

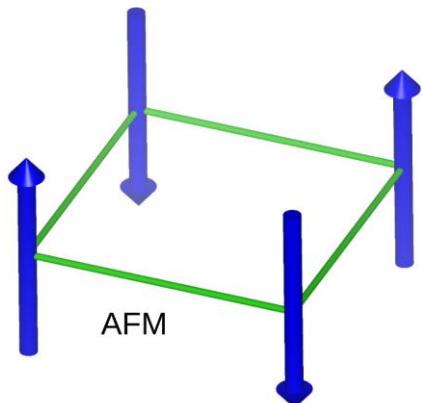
# Structural disorder and magnetic properties of geometrically frustrated magnets

Rafael Sá de Freitas

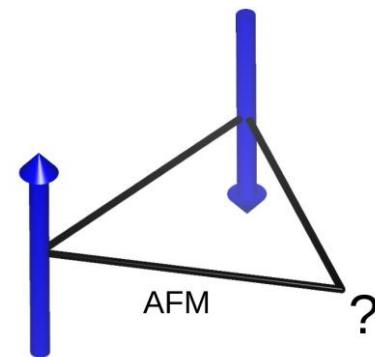
Dep. Física dos Materiais e Mecânica  
IF - USP

# Magnetic Frustration

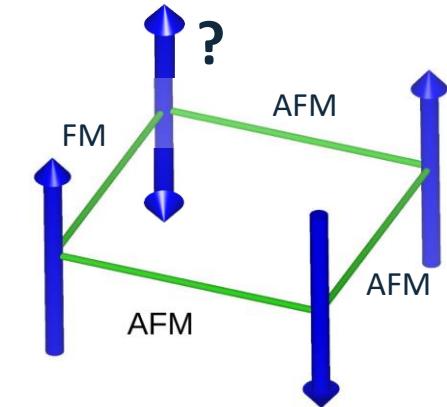
No Frustration



Geometrical Frustration

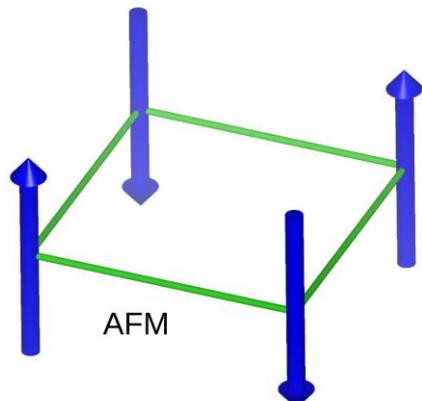


Bond Frustration

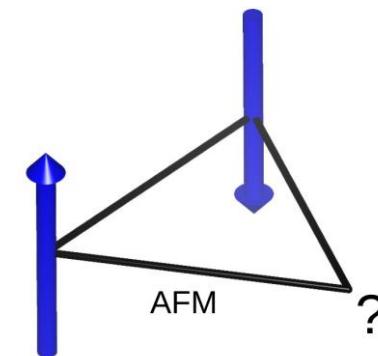


# Magnetic Frustration

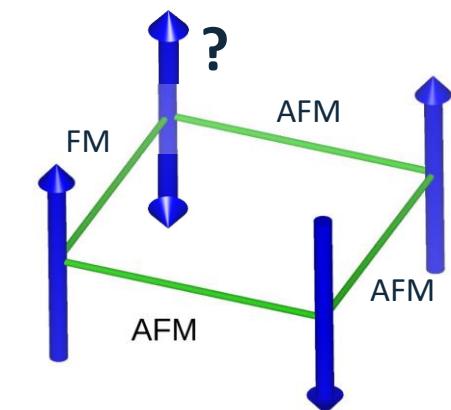
No Frustration



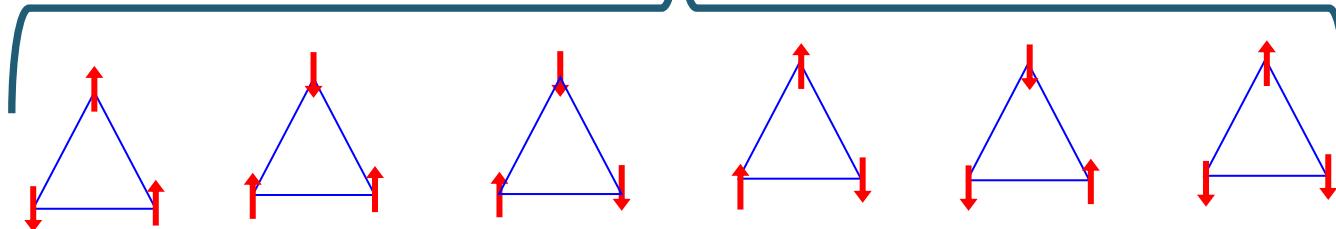
Geometrical Frustration



Bond Frustration

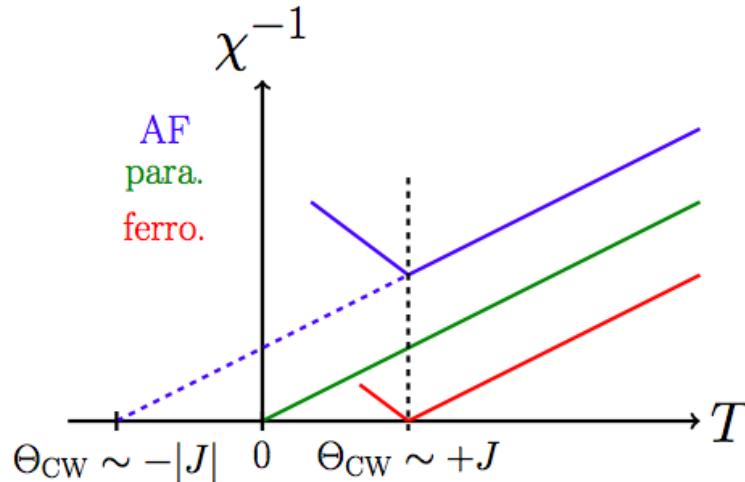


Ground State Degeneracy

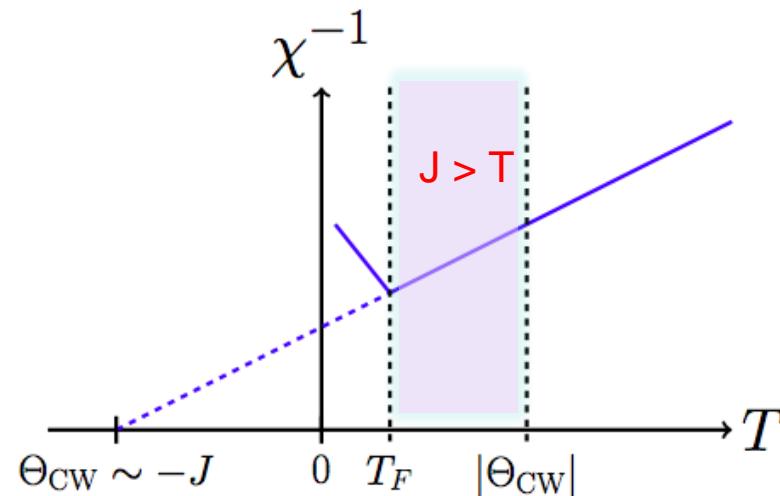


# Magnetic Frustration

Curie-Weiss Law:  $\chi^{-1} = \frac{T - \Theta_{CW}}{C}$ ,  $T \gg \Theta_{CW}$

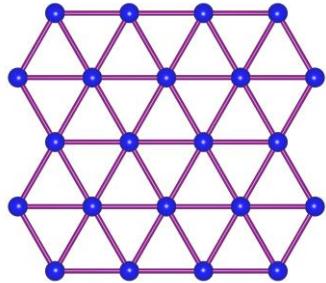


No Frustration  $\rightarrow$  LRO at  $\Theta_{CW}$

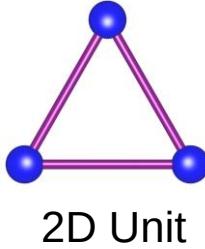


Frustration index:  $f = |\Theta_{CW}| / T_F$

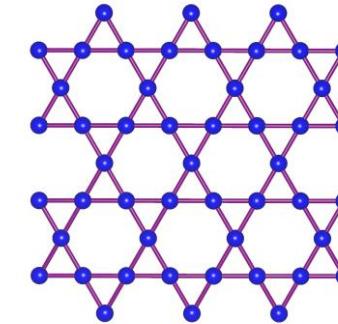
# Frustrated Lattices



Triangular

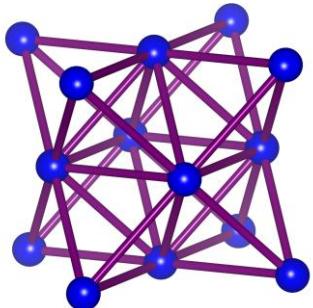


2D Unit

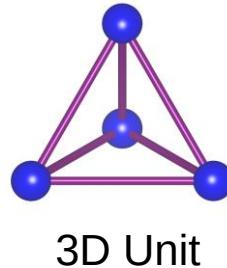


Kagome

Edge-Sharing

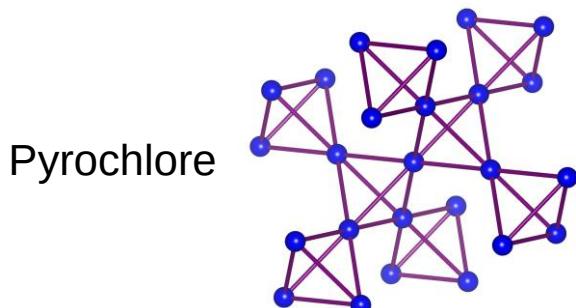


FCC



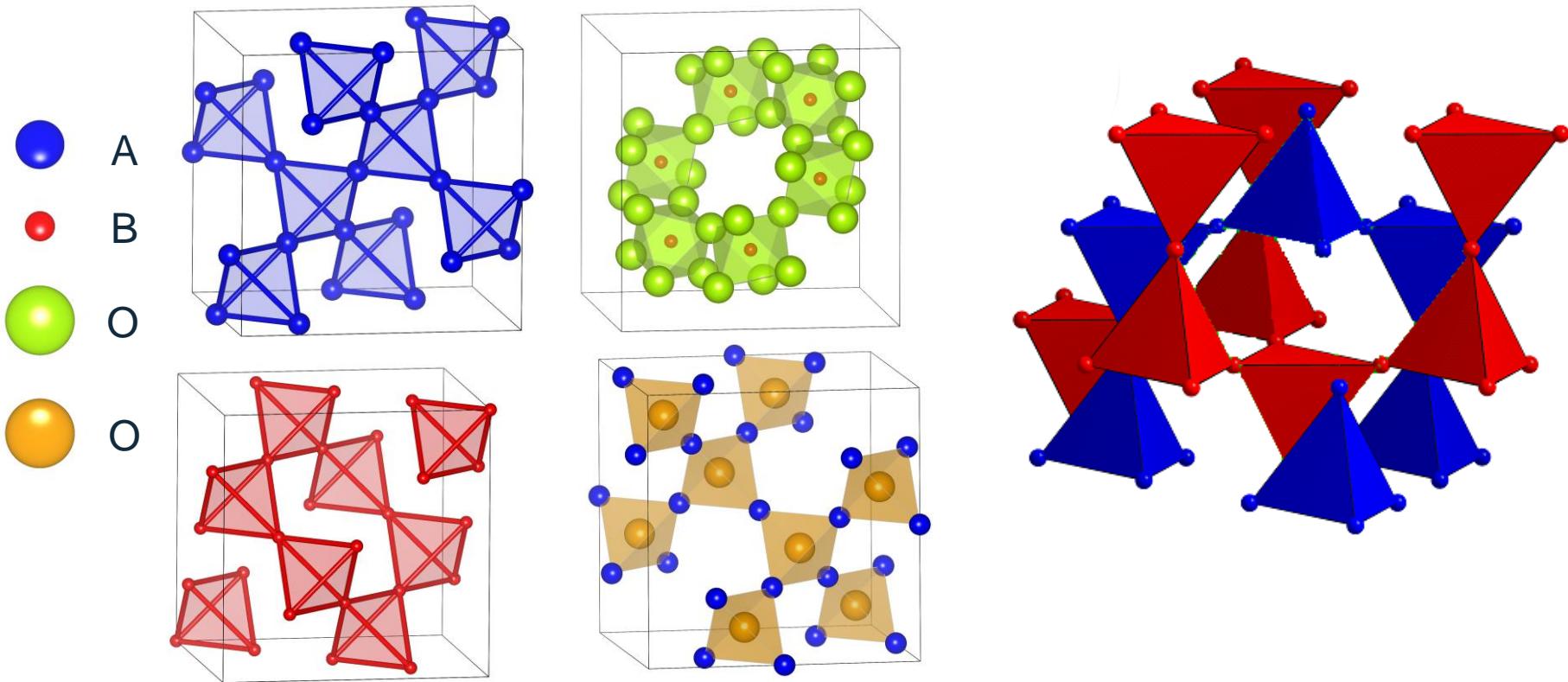
3D Unit

Vertex-Sharing



Pyrochlore

# Pyrochlore Lattice



# Pyrochlore Oxides

H				A <sup>3+</sup>															He
Li	Be				B <sup>4+</sup>														Ne
Na	Mg																		Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br		Kr	
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I		Xe	
Cs	Ba		Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At		Rn	
Fr	Ra		Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og		

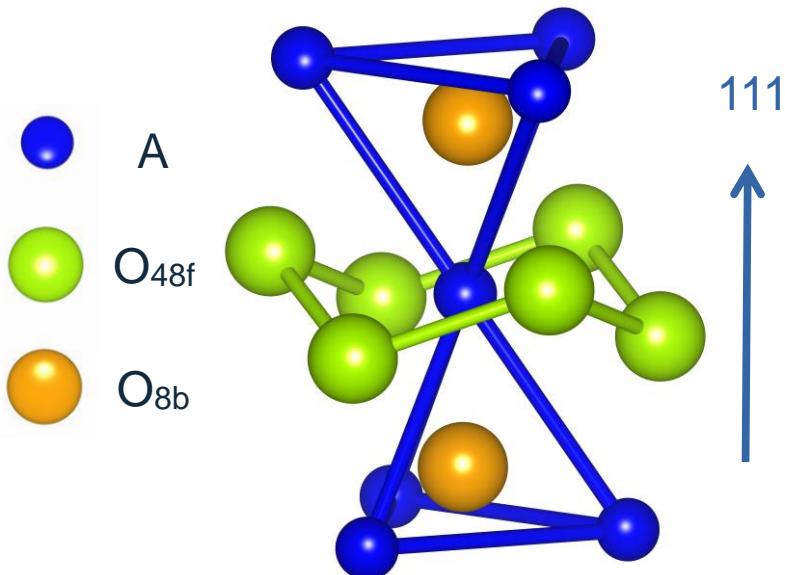
La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu				
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr				

# Pyrochlore Oxides

H				A <sup>3+</sup>															He
Li	Be				B <sup>4+</sup>														Ne
Na	Mg																		Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br		Kr	
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I		Xe	
Cs	Ba		Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At		Rn	
Fr	Ra		Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og		

La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu				
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr				

# Pyrochlore Magnetism



## CEF ANISOTROPY

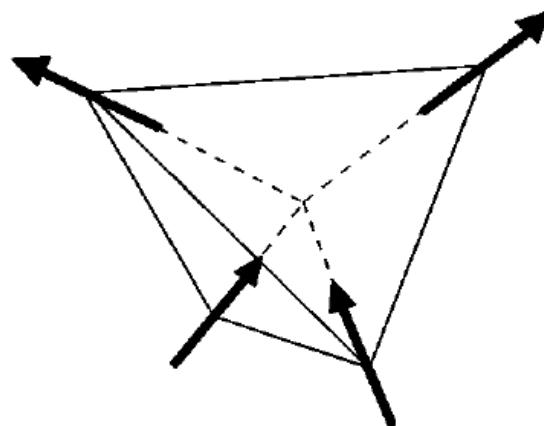
- Gd → isotropic (Heisenberg)  
Tb, Ho, Dy → easy-axis (Ising)  
Er, Yb → easy-plane (xy)

# Spin Ice

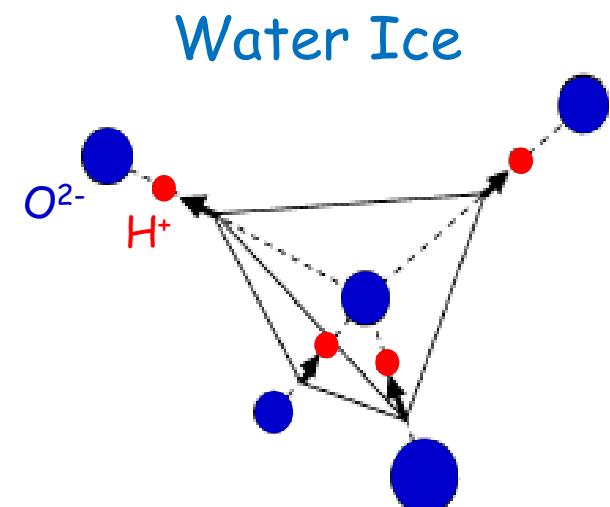
Strong Anisotropy

Ferromagnetic Interaction  $J_{FM} \sim 2K$

Spin Ices:  $Dy_2Ti_2O_7$ ,  $Ho_2Ti_2O_7$



"2 in-2 out" Ice Rules

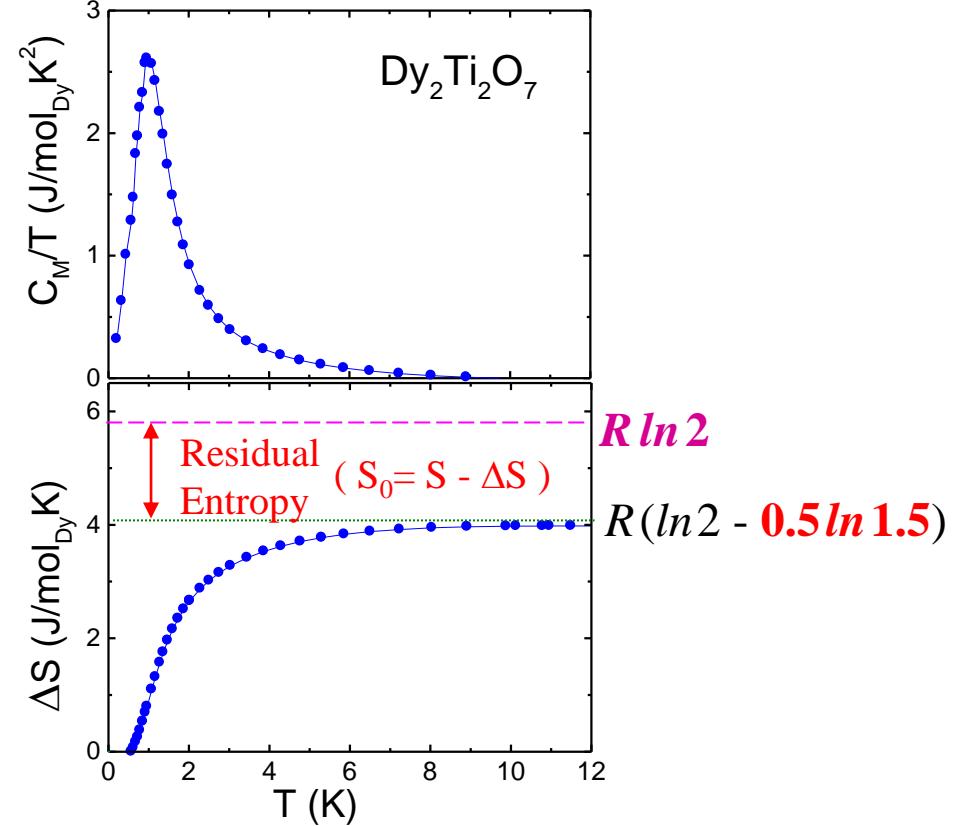


M. J. Harris et al. Phys. Rev. Lett. 79, 2554 (1997)

J. D. Bernal and R. H. Fowler J. Chem. Phys. 1, 515 (1933)

# Spin Ice

## Specific Heat



A.P. Ramirez et al., Nature 399, 333 (1999)

*Pauling's estimation for ice:*

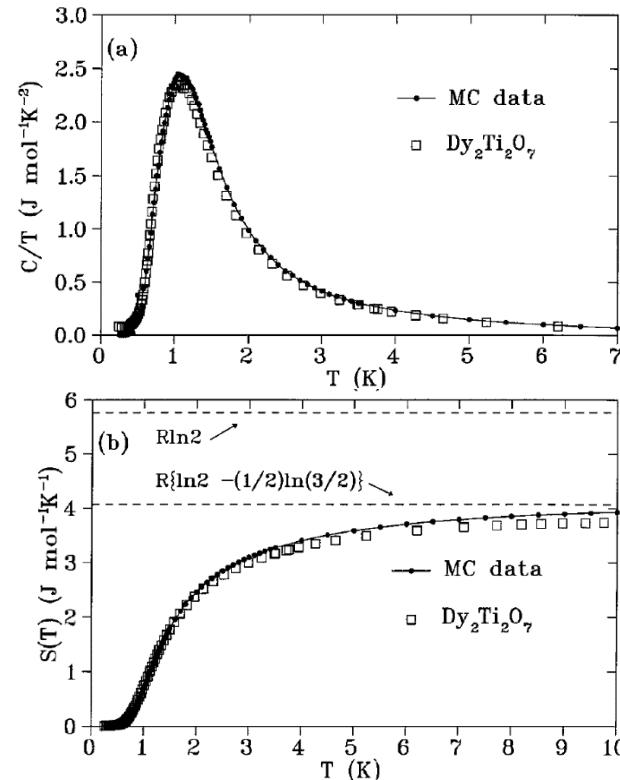
$$S_0 = K_B \ln \left\{ 2^N \left( \frac{6}{16} \right)^{N/2} \right\}$$

$$S_0 = 0.5 R \ln 1.5$$

L. Pauling, *J. Am. Chem. Soc.* **57**, 2680 (1935).

# Dipolar Spin Ice Model

Specific heat  $\text{Dy}_2\text{Ti}_2\text{O}_7$

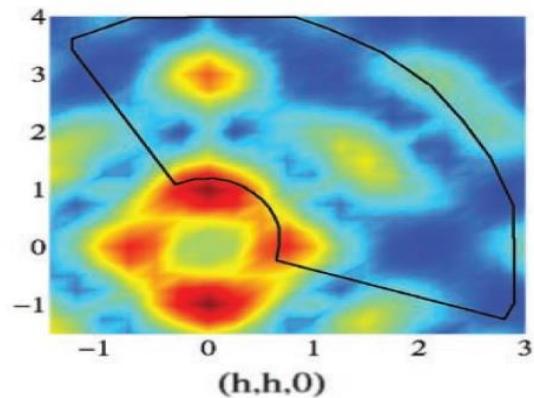


B.C. den Hertog et al. Phys. Rev. Lett. (2000)

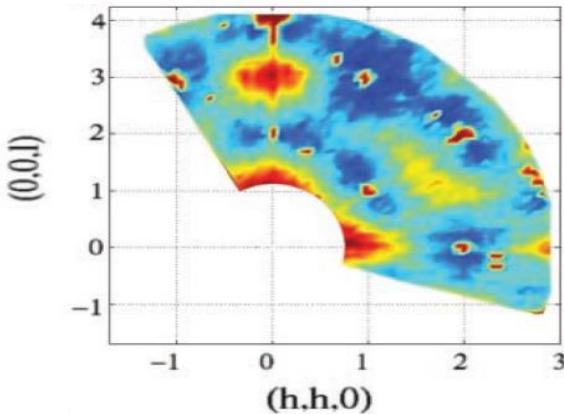
$$\mathcal{H} = -J \sum_{(ij)} \mathbf{S}_i \cdot \mathbf{S}_j + D r_{nn}^3 \sum_{i>j} \left[ \frac{\mathbf{S}_i \cdot \mathbf{S}_j}{|\mathbf{r}_{ij}|^3} - \frac{3(\mathbf{S}_i \cdot \mathbf{r}_{ij})(\mathbf{S}_j \cdot \mathbf{r}_{ij})}{|\mathbf{r}_{ij}|^5} \right]$$

Neutron Scattering  $\text{Ho}_2\text{Ti}_2\text{O}_7$

Theory



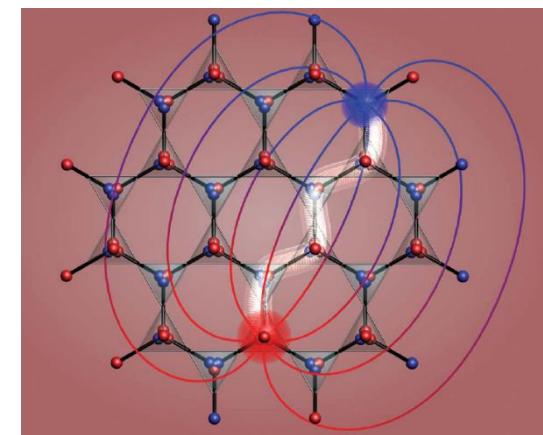
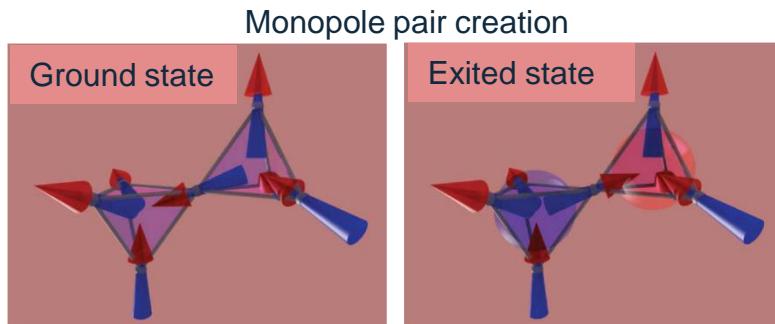
Experiment



S. T. Bramwell et al. Phys. Rev. Lett. (2001)

T. Yavors'kii et al. Phys. Rev. Lett. (2008)

# Spin Ice: A Coulomb Spin Liquid (or glass)



$$V(r_{ij}) = \frac{\mu_0}{4\pi} \frac{q_i q_j}{r_{ij}}$$

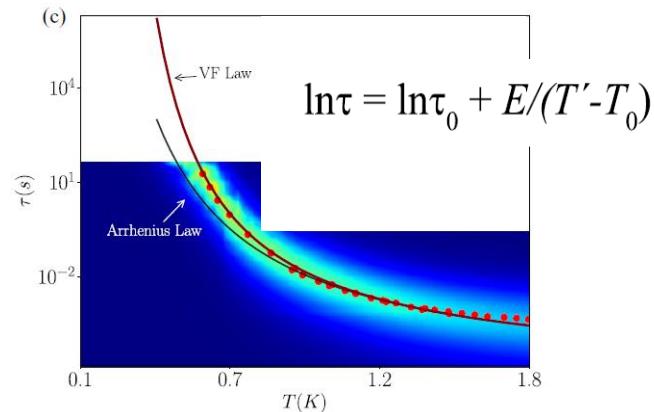
C. Castelnovo et al., Nature 451, 42 (2008)

Spin Dynamics  $\rightarrow$  Motion of Monopoles  
Monopoles increasingly sparse upon cooling.

Cooperative and  
Memory Effects

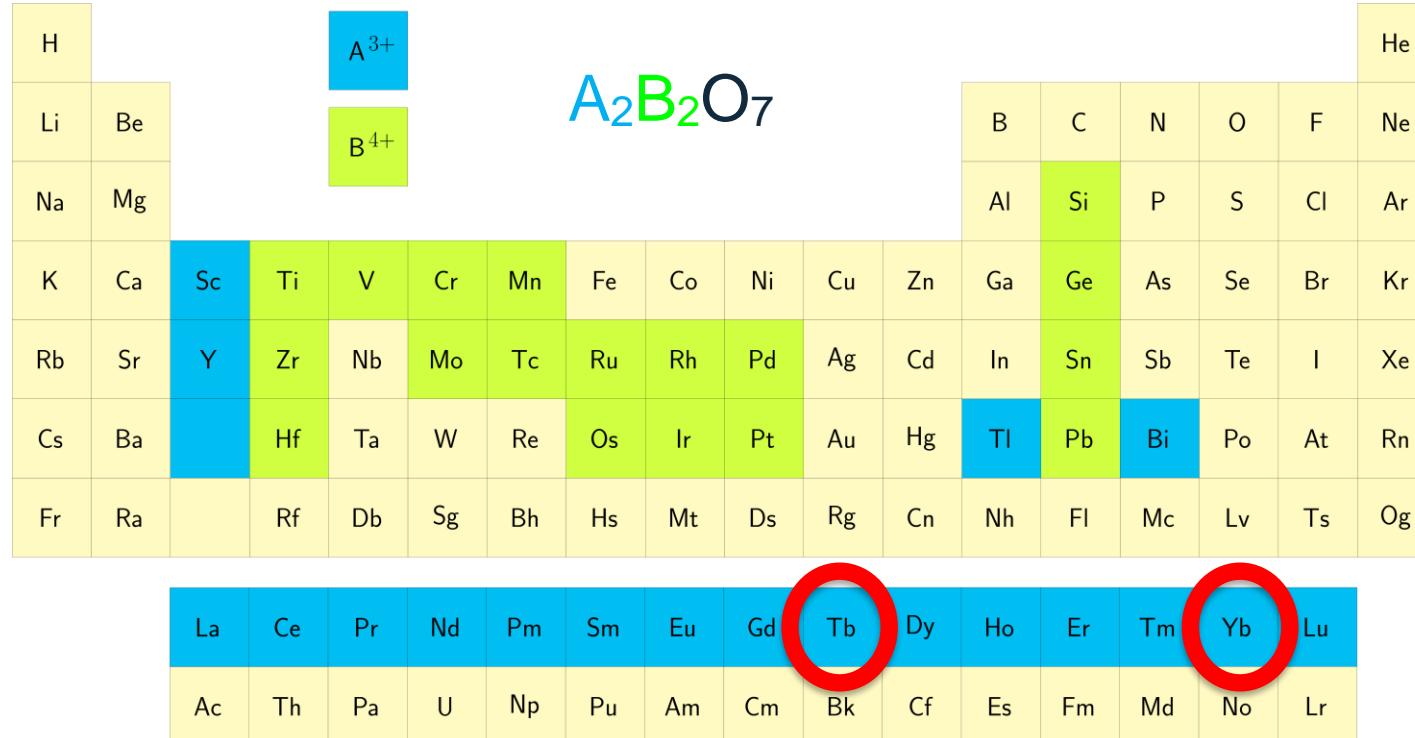
No Evident  
Intrinsic Disorder

Structural magnetic glass



DOI: 10.1103/PhysRevResearch.4.033159 - PNAS 119, e2117453119 (2022)

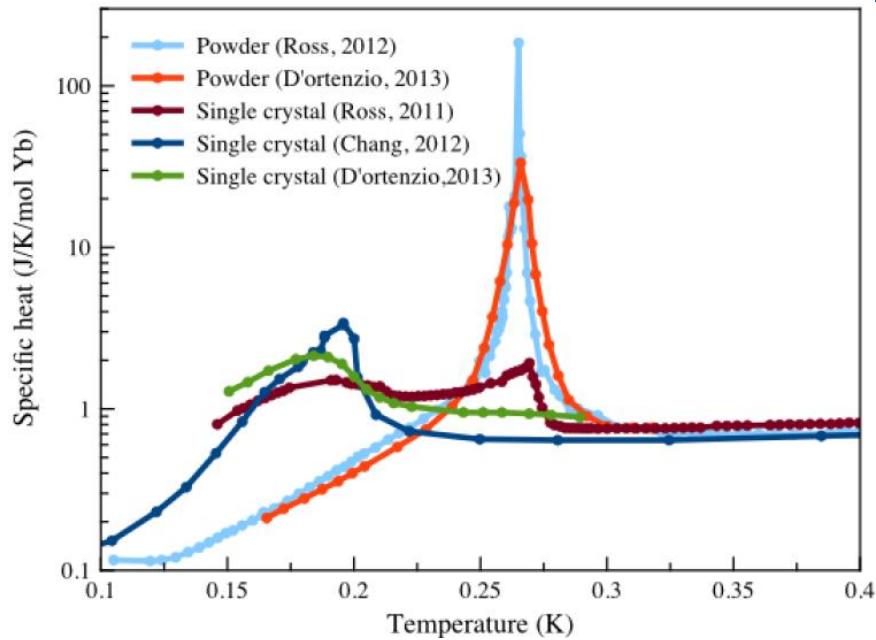
# Pyrochlore Oxides



$A_2B_2O_7$

H																				He
Li	Be																			Ne
Na	Mg																			Ar
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br				Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I				Xe
Cs	Ba		Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At				Rn
Fr	Ra		Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og			
La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu						
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr						

## Signature of spin liquid physics



Continuum of spin excitations which condense into sharp coherent spin waves in a small applied magnetic field

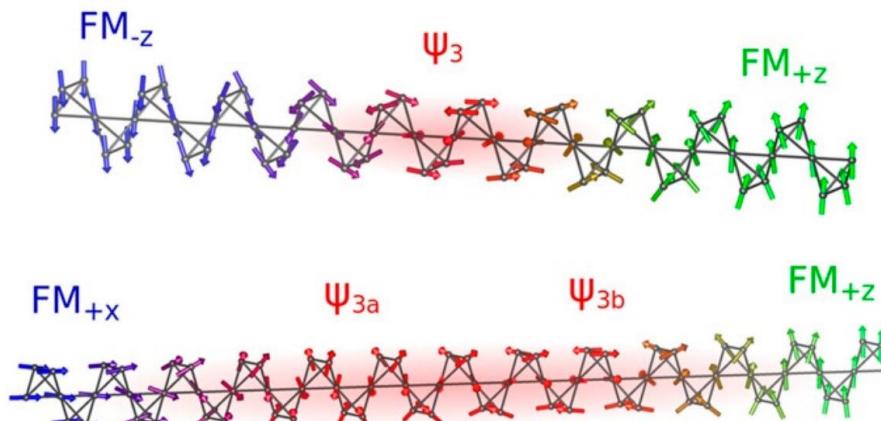
Conventional magnetic order not found in many neutrons experiments

Extreme sensitivity to small amounts of disorder due to variation on 1% level in stoichiometry

# $\text{Yb}_2\text{Ti}_2\text{O}_7$

$$H = \sum_{\langle i,j \rangle} \mathbf{S}_i^T \mathbf{J}_{ij} \mathbf{S}_j$$

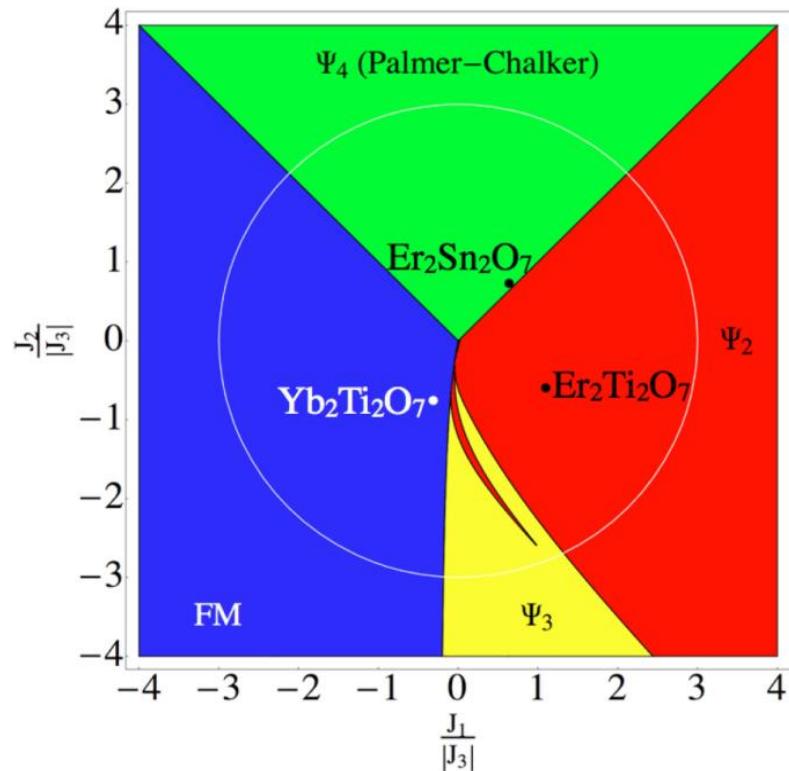
$$\mathbf{J}_{ij} = \begin{bmatrix} J_2 & J_4 & J_4 \\ -J_4 & J_1 & J_3 \\ -J_4 & J_3 & J_1 \end{bmatrix}$$



Physical Review X, 1(2):021002, 2011

PRB 95, 094422. DOI:10.1103/PhysRevB.95.094422

$T_C \approx 260\text{mK}$



PNAS 117 (44) 27245-27254. DOI:10.1073/pnas.2008791117

$$r_{\text{Ti}} = 0.61 \text{\AA}$$

$$r_{\text{Zr}} = 0.72 \text{\AA}$$

Sc	Ti	V
Y	Zr	Nb
	Hf	Ta

Why Zr?

Papers on magnetism

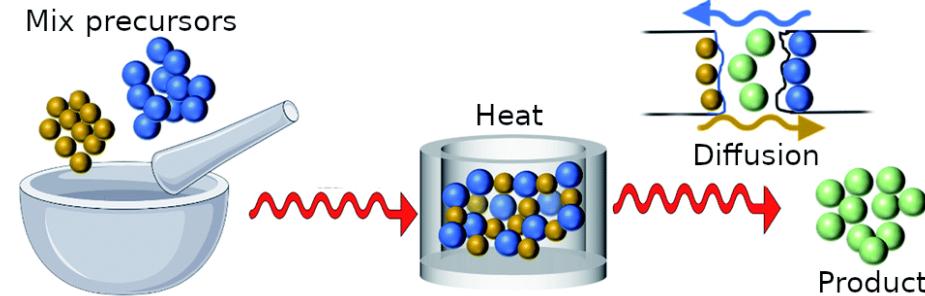
$\text{Yb}_2\text{Ti}_2\text{O}_7$  : 50+

$\text{Yb}_2\text{Zr}_2\text{O}_7$  : 0

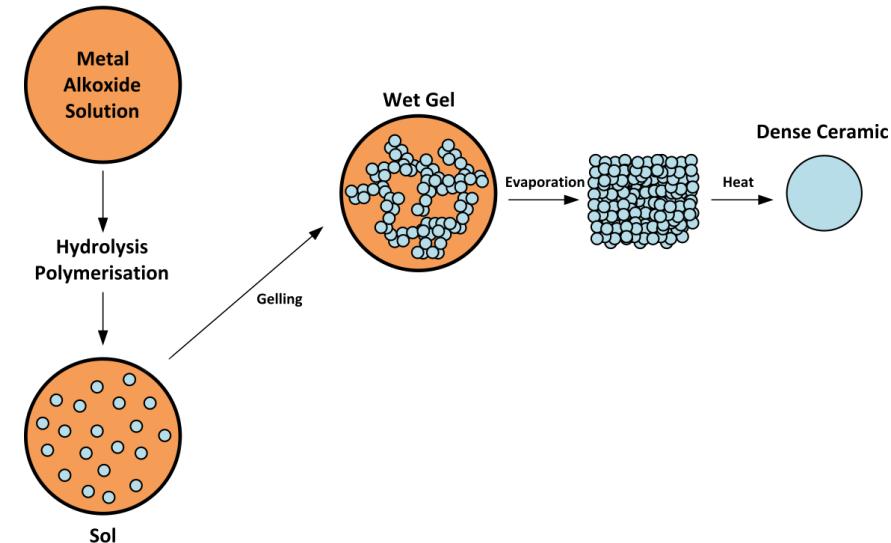
Chemical composition  $x$  is analogous to pressure, can be used to tune material properties

# Synthesis of $\text{Yb}_2\text{Zr}_x\text{Ti}_{2-x}\text{O}_7$

## Solid-State Reaction



## Sol-Gel Method

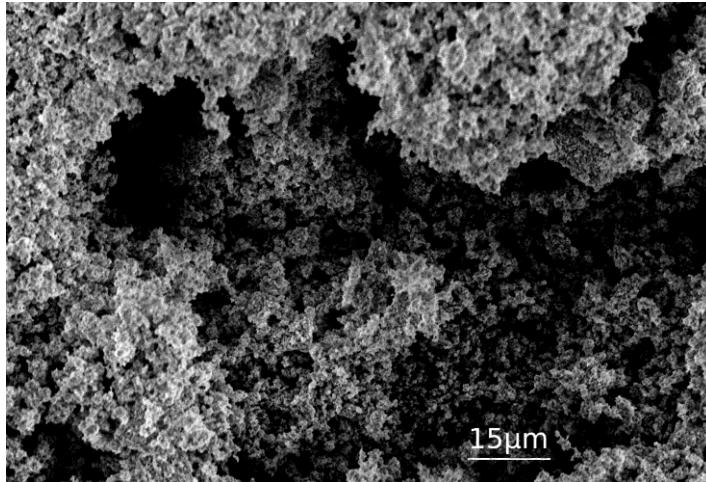


Adapted from DOI: 10.1039/D0RA07884K

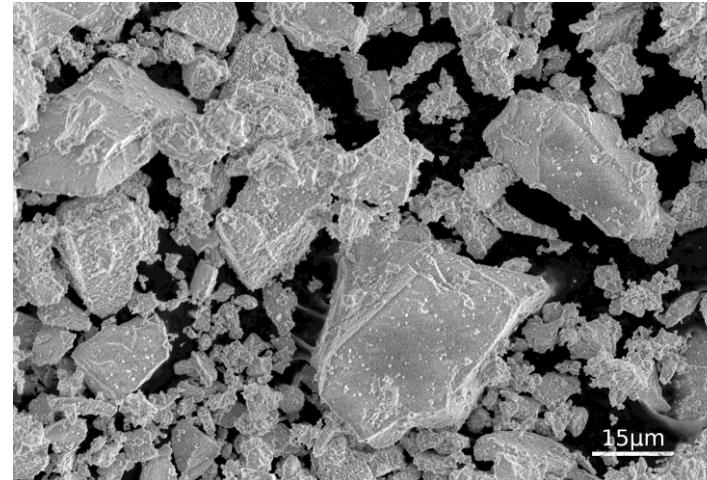
Adapted from DOI:10.1016/j.petlm.2017.03.001

# $\text{Yb}_2\text{Zr}_x\text{Ti}_{2-x}\text{O}_7$ Morphology

$x = 1.5$  (1500°C)



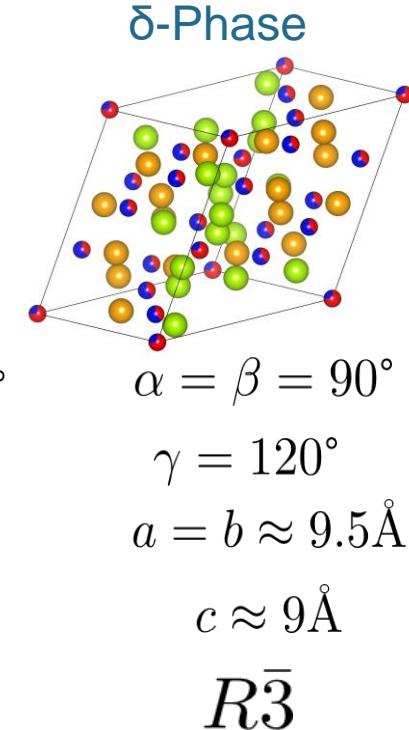
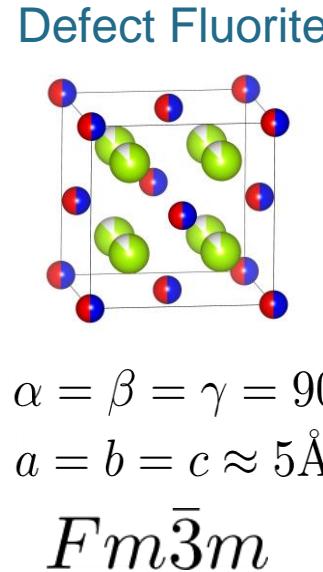
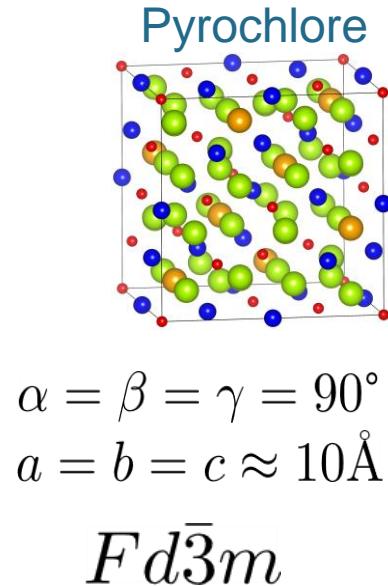
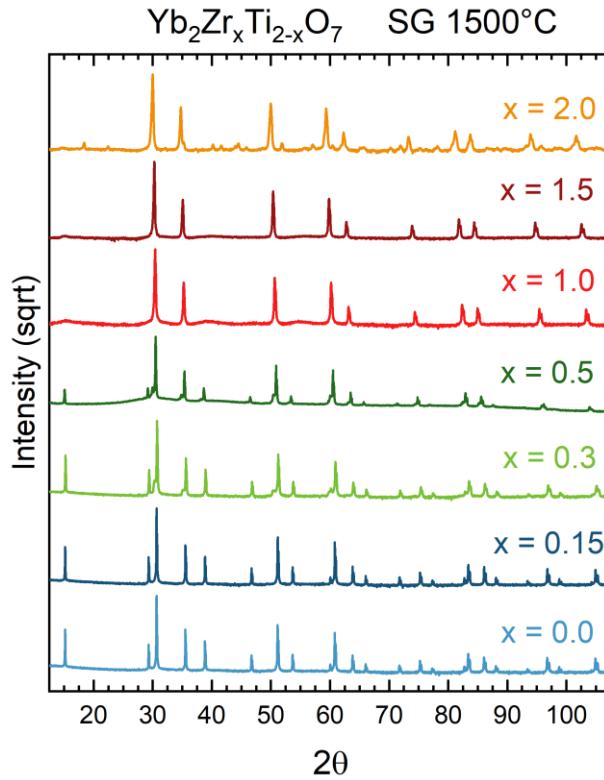
$x = 2.0$  (1500°C)



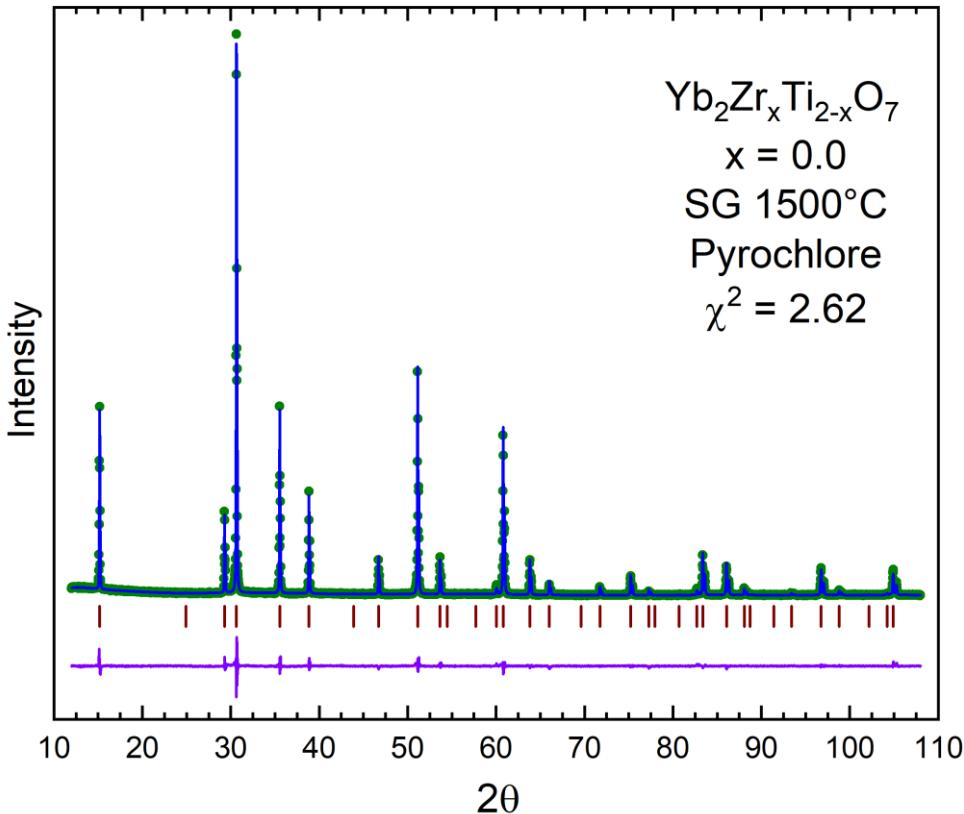
Mixed Zr/Ti → increased porosity

End members ( $x=0$  and  $x=2$ ) → more crystalline

# X-Ray Diffraction

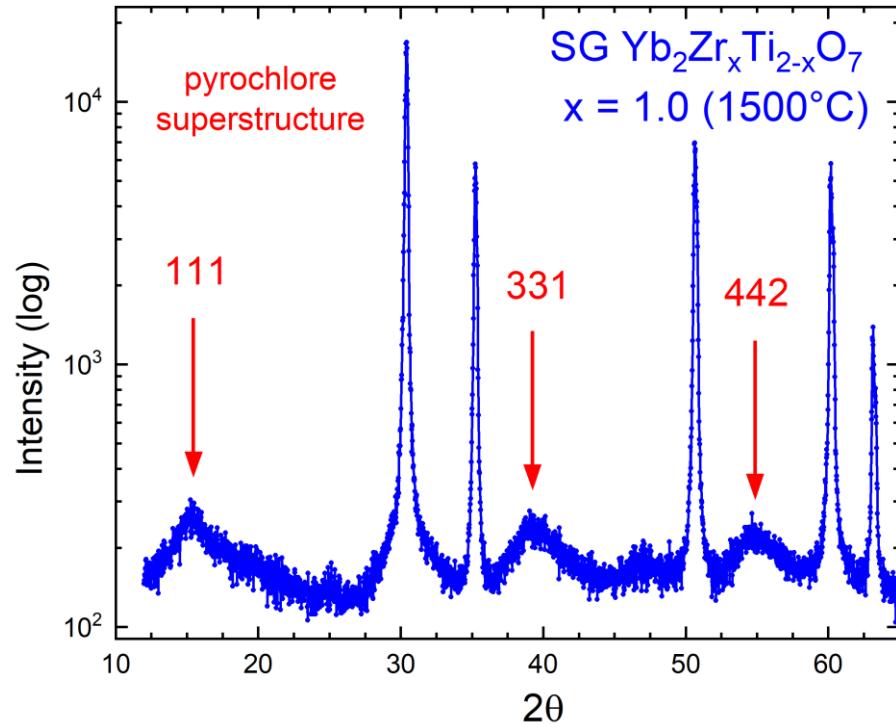
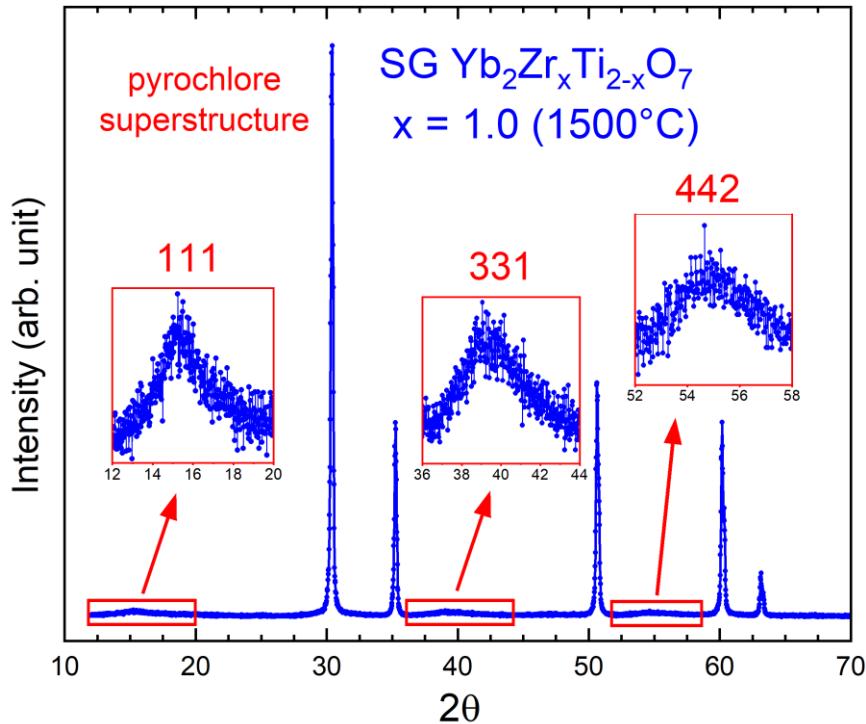


# Rietveld Refinement: $\text{Yb}_2\text{Zr}_x\text{Ti}_{2-x}\text{O}_7$



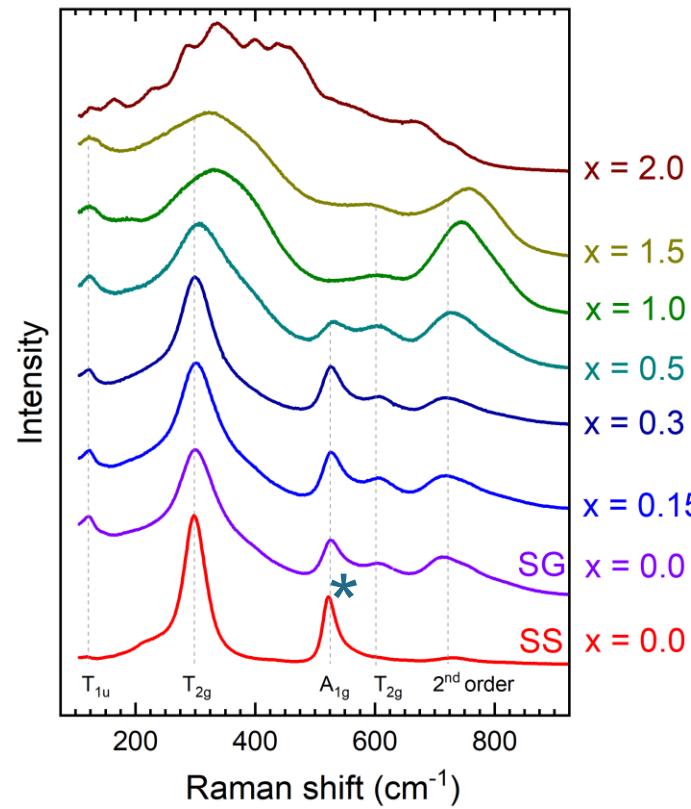
Parameter	Symbol	Refined value	Unit	Occupation
lattice parameter	a	10.09501	Å	
crystallite size	$\mu$	1859	nm	
microstrain	$\epsilon$	640	10 <sup>-6</sup>	
oxygen coordinate	$x_{48f}$	0.3327		
isotropic	$U_{iso}$ (Yb <sub>16d</sub> )	0.02526		0.987
atomic	$U_{iso}$ (Ti <sub>16c</sub> )	0.01517	Å <sup>2</sup>	1.012
displacement	$U_{iso}$ (O <sub>8b</sub> )	0.02965		0.962
parameters	$U_{iso}$ (O <sub>48f</sub> )	0.05890		1.008

# Long-Range vs Local Order



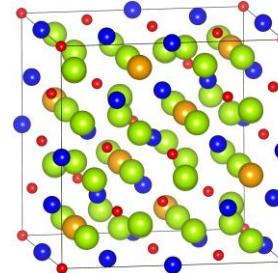
# Raman Spectroscopy

$\text{Yb}_2\text{Zr}_x\text{Ti}_{2-x}\text{O}_7$  SG 1500°C



\*Pyrochlore

Pyrochlore

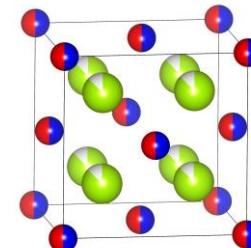


$$\alpha = \beta = \gamma = 90^\circ$$

$$a = b = c \approx 10\text{\AA}$$

$Fd\bar{3}m$

Defect Fluorite

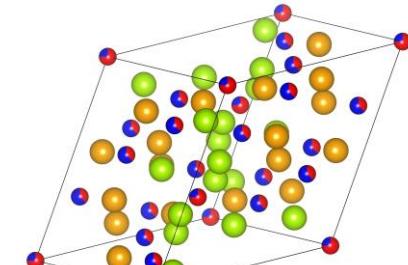


$$\alpha = \beta = \gamma = 90^\circ$$

$$a = b = c \approx 5\text{\AA}$$

$Fm\bar{3}m$

$\delta$ -Phase



$$\alpha = \beta = 90^\circ$$

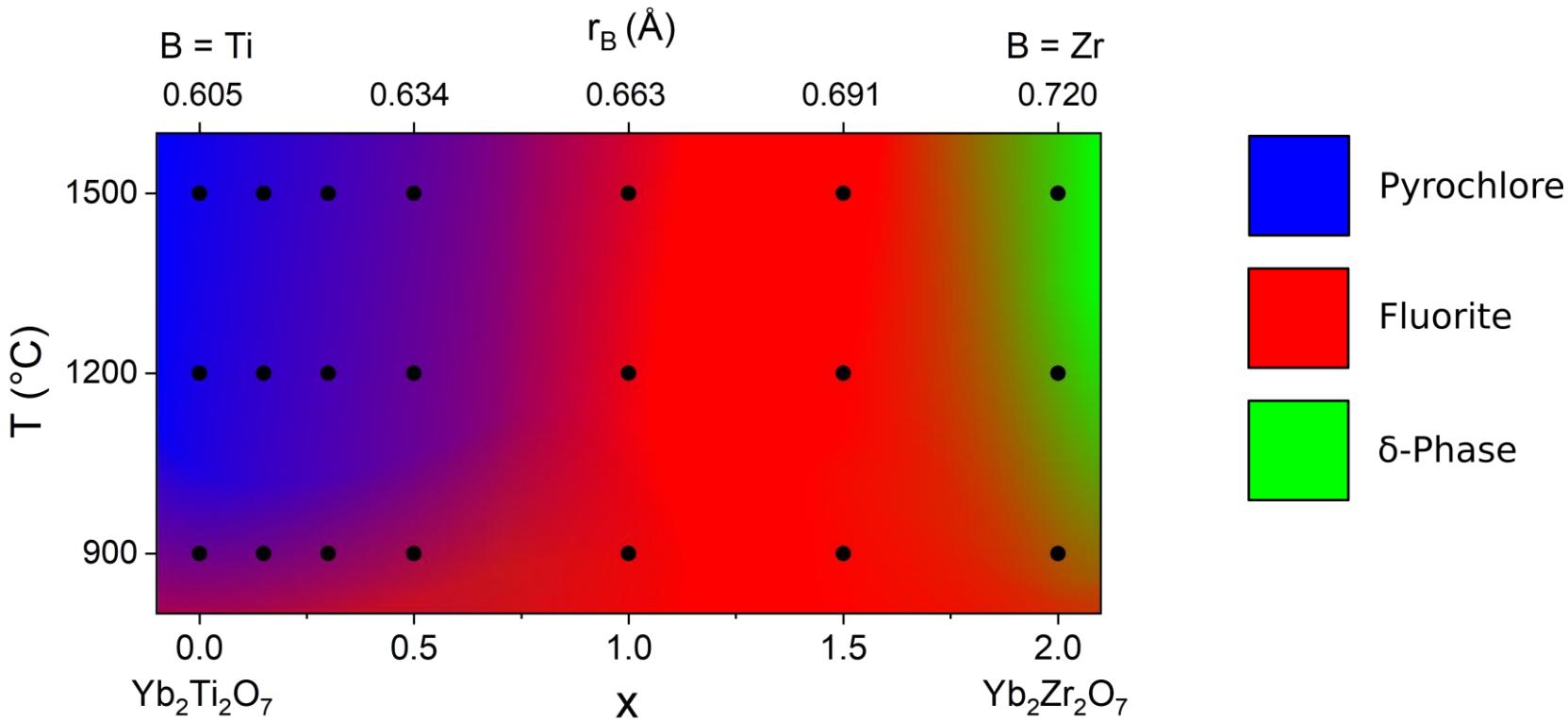
$$\gamma = 120^\circ$$

$$a = b \approx 9.5\text{\AA}$$

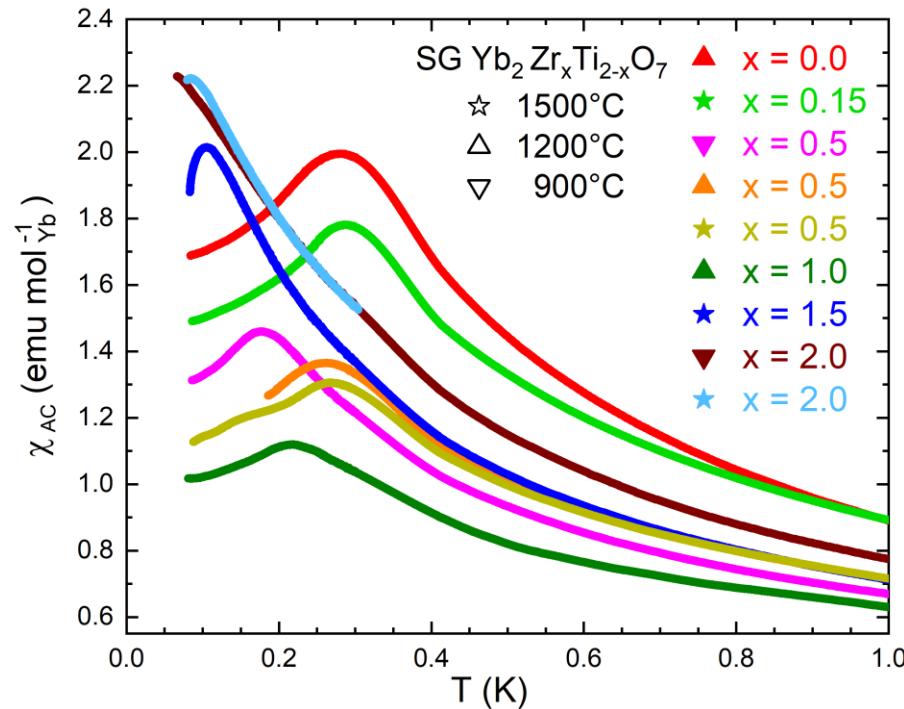
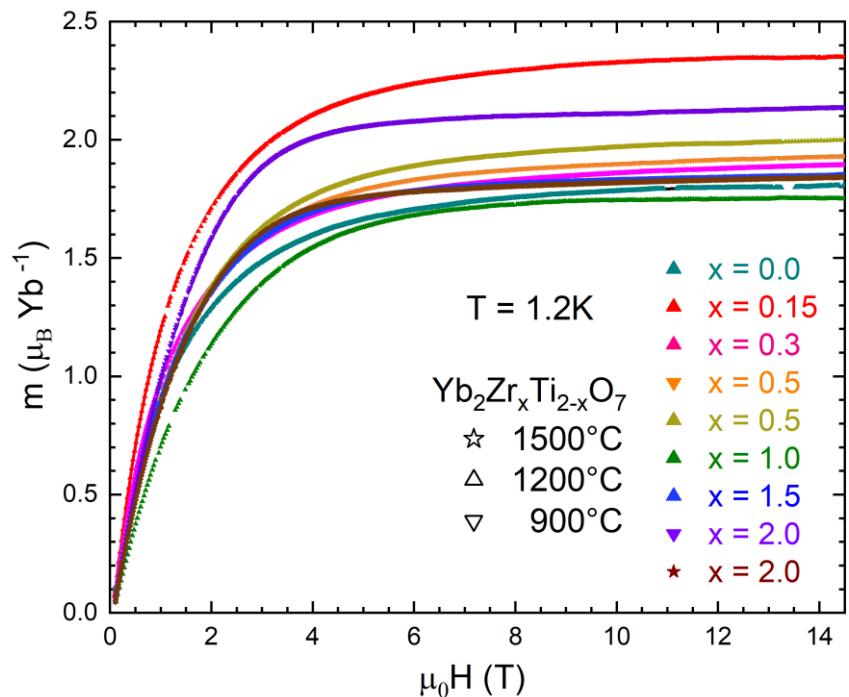
$$c \approx 9\text{\AA}$$

$R\bar{3}$

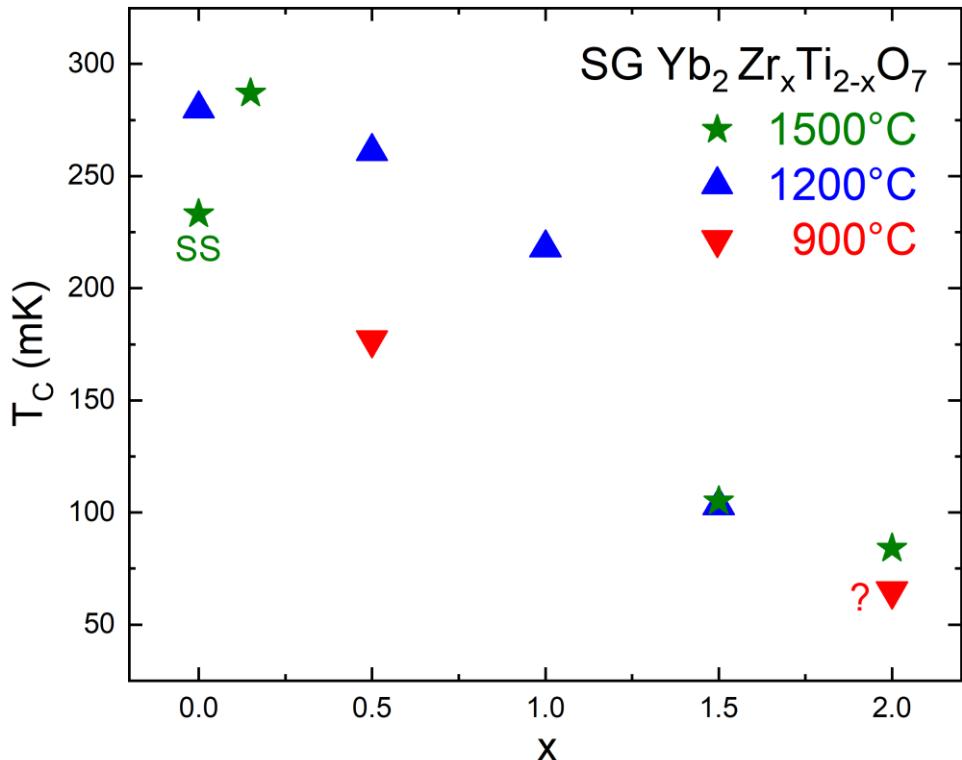
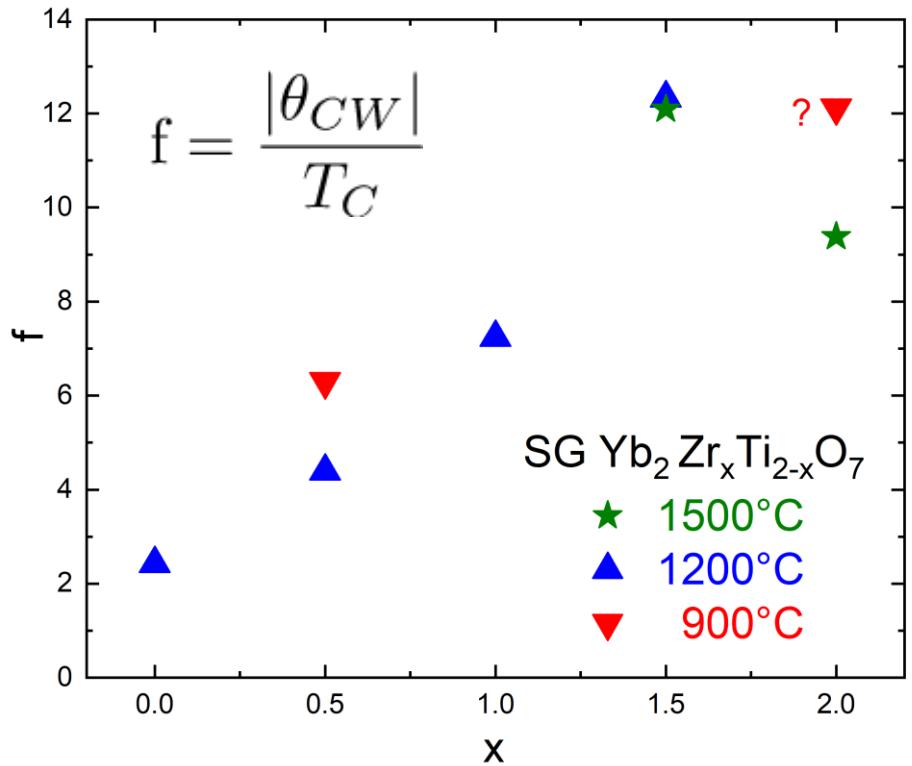
# Phase Diagram



# Magnetic Data



# AC Magnetic Susceptibility



# $Tb_2Ti_2O_7$

Antiferromagnetic correlations

Fluctuating ground state  No long-range order down to 50 mK ( $\Theta_{CW} = -19$  K)

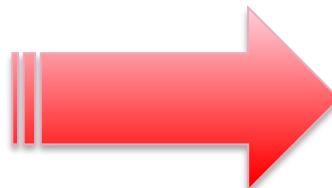
Possible spin-liquid ground state

Pyrochlore

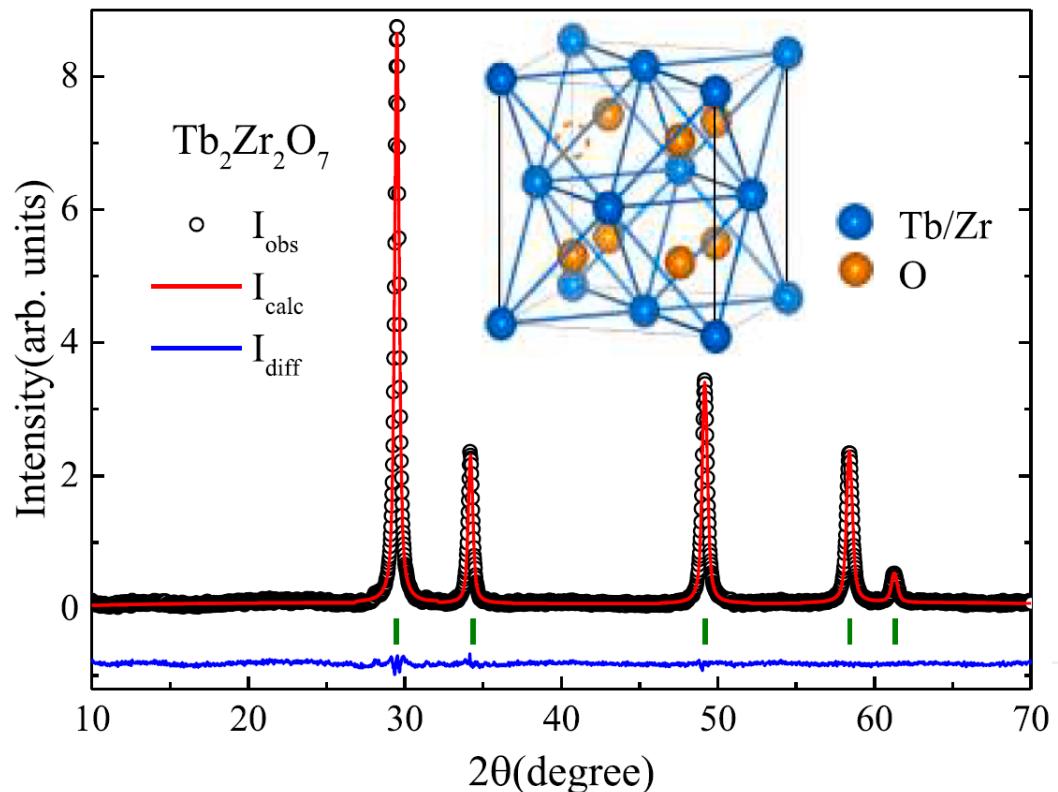
$Tb_2Ti_2O_7$

Defect Fluorite

$Tb_2Zr_2O_7$



# X-Ray Diffraction

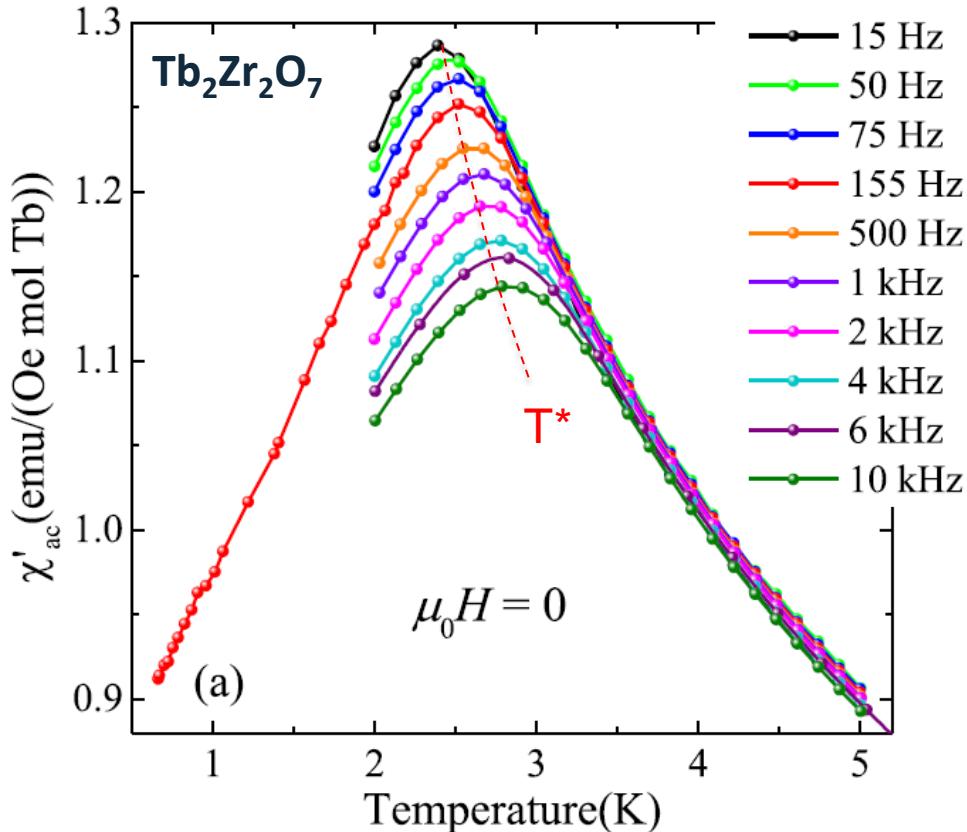


## Sol-gel sample Defect Fluorite Structure

Refined crystallographic parameters for  $\text{Tb}_2\text{Zr}_2\text{O}_7$ .

Crystal system	Cubic
Space Group	$Fm\bar{3}m$
$a$ (Å)	5.233(2)
Tb	4a (0,0,0)
Occupancy	0.499(4)
Zr	4a (0,0,0)
Occupancy	0.499(5)
O	8c (0.25,0.25,0.25)
Occupancy	0.92(2)
Number of variables	21
$R_{\text{wp}}$ (%)	14.3
$R_{\text{exp}}$ (%)	6.6
$\chi^2$	4.6

# AC Magnetic Susceptibility



$\text{Tb}_2\text{Zr}_2\text{O}_7$

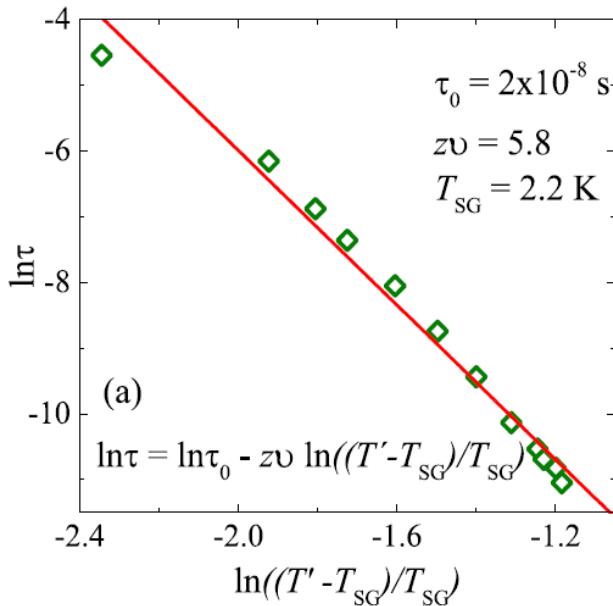
$$\Delta T^*/(T^* \Delta \log f) = 0.064$$

$\text{Tb}_2\text{Ti}_2\text{O}_7$  ( $T^*=0.25$  K)  
 $\text{Tb}_2\text{Hf}_2\text{O}_7$  ( $T^*=0.75$  K)

0.06

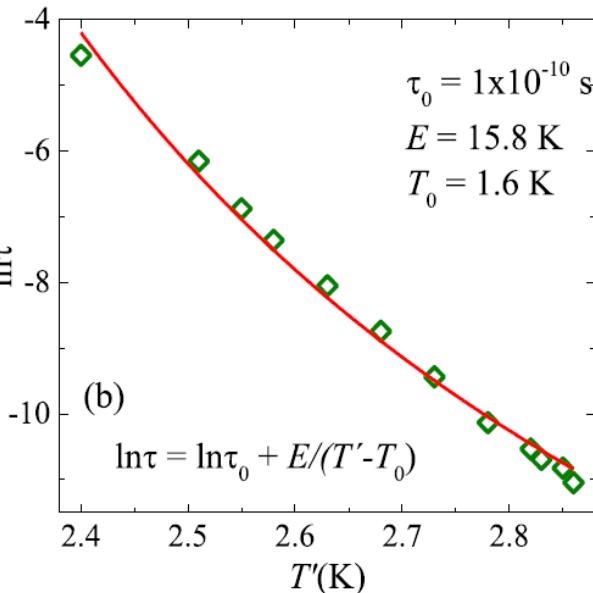
Canonical spin glasses : 0.005 - 0.01

# Spin glasses models



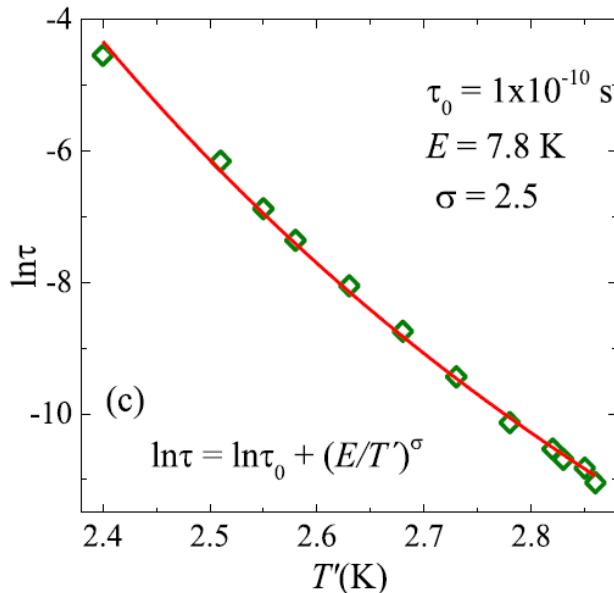
Dynamic scaling law

Canonical SG ( $z\nu = 4-12$ )



Vogel-Fulcher law

$T_0 \neq T^* = 2.5 \text{ K}$



Power law of Arrhenius

$Tb_2Zr_2O_7$   
( $\tau_0 = 1.1 \times 10^{-9} \text{ s}$ ,  $E = 0.91$ )

# Concluding remarks

- Structural disorder increases with Zr content
- Pyrochlore → Defect Fluorite →  $\delta$ -Phase
- Magnetic ordering suppressed by structural disorder
- Increase disorder/frustration → possible spin liquid in  $\text{Yb}_2\text{Zr}_2\text{O}_7$
- Spin-glass-like transition in  $\text{Tb}_2\text{Zr}_2\text{O}_7$
- Considerable spin dynamics remains down to 100 mK

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