



# Vector meson production at large $t$ in eA collisions

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Werner K. Sauter

werner.sauter@ufpel.edu.br

Physics Opportunities at an Electron–Ion Collider 2023

High and Medium Energy Group (GAME)

Instituto de Física e Matemática (IFM)

Universidade Federal de Pelotas

# Outline:

Introduction

Formalism

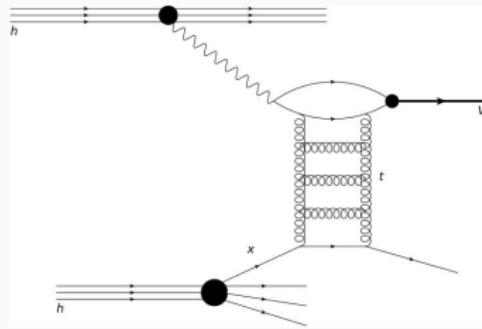
Results & Conclusions

# Introduction

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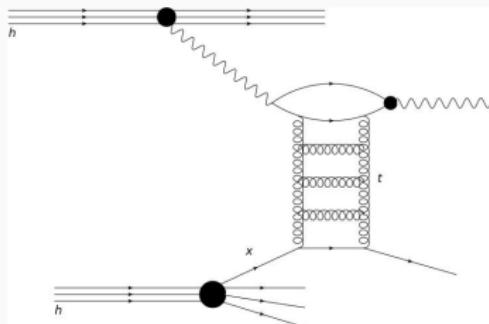
# Motivations

- Diffractive process and rapidity gaps
- Exchange of the BFKL Pomeron in high momentum transfer to study the QCD dynamics at LHC
- Diffractive production of mesons ( $\rho$ ,  $J/\psi$  and  $\Upsilon$ ) in LHC: Gonçalves, Sauter, Phys.Rev. D81 (2010) 074028, Eur.Phys.J. A47 (2011) 117, Phys. Lett B776 (2017) 424



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- Photo-production of photons. Gonçalves, Sauter, Phys.Rev. D87 (2013) 5, 054035



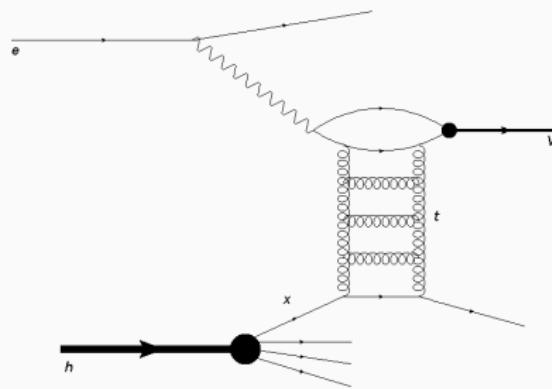
# Motivations for EIC

- Production of vector mesons as observer of QCD dynamics: linear (DGLAP/BFKL) and non-linear (BK)
- Have a clean experimental signature: more precise kinematic variable determination
- Previous measurements in HERA have a limited rapidity acceptance.
- EIC will access a new kinematic regime in  $eA$  scattering

# Motivations for EIC

## Quick calculation:

Change the projectiles to  $eA$  and use more recent nuclear PDFs



## Formalism

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## Previous

The calculation is based on

- Forshaw, Ryskin. *Z. Phys C*68, 137 (1995)
- Bartels, Forshaw, Lotter, Wüsthoff. *PLB* 375 (1996) 301
- Enberg, Motyka, Poludniowski *EPJ C*26, 219 (2002)

$J/\psi$  in  $pA$  collisions:

- Frankfurt, Strickman, Zhalov *PLB* 640(2006)162, *PLB*670 (2008) 32

More recent:

- BFKL Loops in  $J/\psi$  &  $\Upsilon$  production: Kotko, Motyka, Sadzikowski & Stašto: *JHEP07(2019)129*
- In EiC for  $e p$ : Deák, Stašto and Strickman *PRD103*, 014022 (2021)

## Cross sections

- Photo induced particle production.
- Coherent production: almost real photon
- Presence of rapidity gaps
- Large momentum transfer: dissociation of the target
- BFKL Pomeron exchange, but have a limited kinematic window

## Cross sections

The differential and total cross sections: for the diffractive particle photoproduction at large momentum transfer reads

$$\frac{d\sigma_{\gamma h \rightarrow V X}}{dt} = \int_{x_{\min}}^1 dx_j \frac{d\sigma}{dt dx_j}, \quad \sigma_{\text{tot}} = \int_{t_{\min}}^{t_{\max}} dt \frac{d\sigma_{\gamma h \rightarrow V X}}{dt}$$

where  $h$  denote a hadron,  $V$  the vector meson ( $J/\psi$ ),  $X$  the hadron fragments and

$$\frac{d\sigma}{dt dx_j} = \left[ \frac{81}{16} G(x_j, |t|) + \sum_j (q_j(x_j, |t|) + \bar{q}_j(x_j, |t|)) \right] \frac{d\hat{\sigma}}{dt}.$$

The pomeron couples with individual partons in hadron. Moreover,  $G$ ,  $q$  and  $\bar{q}$  are parton distribution functions. Previous we used CTEQ6L (for vectors) and MSTW2008LO (for photons) parton parametrization in proton–proton collisions and EKS for the ion–ion case.

# Partonic cross section

Partonic cross section for vector meson production: is given by

$$\frac{d\hat{\sigma}}{dt}(\gamma q \rightarrow Vq) = \frac{1}{16\pi} |\mathcal{A}_V(s, t)|^2.$$

Meson production:

$$\mathcal{A}_V(s, t) = \frac{2}{9\pi^2} \int d\nu \frac{\nu^2}{(\nu^2 + 1/4)^2} \left( \frac{s}{\Lambda^2} \right)^{\omega(\nu)} I_\nu^\gamma V(Q_\perp) I_\nu^{qq}(Q_\perp)^*,$$

The quantities  $I$ 's are related with the impact factors of  $\gamma \rightarrow V$  and  $q \rightarrow q$ ,

$$I_\nu^{\gamma V_i}(Q_\perp) = -C_i \alpha_s \frac{16\pi}{Q_\perp^3} \frac{\Gamma(1/2 - i\nu)}{\Gamma(1/2 + i\nu)} \left( \frac{Q_\perp^2}{4} \right)^{i\nu} \int_{1/2-i\infty}^{1/2+i\infty} \frac{du}{2\pi i} \left( \frac{Q_\perp^2}{4M_{V_i}^2} \right)^{1/2+u} \times \frac{\Gamma^2(1/2 + u)\Gamma(1/2 - u/2 - i\nu/2)\Gamma(1/2 - u/2 + i\nu/2)}{\Gamma(1/2 + u/2 - i\nu/2)\Gamma(1/2 + u/2 + i\nu/2)}.$$

The quark impact factor is given by

$$I_\nu^{qq}(Q_\perp) = -\frac{4\pi\alpha_s}{Q_\perp} \left( \frac{Q_\perp^2}{4} \right)^{i\nu} \frac{\Gamma(\frac{1}{2} - i\nu)}{\Gamma(\frac{1}{2} + i\nu)}.$$

# BFKL (LO)

**BFKL characteristic function:**

From BFKL equation:

$$\omega(v) = \bar{\alpha}_s \chi(\gamma), \quad \bar{\alpha}_s = (N_c \alpha_s)/\pi, \quad \gamma = 1/2 + iv$$

At leading order: the BFKL function  $\chi(\gamma)$  is given by

$$\chi^{\text{LO}}(\gamma) = 2\psi(1) - \psi(\gamma) - \psi(1 - \gamma)$$

where  $\psi(z)$  is the digamma function. In what follows this expression is used in our calculations of the vector meson production at large- $t$ .

## Problems in LO:

- the energy scale  $\Lambda$  is arbitrary;
- $\alpha_s$  is fixed at LO BFKL;
- the power growth with energy violates  $s$ -channel unitarity at large rapidities.

# BFKL (NLO)

Original NLO BFKL kernel obtained by Fadin, Ciafaloni:

$$\chi(\gamma) = \chi^{\text{LO}}(\gamma) + \bar{\alpha}_s \chi^{\text{NLO}}(\gamma), \quad \bar{\alpha}_s = N_c \alpha_s / \pi,$$

## Several problems:

- the choice of energy scale;
- the renormalization scheme;
- large correction;

## Alternatives:

- Brodsky, Fadin, Kim, Lipatov, Pivovarov (1999) : BLM optimal scale + MOM renormalization scheme
- Sabio-Vera (2005) *All-poles*: collinearly improved BFKL kernel characteristic function:  $\Rightarrow$  resum collinear effects

## Results & Conclusions

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# Vector mesons:<sup>1</sup>

## Strongly depend on

- coupling constant:  $\alpha_s = 0.21$
- energy scale with free parameters  $\Lambda \equiv s_0 = \beta M_V^2 + \gamma |t|$

## Calculation:

Impact factors and BFKL kernel at LO

The NLO BFKL correction is large

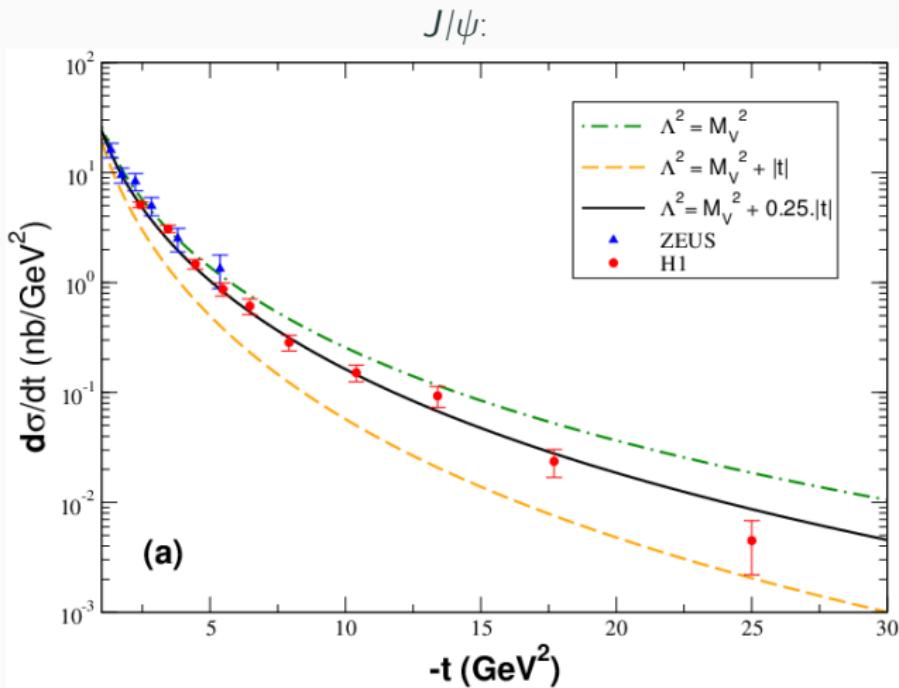
Fit to HERA data to fix the parameters

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<sup>1</sup>Gonçalves, Sauter, Phys.Rev. D81 (2010) 074028, Eur.Phys.J. A47 (2011) 117

# Vector mesons:<sup>1</sup>

$d\sigma/dt$  using to fixing the parameters (using HERA data):

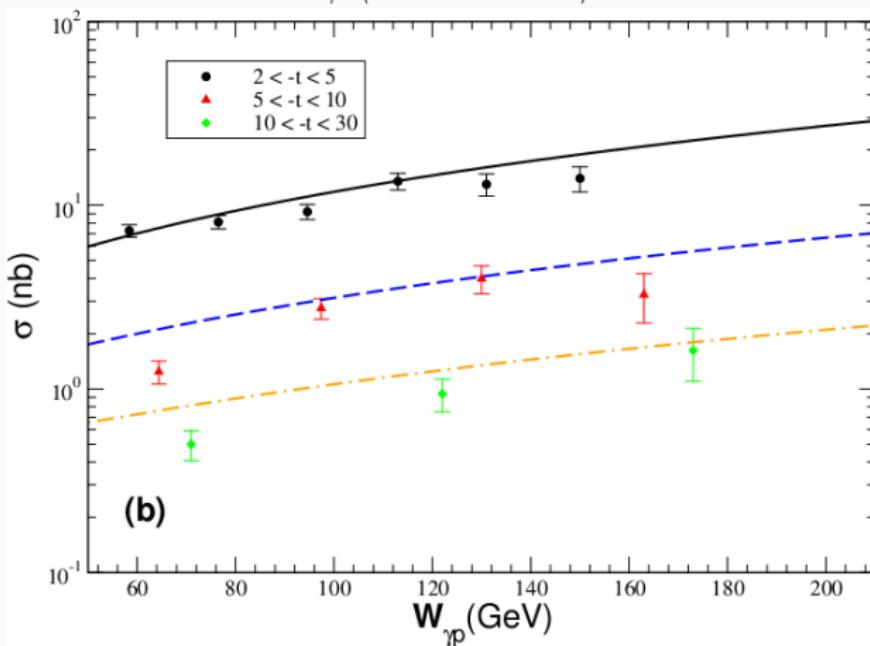


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# Vector mesons:<sup>1</sup>

$\sigma_{tot}$  with the parameters fixed:

$J/\psi$  (H1 & ZEUS03):



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# Hadronic collisions

- Cross section:

$$\frac{d\sigma [h_1 + h_2 \rightarrow h_1 \otimes Y \otimes X]}{dy} = \int_{t_{\min}}^{t_{\max}} dt \omega \frac{dN_\gamma(\omega)}{d\omega} \frac{d\sigma_{\gamma h \rightarrow YX}}{dt} (\omega)$$

- Proton photon flux (Dress *et al.*):

$$\frac{dN_\gamma^{pp}(\omega)}{d\omega} = \frac{\alpha_{em}}{2\pi\omega} \left[ 1 + \left( 1 - \frac{2\omega}{\sqrt{S_{NN}}} \right)^2 \right] \left( \ln \Omega - \frac{11}{6} + \frac{3}{\Omega} - \frac{3}{2\Omega^2} + \frac{1}{3\Omega^3} \right)$$

- Nucleus photon flux (Weissäcker/Williams):

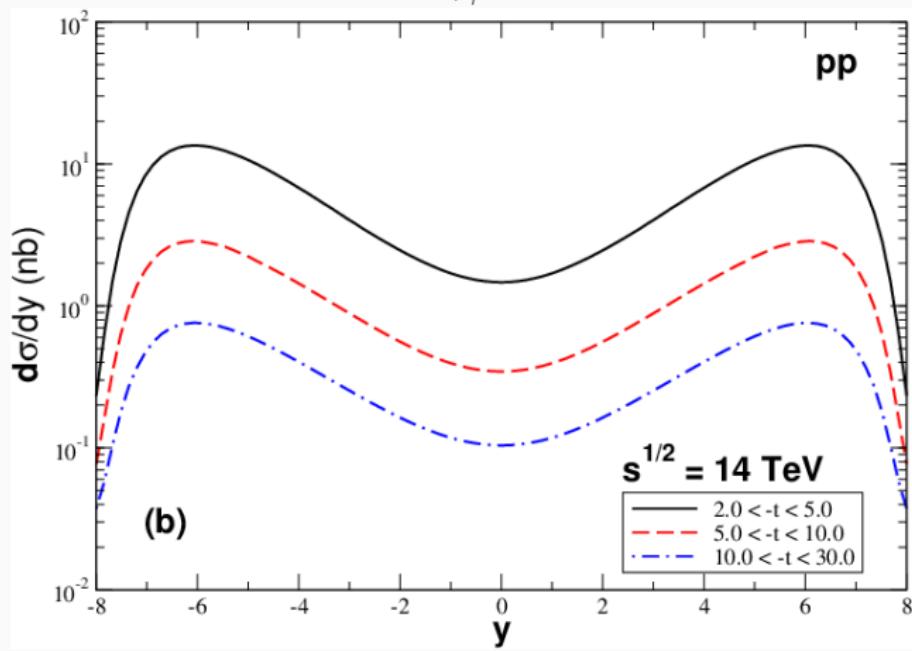
$$\frac{dN_\gamma^{AA}(\omega)}{d\omega} = \frac{2Z^2\alpha_{em}}{\pi\omega} \left[ \bar{\eta} K_0(\bar{\eta}) K_1(\bar{\eta}) - \frac{\bar{\eta}^2}{2} (K_1^2(\bar{\eta}) - K_0^2(\bar{\eta})) \right]$$

where  $\bar{\eta} = \omega(R_{h_1} + R_{h_2})/\gamma_L$

# Hadronic collisions

Using the previous parameters.

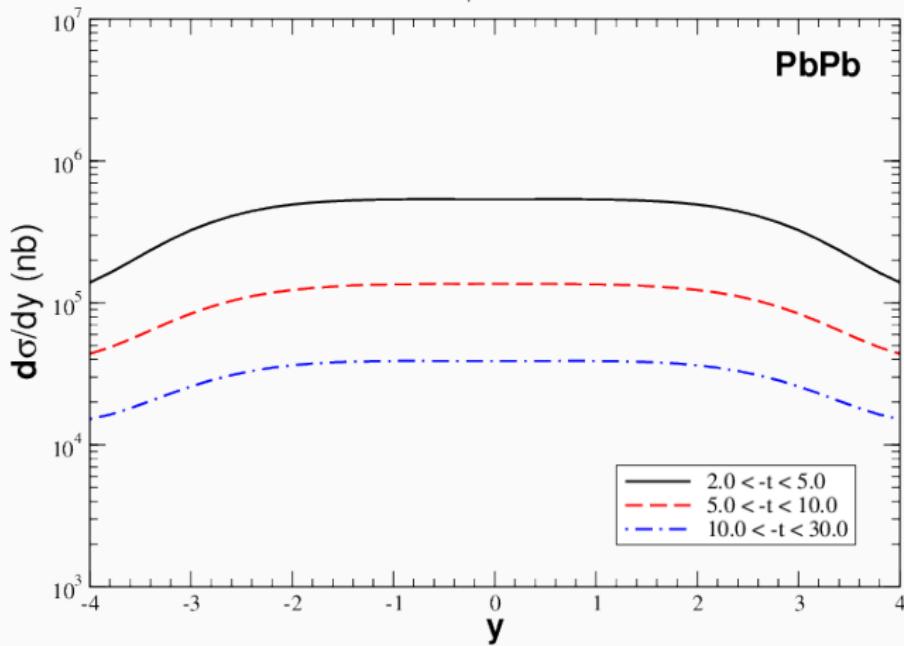
$J/\psi$ :



# Hadronic collisions

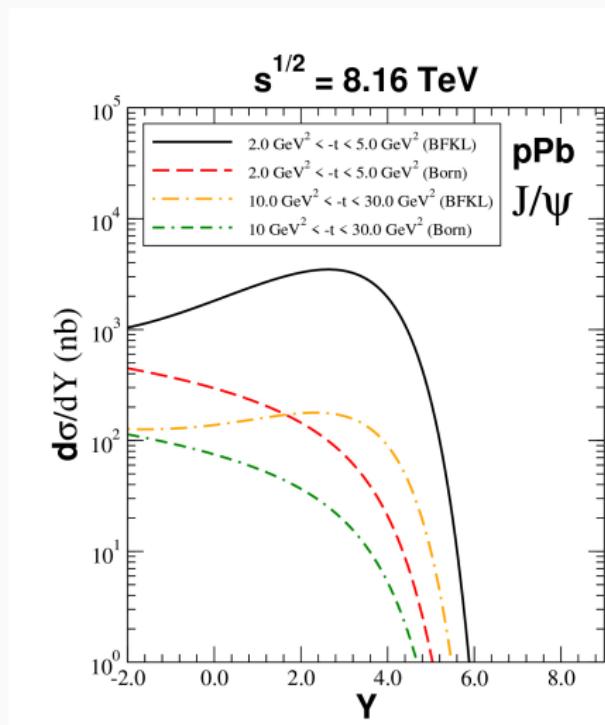
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$J/\psi$ :



# Hadronic collisions

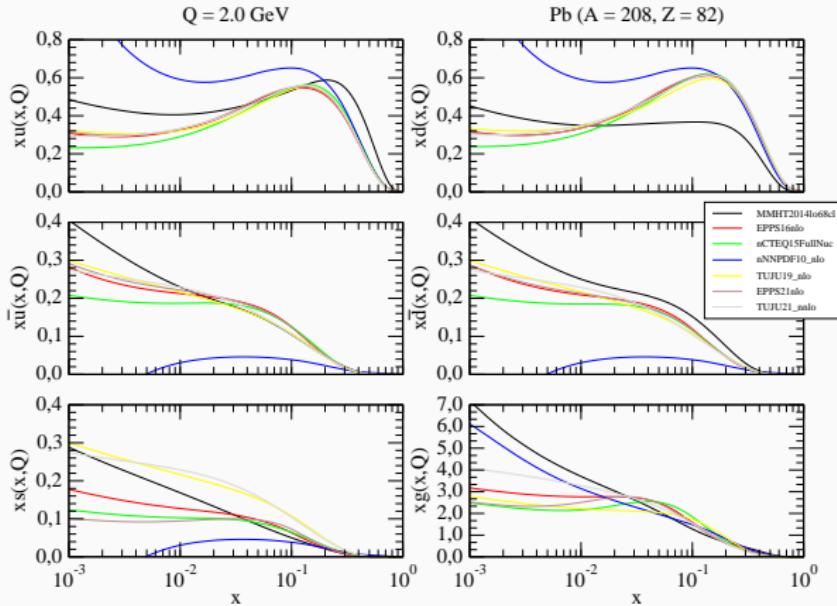
Comparison among Born level (2 gluons) and BFKL ladder:



# Electron-ion collisions

For  $eA \rightarrow eVX$  process, I perform the same calculations as  $hh$  collisions, but replacing the proton PDF by a nuclear one **and** the photon luminosity.

Using the LHAPDF interface: **EPPS21nlo**, **nCTEQ15**, **TUJU21nnlo**



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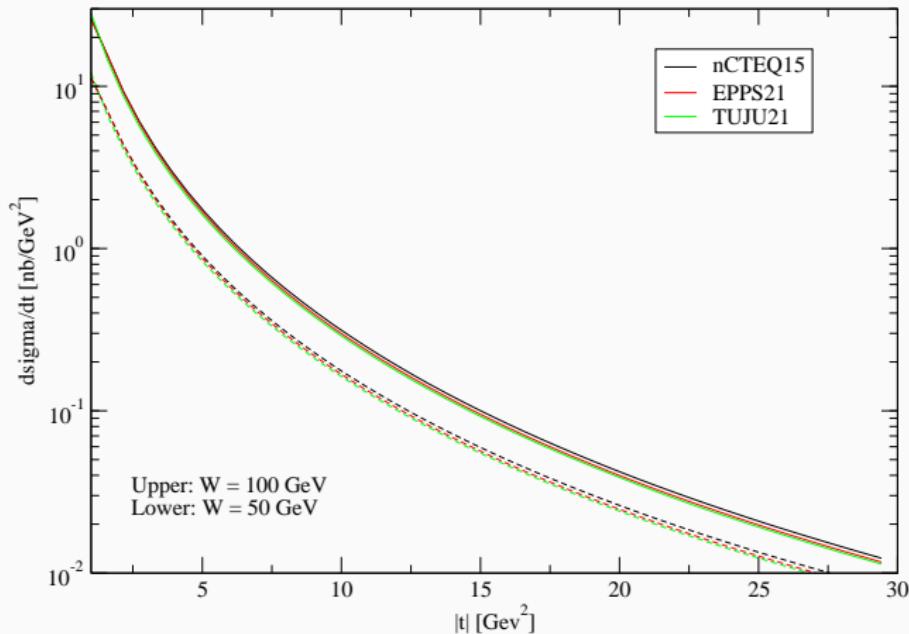
Electron photon flux (Frixione):

$$\frac{dN_\gamma(\omega)}{d\omega} = \frac{\alpha}{2\pi y} \left\{ \left[ 1 + (1-y)^2 \right] \ln \left[ \frac{Q_{\max}^2(1-y)}{m_e^2 y^2} \right] + 2 \left[ \frac{m_e^2 y^2}{Q_{\max}^2} - (1-y) \right] \right\}$$

$$y = \ln(2\omega/m_\nu), \quad Q_{\max}^2 = 4 \text{ GeV}^2$$

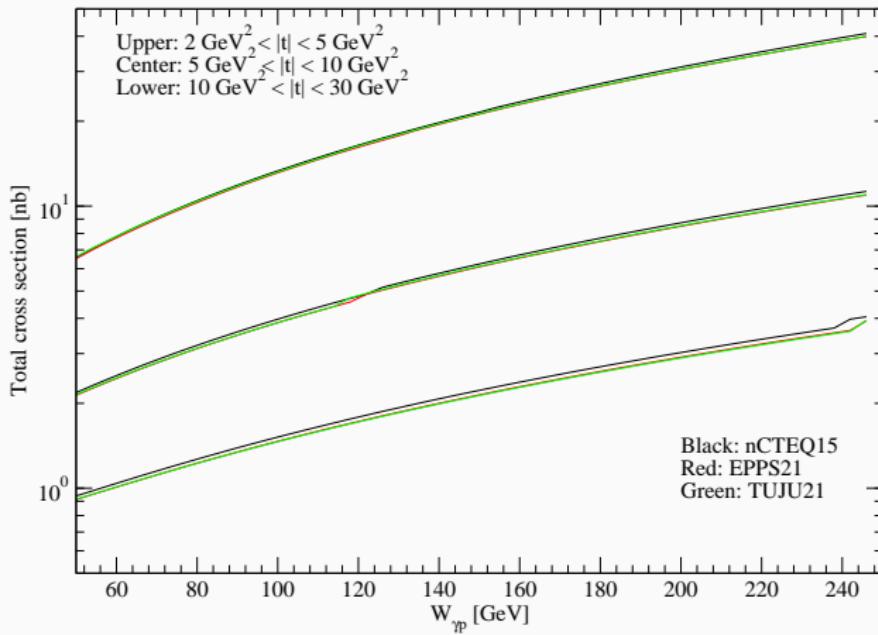
# Electron-Ion collisions: PRELIMINARY RESULTS!

Differential cross-sections: same parameters of previous calculation.



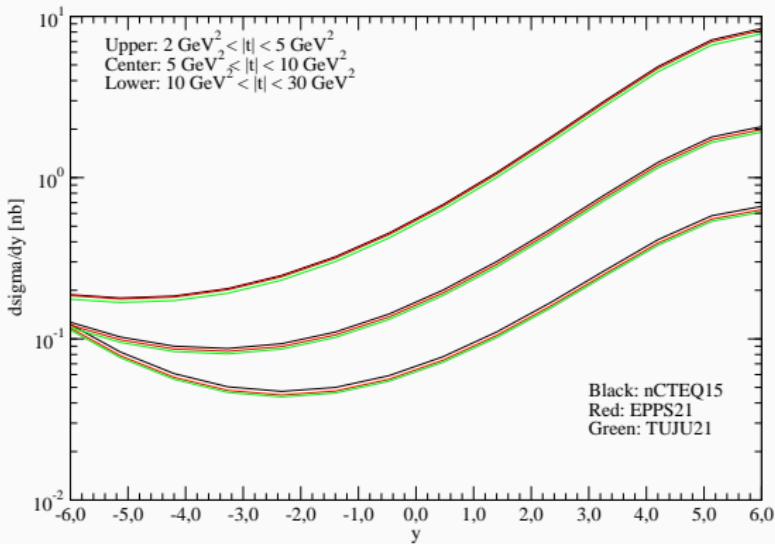
# Electron-Ion collisions: PRELIMINARY RESULTS!

Total cross sections: same  $t$  intervals as  $pp$  and  $pA$  collisions in LHC



# Electron-Ion collisions: PRELIMINARY RESULTS!

Rapidity distribution:



# Conclusions

## Our results:

1. BFKL formalism is able to describe the current experimental data of  $ep$  collisions at HERA with suitable choice of parameters
2.  $pp$  interactions at LHC  $\Rightarrow$  able to constrain the QCD dynamics
3. complementary to the recent theoretical and phenomenological studies that use NLO BFKL Pomeron as  $\gamma^*\gamma^*$ , Mueller-Navelet jets.
4. The exploratory analysis done here is useful to indicate the potentiality of this process to probe the BFKL dynamics as well as to constrain the influence of the higher order corrections

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## To do list:

Other contributions: conformal spin (small effect); NLO BFKL; Other nuclei

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**Thank you!**