



Incommensurate charge density wave vector on multiband intermetallic systems

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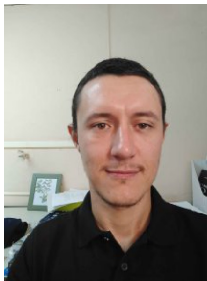
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Our results are discussed in these papers

PHYSICAL REVIEW B **107**, 205141 (2023)

Incommensurate charge density wave in multiband intermetallic systems exhibiting competing orders

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PHYSICAL REVIEW B **103**, 195150 (2021)

Interplay between charge density wave and superconductivity in multiband systems with interband Coulomb interaction

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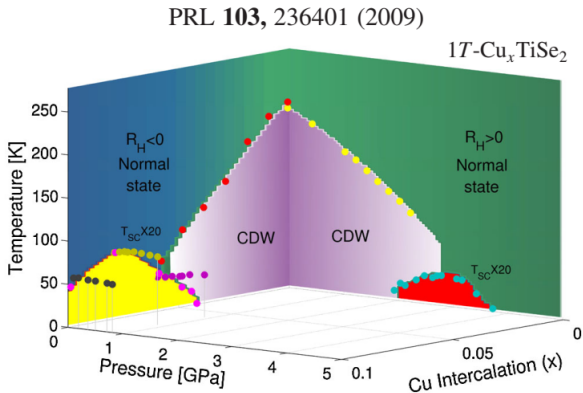
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OVERVIEW

- ▶ Experimental motivation: charge density orders and superconductivity in transition - metal dichalcogenides (TMDs)
- ▶ Some previous theoretical works
- ▶ Hamiltonian model and formalism
- ▶ Results
- ▶ Conclusions

CDW x SC: EXPERIMENTAL MOTIVATION

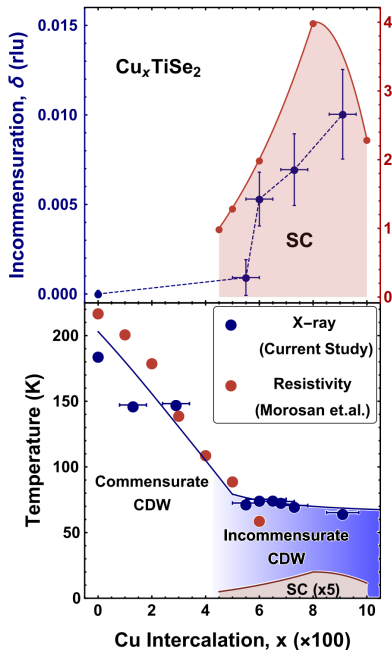
- ▶ Pressure and Cu intercalation induce superconductivity in pristine $1T\text{-Cu}_x\text{TiSe}_2$



CDW - INCDW x SC: EXPERIMENTAL MOTIVATION

Observation of a charge density wave incommensuration near the superconducting dome in Cu_xTiSe_2

A. Kogar *et al.* Phys. Rev. Lett. **118**, 027002 (2017)



SOME PREVIOUS WORKS

- ▶ Theoretical models considering **electronic origin** for CDW order, **without superconductivity**

PHYSICAL REVIEW B **72**, 125122 (2005)

Competing orderings in an extended Falicov-Kimball model

$$\mathcal{H} = -t \sum_{\langle i,j \rangle} d_i^\dagger d_j + \epsilon_f \sum_j n_j^f + \sum_{i,j} (V_{ij} d_i^\dagger f_j + \text{H.c.}) + U \sum_j n_j^d n_j^f.$$

PHYSICAL REVIEW B **77**, 155130 (2008)

Hartree-Fock study of electronic ferroelectricity in the Falicov-Kimball model with f - f hopping

$$H = -t_d \sum_{\langle ij \rangle} d_i^\dagger d_j - t_f \sum_{\langle ij \rangle} f_i^\dagger f_j + U \sum_i f_i^\dagger f_i d_i^\dagger d_i + E_f \sum_i f_i^\dagger f_i,$$

P. M. R. Brydon *et al.*, PRB **72**, 125122 (2005)

P. Farkasovsky PRB **77**, 155130 (2008)

Hamiltonian: two-band model and formalism (Our model generalizes previous works)

$$\begin{aligned} H = & -t_c \sum_{\langle ij \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + \text{H.c.}) - t_d \sum_{\langle ij \rangle, \sigma} (d_{i\sigma}^\dagger d_{j\sigma} + \text{H.c.}) \\ & + \epsilon_{d0} \sum_{i, \sigma} d_{i\sigma}^\dagger d_{i\sigma} - \mu \sum_{i, \sigma} (d_{i\sigma}^\dagger d_{i\sigma} + c_{i\sigma}^\dagger c_{i\sigma}) \\ & + \sum_{i, \sigma} V_{ij} (c_{i\sigma}^\dagger d_{j\sigma} + d_{i\sigma}^\dagger c_{j\sigma}) \\ & + U_{dc} \sum_i n_i^d n_i^c + J_d \sum_i d_{i\uparrow}^\dagger d_{i\uparrow} d_{i\downarrow}^\dagger d_{i\downarrow}, \end{aligned}$$

where $c_{i\sigma}$ ($c_{i\sigma}^\dagger$) and $d_{i\sigma}$ ($d_{i\sigma}^\dagger$) denote annihilation (creation) operators of c - and d -electrons, respectively, in a given site i , with spin σ , in the standard second quantization formalism.

Some parameters of the model

$$\langle n_i^c \rangle = n^c + \delta^c \cos(\mathbf{Q} \cdot \mathbf{R}_i),$$

$$\langle n_i^d \rangle = n^d + \delta^d \cos(\mathbf{Q} \cdot \mathbf{R}_i),$$

- ▶ δ^c and $\delta^d \rightarrow$ **CDW/inCDW order parameters.**

$$\delta^c = \frac{1}{N} \sum_{\mathbf{k}}' \left(\langle c_{\mathbf{k}+\mathbf{Q}\sigma}^\dagger c_{\mathbf{k}\sigma} \rangle + \langle c_{\mathbf{k}\sigma}^\dagger c_{\mathbf{k}+\mathbf{Q}\sigma} \rangle \right)$$

- ▶ $\mathbf{Q} = (Q_x, Q_y)$ is the modulation wave vector.
- ▶ **Considering non-magnetic state**

$$\langle n_{\uparrow}^{d(c)} \rangle = \langle n_{\downarrow}^{d(c)} \rangle.$$

- ▶ **Superconducting order parameter**

$$\Delta_{\mathbf{k}}^d \equiv J_d \langle d_{-\mathbf{k}\downarrow} d_{\mathbf{k}\uparrow} \rangle$$

The matrix Hamiltonian

$H_{MF} = \sum_{\mathbf{k}} \Psi_{\mathbf{k}}^\dagger M \Psi_{\mathbf{k}} + \mathcal{C}$, using the Nambu's spinor basis,

$$\Psi^\dagger = \left(c_{\mathbf{k}\uparrow}^\dagger, c_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger, d_{\mathbf{k}\uparrow}^\dagger, d_{\mathbf{k}+\mathbf{Q}\uparrow}^\dagger, c_{-\mathbf{k}\downarrow}, c_{-\mathbf{k}-\mathbf{Q}\downarrow}, d_{-\mathbf{k}\downarrow}, d_{-\mathbf{k}-\mathbf{Q}\downarrow} \right),$$

$M =$

$$\begin{pmatrix} \epsilon_{\mathbf{k}}^c & U_{dc}\delta^d & V_{\mathbf{k}} & 0 & 0 & 0 & 0 & 0 \\ U_{dc}\delta^d & \epsilon_{\mathbf{k}+\mathbf{Q}}^c & 0 & V_{\mathbf{k}+\mathbf{Q}} & 0 & 0 & 0 & 0 \\ V_{\mathbf{k}}^* & 0 & \epsilon_{\mathbf{k}}^d & U_{dc}\delta^c & 0 & 0 & \Delta_{\mathbf{k}}^d & 0 \\ 0 & V_{\mathbf{k}+\mathbf{Q}}^* & U_{dc}\delta^c & \epsilon_{\mathbf{k}+\mathbf{Q}}^d & 0 & 0 & 0 & \Delta_{\mathbf{k}+\mathbf{Q}}^d \\ 0 & 0 & 0 & 0 & -\epsilon_{-\mathbf{k}}^c & -U_{dc}\delta^d & -V_{-\mathbf{k}}^* & 0 \\ 0 & 0 & 0 & 0 & -U_{dc}\delta^d & -\epsilon_{-\mathbf{k}-\mathbf{Q}}^c & 0 & -V_{-\mathbf{k}-\mathbf{Q}}^* \\ 0 & 0 & \Delta_{-\mathbf{k}}^{d*} & 0 & -V_{-\mathbf{k}} & 0 & -\epsilon_{-\mathbf{k}}^d & -U_{dc}\delta^c \\ 0 & 0 & 0 & \Delta_{-\mathbf{k}-\mathbf{Q}}^{d*} & 0 & -V_{-\mathbf{k}-\mathbf{Q}} & -U_{dc}\delta^c & -\epsilon_{-\mathbf{k}-\mathbf{Q}}^d \end{pmatrix}$$

$$\epsilon_{\mathbf{k}} = -2t_c [\cos(k_x a) + \cos(k_y a)], \quad \epsilon_{\mathbf{k}}^c \equiv \epsilon_{\mathbf{k}} + U_{dc}n^d - \mu,$$

$$\epsilon_{\mathbf{k}}^d \equiv \gamma\epsilon_{\mathbf{k}} + U_{dc}n^c - \mu + \epsilon_{d0}, \quad \gamma = t_d/t_c$$

ϵ_{d0} is the relative depth between the centers of the bands.

Bogoliubov - de Gennes transformation

$$H_{\text{diag}} = \sum_{\mathbf{k}}' \sum_{m=1,2,3,4} E_{m\mathbf{k}} \left(\alpha_{m\mathbf{k}}^\dagger \alpha_{m\mathbf{k}} + \beta_{m\mathbf{k}}^\dagger \beta_{m\mathbf{k}} \right) + \mathcal{C},$$

where $(\alpha, \beta)_{m\mathbf{k}}^\dagger$ and $(\alpha, \beta)_{m\mathbf{k}}$ are new operators given by a linear combination of the original band operators $(c, d)^\dagger$ and (c, d) .

The free energy density is calculated as follows

$$F = -2T \sum_{\mathbf{k}}' \sum_m \ln [1 + \exp(-\beta E_{m\mathbf{k}})] + \mathcal{C},$$

where $\beta = 1/(k_B T)$. We emphasize that we consider both incommensurate and commensurate periodic modulations of the crystal lattice with $\mathbf{Q} = (Q_x, Q_y)$.

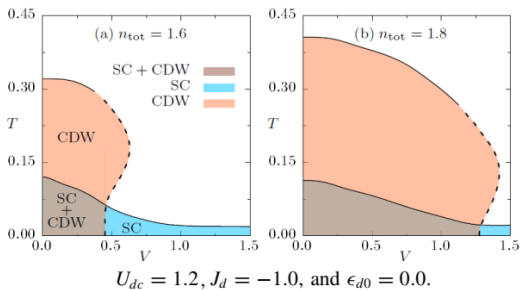
$$\frac{\partial F}{\partial \mu} = \frac{\partial F}{\partial n^d} = \frac{\partial F}{\partial \delta^d} = \frac{\partial F}{\partial \delta^c} = \frac{\partial F}{\partial \Delta^d} = \frac{\partial F}{\partial Q_x} = \frac{\partial F}{\partial Q_y} = 0.$$

RESULTS

Commensurate modulation: $\mathbf{Q} = \left(\frac{\pi}{a}, \frac{\pi}{a}\right)$

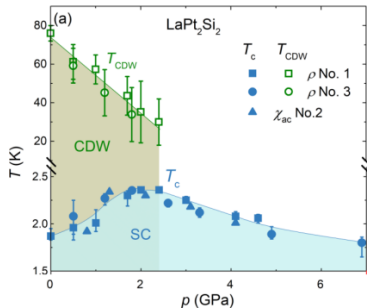
- ▶ Comparing our results with an experimental phase diagram

Physical Review B **103**, 195150 (2021)



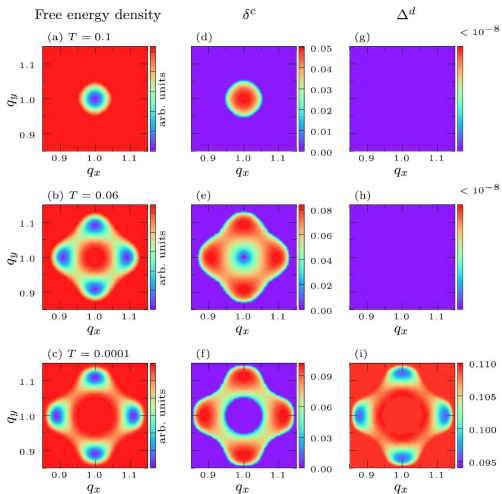
NL, DR, MC, CT, PRB **103**, 195150 (2021)

PHYSICAL REVIEW B **101**, 144501 (2020)



RESULTS

Is the stable solution a mixing phase for SC + inCDW?



$$n_{\text{tot}} = 1.6, V = 0.5, J = -1.0, \\ \epsilon_{d0} = 0.0, U_{dc} = 1.2$$

$$q_x = Q_x / \pi$$

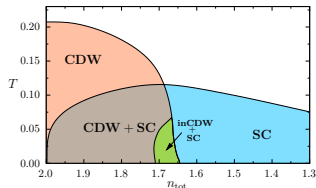
$$q_y = Q_y / \pi$$

For inCDW

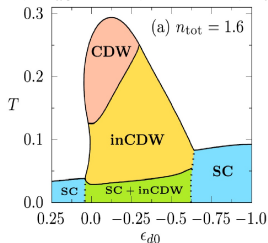
$$\mathbf{Q} = (Q_x, \pi) \equiv (\pi, Q_y)$$

RESULTS

$T \times n_{tot}$ and $T \times \epsilon_{d0}$ phase diagram

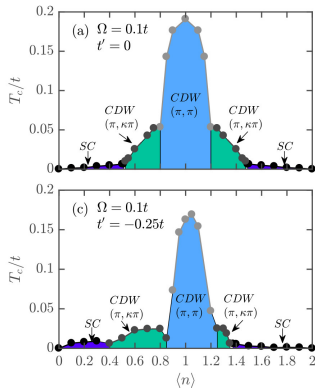


$J = -1.0, U_{dc} = 0.8, V = 0.0, \epsilon_{d0} = 0.0$



$J = -1.0, U_{dc} = 1.2, V = 0.5$

NL, DR, NC, MC, CT, PRB **107**, 205141
(2023)



Comparing with one band model interacting via e-ph.
P.M. Dee *et al.* PRB **99**, 024514 (2019)

CONCLUSIONS

- ▶ After analyzing the free energy density, we discovered that under certain parameter conditions, an **incommensurate CDW** emerges at low temperatures and can coexist with superconductivity.
- ▶ **Away from half-filling**, our findings align qualitatively with previously reported results observed in compounds that undergo a discontinuous disappearance of the CDW transition, indicating a first-order phase transition.
- ▶ Besides these findings, we have obtained diverse phase diagrams using our model. For instance, **hybridization and Coulomb repulsion as a function of band filling**, among others.