Workshop on Multineutron Clusters in Nuclei and in Stars



Sub-Coulomb Nuclear Reactions Studied with the Trojan Horse Method





INFN



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Outline

- Why we need indirect techniques in Nuclear Astrophysics
- Trojan Horse Method (THM)
- Physics cases ...

Charged particle cross section measurements at astrophysical energies

 $\sigma \sim \text{picobarn} \Rightarrow \text{Low signal-to-noise ratio due to the Coulomb barrier between the interacting nuclei}$ measure $\sigma(E)$ over as wide a range as possible, then <u>extrapolate</u> down to E₀!



To give you the feeling what low signal-to-noise ratio means



only two reactions studied directly at the Gamow peak

S(E) experimental enhancement due to the electron screening

 E_c **Coulomb** potential bare E + U_ screened \mathbf{R}_{D} 0 R_n R_t

In astrophysical plasma:

- the screening, due to free electrons in plasma, can be different \rightarrow we need S(E)_b to evaluate reaction rates
- \rightarrow No way to measure S(E)_b from direct experiments at energies where screening is important

 $S_{h}(E)$ -factor extracted from extrapolation of higher energy data



 $\rightarrow \rightarrow \rightarrow \rightarrow$

 $S(E)_{s} = S(E)_{b} \exp(\pi \eta U_{e}/E)$

Indirect Methods for Nuclear Astrophysics

- to measure cross sections at never reached energies (no Coulomb suppression), where the signal is below current detection sensitivity

- to get independent information on U_e
- to overcome difficulties in producing the beam or the target (radioactive ions, neutrons..)

Quite straightforward experiment, no Coulomb suppression, no electron screening but ...



The reaction theory is needed to select only one reaction mechanism. However, nowadays powerful techniques and observables for careful data analysis and theoretical investigation.

THM

Basic principle: relevant low-energy two-body σ from quasi-free contribution of an appropriate three-body reaction in quasi free kinematics

 $A + a \rightarrow b + B + s \rightarrow \rightarrow \rightarrow A + x \rightarrow b + B$

a: $\mathbf{x} \oplus \mathbf{s}$ clusters

Quasi free mechanism ✓ only x - A interaction ✓ s = spectator (p_s~0)

 $E_A > E_{Coul} \Longrightarrow$



plays a key role in compensating for the beam energy

THM applied so far to more than 30 reactions, such as ${}^{6}\text{Li}(p,\alpha){}^{3}\text{He}$, ${}^{7}\text{Li}(p,\alpha)\alpha$, ${}^{2}\text{H}(d,p){}^{3}\text{H}$, ${}^{2}\text{H}(d,n){}^{3}\text{He}$, ${}^{10}\text{B}(p,\alpha){}^{7}\text{Be},{}^{11}\text{B}(p,\alpha){}^{8}\text{Be}$, ${}^{17,18}\text{O}(p,\alpha){}^{14,15}\text{N}$, ${}^{13}\text{C}(\alpha,n){}^{16}\text{O}$, ${}^{7}\text{Be}(n,\alpha){}^{4}\text{He}$, ${}^{18}\text{F}(p,\alpha){}^{15}\text{O}$, ${}^{19}\text{F}(p,\alpha){}^{16}\text{O}$, ${}^{10}\text{B}(p,\alpha){}^{7}\text{Be}$, ${}^{12}\text{C}({}^{12}\text{C},\alpha){}^{20}\text{Ne}$, ${}^{12}\text{C}({}^{12}\text{C},p){}^{23}\text{Na}$...

See for review: R. Tribble et al., Rep. Prog. Phys. **77** (2014) 106901 A. Tumino et al. Ann. Rev. Nucl. Part. Sci. 71 (2021) 346



Theoretical approaches to the THM

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A + a \rightarrow c + C + s \rightarrow \rightarrow \rightarrow A + x \rightarrow c + C
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PWIA hypotheses:

- beam energy > $a = x \oplus s$ breakup Q-value
- projectile wavelength k⁻¹ << x s intercluster distance

MPWBA formalism

(S. Typel and H. Wolter, Few-Body Syst. 29 (2000) 75)

- distortions introduced in the c+C channel, but plane waves for the three-body entrance/exit channel

- off-energy-shell effects corresponding to the suppression of the Coulomb barrier are included

but No absolute value of the cross section



HOES

A. Tumino et al., PRL 98, 252502 (2007)

Theoretical approaches to the THM

R. Tribble et al., Rep. Prog. Phys. 77 (2014) 106901

The THM simple factorization can be deduced from the general formula in the case of resonant reactions

Amplitude of the
TH reaction
$$M^{\text{PWA}(\text{prior})}(P, k_{aA}) = (2\pi)^{2} \sqrt{\frac{1}{\mu_{bB}k_{bB}}} \varphi_{a}(p_{sx})$$

$$\times \sum_{J_{F}M_{F}j'll'm_{j'}m_{l}m_{l'}M_{a}} i^{l+l'} \langle jm_{j}lm_{l}|J_{F}M_{F} \rangle \langle j'm_{j'}l'm_{l'}|J_{F}M_{F} \rangle$$
This accounts for:
$$\cdot \text{ HOES effects}$$

$$\cdot \text{ Normalization (very useful for RIBS)}$$
Moreover:
Possible generalization to
CDCC & DWBA
$$+ \sum_{\nu,\tau=1}^{N} [\Gamma_{\nu sAl'j'J_{F}}(E_{bB})]^{1/2} [A^{-1}]_{\nu\tau} Y_{l'm_{l'}}^{*}(\hat{p}_{xA})$$

$$\times \langle \frac{R_{xA}}{\mu_{xA}} [\Gamma_{\nu xAl'j'J_{F}}(E_{xA})]^{1/2} P_{l'}^{-1/2}(k_{xA}, R_{xA})(j_{l'}(p_{xA}R_{xA}))$$

$$\times [(B_{xAl'}(k_{xA}, R_{xA}) - 1) - D_{xAl'}(p_{xA}, R_{xA})]$$

$$\times [(B_{xAl'}(k_{xA}, R_{xA}) - 1) - D_{xAl'}(p_{xA}, R_{xA})]$$

...for resonant reactions

The A + $a(x+s) \rightarrow F^*(c + C) + s$ process is a transfer to the continuum where particle x is the transferred particle



Standard R-Matrix approach cannot be applied to extract the resonance parameters \rightarrow Modified R-Matrix is introduced instead

In the case of a resonant THM reaction the cross section takes the form

$$\frac{d^2\sigma}{dE_{Cc}\,d\Omega_s} \propto \frac{\Gamma_{(Cc)_i}(E)\,|M_i(E)|^2}{(E-E_{R_i})^2 + \Gamma_i^2(E)/4}$$

 $M_i(E)$ is the amplitude of the transfer reaction (upper vertex) that can be easily calculated \rightarrow The resonance parameters can be extracted

When transfer to a bound F state, M² is proportional to the ANC of the populated F state

Advantages:

- possibility to measure down to zero energy
- No electron screening
- HOES reduced widths are the same entering the OES S(E) factor (New!)

20 2	100		122	101000000	
Reactions s	studied	with	the	THM.	

	Indirect reaction	Direct reaction	References
[1]	2 H(7 Li, $\alpha\alpha$)n	1 H(7 Li, α) 4 He	Spitaleri et al 1999, Lattuada et al 2001 [97]
[2]	3 He(7 Li, $\alpha\alpha$)d	2 H(7 Li, α) 4 He	Tumino et al 2006 [98]
[3]	2 H(⁶ Li, α^{3} He) n	1 H(⁶ Li, α) ³ He	Tumino et al 2003 [88]
[4]	6 Li(6 Li, $\alpha \alpha$) 4 He	2 H(⁶ Li, α) ⁴ He	Spitaleri et al 2001 [22]
[5]	2 H(9 Be, α^{6} Li)n	1 H(⁹ Be, α) ⁶ Li	Wen et al 2008 [99]
[6]	2 H(10 B, α^{7} Be)n	$^{1}\mathrm{H}(^{10}\mathrm{B},\alpha)^{7}\mathrm{Be}$	Lamia et al 2008, Rapisarda et al 2018, Cvetinovic et al 2018 [100–102]
[7]	${}^{2}\mathrm{H}({}^{11}\mathrm{B}, \alpha_{0}{}^{8}\mathrm{Be})\mathrm{n}$	$^{1}\mathrm{H}(^{11}\mathrm{B},\alpha)^{8}\mathrm{Be}$	Spitaleri et al 2004, Lamia et al 2011 [103,104]
[8]	2 H(15 N, α^{12} C)n	1 H(15 N, α) 12 C	La Cognata et al 2007 [105]
[9]	2 H(18 O, α^{15} N)n	1 H(18 O, α) 15 N	La Cognata et al 2009 [106]
[10]	2 H(17 O, α^{14} N)n	${}^{1}\mathrm{H}({}^{17}\mathrm{O},\alpha){}^{14}\mathrm{N}$	Sergi et al 2010, Sergi et al. 2015 [89,90]
[11]	⁶ Li(³ He, p ⁴ He) ⁴ He	2 H(3 He, p) 4 He	La Cognata et al 2005 [107]
[12]	2 H(6 Li, p 3 H) 4 He	2 H(d, p) 3 H	Rinollo et al 2005 [108]
[13]	${}^{6}\text{Li}({}^{12}\text{C}, ^{12}\text{C}){}^{2}\text{H}$	⁴ He(¹² C, ¹² C) ⁴ He	Spitaleri et al 2000 [109]
[14]	² H(⁶ Li, t ⁴ He) ¹ H	n(⁶ Li, t) ⁴ He	Tumino et al 2005, Gulino et al 2010 [110,111]
[15]	² H(p, pp)n	1 H(p, p) 1 H	Tumino et al 2007, Tumino et al 2008 [112,113]
[16]	² H(³ He, p ³ H) ¹ H	${}^{2}H({}^{2}H, p){}^{3}H$	Tumino et al 2011, Tumino et al 2014 [94,114]
[17]	2 H(3 He, n 3 He) 1 H	2 H(2 H, n) 3 He	Tumino et al 2011, Tumino et al 2014 [94,114]
[18]	2 H(19 F, α^{16} O)n	${}^{1}\mathrm{H}({}^{19}\mathrm{F},\alpha){}^{16}\mathrm{O}$	La Cognata et al 2011, Indelicato et al 2017 [32,115]
[19]	¹³ C(⁶ Li, <i>n</i> ¹⁶ O) ² H	$^{13}C(\alpha, n)^{16}O$	La Cognata et al 2014 [116]
[20]	2 H(18 F, α^{15} O)n	${}^{1}\mathrm{H}({}^{18}\mathrm{F},\alpha){}^{15}\mathrm{O}$	Cherubini et al 2015, Pizzone et al. 2016, La Cognata et al. 2017 [92,117,118]
[21]	${}^{2}\mathrm{H}({}^{10}\mathrm{B},^{7}\mathrm{Li}){}^{1}\mathrm{H}$	$n(^{10}\mathbf{B},\alpha)^7$ Li	Guardo et al 2019, Sparta et al 2021 [119,120]
[22]	$^{2}\mathrm{H}(^{7}\mathrm{Be},\alpha\alpha)^{1}\mathrm{H}$	$n(^7\text{Be}, \alpha)^4\text{He}$	Lamia et al 2017, Lamia et al 2019, Hayakawa et al 2021 [121-123]
[23]	${}^{12}C({}^{14}N, ^{20}Ne)^{2}H$	${}^{12}C({}^{12}C, \alpha){}^{20}Ne$	Tumino et al 2018 [30]
[24]	¹² C(¹⁴ N, p ²³ Na) ² H	¹² C(¹² C, p) ²³ Na	Tumino et al 2018 [30]
[25]	⁶ Li(¹⁹ F, <i>p</i> ²² Ne) ² H	4 He(19 F, p) 22 Ne	Pizzone et al 2017, Dagata et al 2018 [117,124]
[26]	2 H(17 O, α^{14} C) 1 H	$^{17}O(n, \alpha)^{14}C$	Oliva et al 2020 [125]
[27]	2 H(3 He, <i>pt</i>) 1 H	3 He $(n, p)^{3}$ H	Pizzone et al 2021 [126]
[28]	2 H(7 Be, $p{}^{7}$ Li) 1 H	$n(^7\text{Be}, p)^7\text{Li}$	Hayakawa et al 2021 [123]
[29]	² H(²⁷ Al, α^{24} Mg)n	$^{27}\mathrm{Al}(p,\alpha)^{24}\mathrm{Mg}$	Palmerini et al 2021, La Cognata et al. 2022 [127-129]

12C+12C fusion

C-burning crucial phase in the nucleosynthesis of massive stars (> 8 M₀), determines M_{up}, ignition trigger for superbursts and Type Ia supernovae

astrophysical energy: 1 – 3 MeV From direct measurement, minimum E: 2.1 MeV

extrapolations differ by 3 orders of magnitude without inclusion of resonances

Indirect measurement with THM down to 1 MeV: ${}^{12}C({}^{14}N,\alpha{}^{20}Ne){}^{2}H$ and ${}^{12}C({}^{14}N,p{}^{23}Na){}^{2}H$.

Resonances dominate the astrophysical energy



International journal of science

Letter Published: 23 May 2018

An increase in the ${}^{12}C + {}^{12}C$ fusion rate from resonances at astrophysical energies

A. Tumino ^{SEI}, C. Spitaleri, M. La Cognata, S. Cherubini, G. L. Guardo, M. Gulino, S. Hayakawa, I. Indelicato, L. Lamía, H. Petrascu, R. G. Pizzone, S. M. R. Puglia, G. G. Rapísarda, S. Romano, M. L. Sergi, R. Spartá & L. Trache

Nature 557, 687–690 (2018) Download Citation ±

Our Experiment with theTHM

¹²C(¹²C,α)²⁰Ne and ¹²C(¹²C,p)²³Na reactions via the <u>Trojan Horse Method</u> applied to the ¹²C(¹⁴N,α²⁰Ne)²H and ¹²C(¹⁴N,p²³Na)²H three-body processes

²H from the ¹⁴N as spectator s

Observation of ¹²C cluster transfer in the ¹²C(¹⁴N,d)²⁴Mg^{*} reaction (R.H. Zurmûhle et al. PRC 49 (1994) 5)

E_{14N} =30 MeV> E_{coul}

d,p/ α coincidence detection







A. Tumino et al., Nature (2018)



 $\widetilde{\chi}^2 = 0.1$

nature

Çompared to CF88, the present rate increases from a factor of 1.18 at 1.2 GK to a factor of more than 25 at 0.5 GK

12C+160 fusion

- In the late stages of C-burning the abundance of ¹⁶O is larger than ¹²C
 - Ashes of the ${}^{12}C(\alpha,\gamma){}^{16}O$
 - Minor contribution from ${}^{12}C({}^{12}C,2\alpha){}^{16}O$
- For T > 1GK the rate of the ¹²C+¹⁶O fusion starts to be relevant. Principal reactions involved in the process:
 - ${}^{12}C({}^{16}O, \alpha){}^{24}Mg$
 - ¹²C(¹⁶O, p)²⁷Al
 - ¹²C(¹⁶O, n)²⁷Si

High level density in ²⁸Si. One should see only special states





New results with the THM down to 2 MeV, pape in preparation

Charge independence and charge symmetry

After removing the electromagnetic interactions, the NN force between nn, np, pp are almost the same

Charge independence: equality between pp/nn force and np force

Violation: associated to the mass difference between charged and neutral pions (identical nucleons exchange a neutral pion, a neutron and a proton may exchange both a neutral and a charged pion)

Charge symmetry: equality between pp and nn forces

Charge symmetry breaking: mainly attributed to the up-down quark mass difference Its validity is supported to some extent by an approximate equality of binding energies of isobar nuclei.

Charge symmetry breaking manifested in the s-wave scattering lengths, a_{NN} that determine the low-energy behavior of NN scattering.

anp directly determined from experiments

 a_{pp} not directly accessible from experiments because of Coulomb effects \rightarrow need to remove them theoretically to reveal the strong interaction contribution to the scattering length

ann not directly accessible from experiments because of the absence of neutron targets.

... we propose an innovative way to determine $a_{pp} \rightarrow$

Two-body cross-section from THM data



nature > communications physics > articles > article

Article Open Access Published: 18 May 2023

Coulomb-free ${}^{1}S_{0}p - p$ scattering length from the quasi-free $p + d \rightarrow p + p + n$ reaction and its relation to universality

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Notice: the NN s-wave phase shift δ contains all short range effects, including the electromagnetic ones. This means that the present analysis of the HOES cross section allows direct access to the short-range p-p interaction as a whole, with its peculiar a_{pp} and r_0 values.

We propose a new paradigm: to assess the charge symmetry breaking of the short-range interaction as a whole, in line with the current understanding that, at a fundamental level, the charge dependence of nuclear forces is due to a difference between the masses of the up and down quark and to electromagnetic interactions among the quarks.

We can exploit universal concepts to better interpret the results, now that Coulomb effects have been removed from the p-p system.

Notably, in the universal window the dynamics is largely independent of the details of the interaction. It is dominated by the long-range behavior allowing for a description based on few parameters.

We construct a two-parameter Gaussian NN interaction with fixed range, valid for s-wave in the spin singlet channel

$$V_{NN}(r) = V_0 e^{-r^2/r_G^2} + \frac{e_{NN}^2}{r}$$

with NN \equiv nn, np, pp and e_r^2

 $r_0 = 2R\frac{\beta+1}{\beta}$

the Gaussian form selected to represent the short-range interaction is not relevant, other choices are acceptable as well. Very recently a new calculation using the Eckart potential that exactly represents the S-matrix for the NN system in the universal window (S-matrix is equivalent to the effective range expansion up to the second order):

$$egin{aligned} V_{Eck}(eta,R,r) &= -2rac{\hbar^2}{mR^2}rac{eta e^{-r/R}}{(1+eta e^{-r/R})^2} \ a &= 4Rrac{eta}{eta - 1} \ \hline NN \ \hline \end{array}$$

NN	$ a^N(fm)$	$ $ $r_0^N(fm)$	a^{THM} (fm)	$ \mathbf{r}_0^{THM}(\mathrm{fm}) $	$a^{sr}(fm)$	$r_0^{sr}(fm)$
np	-23.08 ± 0.02	2.77 ± 0.05			-23.74 ± 0.02	2.80 ± 0.08
pp	-17.3 ± 0.4	2.85 ± 0.04	$-18.17\substack{+0.53\\-0.59}$	$2.80{\pm}0.05$	-17.9 ± 0.5	2.85 ± 0.09
nn	-18.9 ± 0.4	2.75 ± 0.11			-18.6 ± 0.4	2.85 ± 0.08

A. Tumino, A Kiewsky et al. Few Body Systems 2025

The universal window shows the location of the different NN systems using the numbers here obtained: the coordinates are given by

 $[x, y] = [r_0/a_B, r_0/a]$

With a_B given by

$$\frac{1}{a_B} = \frac{1}{a} + \frac{1}{2} \frac{r_0}{a_B^2}$$

From low-energy effective range plus S-matrix pole equation

Interestingly, they lie on the curve $y = x - 0.5x^2$ verifying the correlation as above.

The NN systems are well determined by the corresponding experimental values, and have a precise position along the y(x) curve.

Using the property highlighted here that the systems move along the universal curve, it is possible to reduce the model dependence in the determination of the scattering parameters as produced by the short-range part of the interaction without discriminating between nuclear and electromagnetic.



THM and RIB experiments

RIB experiments: mostly neutron but also p,a induced reactions to tackle the nucleosynthesis beyond Fe T > 10⁸ K \Rightarrow E₀ ~ 100 keVs - MeVs \leq E_{coul} \rightarrow 10⁻⁶ barn < σ < 10⁻³ barn

Issues:

- low beam intensities (several o.d.m. lower than for stable beams)
- beam energies usually significantly larger than those needed for astrophysical studies
- changing beam energies in small steps to study the excitation function is often impractical.
- n-targets still under development, low density



THM

- Higher beam energies complying with available RIB facilities
- A single beam energy to study the excitation function → intercluster motion used to cover the astrophysical energy region.
- Use of d-targets (CD₂) as virtual n-targets

very welcome the use of storage rings to overcome beam intensity limitations and improving beam purity at every turn

⁷Be destruction and the cosmological Li problem

⁷Li also from primordial ⁷Be, but in this case need to measure processes that would get rid of ⁷Be

13. ⁷Be(n,p)⁷Li 14. ⁷Be(n,α)⁴He 15. ⁷Be(d,p)2⁴He

Recent experiment: ${}^{7}Be(n,a){}^{4}He$ down to $E_{cm} \sim 20$ keV via ${}^{7}Be(d,a{}^{4}He){}^{1}H$

EXOTIC facility E_Beam=20.4 MeV, purity ~ 99 % i ~5-8 10⁵ pps, beam spot of ~ 9 mm

Another experiment @ CRIB to also measure the ${}^{7}Be(n,p_{0,1}){}^{7}Li$ E_Beam=22.2 MeV, purity ~ 99 % i ~ 10⁶ pps, beam spot of ~ 9 mm

Role of ⁷Be clear only after systematic measurements of all relevant reactions

Influence on primordial ⁷Li abundance of about 10% Potential influence also from 7Be(d,) and 7Be(t,)





Conclusions

Nuclear physics is a fundamental pillar of Nuclear Astrophysics

Indirect methods are unique tools to investigate reactions on energy ranges difficult to study otherwise

Still great potential for future applications (also beyond astrophysical applications)

Thank you for your attention!