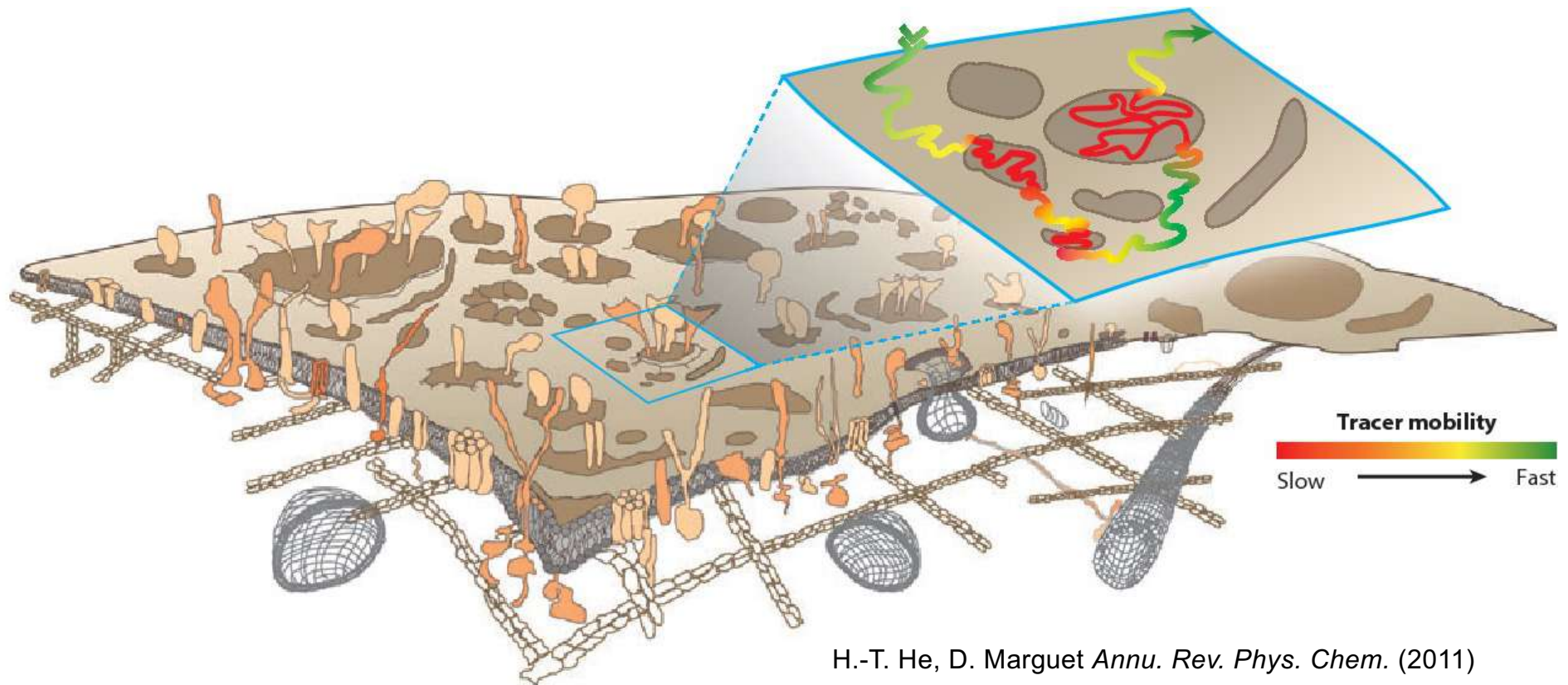




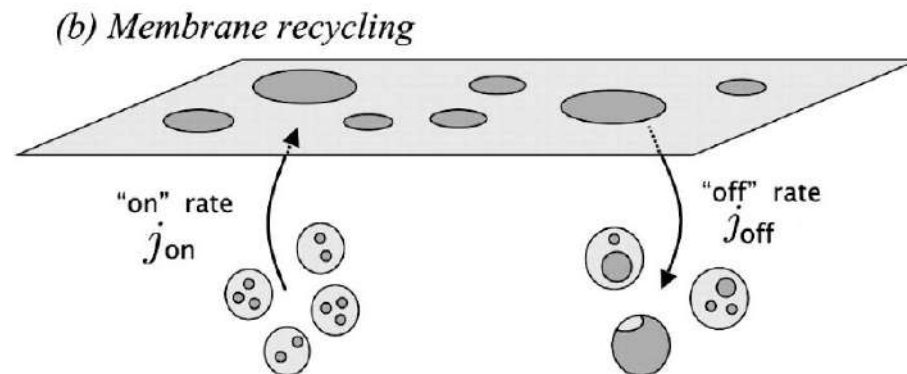
4. Active Protein Clustering

Previous lecture: Thermodynamic equilibrium

Why clusters of finite, small size in cells?

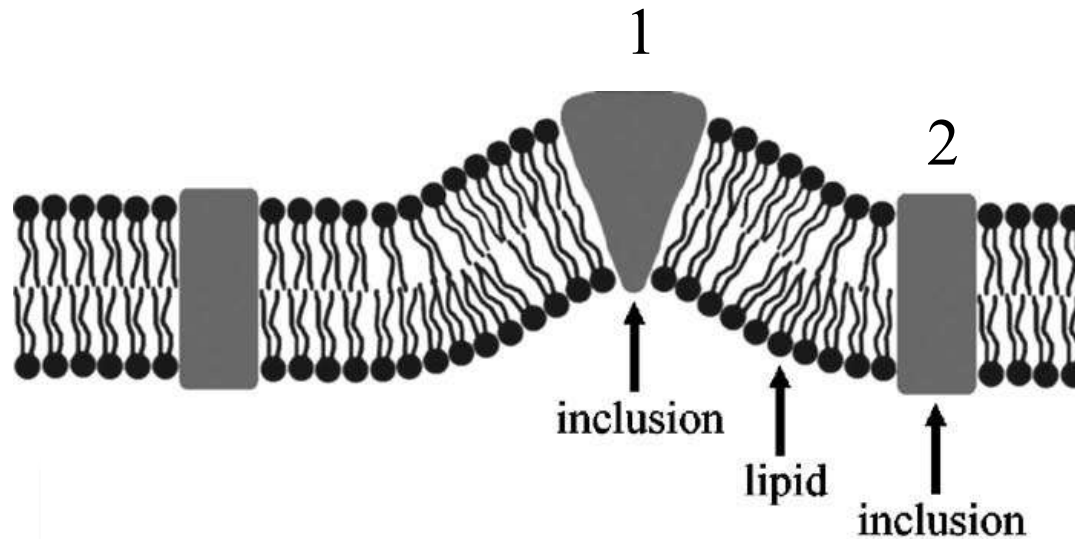
➡ *Non-equilibrium* considerations to be added

- Active remodeling of the cortical cytoskeleton
- Rapid traffic of membrane components

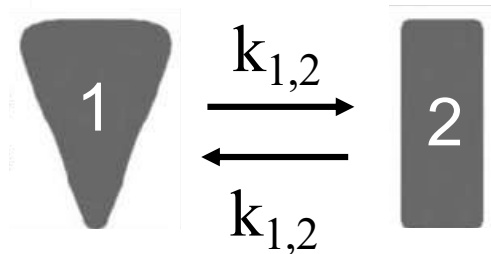


- Transfer of energy to the membrane by active "machines"

Active Inclusions: Finite Size of the Clusters



Monte-Carlo
simulations



1 attracts 1

G: inclusion (1) coupling to curvature

2/1, 2/2 or 2/lipids: no interaction

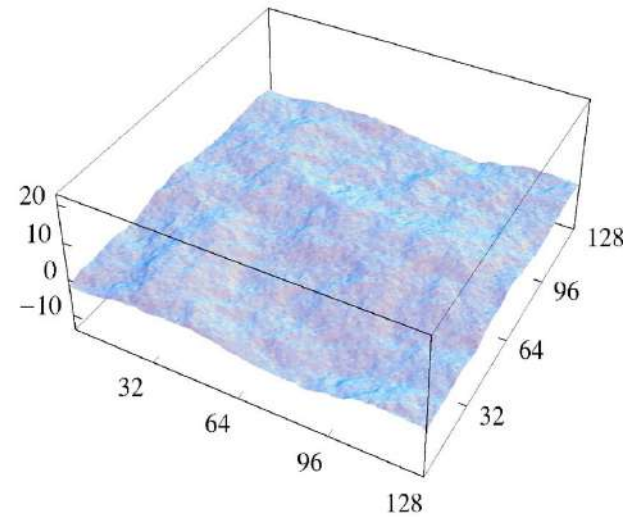
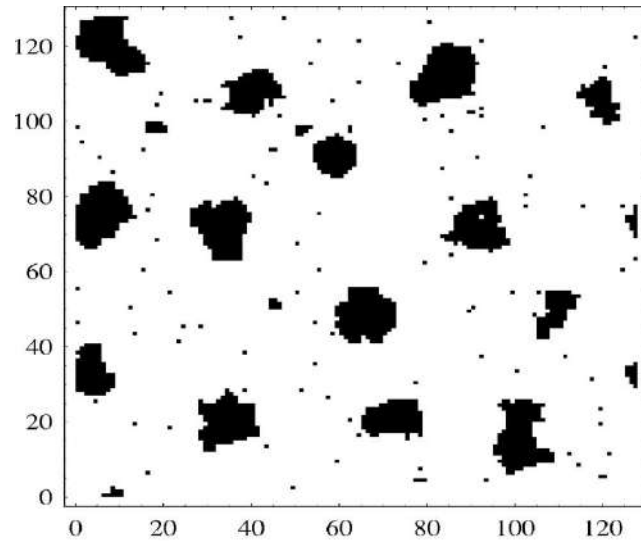
Active Inclusions: Finite Size of the Clusters

Steady state

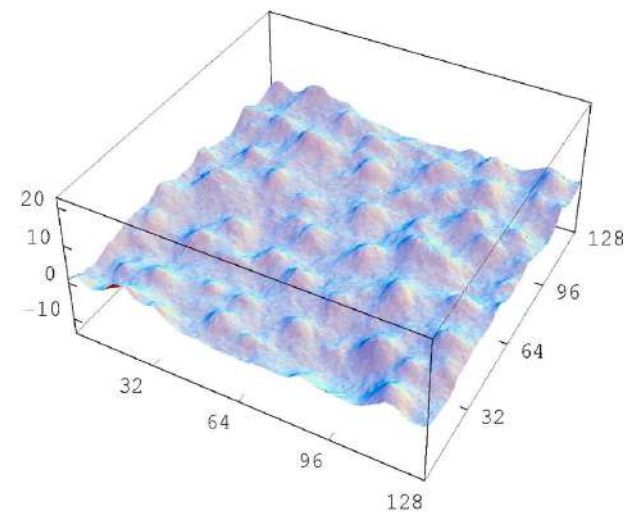
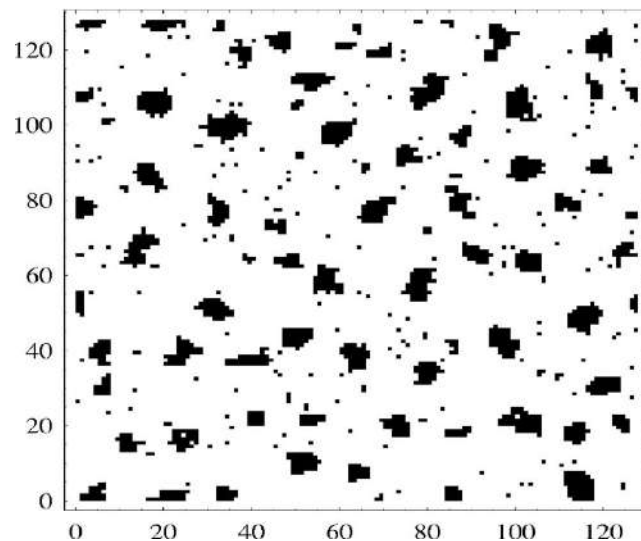
Inclusions

Membrane

$G=0$

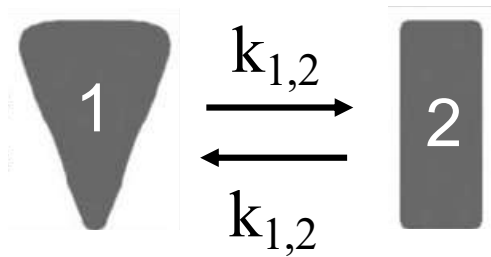


$G=2$

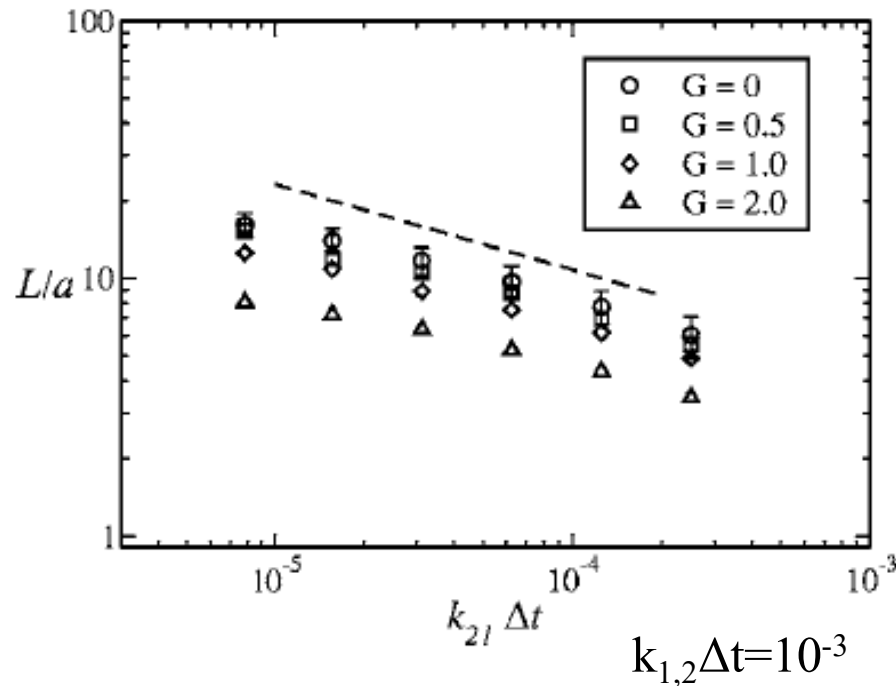


Adimensional length ($/a$ =lattice Ct)

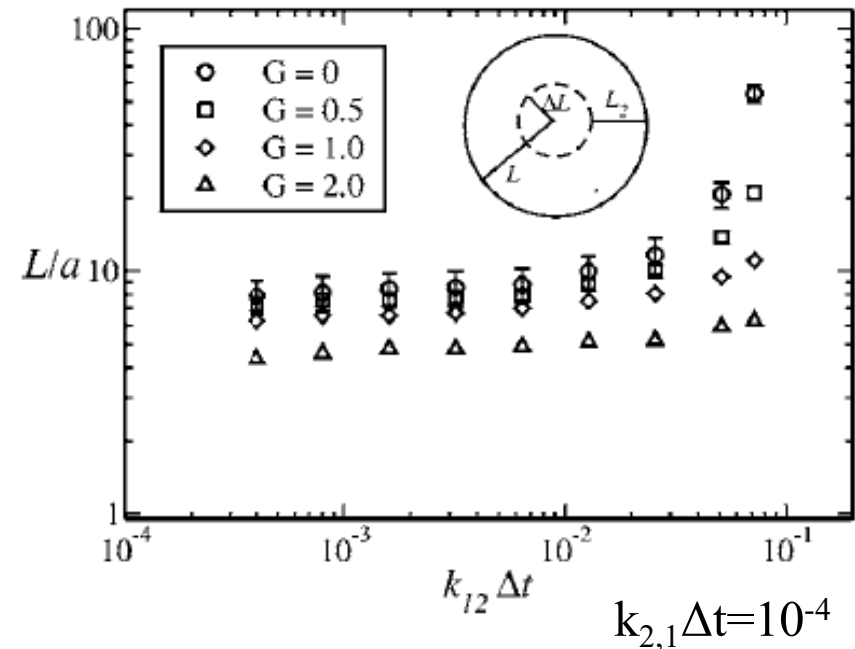
Active Inclusions: Finite Size of the Clusters



Cluster size

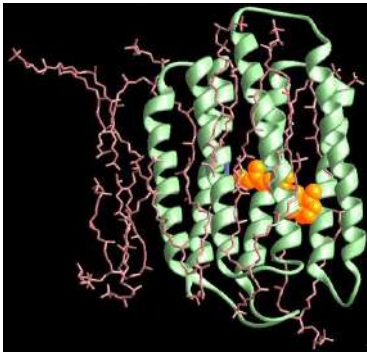


$$L \sim k_{2,1}^{1/3}$$



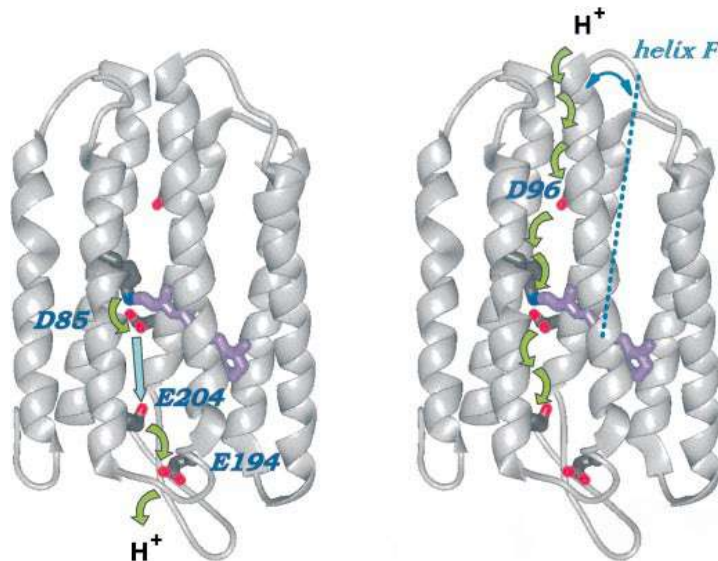
Depends weakly on $k_{1,2}$

Bacteriorhodopsin Clustering due to Light Activation



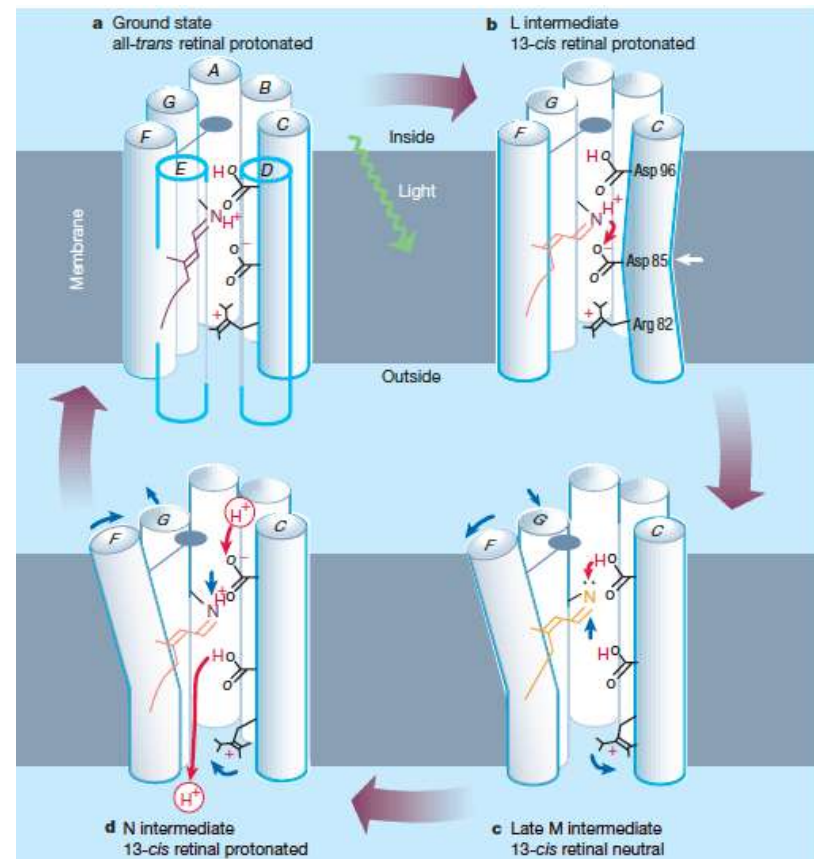
Proton pump

Activated by green light



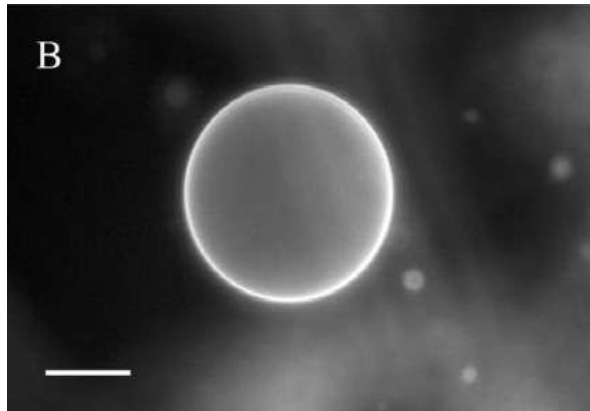
J.K. Lanyi *J. Biol. Chem.* (1997)

Conformational changes
during transport cycle

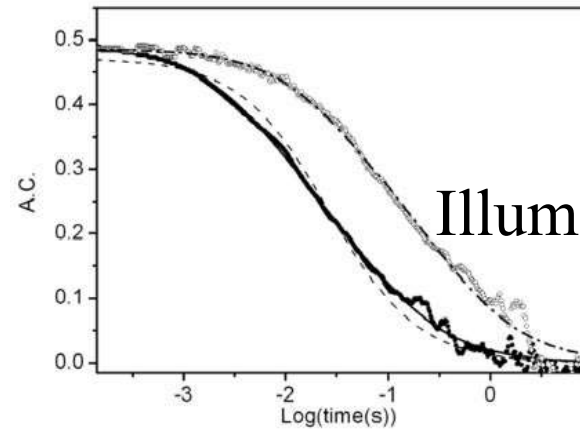


W. Kühlbrand *Nature* (2000)

Bacteriorhodopsin Clustering due to Light Activation



Low protein density

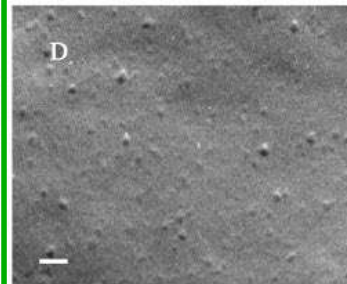
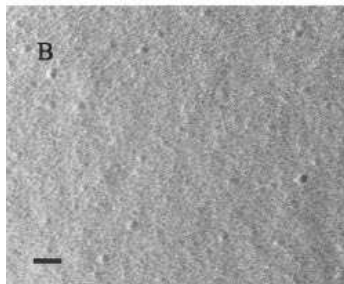
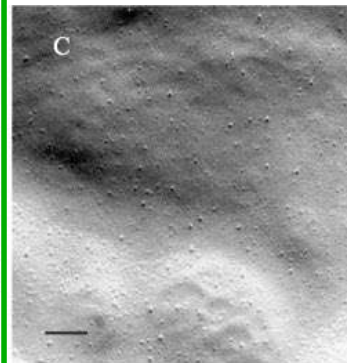
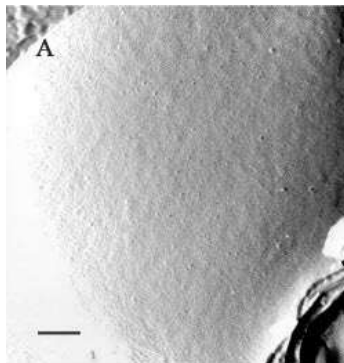


FCS

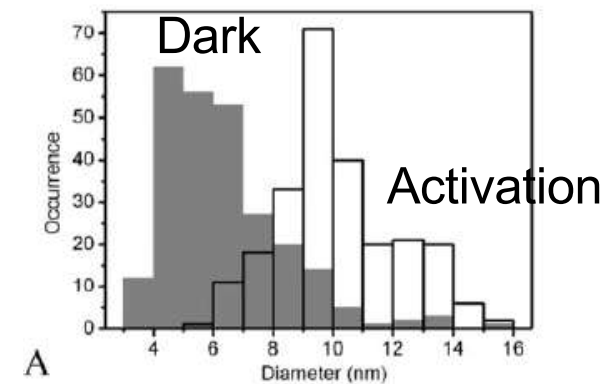
Illumination (Activation)

Dark

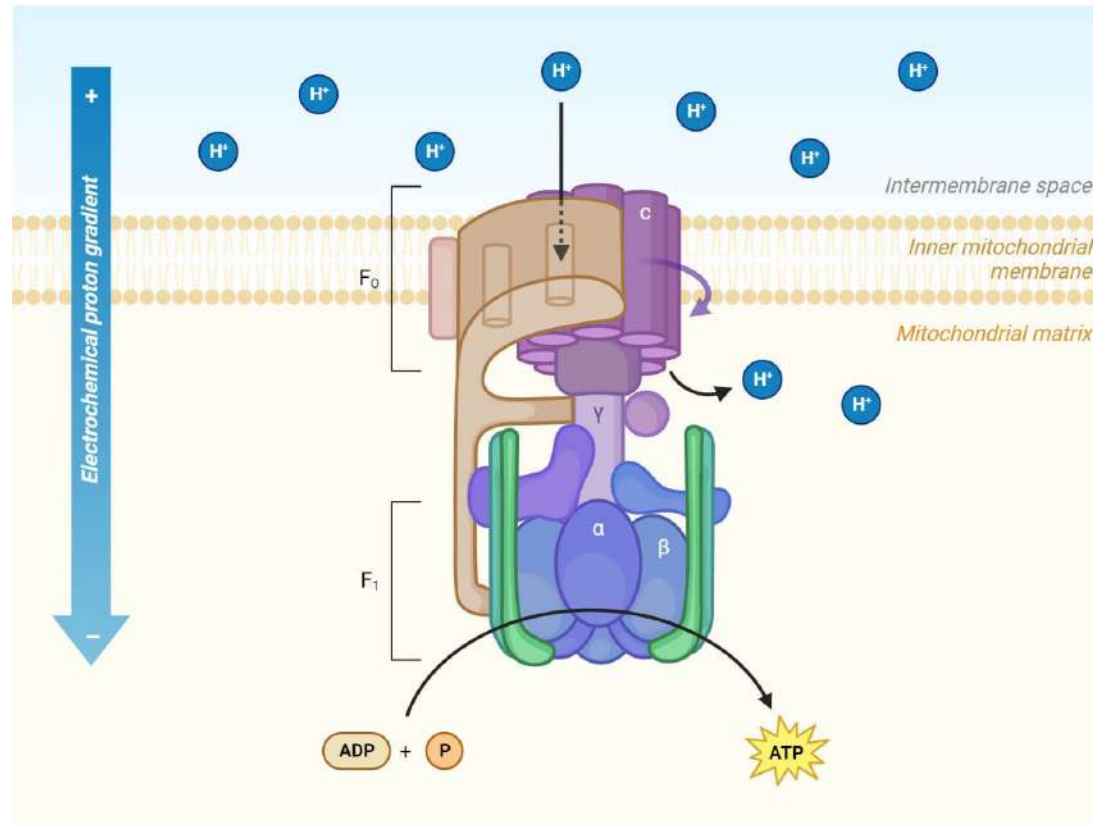
Activation



Clustering
Finite size



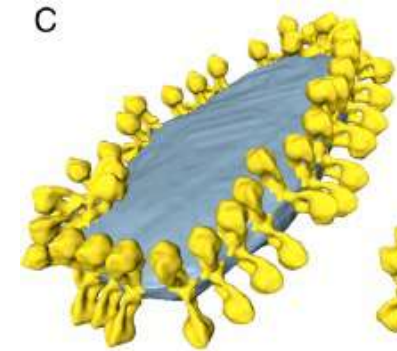
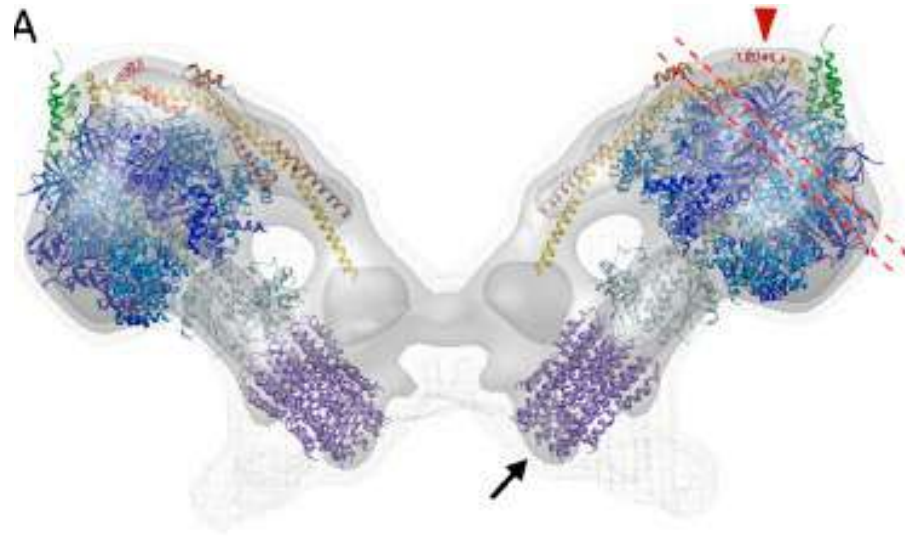
Clustering of Active ATP-Synthase (F_1F_0)



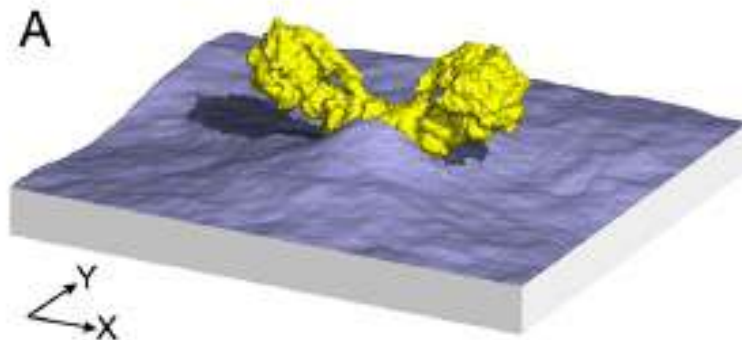
<https://microbenotes.com/atp-synthase/#mechanism-of-atp-synthesis>

ATP production in mitochondria, induced by H^+ gradient

ATP-Synthase: Dimers that Bend Membrane

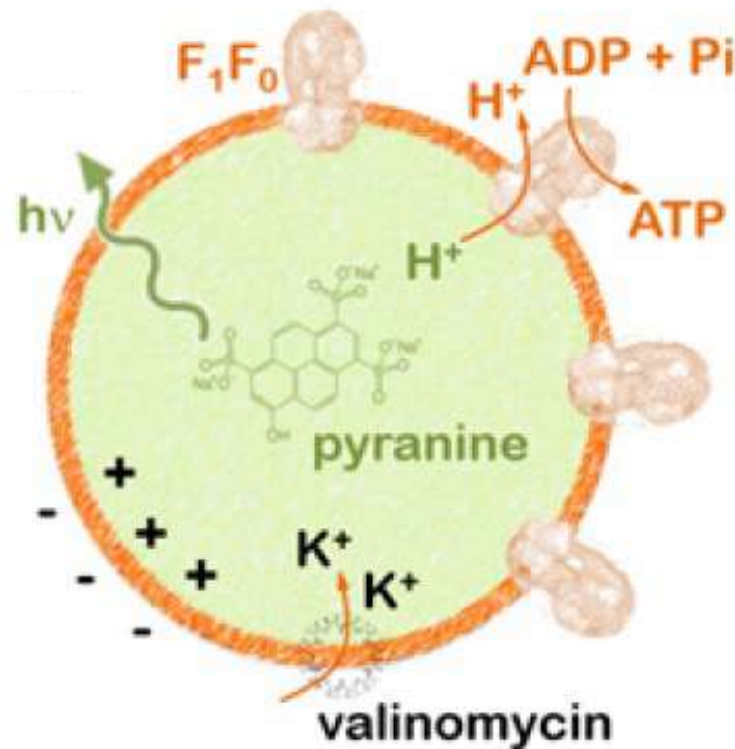


K.M. Davies et al. *PNAS* (2012)



Clustering of Active ATP-Synthase (F_1F_0)

In vitro system



Valinomycin

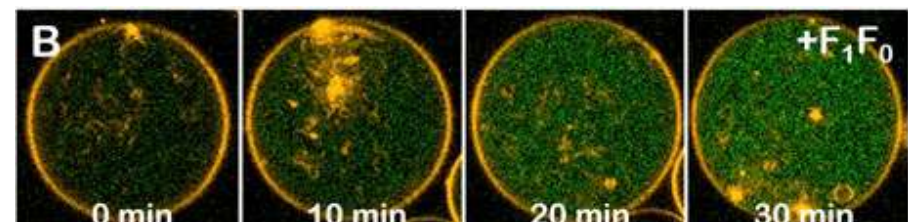
→ K^+ entry

→ H^+ exit

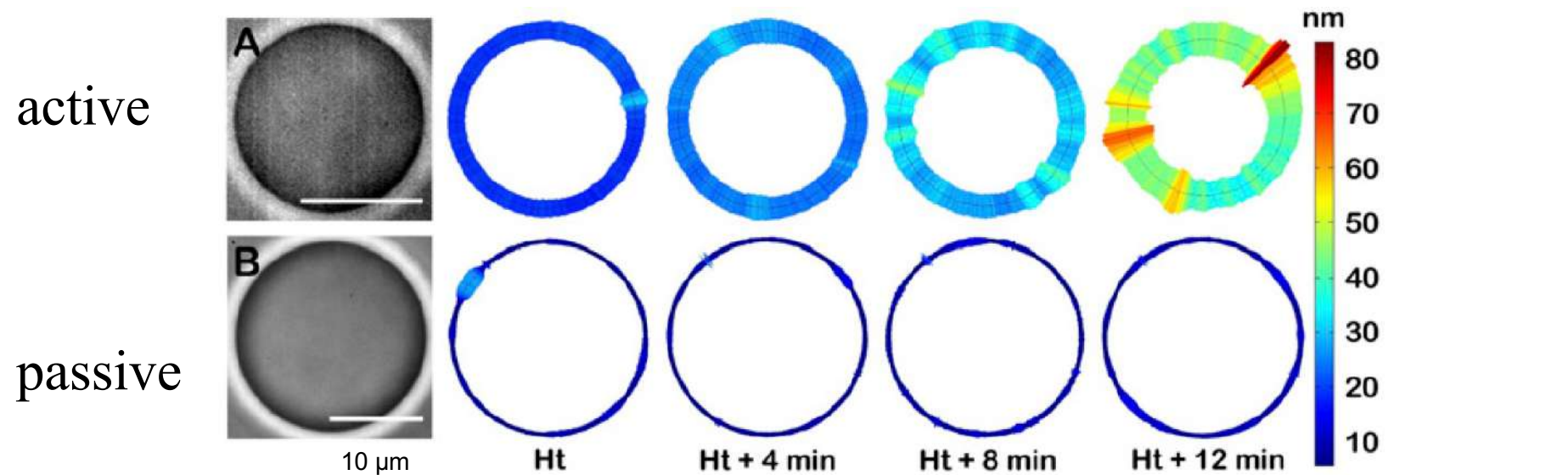
→ Activates F_0

→ ATP production

Pyranine: pH sensor

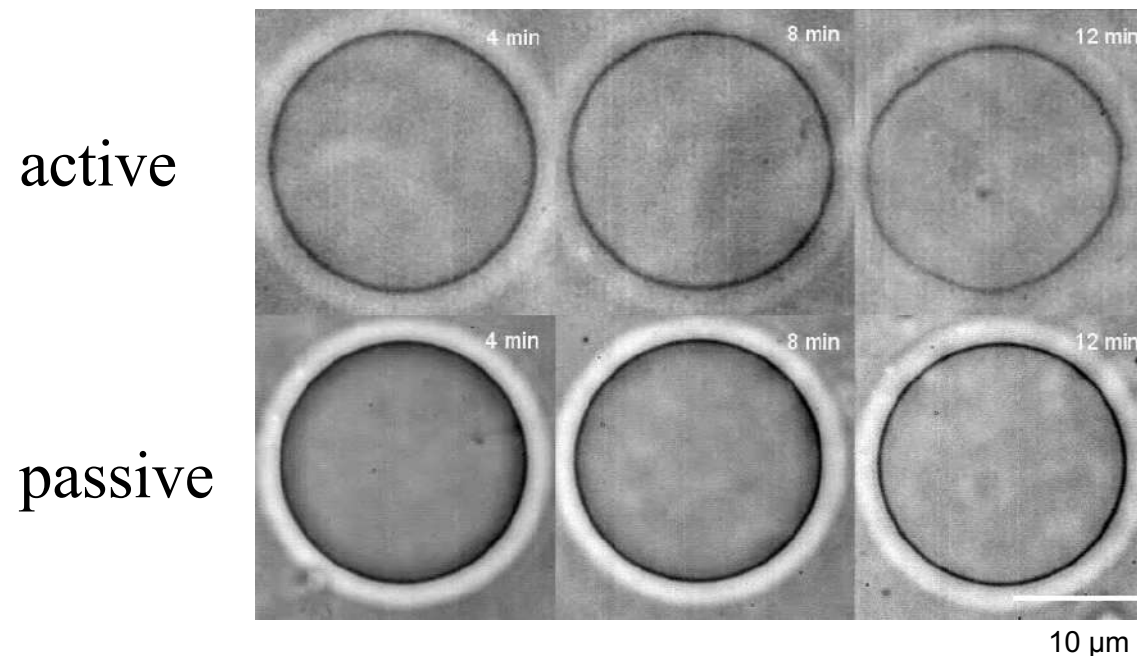


Localized Enhanced Fluctuations of Active F_1F_0



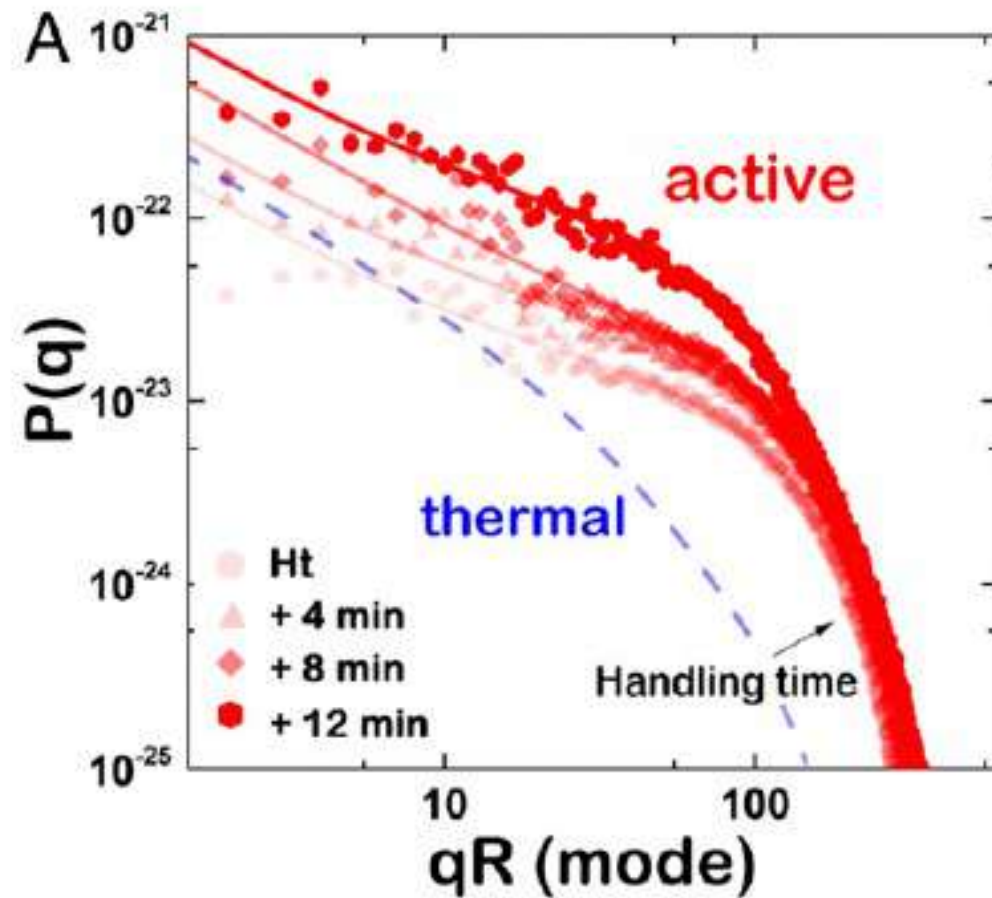
Fluctuation amplitude

Protein clusters?



V.G. Almendro-Vedia...
I. López-Montero *PNAS* (2017)

Activity Changes Fluctuation Spectrum



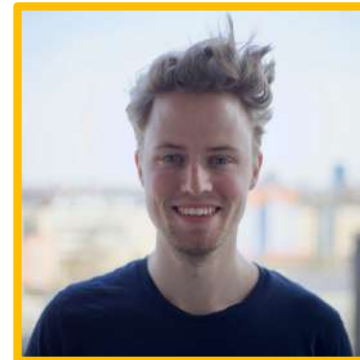
Clustering of an Active Transporter



Raju Regmi



Daniel Lévy



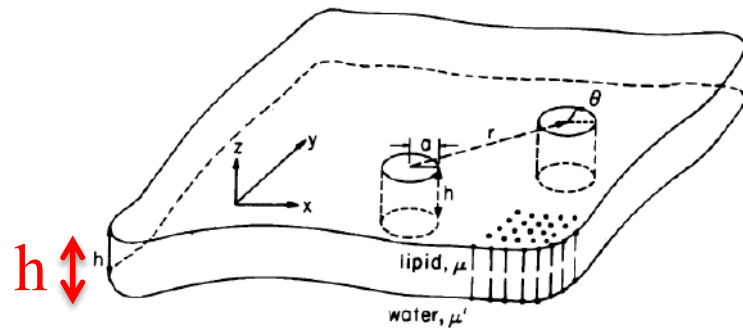
**Jacob Kaestel-
Hansen**



**Nikos
Hatzakis**

Diffusion of a Protein in a Membrane: “Classical” Hydrodynamic Model

- Brownian motion in membranes

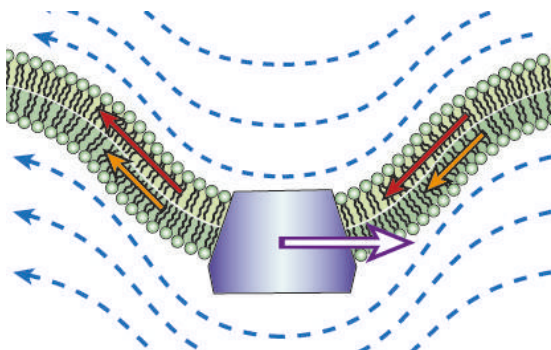


*Saffman and Delbrück, PNAS
1975*

Finite membrane size R_{mem}

$$D = \frac{kT}{4\pi\mu_{mem}h} \ln\left(\frac{R_{mem}}{R_{prot}}\right)$$

Depends on *membrane viscosity* - Weak dependence on the size R_{prot}



- Curvature-coupled protein
Deforms the bilayer



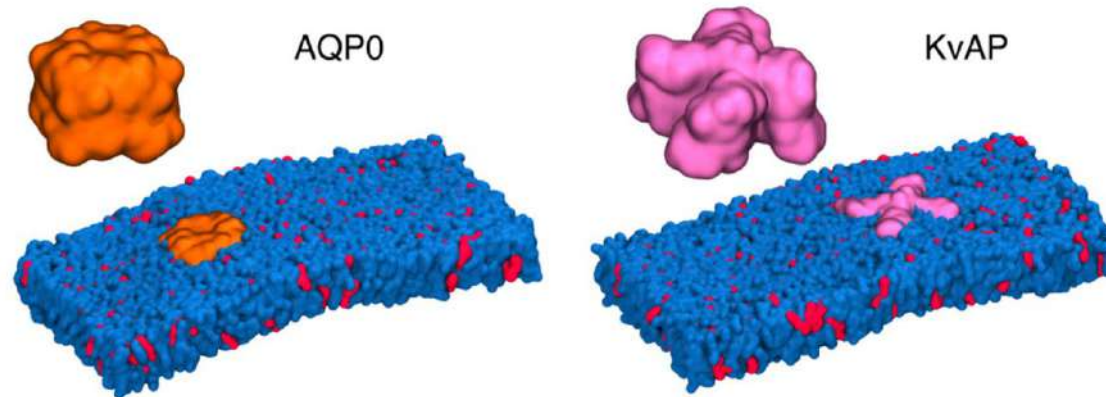
Additional dissipation

A. Naji, A. J. Levine, P. Pincus, *Biophys. J.* (2007)

KvaP Bends Membrane - AQP0 Not

Coarse-grained simulations

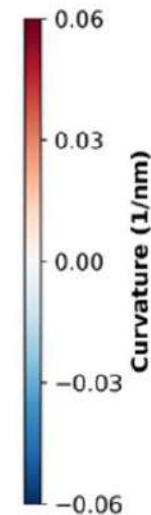
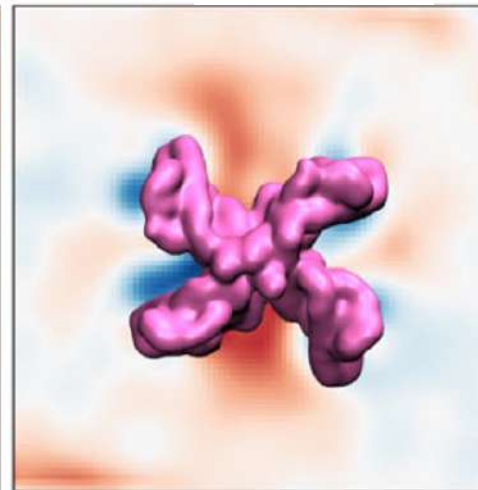
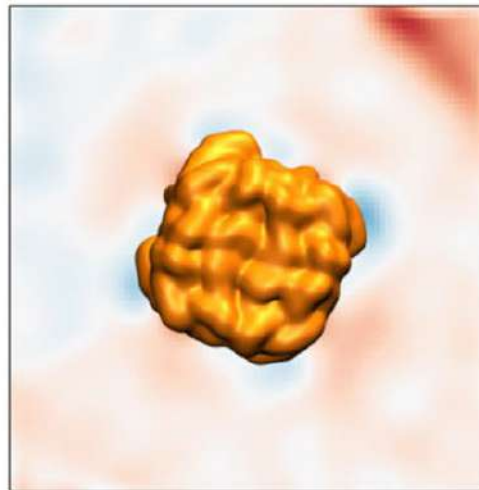
D. P. Tieleman et al *Biophys. Rev.* (2021)



AQP0

KvAP

Cylindrical



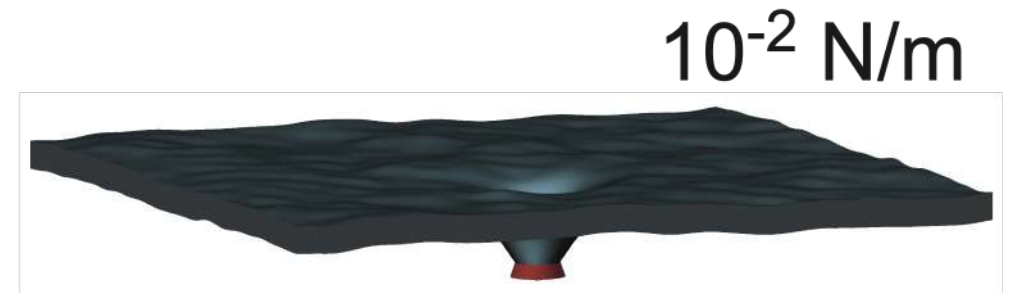
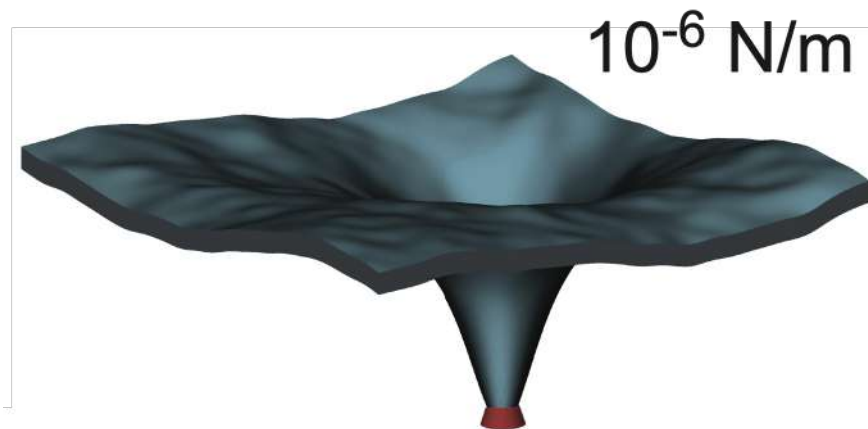
Conical



Membrane Deformation Depends on Tension



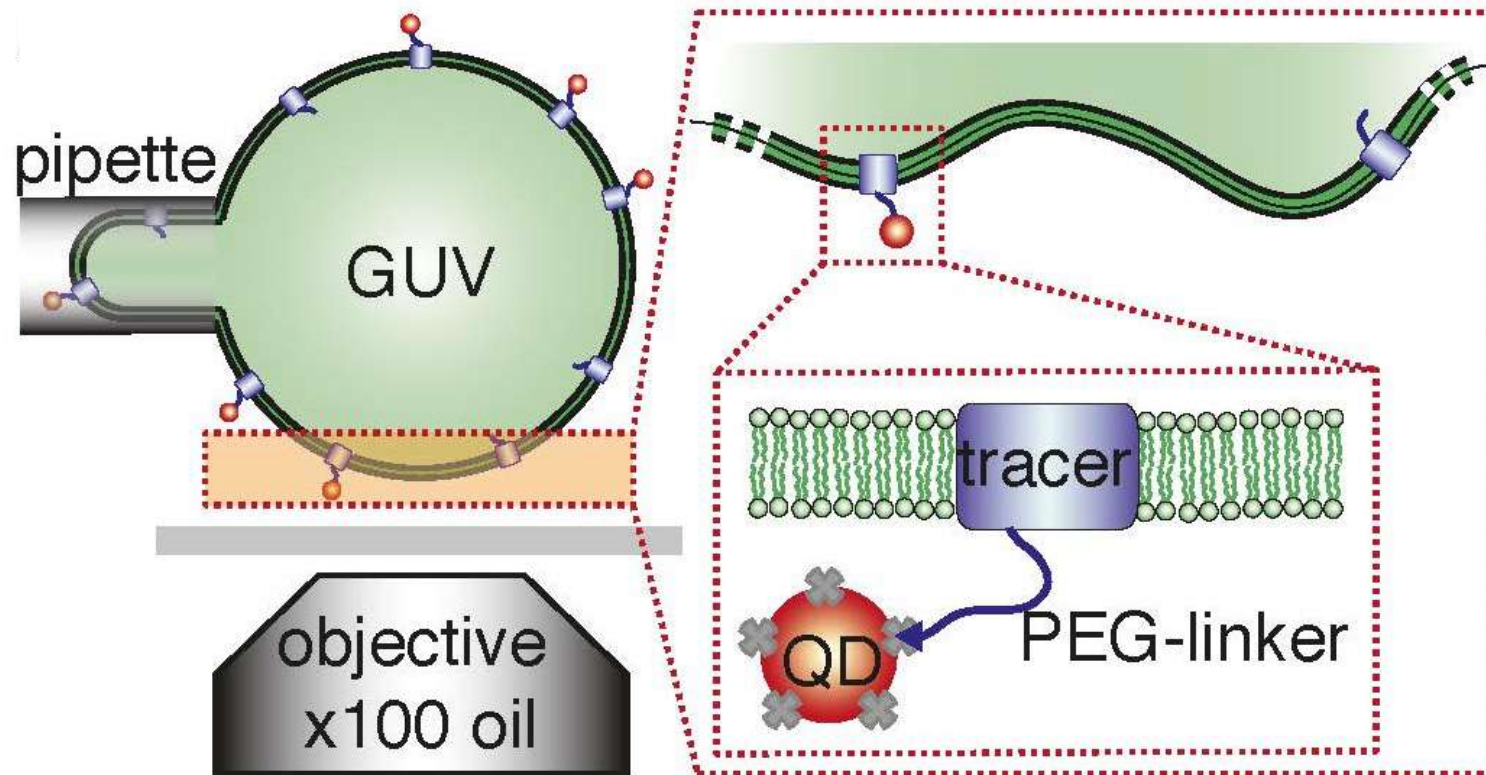
conical



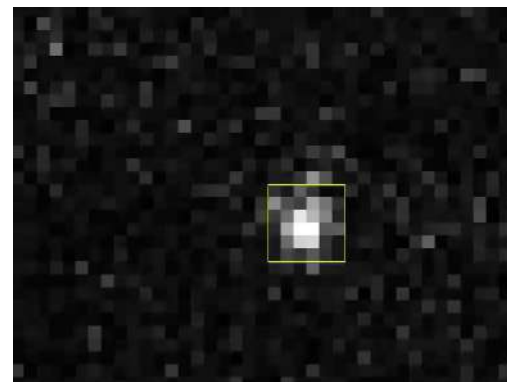
Simulations: 135x135 nm

J. Sigurdsson and P. Atzberger (UCSB)

Single Particle Tracking on GUVs

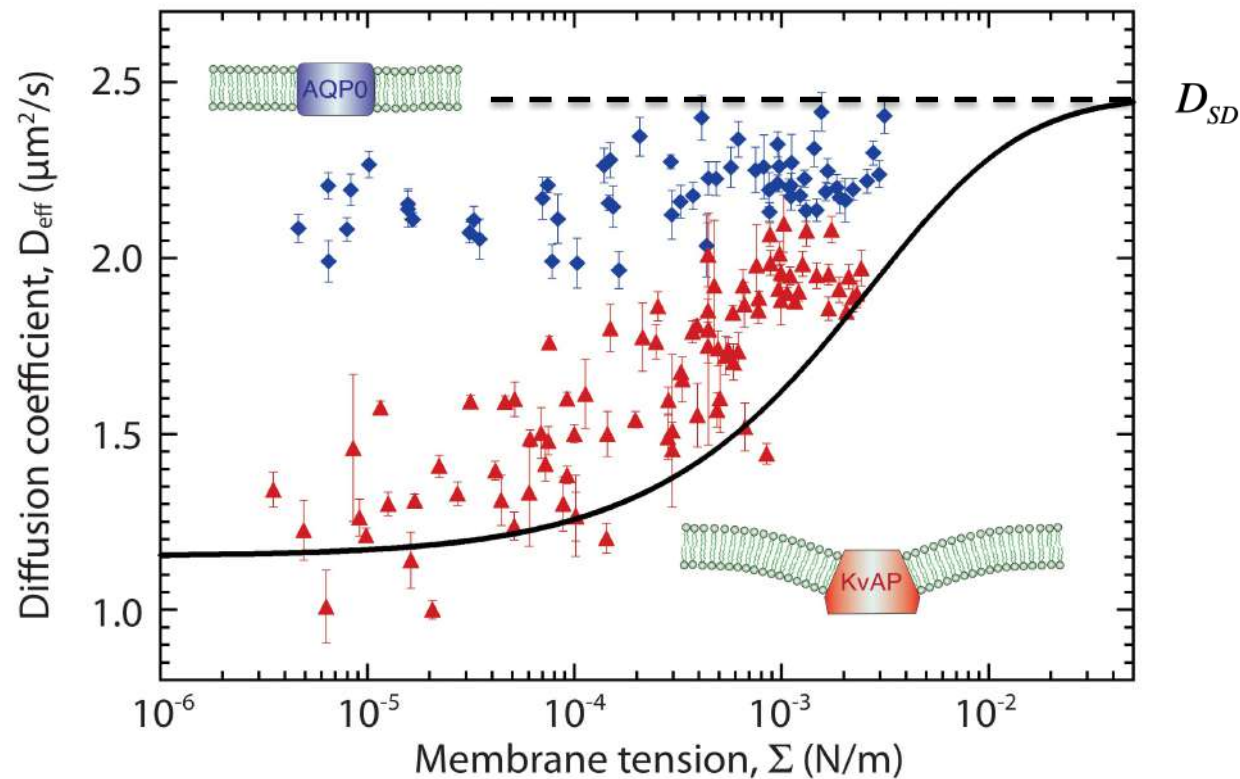


Low density:
100 proteins/ μm^2



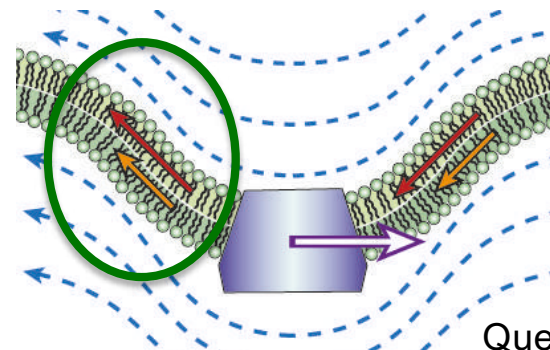
Quemeneur *et al.*,
PNAS (2014)

Effect of Membrane Tension on Diffusion



Model: *dissipation* mechanisms with the bulk and inside the bilayer

Dominant: *interleaflet friction*



D. Lacoste (ESPCI)

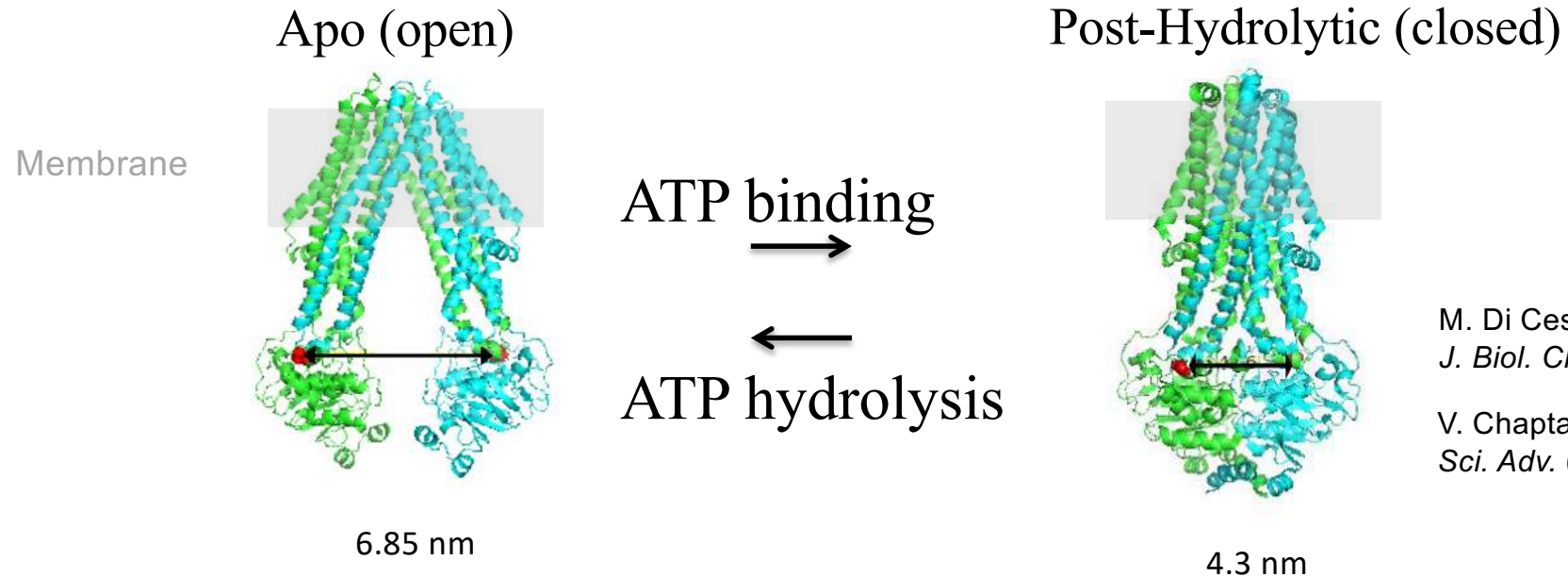
J. Sigurdsson, P. Atzberger (UCSB)

Quemeneur *et al.*, *PNAS* (2014)



BmrA

Bacterial ABC Transporter (*B subtilis*)

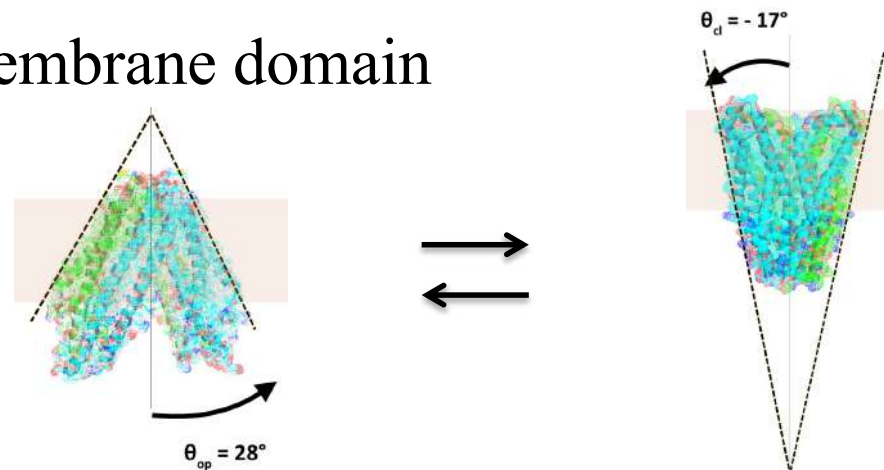


M. Di Cesare et al
J. Biol. Chem. (2024)

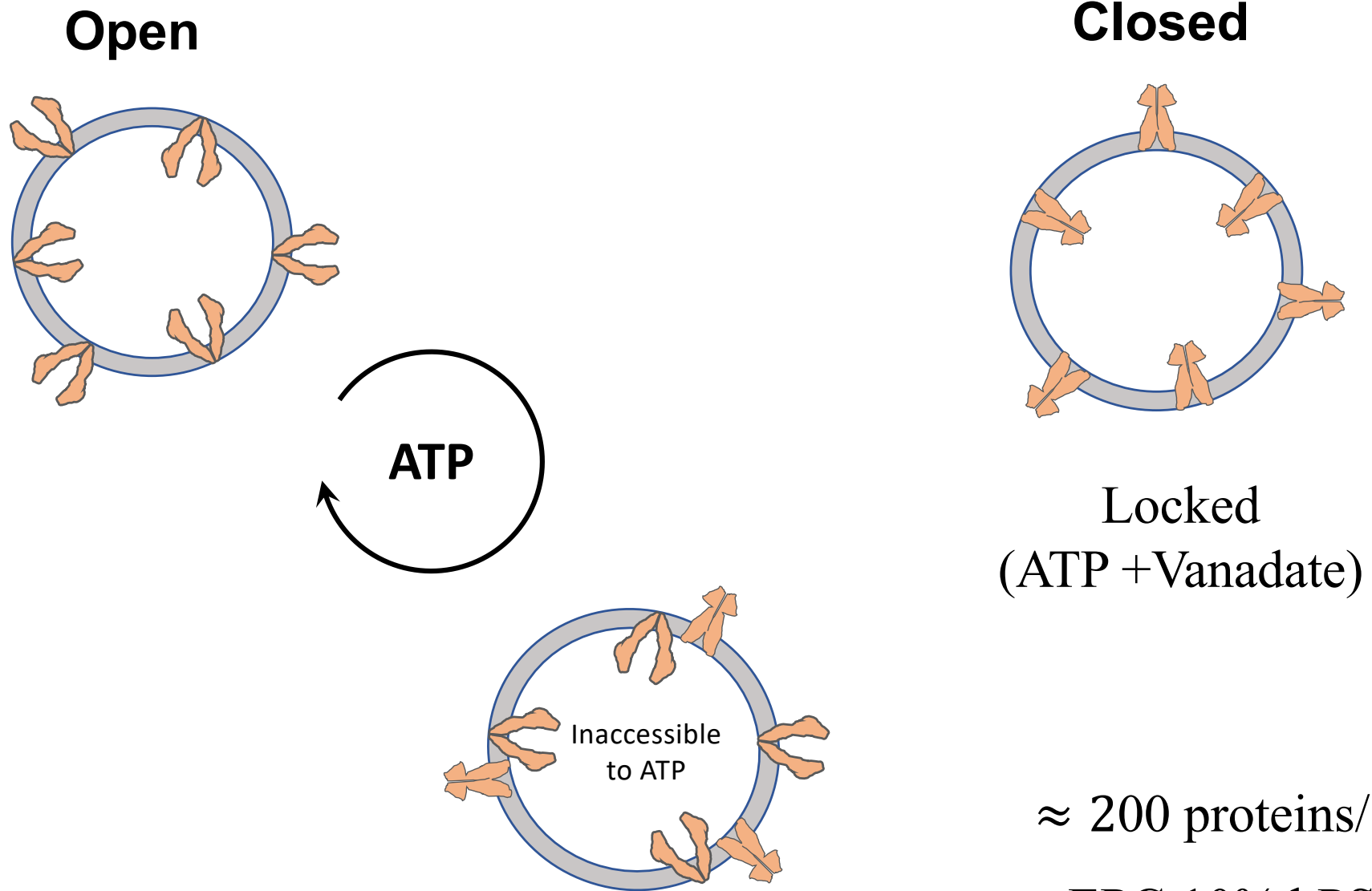
V. Chaptal et al
Sci. Adv. (2022)

Large conformational changes

Also in the trans-membrane domain



Single BmrA Diffusion in GUVs



≈ 200 proteins/ μm^2

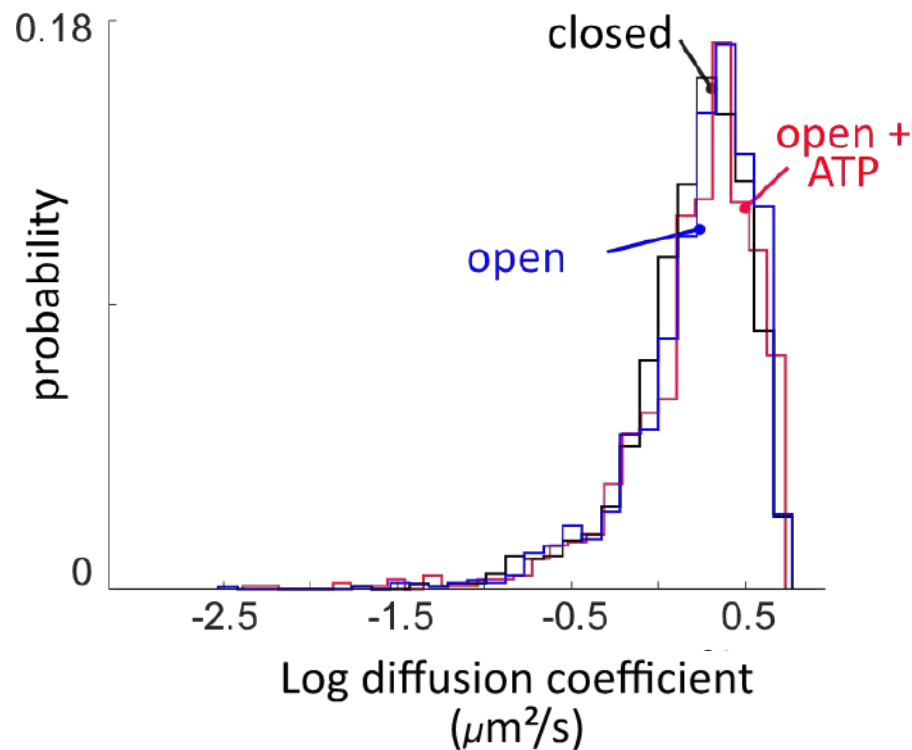
EPC:10% bPS

T=20°C

MSD Analysis :

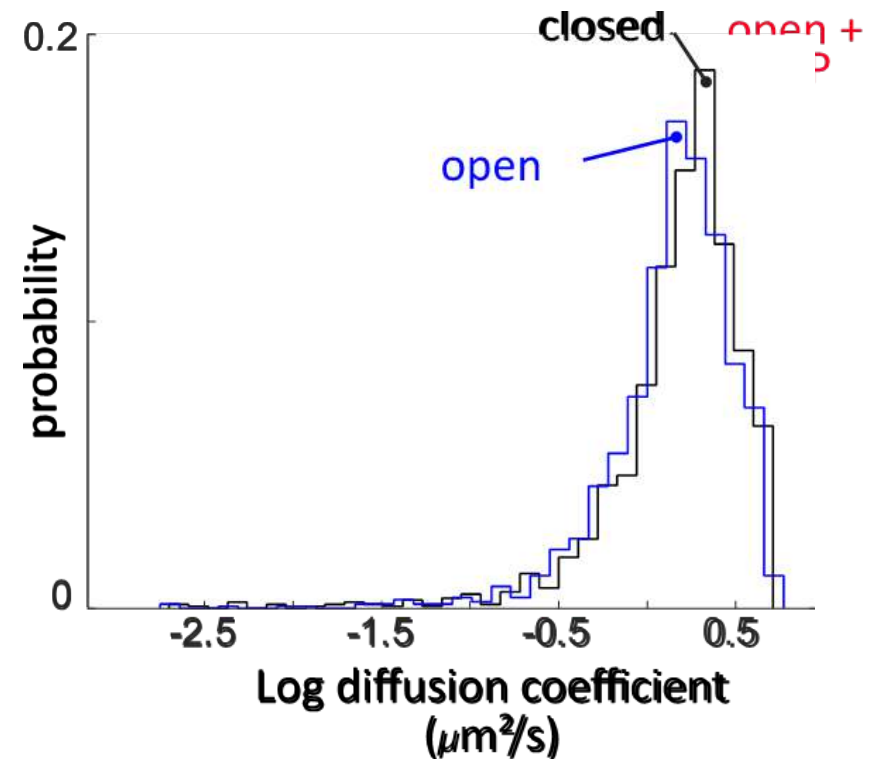
Diffusion Depends upon Activity at Low Tension

High tension ($\sim 10^{-3}$ N/m)



No difference

Low tension ($\sim 10^{-5}$ N/m)



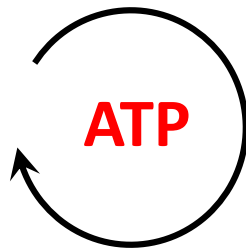
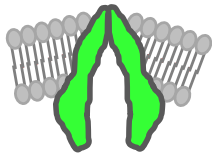
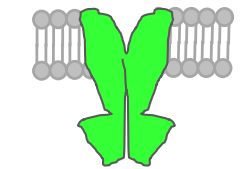
+ATP: **Non trivial**

Fast and slow diffusion

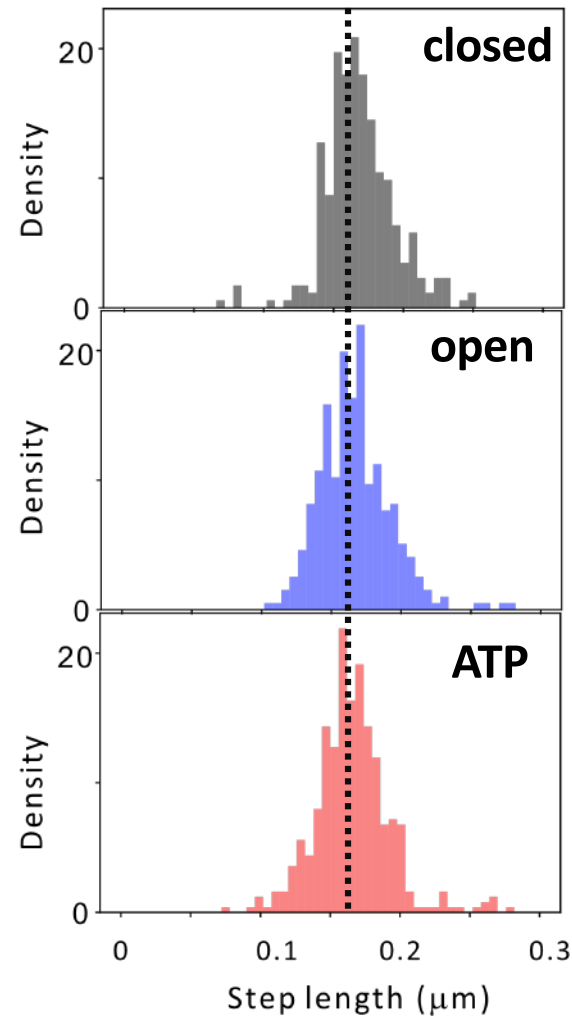
ATP-Dependent Clustering at Low Tension ?

J. Kæstel-Hansen, N. Hatzakis
Machine learning approach

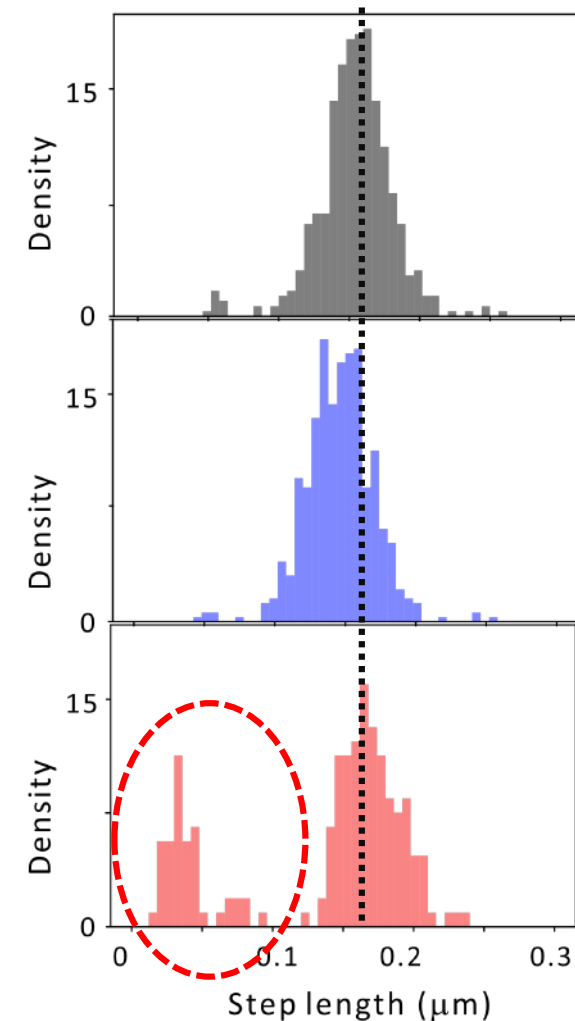
$\Delta t = 5$ ms



High tension



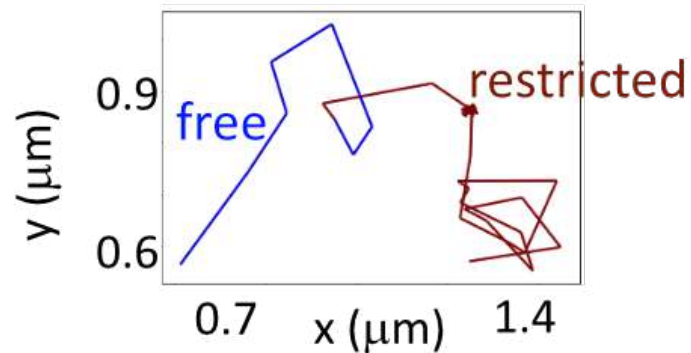
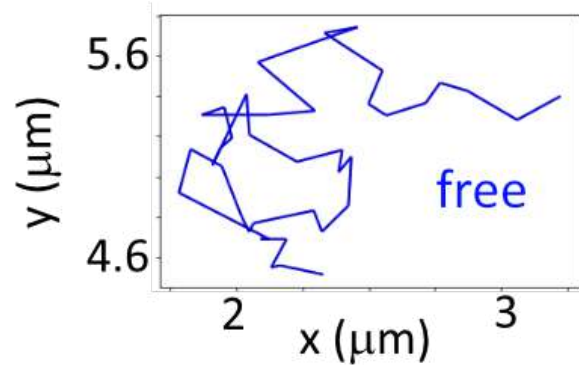
Low tension



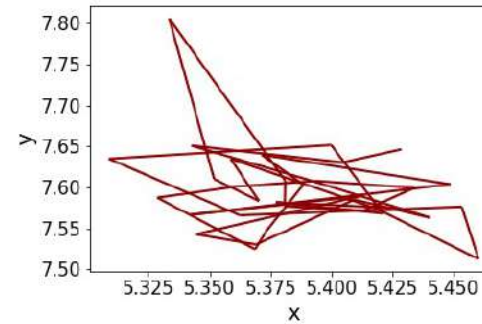
Upon ATP Activation, Restricted Motion

Segmentation (Deep Learning)

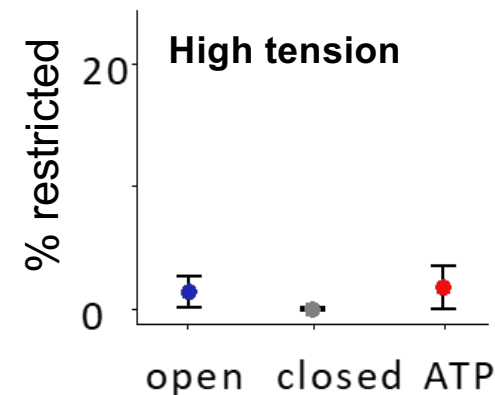
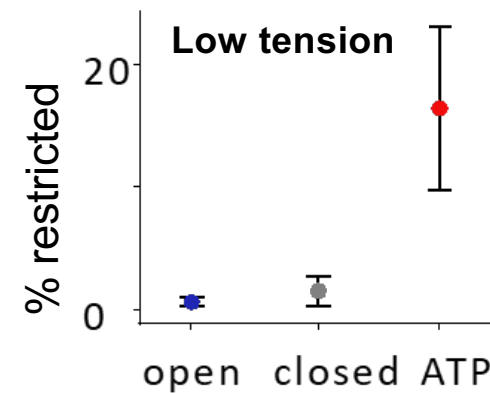
Trajectories ≤ 1 sec



only restricted



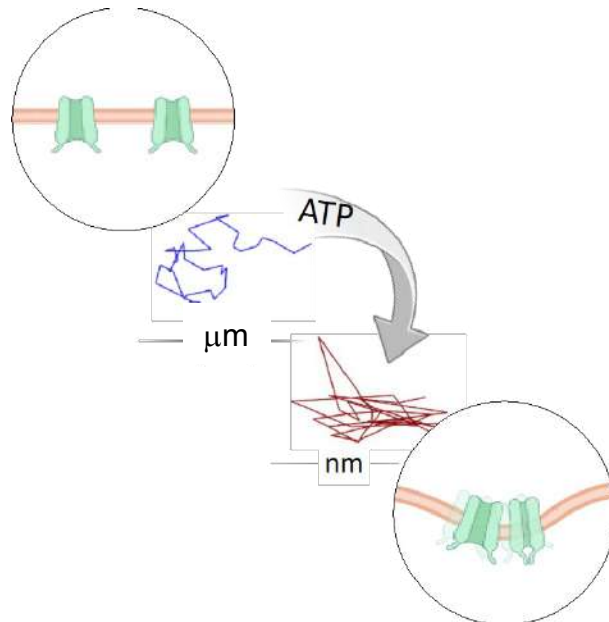
Restricted area
 $\sim$ psf



Restricted motion $\longleftrightarrow$ Higher local density of proteins
Protein clusters

- Protein *activity* induces *clustering*
- Significant at low membrane tension, disappears at high tension

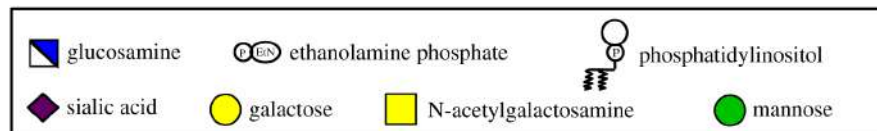
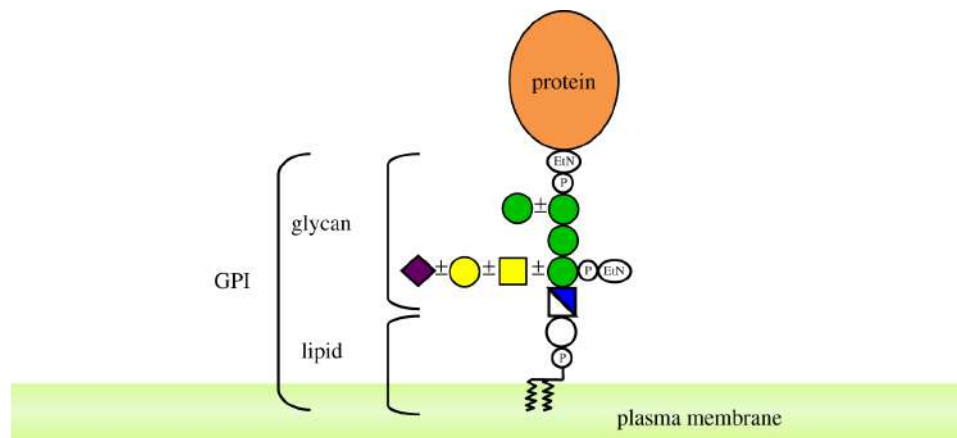
 membrane-mediated



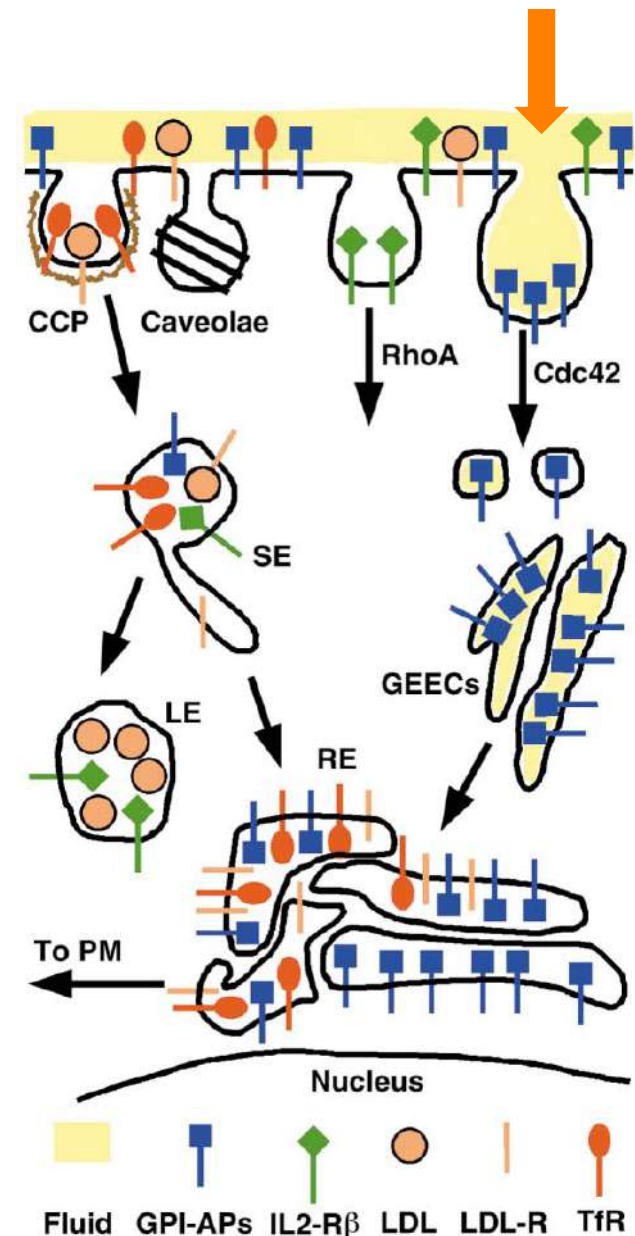
Mechanism ????

Clustering via Cytoskeleton and Motors

GPI-Anchored Proteins: Clathrin-Independent Endocytosis



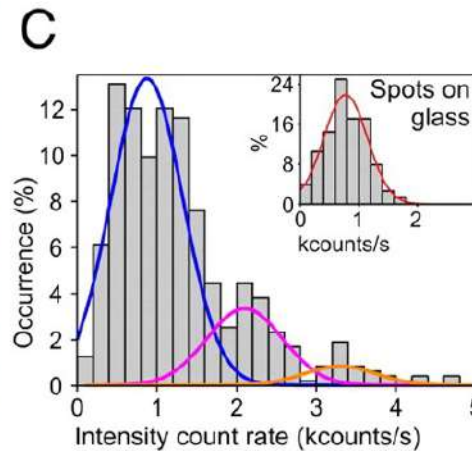
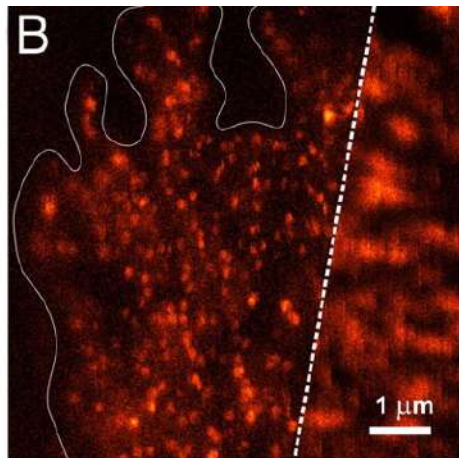
T. Kinoshita *Open Biol* (2020)



S. Sabharanjak... **J. Mayor** *Dev. Cell* (2002)

GPI-Anchored Protein Clustering

Single-molecule Near-field Optical Microscopy – Non activated monocytes

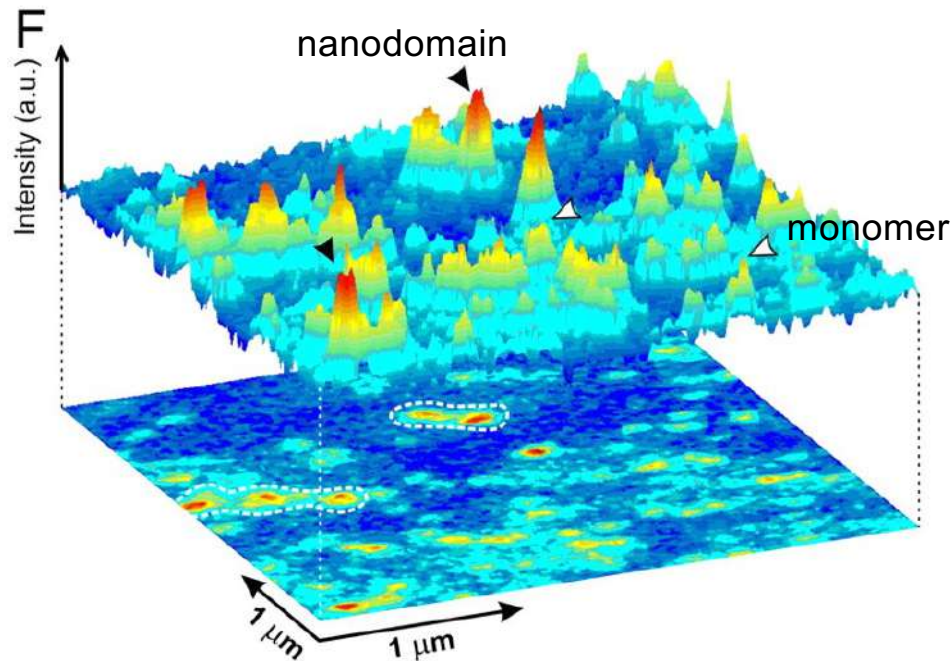


Nanodomains

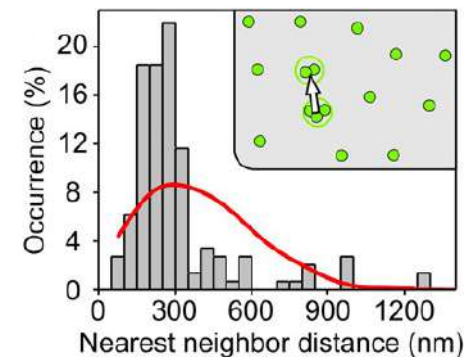
Dimers: 19%

Trimers 5%

Oligomers: 5%

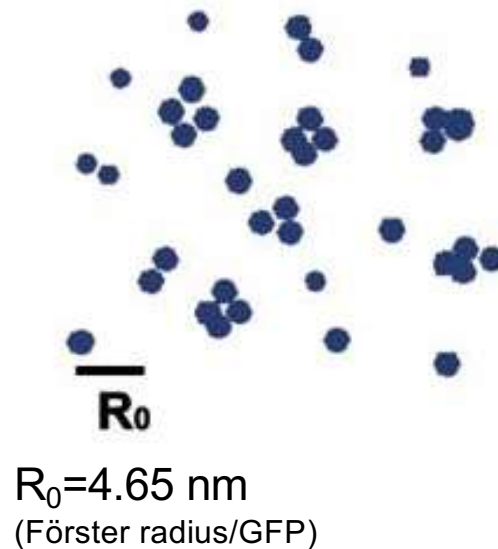


Nano-domains (4-5 nm)
not randomly distributed



GPI-Anchored Protein Clustering

Also: GPI-AP nanodomains on CHO cells (fluorescence anisotropy)

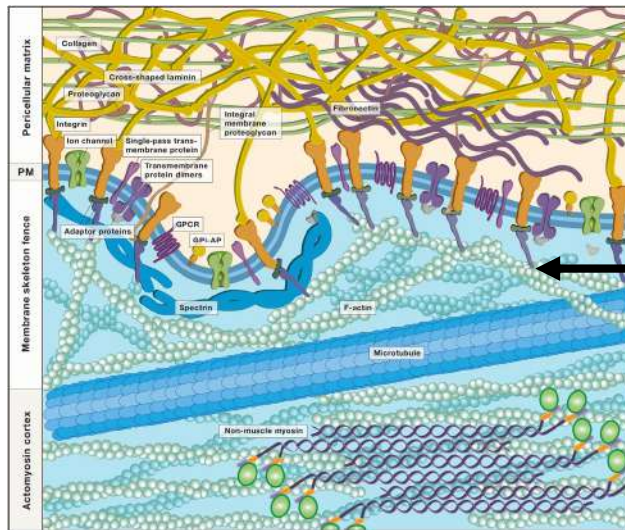


+ Role of Cholesterol and Sphingolipids

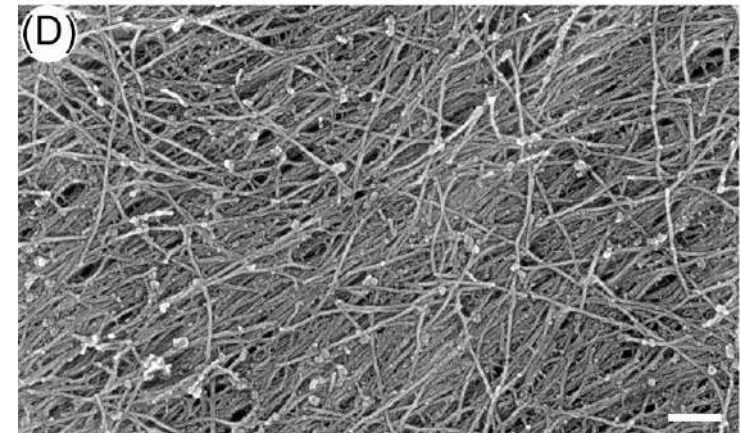
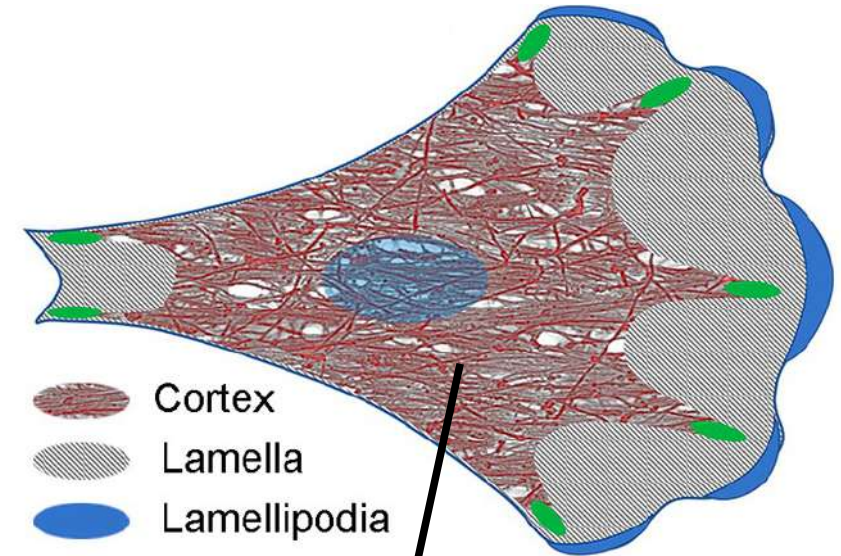
Not randomly mixed: *active* process?

P. Sharma... **M. Rao, S. Mayor**, *Cell* (2004)

Correlation between Distribution and Dynamics of Nanoclusters and Cortical Actin



K. Jacobson et al *Cell* (2019)



T.M. Svitkina *Trends Cell Biol.* (2020)

200 nm

Correlation between Distribution and Dynamics of Nanoclusters and Cortical Actin

Nanoclusters: spatial distribution and dynamics (formation, break-up)

↔ Local cortical Actin active remodeling ((de)polymerization, acto-myosin contractility)

Different signs of an *active process*

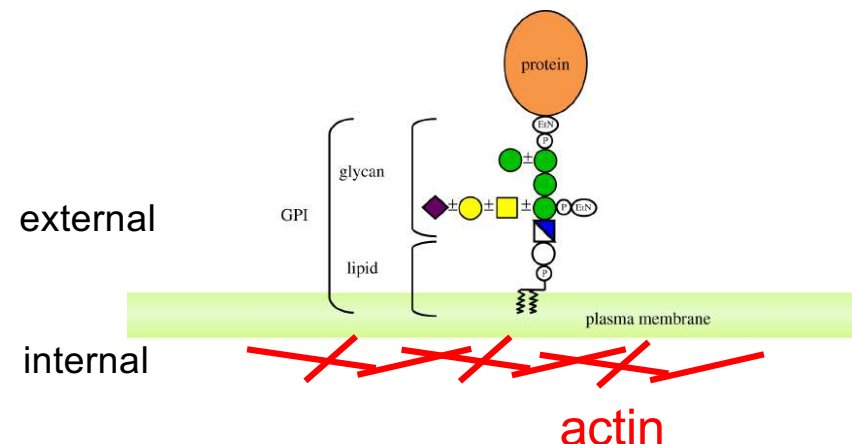
(i.e. exponential tails of distributions)

2 scales: nanodomains (<10 nm)

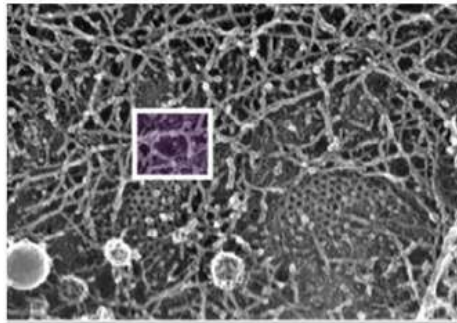
larger domains (450 nm) where nanodomains concentrate (Cf rafts)

Coupling between GPI-AP and actin??

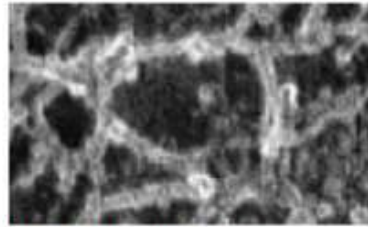
Cholesterol important



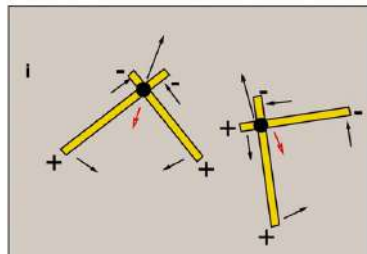
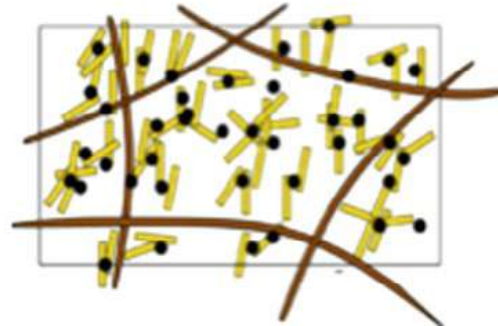
Active Clustering (Model)



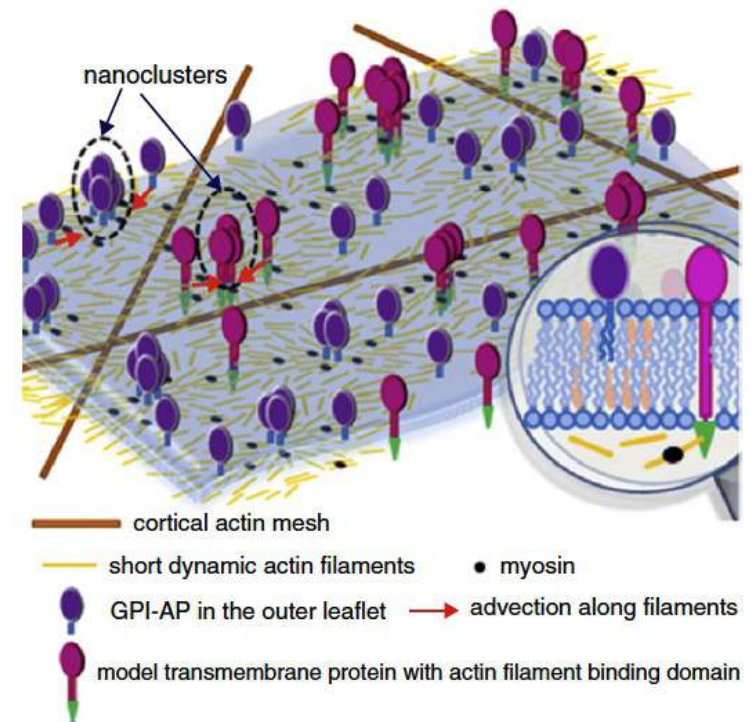
Stable crosslinked actin filaments



Short dynamic actin

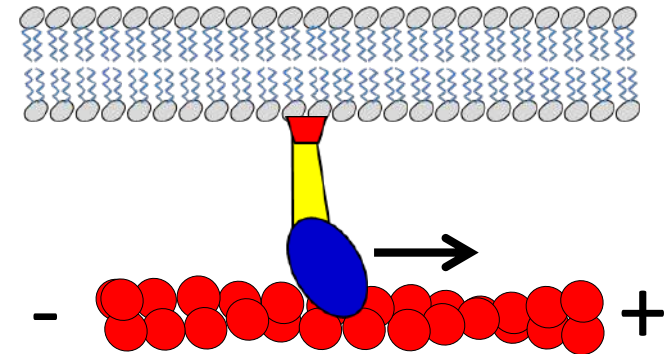
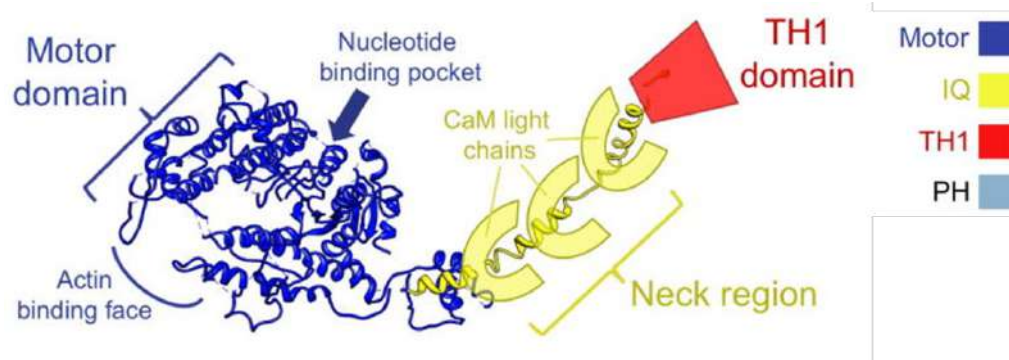


Myosin motors crosslink
short actin filaments
+ reorganize them (asters)

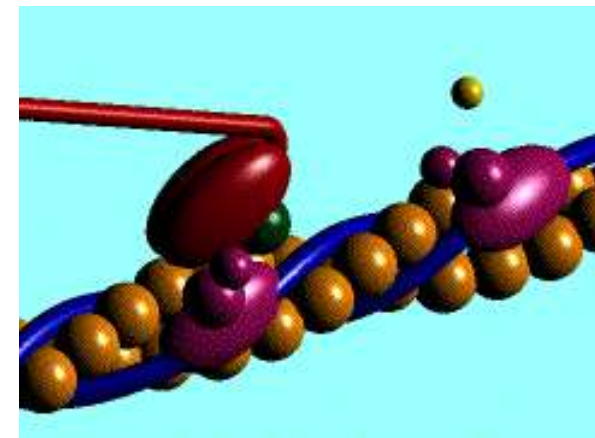
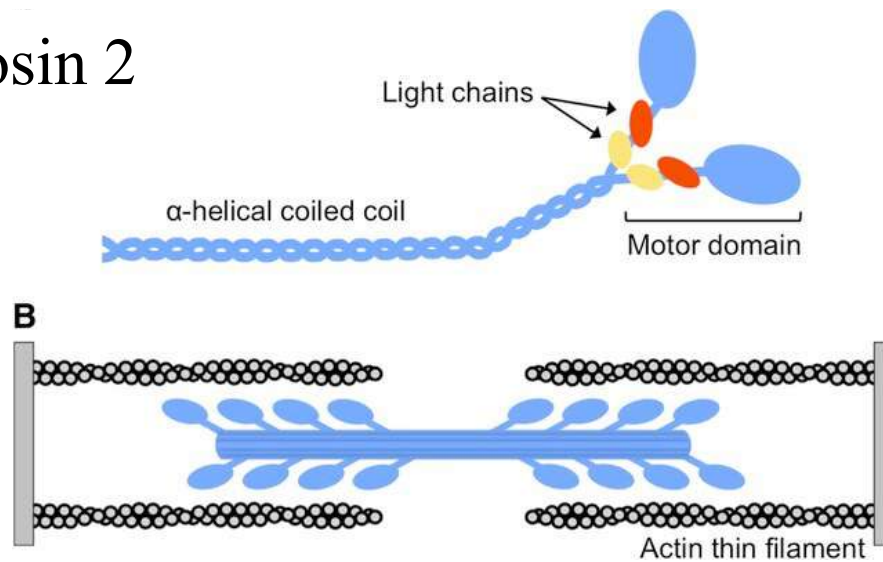


Myosins

Myosin 1



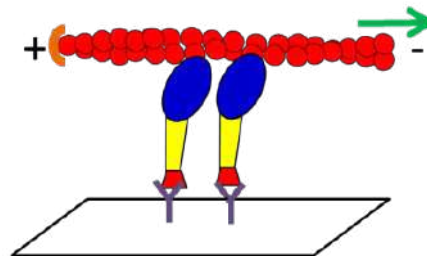
Myosin 2



Can for short bundles

Gliding Assays

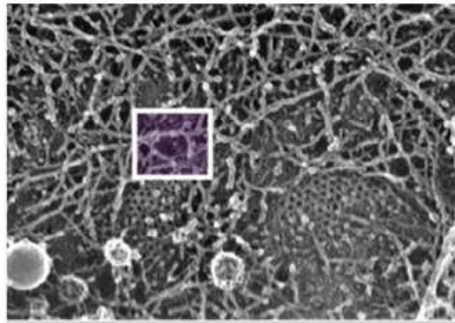
Stabilized F-actin



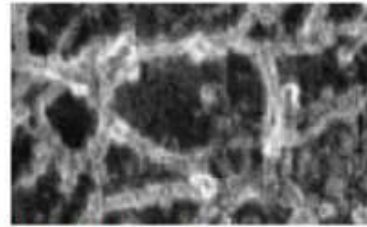
X 200 times

J. Pernier

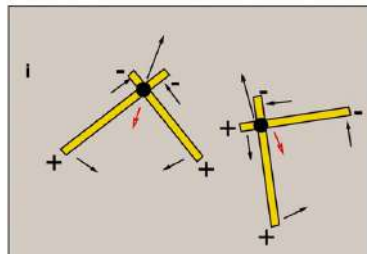
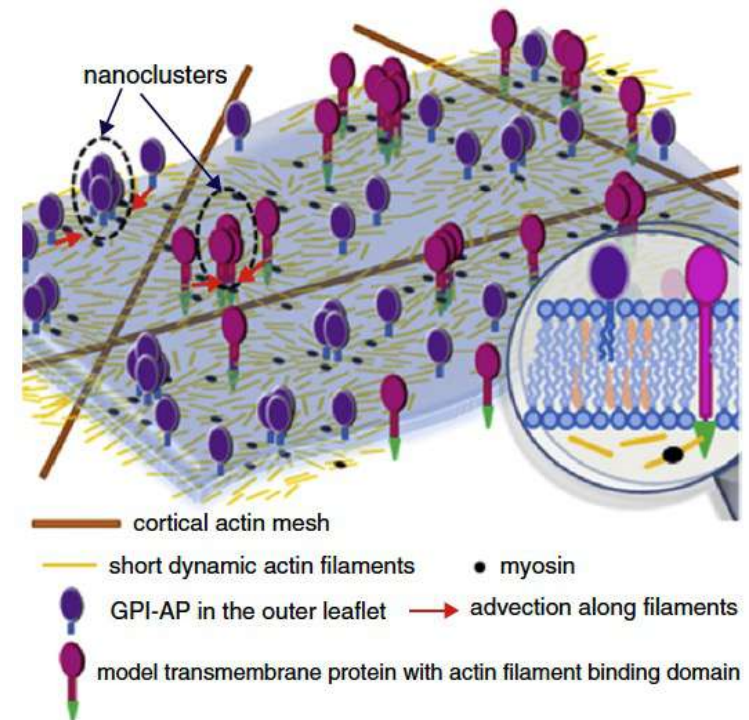
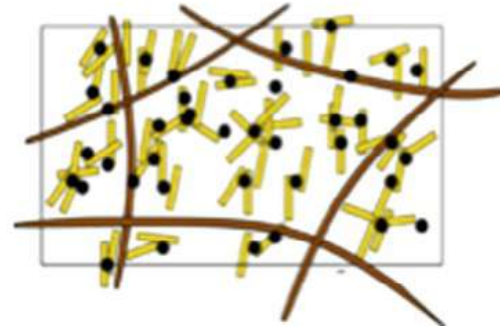
Active Clustering (Model)



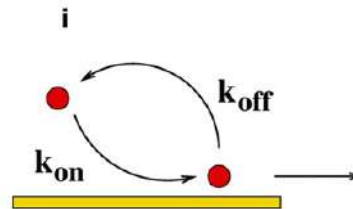
Stable crosslinked actin filaments



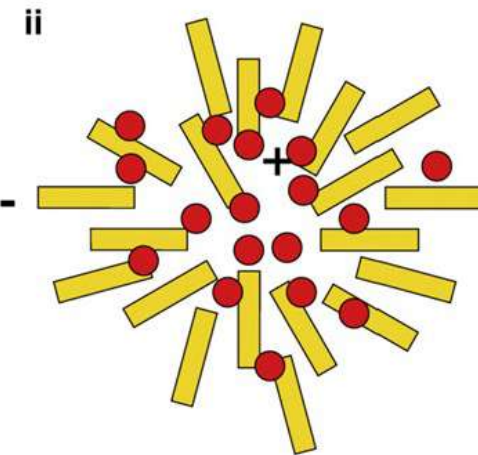
Short dynamic actin



Myosin motors crosslink
short actin filaments
+ reorganize them (asters)



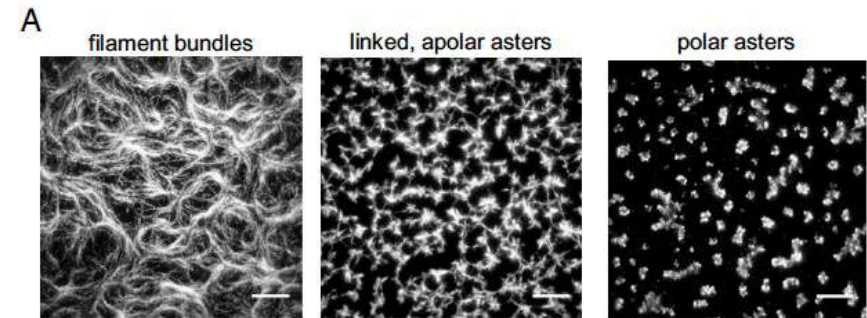
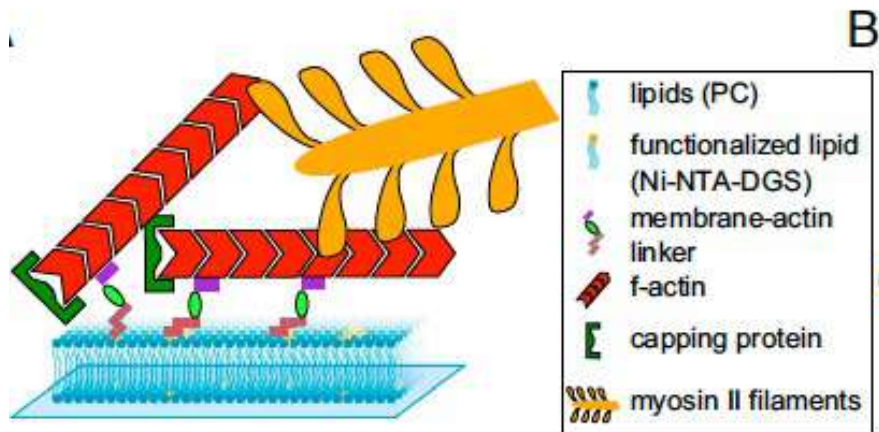
Passive molecules
(GPI-AP) bind,
advected to aster/core



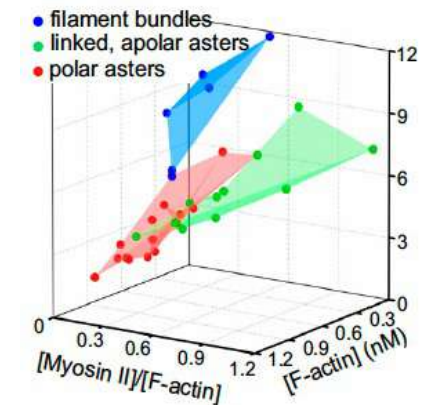
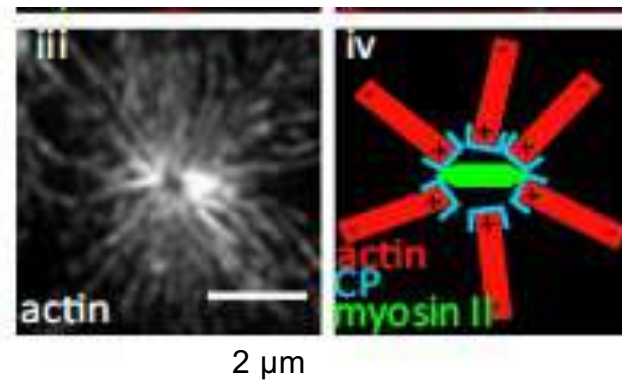
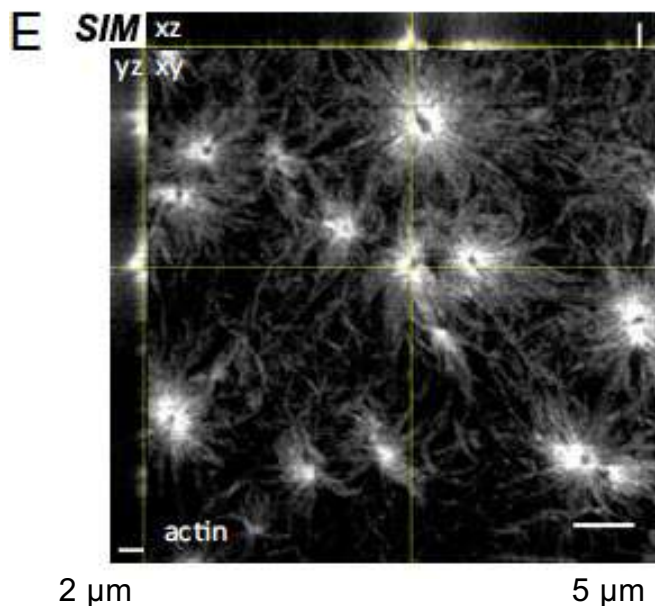
K. Gowrishankar ... **S. Mayor, M. Rao** *Cell* (2012)
M. Rao, S. Mayor, *Curr. Opin. Cell Biol.* **29**, 126 (2014)

Active Clustering (*in vitro* Exp.)

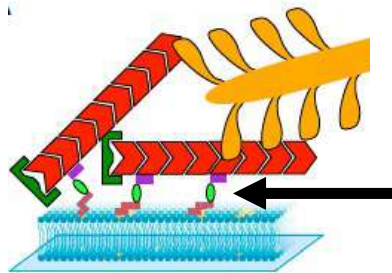
3 actin organizations



Polar asters



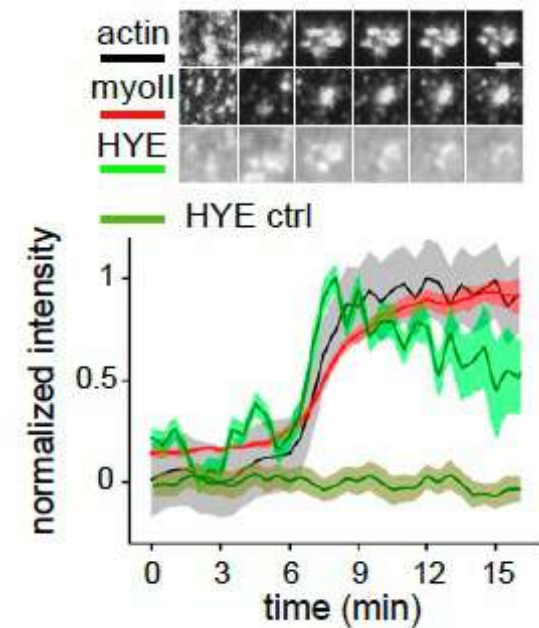
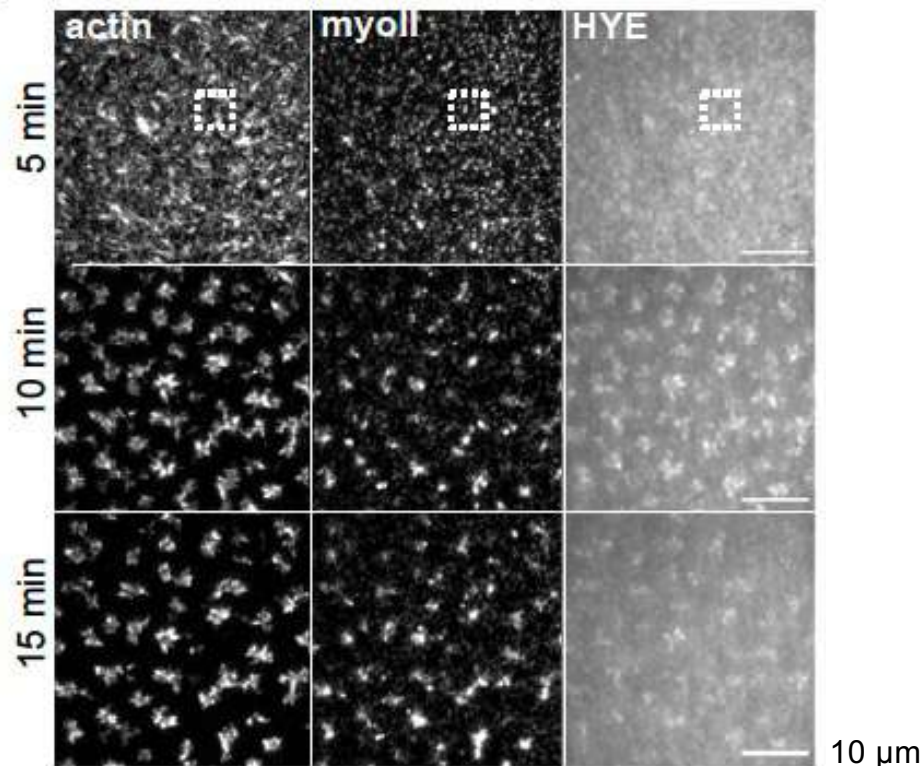
Active Clustering (*in vitro* Exp.)



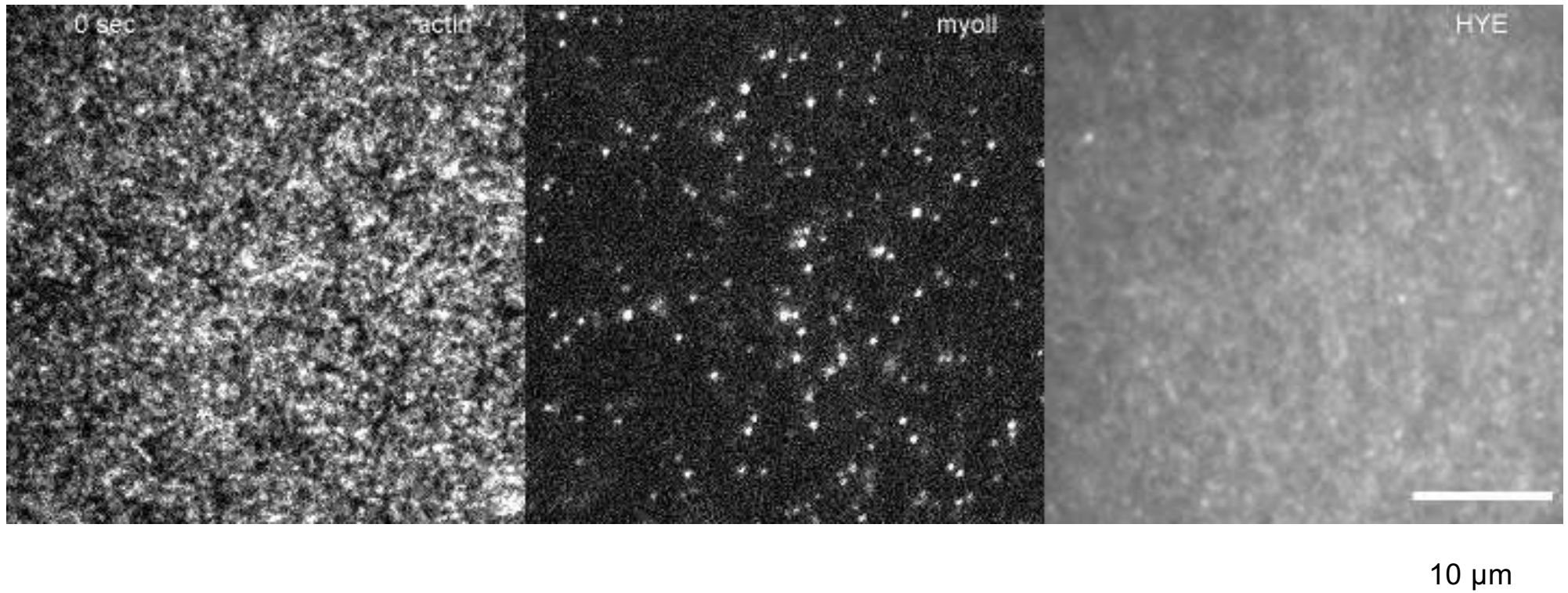
Actin-membrane linker

HYE 10x His YFP EzrinABD

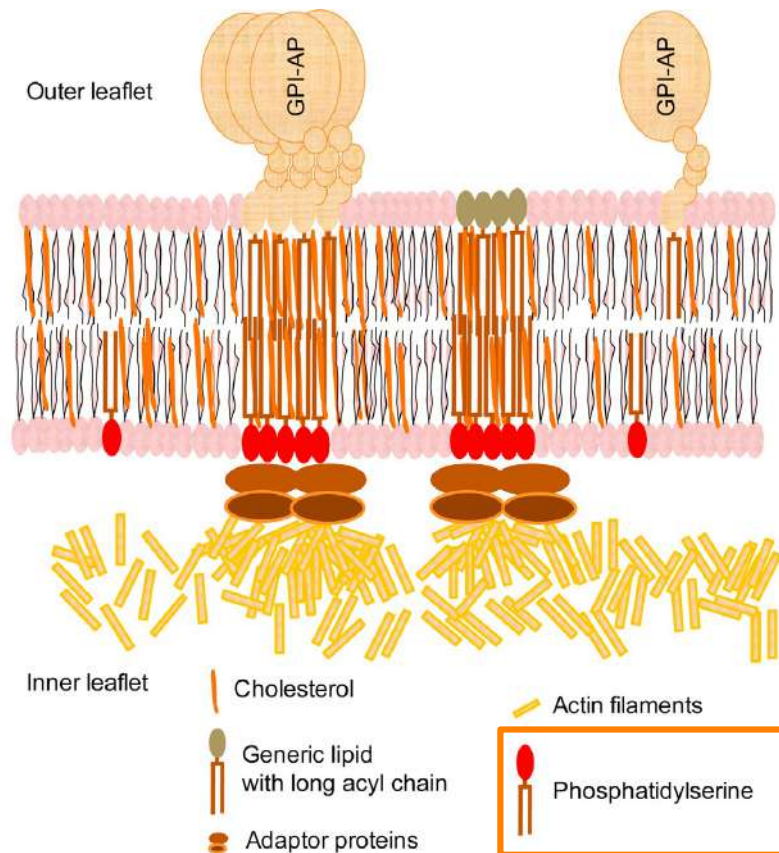
HYE clustering upon aster formation Only when actomyosin dynamical



Active Clustering (*in vitro* Exp.)

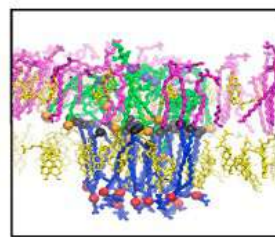
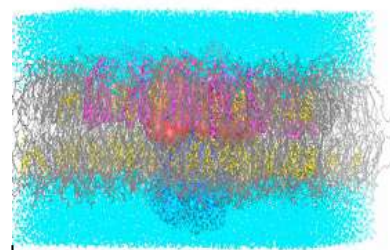


Trans-Bilayer Coupling

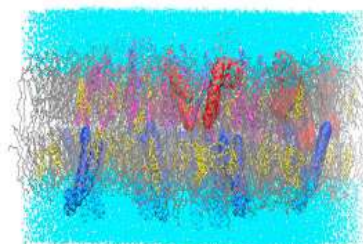


Requires:

- Long chain PS lipids
- Long saturated GPI lipids
- Cholesterol



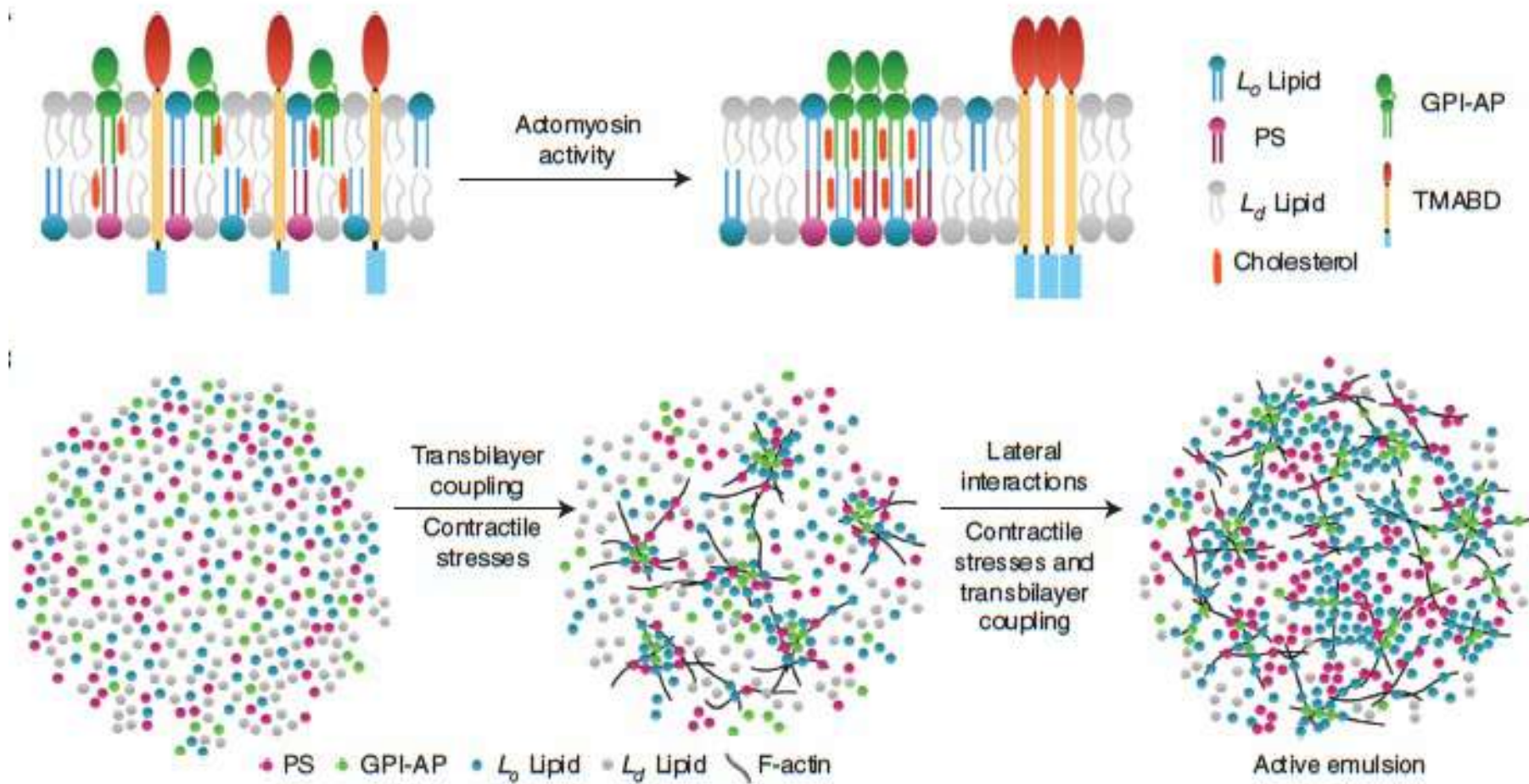
PS immobilized



GPI or GPI
PS Cholesterol
Sphingomyelin

D.V. Köster ... M. Rao, S. Mayor *PNAS* (2016)

New Vision of the PM: Active Emulsion



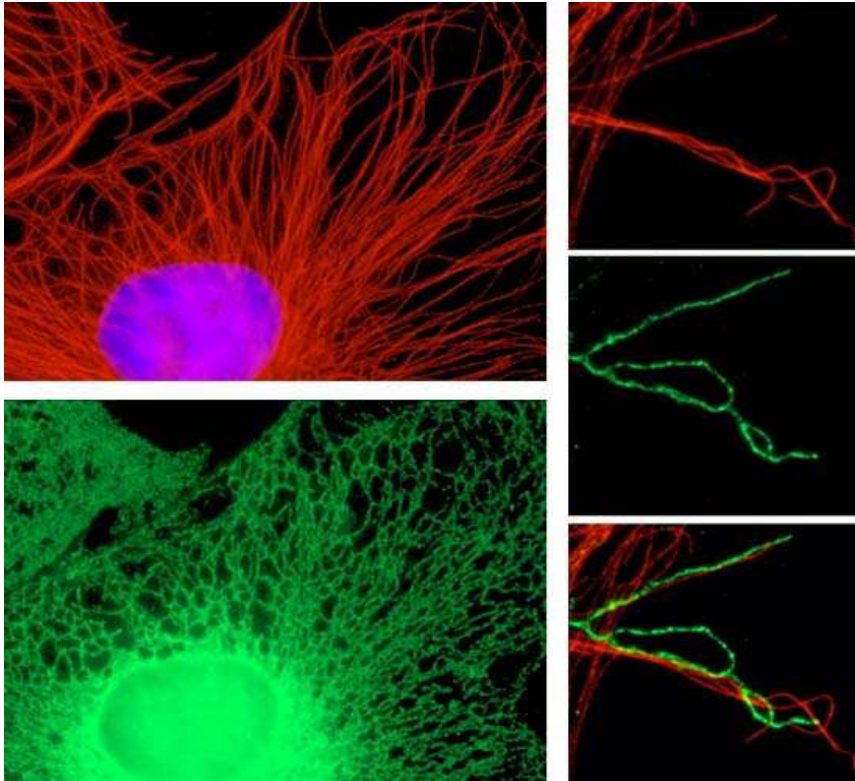
S. Saha... **S. Mayor, M. Rao** *PNAS* (2022)

S. Mayor et al. *Cold Spring Harb. Perspect. Biol.* (2023)

Dynamical Clustering of
Molecular Motors
to form Membrane Nanotubes
in Cells

Endoplasmic Reticulum Dynamics

MT



ER

Lane & Allan, *MBC* (1999)

ER Tubules
Form
by Sliding
along
Pre-existing
Microtubules

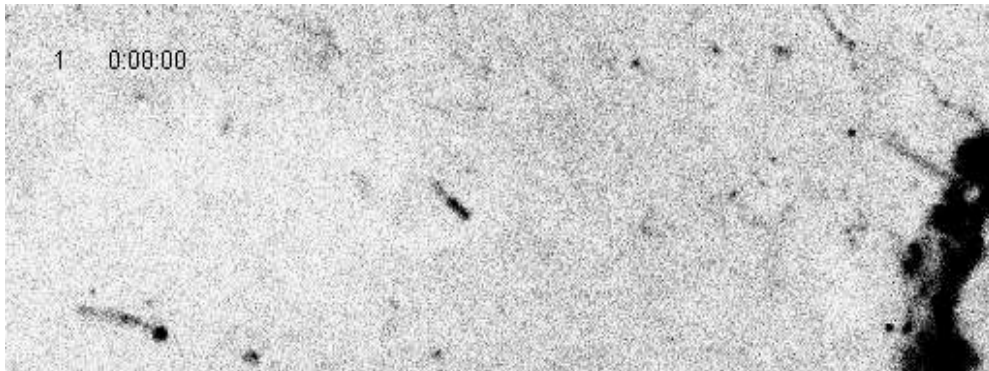
elapsed time = 3'25"

Waterman-Storer & Salmon,
Curr. Biol. (1998)

Microtubules

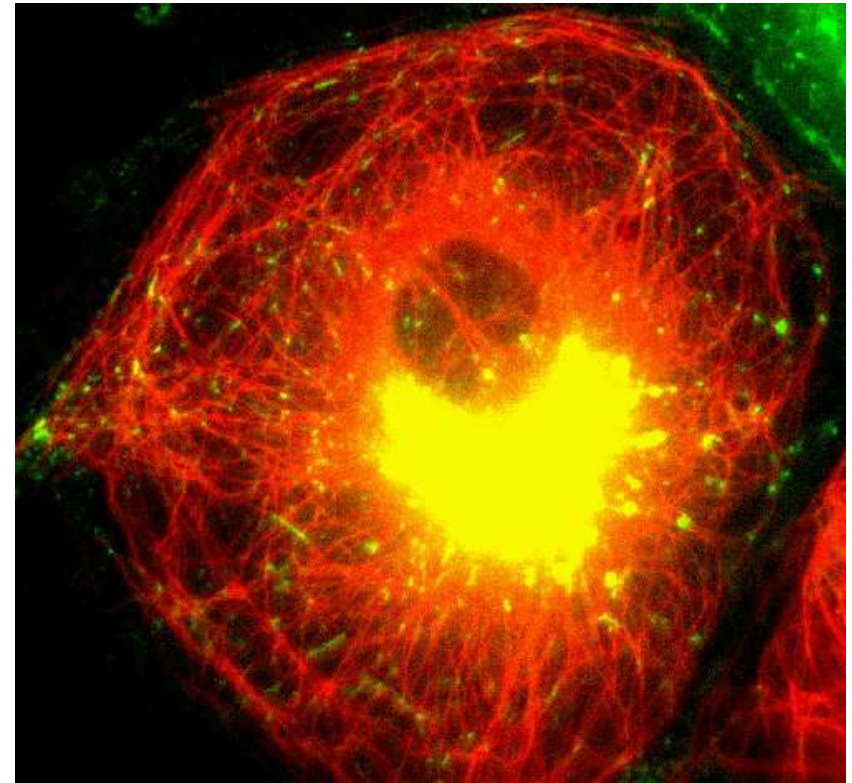
ER Membrane

Tubular Transport Intermediates



VSVG-GFP

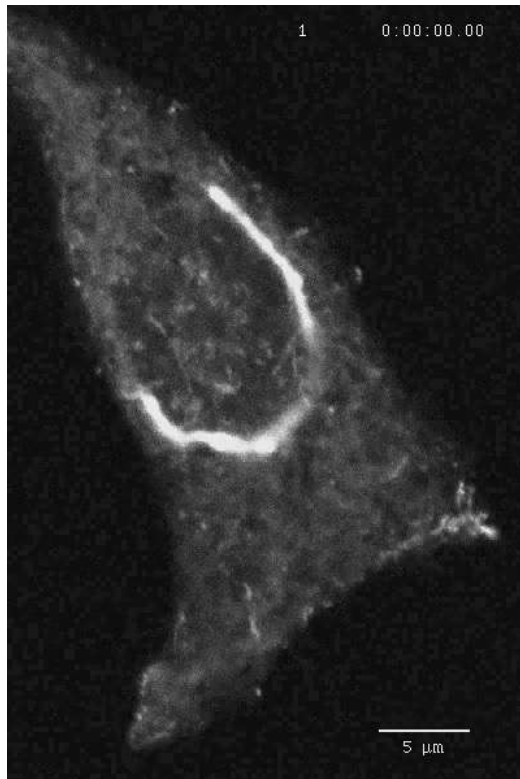
J. Lippincott Schwartz (CBMB-NIH)



Microtubules
Golgi
Overlap

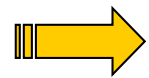
Toomre et al
J. Cell Sci. (1999)

Golgi



Trafficking of Rab6 in HeLa cell
White & al. *JCB* (1999)

No Microtubules
or Motor (kinesin) inhibition

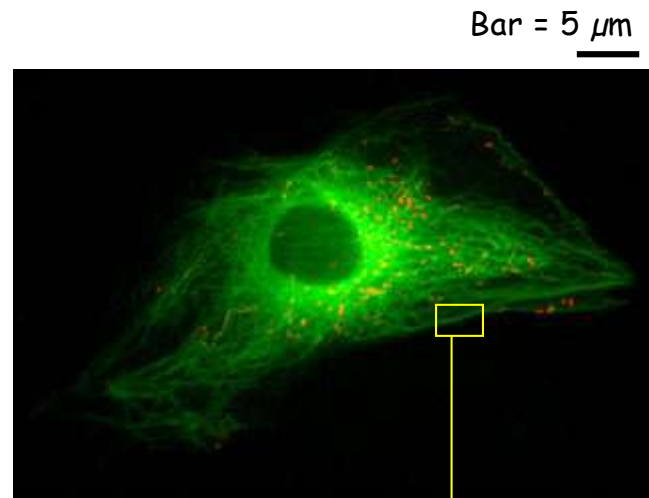


NO TUBE

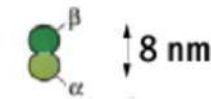
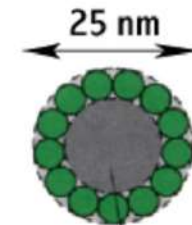
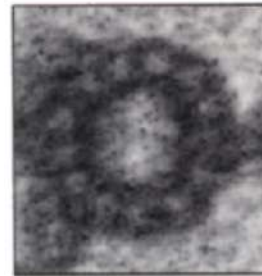


Required :
Microtubules + Motors

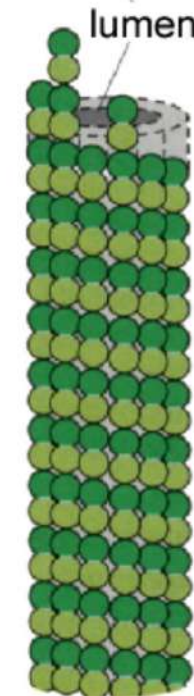
Microtubules: Rails for Membrane Transport



- Tubulin dimers self-assembled in *parallel protofilaments*
- *Hollow* rigid cylinders
- Dynamics: growth by + end but *fast depolymerization* (catastrophy)



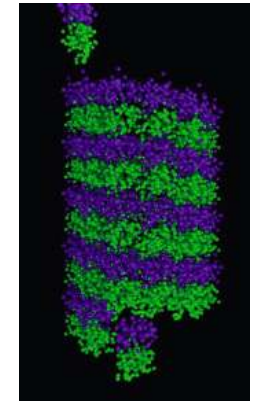
Tubulin dimer



protofilament

Plus end

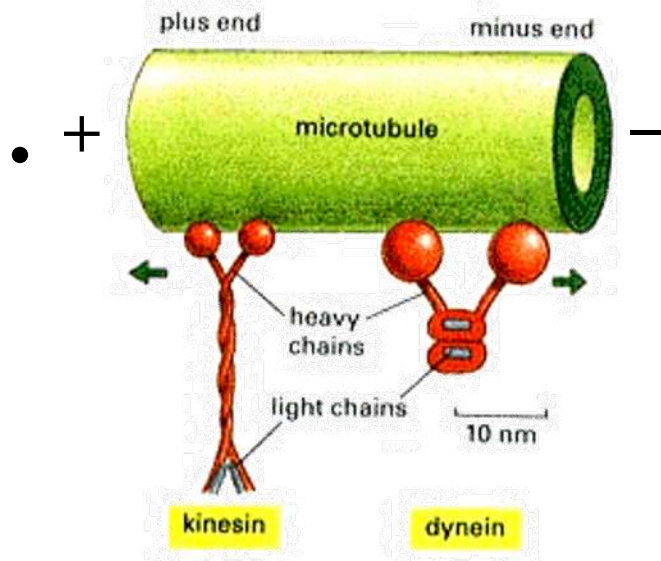
Minus end



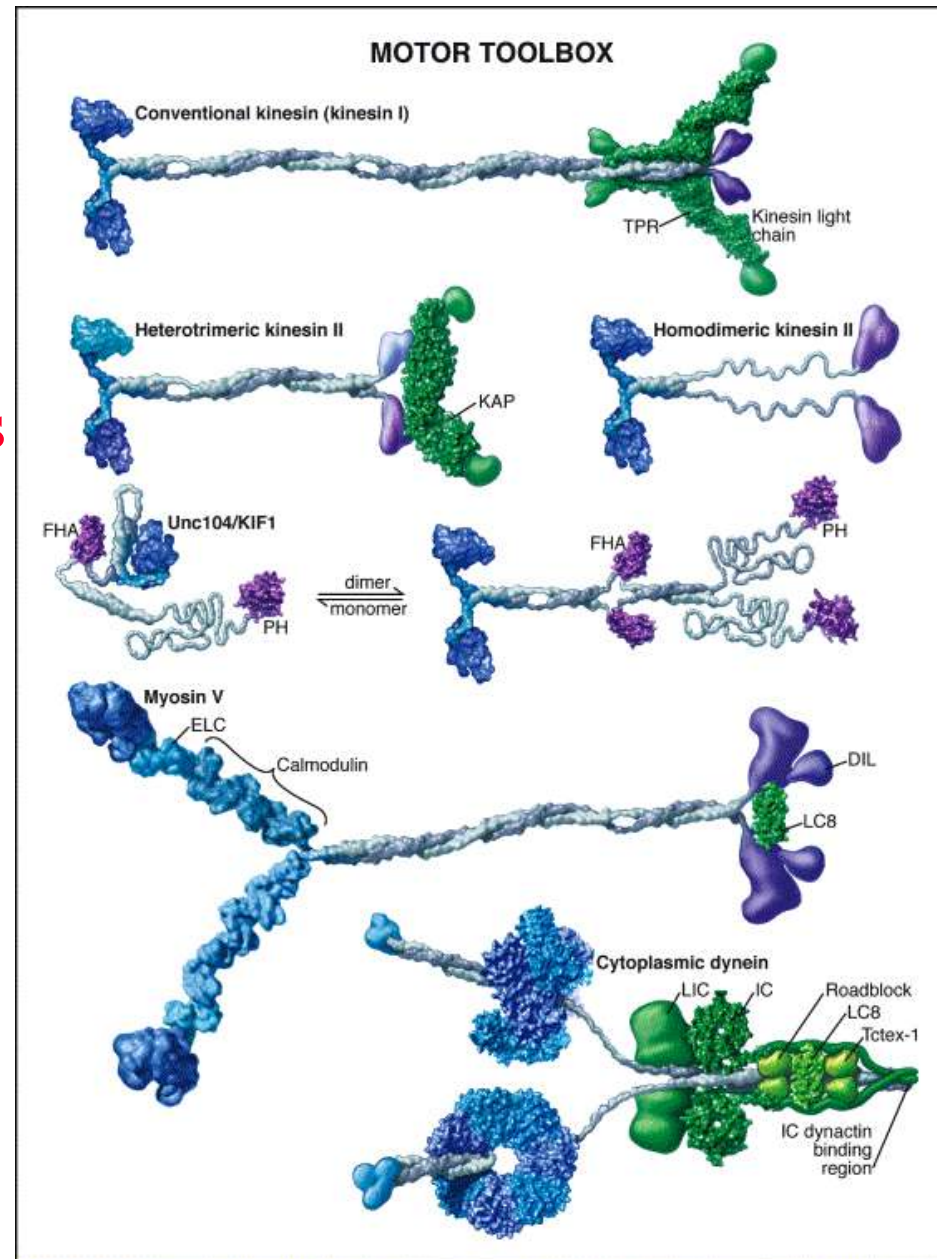
Molecular Motor Toolbox for Transport

3 motor families

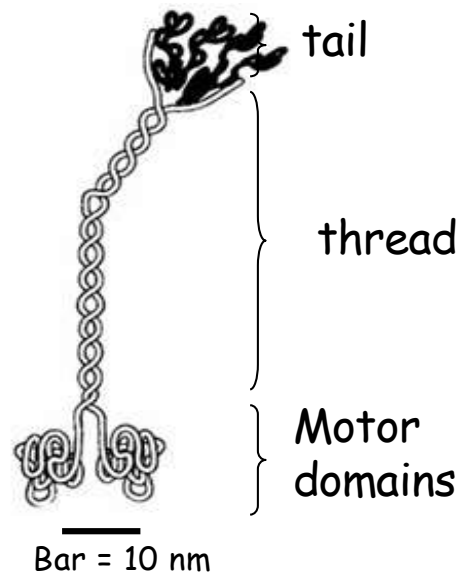
- Kinesins → Microtubules
- Dyneins



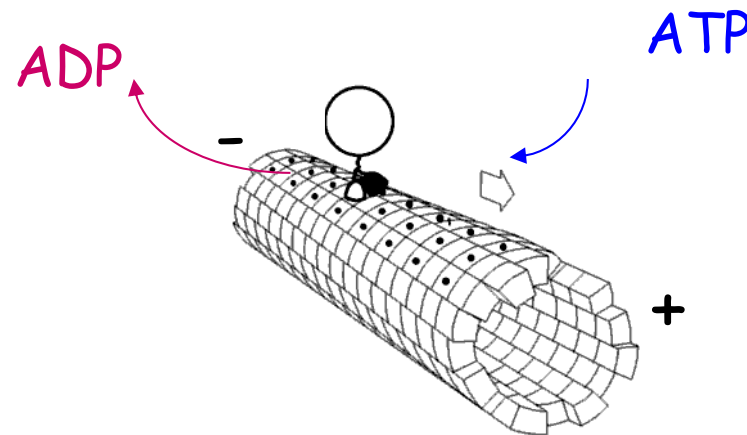
- Myosins → Actin



Kinesin-1 (Conventional): the best characterized kinesin



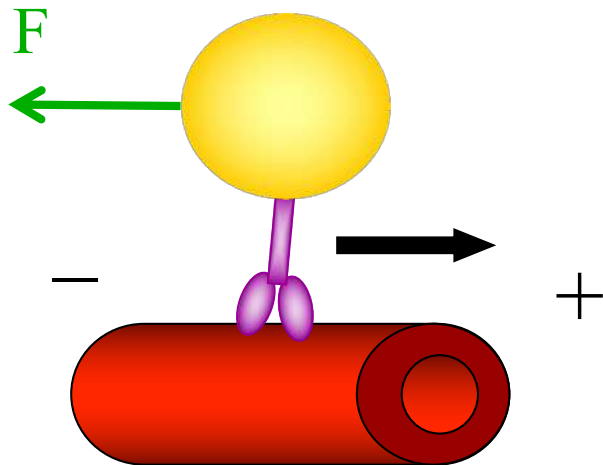
Movement along a Single Protofilament



Linear displacement

Processive motor: ≈ 100 steps before detachment

Kinesin Dynamics



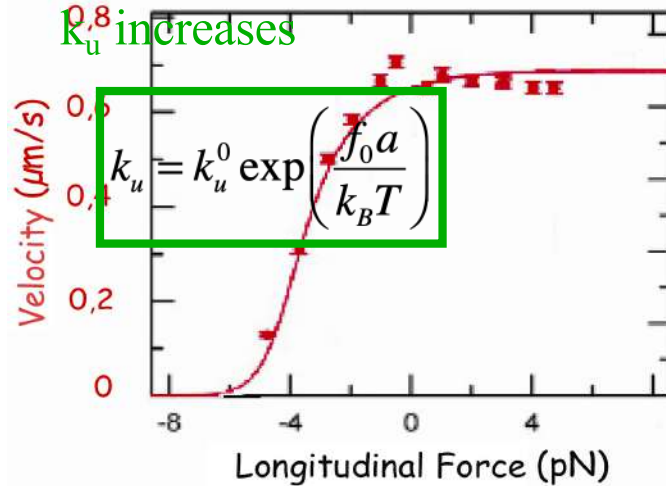
Bead assay

V_0 : velocity of kinesin in absence of external load

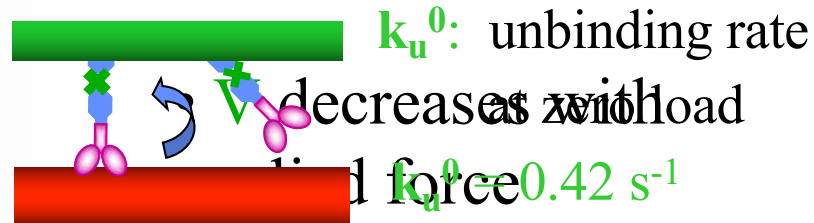
$$V_0 = 0.6 \pm 0.1 \mu\text{m/s}$$

In presence of applied force

$k_u^{0.8}$ increases

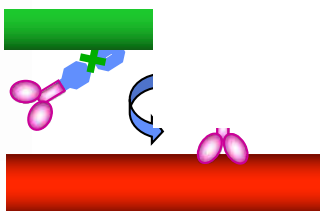


Block et al., *PNAS* (2003)



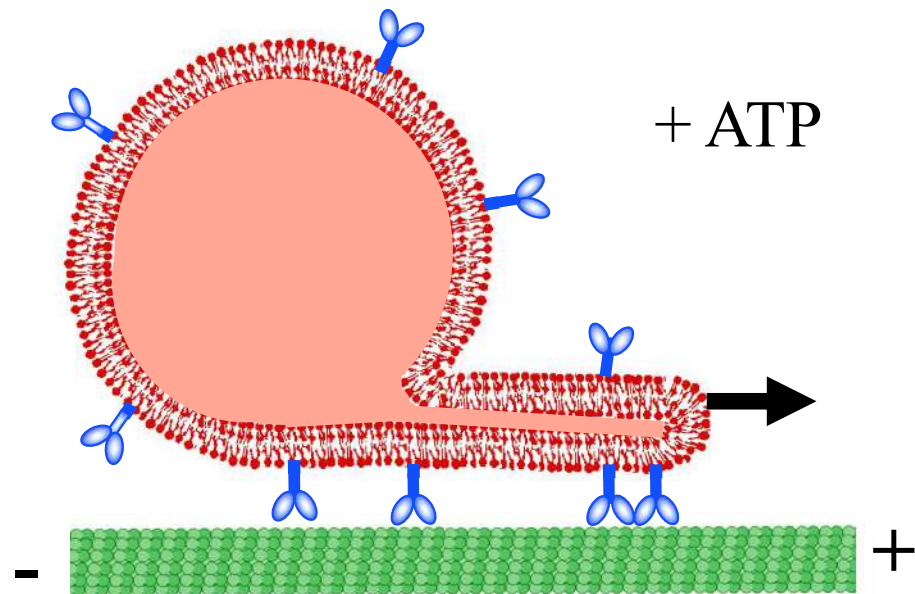
Vale et al., *Nature* (1996)

• Stall force:



KINESIN ONTO MT

Minimal Biomimetic System



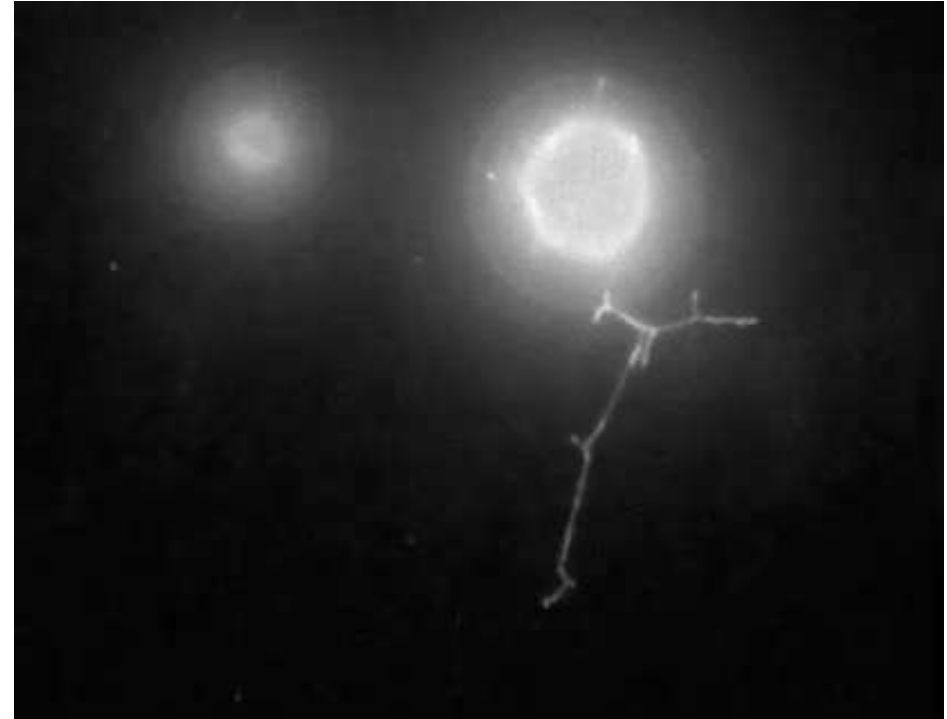
Kinesin



Microtubule



Membrane



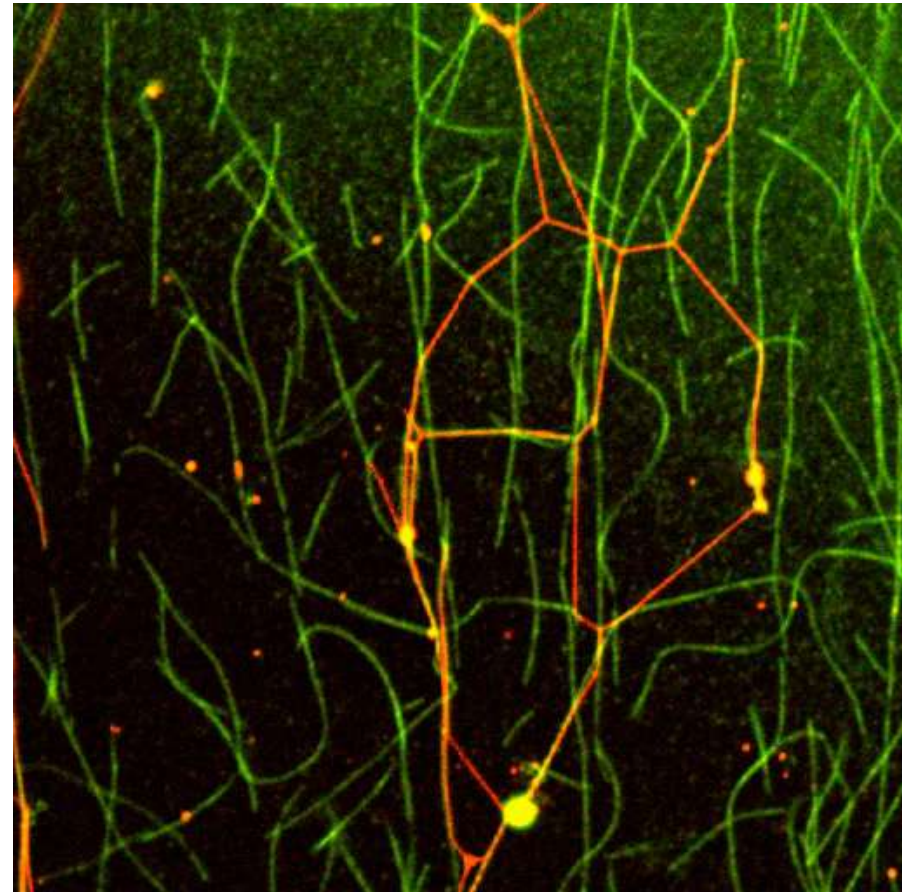
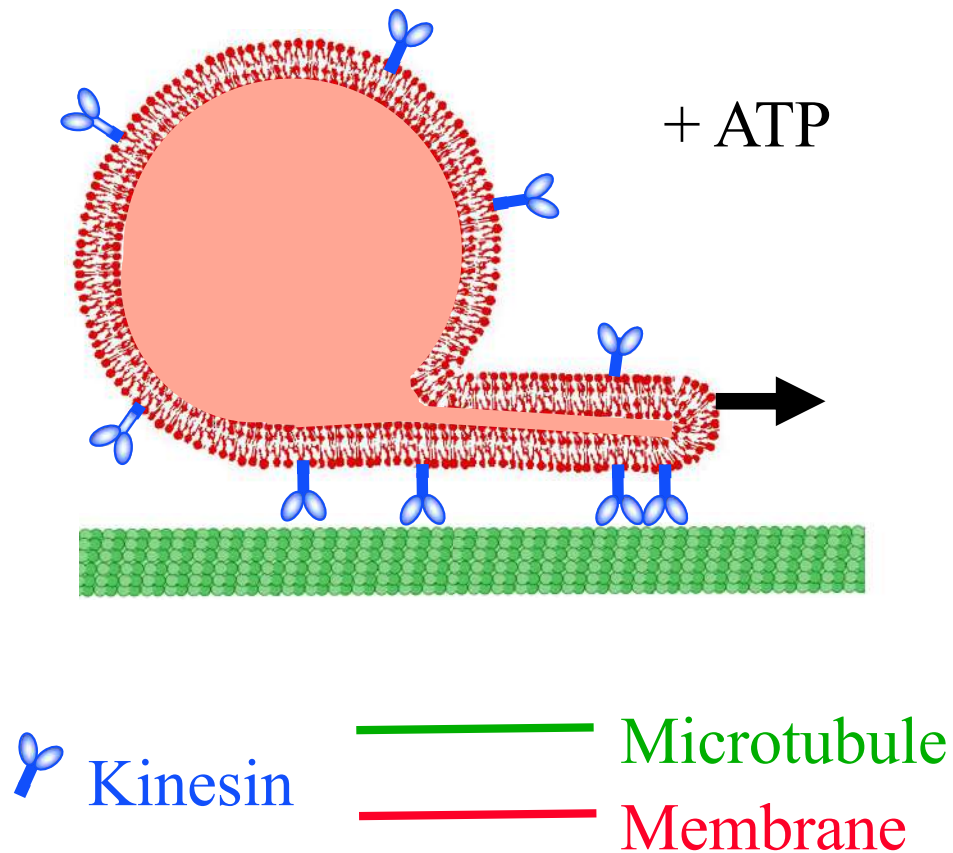
C. Leduc et al *PNAS* (2004)

X40 accelerated

A. Roux et al, *PNAS* (2002)

C. Leduc, O. Campàs et al, *PNAS* (2004)

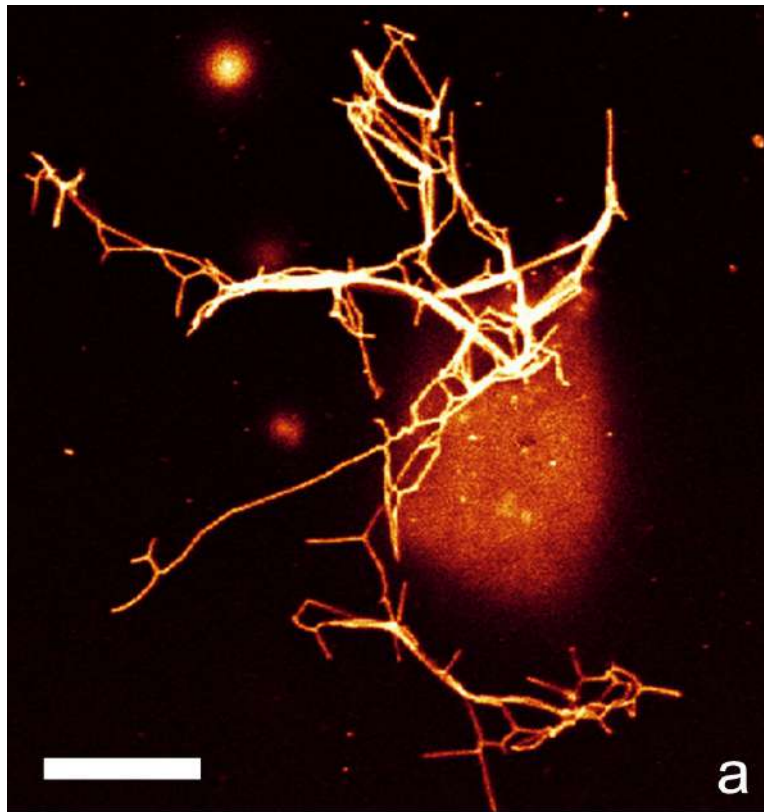
Minimal Biomimetic System



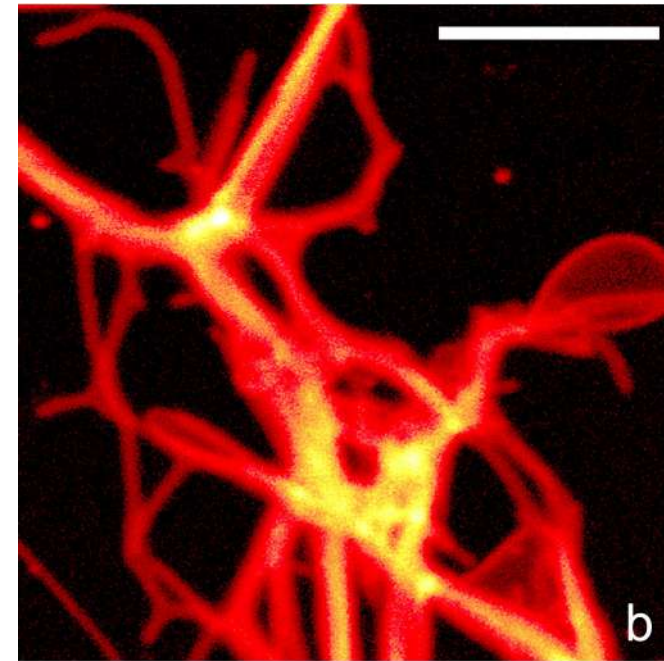
5 μm

A. Roux et al, *PNAS* (2002)

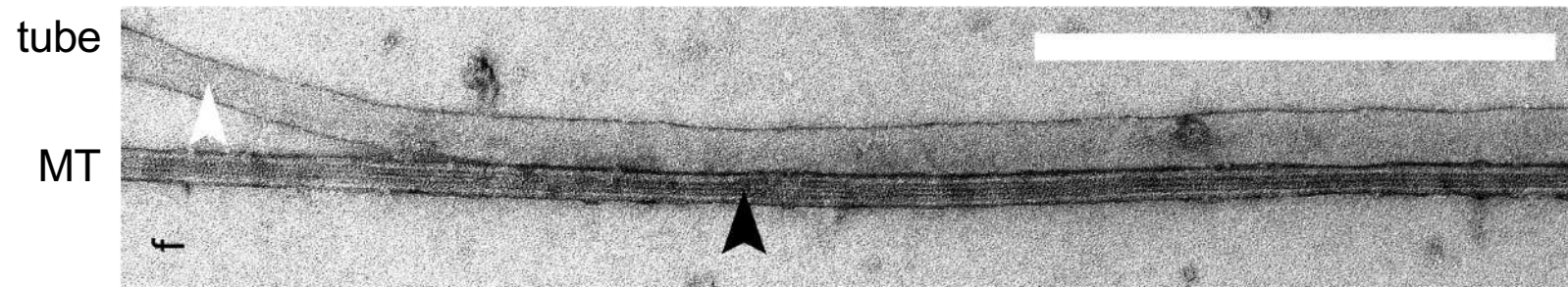
C. Leduc, O. Campàs et al, *PNAS* (2004)



5 μ m



5 μ m



500 nm

tube

MT

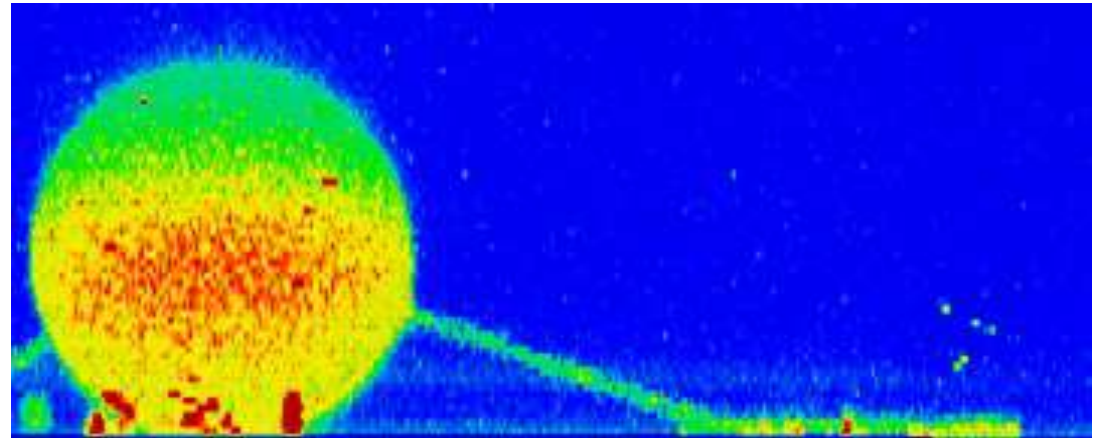
f

10 μm



Membrane labeling

Side view



$10 \text{ nm/s} < V < 300 \text{ nm/s}$

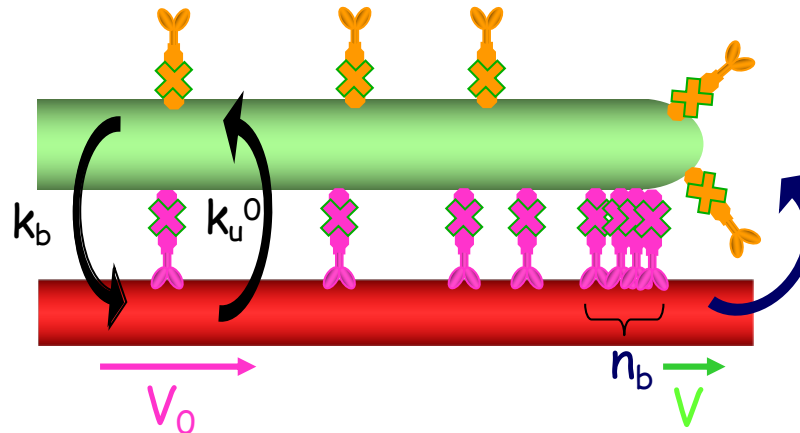
for $\sigma = 2.10^{-4} \text{ N/m}$

X40
accelerated

Mechanism for Tube Formation by Molecular Motors

- With our optical tweezers: $F=30$ pN for pulling these tubes
- Force max/1 motor = 6 pN

Motors have to work *COLLECTIVELY*
to pull these tubes



- Full theoretical model describing motor fluxes

(O. Campàs, JF Joanny, J. Prost)

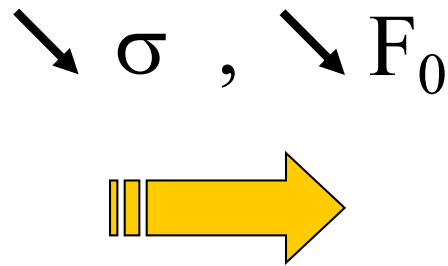
G. Koster M. Dogterom *PNAS* (2003)
C. Leduc, O. Campàs et al, *PNAS* (2004)

Conditions for Tube Extraction

- Fixed motor concentration ρ_{∞} :



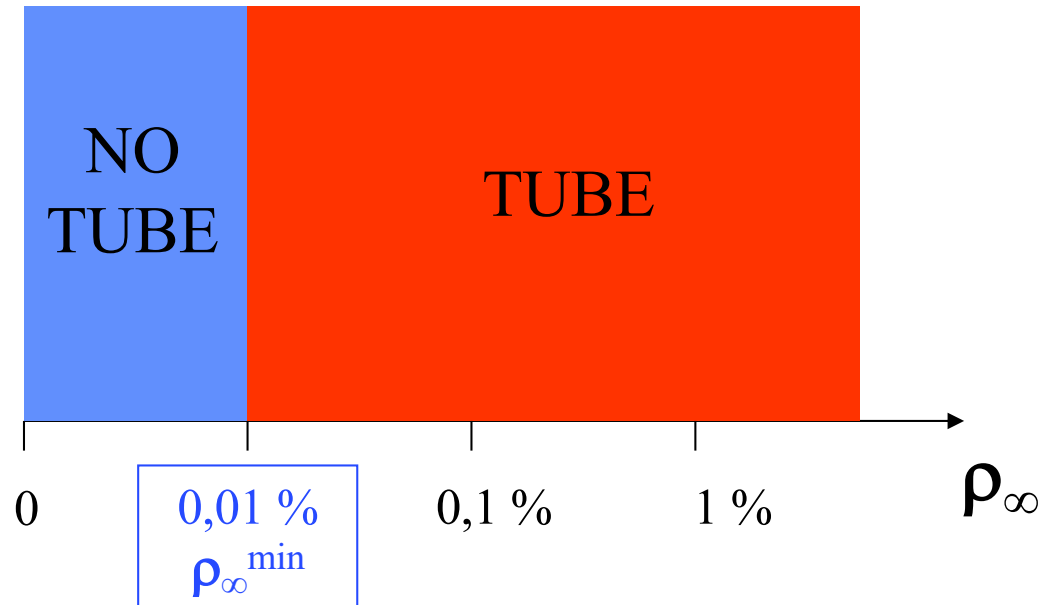
High tension



Lower tension

Tension Threshold for a given motor concentration

- Fixed membrane tension σ



Quantitative measurements

For $\sigma = 2 \cdot 10^{-4}$ N/m,

$$\rho_{\infty}^{\min} = 200 \text{ motors}/\mu\text{m}^2$$

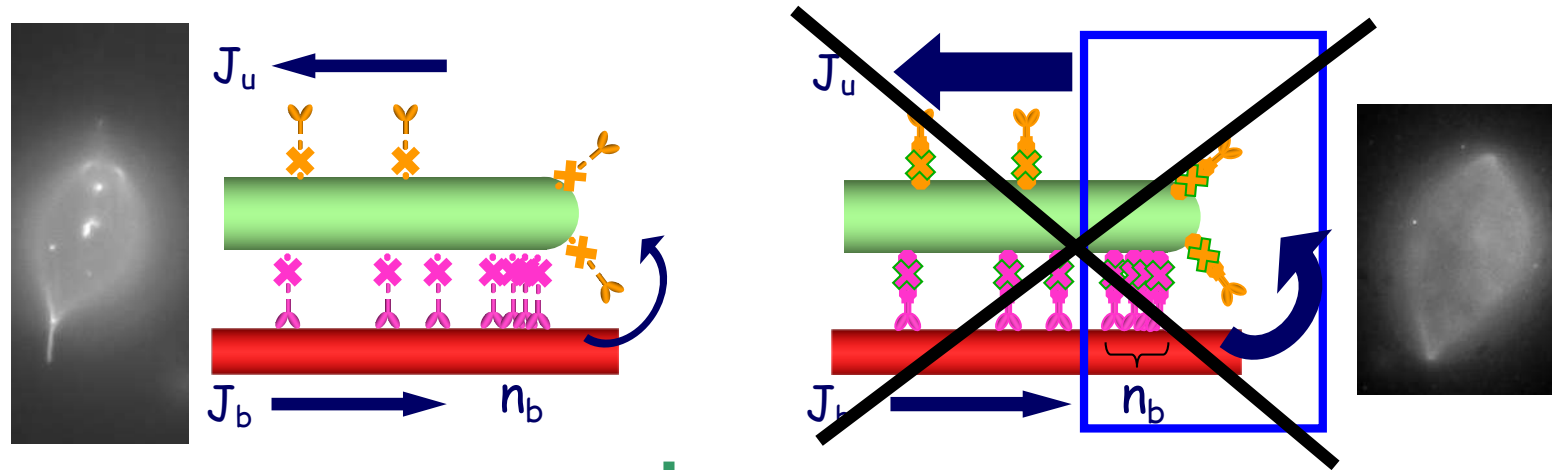
Threshold in motor concentration for a given tension

- Theoretical analysis effectively predicts:

$$\rho_{\infty}^{\min} = \text{cste} \cdot \sigma^{\max}$$

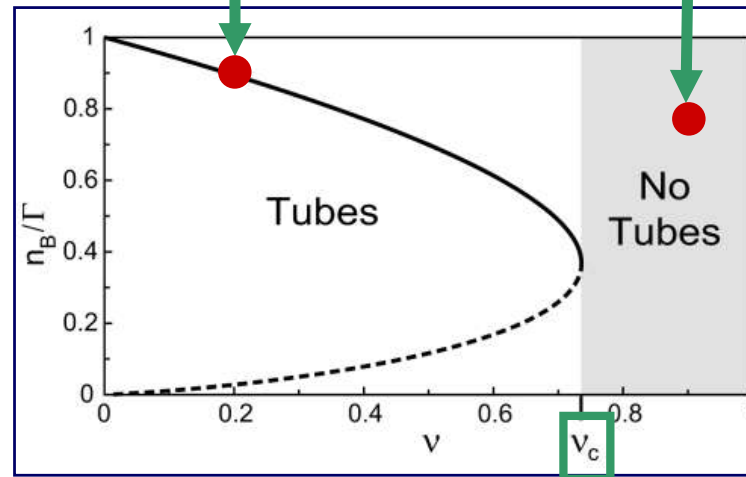
Theoretical Analysis

O. Campàs, J.-F. Joanny and J. Prost



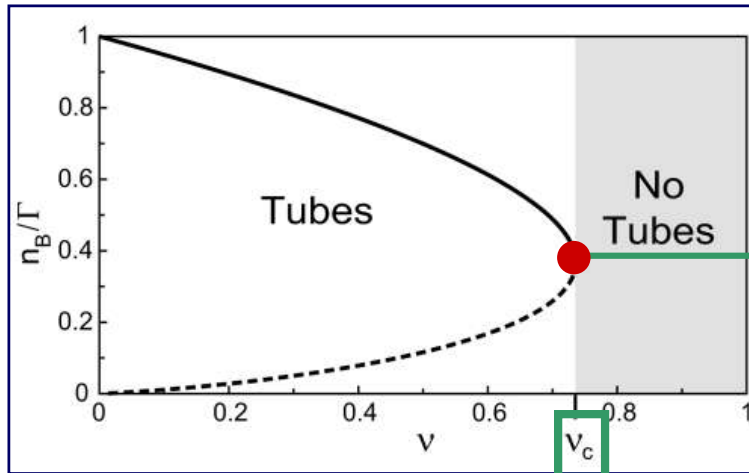
Analytical solutions

Bifurcation diagram



$$v \sim \sqrt{\frac{\sigma}{\rho_{\infty}}}$$

Condition for Tube Formation at the Threshold



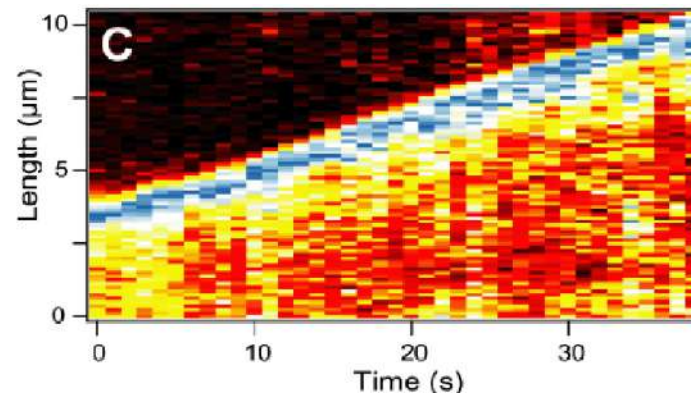
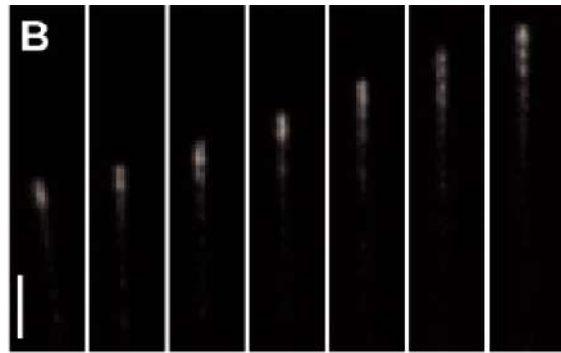
$$\rho_\infty > \frac{e^2}{2} f_s \left(\frac{a}{K_B T} \right)^2 \frac{k_b + k_u^0}{k_b} \frac{k_u^0}{V_0} \equiv \rho_\infty^{\min}$$

$$n_b^{\min} = \frac{f_0 a}{2 K_B T}$$

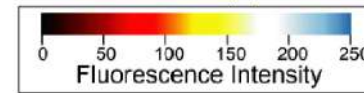
At the threshold:

$$\left\{ \begin{array}{ll} \rho_\infty^{\min, th} = 400 \pm 200 \text{ motors}/\mu\text{m}^2 & \text{Theory} \\ \rho_\infty^{\min, exp} = 200 \pm 100 \text{ motors}/\mu\text{m}^2 & \text{Experiments} \\ n_b^{\min} \sim 5 \text{ motors} & \end{array} \right.$$

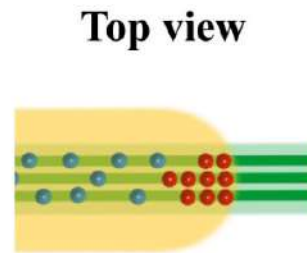
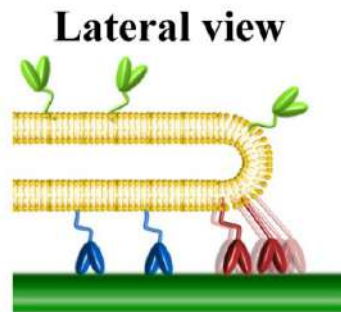
Motor Distribution along the Tubes



Motor accumulation at the tip



C. Leduc, O. Campàs et al, *PNAS* (2004)



Motor
labeling



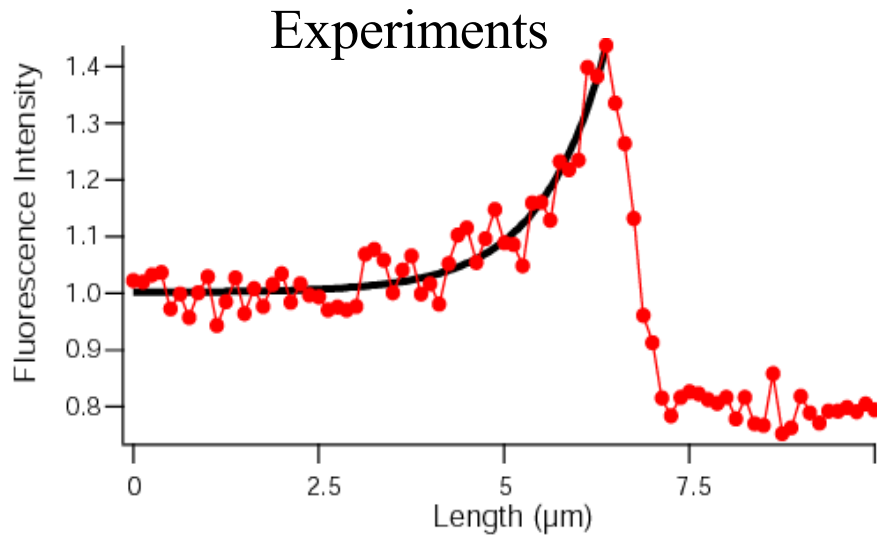
9 motors pull

O. Campàs, C. Leduc et al, *Biophys. J.* (2008)

Bar : 1 μ m

speed x 60

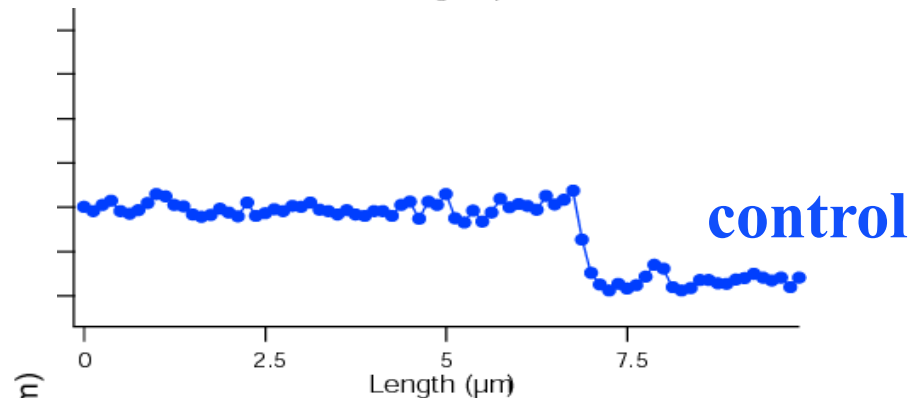
Experiments vs. Theory



Theory

Exponential distribution

$$\lambda = \frac{k_u^0 D}{2k_B(V_0 - V)} \left(1 + \sqrt{1 + \frac{4k_B}{k_u^0} \frac{(V_0 - V)^2}{k_u^0 D}} \right)$$



With

$$k_u^0 = 0.42 \text{ s}^{-1}$$

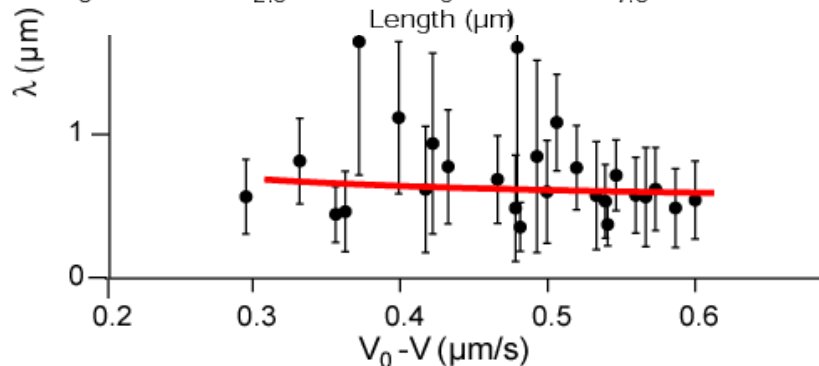
$$D = 1.0 \pm 0.5 \text{ } \mu\text{m}^2/\text{s}$$

(FRAP)

$$V_0 \approx 0.6 \pm 0.1 \text{ } \mu\text{m/s}$$

pulling the tube

One parameter fit: $k_b = 4.7 \pm 2.4 \text{ s}^{-1}$



Thanks!

