

Weak magnetic field corrections to low energy light vector and axial mesons couplings and mixings

Fabio L. Braghin

Federal University of Goiás, Goiânia

Workshop on Electromagnetic Effects in Strongly Interacting Matter

ICTP-SAIFR / IFT-UNESP – São Paulo, October 25-28th 2022





OUTLINE

- 1- Motivations and framework
- Dynamical derivation of hadron models/couplings from QCD
- The limiting case of the NJL model under strong B

2- Light Vector/axial mesons couplings (Yukawa and higher order)

- Wess-Zumino-Witten type couplings

and the axial (vector) content of vector (axial) mesons

- 3 (Relatively) Weak magnetic fields
- Vector/axial mesons mixings and VMD at finite magnetic field
- Results for vector and axial coupling constants, form factors, averaged quadratic radii

- Final remarks

Talk based on:

F.L.B., Phys. Rev. D105, 054009 (2022)
T.H.Moreira, F.L.B., Phys. Rev. D105, 114009 (2022)
F.L.B., Journ. of Phys. G47, 115102 (2020)
F.L.B., Phys. Rev. D97, 0140022 (2018); D101, 039902(E) (2020)
F.L.B., Phys. Rev. D94, 074030 (2016)

Funding:





Motivations

Constituent Quark Model (CQM)

GellMann-Zweig And many others

In these models: "dressed" (constituent) quark masses are responsible for the hadrons masses They are assumed to be "quasiparticles" (not propagating(?)) And it works...

Quark masses (from the HIggs) are much smaller than needed to describe hadron masses

Mechanisms of mass generation : Dynamical Chiral Symmetry Breaking Associated to other effects

 $\langle \bar{q}_R q_L + \bar{q}_L q_R \rangle \simeq -(250 MeV)^3$

Other works/talks in this conference

```
From constituent quarks 

M*u ~ 360 MeV

M*d ~ 370 MeV

M*s ~ 510 MeV
```

Most of Hadrons Spectra support or suggest the idea (original quark models/ eightfold way)

> It can receive corrections: Diquarks Virtual n-quarks states from Fock space etc



Motivations

Strong magnetic fields

Weak with respect to a hadron energy scale M*, Mproton, Mpion

$$\frac{eB_0}{M^*} \sim 0.2 \to 10$$

Non-central Relativistic Heavy Ions Collisions (r.h.i.c.)

$$\left(\frac{eB_0}{M^*}\right)^n, \quad n=1,2$$

$$eB_0 \simeq 0.5 m_\pi^2 \simeq 0.1 \dot{M}^{*2} \simeq 10^{17} \,\mathrm{G},$$

Many possible effects some of them addressed in this conference



Dense-stars/ Magnetars

And

Primoridial Universe Specific questions: Usually: how masses, decay rate change with B? <u>Here mostly: how couplings between hadrons change with B?</u>

Several groups addressed hadron couplings under B Ferrer, de la Incera, Hoffmann, Ayala, etc The idea is to investigate a leading term of the QCD quark-effective action Obtained from QCD Lagrangian



The quark-quark interaction mediated by ONE gluon exchange

WITH however an improvement due to "non perturbative" (non Abelian) effects

This present approach provides, to some extent, similar results to the QCD-SDE at the rainbow ladder approach

And also, to some extent, similar to the **NJL model** - leading flavor structure independent of gluon sector

Other effects for quark interactions and/from Gluon dynamics and related effects: under work

 $G_{NJL} \sim 1/Mg^2$

QCD Effective action \rightarrow quark antiquark interaction

One leading term of the QCD effective action (quarks)

$$Z = N \int \mathcal{D}[\bar{\psi}, \psi] \exp i \int_{x} \left[\bar{\psi}(i\partial - m)\psi - \frac{g^{2}}{2} \int_{y} j^{b}_{\mu}(x) \tilde{R}^{\mu\nu}_{bc}(x - y) j^{c}_{\nu}(y) + \bar{\psi}J + J^{*}\psi \right]$$
Gluon propagator as external input
Quark-gluon (running)
Coupling Constant
(external input)
Gluon propagator as external input
* non perturbative one \rightarrow DChSB
* to some extent non Abelian
dynamics accounted
In the 1980's and 1990's by considering

Equal current quark mass Flavor SU(2) or SU(3) Chiral Perturbation theory Has been derived from quark-antiquark interaction by many With works in the following decades Roberts,Praschifka,Cahill,Ebert,Reinhardt,Volkov,Holdom and others

General approach For the flavor structure



Quark sector (very large gluon Effective mass)

Nambu-Jona-Lasinio model: ONE-LOOP BACKGROUND quark sector

Many works with **G(B)** for strong magnetic fields Farias, Krein, Avancini, Costa, Oliveira, Endrodi, Marko, Chao, Scoccola, Coppola, and several others Usually **G(B)** is atributed to gluon dynamics (polarization) So that gluon propagator and effective mass should depend on B

The difference

Between Gs and Gps

A mechanism to generate **G(B)** different from gluon dynamics 1-loop

Non degenerate

Guu, Gdd, Gss

Gij, including mixing

However when using effetive models (or any EFT)

 trying to improve the predictive power
 one may has to deal with possible double counting effects
 (eg. Quantum fluctuations of fundamental d.o.f OR of effective d.o.f.)

- in other words: what is an effective model?

Other mixing effects for the NJL model: On going

$$\mathcal{O}\left(\frac{1}{M^{*2n}}\right)$$
Vacuum and
Weak B

$$\mathcal{L}_{1} = -g_{1} \operatorname{tr}_{F} (U + U^{\dagger}) + \frac{F^{2}}{4}g_{c} \operatorname{tr}_{F} D^{\dagger}U^{\dagger}DU$$

$$-l_{5} e^{2} \operatorname{tr}_{F} (QF_{\mu\nu}U^{\dagger}QF^{\mu\nu}U),$$

$$T_{\pi-A_{\mu}} = +\frac{(l_{3} + l_{4})}{16}m_{\pi}^{4} \operatorname{tr}_{F} (U^{2} + U^{\dagger}^{2})$$

$$+\frac{l_{4}}{8}m_{\pi}^{2} \operatorname{tr}_{F} (D_{\mu}U^{\dagger}D^{\mu}U) (U + U^{\dagger})$$

$$-\frac{l_{1}}{4} \operatorname{tr}_{F} (D_{\mu}U^{\dagger}D^{\mu}U)^{2}$$

$$-\frac{l_{2}}{4} \operatorname{tr}_{F} (D_{\mu}U^{\dagger}D_{\nu}U) \cdot (D^{\mu}U^{\dagger}D^{\nu}U),$$

$$L_{D-F} = -i\frac{l_{6}}{2} \operatorname{tr}_{F} \left[(QF_{\mu\nu}(D^{\mu}U)^{\dagger}(D^{\nu}U))$$

$$+ (QF_{\mu\nu}(D^{\mu}U)(D^{\nu}U)^{\dagger}) \right],$$

<u>This EFT (local pion field)</u> <u>with electromagnetic couplings</u> + chiral symmetry breaking terms:

F.L.B. Eur. Phys. Journ. (2018)

arge Nc EFT: benchmark of the method

S.Weinberg, (2010) to cope * CQM - Manohar-Georgi form And * Large Nc- 't Hooft]

Including hadron electromagnetic couplings U(1)

$$\begin{split} D_{\mu}U &= \partial_{\mu}U + ieA_{\mu}\left[\frac{\tau_3}{2}, U\right],\\ (D_{\mu}U)^{\dagger} &= \partial_{\mu}U^{\dagger} - ieA_{\mu}\left[\frac{\tau_3}{2}, U^{\dagger}\right], \end{split}$$

Coupling of photon To Quarks and to mesons states Emerge naturally

$$L_{q-\pi-A} = (M_{AA}A_{\mu}^{2} + M_{FF}F_{\mu\nu}F^{\mu\nu}) j_{s} + g_{vmd}A_{\mu} j_{i=3}^{\mu}$$

+ $ig_{F-js-\pi} F F_{\mu\nu}^{2} \operatorname{tr}_{F}(\{Q, Z_{+}\}Q)j_{s}$
+ $ig_{F-ps-\pi} F F_{\mu\nu}^{2} \operatorname{tr}_{F}([Q, Z_{-}][Q, \sigma_{i}]) j_{ps}^{i}$
+ $ig_{jVA} F F^{\mu\nu} \operatorname{tr}_{F}([\partial_{\mu}Z_{+}, Q]\sigma_{i}) j_{V,\nu}^{i}$
+ $ig_{jAA} F F^{\mu\nu} \operatorname{tr}_{F}([Q, \partial_{\mu}Z_{-}]\sigma_{i}) j_{A,\nu}^{i} + \mathcal{O}(A_{\mu}^{2})$

Veff for U(1) NJL in terms of sigma+pion Miransky-Shovkovy - 2015

Unusual ("anomalous") Vector mesons couplings to the axial quark current

In the vacuum

$$\mathcal{L}_{\nu j a} = i \delta_{i j} \epsilon^{\sigma \rho \mu \nu} F^{\nu j a} K_{\sigma} \mathcal{F}^{i}_{\rho \mu} j^{A, j}_{\nu} + i \epsilon^{\sigma \rho \mu \nu} F^{\nu j a} K_{\sigma} \mathcal{F}_{\rho \mu} j^{A}_{\nu},$$
$$\mathcal{F}^{i}_{\rho \mu}(Q) = Q_{\rho} V_{\mu}(Q) - Q_{\mu} V_{\rho}(Q).$$

These are Wess-Zumino-Witten terms

$$n\Gamma = -\frac{i}{240\pi^2} \int d^4K \ d^4Q \ \epsilon_{\sigma\rho\mu\nu} F^{\nu j a}(K,Q) K_\sigma \mathcal{F}^i_{\rho\mu}(Q) j^{A,i}_\nu(K,K+Q)$$

By comparing the anomalous vector meson coupling to jA

To the pion axial coupling (jA)

And to the axial meson coupling to jA

$$\mathcal{L}_{j_A} = \left[G_A Q_\mu \pi^i + G_{\bar{A}} \bar{A}^i_\mu + i \ F_{vja} \epsilon_{\mu\nu\rho\sigma} K^\nu Q^\rho V_i^\sigma \right] j^\mu_{A,i}$$

In the vacuum

$$\frac{F_{vja}(K,Q)}{G_A(K,Q)} = \frac{1}{4M^*F}.$$

Equal Internal Momentum dependence to the constituent quark axial form factor (1-loop level)

$$\frac{F_{\rm vja}(K,Q) \times |K||Q|}{G_V(K,Q)}\Big|_{Q \sim K \sim 200-500 \text{ MeV}} \sim 0.1.$$

Effect of "weak" magnetic field: eB << M*²

The background photon field interacting with hadrons (B as "strong-photon field")

And

2

Quark propagator

 $G(k) = S_0(k) + S_1(k)(eB_0)$:

Both lead basically/mostly to equal structures

Possibly with a Different proportionality factor

Vector / axial mesons couplings to constituent quarks

- relatively weak B -

Background photon field

$$I_{AV} = g_{qA} \left(A_{\mu}(x) j_{3}^{\mu}(x) + \frac{1}{3} A_{\mu}(x) j^{\mu}(x) \right) \longrightarrow Vector meson dominance$$

$$I_{FFm} = g_{1} [F_{\mu\nu} \mathcal{F}_{3}^{\mu\nu} j_{s} + F_{\mu\nu} \mathcal{F}^{\mu\nu} j_{s}^{3} + F_{\mu\nu} \mathcal{G}_{3}^{\mu\nu} j_{p} + F_{\mu\nu} \mathcal{G}^{\mu\nu} j_{p}^{3} + \frac{1}{3} (F_{\mu\nu} \mathcal{G}^{\mu\nu} j_{p} + F_{\mu\nu} \mathcal{F}^{\mu\nu} j_{s} + F_{\mu\nu} \mathcal{G}_{i}^{\mu\nu} j_{p}^{i} + F_{\mu\nu} \mathcal{F}_{i}^{\mu\nu} j_{s}^{i})],$$

$$Vector meson dominance$$

There are some not explicitly gauge invariant Because it is missing writing them The photon field as part of a covariant derivative Constant Magnetic field along z-direction:

$$\begin{split} I_{FFm} &\to g_1^B \left[\mathcal{F}_3^{xy} j_s + \mathcal{F}^{xy} j_s^3 + \mathcal{G}_3^{xy} j_p + \mathcal{G}^{\mu\nu} j_p^3 \right. \\ &+ \frac{1}{3} (\mathcal{G}^{xy} j_p + \mathcal{F}^{xy} j_s + \mathcal{G}_i^{xy} j_p^i + \mathcal{F}_i^{xy} j_s^i) \right], \qquad I_{AF} \to g_3^{B_2} i \epsilon_{ij3} [\mathcal{F}_{y\delta}^i j_{j,V}^\delta + \mathcal{G}_{y\delta}^i j_{j,A}^\delta)], \end{split}$$

$$\frac{g_1^B}{g_3^{B_1}} \sim \frac{1}{M^*}, \qquad \frac{g_3^{B_2}}{g_2^B} = \frac{1}{M^*}.$$

$$L_{v-q} = g_{r1}(V_i^{\mu}(x)j_{\mu}^{V,i}(x) + \bar{A}_i^{\mu}(x)j_{\mu}^{A,i}(x))$$

$$\frac{g_3^{B_1}}{g_{r1}} \sim \frac{3}{4}\frac{eB_0}{M^{*2}}.$$

All the coupling constants (in momentum space) correspond to the zero momentum limit (external lines) of a (momentum-dependent) form factor

 $K,Q \rightarrow 0$

From the form factors: **Corrections to rho/omega a.q.r.** due to weak magnetic fields In the plane perpendicular to the Magnetic field:

Unusual ("anomalous") Vector mesons couplings to the axial guark current K=quark incoming momentum Weak B Q=meson incoming momentum $\mathcal{L}_{vjaB} = \frac{(eB_0)}{M^{*2}} \epsilon_{ij3} \frac{F_{vja}^B(K,Q)}{M^{*2}} \left[\epsilon^{12\rho\mu} K_{\rho} Q_{\nu} \cdot V_{\nu}^i + 2\epsilon_{12\rho\nu} K^{\rho} \mathcal{F}_i^{\mu\nu} \right] j_{\mu}^{A,j} + \frac{(eB_0)}{M^{*2}} \frac{F_{vja}^B}{3M^{*2}} \left[\epsilon^{12\rho\mu} K_{\rho} Q_{\nu} \cdot V_{\nu} + 2\epsilon_{12\rho\nu} K^{\rho} \mathcal{F}^{\mu\nu} \right] j_{\mu}^{A,3}$ Small with respect to The pion axial coupling Also Wess-Zumino-Witten But with similar (equal) term That might lead to Momentum dependence to the Quantization of currents constituent quark axial form factor

$$n\Gamma = -\frac{i}{240\pi^2} \int d^4K \ d^4Q \ \epsilon_{\sigma\rho\mu\nu} F^{\nu ja}(K,Q) K_\sigma \mathcal{F}^i_{\rho\mu}(Q) j^{A,i}_\nu(K,K+Q),$$

Other WZW terms only with mesons (local) fields (same limit as NJL model, with different values/structure for coupling constants)

$$\mathcal{L}_{mix,B} = \frac{(eB_0)}{M^{*2}} G^{B,1}_{v-a} i \epsilon_{12\mu\nu} M^{*2} i \epsilon_{ij3} V^{\mu}_{i} \bar{A}^{\nu}_{j}(K) \delta(Q+K) \qquad (\xi + \frac{(eB_0)}{M^{*2}} G^{B,1}_{v-a-\pi} i \epsilon_{12\mu\nu} M^{*} (\pi_3(Q) V^{\mu} \bar{A}^{\nu} + T_{ijk} \pi_i V^{\mu}_{j} \bar{A}^{\nu}_{k})$$

Vector- axial mixing Induced by pion

Three-meson coupling Usually considered In medium calculations Vector-axal mixing

Two-meson coupling Only possible in a medium

Or in the presence of 3rd particle

For conservation of momentum

Increase of External momenta (rho and constituent quark)

Lead to fast decrease of Gvja

$$F(K,Q;B_0) = F(K,Q) + f\frac{(eB_0)}{M^{*2}}F^B(K,Q),$$

Weak magnetic field Correction to the Axial a.q.r of the rho meson

$$\Delta_A^B \langle r_\rho^2 \rangle \sim \frac{\Delta_A \langle r_\rho^2 \rangle}{10}.$$

$$\Delta_A < r_\rho^2 > \sim \frac{< r_\rho^2 >}{10}$$

at
$$M^* \sim 0.35 \text{GeV}$$

Calculation with same grounds as the vector - NJL model

Expansion of quark determinant With a background photon field:

This also suggests vector meson dominance: (VMD) different MIXING couplings between rho/omega and the photon

Quadratic terms

Thomas,Coon, Biswas, McNamee, Krein, Schildknecht, O'Connel, and other

$$\mathcal{L}_{\text{VMD}} = -g_{\rho A} V_3^{\mu} A_{\mu} - g_{\omega A} V_{\mu} A^{\mu} - g_{F \rho} \mathcal{F}_{\mu \nu}^3 F^{\mu \nu} - g_{F \omega} \mathcal{F}_{\mu \nu} F^{\mu \nu},$$
$$g_{\rho A} = 3g_{\omega A}:$$

$$g_{F\rho} = 3g_{F\omega}$$

This procedure eliminates The photon mass from expansion of determinant And the non gauge invariant VMD couplings FLB, JPG (2020) Kroll, B. Lee, Zumino

To redefine **the fields** It restores gauge invariance

$$A_{\mu}=c ilde{A}_{\mu}, \qquad V^3_{\mu}= ilde{V}^3_{\mu}+rac{ce}{2f_{
m v}} ilde{A}_{\mu}, \qquad V_{\mu}= ilde{V}_{\mu}+rac{ce}{6f_{
m v}} ilde{A}_{\mu},$$

 $\mathcal{L}_{F} = g_{F\rho\omega}(F^{\mu\nu}_{\vee}\mathcal{F}^{3}_{\nu\rho}\mathcal{F}^{\rho}_{\mu} + F^{\mu\nu}\mathcal{G}^{3}_{\nu\rho}\mathcal{G}^{\rho}_{\mu}) - g_{FF\omega}F_{\mu\nu}F^{\nu\rho}\mathcal{F}^{\mu}_{\rho} - g_{FF\rho}F_{\mu\nu}F^{\nu\rho}\mathcal{F}^{3,\mu}_{\rho}$

VMD induced by background photon field

3rd order terms

Mechanism for Vector or axial mesons mixings

FLB, JPG 47 (2020) 115102

Leading vector mesons and photon interactions

Yield both: Vector mesons mixings and VMD

Induced by background photons

The non-explicitly U(1) gauge invariant couplings above become gauge invariant by considering leading derivative couplings.

Final remarks

The method has a starting point the QCD Lagrangian to obtain hadrons couplings

It yields many aspects of low energy (maybe intermediary energies) phenomenology With good resulting numerical values for observables

Most of constituent quark coupling constants are UV finite

Relatively weak magnetic field and photons induce anisotropic mesons couplings to quarks and among mesons

It allows directly and naturally to compute in medium effects

Hadrons Group at UFG

F.L.B. Current Graduate Students: Willian F. De Sousa João Gabriel M Mendes Igor de M. Froldi

Under grad: Davi de A. Camargos

Thank you for your attention!