#### GRAVITATIONAL WAVES: FROM DETECTION TO NEW PHYSICS SEARCHES

Masha Baryakhtar New York University

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#### Superradiance and Black Holes

or

## How to Extract Energy from Black Holes and Discover New Particles

- Superradiance and rotating BHs
- Gravitational Atoms
- Signs of New Particles
  - Black Hole Spindown
  - Gravitational Wave Signals

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- Rotational, or Zeldovich, superradiance: extraction of an object's rotational energy by an incident wave in the presence of dissipation
- Rotating (Kerr) black holes can superradiance and lose energy and angular momentum

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- Ultralight fields can form macroscopic gravitationally bound states with astophysical black holes, or ``gravitational atoms''
- Bosonic fields can form states with exponentially large occupation values which grow spontaneously through superradiance

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- If there is a light axion (scalar/ vector) with compton wavelength comparable to astrophysical BH sizes, it will cause astrophysical black holes to spin down
- The resulting bound states of light particles will source gravitational wave radiation that is observable by LIGO

#### Motivation

- Ultralight scalar particles often found in theories beyond the Standard Model
- E.g. the QCD axion solves the `strong-CP' problem
- As already discussed, ultralight scalars can make up the DM



#### Astrophysical Black Holes and Ultralight Particles

- Black holes in our universe provide nature's laboratories to search for light particles
- Set a typical length scale, and are a huge source of energy
- Sensitive to QCD axions with GUTto Planck-scale decay constants  $f_a$



for a 10<sup>-12</sup> eV particle:





- A an object scattering off a **rotating** cylinder can increase in angular momentum and energy.
- Effect depends on dissipation, necessary to change the velocity



#### Ball incident on cylinder with lossy surface slows down due to friction

- A an object scattering off a **rotating** cylinder can increase in angular momentum and energy.
- Effect depends on dissipation, necessary to change the velocity



If the cylinder is rotating at angular velocity equal to the angular velocity of the ball about the axis,  $\Omega_i = v_{\phi,i}$  the relative velocity at the point of contact is zero: no energy loss

- A an object scattering off a **rotating** cylinder can increase in angular momentum and energy.
- Effect depends on dissipation, necessary to change the velocity



- If the cylinder is rotating even faster,  $\Omega_i > v_{\phi,i}$
- Ball scattering off rapidly rotating cylinder with lossy surface speeds up!
- Energy increase comes from cylinder slowing down, losing energy and angular momentum

• Scalar perturbations scattering off of rotating cylindrical medium with absorption



superradiance condition

- A wave scattering off a rotating object can increase in amplitude by extracting angular momentum and energy.
- Growth proportional to probability of absorption when rotating object is at rest: dissipation necessary to increase wave amplitude



#### Superradiance condition:

Angular velocity of wave slower than angular velocity of BH horizon,

 $\Omega_a < \Omega_{BH}$ 

Zel'dovich; Starobinskii; Misner

Gravitational wave amplified when scattering from a rapidly rotating black hole



Angular velocity of wave slower than angular velocity of BH horizon,

 $\Omega_a < \Omega_{BH}$ 

What is the `angular velocity' of the BH horizon?

$$ds^2 = -\left(1 - \frac{2r_g r}{\Sigma}\right)dt^2 + \frac{\Sigma}{\Delta}dr^2 + \Sigma d\theta^2 + \left(r^2 + a^2 + \frac{2r_g ra^2}{\Sigma}\sin^2\theta\right)\sin^2\theta d\phi^2 - \frac{4r_g ra}{\Sigma}\sin^2\theta dt d\phi$$

$$r_g \equiv GM, \quad a \equiv \frac{J}{M} \equiv a_* r_g, \quad \Sigma = r^2 + a^2 \cos^2 \theta, \quad \Delta = r^2 - 2r_g r + a^2$$



Symmetry axis  $\theta = 0, \pi$ 

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$$r_g \equiv GM$$
,  $a \equiv \frac{J}{M} \equiv a_* r_g$ ,  $\Sigma = r^2 + a^2 \cos^2 \theta$ ,  $\Delta = r^2 - 2r_g r + a^2$ 

Horizon: coordinate singularity: the purely radial component  $g_{rr}$  of the metric goes to infinity.







Angular velocity of wave slower than angular velocity of BH horizon,

 $\Omega_a < \Omega_{BH}$ 

#### What is the `angular velocity' of the BH horizon?

`Blackboard'

Angular velocity of wave slower than angular velocity of BH horizon,

 $\Omega_a < \Omega_{BH}$ 

For a scalar field mode with energy  $\omega$  and angular momentum m ,

$$\Phi = \phi(r)e^{-i\omega t + im\varphi}$$

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For a scalar field mode with energy  $\omega$  and angular momentum m ,

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And a Kerr black hole,

$$\frac{\omega}{m} < \frac{1}{2r_g} \frac{a_*}{1 + \sqrt{1 - a_*^2}}$$

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For a nonrelativistic field with mass  $\mu$  and angular momentum m, the SR condition is

$$\frac{\mu r_g}{m} < \frac{1}{2} \frac{a_*}{1 + \sqrt{1 - a_*^2}} < \frac{1}{2}$$

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- Bosonic fields can form states with exponentially large occupation values which grow spontaneously through superradiance

Particles/waves trapped in orbit around the BH repeat this process continuously

Press & Teulkosky "Black hole bomb" exponential instability when surround BH by a mirror Kinematic, not resonant condition Superradiance condition:

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"Black hole bomb": exponential instability when surround BH by a mirror

Kinematic, not resonant condition



Angular velocity of wave slower than angular velocity of BH horizon,

 $\Omega_a < \Omega_{BH}$ 

 $\mu_a^{-1}$ 

- Particles/waves trapped near the BH repeat this process continuously
- For a massive particle, e.g. axion, gravitational potential barrier provides trapping

 $V(r) = -\frac{G_{\rm N}M_{\rm BH}\mu_a}{r}$ 

 For high superradiance rates, compton wavelength should be comparable to black hole radius:

$$r_g \lesssim \mu_a^{-1} {\sim} 3\,\mathrm{km}\,\frac{6{\times}10^{-11}\mathrm{eV}}{\mu_a}$$

[Zouros & Eardley'79; Damour et al '76; Detweiler'80; Gaina et al '78] [Arvanitaki, Dimopoulos, Dubovsky, Kaloper, March-Russell 2009; Arvanitaki, Dubovsky 2010]

 $\overline{r_g}$ 

#### Gravitational Atoms?



#### Gravitational Atoms?



#### Gravitational Atoms



Gravitational potential similar to hydrogen atom

`Fine structure constant`

 $\alpha \equiv G_{\rm N} M_{\rm BH} \mu_a \equiv r_g \mu_a$ 

Constraint on  $\alpha$  from SR condition:

$$\frac{\alpha}{m} < \frac{1}{2} \frac{a_*}{1 + \sqrt{1 - a_*^2}} < \frac{1}{2}$$

#### Gravitational Atoms



Gravitational potential similar to hydrogen atom

`Fine structure constant`RadiusOccupation number $\alpha \equiv G_{\rm N} M_{\rm BH} \mu_a \equiv r_g \mu_a$  $r_c \simeq \frac{n^2}{\alpha \mu_a} \sim 4 - 400 r_g$  $N \sim 10^{75} - 10^{80}$ 

#### Gravitational Atoms



Gravitational potential similar to hydrogen atom

`Fine structure constant`

Radius

Occupation number

$$\alpha \equiv G_{\rm N} M_{\rm BH} \mu_a \equiv r_g \mu_a$$
  $r_c \simeq \frac{n^2}{\alpha \mu_a} \sim 4 - 400 r_g$   $N \sim 10^{75} - 10^{80}$ 

Boundary conditions at horizon give imaginary frequency: **exponential growth for rapidly rotating black holes** 

$$E \simeq \mu \left( 1 - \frac{\alpha^2}{2n^2} \right) + i\Gamma_{\rm sr}$$
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#### Superradiance Timescales

$$\alpha = G_{\rm N} M_{\rm BH} \mu_a = r_g \mu_a \lesssim \frac{m}{2} a_*$$



#### Superradiance Timescales





Flux into horizon:  $\Gamma_{\mathrm{sr}}^{\mathrm{scalar}} \sim \int_{r=r_q} \psi^* \psi \cdot dA$ 

#### Superradiance: a stellar black hole history

A black hole is born with spin  $a^* = 0.95$ , M = 40 M $_{\odot}$ .



#### Superradiance: a stellar black hole history

BH spins down and fastest-growing level is formed Cloud radius Once BH angular velocity matches that of the level, growth stops  $_{6 \text{ msec}}$  (2000 km)



#### Superradiance: a stellar black hole history

Cloud can carry up to a few percent of the black hole mass: huge energy density



~10<sup>78</sup> particles

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## Black Hole Spins

Five currently measured black holes combine to set limit:

$$2 \times 10^{-11} > \mu_a > 6 \times 10^{-13} \text{ eV}$$



#### Many BH-BH mergers detected



Each detection comes with a measurement of the initial black hole masses, and, to a lesser extent, spins

Updated 2020-05-16 LIGO-Virge | Frank Elavsky, Aaron Geller | Northwestern

#### Black Hole Spins at LIGO

9-240 BBHs/Gpc<sup>3</sup>/yr.: 1000s of BHs merging in low-redshift universe



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#### Black Hole Spins at LIGO

If light axion exists, many initial BHs would have low spin due to superradiance, limited by age and radius of binary system



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# Gravitational Wave Signals Transitions between levels Annihilations to gravitons

 Signals coherent, monochromatic, last hours to millions of years



#### Superradiance: a stellar black hole histor $\mathcal{F}_{\ell}$

- BH spins down: next level formed; annihilations to GWs deplete first level
- Next level has a superradiance rate exceeding age of BH





 $\ell = 2$ 

• Gravitational wave strain emitted from a time-varying energy density

$$h_{ij} = \frac{2G}{r} \frac{d^2 I_{ij}}{dt^2}, \quad I_{ij} = \int T_{00} x^i x^j d^3 x$$

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$$\phi = \frac{1}{\sqrt{2\mu}} \sum_{i} \sqrt{N_i} \left( \psi^i e^{-i\omega t} + \psi^{i*} e^{i\omega t} \right)$$

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• With stress-energy components of the form

$$T_{\mu\nu} \supset \mu^2 \phi^2 + \dots = \frac{1}{2\mu} \sum_{i,j} \sqrt{N_i N_j} \left( \underbrace{\psi^i \psi^j e^{-i(\omega_i + \omega_j)t}}_{\text{`annihilations'}} + \underbrace{\psi^i \psi^{j*} e^{-(\omega_i - \omega_j)t}}_{\text{`transitions'}} + \text{h.c.} \right) + \dots,$$

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#### Blackboard estimate for annihilations

#### Superradiance Timescales





Gravitational Wave Power:  $P_{GW} \sim G_N \omega^2 \overline{T}_{ij}(\omega, k) \overline{T}_{ij}^*(\omega, k)$ 



Time-varying energy density sources gravitational waves: two bosons annihilating into gravitational waves

- coherent and monochromatic:
- fit into searches for long, continuous, monochromatic gravitational waves ("mountains" on neutron stars)





- Weak, long signals last for ~ thousand- billion years, visible from our galaxy
  - Event rates up to 10,000 can be observed and studied in detail Arvanitaki, MB, Huang (2015)

Arvanitaki, **MB**, Dimopoulos, Dubovsky, Lasenby (2017) Brito et al (2017)





- Weak, long signals last for ~ thousand- billion years, visible from our galaxy
  - Event rates up to 10,000 can be observed and studied in detail
- Loud, short signals last for ~ days months, observable from BBH or NS-NS merger events
  - Event rates <1/year at design aLIGO sensitivity, up to 100's at future observatories
     Arvanitaki, MB, Dimopoulos, Dubovsky, Lasenby (2017) Isi, Sun, Brito, Melatos (2019)



time

#### Gravitational Wave Searches

- Current searches for gravitational waves from asymmetric rotating neutron stars ongoing
- Targeted as well as all-sky searches, reaching to very weak signals with large computational efforts



#### All-SkyOI Upper Limits

Abbott et al PRD 96, 122004 (2017)





Cambridge University Lucky Imaging Group



- Weak, long signals last for ~ million years, visible from our galaxy
- Very sensitive to number of rapidly rotating black holes
- Weak dependence on mass distribution except at low axion masses
- Up to 1000 signals above sensitivity threshold of Advanced LIGO searches today
- See also papers by Brito et al on stochastic searches for these signals when many signals are present

#### New Physics with Gravitational Waves

- If ultralight axions (bosons) exist, black holes spin down.
- Measurement of high spin black holes places exclusion limits; LIGO will provide more data points
- Axion clouds produce monochromatic wave radiation; we are looking for these signals in LIGO data



#### GRAVITATIONAL WAVES: FROM DETECTION TO NEW PHYSICS SEARCHES

- Detection at LIGO and physics of LIGO
- Pulsar timing for GWs and ultralight scalar DM
- Axion clouds around black holes and GWs

Potentially new discoveries await!