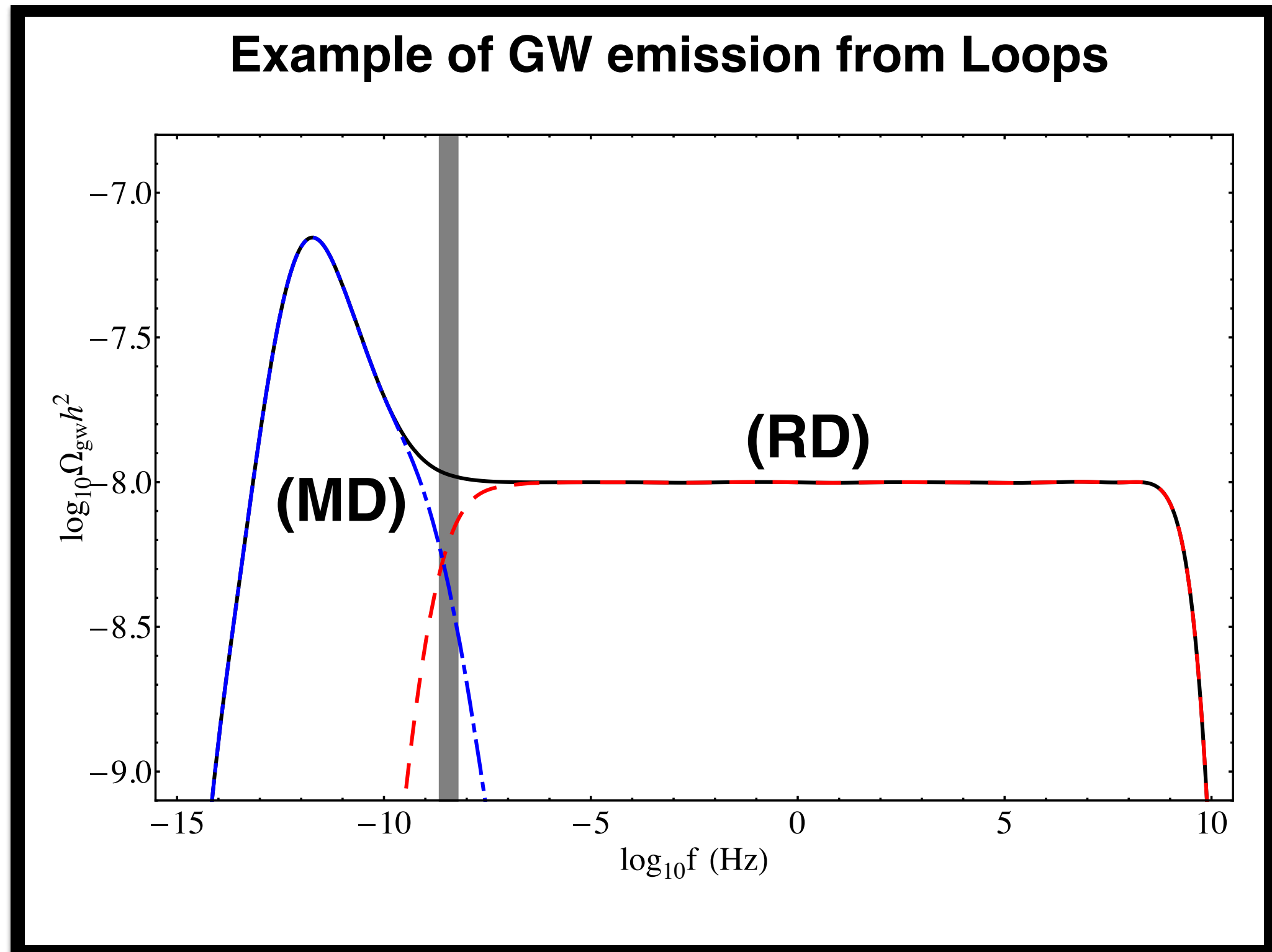
expansion history

length

number density

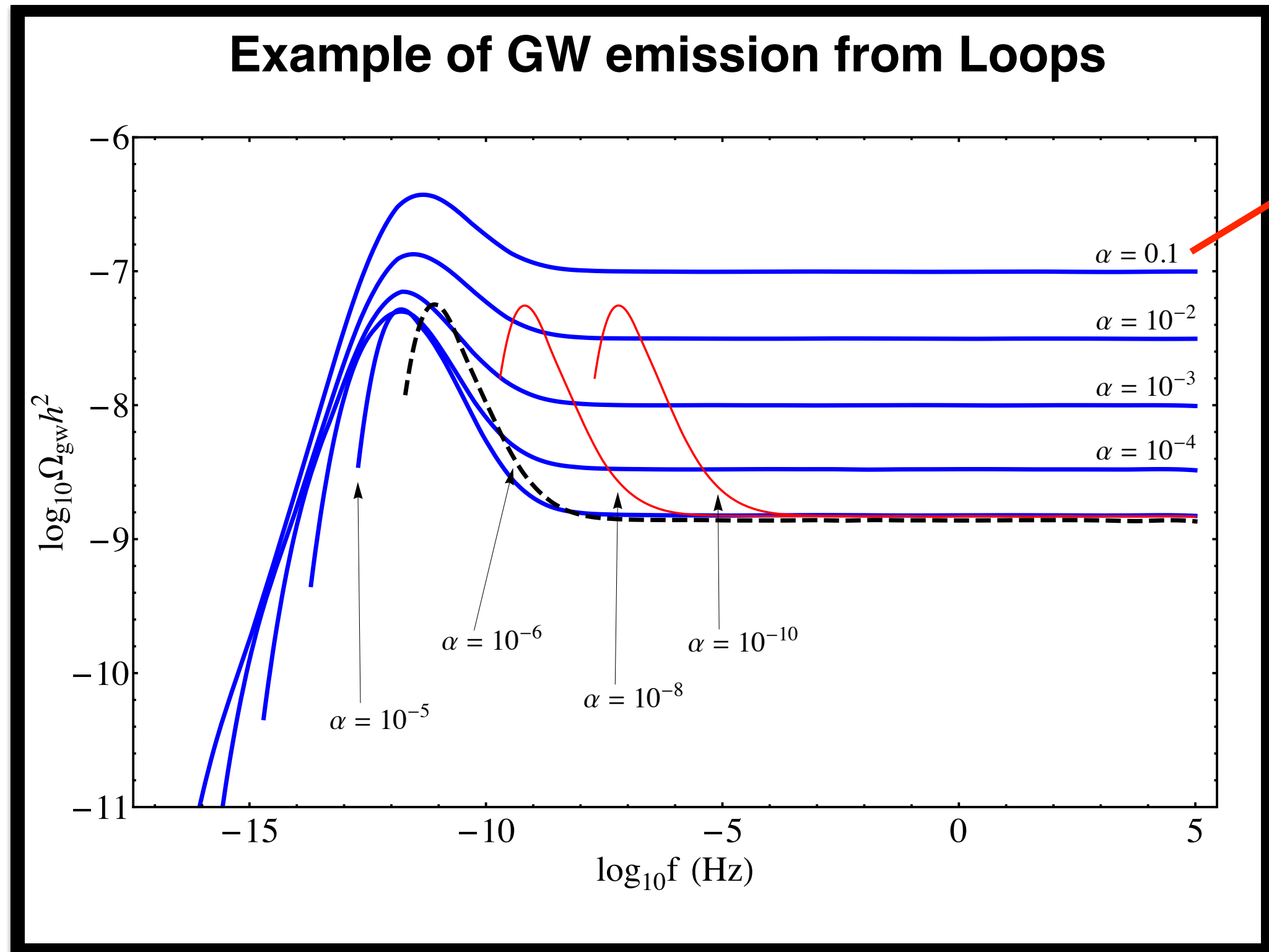
GW power emission  
 $\propto 1/(fl)^{q+1}$   
features (kinks, cusps,...)

# Cosmic strings loops: GW background



e.g. Sanidas et al 2012

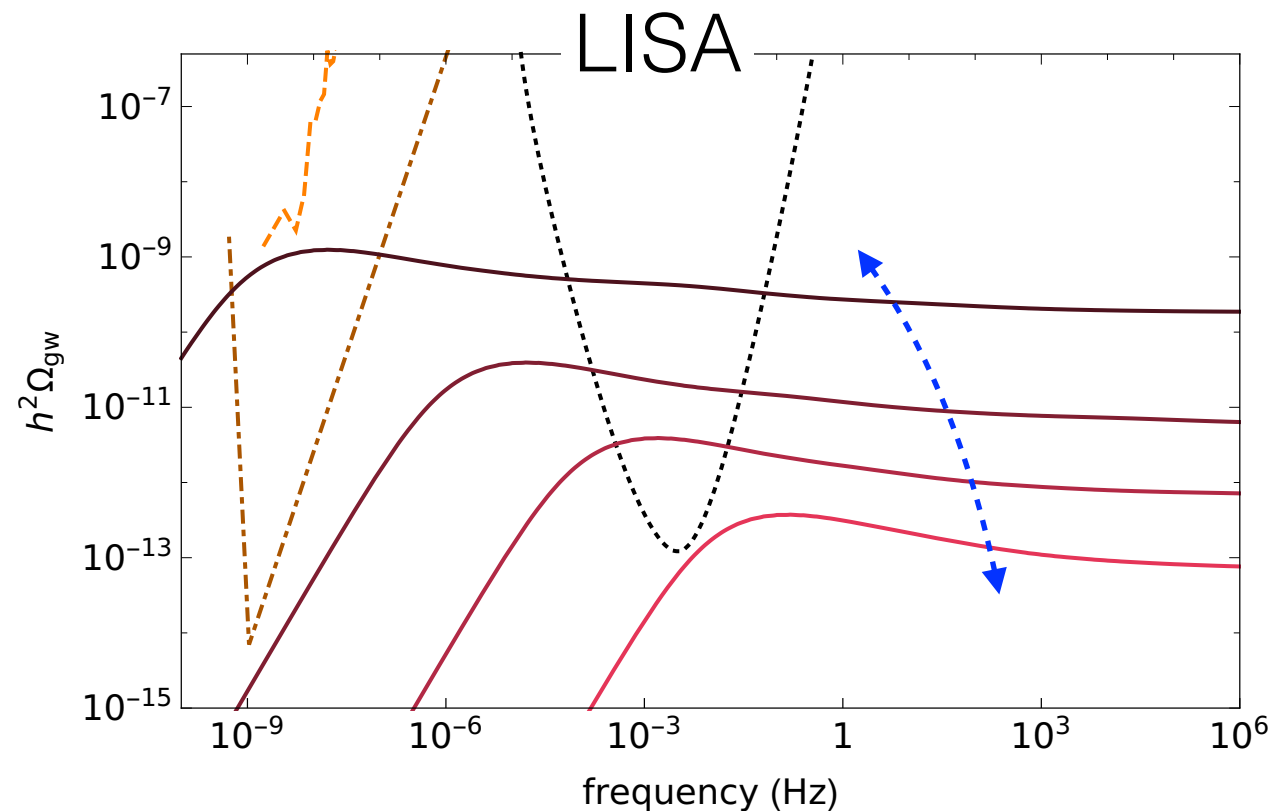
# Cosmic Strings Network: Loop configurations



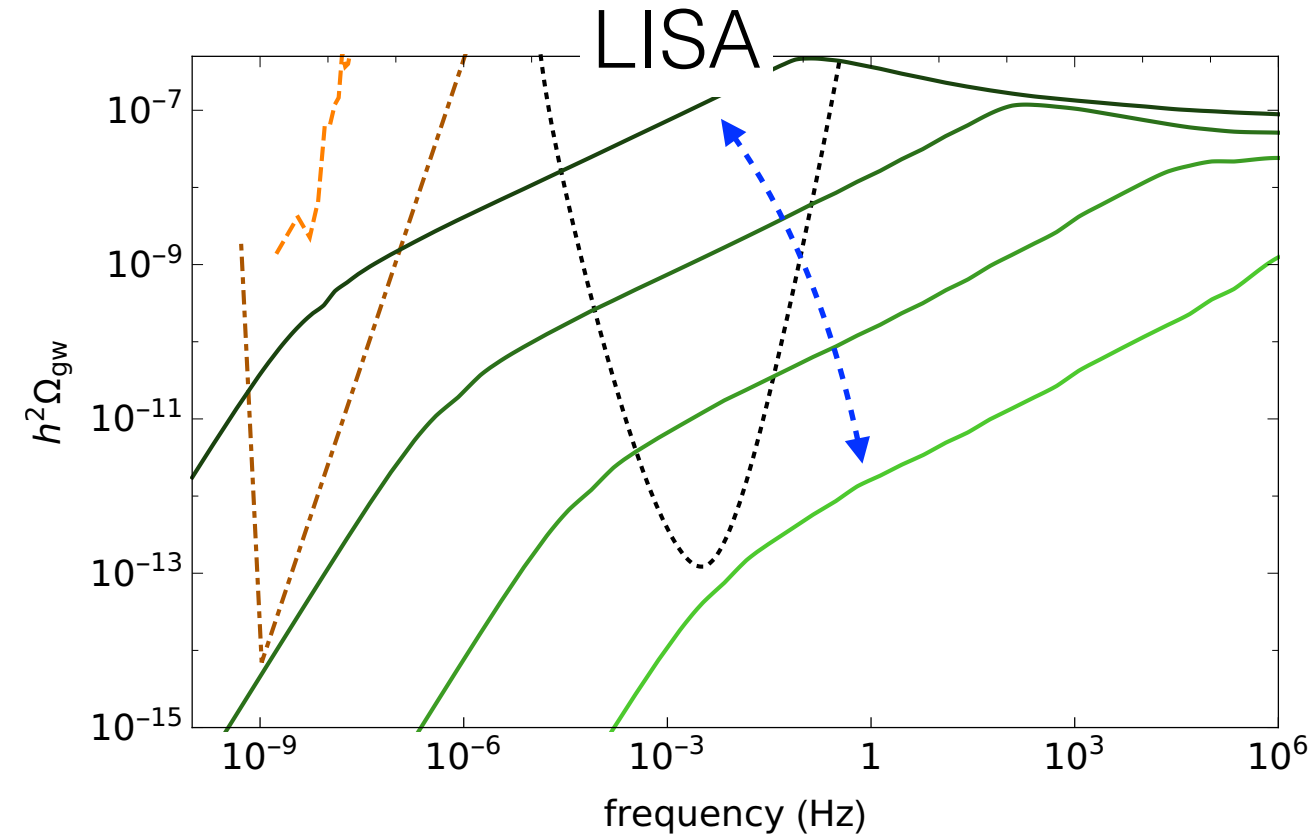
$\alpha$   
**loop size**  
(relative to horizon)

# Cosmic strings loops: GW background

Blanco-Pillado, Olum, Shlaer



Lorenz, Ringeval, Sakellariadou



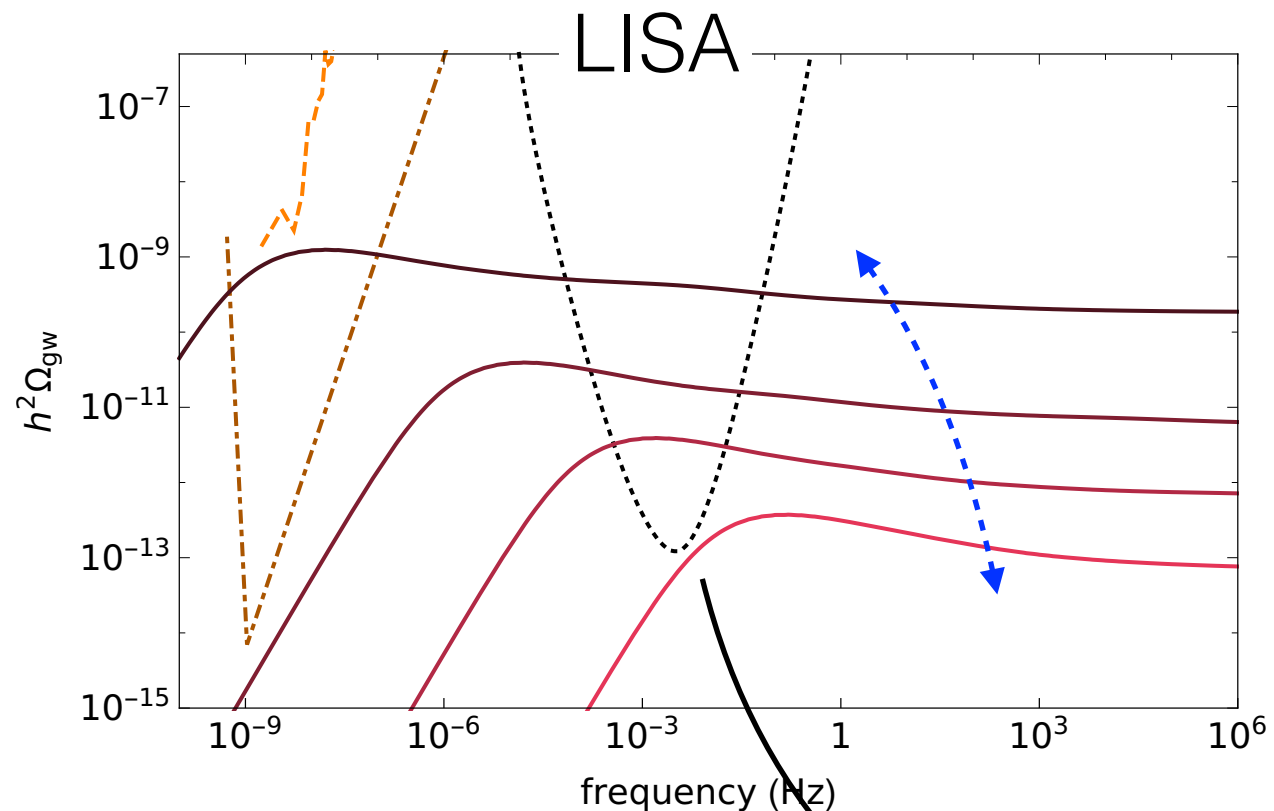
$$G\mu \sim 10^{-11} - 10^{-17}$$

**Very large parameter space !**

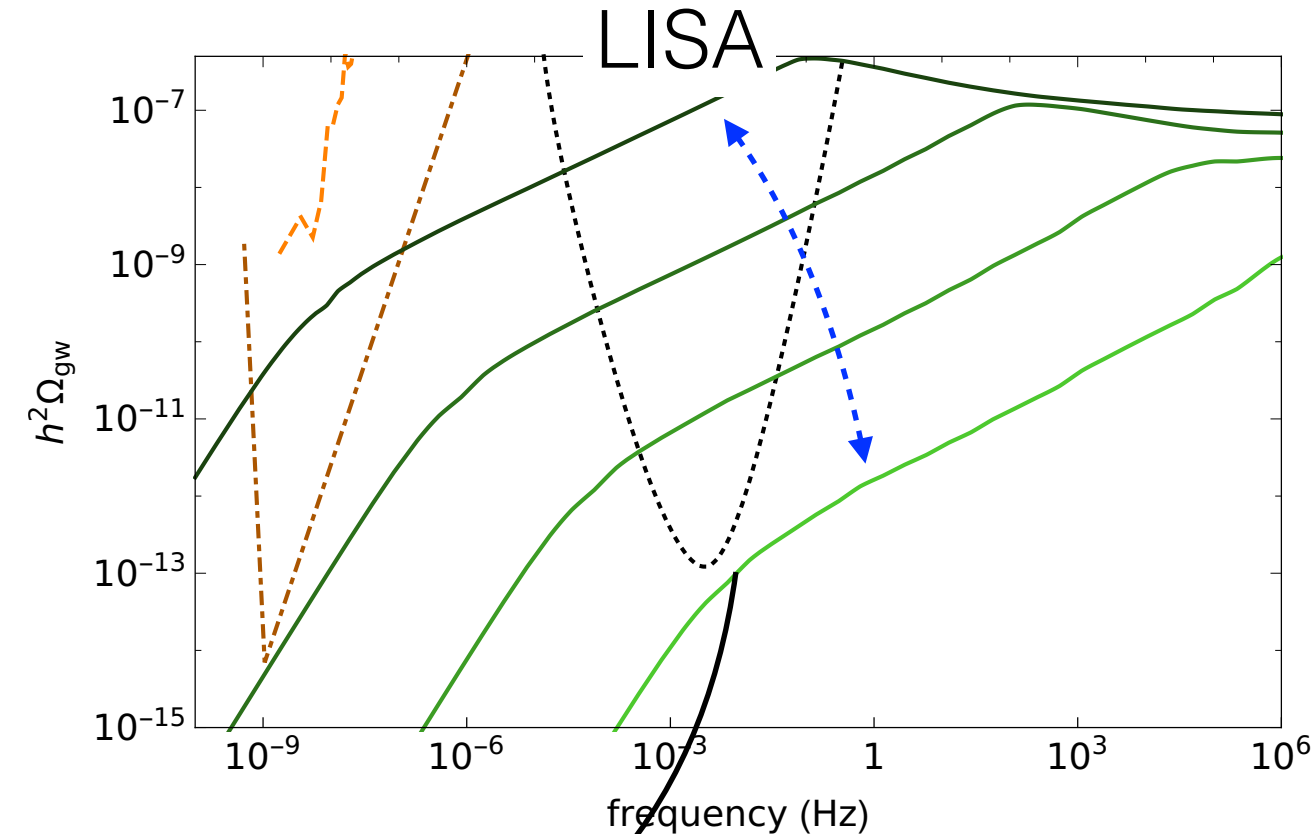
**LISA paper  
1909.00819**

# Cosmic strings loops: GW background

Blanco-Pillado, Olum, Shlaer



Lorenz, Ringeval, Sakellariadou



$$G\mu \gtrsim 10^{-17}$$

**Very large parameter space !**

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# GW background constrained by LISA

$$G\mu \gtrsim 10^{-17} \quad (v \gtrsim 10^{10} \text{ GeV})$$

CMB

PTA (today)

PTA (future)

$$G\mu \sim 10^{-7}$$

$$G\mu \sim 10^{-11}$$

$$G\mu \sim 10^{-14}$$

LISA improve:

$$\mathcal{O}(10^{10})$$

$$\mathcal{O}(10^6)$$

$$\mathcal{O}(10^3)$$

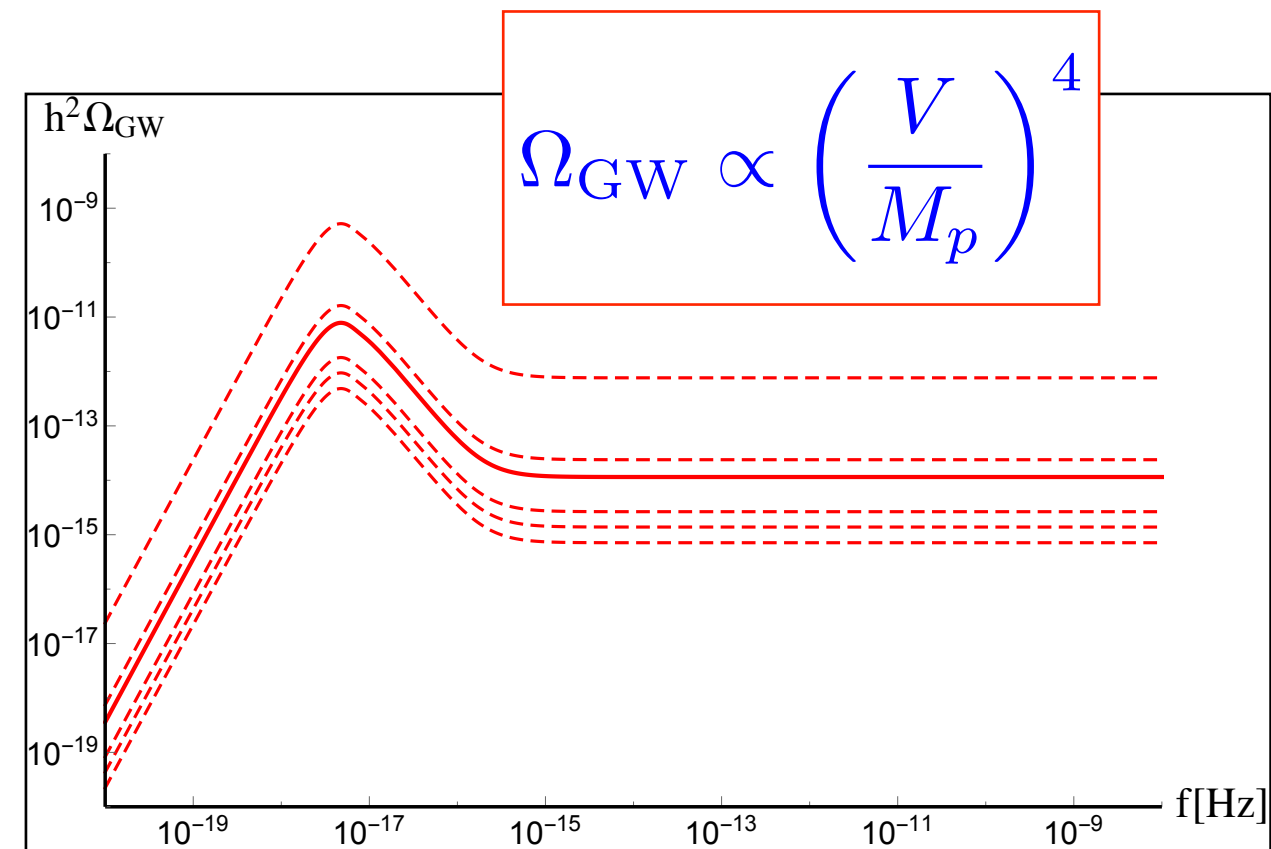
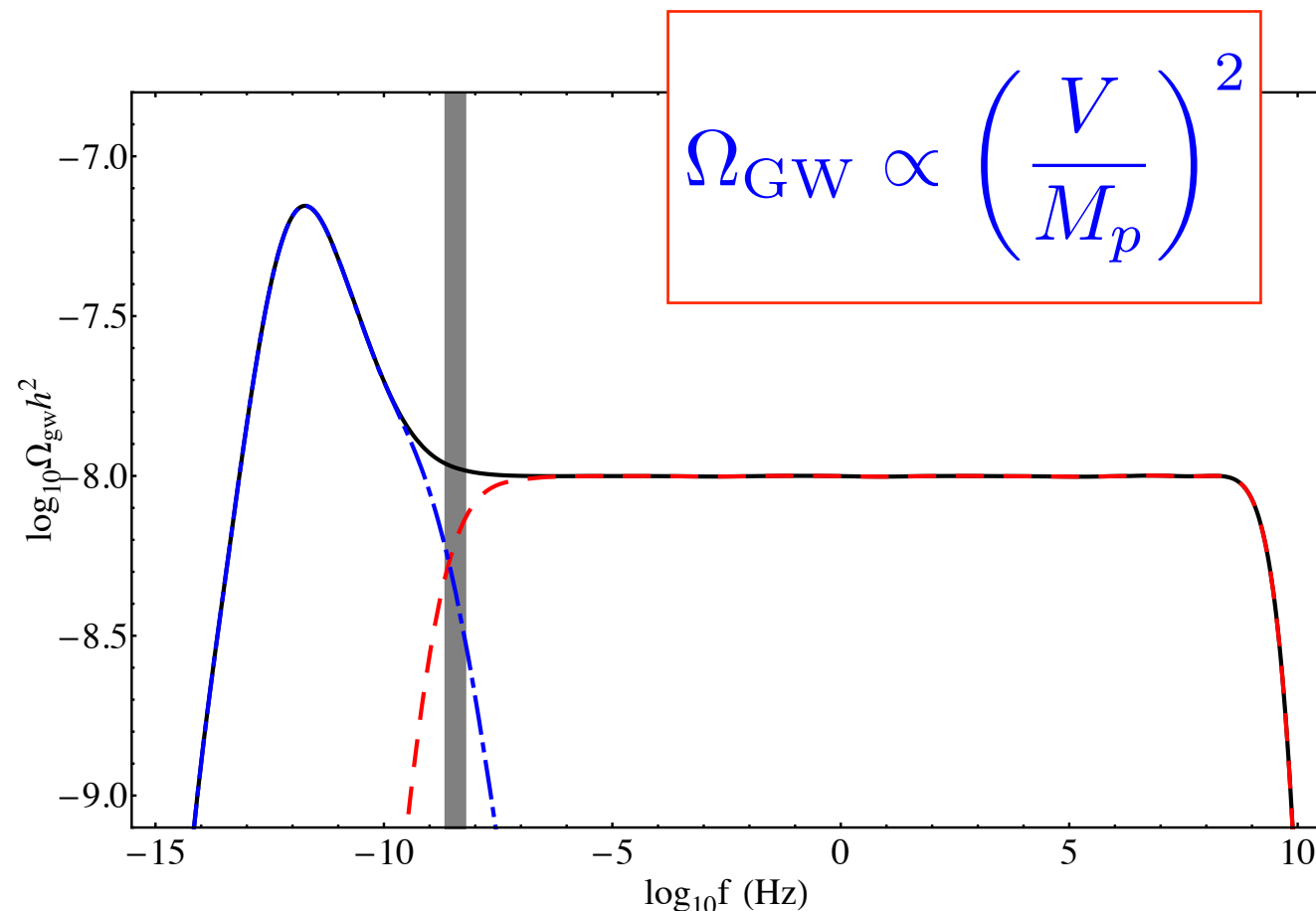
**LISA** {  
\* **Best constraints on Cosmic Strings**  
\* **(actually only way to obtain them)**  
\* **Discovery, or stringent constraints**

**LISA paper**  
**1909.00819**



# Cosmic Strings Network: Loop configurations

GW from string loops  $\neq$  GW from "Infinite"-Strings  
(particular emission) (irreducible emission)



*Vilenkin, Vachaspati, Bouchet, Siemens et al,  
Sanidas et al, Blanco-Pillado et al, ... 1981 - 2020*

*DGF, Hindmarsh, Lizarraga, Urrestilla,  
work in progress 2013-2020*

# OUTLINE

1st lecture

1) GWs Definition

2nd lecture

2) GWs from Inflation

3) GWs from Preheating

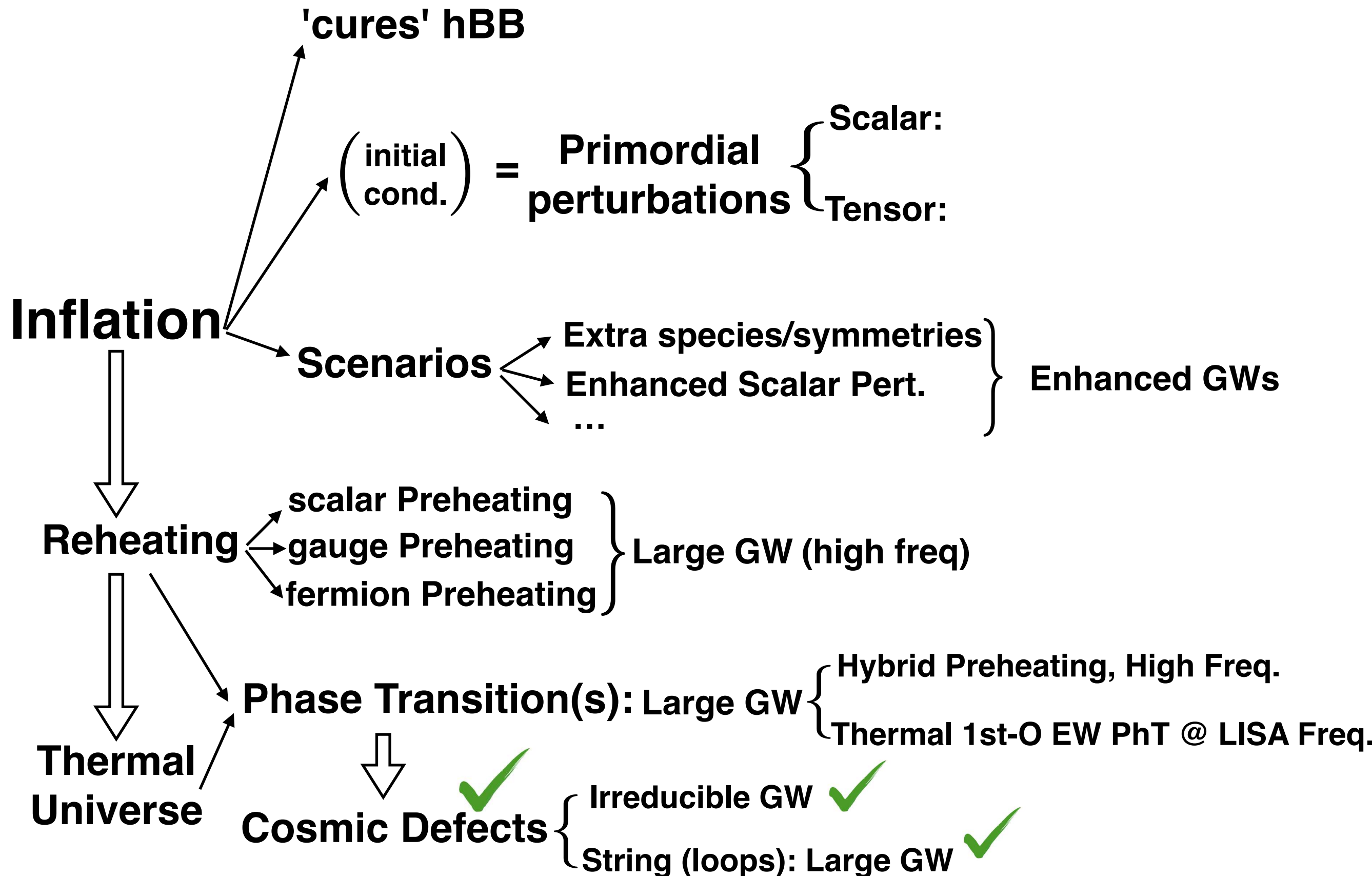
4) GWs from Phase Transitions

5) GWs from Cosmic Defects

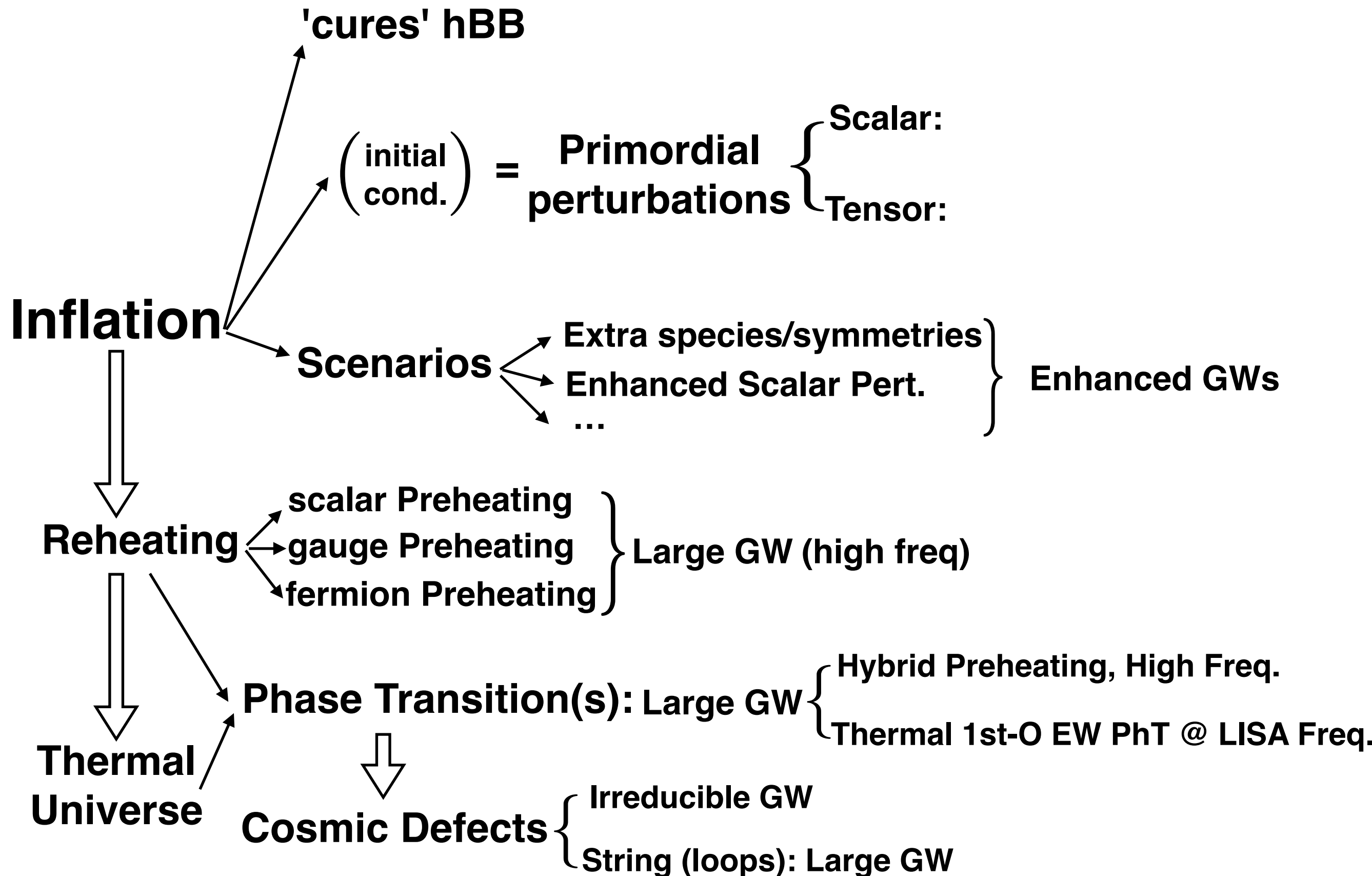
3rd lecture



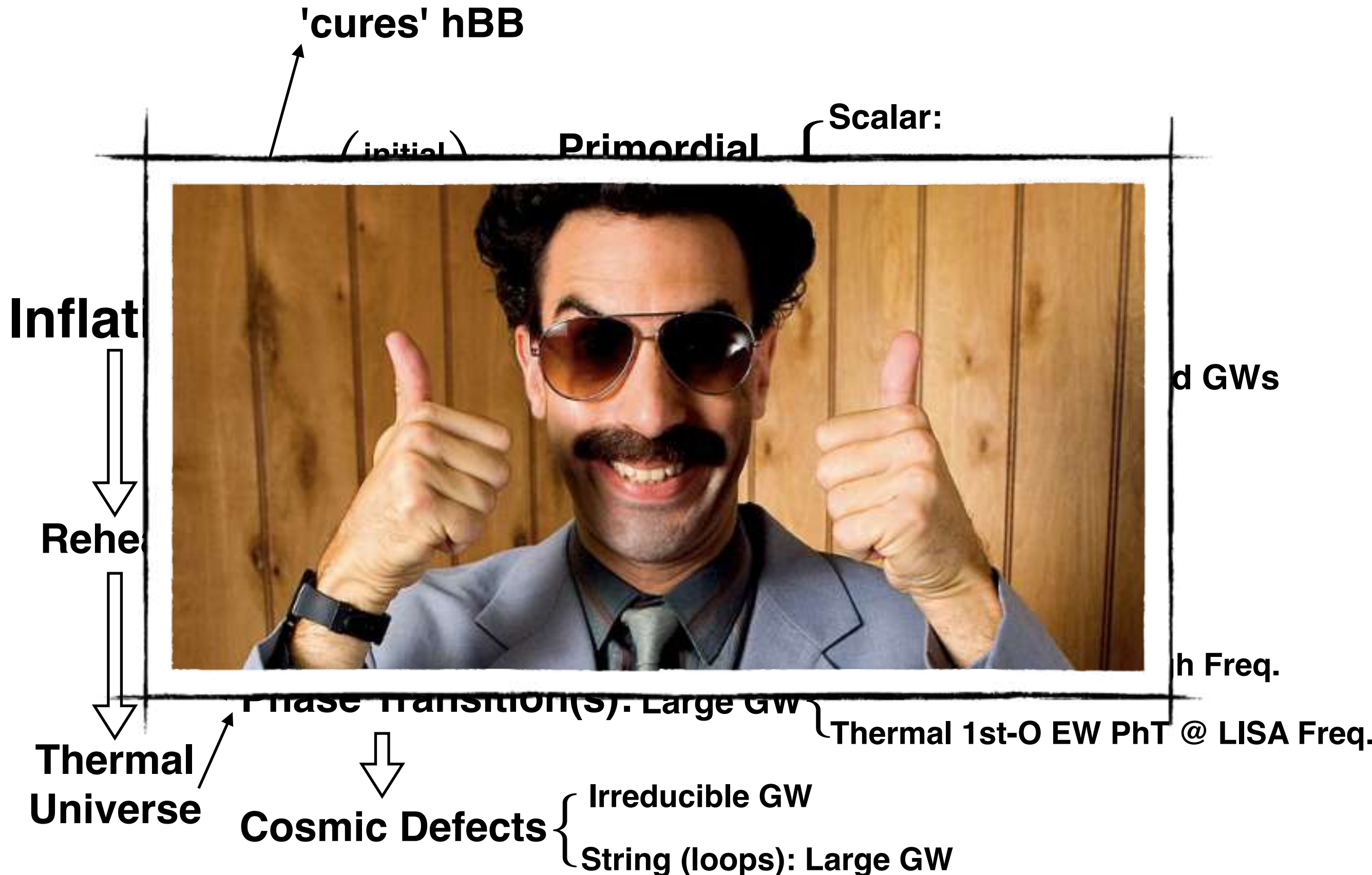
# EARLY UNIVERSE in GWs



# EARLY UNIVERSE in GWs



# EARLY UNIVERSE in GWs



# COSMOLOGICAL GRAVITATIONAL WAVES

## OUTLINE (~ 4.5 h)

1) GWs definition

1st lecture (~ 1.5 h)

2) GWs from Inflation

3) GWs from Preheating

4) GWs from Phase Transitions

5) GWs from Cosmic Defects

2nd lecture  
(~ 1.5 h)

3rd lecture  
(~ 1.5 h)

Early  
Universe



# COSMOLOGICAL GRAVITATIONAL WAVES

## OUTLINE (~ 4.5 h)

**Early  
Universe**

**1) GWs definition**

**2) GWs from Inflation**

Intensive search  
at the CMB.  
Extra ingredients  
= enhance GW

**3) GWs from Preheating**

High amplitude,  
unlike detection

**4) GWs from Phase Transitions**

**5) GWs from Cosmic Defects**

# COSMOLOGICAL GRAVITATIONAL WAVES

## OUTLINE (~ 4.5 h)

**Early  
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High amplitude,  
unlike detection

**4) GWs from Phase Transitions**

EWPT (1st)  
observable\*

**5) GWs from Cosmic Defects**

GUT-PT  
observable\*\*

[\*At LISA if EWPT is strong 1st order]

[\*\*By PTA, If large loops present]

**To know more ...**

**Review on Cosmological  
Gravitational Wave Backgrounds**

**Caprini & Figueroa**  
**arXiv:1801.04268**

**Obrigado pela  
sua atenção !**

**Gracias por  
vuestra atención !**

# **COSMOLOGICAL GW CLASSIFICATION**

# INFLATION

- \* Wide Freq. Range
- \* Small Amplitude naturally
- \* Blue-tilted  $\longleftrightarrow$  Special Physics

# PREHEATING

- Narrow Freq. Range \*
- Large amplitude @ High Freq \*
- Very Model Dependent \*

## High Frequency Gravitational Waves

$$f \sim \frac{1}{\epsilon_*} 10^{-8} (E_*/\text{GeV}) \text{ Hz}$$

$$f \sim \frac{1}{\epsilon_*} 10^{-8} (E_*/\text{GeV}) \text{ Hz}$$

- \* Narrow Freq. Range (~peak)
- \* Large amplitude IF 1stO PhT
- \* EWPhT @ LISA / GUT-PhT GHz

- Large Freq. Range \*
- Large amplitude naturally \*
- Very Model Dependent \*

# PHASE TRANSITIONS

# TOPOLOGICAL DEFECTS