Toroidal vorticity in light-on-heavy collisions: Event-by-event simulations

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<u>light-on-heavy</u>
 Phys. Rev. C104 (2021) 011901
 Phys. Rev. C110 (2024) 054908

this talk

jet-through-plasma Phys. Lett. **B820** (2021) 136500 Phys. Rev. **C109** (2024) 014905

 Talk by Cicero Muncinelli

João Prado Barbon, David D. Chinellato, MAL, Vítor H. Ribeiro, Willian M. Serenone, Chun Shen, Jun Takahashi, Giorgio Torrieri (3C Collaboration)









Outline

- Vorticity patterns in seen and not-yet seen
 - global / longitudinal / circular / toroidal
- Vortical toroids ("smoke rings") in small-on-large collisions
 - simulations with smooth IC
 - simulations with e-by-e fluctuating IC
 - possibility to measure in p+A collisions in final RHIC run

• Summary

Polarization patterns in heavy ion collisions- seen





Polarization patterns in heavy ion collisions- seen & not yet seen







Polarization patterns in heavy ion collisions- seen & not yet seen

Xia, Li, Tang, Wang PRC 98, 024905 (2018)

PRC104 (2021) 011901

Development of circular vorticity in MUSIC

Vorticity "of the flow field"

Vorticity toroids visible *due to* transverse flow

Talk Wed by C. Muncinelli

Like an armor-piercing shell

brief fluid-like behavior

Hydronamization during penetration?

Would provide novel evidence of "smallest droplet of QGP" and its formation

Helmholtz (1867): Persistent vortical toroids (smoke rings) are quintessential fluid behavior in response to a localized disturbance

EM tensor $T^{\tau\tau} = e(\vec{x}_{\perp}, \eta_s) \cosh(fy_{\rm CM}(\vec{x}_{\perp}))$ $T^{\tau\eta} = \frac{1}{\tau_0} e(\vec{x}_{\perp}, \eta_s) \sinh(fy_{\rm CM}(\vec{x}_{\perp}))$ where $y_{\rm CM}(\vec{x}_{\perp}) = \arctan\left[\frac{T_A - T_B}{T_A + T_B} \tanh(y_{\rm beam})\right]$

MUSIC [1] hydro with Lattice EoS [2]

 $\rm T_{\rm A}$, $\rm T_{\rm B}$ are nuclear thickness functions at $\rm x_{\perp}$

smooth or e-by-e fluctuating [3]

[1] PRC102 (2020) 014909
[2] PRC82 (2010) 014903
[3] PRC102 (2020) 044905

EM tensor $T^{\tau\tau} = e(\vec{x}_{\perp}, \eta_s) \cosh(fy_{\rm CM}(\vec{x}_{\perp}))$ MUSIC [1] hydro with Lattice EoS [2] $T^{\tau\eta} = \frac{1}{\tau_0} e(\vec{x}_\perp, \eta_s) \sinh(f y_{\rm CM}(\vec{x}_\perp))$ T_A , T_B are nuclear thickness functions at x smooth or e-by-e fluctuating [3] $y_{\rm CM}(\vec{x}_{\perp}) = \operatorname{arctanh} \left| \frac{T_A - T_B}{T_A + T_B} \tanh(y_{\rm beam}) \right|$ where [1] PRC102 (2020) 014909 [2] PRC82 (2010) 014903 [3] PRC102 (2020) 044905 Similar reasoning as in this case... spectators f=1 participants

(b) Matter-overlap flow profile

• Basic observables are ~identical in these scenarios

(a) Bjorken flow profile: $u_z = \eta_s$ atter - São Paulo - July 2025

(b) Matter-overlap flow profile

- Basic observables are ~identical in these scenarios
- Vorticity is very different

See also S. Voloshin, EPJ Web Conf. 171 (2018) 07002 arxiv: 1710.08934

(a) Bjorken flow profile: $u_z = \eta_s$ atter - São Paulo - July 2025 Mike Lisa - 91

(b) Matter-overlap flow profile

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(b) Matter-overlap flow profile

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Relation to Takahashi geometry

The experimental geometry was **not** this

It was flow thru capillary tube:

 V_z $i_s \theta$ v_z E_z

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R. Takahashi, Nature Phys. 12 (2016) 52-56

(b) Radial-gradient flow profile

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MUSIC hydrodynamics, with baryon currents ds in Quantum Matter - São Paulo - July 2025

PR**C104** (2021) 1, 011901

p+Au matter-overlap flow

- strong
- ~rapidity-even

smooth-on-smooth, b=0 collisions at 200 GeV

Fluid \rightarrow particles (vorticity \rightarrow polarization)

$$\begin{array}{ll} \mbox{Cooper-Frye} & for spin \end{array} S^{\mu}(p) = -\frac{1}{8m} \epsilon^{\mu\rho\sigma\tau} p_{\tau} \frac{\int d\Sigma_{\lambda} p^{\lambda} n_{F} (1-n_{F}) \omega_{\rho\sigma}}{\int d\Sigma_{\lambda} p^{\lambda} n_{F}} \end{array}$$

$$\mbox{Becattini et al, Annal. Phys. 338 (2013) 32}$$

$$\omega_{\mu\nu}^{(th)} = -\frac{1}{2} \left[\partial_{\mu} \left(u_{\nu}/T \right) - \partial_{\nu} \left(u_{\mu}/T \right) \right]$$

(or alternative vorticities...)
$$\omega_{\mu\nu}^{(K)} = -\frac{1}{2} \left(\partial_{\mu} u_{\nu} - \partial_{\nu} u_{\mu} \right)$$
$$\omega_{\mu\nu}^{(T)} = -\frac{1}{2} \left[\partial_{\mu} \left(T u_{\nu} \right) - \partial_{\nu} \left(T u_{\mu} \right) \right]$$

non-vortical
symmetric shear
$$\xi^{\mu\nu} \equiv \frac{1}{2} \left[\partial^{\mu} \left(\frac{u^{\nu}}{T} \right) + \partial^{\nu} \left(\frac{u^{\mu}}{T} \right) \right]$$

 $S_{\mu} \rightarrow S_{\mu} + \langle \mathcal{A}_{\mu} \rangle$
 $\mathcal{A}_{\mu} = \frac{1}{E} \varepsilon^{\mu\rho\tau\sigma} p_{\tau} \xi_{\sigma\lambda} \times \begin{cases} \hat{t}_{\rho} p^{\lambda} \longleftarrow \text{Becattini et al (2021)} \\ u_{\rho} p_{\perp}^{\lambda} \longleftarrow \text{Liu \& Yin (2001)} \end{cases}$

fluctuating initial conditions

- ✓ Event-by-event calculation with lumpy initial conditions, following prescription in [1]
 → little difference with smooth initial conditions
- ✓ reduced R_{spin} for more symmetric system

[1] Shen, Alzhrani, PRC102 (2020) 014909

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PRC110 (2024) 054908

Vortex rings at top RHIC energy: momentum dependence

LHCb SMOG: predictions for the LHC

Sensitivity to physics of "smallest droplet of QGP"

PR110 (2024) 054908

Experimental issues

$$\overline{\mathcal{R}}_{\Lambda}^{\hat{z}} = 2\left\langle \frac{\vec{s}_{\Lambda}' \cdot \left(\hat{z}' \times \vec{p}_{\Lambda}'\right)}{|\hat{z}' \times \vec{p}_{\Lambda}'|} \right\rangle_{\phi} = \frac{8}{\pi\alpha} \left\langle \sin\left(\phi_p - \phi_{\Lambda}\right) \right\rangle$$

Advantage:

no event plane needed!

→ measuring ~1% toroidal polarization is much easier than 1% global polarization (for same stats)

$$\overline{P}_{H} = -\frac{8}{\pi \alpha R_{\rm EP}^{(1)}} \left\langle \sin\left(\phi_{p} - \Phi_{EP,1}\right) \right\rangle_{\phi}$$

$$\delta_{\overline{P}_H} \propto \left(\#_\Lambda
ight)^{-1/2} \left(R_{
m EP}^{(1)}
ight)^{-1}$$

Required statistics:

- similar #∧
 - → scaling from 11 BES global polarization [1]: <u>300M central (0-10%) events</u> to discover 1% vortical polarization with 7σ significance
 - ✓ 5-week p-Au run ~ 350 M

Crucial experimental issue

STARNote **SN0819 : The STAR Beam Use Request for Run-24-25** https://drupal.star.bnl.gov/STAR/starnotes/public/SN0819

- STAR: Midrapidity hyperons from Au+Au collisions signal must vanish by symmetry
- Tracking-induced artifacts
 - large! bigger than likely signal
 - **complicated**! depends strongly on cuts, method, detector. Seen also in simulation, but not exactly the same
 - equal and opposite for Lambda & antiLambda → artifact will flip with B-field.

Mike Lisa - 9th Confer If STAR measures p+Au collisions in the final run, it must measure both field configurations!

Summary

- A+A / p+A collisions generate complex flow structures; probed by vorticity at small scale
- Circular vorticity pattern predicted for b=0 collisions at all energies
 - LHCb take a look!
- Fluid system with localized disturbance toroidal vortex structure forms
 - Helmholtz (1867): Persistent vortical toroids (smoke rings) are quintessential fluid behavior
 - thermalized energy from jet quenching sensitive to virtuality, fluid properties
 - p+A would be a compelling evidence for hydro nature of the smallest system & physical properties
- Experimentally observable (R)
 - distinct from hadronic processes by particle/antiparticle similarity, eta dependence
 - challenging to observe few % effect, but possible during this last RHIC run flip B-field

Muito obrigado pela sua atenção

Backup

At very high Vs_{NN} : signal reverses

✓ RHIC energy is a good place to look

PRC104 (2021) 011901; arxiv: 2101.10872 agnetic Fields in Quantum Matter - São Paulo

Contributions from shear terms and gradients in chemical potential

- Formulation of Becattini et al has very strong effect
- Formulation of Liu et al significant at high pT
- Chemical gradients minor effect

$$S_{\text{SIP(type I)}}^{\mu}(p) = -\frac{1}{4m} \epsilon^{\mu\rho\sigma\tau} \left\langle \frac{1}{p \cdot u} \hat{t}_{\rho} \xi_{\sigma\lambda} p^{\lambda} p_{\tau} \right\rangle, \quad [1]$$

$$S_{\text{SIP(type II)}}^{\mu}(p) = -\frac{1}{4m} \epsilon^{\mu\rho\sigma\tau} \left\langle \frac{1}{p \cdot u} u_{\rho} \xi_{\sigma\lambda} p_{\perp}^{\lambda} p_{\tau} \right\rangle, \quad [2]$$

$$S_{\mu_{B}\text{IP}}^{\mu}(p) = -\frac{1}{4m} \epsilon^{\mu\rho\sigma\tau} \left\langle \frac{T}{p \cdot u} u_{\rho} \partial_{\sigma} \left(\frac{\mu_{B}}{T}\right) p_{\tau} \right\rangle \quad [3]$$

Thermal shear tensor
$$\xi^{\sigma\lambda} \equiv \frac{1}{2} \left[\partial^{\sigma} \left(\frac{u^{\lambda}}{T} \right) + \partial^{\lambda} \left(\frac{u^{\sigma}}{T} \right) \right]$$

[1] Becattini, Buzzegoli, Palermo PLB 820, 136519 (2021); Buzzegoli PRC105, 044907 (2022)
[2] Liu, Yin PRD 104, 054043 (2021); JHEP 07, 188 (2021)
[3] Liu, Huang Sci. China Phys. Mech. Astron. 65, 272011 (2022),

Hydrodynamics: simulation setup

The energy-momentum tensor is initialized as:

 $T^{\tau\tau} = e(\vec{x}_{\perp}, \eta_s) \cosh(f y_{\rm CM}(\vec{x}_{\perp}))$ $T^{\tau\eta} = \frac{1}{\tau_0} e(\vec{x}_\perp, \eta_s) \sinh(f y_{\rm CM}(\vec{x}_\perp))$

with $y_{\rm CM}(\vec{x}_{\perp})$ defined as:

 $y_{\rm CM}(\vec{x}_{\perp}) = \operatorname{arctanh} \left| \frac{T_A - T_B}{T_A + T_B} \operatorname{tanh}(y_{\rm beam}) \right|$

And *f* being a free parameter $\in [0, 1]$ such that:

f = 0: bjorken

f = 1:'matter

- **3D Initial conditions** with [1]
- Hydro: MUSIC [2] with Lattice QCD EoS [3]
- Particlization: Cornelius [4]
- Parameters most relevant to this study (varied later):
 - -: nucleus size (default: 0.5 fm)
 - $-\tau_{o}$: hydrodynamization time (default: 1 fm/c)
 - $-\eta$ /s: shear viscosity (default: 0.08)
 - $-e_{sw}$: freeze-out energy density (default: 0.5 GeV/fm³)
- Freeze out hypersurface (spin) polarizationpuia [5]: **Thermal vorticity**
- average: done over the freeze-out hypersurface

[1] Phys. Rev. C 102, 014909 (2020) Phys. Rev. C 82, 014903 (2010) [3] Phys. Rev. C 100, 024907 (2019)

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Model dependence of the ring observable: hotspot size

- The **hotspot transverse size** has a strong impact:
 - smaller hotspots → larger T gradients → larger thermal vorticity
 - $\mathcal{R}^{\hat{z}}_{\Lambda}$
- Both a larger hotspot and a smaller f can reduce significantly $\mathcal{R}^{\hat{z}}_{\Lambda}$
 - But: distinct p_T dependence of f = 0 or 1 breaks this degeneracy!
 - Negative derivative of with p_{T} only appears if f = 0

Model dependence of the ring observable: freeze-out energy density

- The **freeze-out energy density** also impacts the outcome
 - Tested with 0.25 and 0.5 GeV / fm^3
 - Larger evolution time → vorticity relaxed to smaller values
 - Effect is most significant at larger momenta
- Other model variables were tested but have subdominant effects:
 - Hydrodynamization time
 - Specific shear viscosity
- Even beyond: coupling of hypersurface properties and spin matters!

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From STAR BUR 2024-25 – statistical requirements

The statistical requirement to discover these toroidal vortex structures may be estimated by STAR's previous hyperon polarization measurements. The uncertainty on global polarization measurements $\delta \overline{P}_{\Lambda} \propto N_{\Lambda}^{-1/2} \cdot R_{\rm EP}^{-1}$, where N_{Λ} is the total number of hyperons in the analysis, and $R_{\rm EP}$ is the event plane resolution [7]. Because there is no event plane involved in the production plane polarization, on the other hand, the uncertainty on the ring observable goes as $\delta \overline{\mathcal{R}}_{\Lambda}^{z} \propto N_{\Lambda}^{-1/2}$. For the same-magnitude signal, then, $\overline{\mathcal{R}}_{\Lambda}^{z}$ enjoys an effective $R_{\rm EP}^{-2}$ "statistical advantage" over \overline{P}_{Λ} . Since STAR measured [104] $\overline{P}_{\Lambda} \approx 1\%$ at $\sqrt{s_{NN}} = 11$ GeV with 3.5 σ significance, with the same number of hyperons in the analysis, we should be able to measure $\overline{\mathcal{R}}_{\Lambda}^{z} \sim 1\%$ with 7 σ significance. The 11-GeV analysis involved 6M As, and we estimate 0.02 As per central (0 - 10%) p+Au collision at $\sqrt{s_{NN}} = 200$ GeV. Therefore, the 7 σ measurement will require 6M/0.02 = 300M central p+Au collisions.

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Experimental issues

$$\overline{\mathcal{R}}_{\Lambda}^{\hat{z}} = 2 \left\langle \frac{\vec{S}_{\Lambda}' \cdot \left(\hat{z}' \times \vec{p}_{\Lambda}'\right)}{|\hat{z}' \times \vec{p}_{\Lambda}'|} \right\rangle_{\phi} = \frac{8}{\pi \alpha} \left\langle \sin\left(\phi_p - \phi_{\Lambda}\right) \right\rangle$$

Challenge: large topological dependence of efficiency

- artifacts *complicated* and ~10% (or more)
- will affect any tracking detector
- *must flip B-field* to cancel artifact

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1.13

Experimental issues

FIG. 1. The measured m_{inv} distributions of two classes of Λ -hyperon decays: "right" decays in blue, with $(\vec{p}_{\Lambda} \times \vec{p}_{p}^{*}) \cdot \vec{B}_{STAR} > 0$, and "left" decays in red, with $(\vec{p}_{\Lambda} \times \vec{p}_{p}^{*}) \cdot \vec{B}_{STAR} < 0$. The "right" decay class has a notably sharper m_{inv} distribution than the "left" decay class, and this is due to the effects of daughter tracks crossing in the STAR TPC with $\vec{B}_{STAR} || - \hat{z}$. The opposite pattern is obtained by flipping the sign of \vec{B}_{STAR} or by reconstructing $\bar{\Lambda}$ hyperons.

Experimental issue – requirement to flip field

Figure 104: Production-plane polarization (modulo an overall scaling by $\frac{8\pi}{\alpha_{\Lambda}}$) for Λ (blue) and $\overline{\Lambda}$ (red) candidates, as a function of invariant mass. The data comes from STAR measurements of Au+Au collisions at $\sqrt{s_{NN}}$ in the BES-I (left) and BES-II (right) campaigns. STAR's solenoidal magnetic field was directed to the West and East, respectively, for these two datasets. For the BES-I data, hyperon candidates were identified with "standard" topological cuts, whereas the candidates shown in BES-II were identified using the new KFParticle package.

f parameter and global polarization

FIG. 1. Color contours show the initial energy density distributions in the $x - \eta_s$ plane for 20-30% Au+Au collisions at 19.6 GeV with the longitudinal rapidity fraction f = 0 (a) and f = 1 (b). The grey arrows in panel (b) indicate the nonzero initial longitudinal flow u^{η} with $y_L = y_{\rm CM}$ in Eqs. (13) and (14). $u^{\eta} = 0$ in panel (a).

It is unclear to me that f will be the same in p+A

Reminder from 1970's (through 2010's)

production-plane polarization in p+A collisions.

- Same observable as ours!
- high-x signal
- ~independent of target (p, Be, C, Cu, W)
- ~independent of energy (only measured to ~40 GeV)
- odd in rapidity for p+p, but also p+A
- no signal for anti-Lambdas

+

Ο