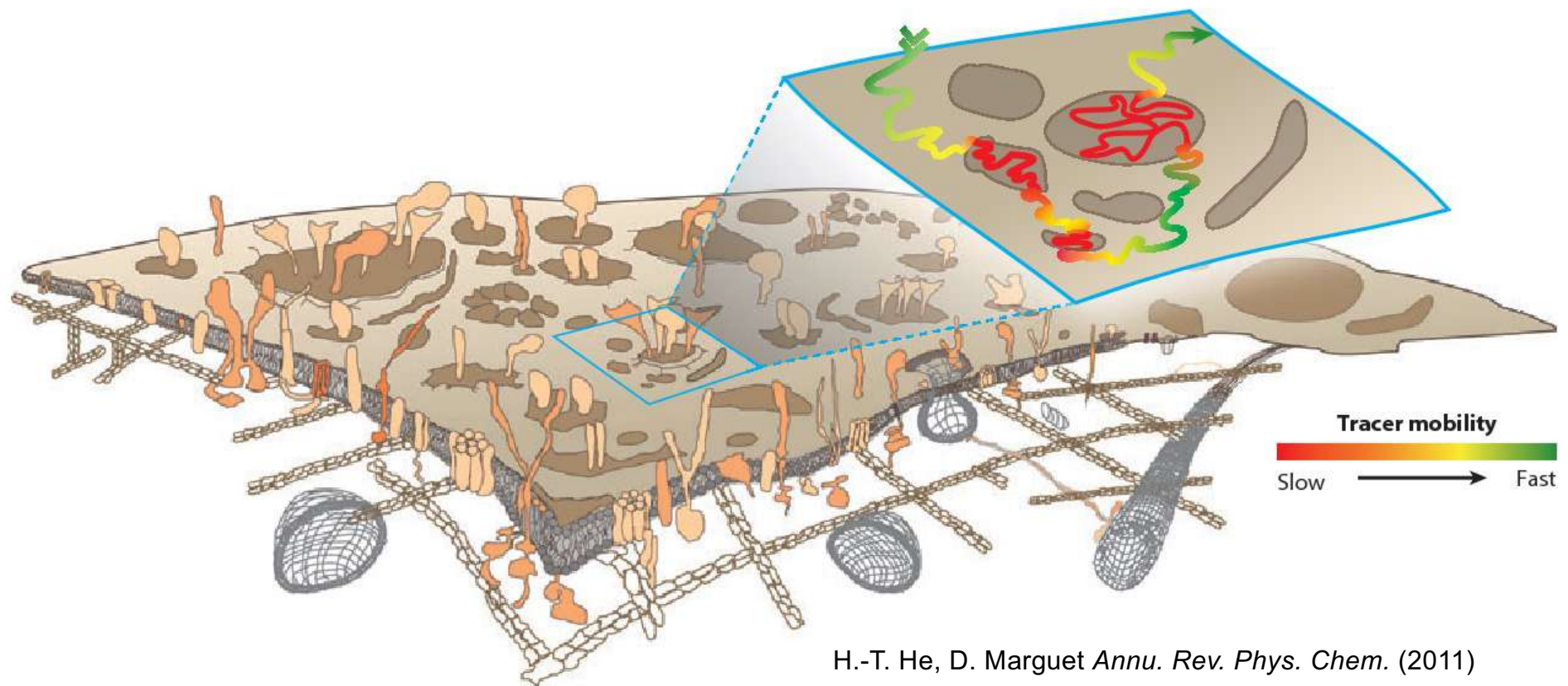
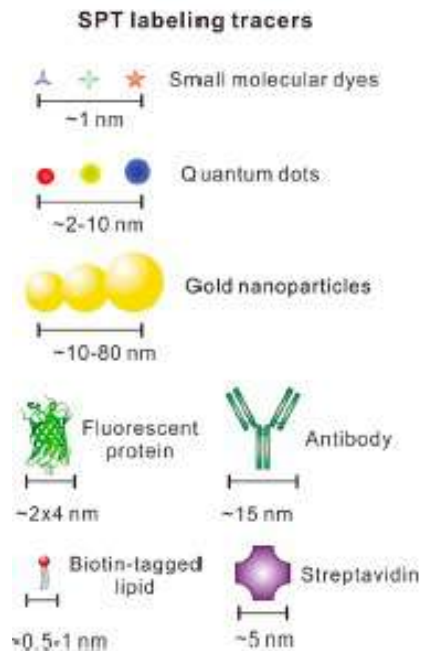
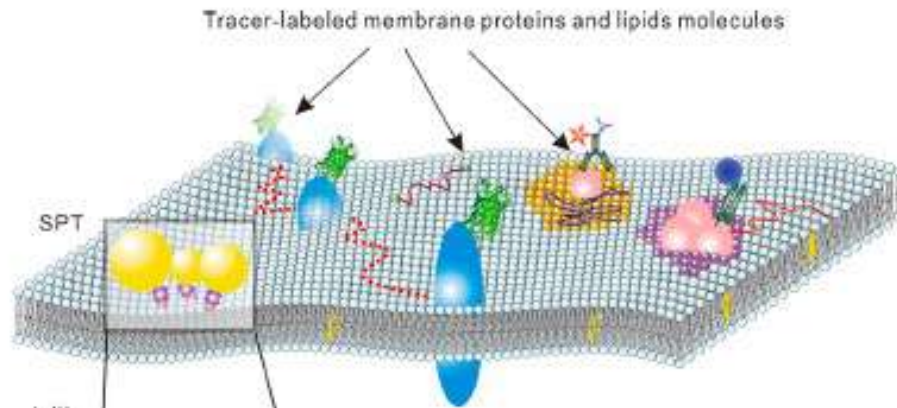




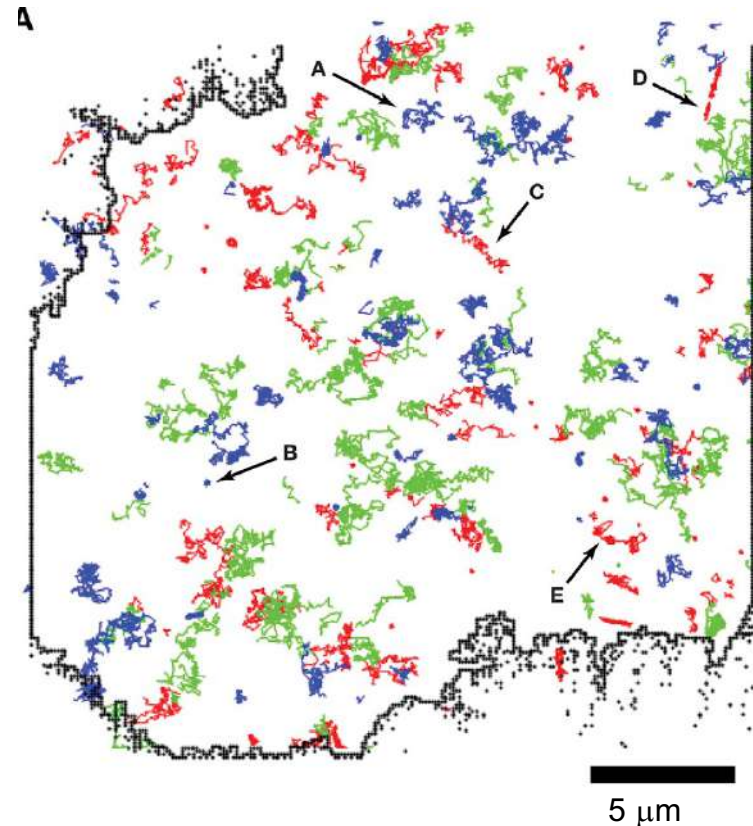
3. Protein Clustering on Membranes

Heterogeneous Diffusion in the Plasma Membrane

Single Particle Tracking at the PM



Y. Yu, M. Li, Y. Yu *ACS Nano* (2019)



K. Jacobson et al *Cell* (2019)

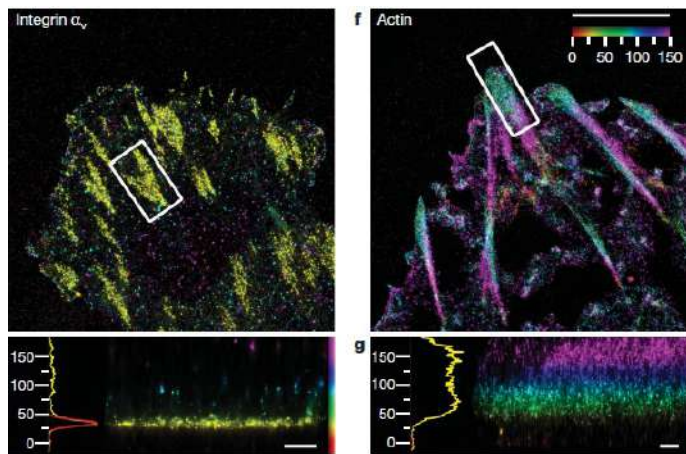
Heterogeneous mobility

But, difficult to determine if lipid or protein nano-domains

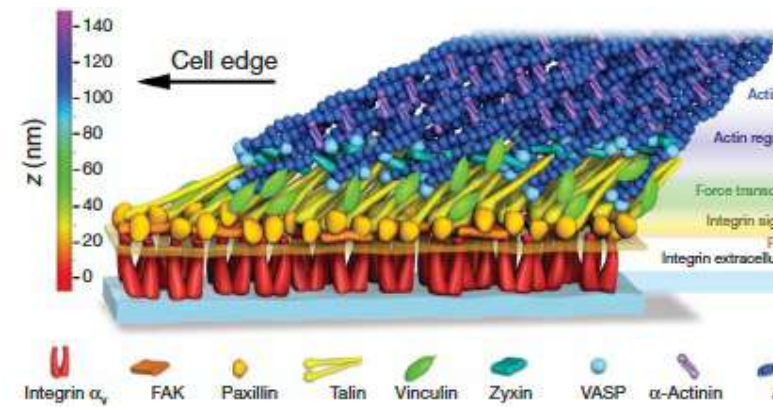
In Living Cells, *no Macroscopic* Lipid or Protein Domains in General

Except special cases, nanodomains *below optical resolution* ($<300\text{ nm}$)

- Focal adhesion (cell adhering)

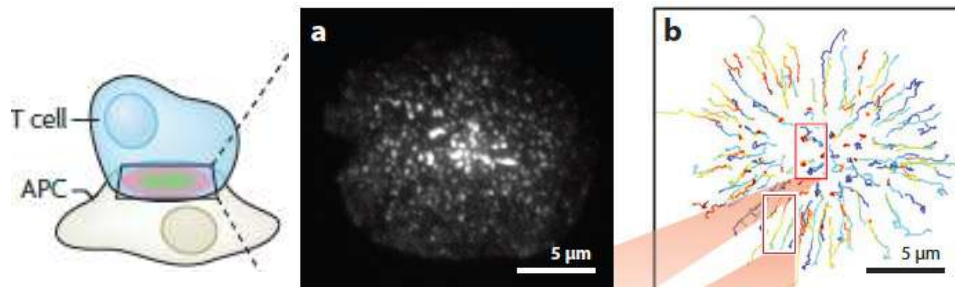


500 nm



P. Kanchanawong.... C. Waterman *Nature* (2010)

- Immune synapse



T-cell interacting with a bilayer
containing T-cell receptors (fluo)

M.L. Dustin, J.T. Groves *Annu. Rev. Biophys.* (2012)

With super resolution microscopy (optics, CryoEM)
or sophisticated technics (high-speed AFM, FRET etc..)

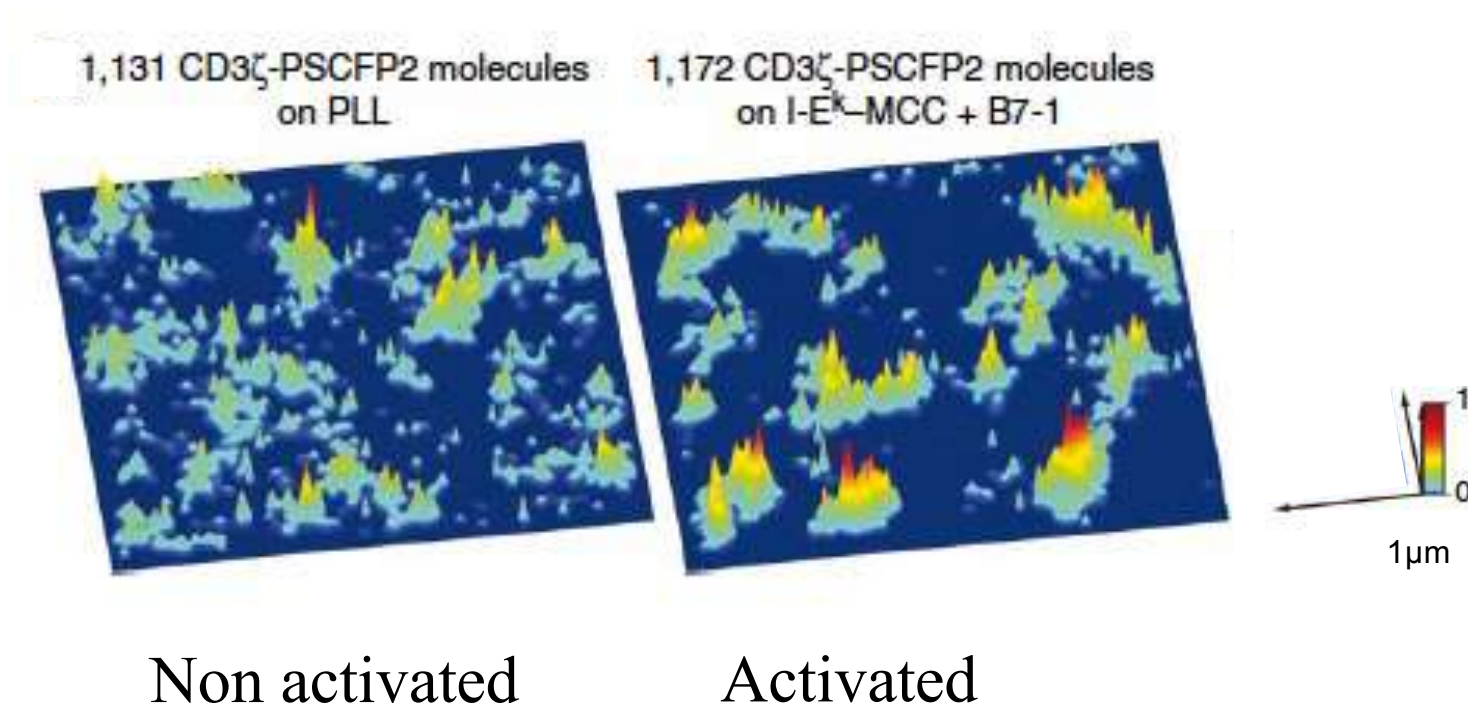
Small protein clusters in cell membranes

(<100 nm, some time also dimers, trimers...)

Membrane Protein Clustering

- Membrane Receptors

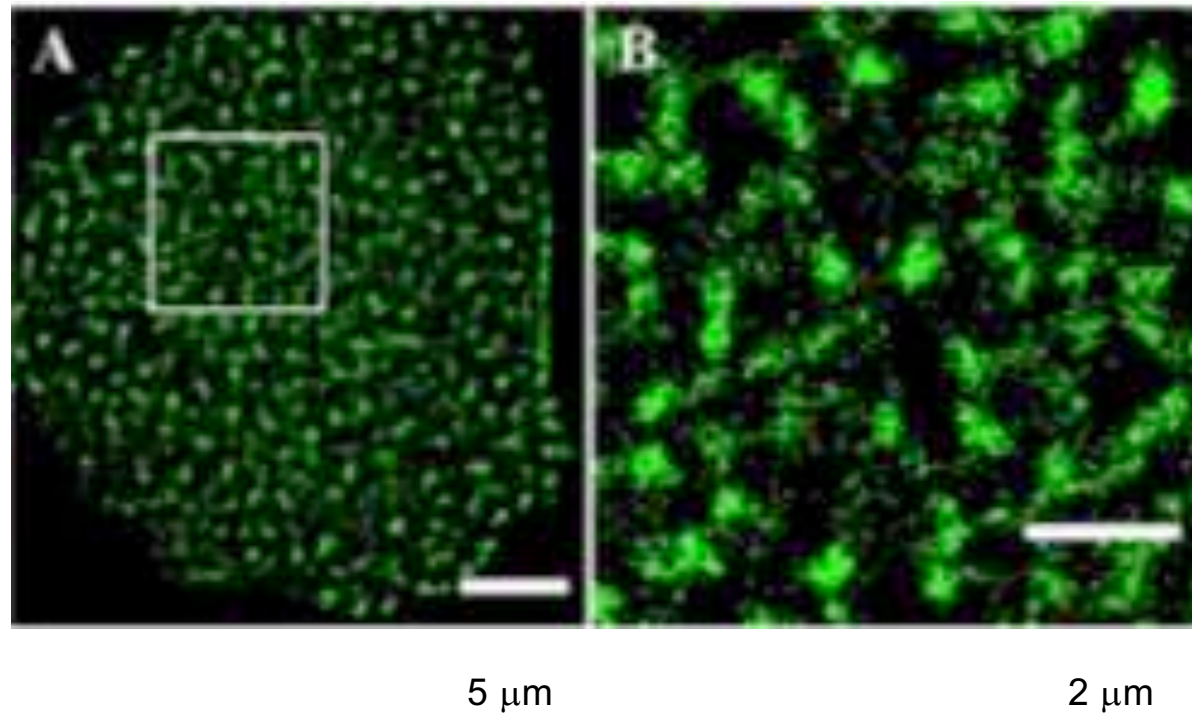
In native T-cells membranes



Membrane Protein Clustering

- Glucose Transporter
GLUT1

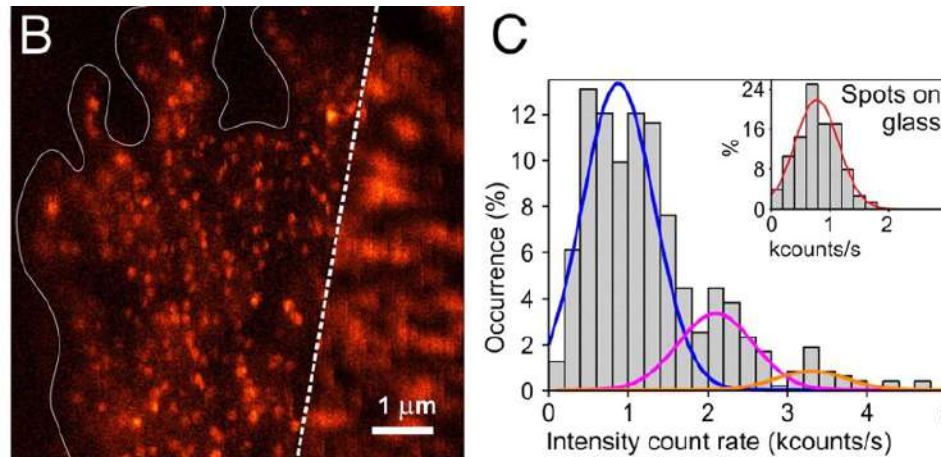
dSTORM



Yan Q...**Wang H.** *PNAS* (2018)

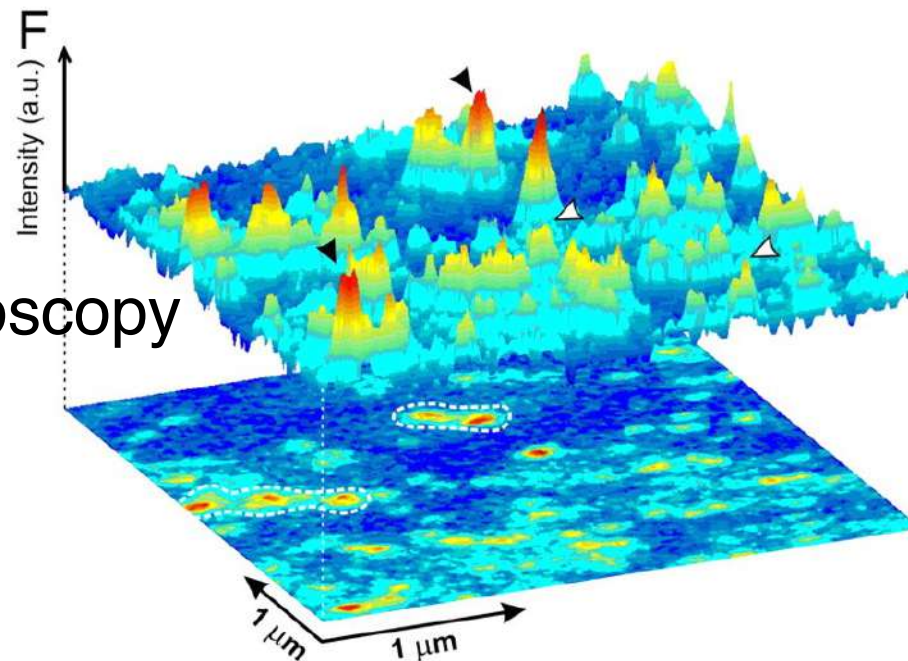
Membrane Protein Clustering

- GPI-anchored proteins



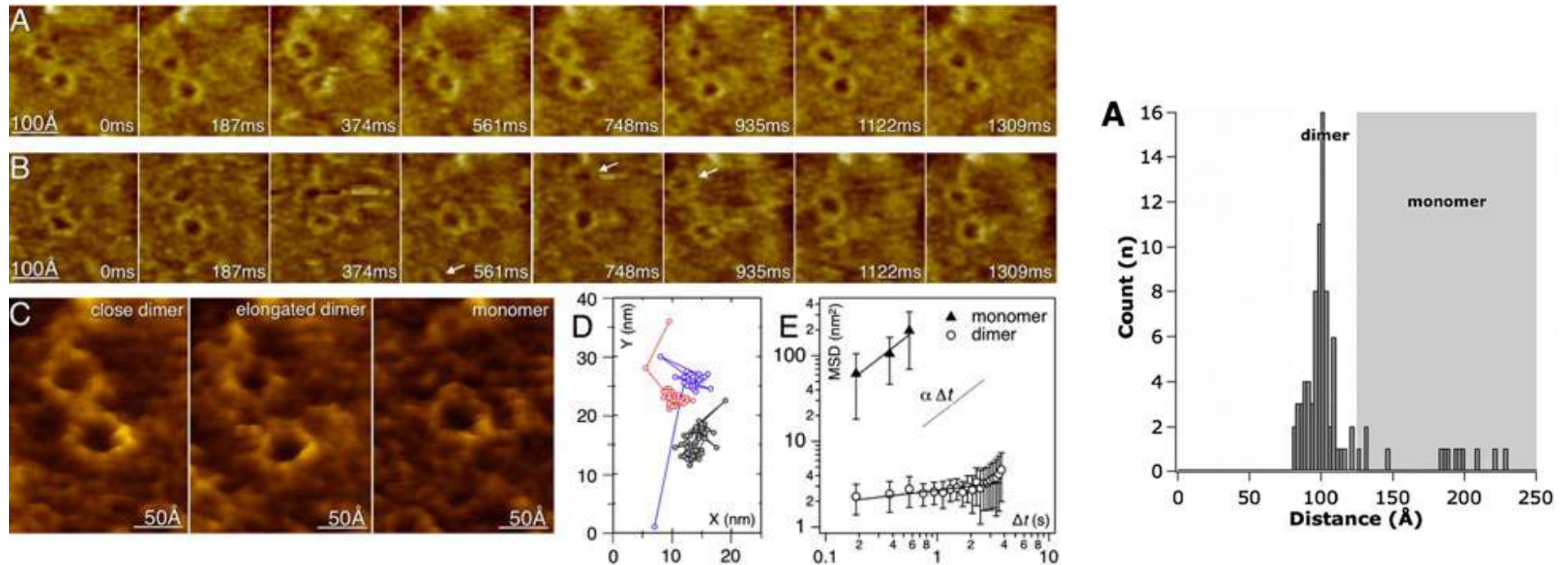
Single-molecule

Near-field Optical Microscopy



Membrane Protein Clustering

Direct visualisation of dimer formation



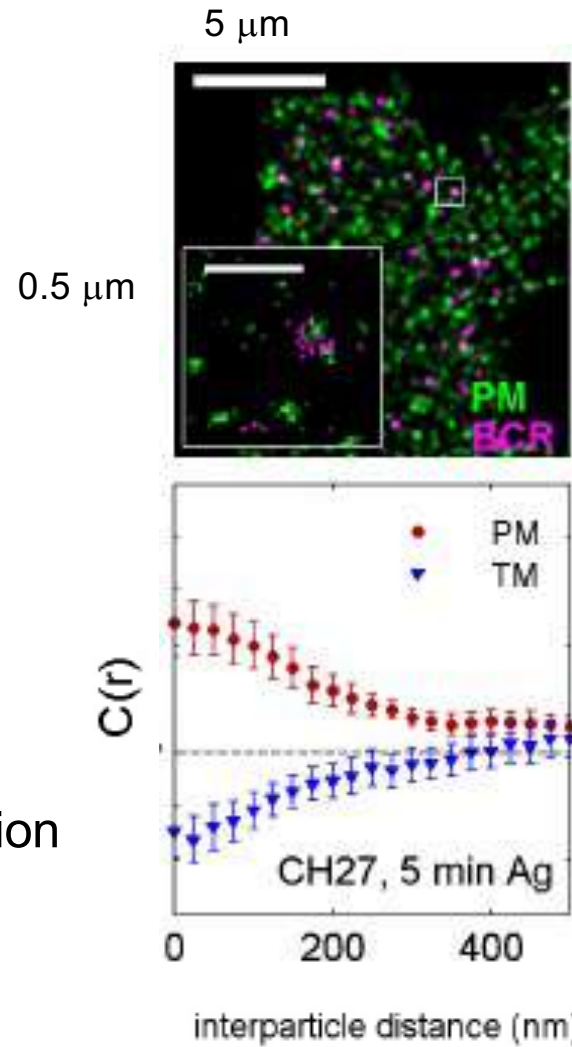
High-speed AFM

C-rings of the ATP-synthase moving in a supported bilayer

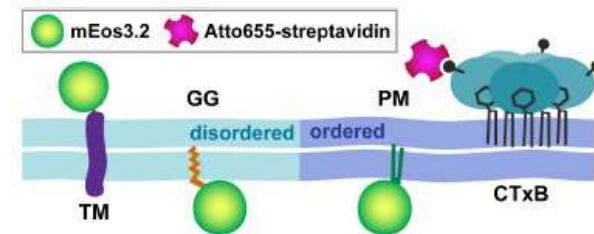
I. Casuso... S. Scheuring *Biophys. J.* (2010)

Role of Rafts in Receptor Clustering

B Cell Receptor
BCR



Super Resolution
Microscopy



Stone M. B... **Veatch S. L.** *Elife* (2017)

Which interactions can lead to protein clustering?

- Many theoretical work on protein on or embedded in membranes
(inclusions)

Much less in vitro work, or evidence in cells (recent)

- "Colloidal interactions" : electrostatic, van der Waals (attractive)
More specific: Hydrophobic, hydrogen bonds

Entropic repulsions between lipid bilayers (Cf. Helfrich)

- But, with fluid 2D membrane:
membrane-mediated interactions between proteins
Due to membrane elastic properties

Long-Range Interactions

EUROPHYSICS LETTERS

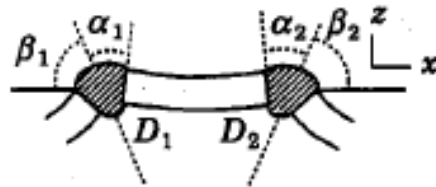
10 April 1993

Europhys. Lett., **22** (2), pp. 145-150 (1993)

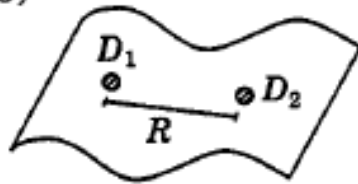
Long-Range Forces in Heterogeneous Fluid Membranes.

M. GOULIAN(*), R. BRUINSMA(**)([§]) and P. PINCUS(*)(**)

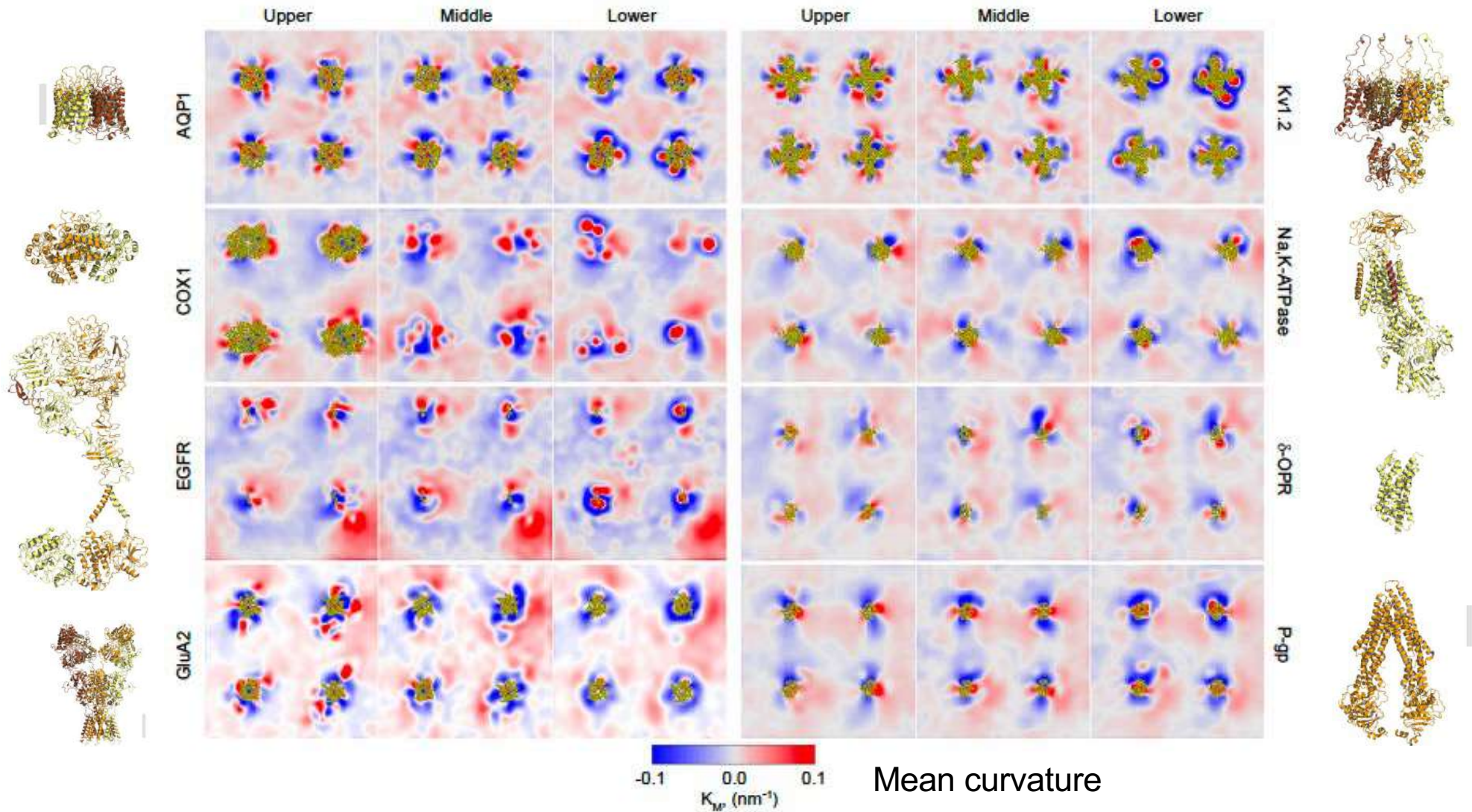
a)



b)



Local Membrane Bending: "Fingerprint" of Membrane Proteins



Long-Range Interactions

EUROPHYSICS LETTERS

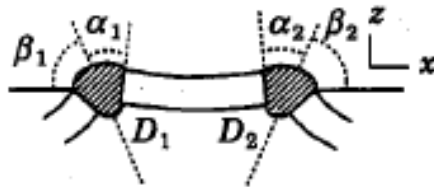
10 April 1993

Europhys. Lett., **22** (2), pp. 145-150 (1993)

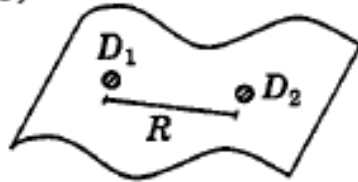
Long-Range Forces in Heterogeneous Fluid Membranes.

M. GOULIAN(*), R. BRUINSMA(**)([§]) and P. PINCUS(*)(**)

a)



b)



$$V^T(R) = \frac{\kappa_B T}{4\pi^2 \kappa_0^2 R^4} \int_{D_1} d^2r \delta\kappa(\mathbf{r}) \int_{D_2} d^2r \delta\bar{\kappa}(\mathbf{r}) +$$

Long range interaction

If $R \gg A$

$$V(R) = \frac{2}{\pi} (2\kappa + \bar{\kappa}) (\alpha_1^2 + \alpha_2^2) \frac{A^2}{R^4}$$

Always repulsive

M. Goulian *Curr. Opin. Colloid Interf.* (1996)

Many follow up theoretical papers and simulations....

- A new type of interaction, for very stiff proteins that *perturb membrane fluctuations (Casimir-like)*

M. Goulian et al. *Europhys. Lett.* (1993)

$$V(R) = -6k_B T A^2 \frac{1}{R^4}$$

Always attractive

Independent of membrane elastic constants

Significant at $R \sim$ a few protein diameter



Fluctuations: peristaltic thickness fluctuations, local protrusion modes, lipid density fluctuations, and fluctuations of lipid tilt

See L. Johannes... J. C. Shillcock. *Trends Cell Biol.* (2018)

- Curvature-mediated force

$$V_c(R) = \frac{2}{\pi} (2\kappa + \bar{\kappa}) (\alpha_1^2 + \alpha_2^2) \frac{A^2}{R^4}$$

For vesicles that do not change topology, the $\bar{\kappa}$ term can be omitted

For identical inclusions:

$$V_c(R) = \frac{8}{\pi} \kappa \alpha^2 \frac{A^2}{R^4}$$

- Fluctuation-mediated force

$$V_f(R) = -6k_B T A^2 \frac{1}{R^4}$$

$$V_c(R) = |V_f(R)| \longrightarrow \alpha = \sqrt{\frac{3}{4\pi} \frac{k_B T}{\kappa}}$$

$$\kappa \approx 25 k_B T \quad \alpha \approx 6^\circ$$

If *large* contact angles α , *curvature* forces dominate

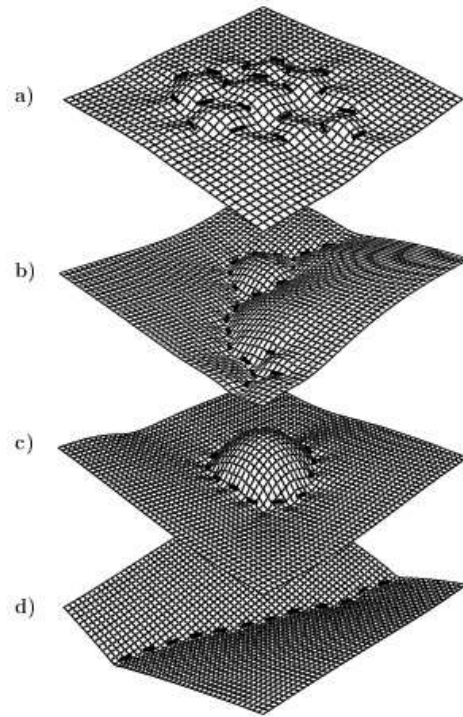
For *quasi-flat* inclusions, *fluctuation* forces dominate

- *Multi-body effects*

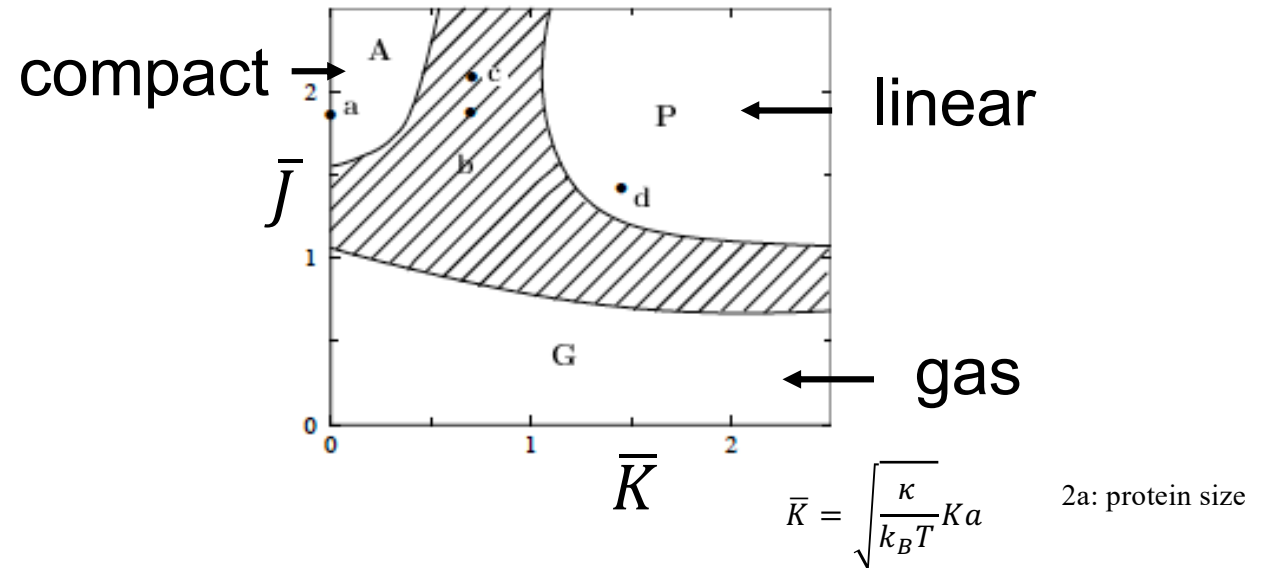
Inclusions:

$\bar{K}$ mean curvature)

$\bar{J}$ mean Gaussian (anisotropic) curvature)

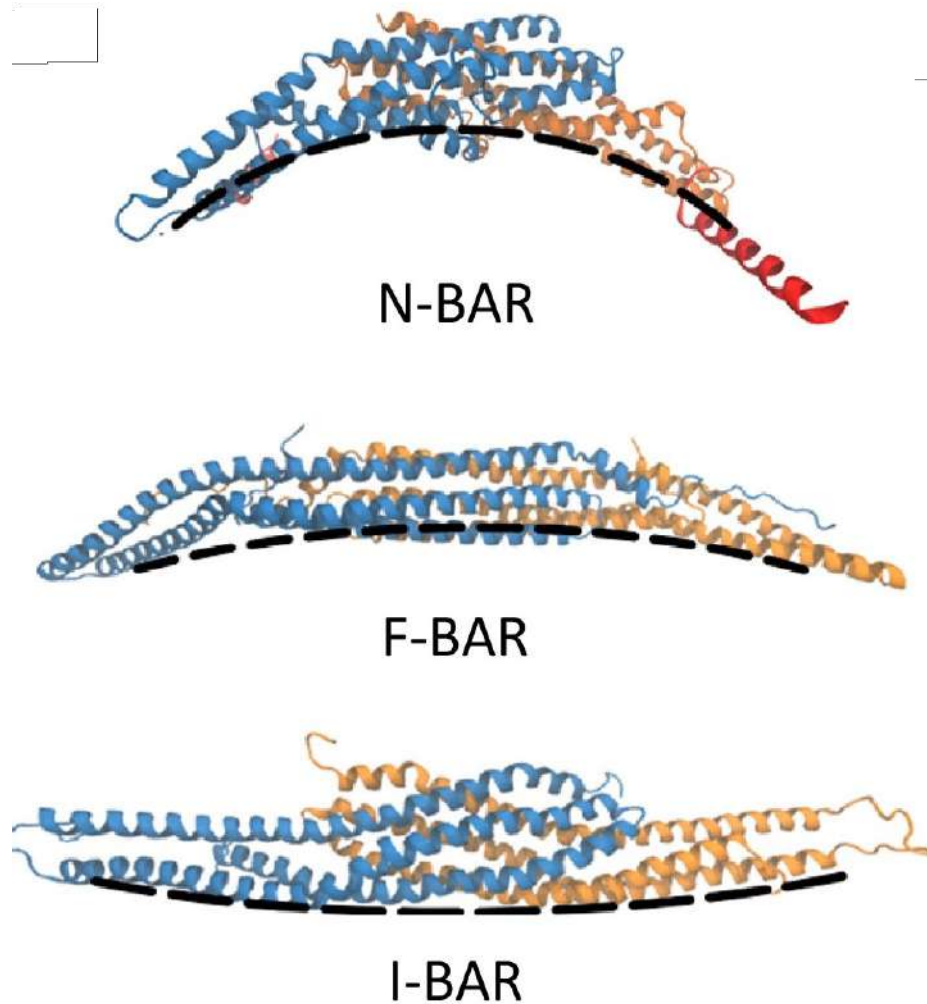


Monte Carlo simulations



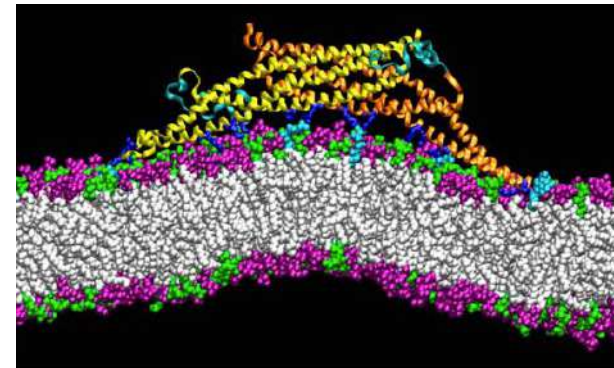
BAR-Domain Proteins:

Dimers with Various Intrinsic Curvatures



15 nm

Bind to
negatively-charged membranes
(PS, PI(4,5)P₂ etc...)

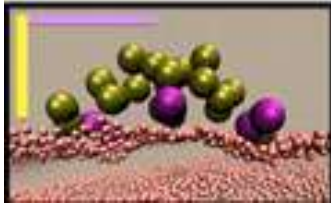


Blood P *et al*
Biophys. J. (2008)

M. Simunovic *et al*, *Trends Cell Biol.* (2015)

Local Membrane Deformation Induces Long Distance Protein-Protein Interaction

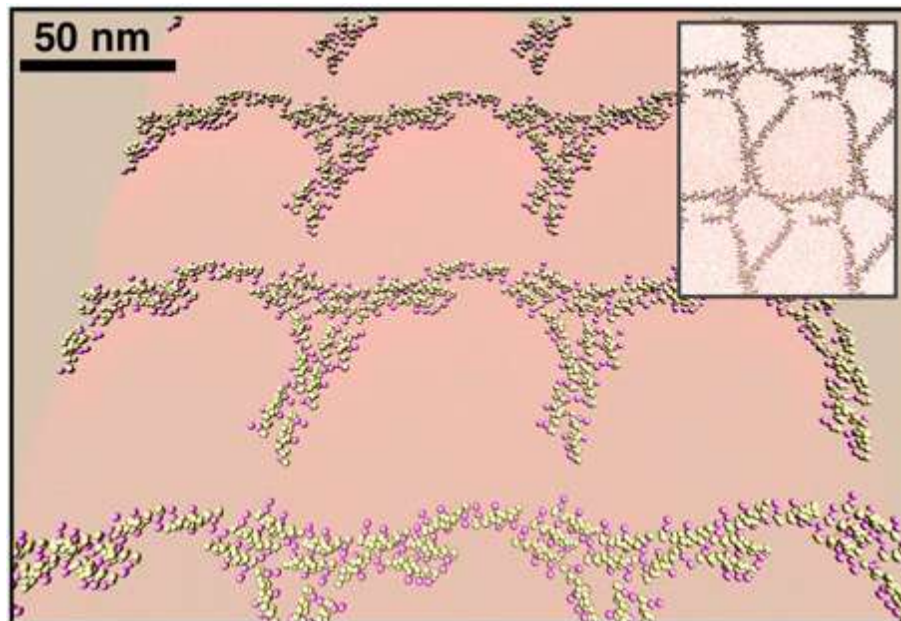
M. Simunovic, G. Voth (U. Chicago)



Coarse Grained model
of N-BAR (endophilin)

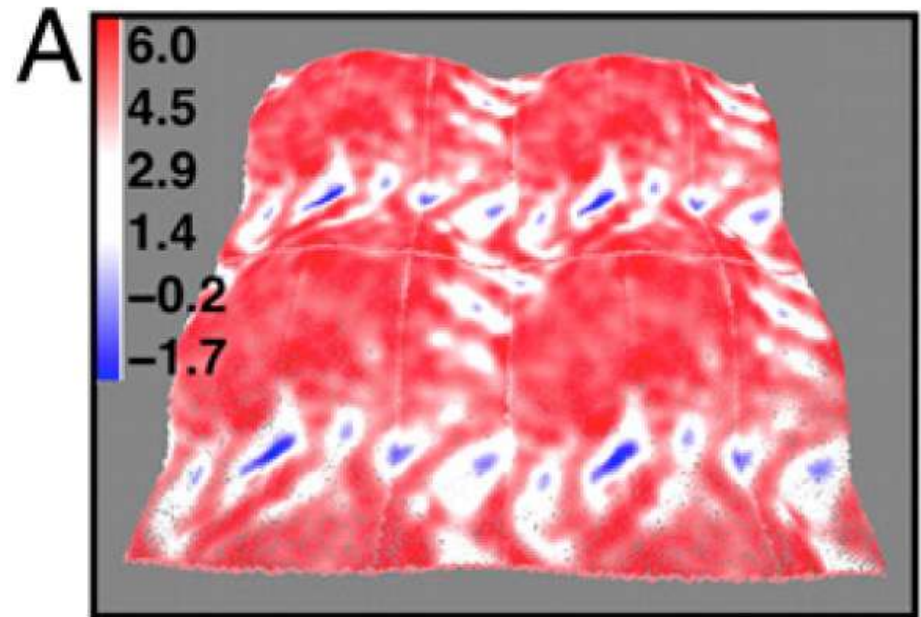


Proteins: Linear organization



$\phi = 18\%$

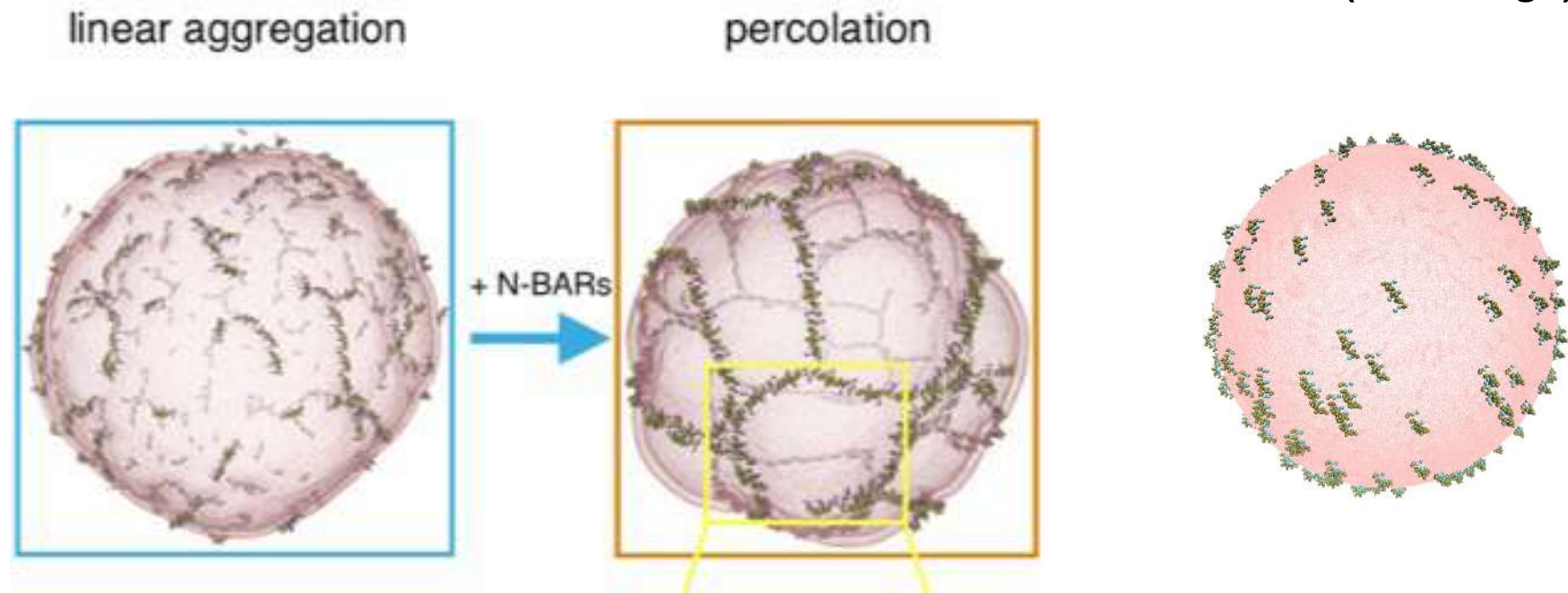
Membrane local mean-curvature



Simunovic, Srivastava, Voth, *PNAS* (2013)

Membrane Mediated N-BAR Assembly

M. Simunovic,
G. Voth (U. Chicago)

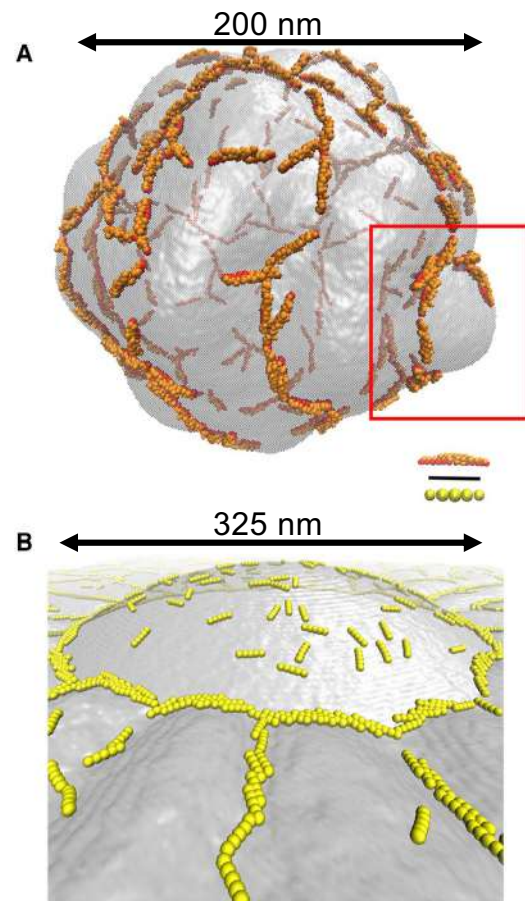
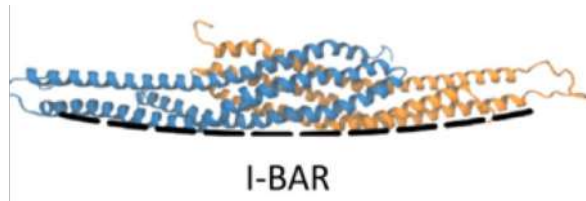


Simunovic, Srivastava, Voth, *PNAS* (2013)

Simunovic, ..., Voth, *Biophys J.* (2013)

Simunovic, Voth, *Nat. Commun.* (2015)

Membrane Mediated I-BAR Assembly

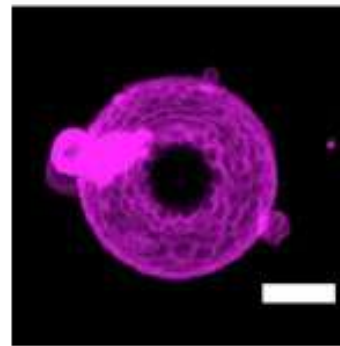


IRSp53

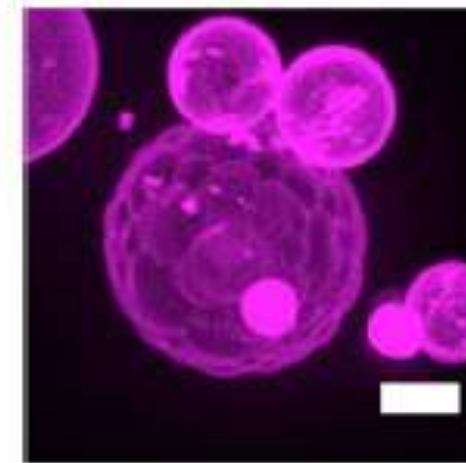
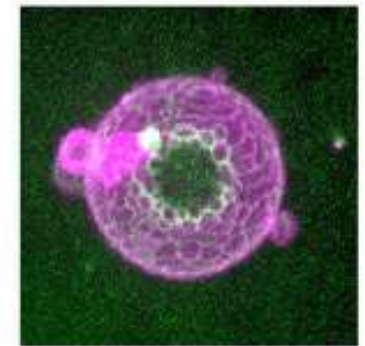
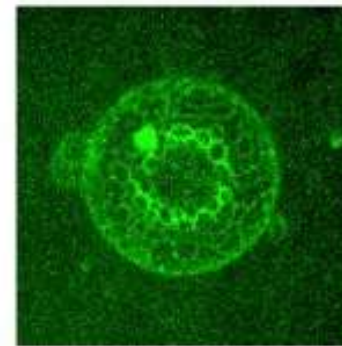
Lipids

IRSp53

maximum intensity
projection



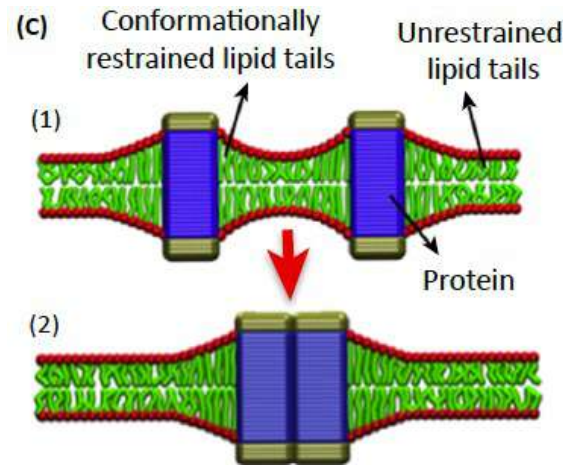
5 μ m



5 μ m

Short Range Interactions

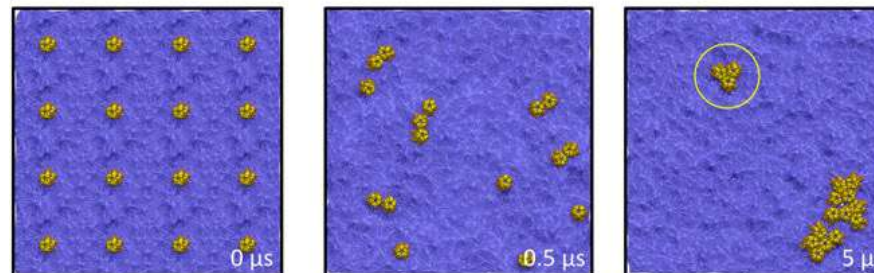
- Local membrane thickness deformations (hydrophobic mismatch)



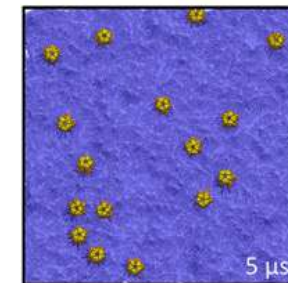
Many models

See A.-F. Bitbol...J.B. Fournier in
Physics of Biological Membranes (2018)

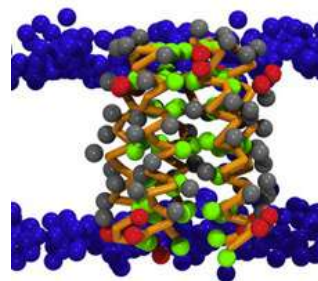
Positive mismatch



No mismatch



12 nm

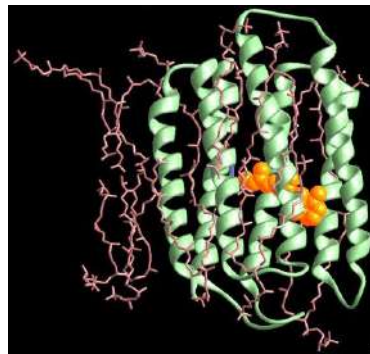


Gα

Martini force field

D.L. Parton...M. S. P. Sansom. *Biophys. J.* (2011)

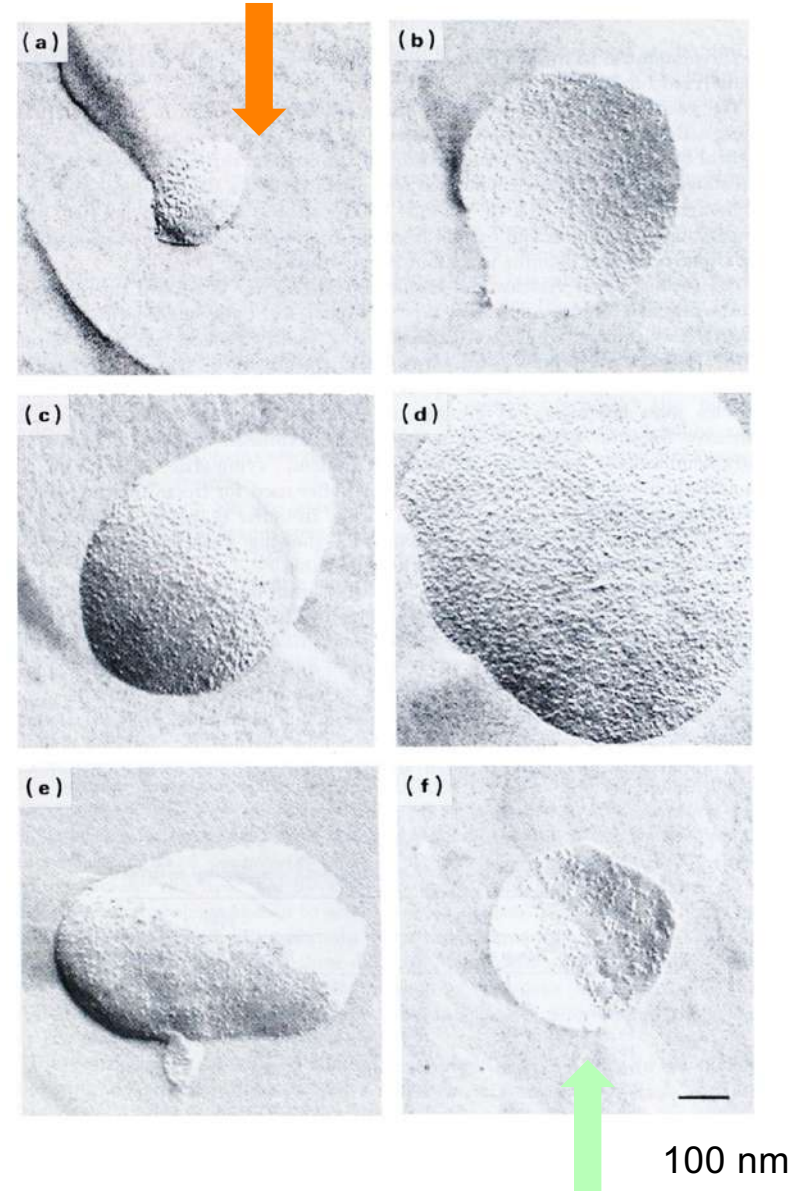
Bacteriorhodopsin Aggregation due to Mismatch



Hydrophobic part
~30 Å

Phosphatidilcholine vesicles

Acyl chain	Lipid t_m (°C)	Temperature (°C)	HC thickness (Å)†	Distribution
10:0	0	15	15.5	Aggregated
12:0	-1.8‡	22	19.5	Dispersed
14:0	23‡	34	23	Dispersed
16:0	41.4§	50	26	Dispersed
18:0	54.9§	60	29.5	Dispersed
22:1	11	35	34	Dispersed
24:1	24	45	37.5	Dispersed, aggregated and ordered arrays

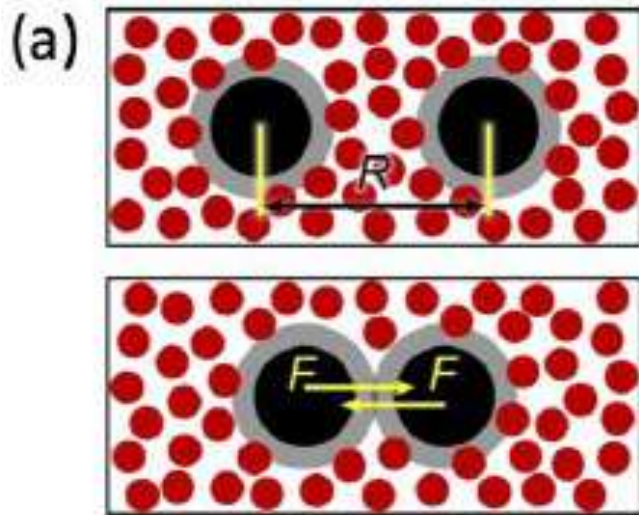


Large mismatch (+/-) required

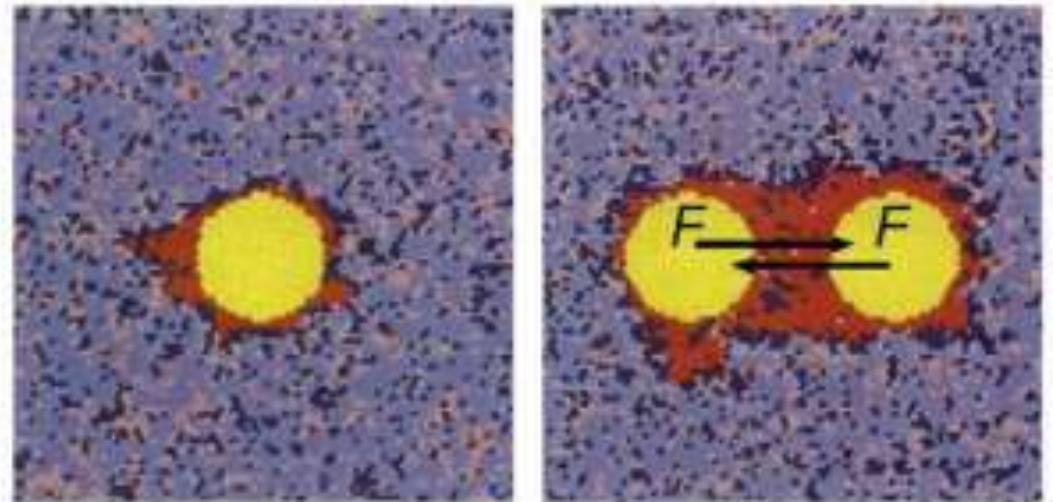
Short Range Interactions

Depletion/Capillary Force

"Wetting" Force



(c)



Multicomponent membrane

Destainville N et al *Current topics in membranes* (2016)



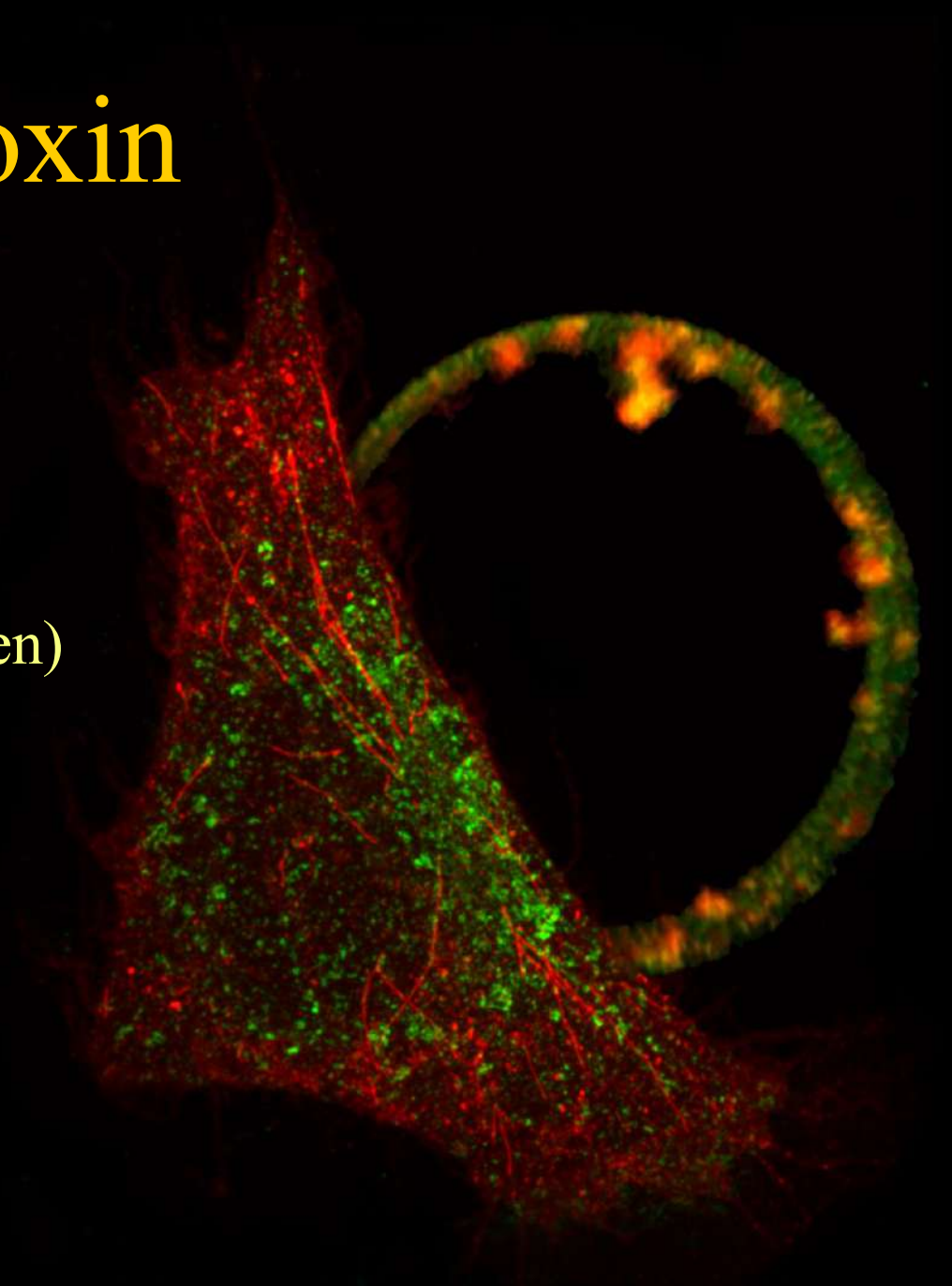
Attraction

ShigaToxin

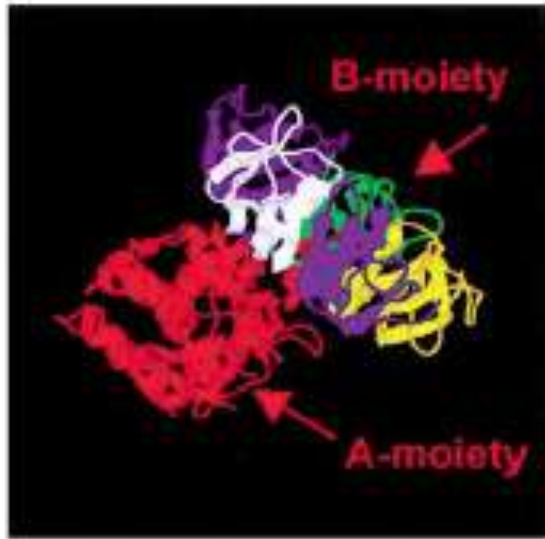
Collaborators:

L. Johannes (I. Curie)

W. Pezeshkian, J. Ipsen (Copenhagen)

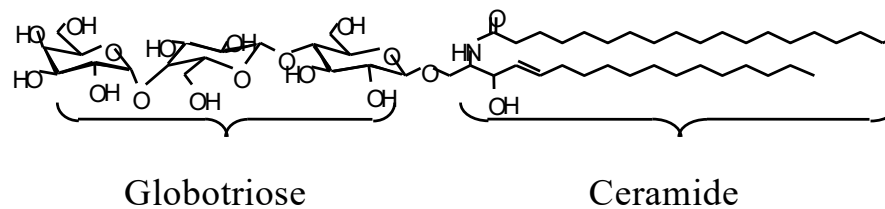


Shiga Toxin (STxB)

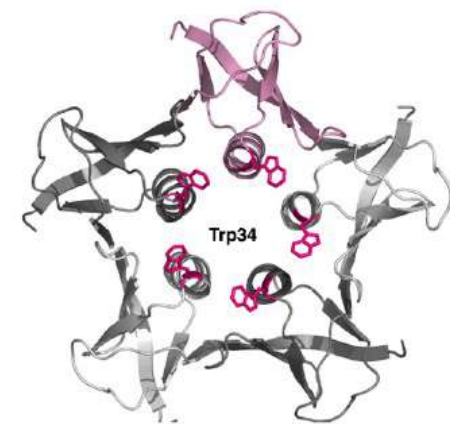


- B moiety: pentamer
- "Toxin transporter"

- Receptor = Gb3 LIPID



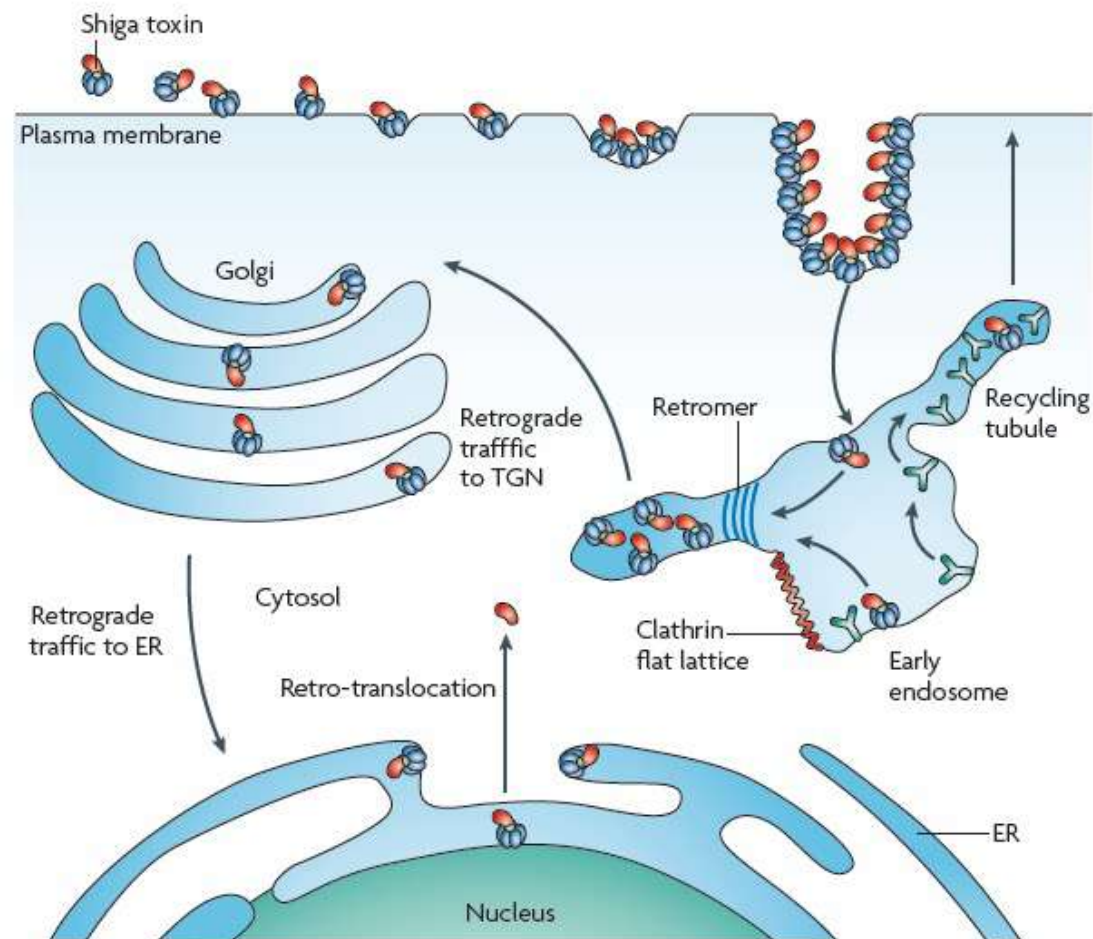
- 1 STxB pentamer $\longleftrightarrow$ 10-15 Gb3



Top view of B pentamer

Shiga Toxin Endocytosis

Shiga-toxin: Clathrin-independent endocytosis mediated by binding to its lipid ligand Gb3

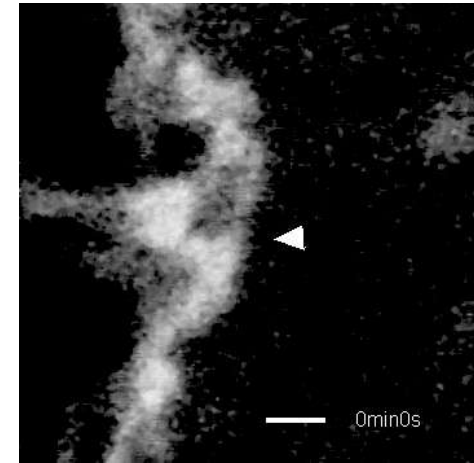
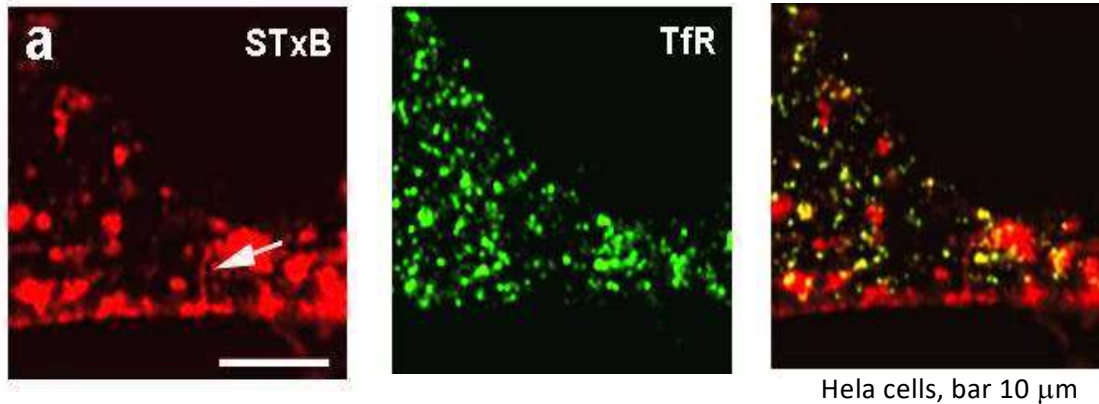


Similar for **Cholera-toxin** (binding to GM1)

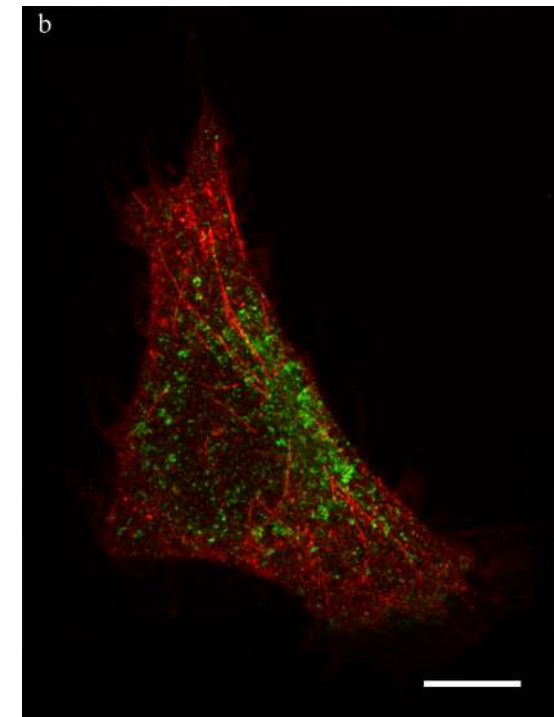
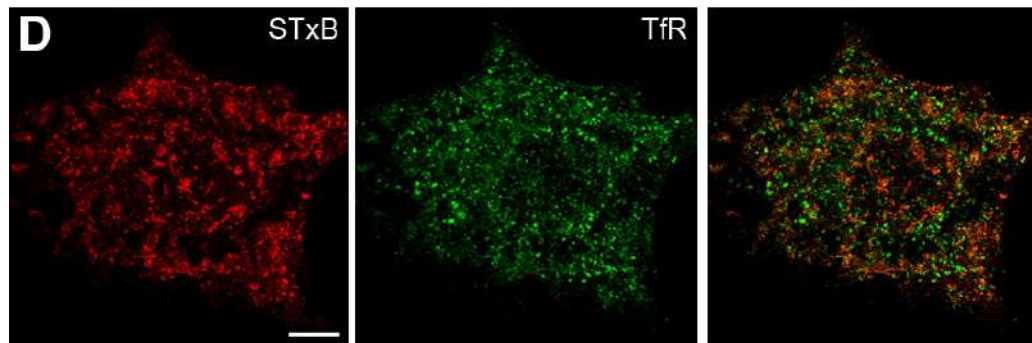
Tubular Structures for Toxin Endocytosis

W. Römer, L. Johannes

Toxin entry:



ATP-depleted HeLa cells : More tubes

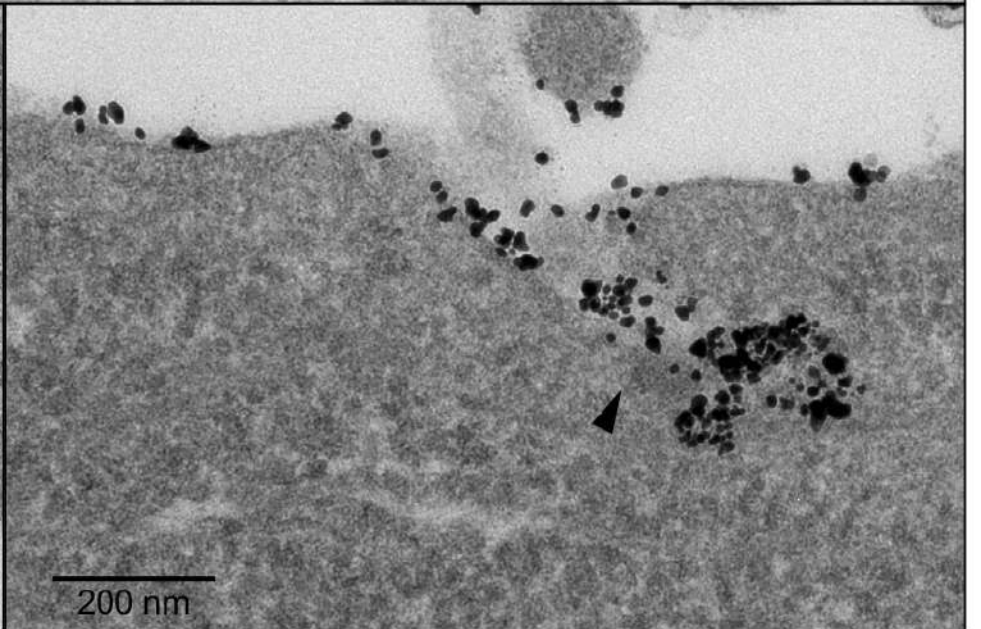
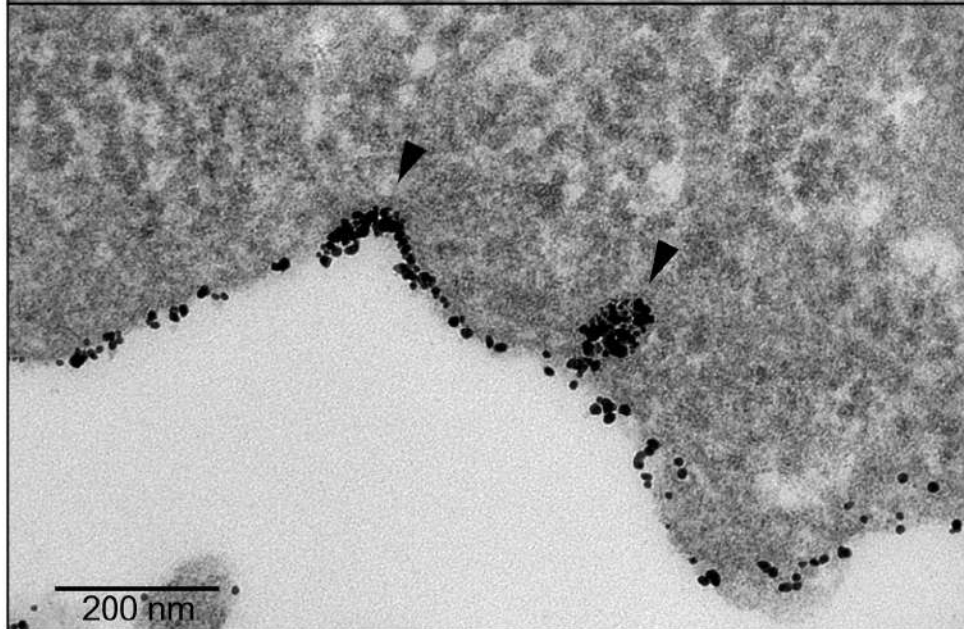
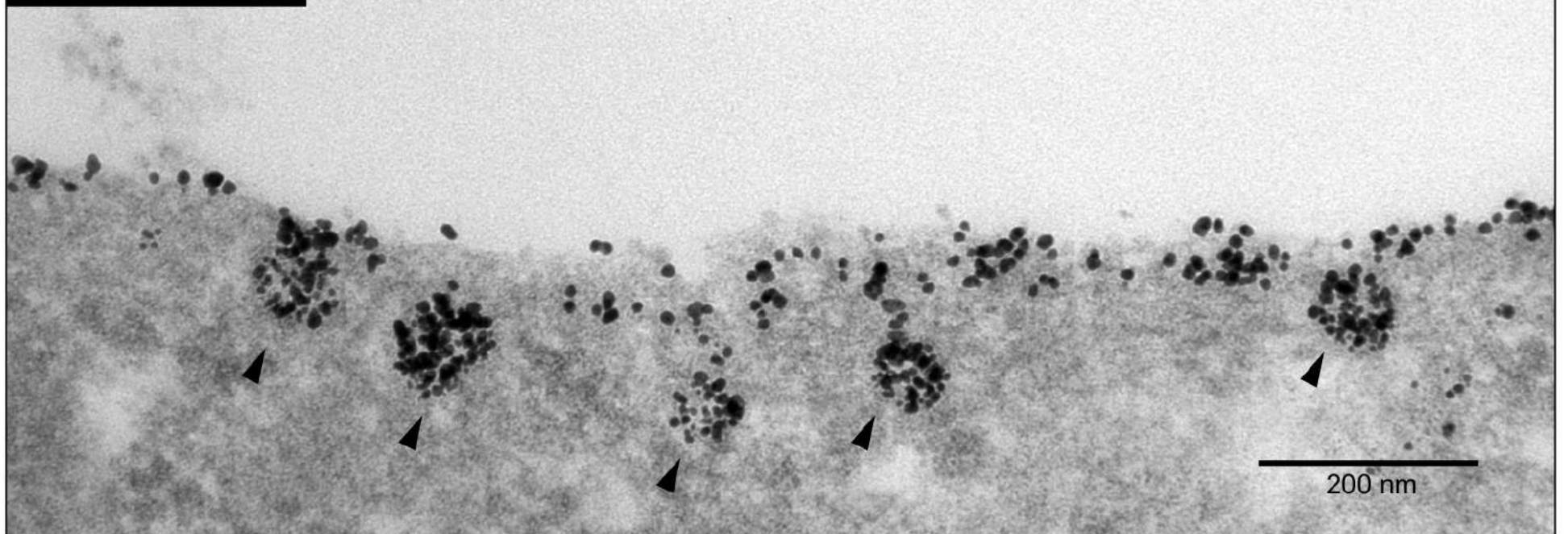


Similar tubes if interfering with fission
(dynamin)

STxB ⇌ Membrane tubulation?
Mechanism ?

W. Römer et al, Nature (2007)

-ATP / +Nocodazole

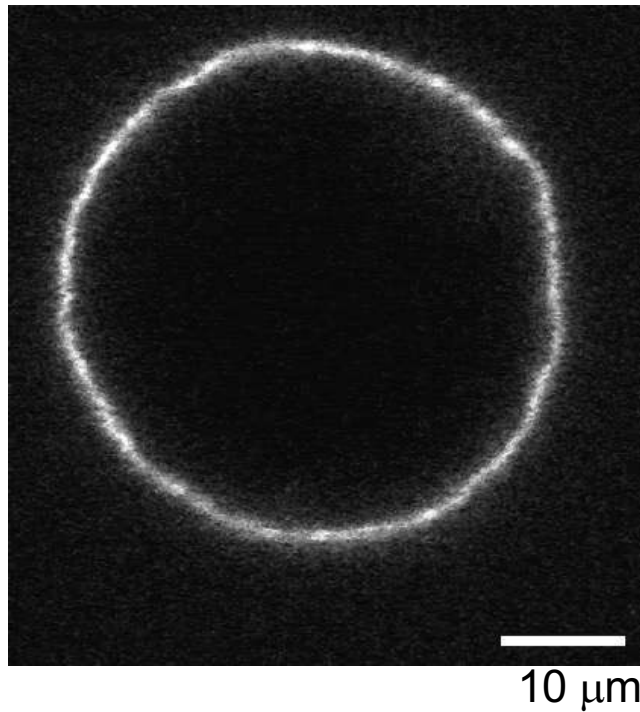


Similar Tubular Structures with Model Membranes

GUVs: DOPC + 30% Chol + 5 % Gb3

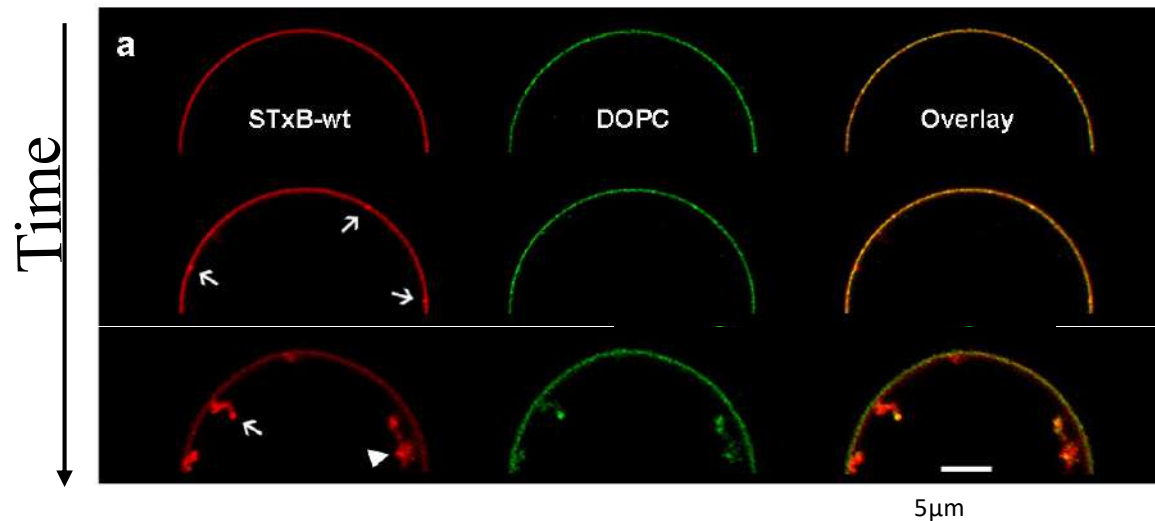
+ STxB (200 nM)

STxB



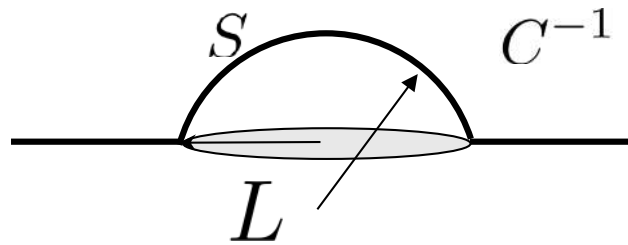
X3 accelerated

STxB alone Tubulates Membranes



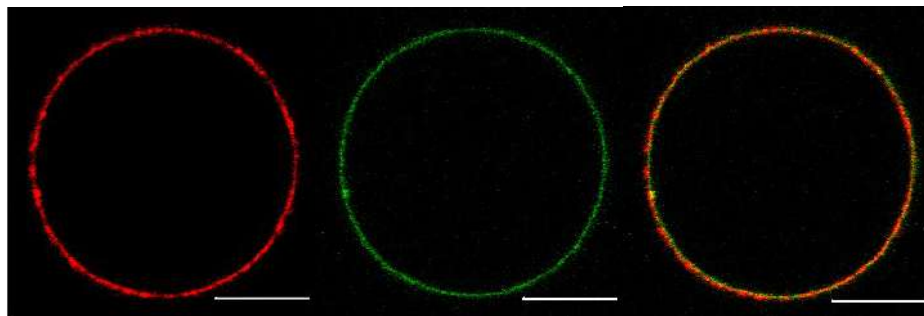
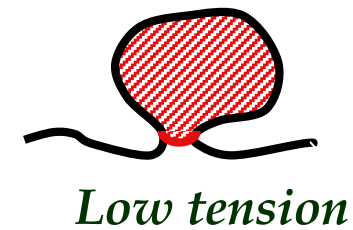
- 1 : Fast **uniform binding** of STxB
- 2 : Small **domains/cluster** of STxB
- 3 : **If initially low membrane tension:**
tubular deformations

Effect of Membrane Tension



$$F = \gamma_L 2\pi L + \frac{1}{2} \kappa S (C - C_0)^2 + \sigma (S - \pi L^2)$$

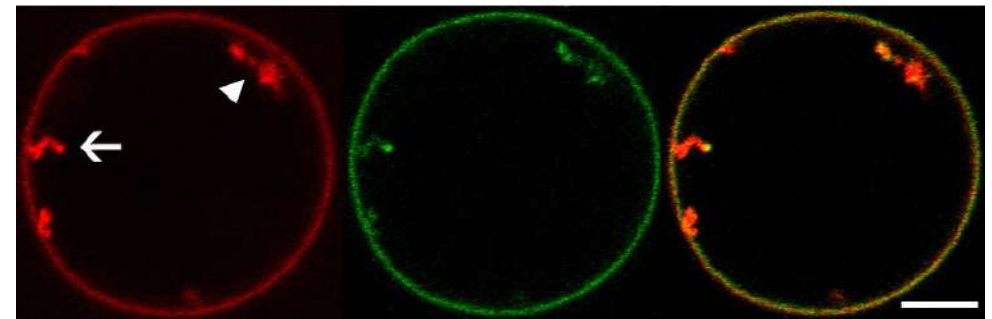
P. Sens, M.S. Turner *Phys. Rev. E* (2006)



STxB

Membrane

No tubule
STxB clusters

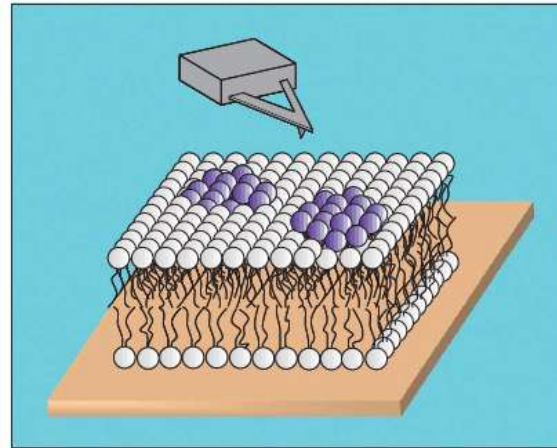


10 μm

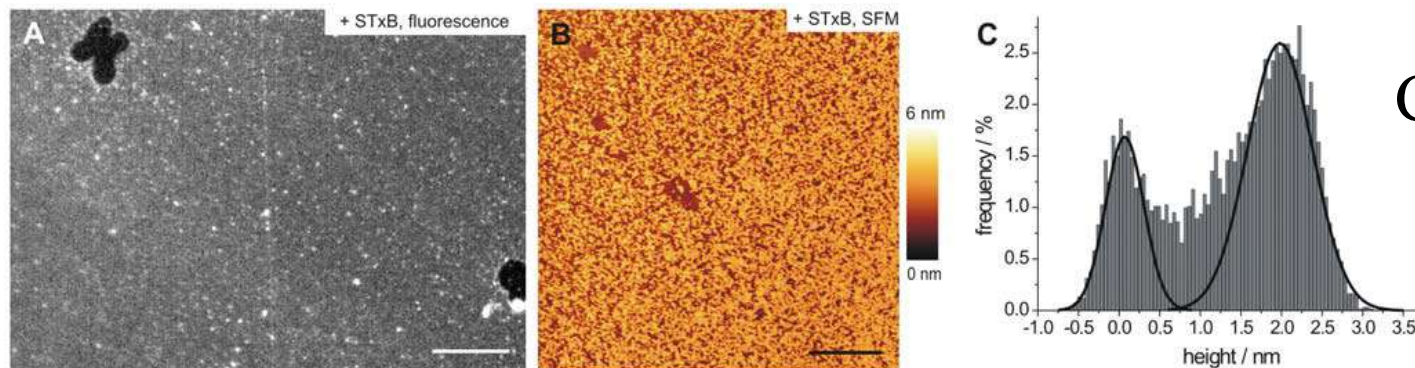
Tubules

STxB Clusters on Supported Membranes

AFM on SLB



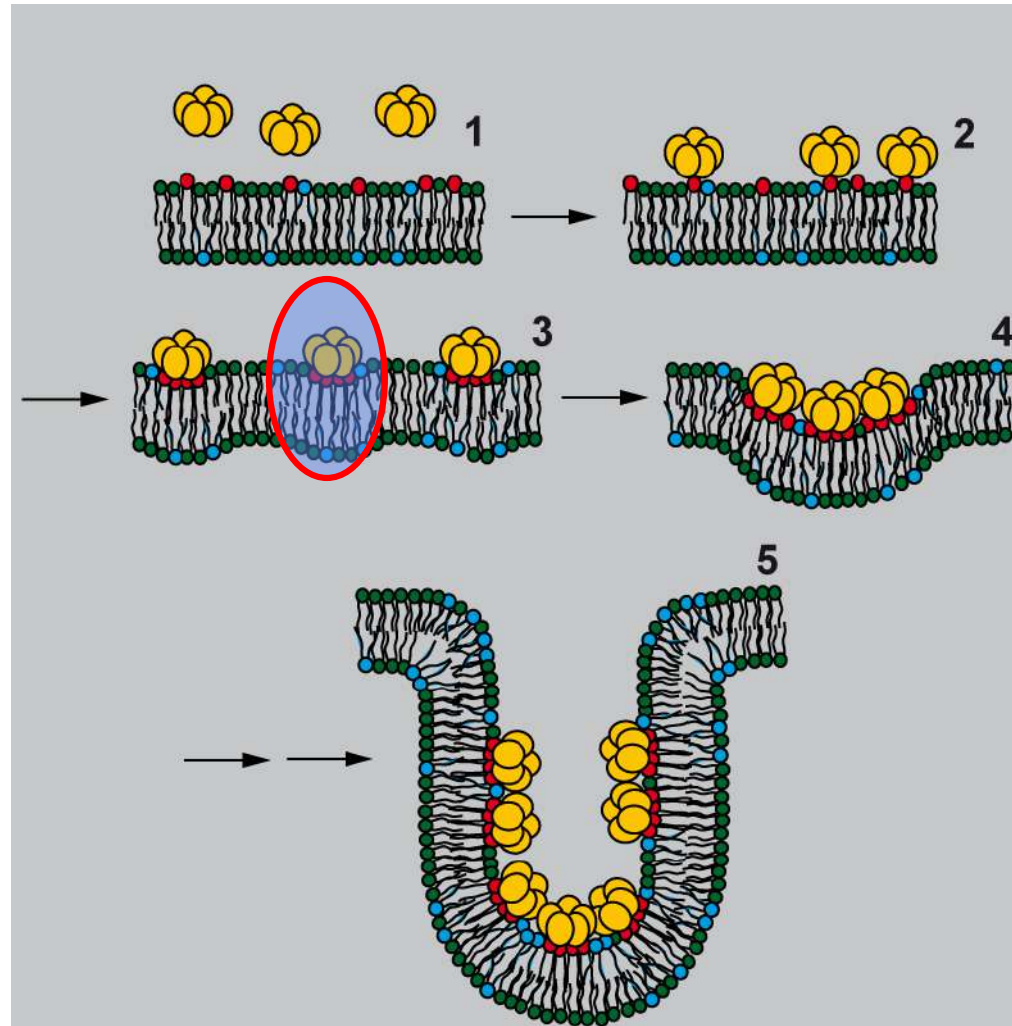
From M.-P. Mingeot-Leclercq et al.
Nat. Protoc. (2008)



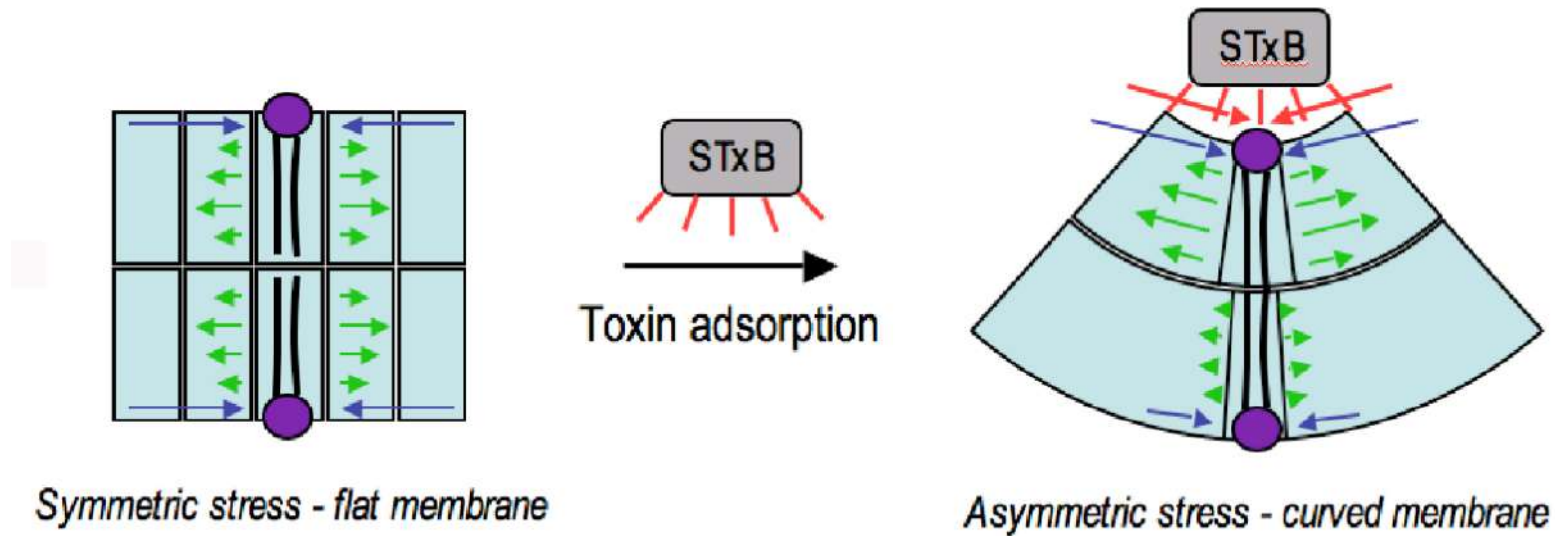
Clusters

B. Windschiegl....C. Steinem *PLoS ONE* (2009)

Shiga Toxin-induced Endocytic Pit Construction



Membrane Bending

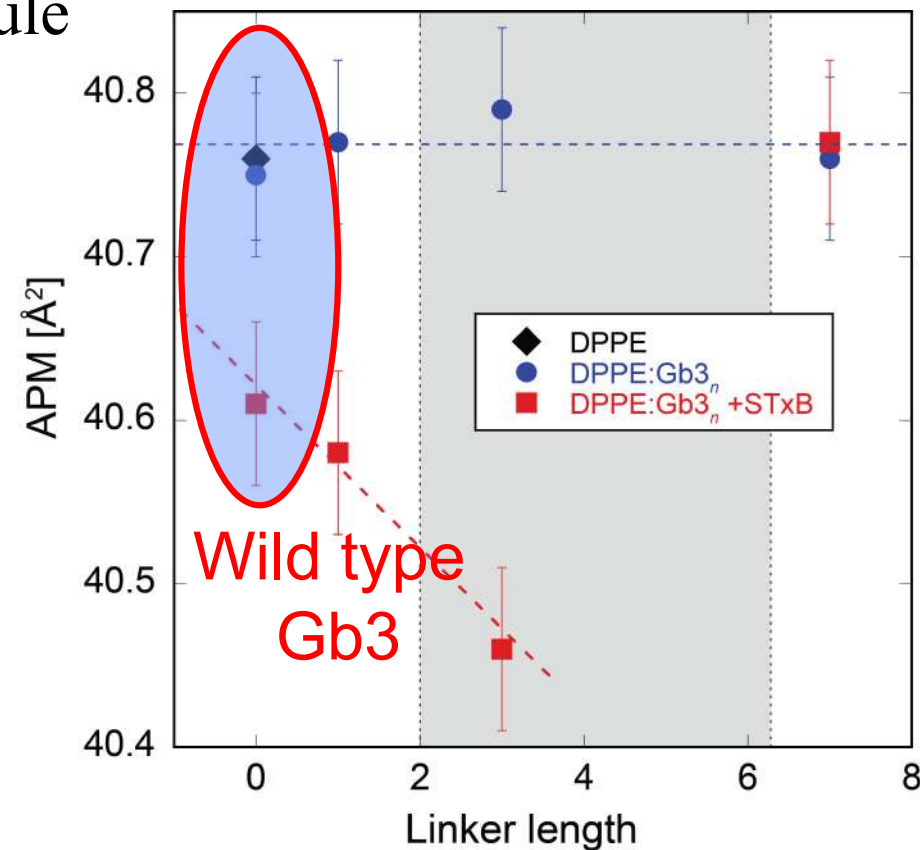


STxB induces Gb3 compaction on the external leaflet

STxB Induces Lipid Compression on One Leaflet

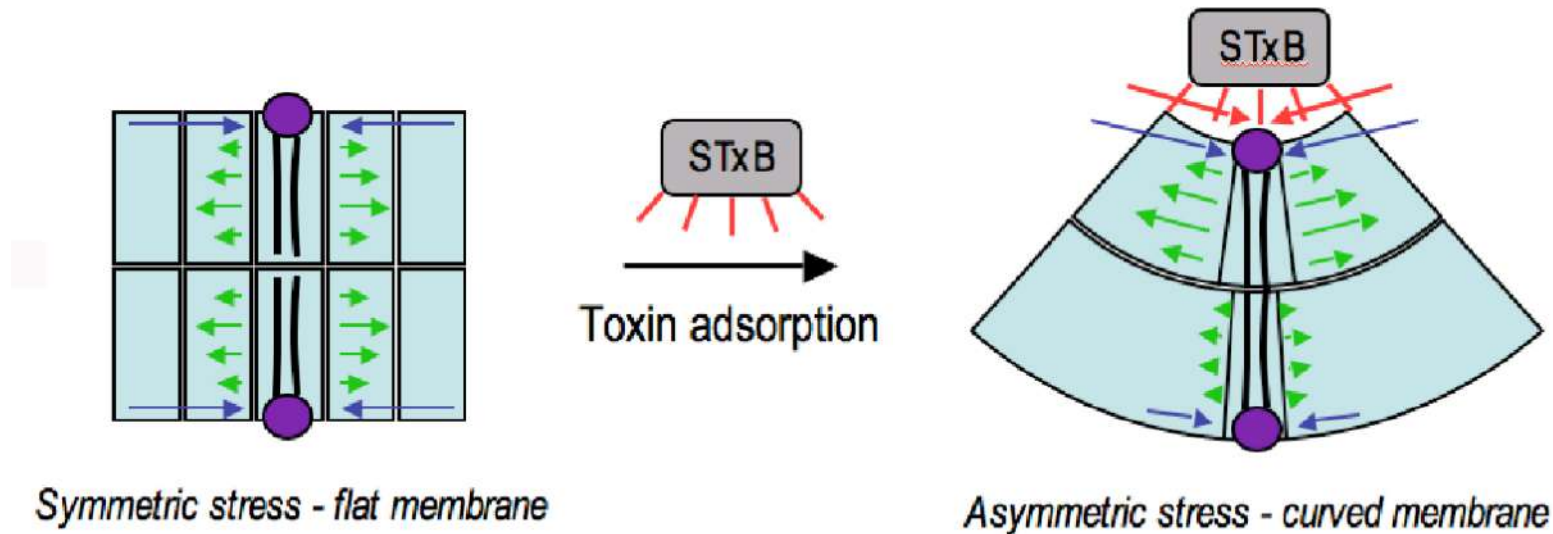
X-ray surface scattering – Monolayer on water

Area per Molecule



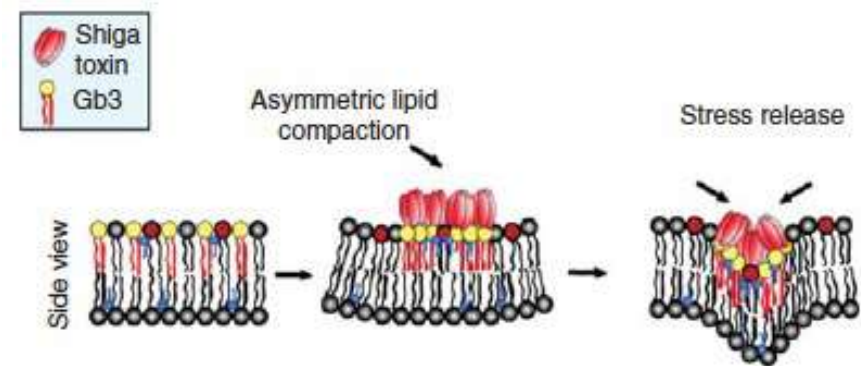
E.B. Watkins ... L. Johannes *Nano Lett.* (2019)

Membrane Bending



STxB induces Gb3 compaction on the external leaflet

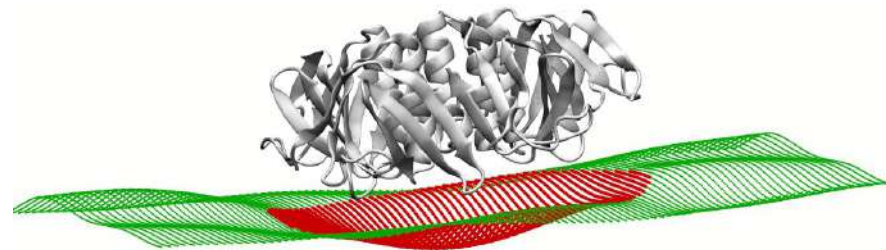
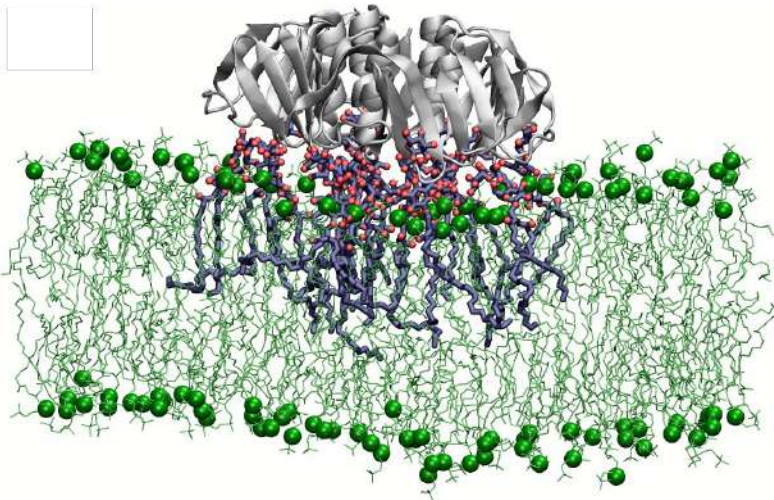
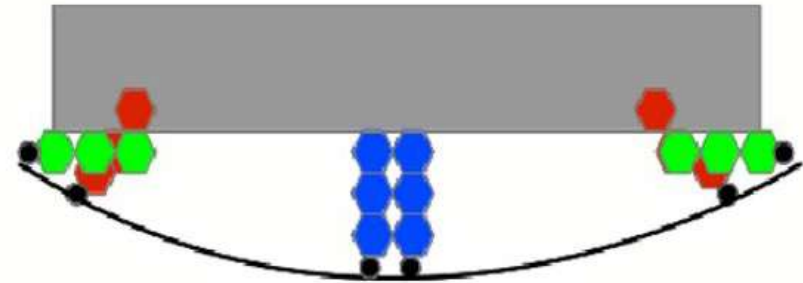
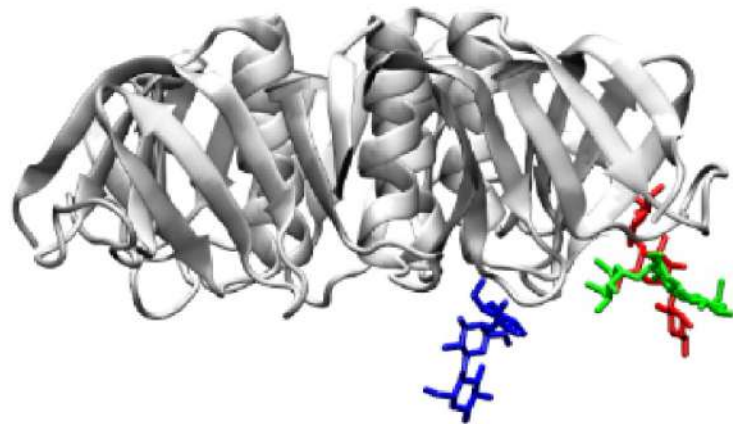
➡ Negative spontaneous curvature



Membrane Bending: Molecular Scale

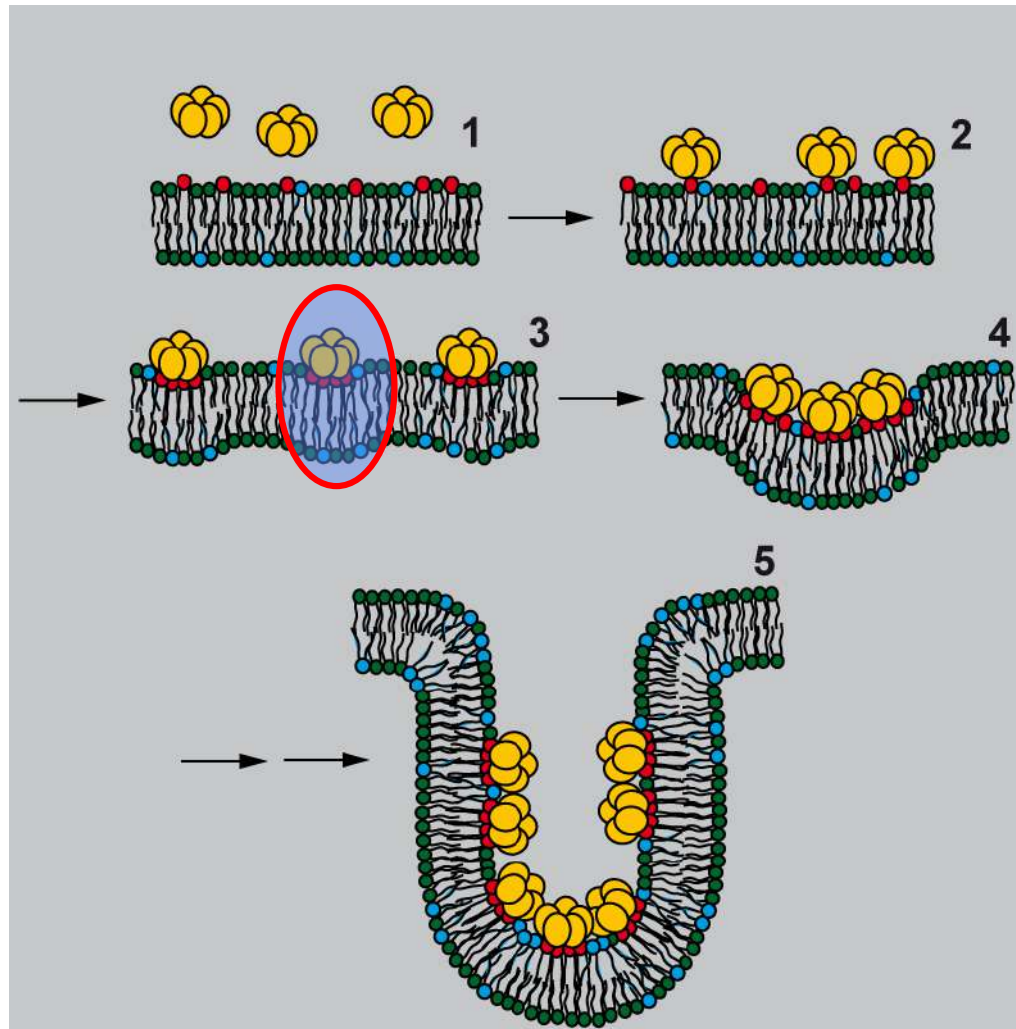
STxB binding → Gb3 lipid tilt

→ Negative membrane curvature



Membrane Bending

- Toxin-lipid geometry
- Asymmetric membrane compression

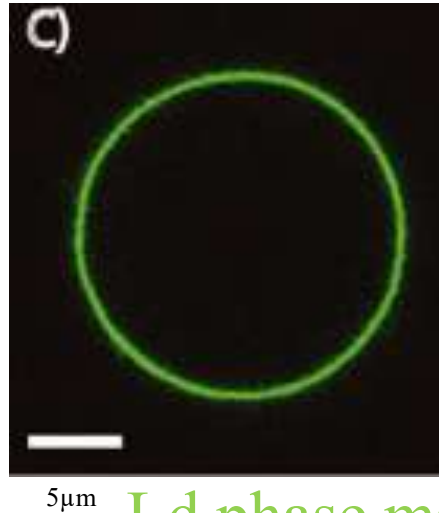


New mechanism for clathrin-independent endocytosis:
Cargo-Mediated budding

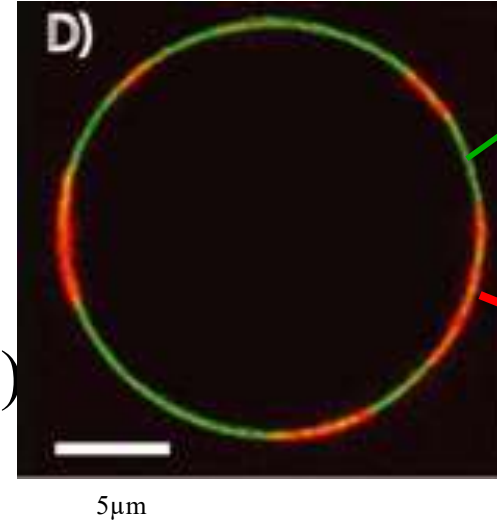
Lipid Composition in Tubules ?

DOPC:Chol:SM + 5% Gb3 :
(41:32:21)

Homogeneous



+ STxB
→
(200 nM)



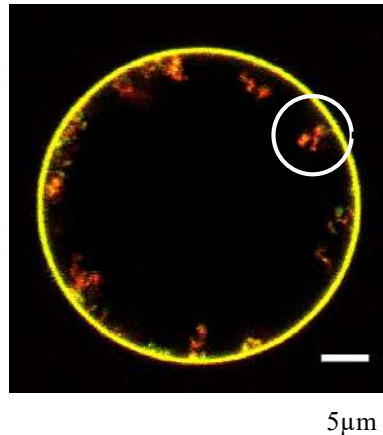
L_d phase:
PC- rich

STxB
in L_o phase:
SM- rich

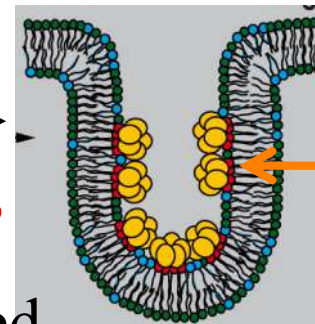
L_d phase marker

STxB : induction of *SM-rich* environment

In tubules?



STxB
enriched



Enriched
in SM ?

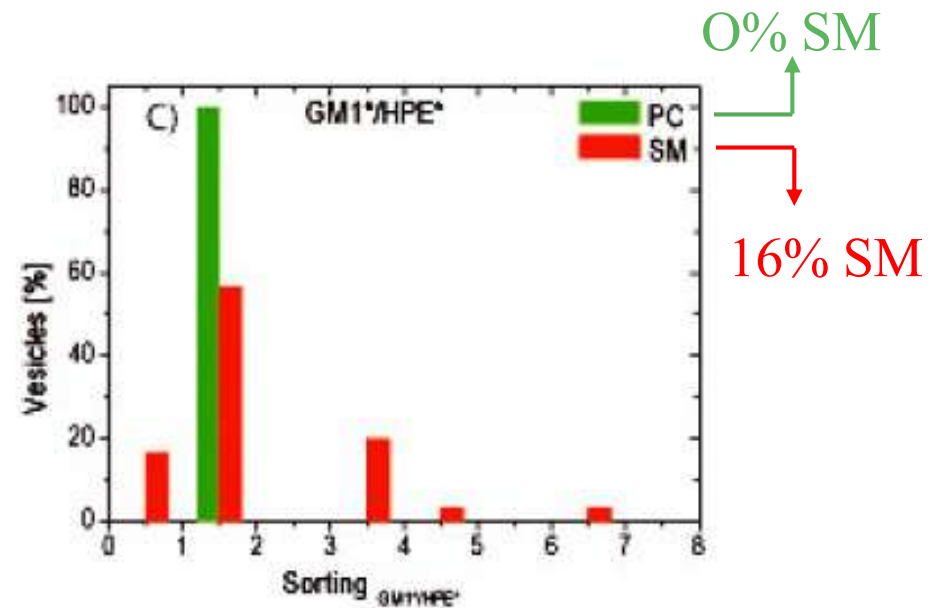
SM Enriched in STxB-induced Tubules

2 fluorescent lipid analogs:

GM1*: No phase preference

HPE*: Ld phase

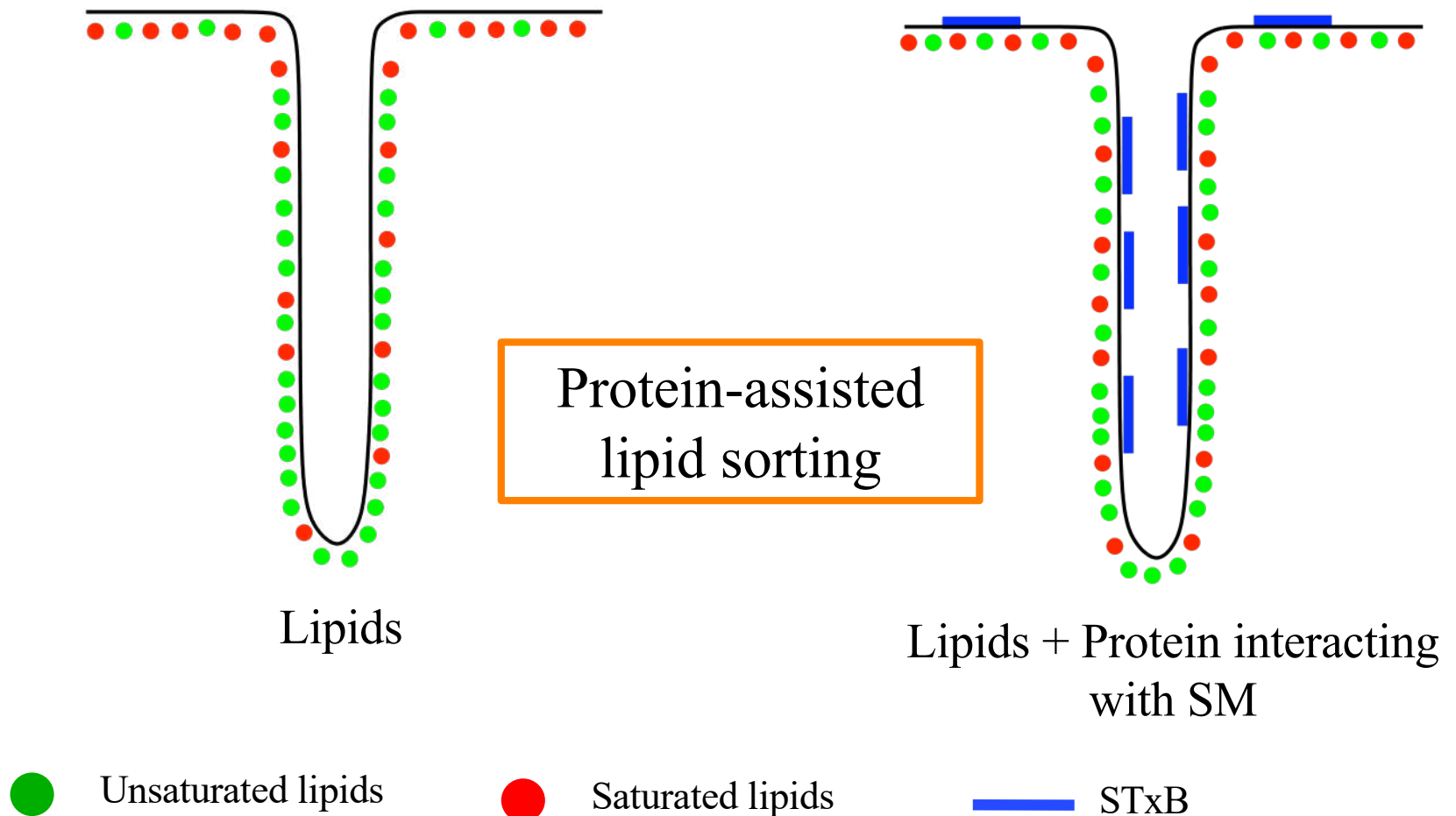
$$Sorting_{GM1^*/DHPE^*} = \frac{I_t^{GM1^*} / I_t^{DHPE^*}}{I_v^{GM1^*} / I_v^{DHPE^*}}$$



➡ *SM enriched in the tubes*

Confirmed in vivo (Laurdan experiments)

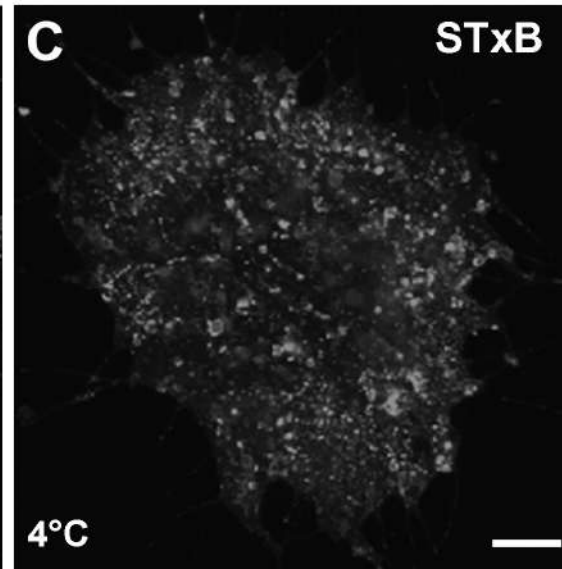
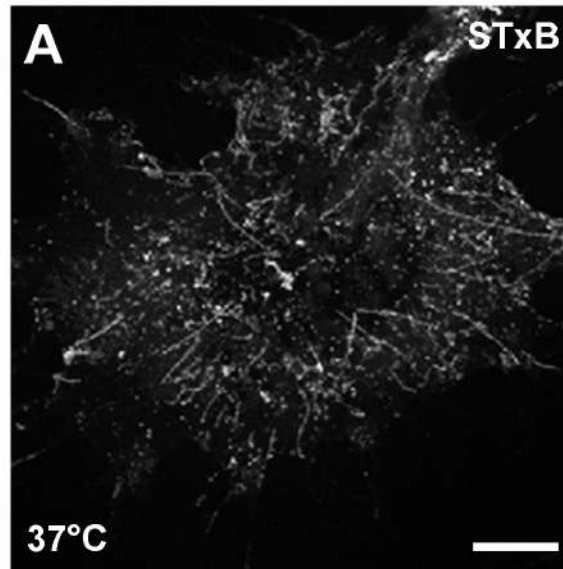
Enrichment of Gb3 by STxB in the Tubes drives SM Enrichment in a Curved Membrane



Interaction (direct or indirect) with proteins can influence lipid sorting

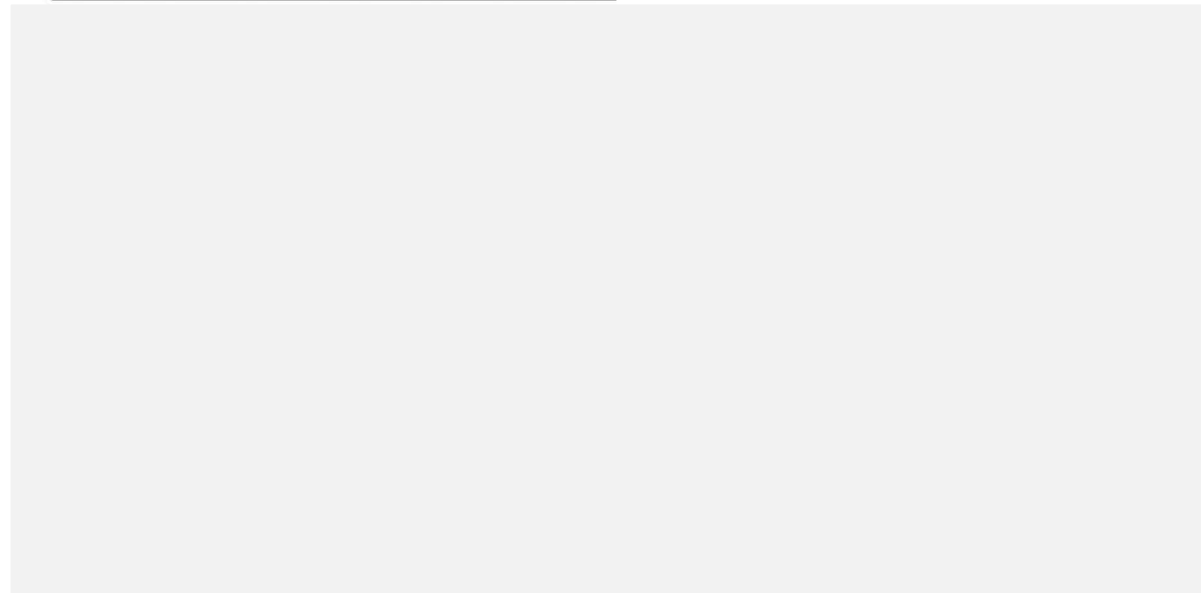
Temperature-induced Scission of STxB Tubules

**37°C
Control**



**4°C
Control**

**37°C
- Cholesterol**

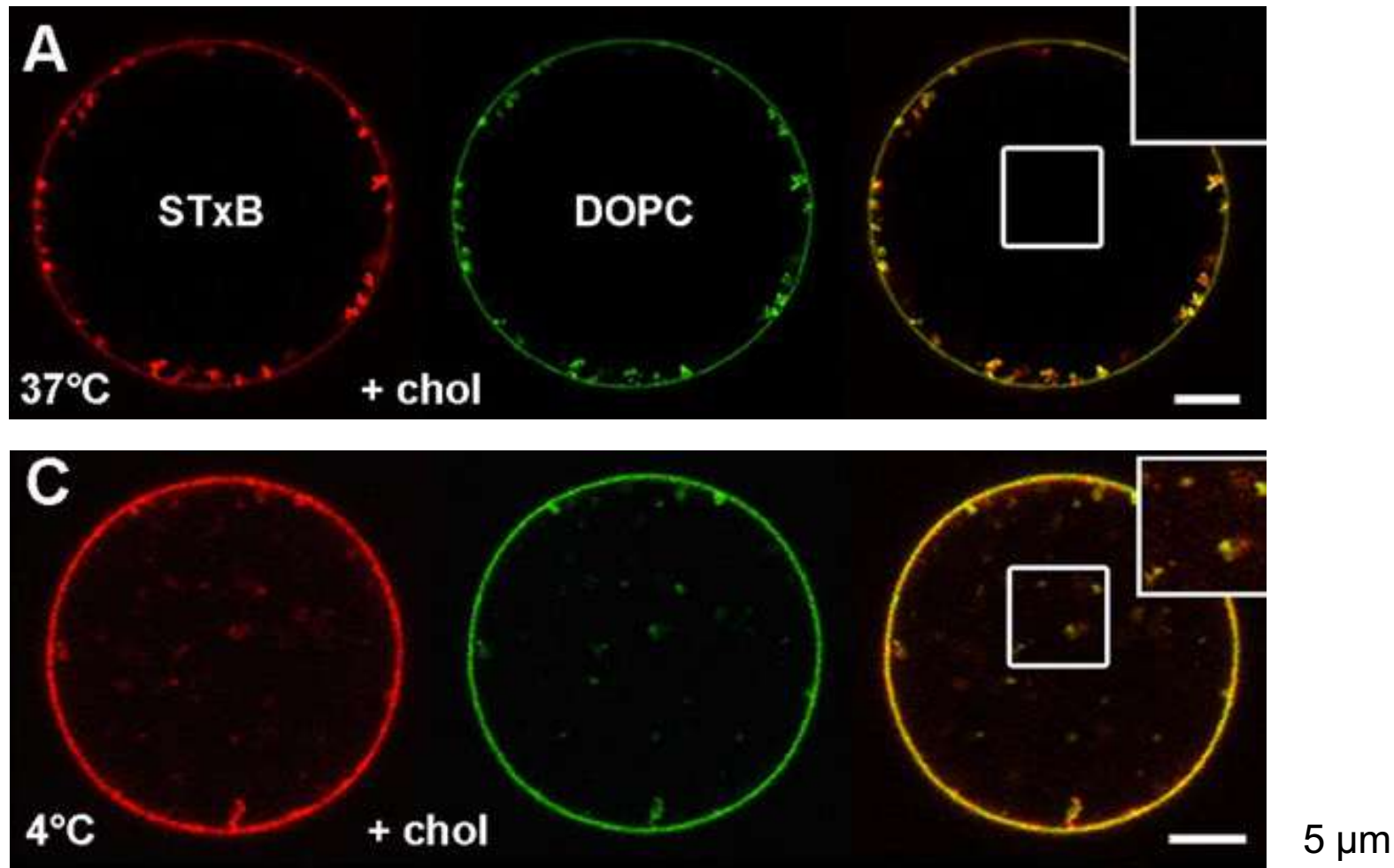


**4°C
- Cholesterol**

But not if cholesterol is decreased

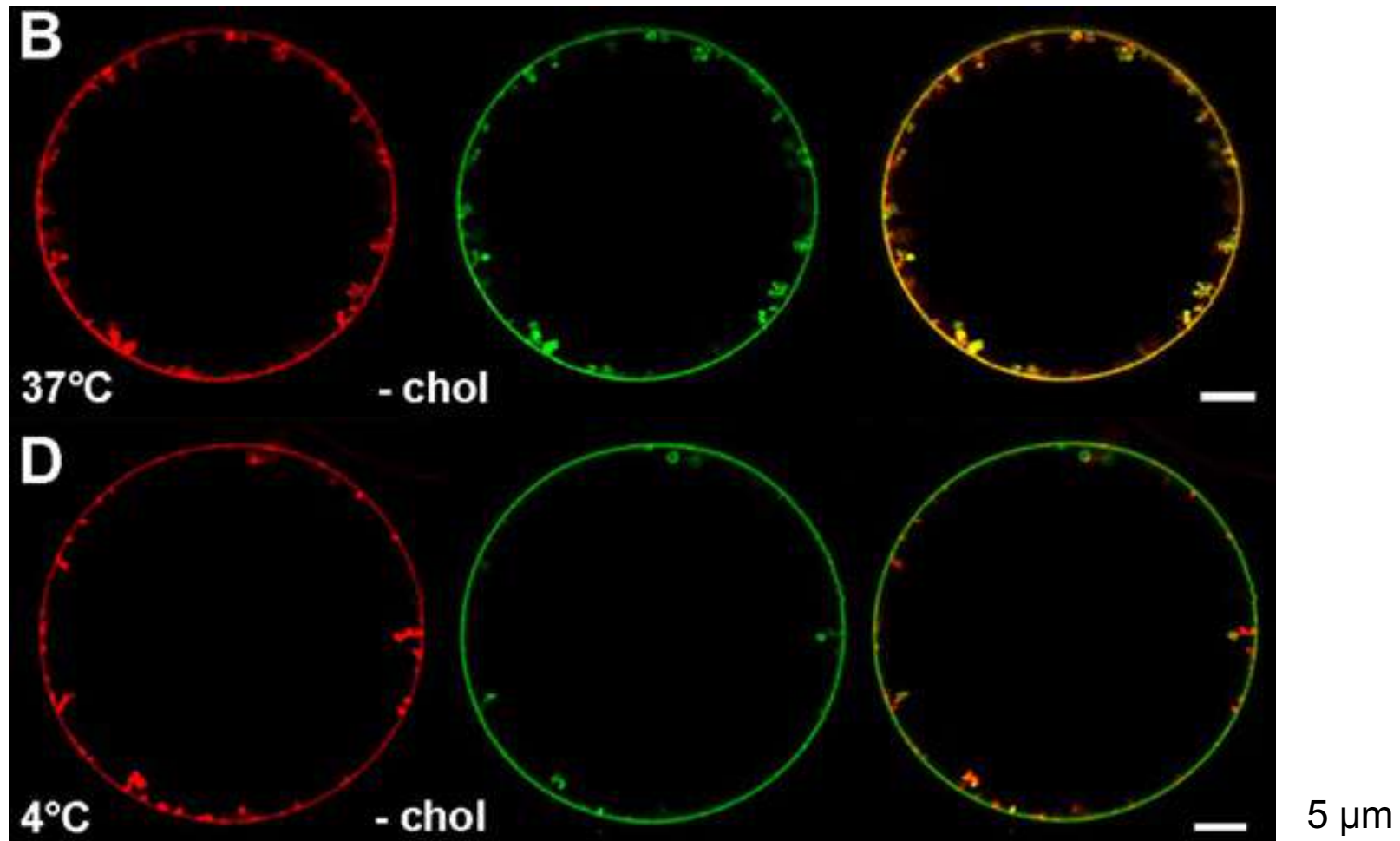
Shiga Toxin Induces Fission of its own Tubules

DOPC + 5% HeLa Gb3(α -hydroxylated) + 30% Cholesterol



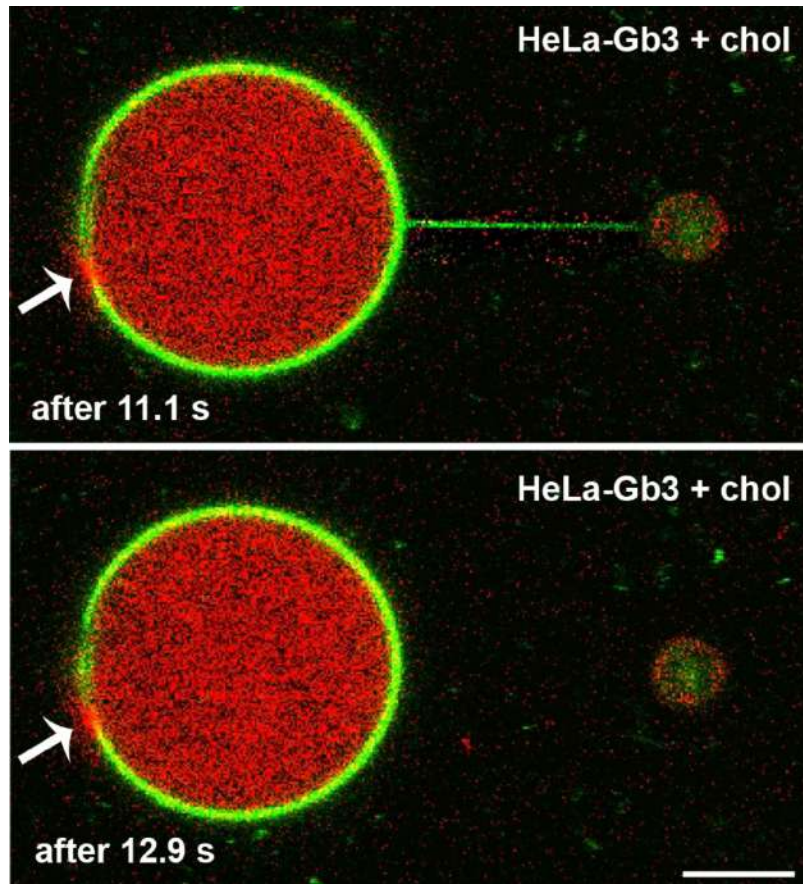
No Fission in the Absence of Cholesterol

DOPC + 5% HeLa Gb3(α -hydroxylated) - *NO Cholesterol*



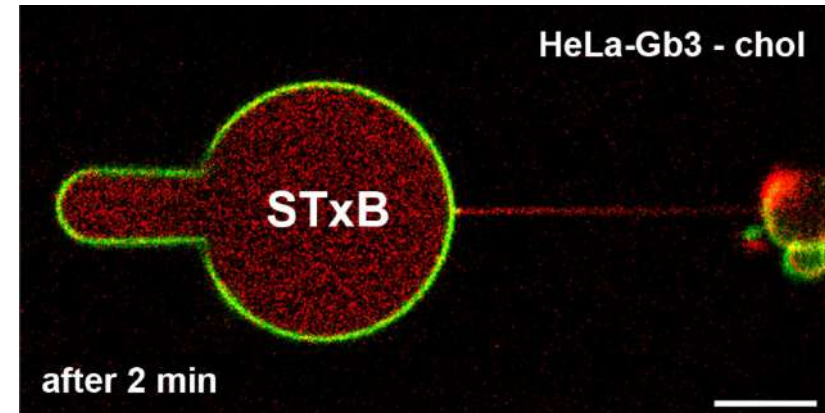
Line Tension-Induced Fission

+ cholesterol



Fission

- cholesterol



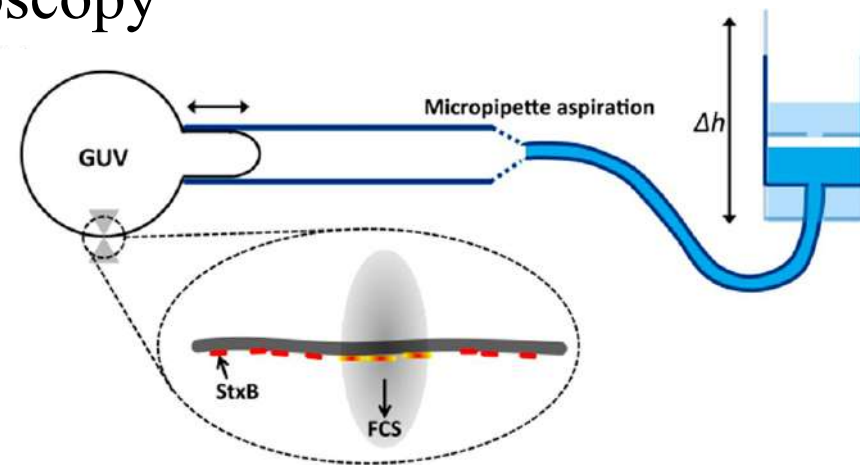
No domain → no fission

Encapsulated STxB

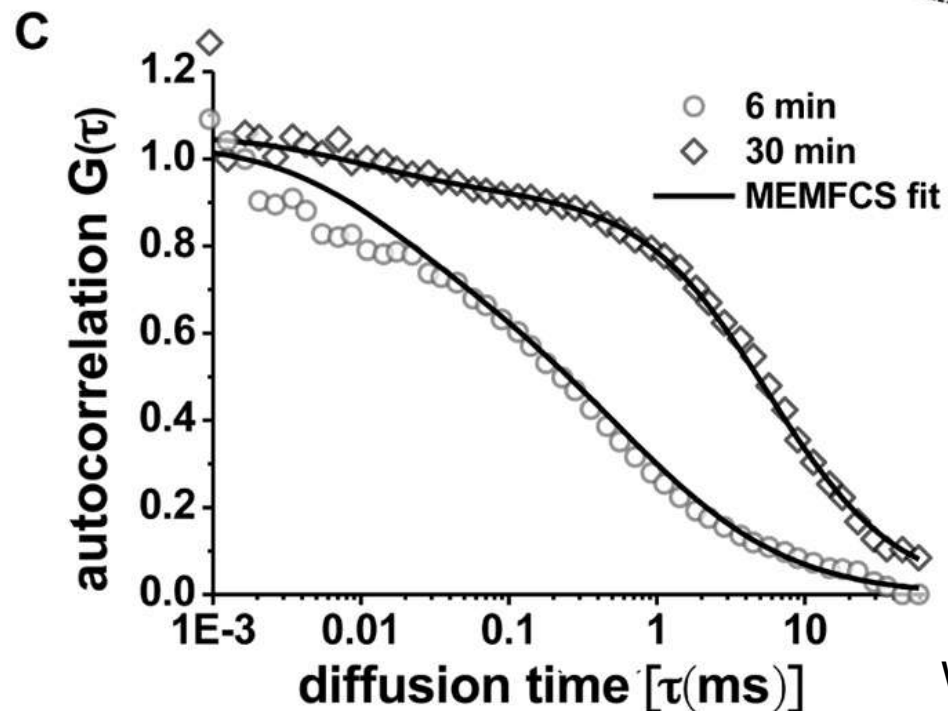
Fluorescent lipid

STxB Clustering

Fluorescence Correlation Spectroscopy



Autocorrelation function



Characteristic
diffusion time τ_D

$$\tau_D = \frac{r^2}{4D} \longleftarrow \text{Spot size}$$

Diffusion coefficient $D \longleftrightarrow$ Cluster size R

Small cluster size

$$D = \frac{k_B T}{4\pi\mu_m h} \ln \left(\frac{R_{mem}}{R} \right)$$

(for finite size membrane R_{mem})

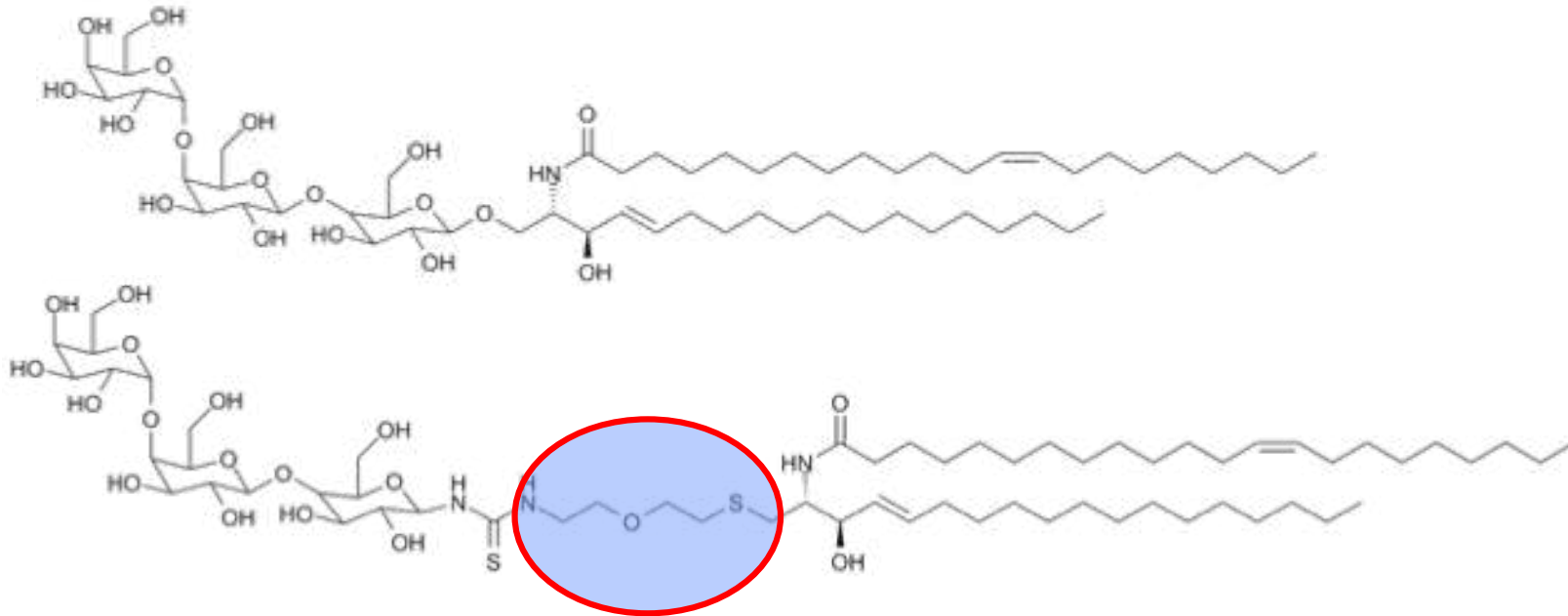
Saffman and Delbrück, *PNAS* (1975)

Large cluster size

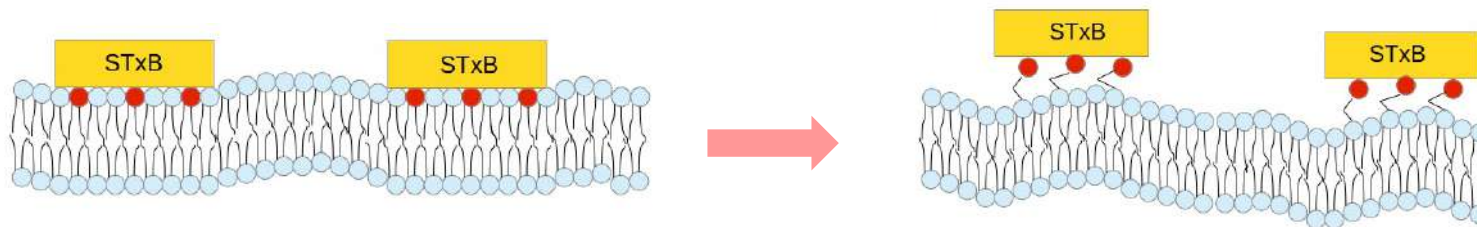
$$D = \frac{k_B T \lambda}{4\pi\mu_m h} \frac{1}{R}$$

Here $R_{max} = 180 \text{ nm}$ (~ 50 monomers)

Reduce Mechanical Coupling between Sugar and Ceramide

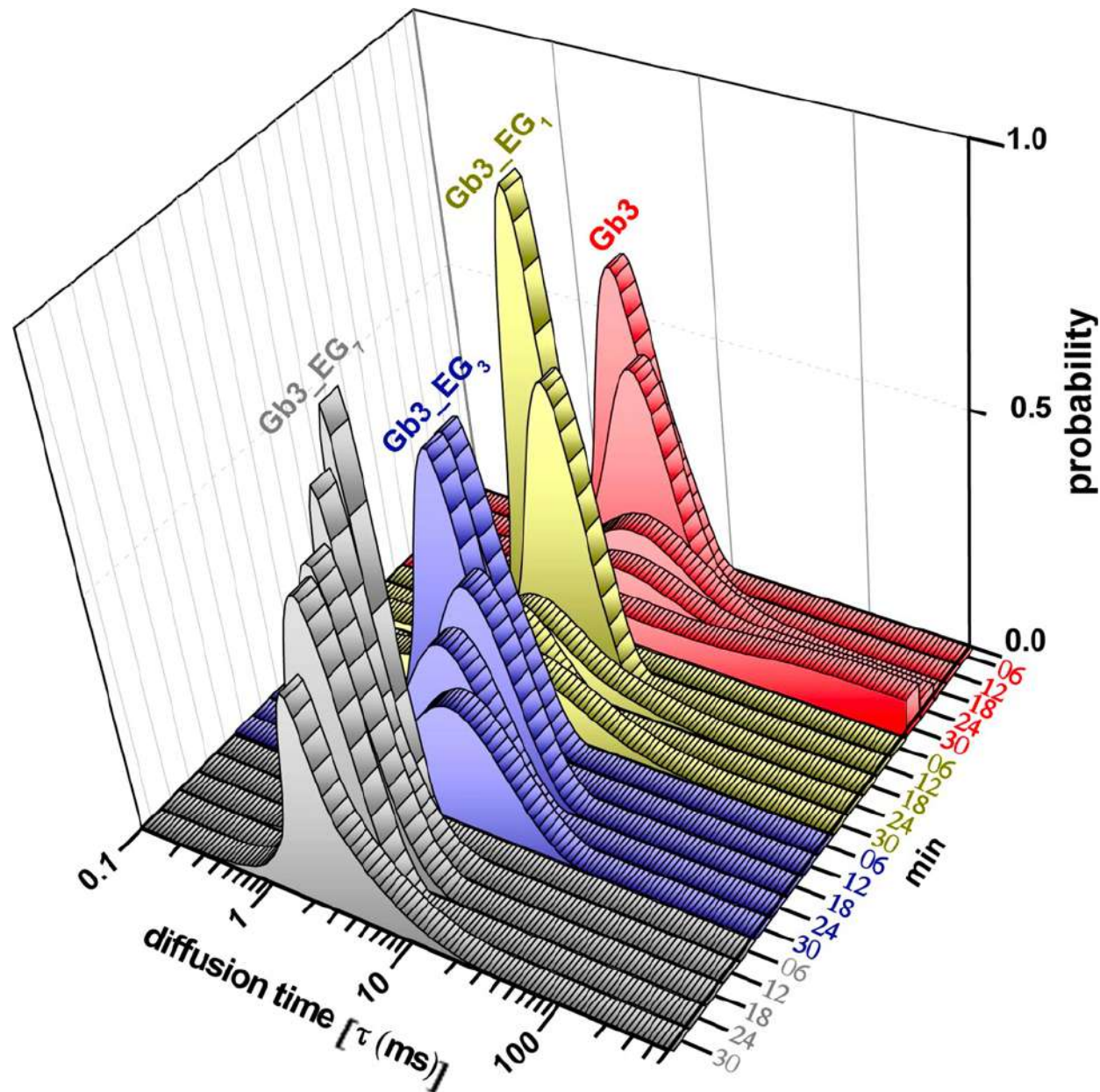


PEG linker: 1x, 3x, 7x

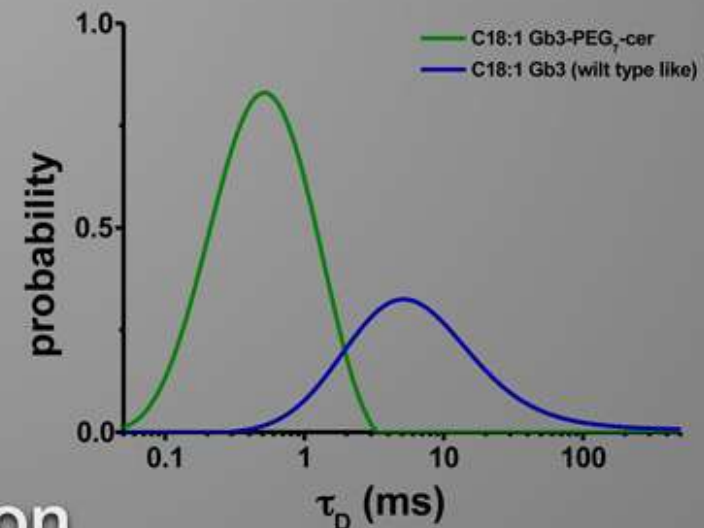
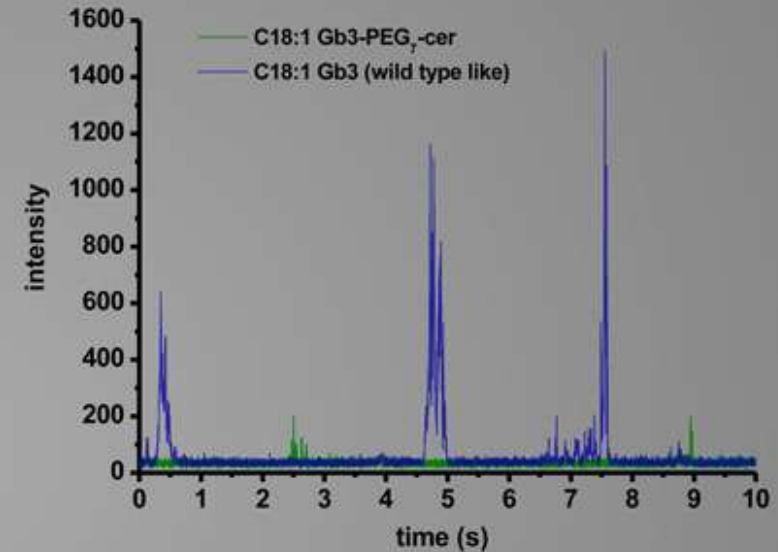
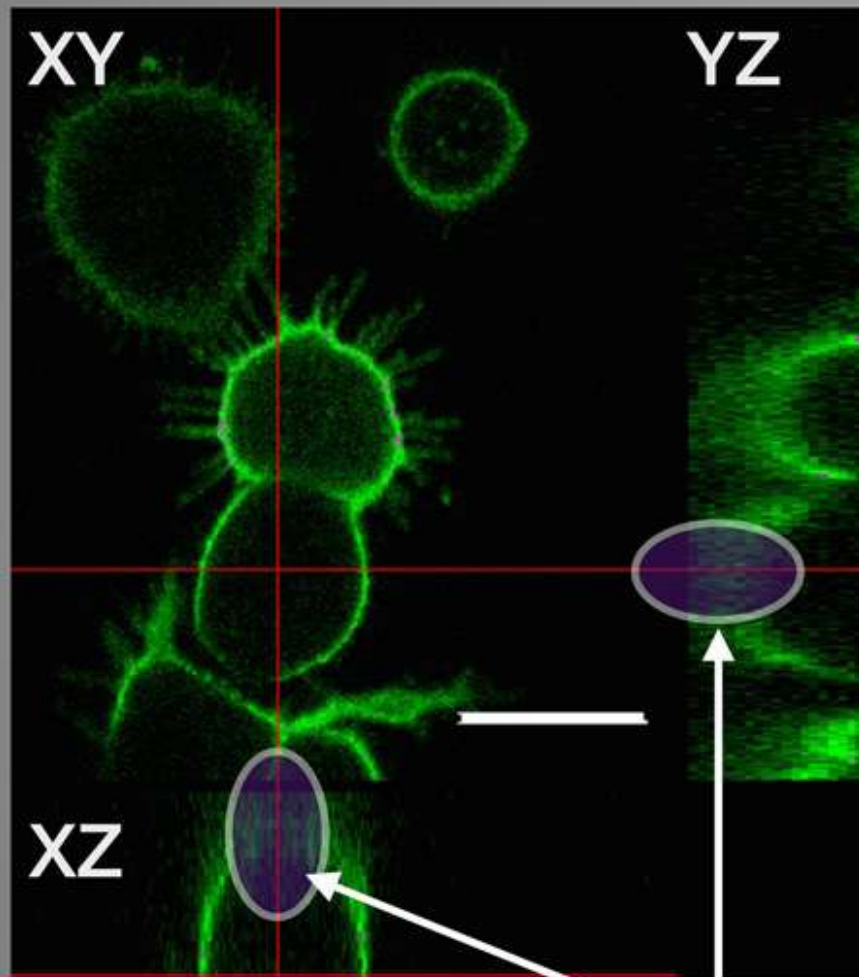


➡ Reduce tight binding of STxB on the membrane

No Mechanical Coupling – No Clustering

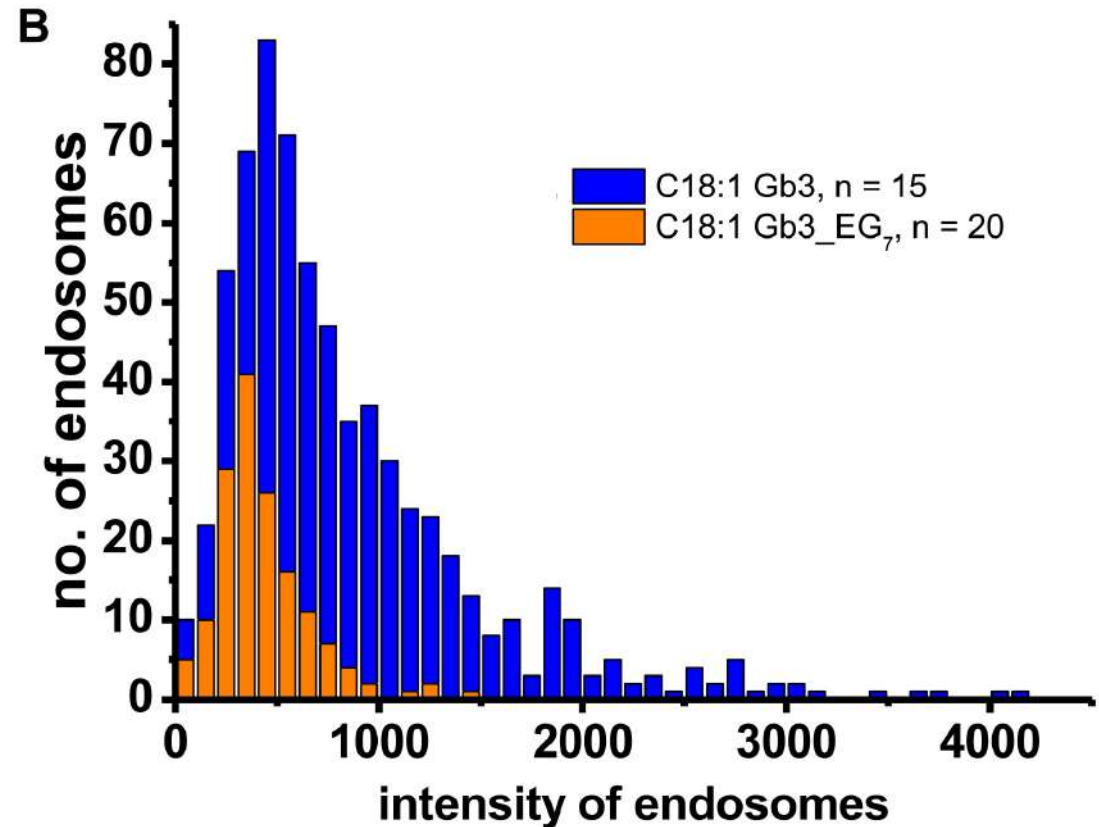
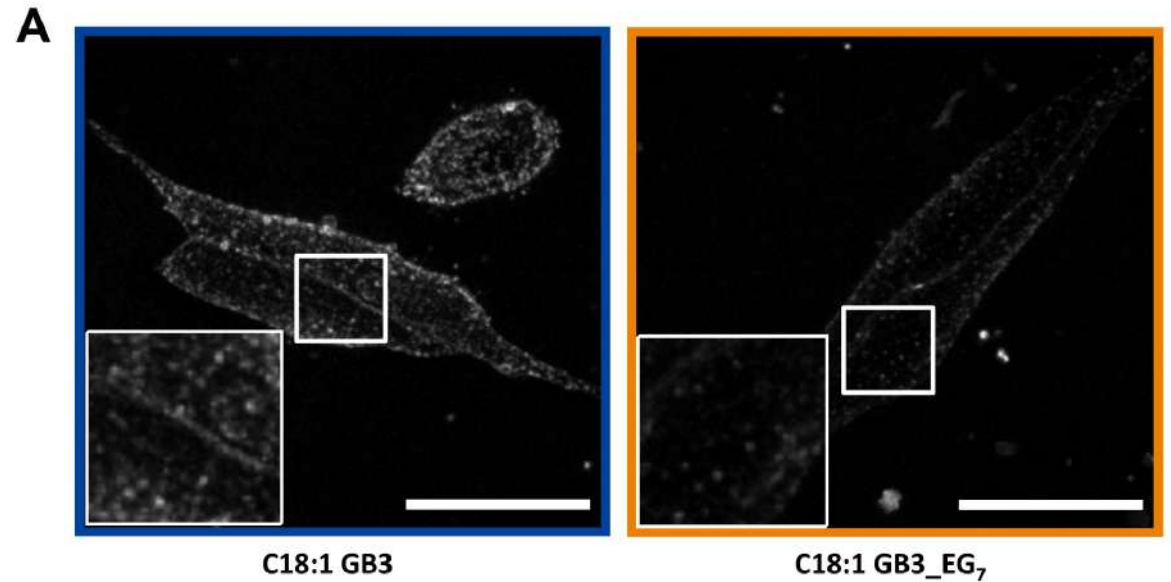


Mechanical coupling is required for efficient clustering of STxB as measured by FCS



measurement region

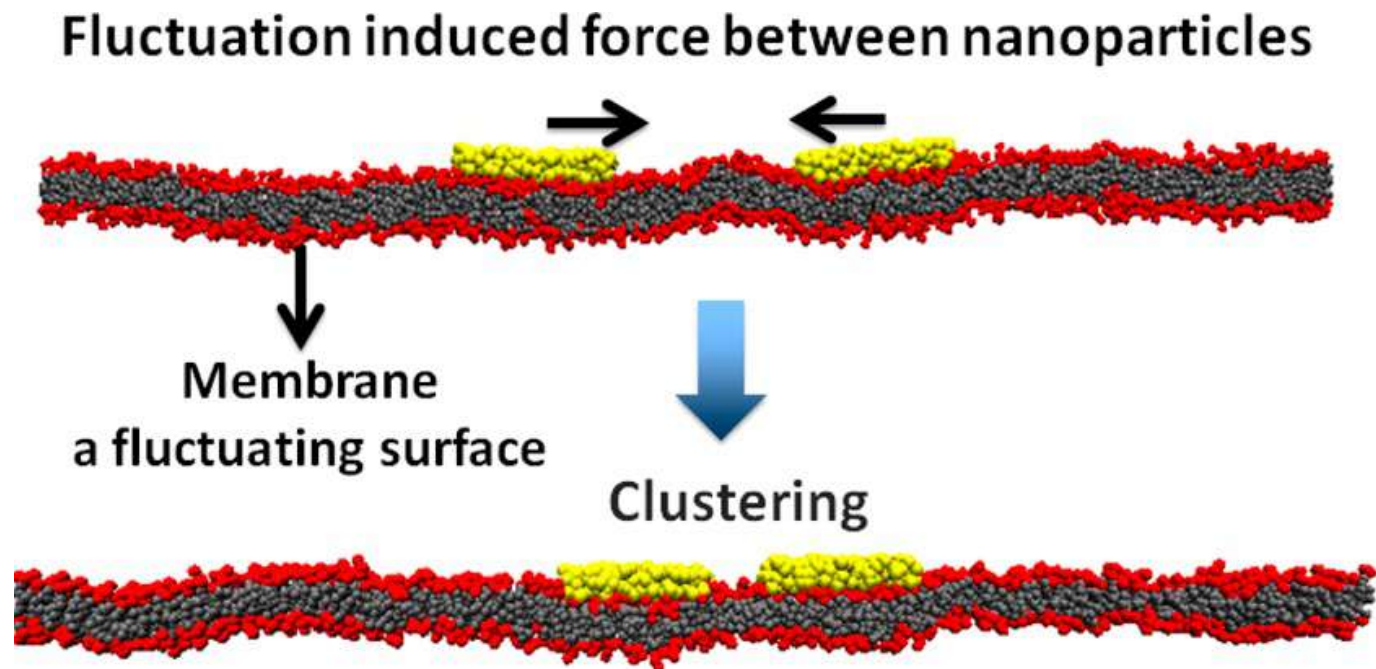
Mechanical
coupling is
required for
efficient
endocytosis of
STxB



Membrane Fluctuation Force

No hydrophobic mismatch (no line tension)

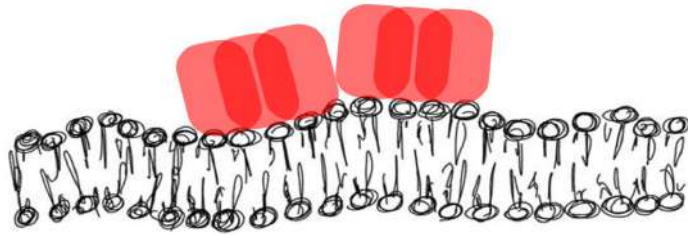
Membrane bending: repulsive force



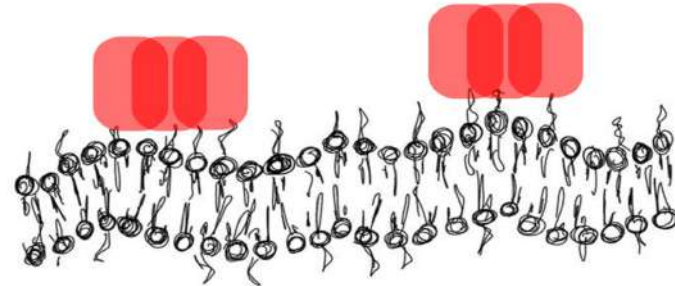
Force $\sim$ a few pN

Range $\sim$ protein size (5-10 nm)

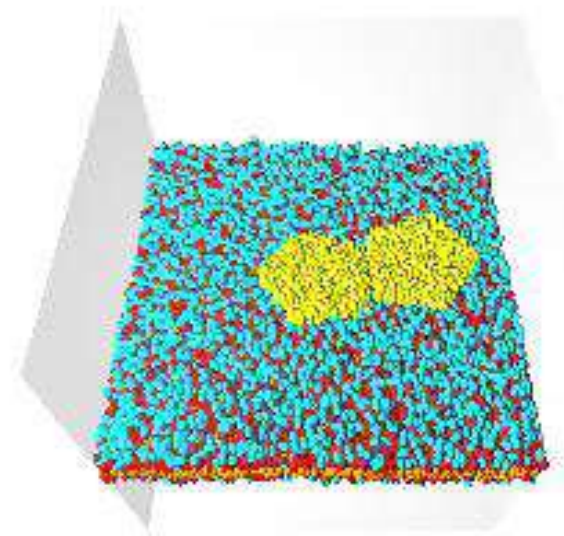
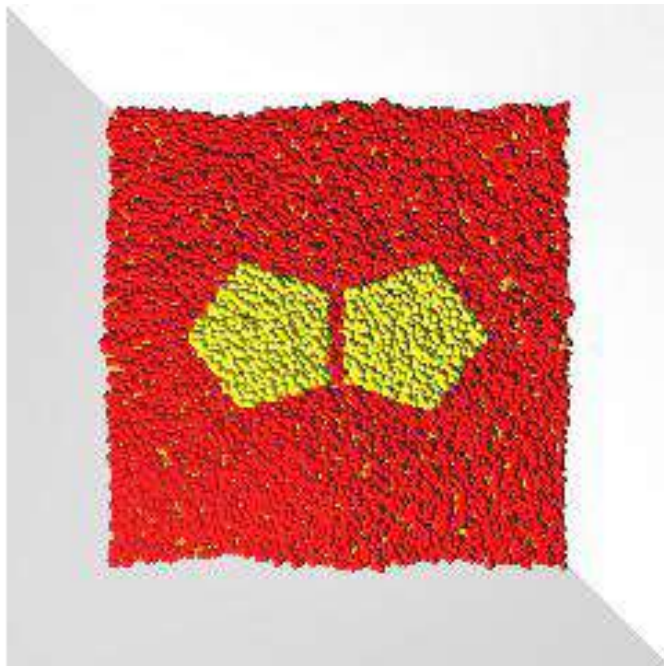
Membrane Fluctuation Force



No linker



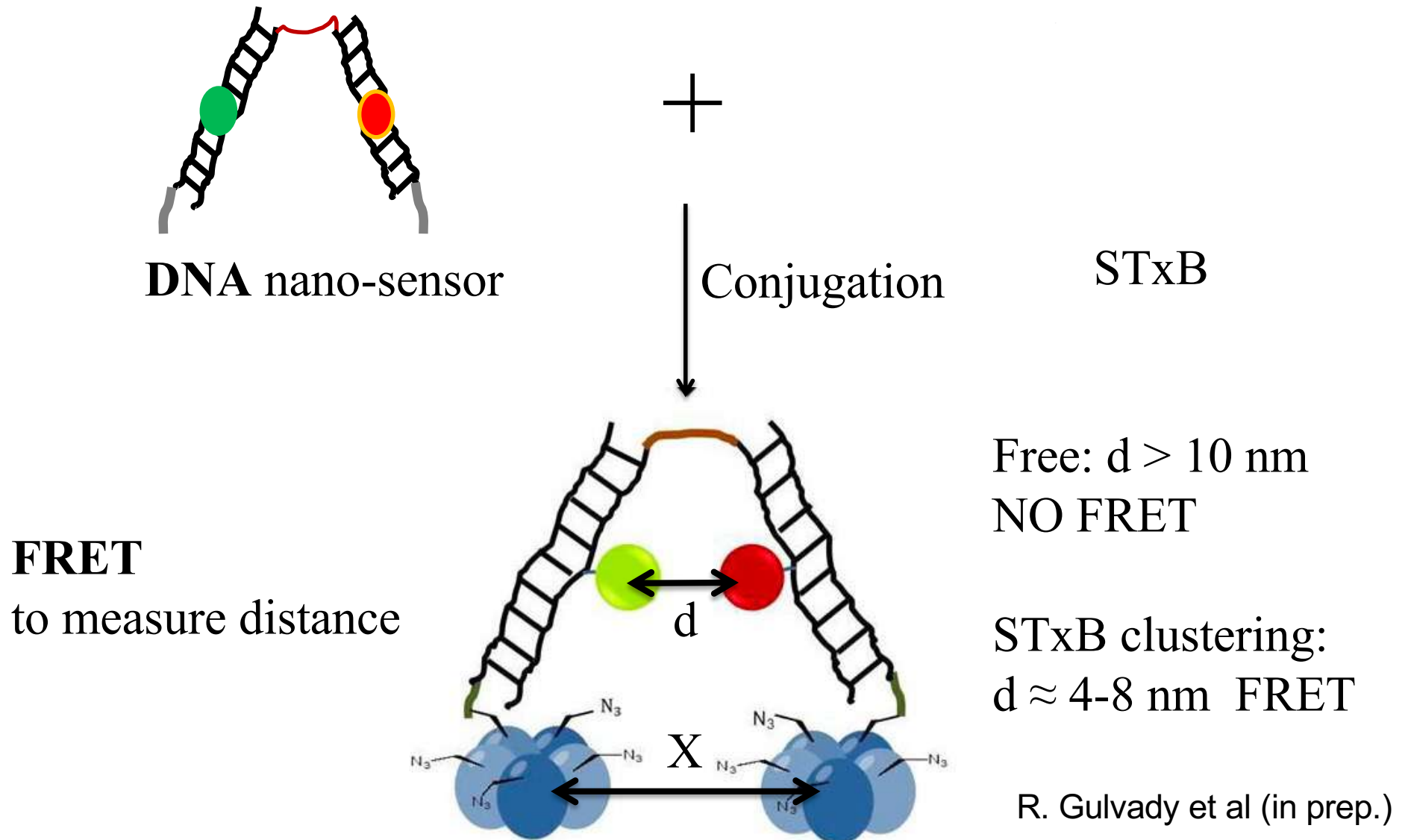
Linker



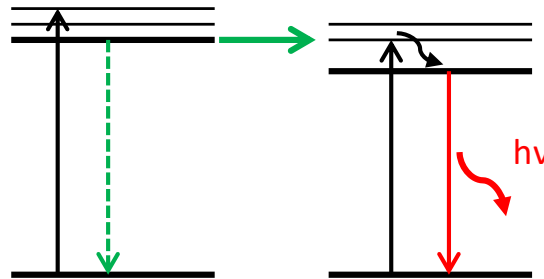
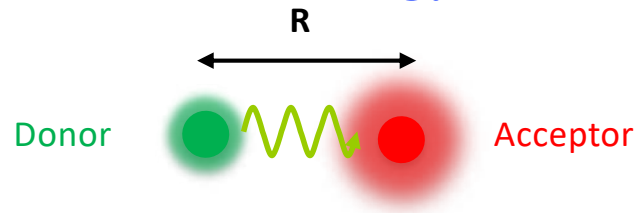
Coarse-grained simulation: *Dissipative Particle Dynamics (DPD)*

W. Pezeshkian et al. *ACS Nano* (2017)

DNA Nanosensor : STxB Clustering Energy



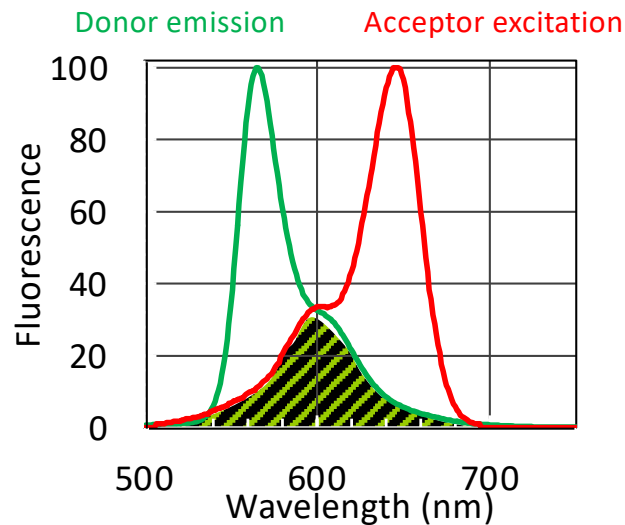
Principle of Förster Resonance Energy Transfer (FRET)



Transfer

Couple **D/A**
Förster radius: R_0

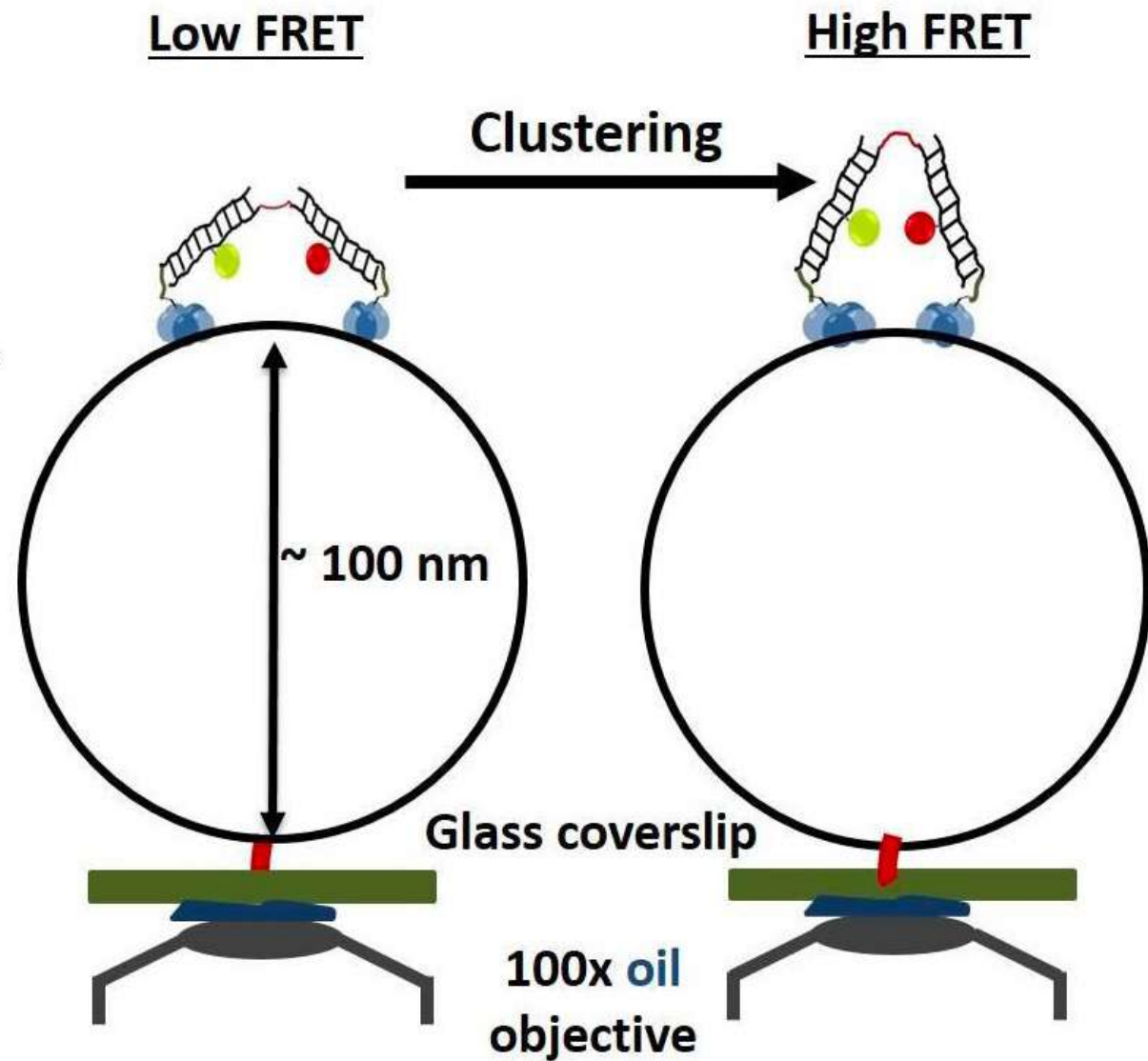
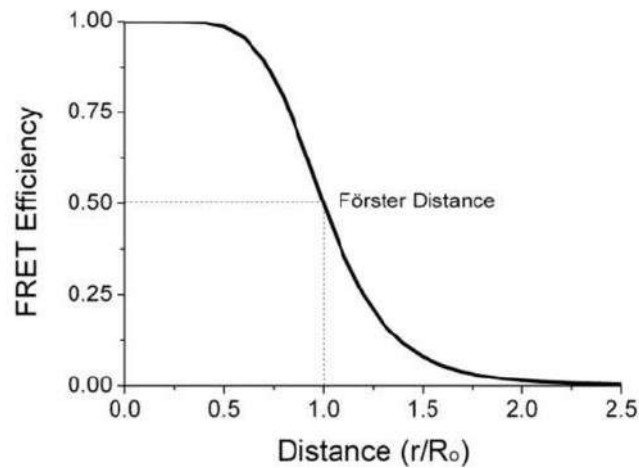
Distance between
D and **A**: R



Spectral overlap
between D and A

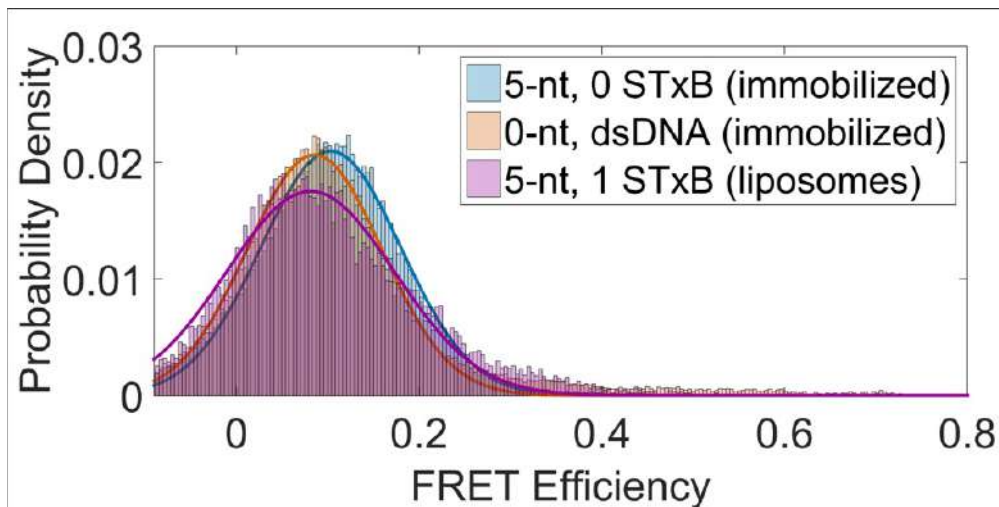
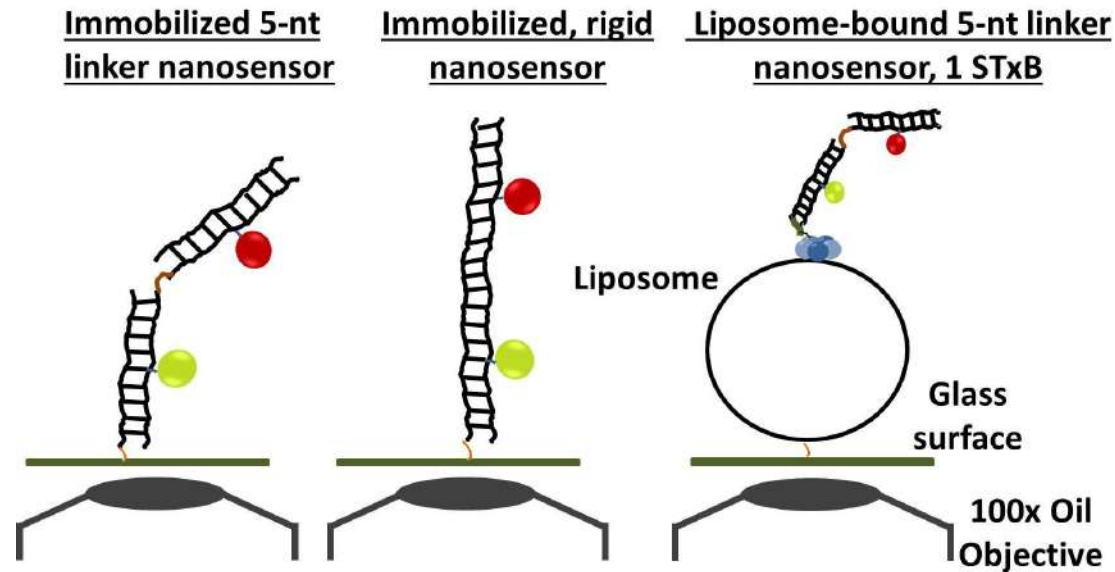
$$E_{th} = \frac{R_0^6}{R_0^6 + R^6}$$

DNA Nanosensor : STxB Clustering Energy



No Attraction

if the 2 STxB are not bound to a Membrane



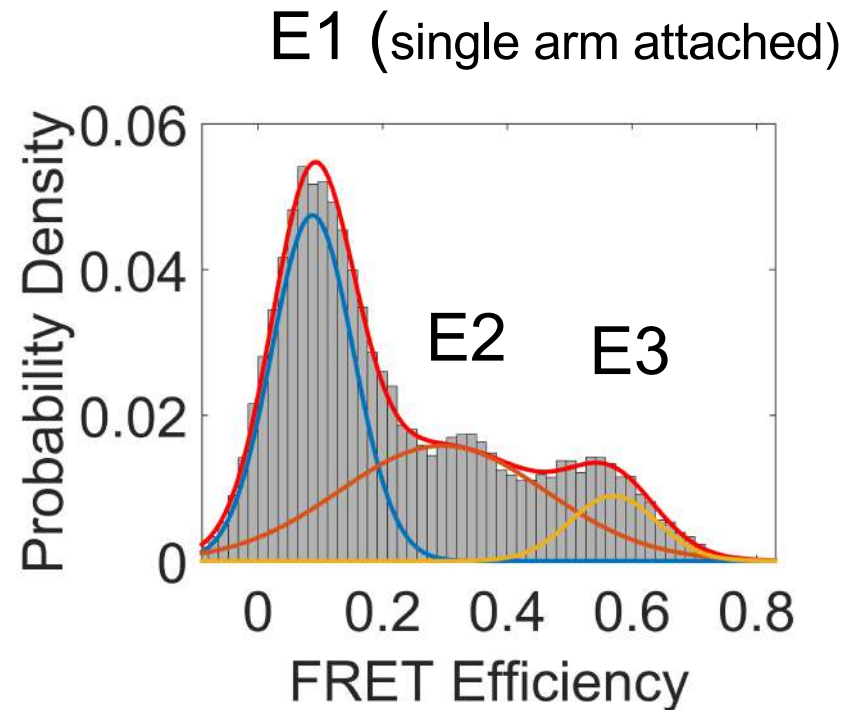
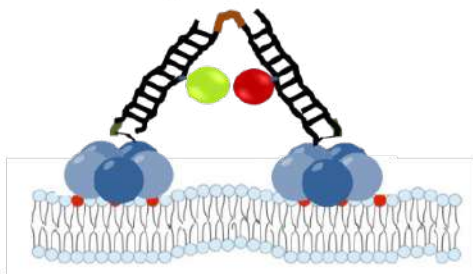
In solution

$E = 0.132$ (no STxB)

$E = 0.138$ (with STxB)

Attraction when both STxB are bound to Membrane

Natural Gb3

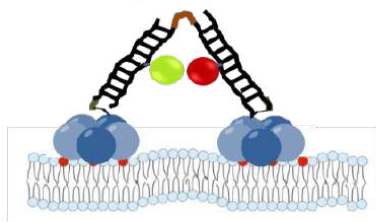


$$E3 = 0.571$$

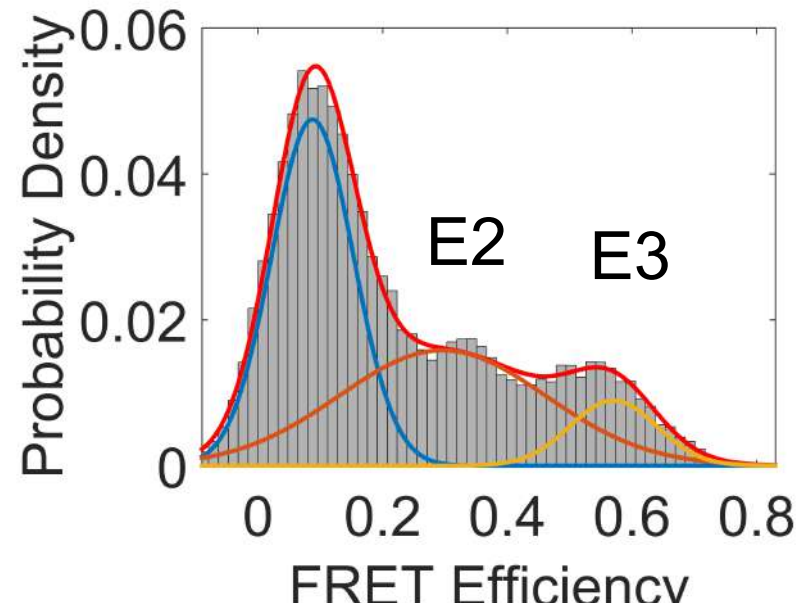
$$E2 = 0.294$$

Reducing Mechanical Coupling Reduces Attraction

Natural Gb3



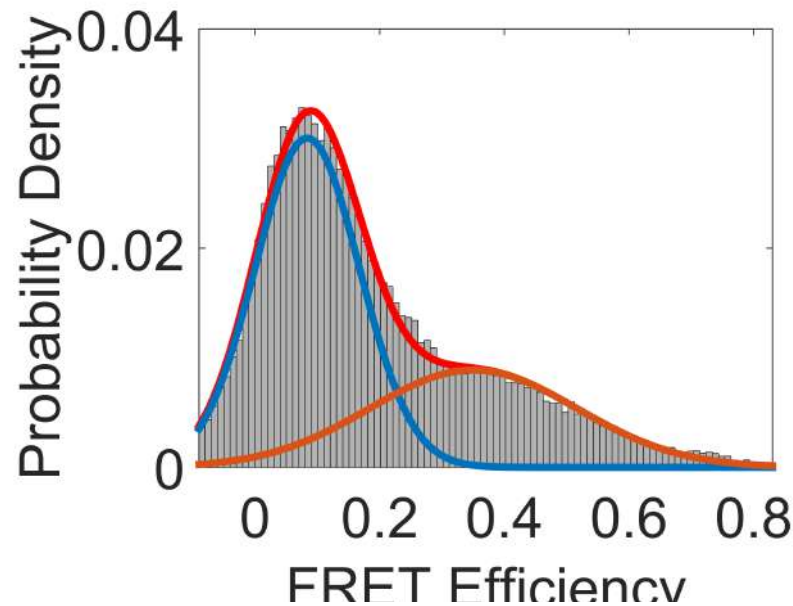
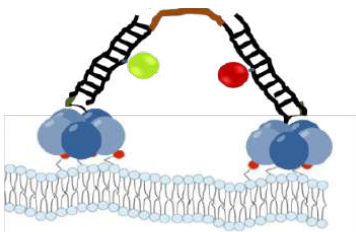
E1 (single arm attached)



$$E3 = 0.571$$

$$E2 = 0.294$$

Gb3-EG₇



$$E3 = 0.351$$

R. Gulvady et al
(in preparation)

In progress:

Simulations and theory (Neda Rahmani, W. Pezeshkian and J. Ipsen)

Calculation of the attraction energy

Prediction of fluctuation force

Comparison with our FRET measurements

Thanks!

