

Challenges to Quantum Gravity in the Laboratory

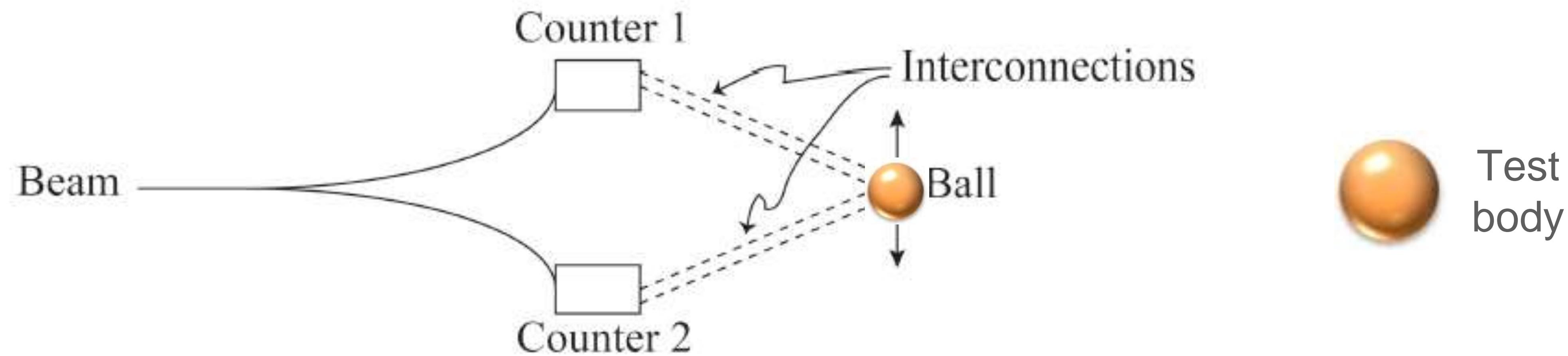
Towards Robust Interference with Massive Particles

Martin B Plenio

**Institute of Theoretical Physics
&
Center for Quantum-BioSciences
Ulm University**

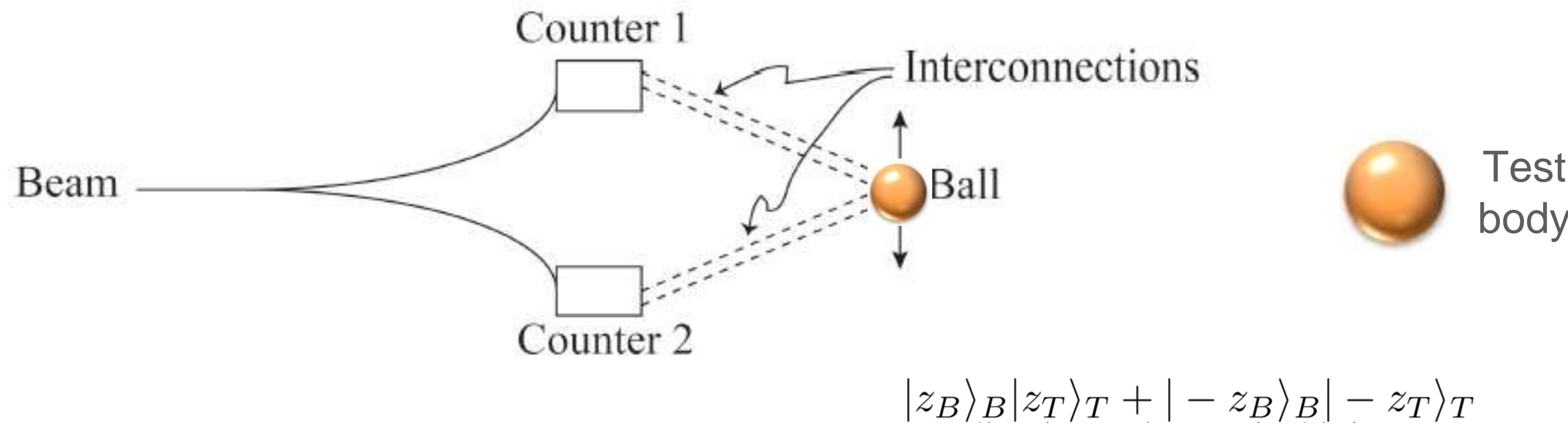
Challenges to Quantum Gravity in the Laboratory

Feynman's Thought Experiment



Challenges to Quantum Gravity in the Laboratory

Feynman's Thought Experiment



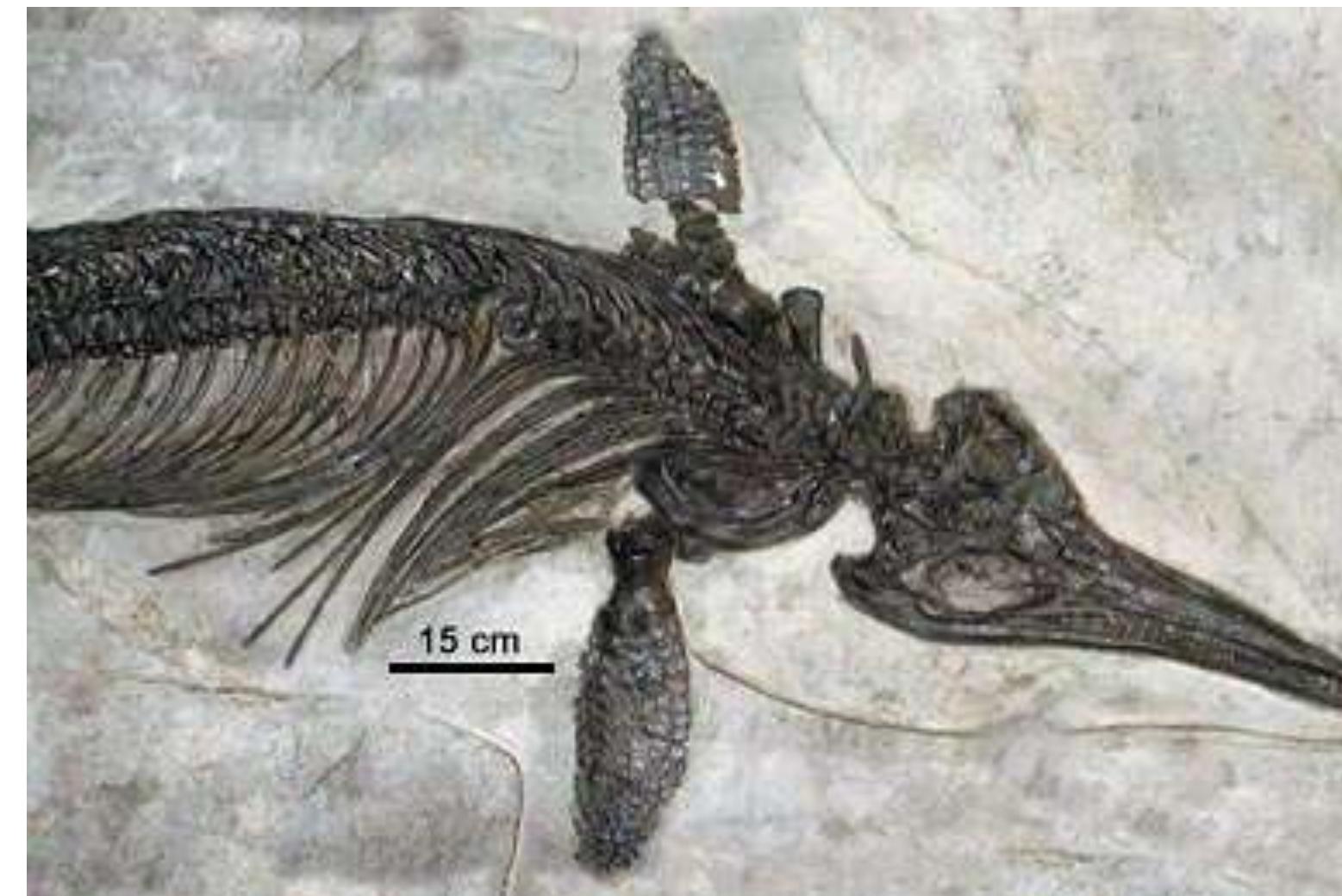
But, gravitational interaction yield tiny displacements,
so the experiment is really really hard.

Challenges to Quantum Gravity in the Laboratory

1952

Schrödinger in 1952

"... whenever experiment with just one electron or atom or (small) molecule. In thought experiments, we sometimes assume that we do; this invariably entails ridiculous consequences ... we are not experimenting with single [quantum] particles, any more than we can raise Ichthyosauria in the zoo."

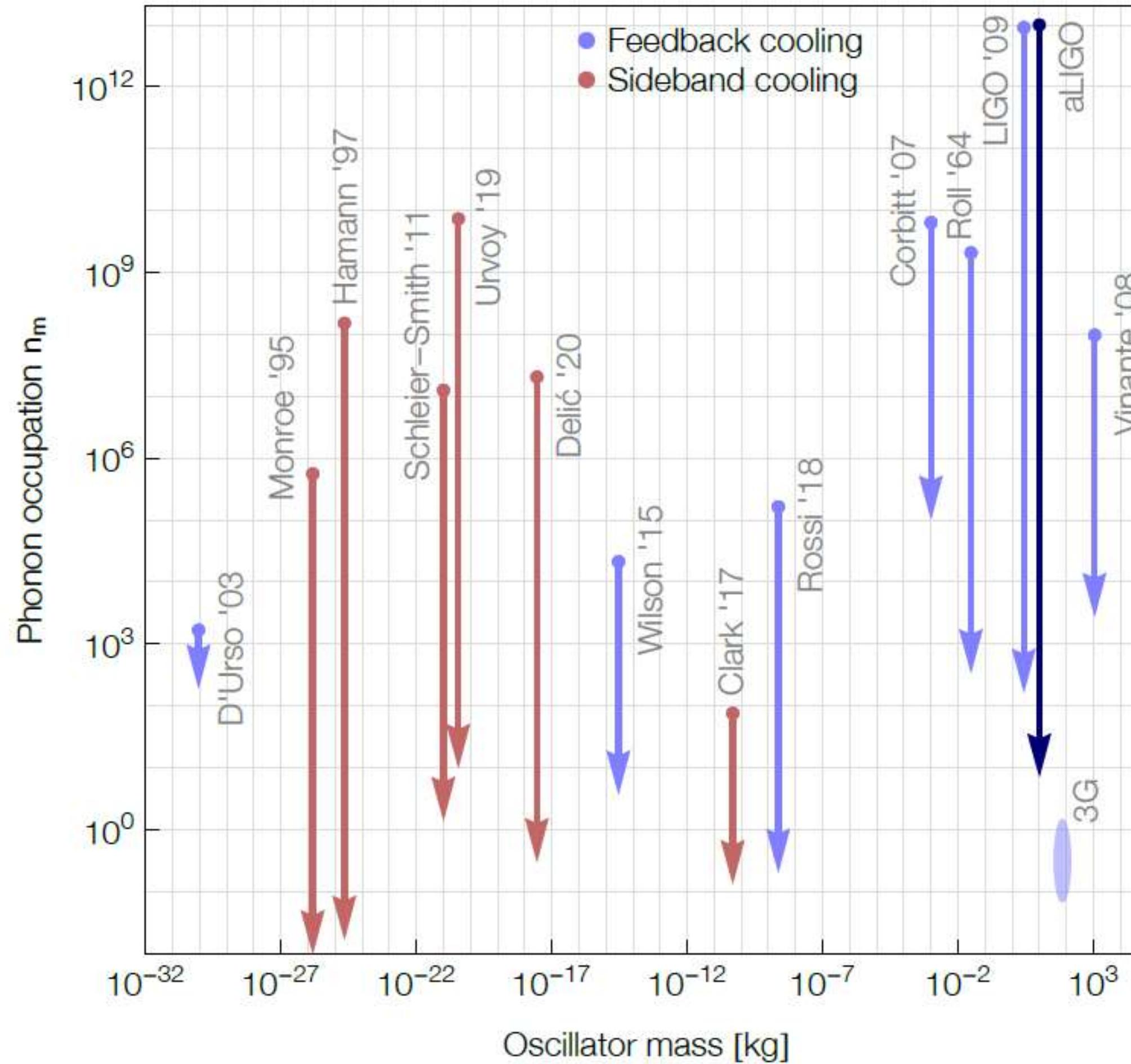


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2021

Schrödinger in 1952

"... whenever experiment with just one electron or atom or (small) molecule. In thought experiment entails ridiculous [quantum] particle..."

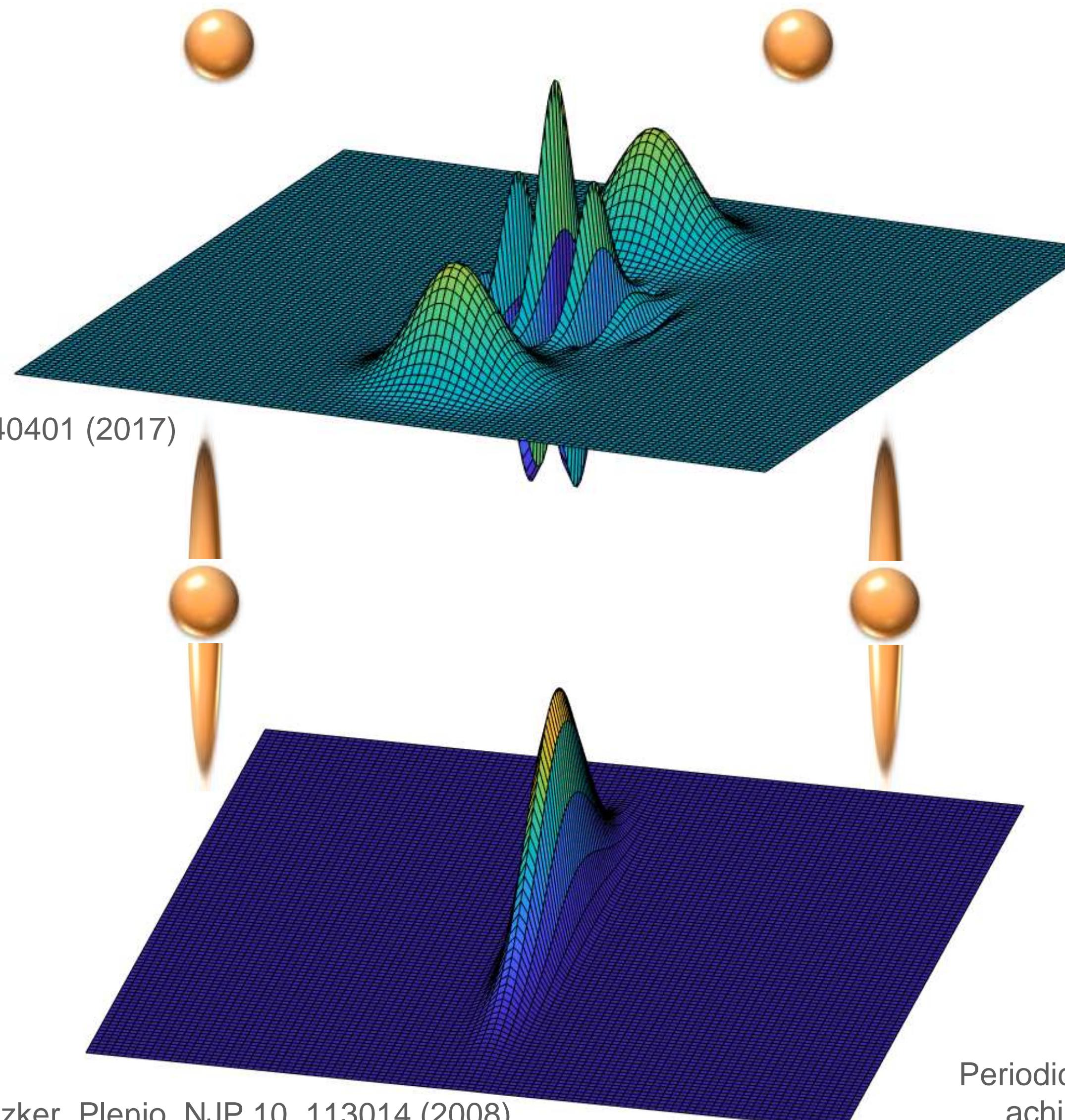


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Challenges

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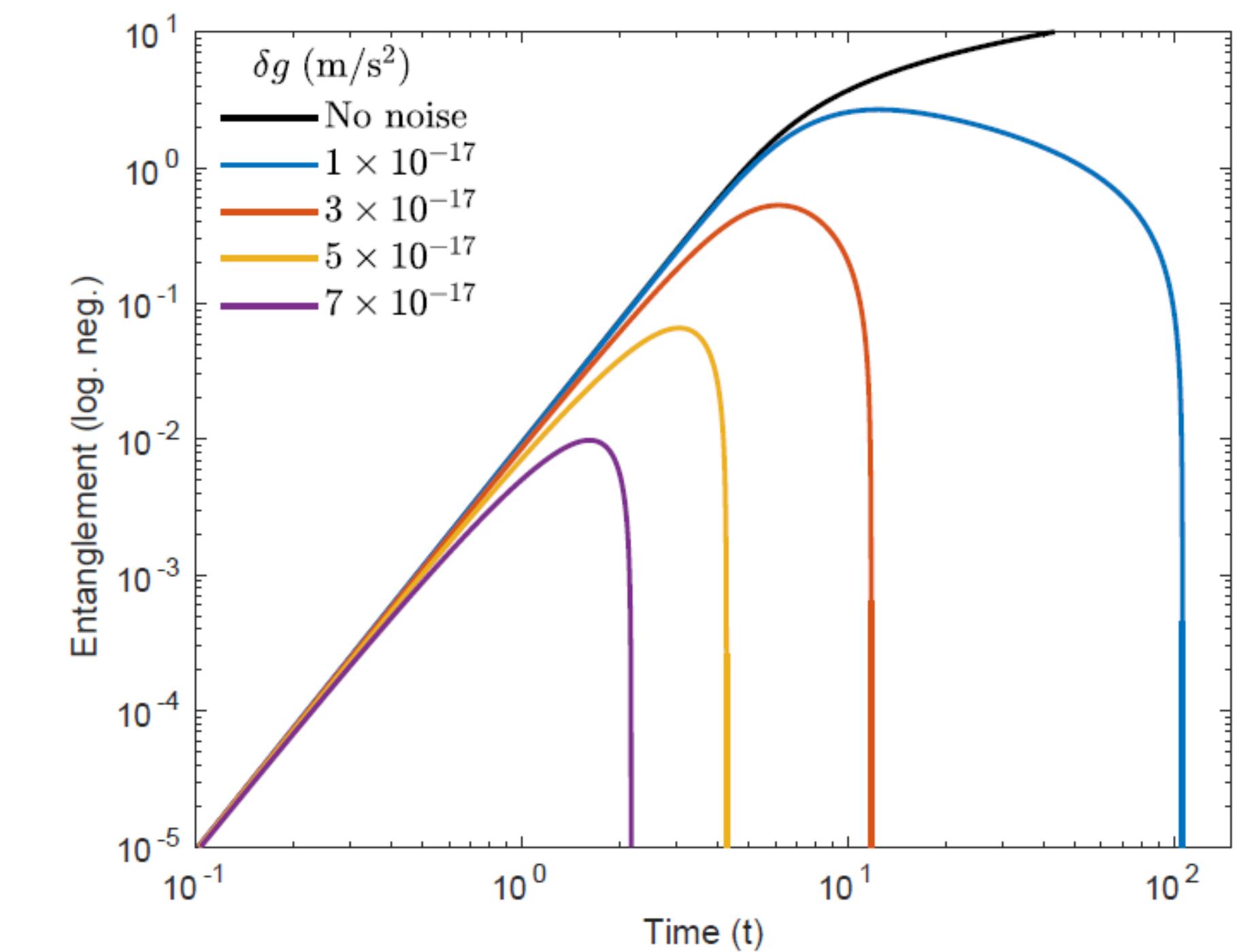


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Cosco, Pedernales, Plenio, arXiv:2012.07815 & Weiss, Road, Torrontegui, Aspelmeyer, Romero-Isart, arXiv:2012.11235

Periodic modulation of potential
achieves rapid squeezing



Mendez-Veiga, Pedernales, Plenio

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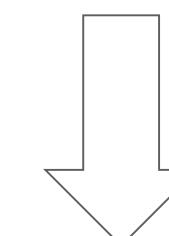
Challenges

Gravity: $M = 1 \text{ Kg} @ L = 1000 \text{ m} \rightarrow \delta g = 6.67 \cdot 10^{-17} \frac{\text{m}}{\text{s}^2}$

Electric: $M = 1e^- @ L = 10\text{cm}$
from $1\mu\text{m}$ body with static dipole moment due to $1e^-e^+$ $\rightarrow \delta g = 4.62 \cdot 10^{-17} \frac{\text{m}}{\text{s}^2}$

Magnetic: Diamagnetic particle in $B = 0.1\text{T}$ & random gradient 10^{-12} T/m $\rightarrow \delta g = 7.96 \cdot 10^{-17} \frac{\text{m}}{\text{s}^2}$

Temperature, collisions, spin flips, ...

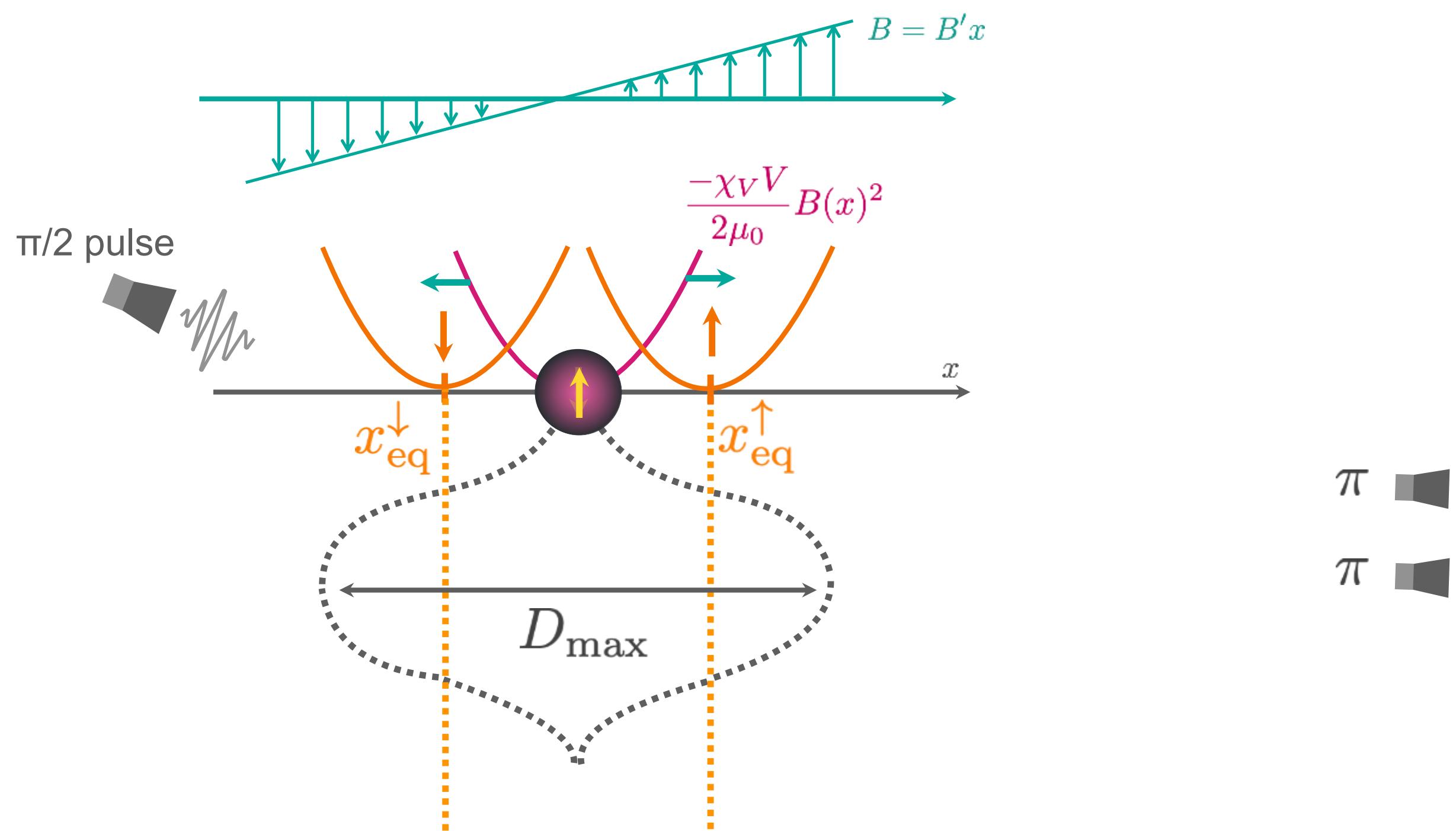


Clean up experimental environment
as much as possible

Need to develop strategies for measurement protocols that are robust to noise.

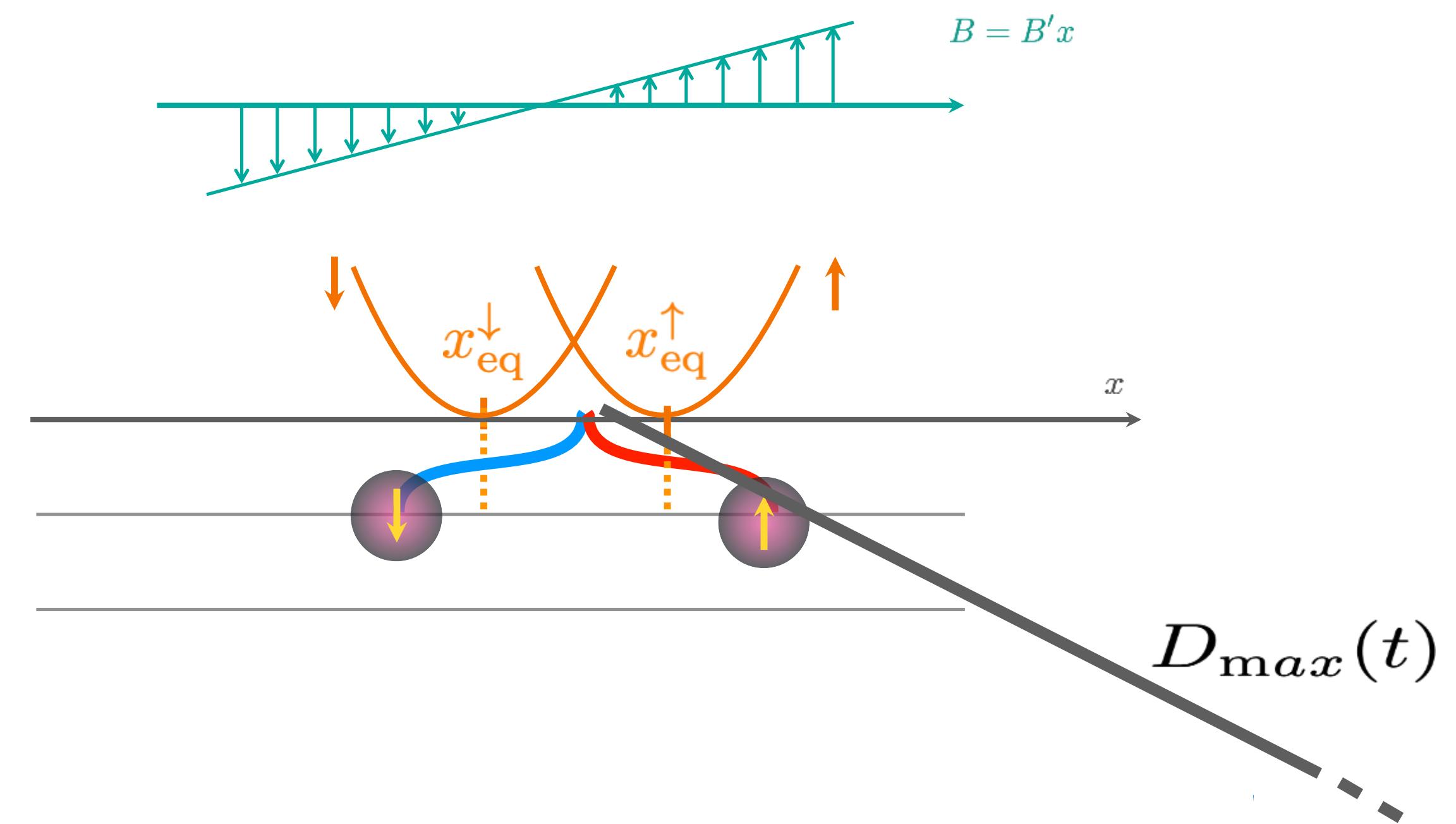
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Curing Slow Noise by Symmetrisation



π

π



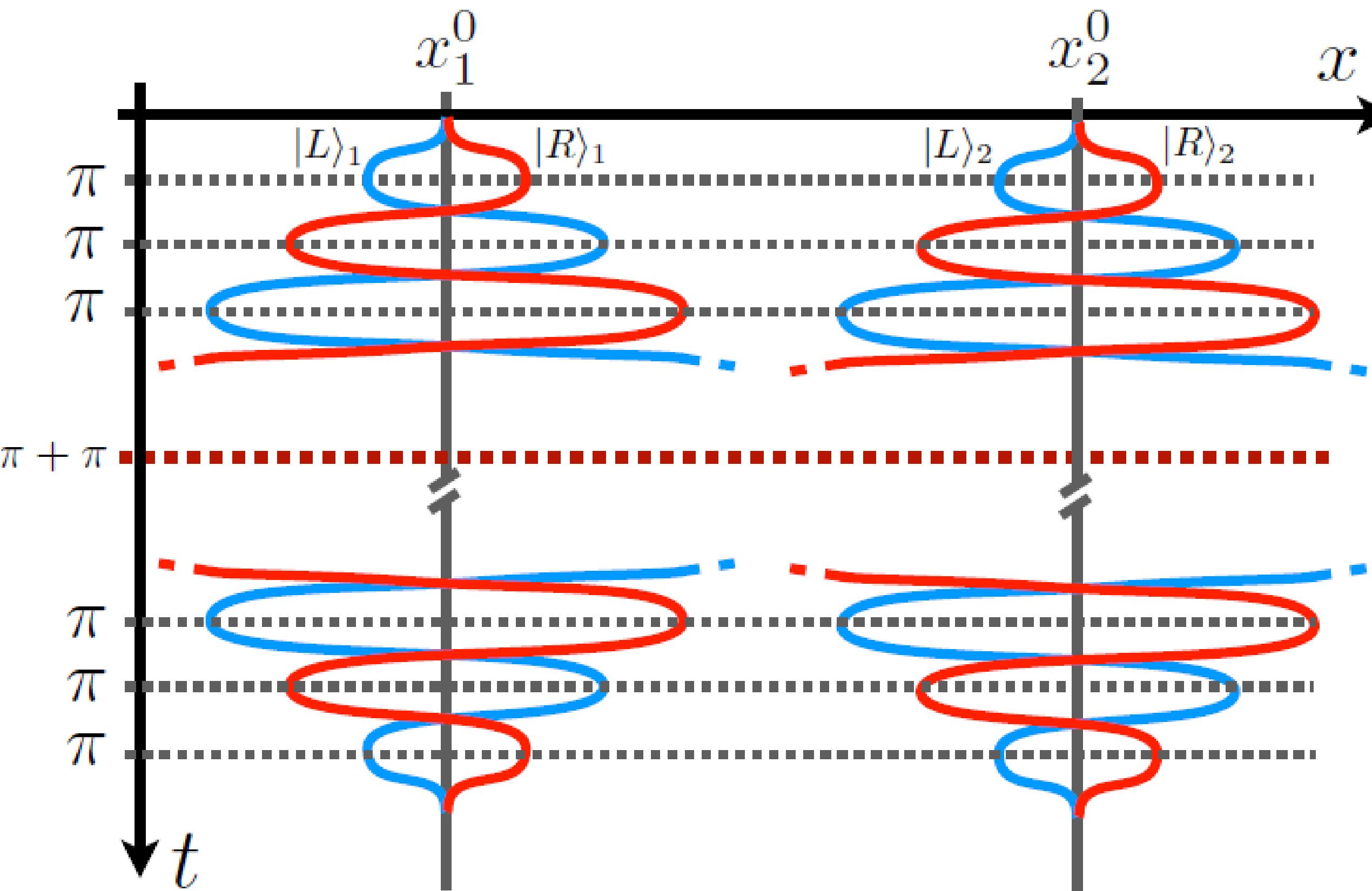
$$D_{max} = \frac{4\hbar\gamma_e\mu_0}{-\chi_V} \frac{1}{VB'}$$

$$D_{max} = \frac{4\hbar\gamma_e}{\pi V} \sqrt{\frac{\mu_0}{-\chi_V \rho_D}} t$$

Symmetrisation of path averages slow random forces

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Curing Slow Noise by Symmetrisation

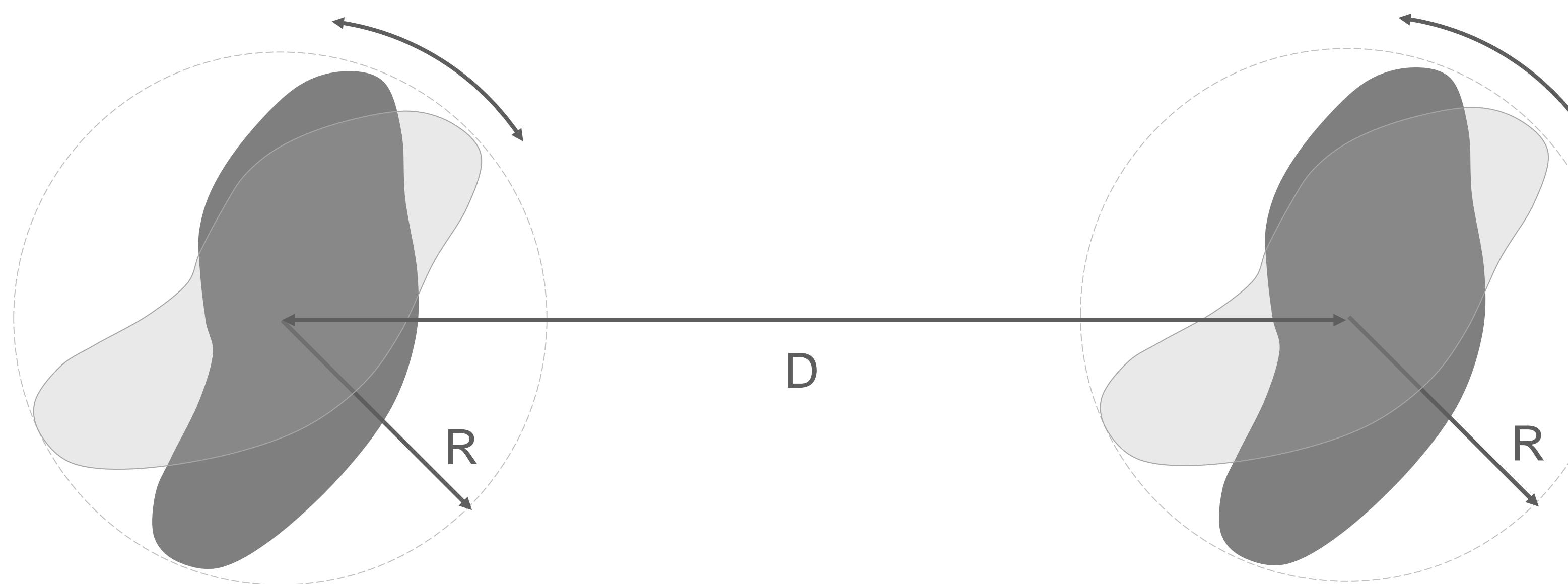


Force gradients are not averaged, hence short distance interaction between particles is preserved

Signal to noise ratio is improved

Challenges to Gravity in the Laboratory

Curing Noise from Distant Sources Part I

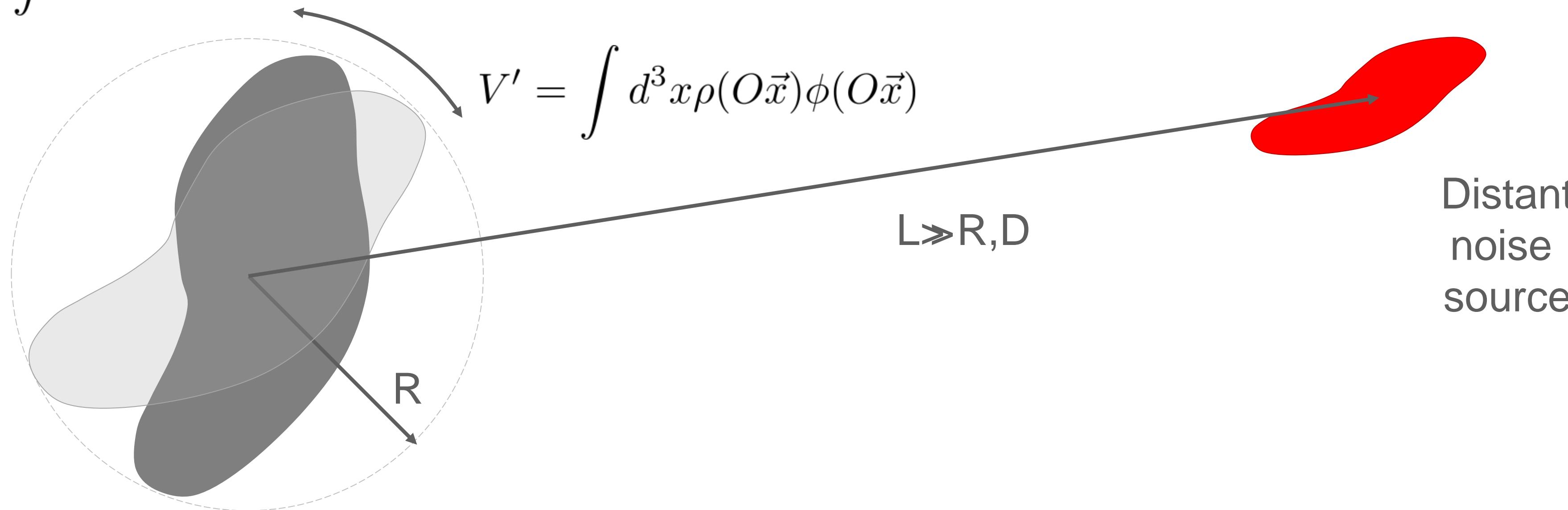


Interaction of masses in
superposition of orientations

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Curing Noise from Distant Sources Part I

$$V = \int d^3x \rho(\vec{x}) \phi(\vec{x})$$



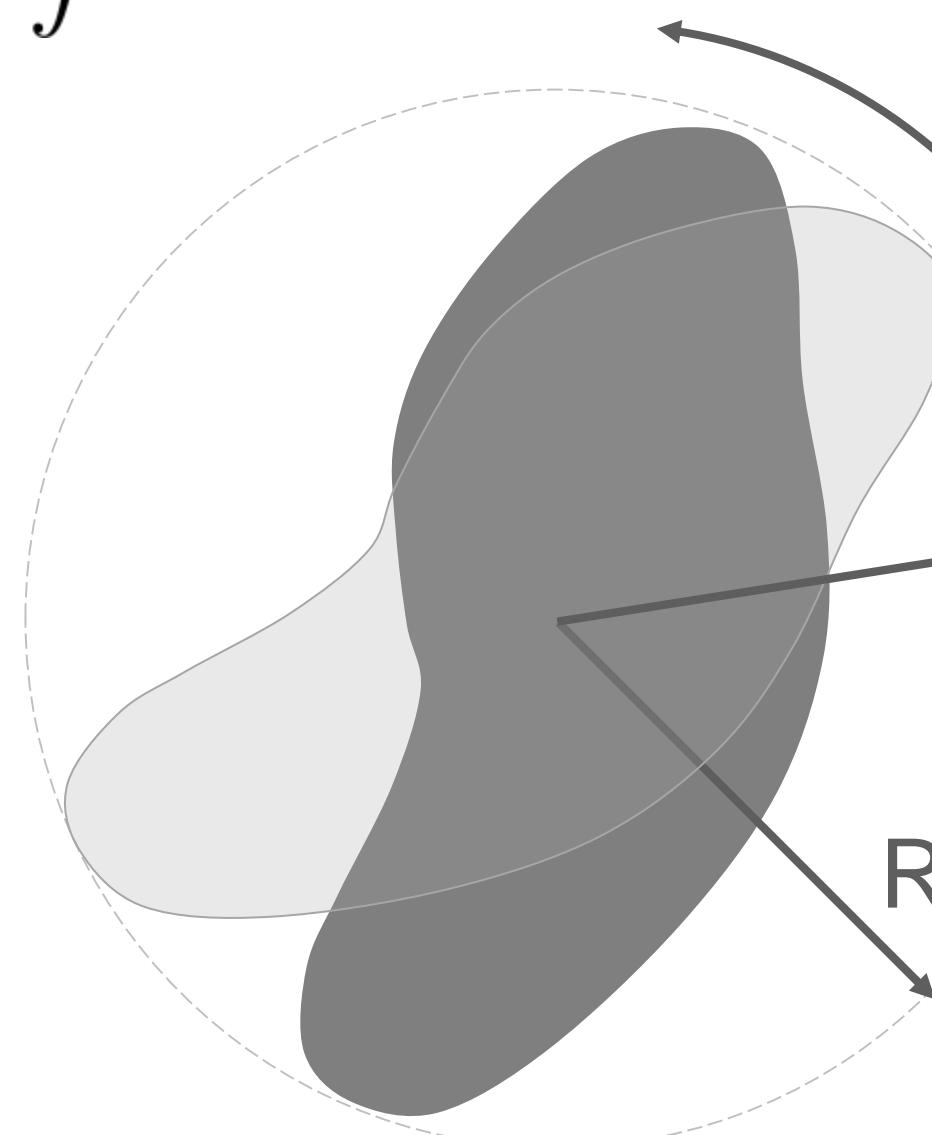
Mass in superposition
of orientations

Presence of distant noise source
leads to fluctuation in energy of
different orientations of test mass.

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Curing Noise from Distant Sources Part I

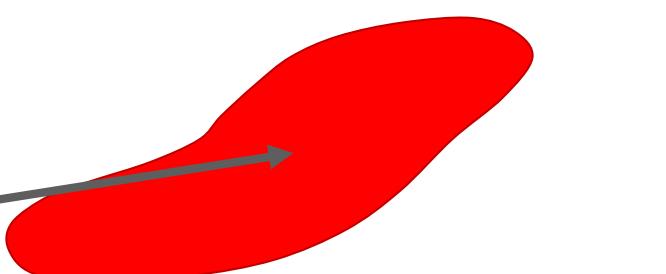
$$V = \int d^3x \rho(\vec{x}) \phi(\vec{x})$$



Mass in superposition
of orientations

$$V' = \int d^3x \rho(O\vec{x}) \phi(O\vec{x})$$

$$L \gg R, D$$



Distant
noise
source

$$\phi(\vec{x}) = \sum_{n=0}^{\infty} \phi_n(\vec{x})$$

$$= \sum_{n=0}^{\infty} \sum_{i_1, \dots, i_N=1}^3 M_{i_1, \dots, i_N} \underbrace{\vec{x}_{i_1} \cdot \dots \cdot \vec{x}_{i_N}}_{\sim R^N}$$

$$\sim \left(\frac{1}{L}\right)^N$$

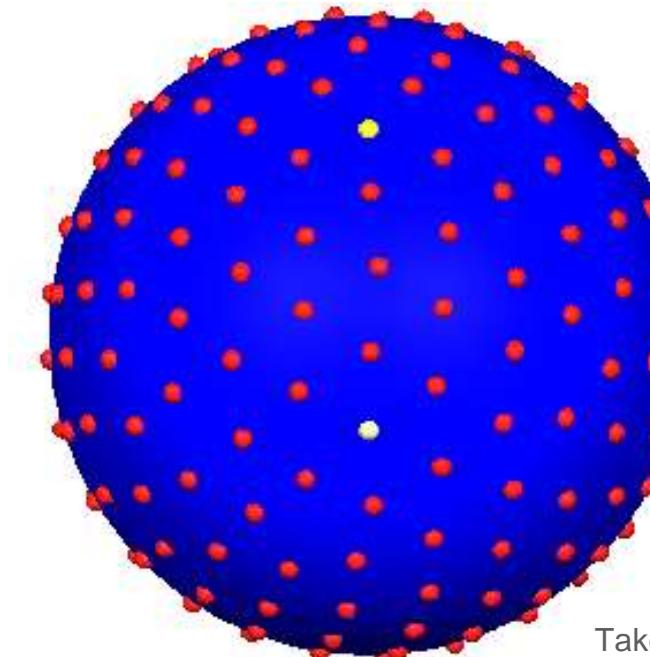
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Curing Noise from Distant Sources Part I

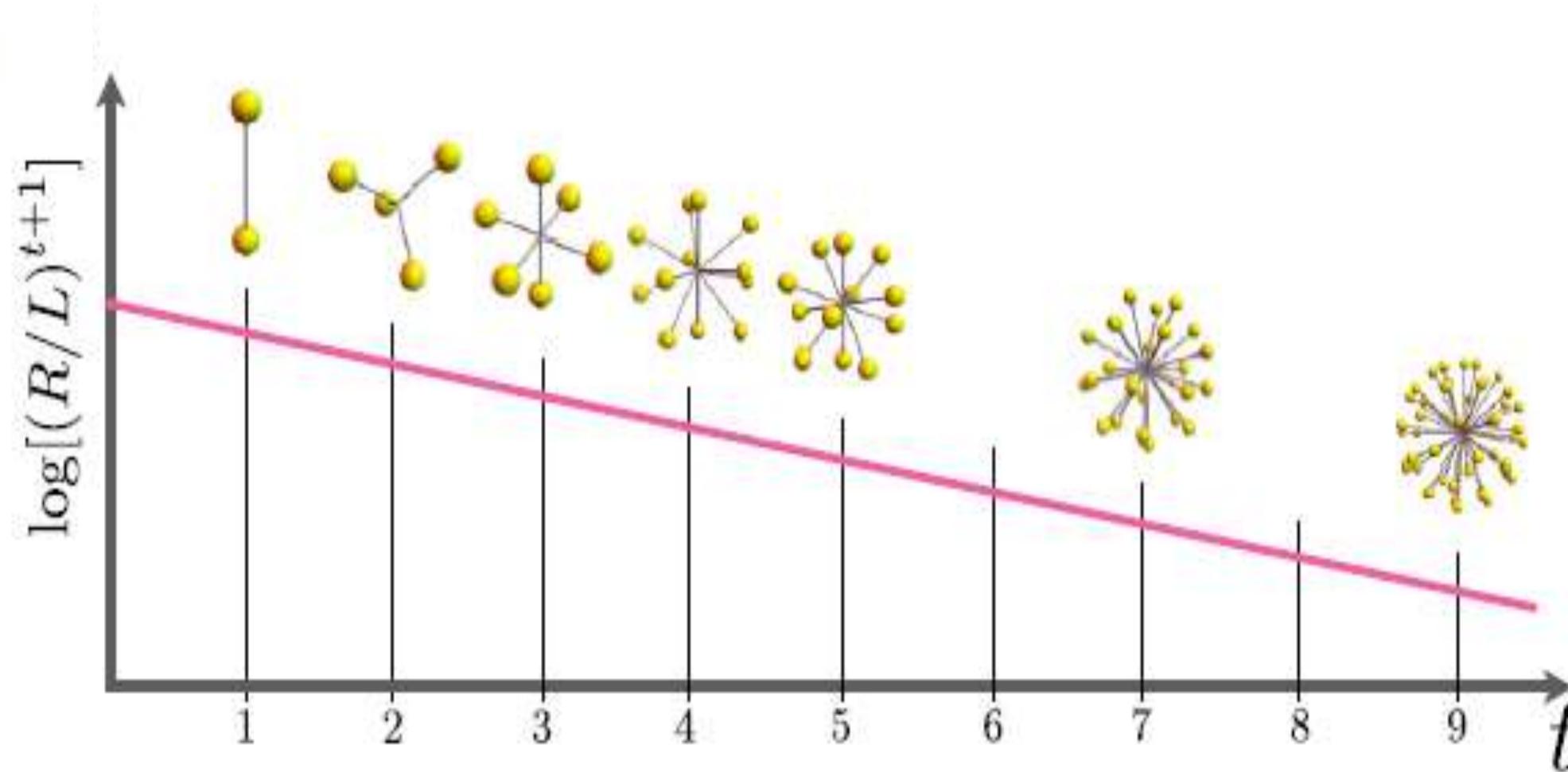
Spherical t-design: Any set of points \vec{x}_i such that

$$\int_{S^2} f(\vec{x}) d\mu(\vec{x}) = \frac{1}{N} \sum_{i=1}^N f(\vec{x}_i)$$

for any polynomial of order t .



Taken from An & Chen, arXiv1611.02785



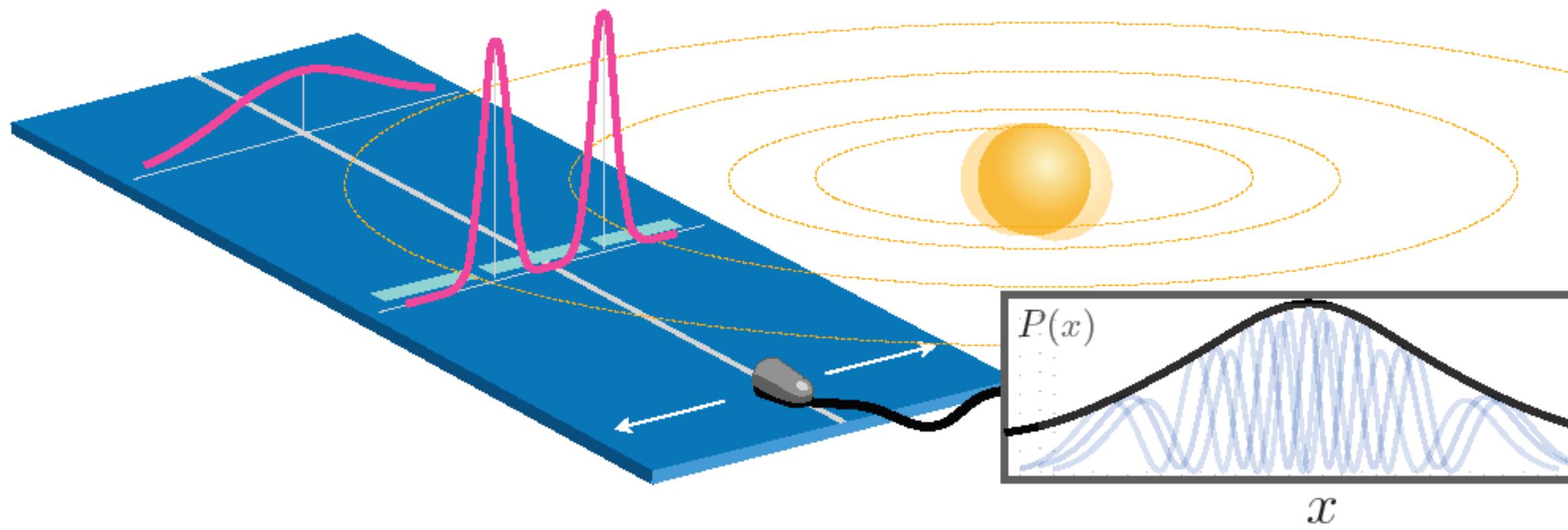
Noise $\sim \left(\frac{R}{L}\right)^N$

Interaction $\sim \left(\frac{R}{D}\right)^N$

SNR $\sim \left(\frac{L}{D}\right)^N \rightarrow \infty$

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Curing Noise from Distant Sources Part II



$$\bar{P}(x, t_k) = \frac{e^{-\frac{x^2}{2(\sigma_{t_k}^2 + \sigma_\gamma^2)}}}{N_{t_k}} e^{-\frac{[x - x_\gamma(t_k)]^2}{2(\sigma_{t_k}^2 + \sigma_\gamma^2)}} \cos\left[k t_k \cos\left(2kx_k - \frac{\sigma_{t_k}^2}{\sigma_\gamma^2} x_\gamma(t_k)\right)\right]$$

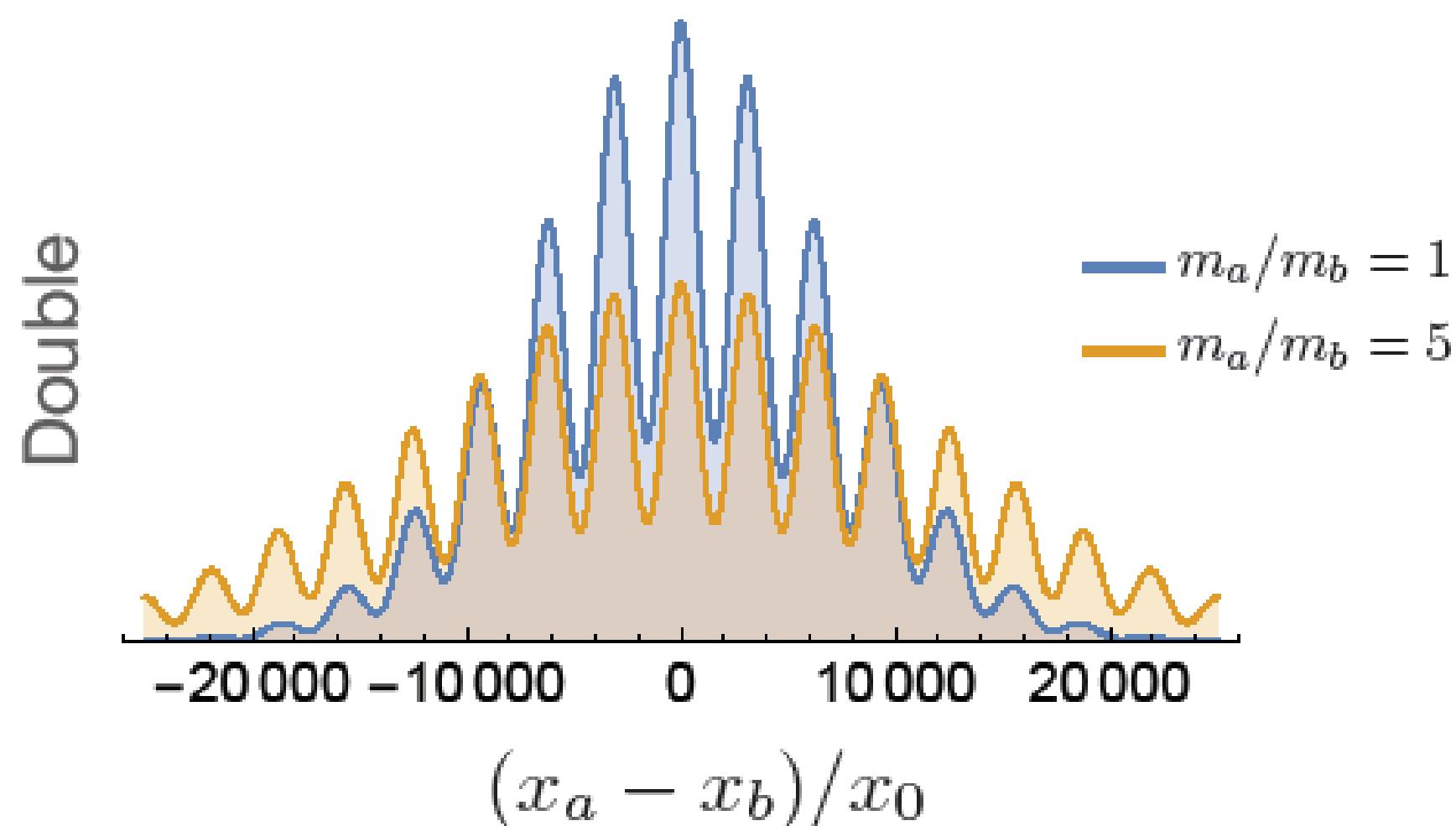
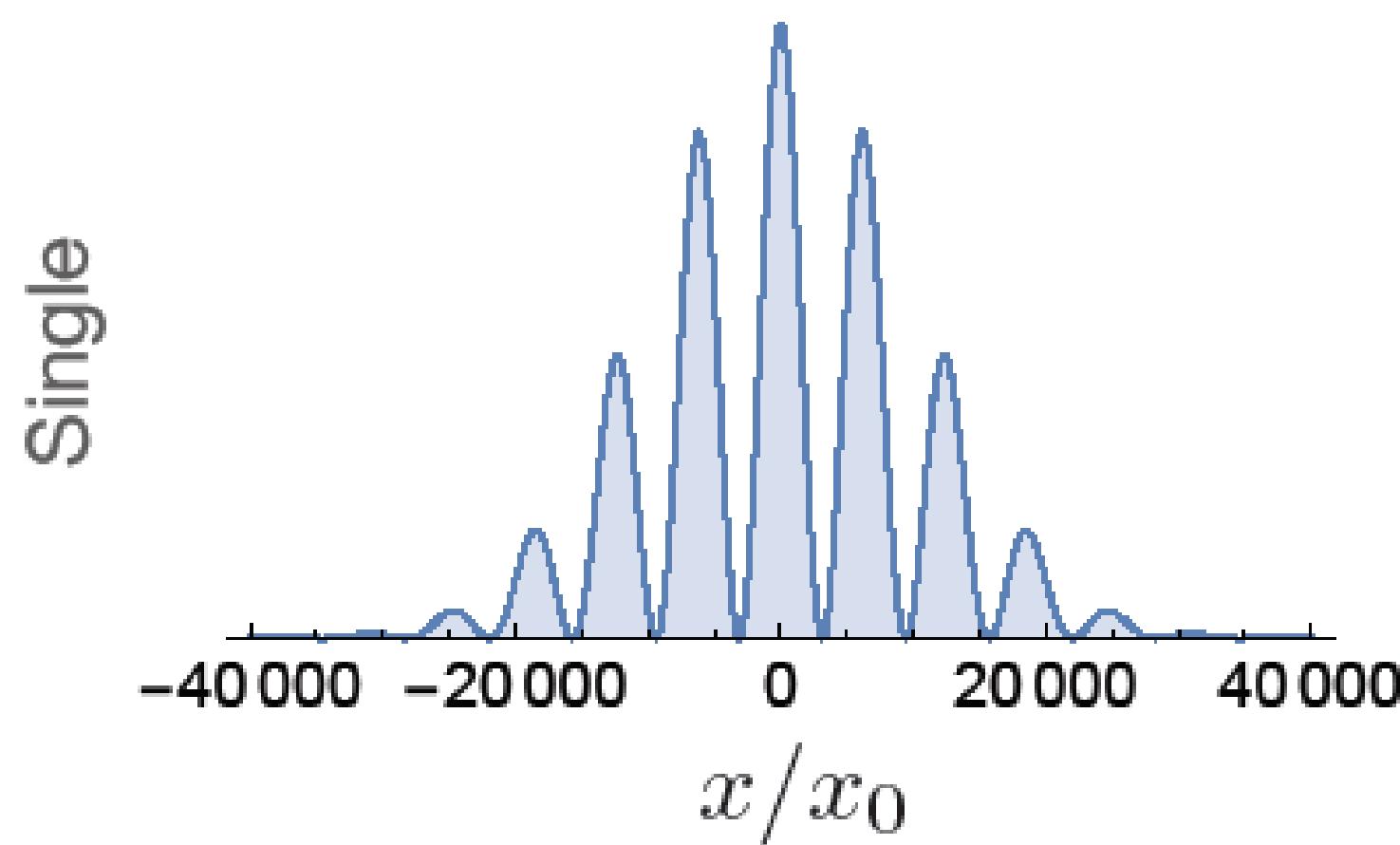
Coordinate $x_- = \frac{x_1 - x_2}{2}$ is insensitive
to fluctuations

but do the setups have to be identical?

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Curing Noise from Distant Sources Part II

Noiseless



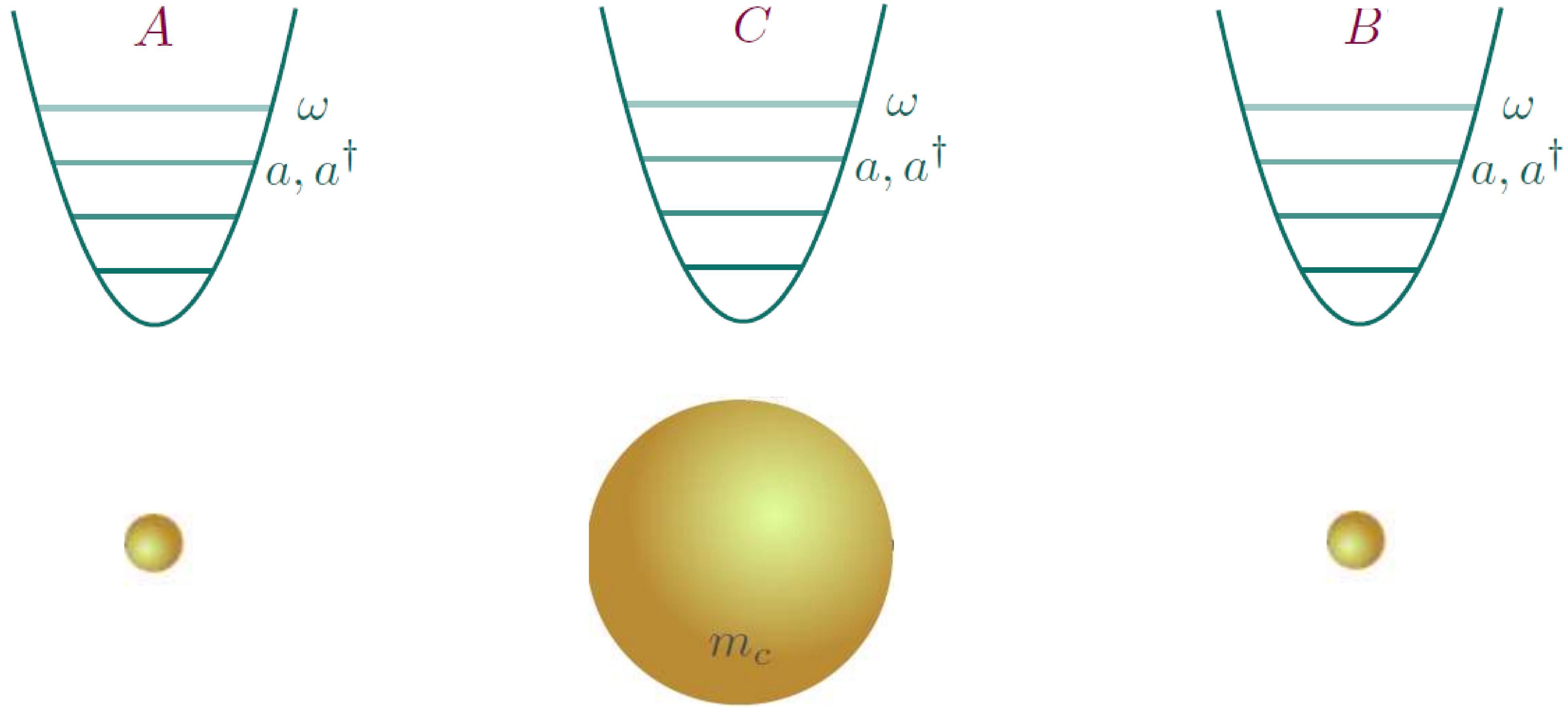
Can be generalised to

- arbitrary masses between experiments
- Use n setups to eliminate n^{th} order gradient perturbations

...

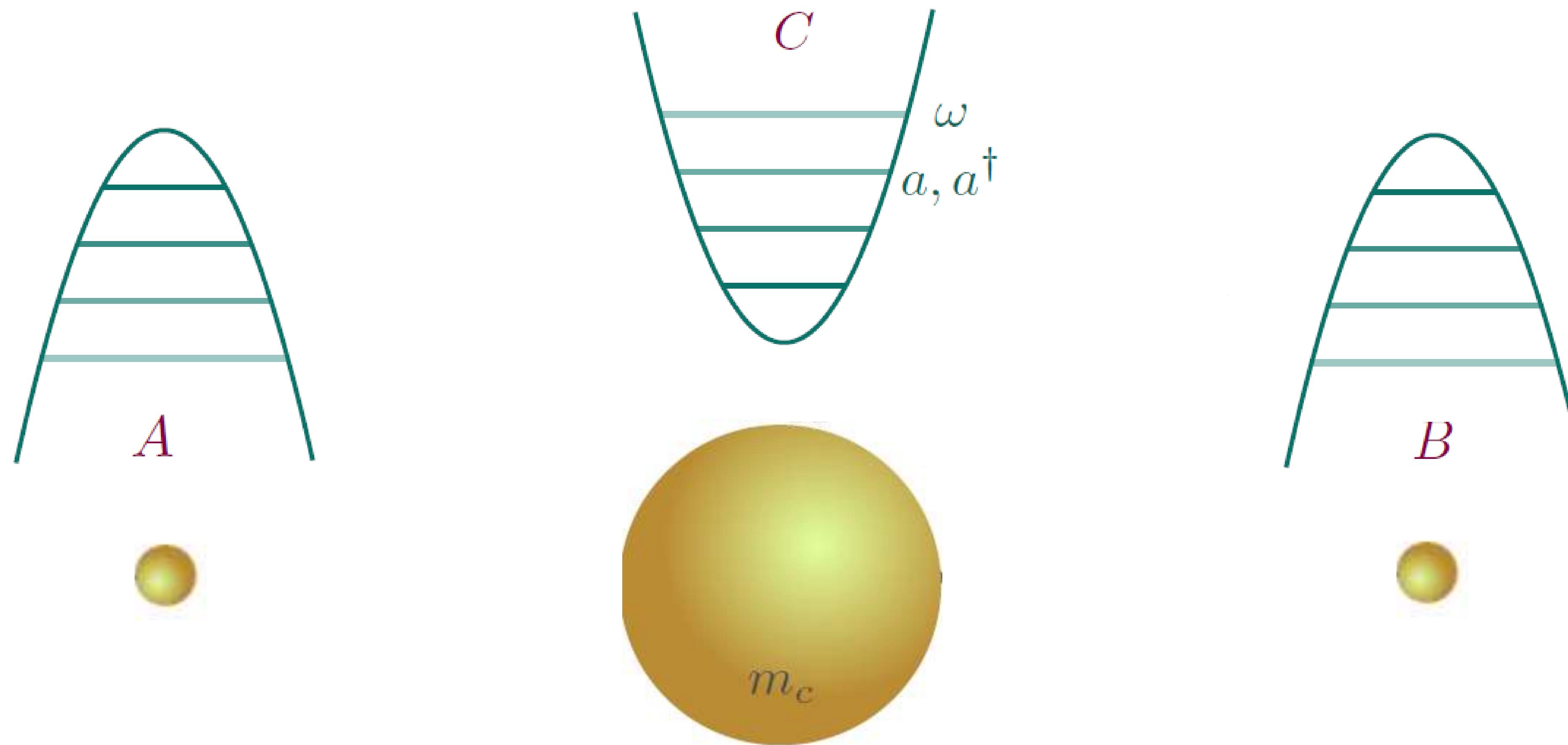
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Speeding up Protocols



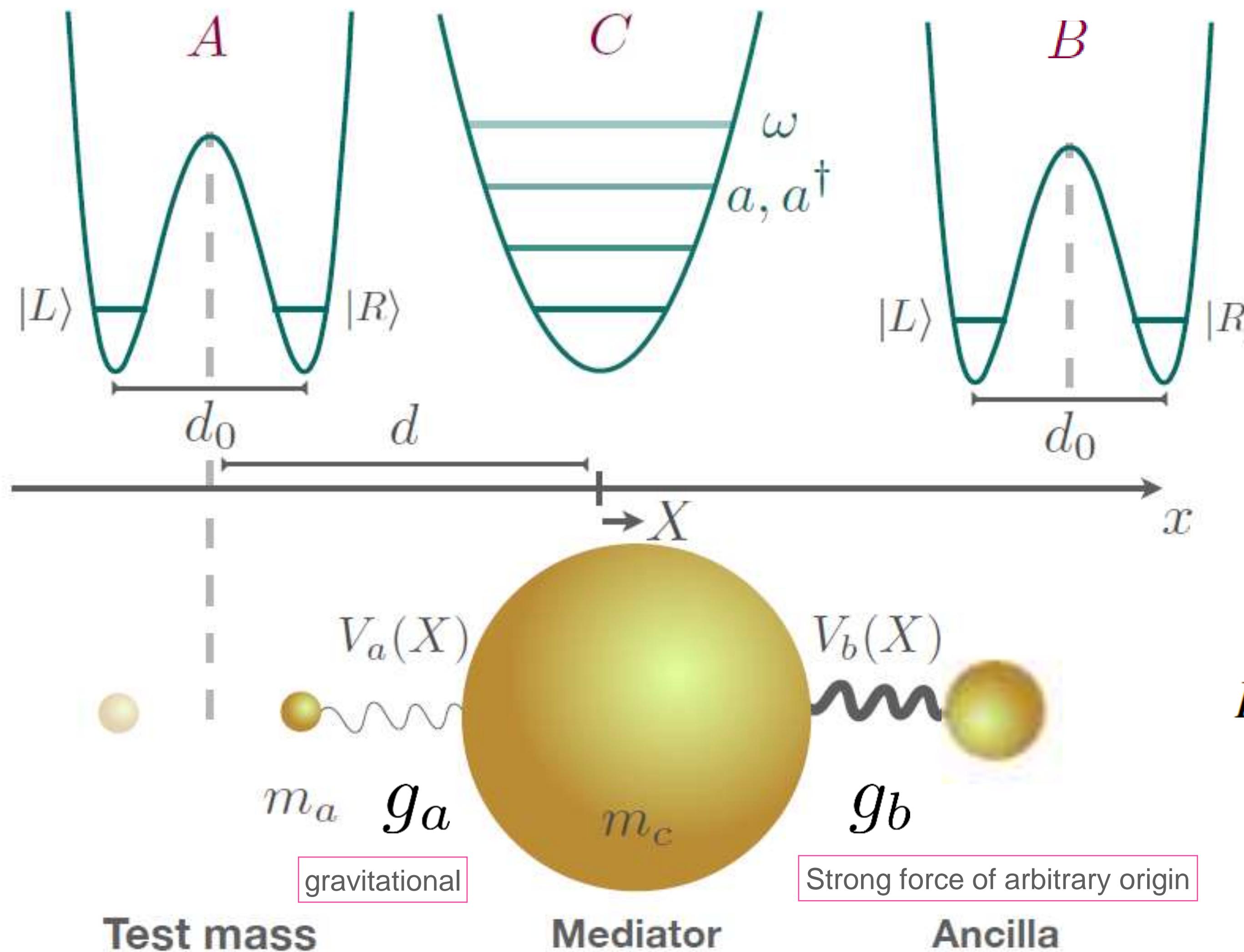
Challenges to Gravity in the Laboratory

Speeding up Protocols



Challenges to Gravity in the Laboratory

Speeding up Protocols



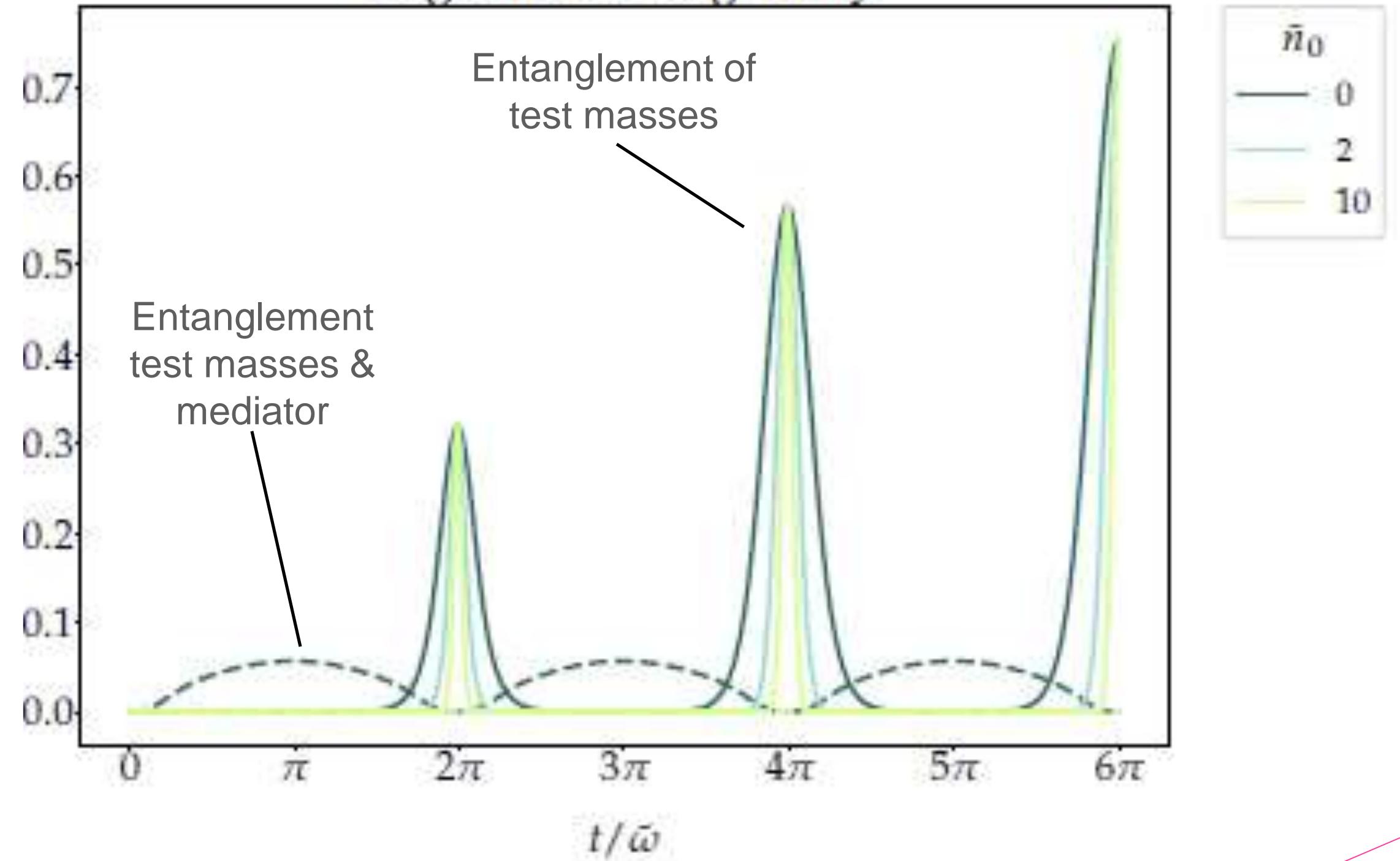
$$H = \hbar\omega_a \sigma_a^z + \hbar\omega_b \sigma_b^z + \hbar\tilde{\omega} a^\dagger a + \hbar(g_a \sigma_z^a + g_b \sigma_z^b)(a + a^\dagger)$$

$$g_b \gg g_a$$

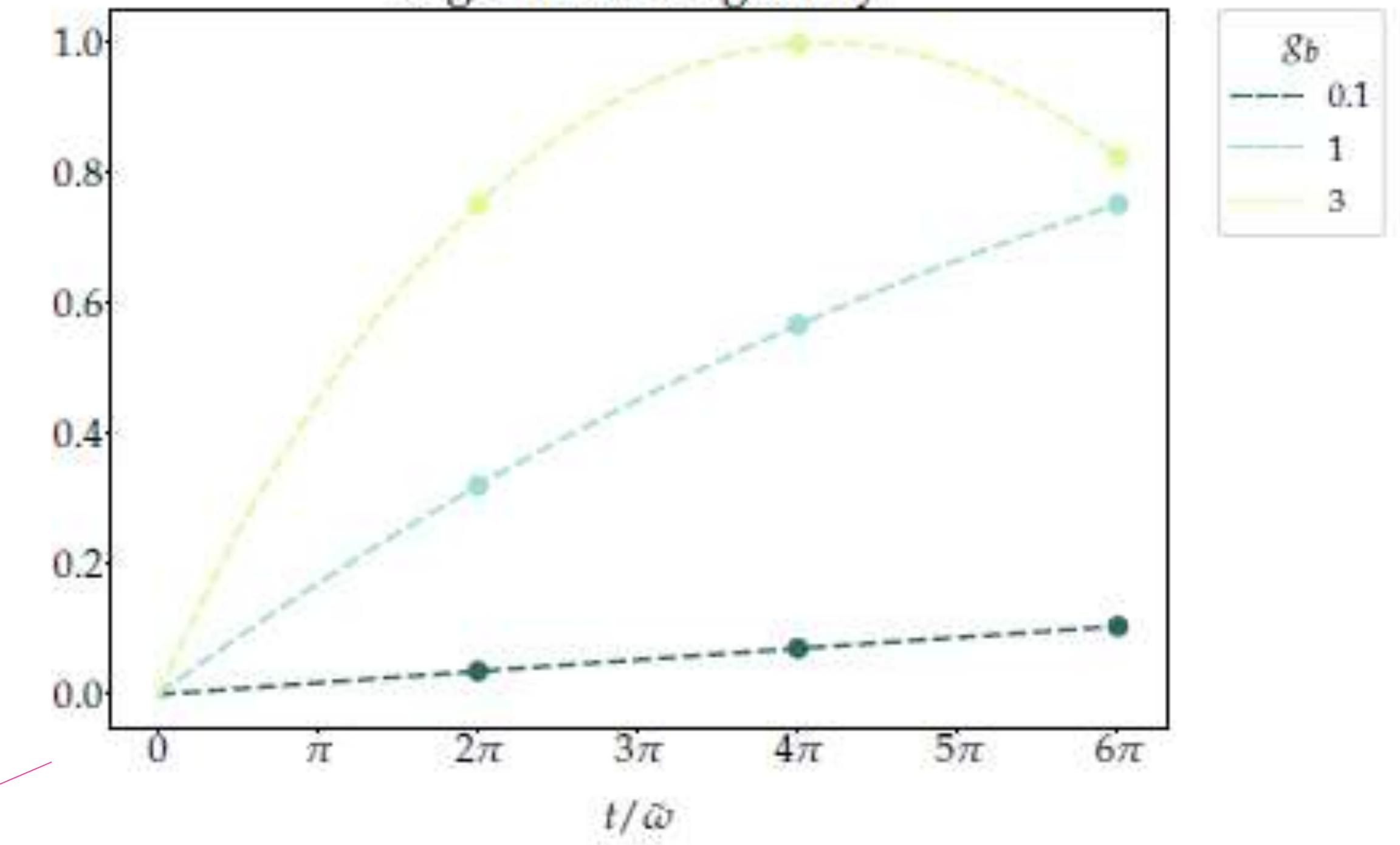
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Speeding up Protocols

Logarithmic Negativity



Logarithmic Negativity



$$U(t) =$$

$$\alpha_t = \frac{e^{-i\omega t} - 1}{\omega}$$

$$e^{-i\left[\frac{2g_a g_b}{\tilde{\omega}}\right]\sigma_z^a \sigma_z^b \left(t - \frac{\sin \tilde{\omega}t}{\tilde{\omega}}\right)}$$

Challenges to Gravity in the Laboratory

Speeding up Protocols

Origin of enhancement is mass and amplitude of mediator

Limit: Amplitude comparable to distance of test masses

Ratio of achievable
entanglement
for the same time t

$$\frac{\phi_m}{\phi_d} = \frac{1}{\sqrt{2}} \frac{m_c}{m_a} \frac{\Delta_c}{d_0} \leq \frac{1}{\sqrt{2}} \frac{m_c}{m_a} \frac{d}{d_0}$$

Independent of temperature of mediator !

Conclusion: With the investment of sufficiently much thought to increase experimental perfection, material properties etc and, at the same time, an effort to design robust protocols, Feynman's thought experiment may well become a reality before the 100th birthday of its original proposal.

Institute of Theoretical Physics & Center for Quantum Biosciences



Professors

Martin Plenio
Susana Huelga

Postdocs

Benjamin D'Anjou
Ish Dhand
Shreya Kumar
Ludovico Lami
Jaemin Lim
Julen Pedernales
Dayou Yang

PhD students

Benjamin Desef
Giovanni Di Meglio
Giovanni Ferrari
Theodore Ilias
Kevin Kessing
Martin Korzeczek
Trinidad Lantaño-Pinto
Lea Lautenbach
Nicola Lorenzoni
Alexander Nüßeler
Ilai Schwarz
Alejandro Somoza Marquez
Giovanni Spaventa
Kirill Streitsov
Thomas Theurer
Clemens Vittmann

Master students

Lennart Bosch
Iyan Mendez-Veiga
Marit Steiner
Raphael Weber



Alexander von Humboldt
Stiftung/Foundation

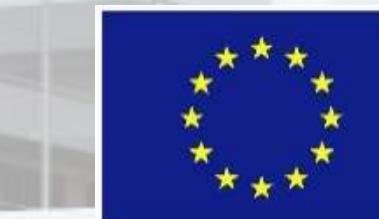


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(BioQ) 2013 -2019



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