

Monopole dark matter ?

Michele Frigerio

Laboratoire Charles Coulomb, CNRS & Université de Montpellier

Laboratoire Physique Théorique Hautes Énergies, CNRS & Sorbonne Université, Paris

with **Felix BRUMMER, Giacomo FERRANTE, Théodore FISCHER**

*** No room for minimal monopole dark matter**, PRD 113 (2026) L091701 - 2509.21924

*** The price for monopole dark matter**, 260x.xxxxx

Horizons Beyond the Standard Model

ICTP-SAIFR, São Paulo, June 1-12, 2026

LUPM
Montpellier



SPhT
Bruxelles



LUPM
Montpellier



with **Felix BRUMMER, Giacomo FERRANTE, Théodore FISCHER**

*** No room for minimal monopole dark matter, PRD 113 (2026) L091701 - 2509.21924**

*** The price for monopole dark matter, 260x.xxxxx**

Outline

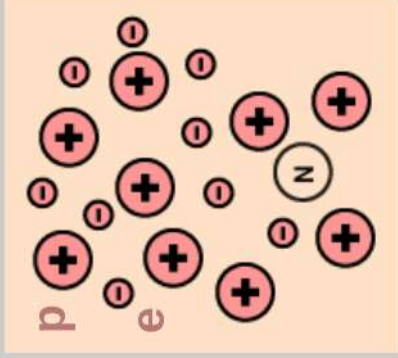
- * Reminder: why no observable magnetic monopoles
- * Dark-sector magnetic monopoles: can they be dark matter ?
- * Monopole relic abundance from phase transitions
- * Comparing abundances of electric & magnetic relics
- * Minimal model in details, possible extensions...

The sorrows of old Monopole



Why no magnetic monopoles?

Electric monopoles (charges) :



Magnetic monopoles : never observed

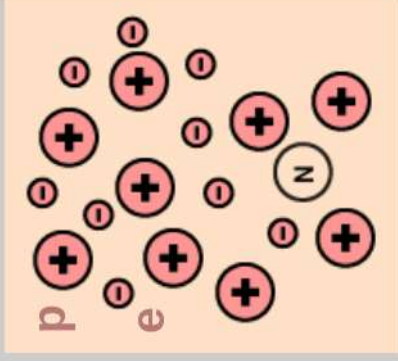
$$F_M = n_M v \lesssim 10^{-16} \text{ cm}^{-2} \text{ s}^{-1}$$

(variety of cosmo / astro / direct bounds)

e.g. Mavromatos, Mitsou, 2020

Why no magnetic monopoles?

Electric monopoles (charges) :



Magnetic monopoles : never observed

$$F_M = n_M v \lesssim 10^{-16} \text{ cm}^{-2} \text{ s}^{-1}$$

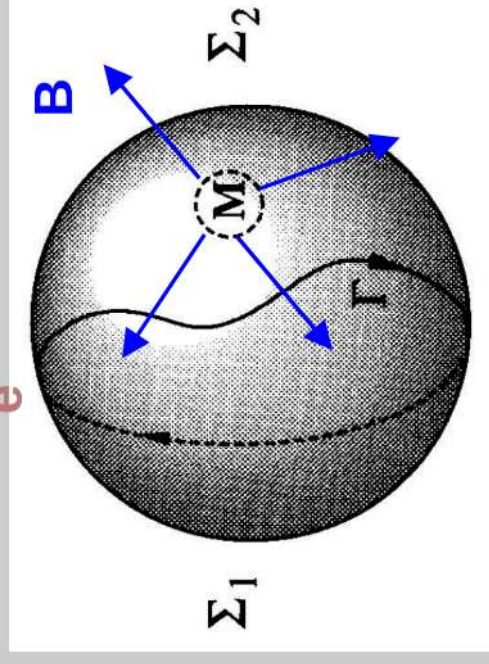
(variety of cosmo / astro / direct bounds)

e.g. Mavromatos, Mitsou, 2020

However, electric charges ARE quantised.

Dirac (1931): if a magnetic monopole exists, then charges MUST BE quantised.

$$q_E q_M = 2\pi n$$



Vilenkin
Shellard
1994

Why no magnetic monopoles?

Magnetic monopoles DO exist

IF electromagnetism descends

from **simple non-abelian symmetry**

Vacuum manifold

(minima of scalar-field potential)

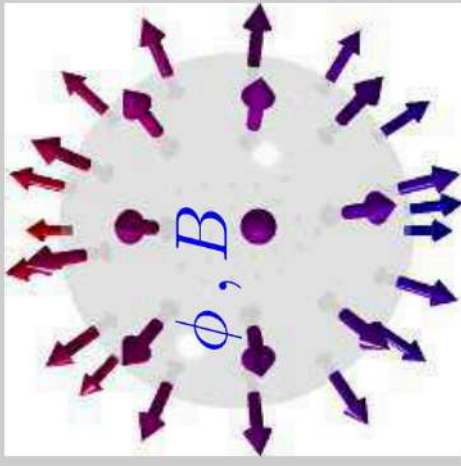
Maps from **dim-2 closed surfaces**
into vacuum manifold

$$SO(3) \xrightarrow{\langle \phi_3 \rangle} U(1)_{em} \simeq SO(2)$$

't Hooft 1974
Polyakov 1974

$$\frac{G}{H} = \frac{SO(3)}{SO(2)} \simeq S^2$$

$$\pi_2(S^2) = \mathbb{Z}$$



Why no magnetic monopoles?

Magnetic monopoles DO exist

IF electromagnetism descends

from **simple non-abelian symmetry**

Vacuum manifold

(minima of scalar-field potential)

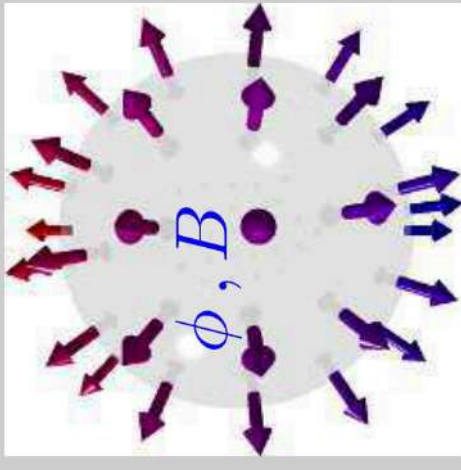
Maps from **dim-2 closed surfaces**
into vacuum manifold

$$SO(3) \xrightarrow{\langle \phi_3 \rangle} U(1)_{em} \simeq SO(2)$$

't Hooft 1974
Polyakov 1974

$$\frac{G}{H} = \frac{SO(3)}{SO(2)} \simeq S^2$$

$$\pi_2(S^2) = \mathbb{Z}$$



But, in **Standard Model** ...

... **no monopoles** !

$$SU(2)_w \times U(1)_Y \xrightarrow{\langle \phi_2 \rangle} U(1)_{em}$$

$$SO(4) \xrightarrow{\langle \phi_2 \rangle} SO(3)_{custodial}$$

$$\pi_2(S^3) = 1$$

Why no magnetic monopoles?

Still, charge quantisation can be realised by **Grand Unification** ...

$$SU(5) \xrightarrow{\langle \phi_{24} \rangle} SU(3)_c \times SU(2)_w \times U(1)_Y$$

... far too many monopoles !

$$F_M = n_M v \sim 10^{-2} cm^{-2} s^{-1}$$

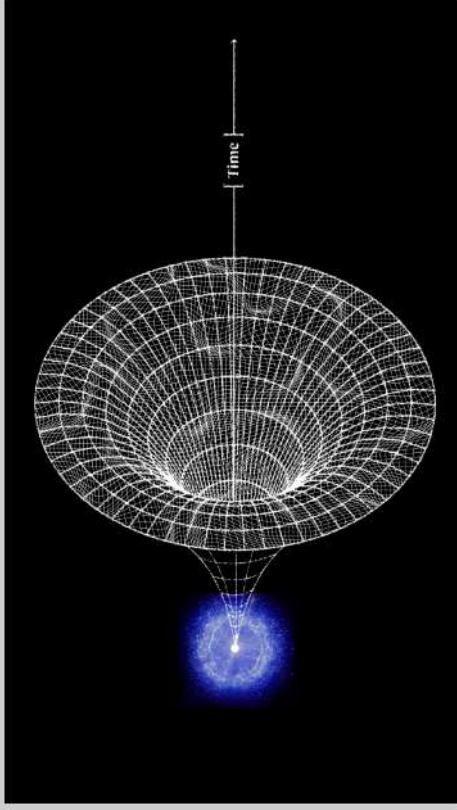
Why no magnetic monopoles?

Still, charge quantisation can be realised by **Grand Unification** ...

$$SU(5) \xrightarrow{\langle \phi_{24} \rangle} SU(3)_c \times SU(2)_w \times U(1)_Y$$

... far too many monopoles !

$$F_M = n_M v \sim 10^{-2} \text{cm}^{-2} \text{s}^{-1}$$



Inflation exponentially dilutes

relic abundances,

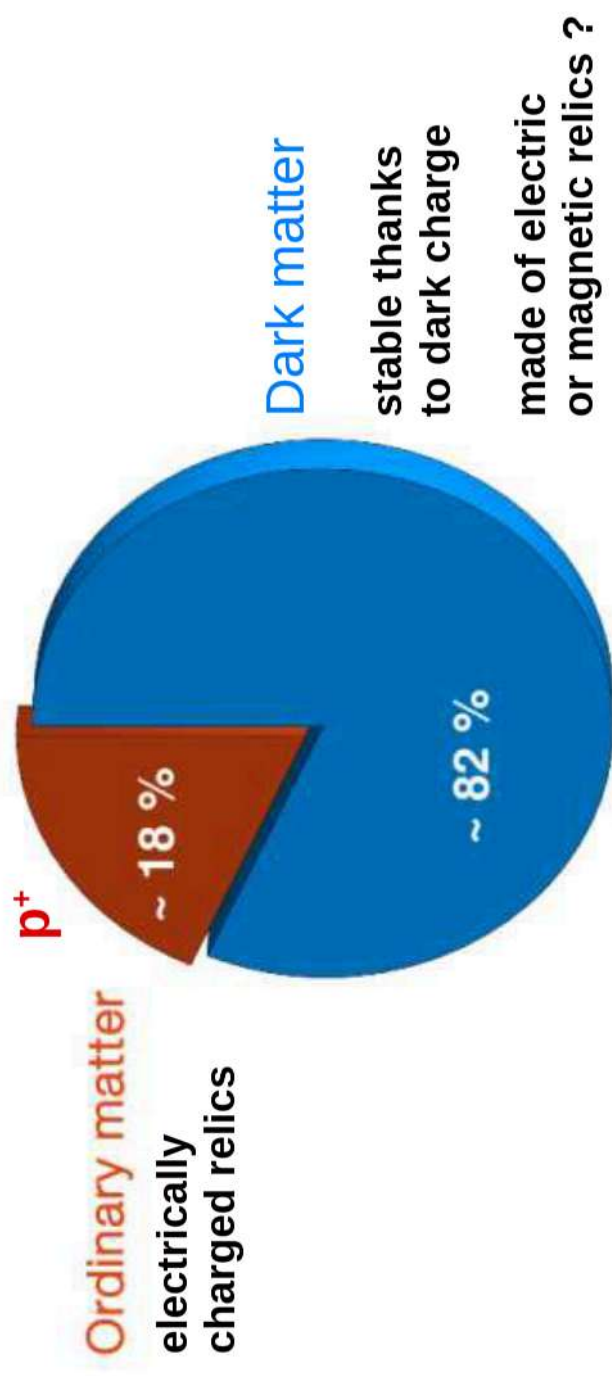
solving monopole problem

as long as

$$T_{inf} < T_{GUT}$$

“Monopoles are a sharp prediction of Grand Unification, but possibly *the only monopole in the Universe passed by the Earth* just before we built the detector” **G. Senjanovic**

Monopoles in the dark sector ?



Dark monopoles as dark matter ?

Dark gauge symmetry. Motivations:

- analogy with visible sector
- lightest charged particles are absolutely stable
- calculable relic abundances

Dark monopoles as dark matter ?

Dark gauge symmetry. Motivations:

- analogy with visible sector
- lightest charged particles are absolutely stable
- calculable relic abundances

Dark electrically-charged particles widely studied.

Only few interesting papers on **dark magnetic monopoles**.

idea by

Murayama, Shu 2009,

building on

Kibble 1976,

Zurek 1985,

explicit models by

Baek, Ko, Park 2013

Khoze, Ro 2014

...

Dark monopoles as dark matter ?

Dark gauge symmetry. Motivations:

- analogy with visible sector
- lightest charged particles are absolutely stable
- calculable relic abundances

Dark electrically-charged particles widely studied.

Only few interesting papers on **dark magnetic monopoles**.

idea by
Murayama, Shu 2009,

building on
Kibble 1976,
Zurek 1985,

explicit models by
Baek, Ko, Park 2013
Khoze, Ro 2014
...

Limitations of available analyses:

- *second-order phase transition only*
- *electric counterpart: initially ignored, later studied in restricted range of parameters*
- *monopole abundance overestimated in some cases*

Minimal dark sector

't Hooft 1974
Polyakov 1974

SO(3) spontaneous breaking to SO(2)

$$0 < g \ll 4\pi$$

dark SO(3) gauge coupling

$$m_W = g\eta \ll m_M \simeq \frac{4\pi}{g}\eta$$

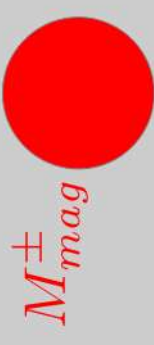
scalar self-coupling

$$V(\phi) = \frac{\lambda}{4}(\phi^a \phi^a - \eta^2)^2$$

symmetry breaking scale

$$r_M \simeq \frac{1}{m_W} \gg \frac{1}{m_M}$$

Monopole is large, classical
field configuration



[CP conservation assumed for simplicity : no θ term, no dyons]

Minimal dark sector

't Hooft 1974
Polyakov 1974

SO(3) spontaneous breaking to SO(2)

$$0 < g \ll 4\pi$$

dark SO(3) gauge coupling

$$m_W = g\eta \ll m_M \simeq \frac{4\pi}{g}\eta$$

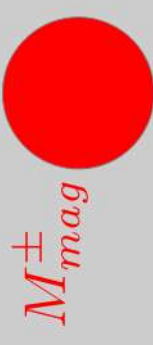
scalar self-coupling

$$V(\phi) = \frac{\lambda}{4}(\phi^a \phi^a - \eta^2)^2$$

symmetry breaking scale

$$r_M \simeq \frac{1}{m_W} \gg \frac{1}{m_M}$$

Monopole is large, classical
field configuration



$M_{mag}^{\pm}$



$W_{ele}^{\pm}$

[CP conservation assumed for simplicity : no θ term, no dyons]

Portal between **dark sector** & **visible sector**

$$V_{portal} = \frac{\lambda_{\phi H}}{2} \phi^a \phi^a H^\dagger H$$

(i) thermalisation at phase-transition time

$$\left(\frac{T_c}{10^{14} \text{GeV}} \right)^{1/2} \lesssim \lambda_{\phi H} \ll \lambda, g^2$$

(ii) small perturbation to dark thermal potential

Monopoles from phase transition

Kibble mechanism to form topological defects:

symmetry restoration at large T

$$\langle \phi_a \rangle = 0$$

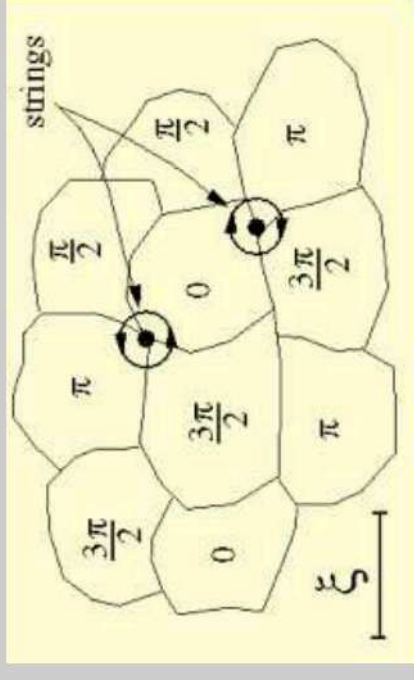
phase transition below T_c

$$\langle \phi_a(\mathbf{x}) \rangle = \eta \hat{\mathbf{n}}(\mathbf{x})$$

scalar-field correlation length is finite

Kibble 1976

$$n_M \simeq \frac{1}{8\xi^3}$$



just imagine one additional dimension, to form monopoles

Monopoles from phase transition

Kibble mechanism to form topological defects:

symmetry restoration at large T

$$\langle \phi_a \rangle = 0$$

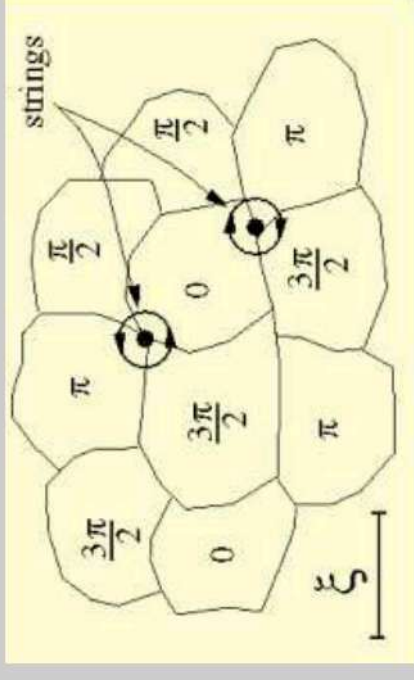
phase transition below T_c

$$\langle \phi_a(\mathbf{x}) \rangle = \eta \hat{\mathbf{n}}(\mathbf{x})$$

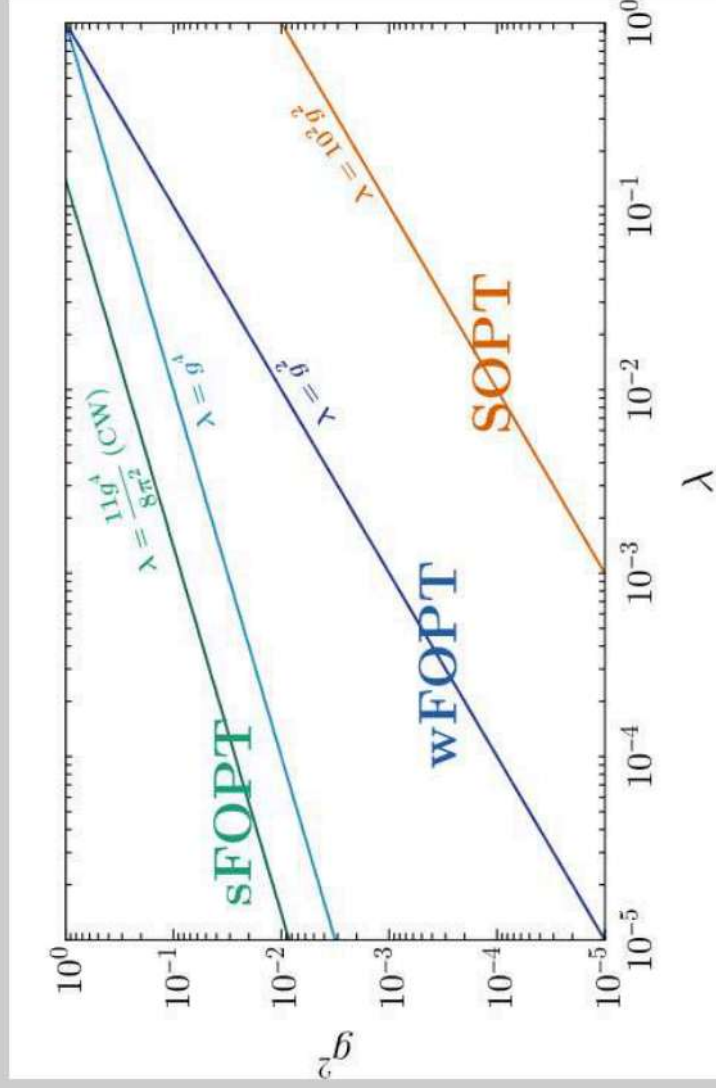
scalar-field correlation length is finite

$$n_M \simeq \frac{1}{8\xi^3}$$

Kibble 1976



just imagine one additional dimension, to form monopoles

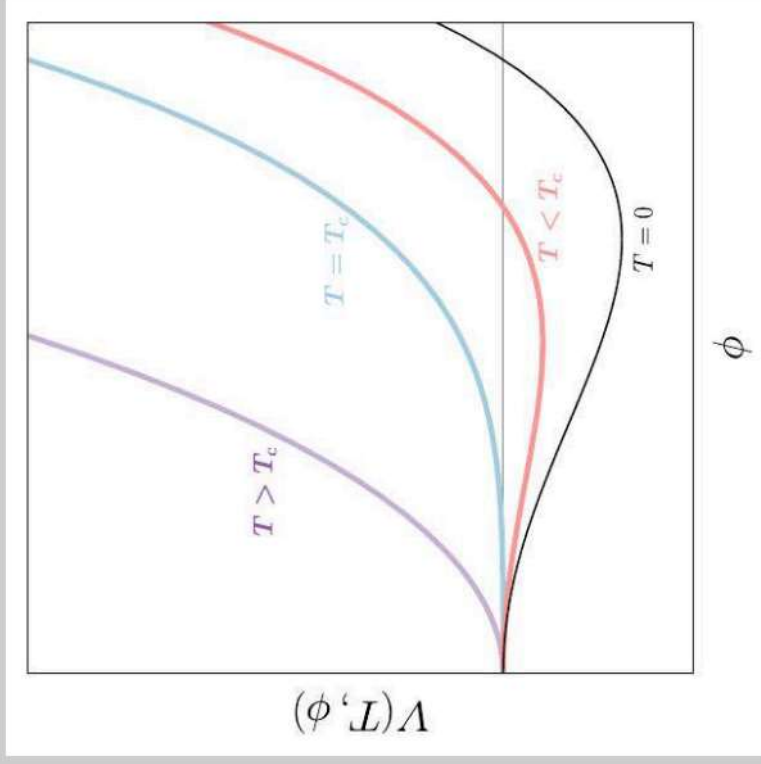


Correlation length ξ strongly depends on **Order of Phase Transition**:
Second, weakly First, strongly First

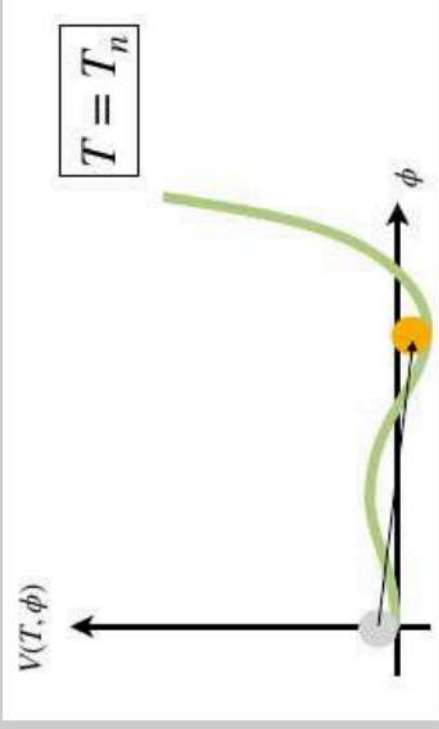
Order depends on
shape of scalar thermal potential,
determined by couplings

Scalar thermal potential

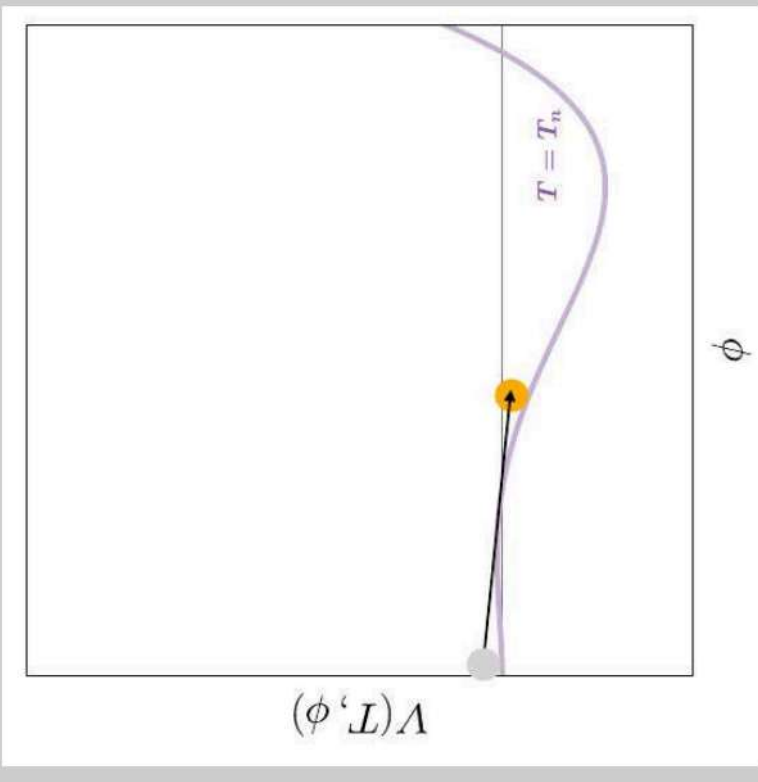
SOPT

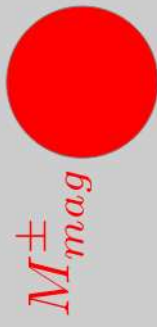


wFOPT



sFOPT

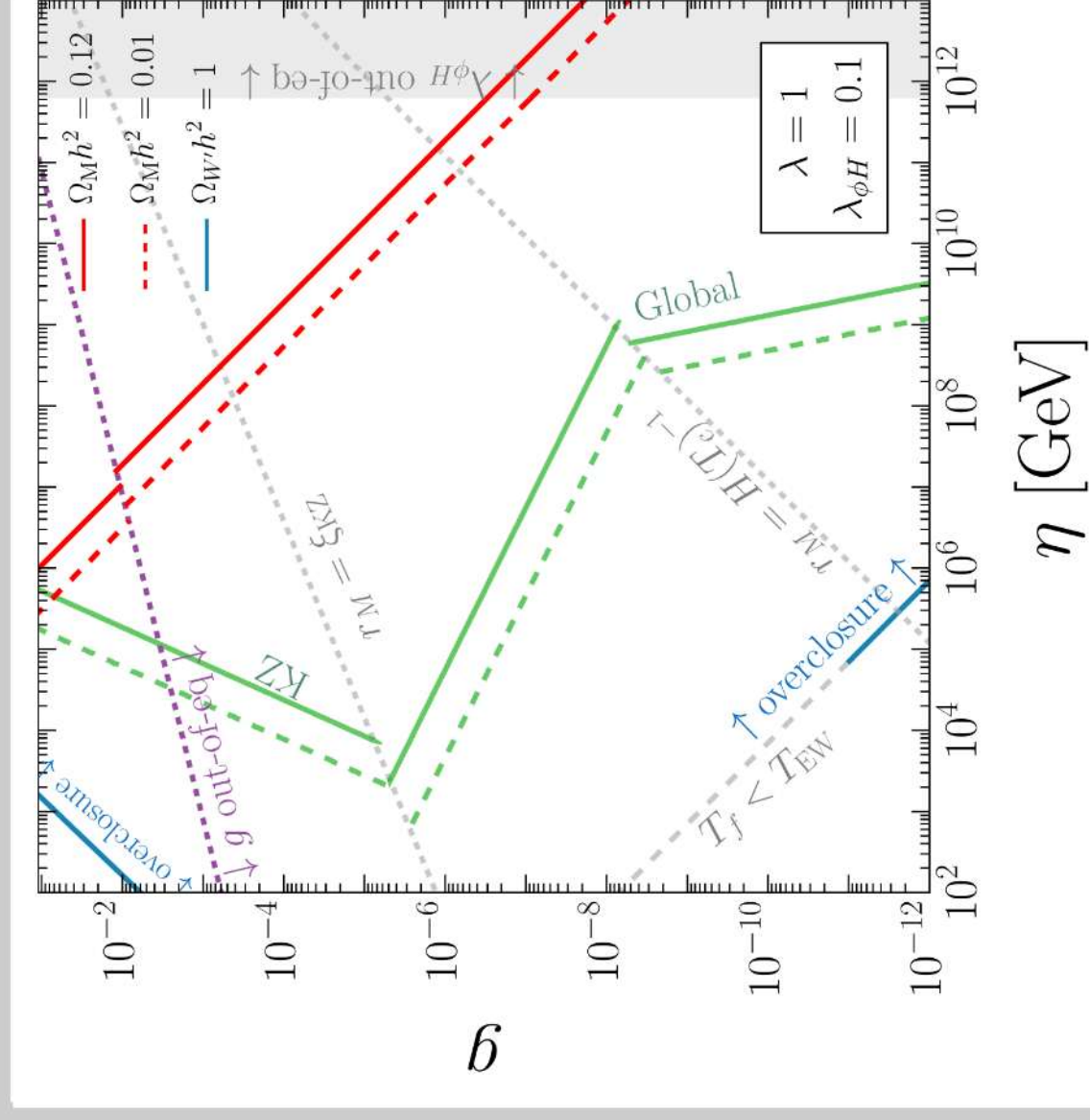


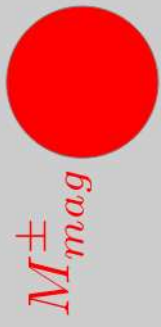


$M_{mag}^{\pm}$

$W_{ele}^{\pm}$

Second order





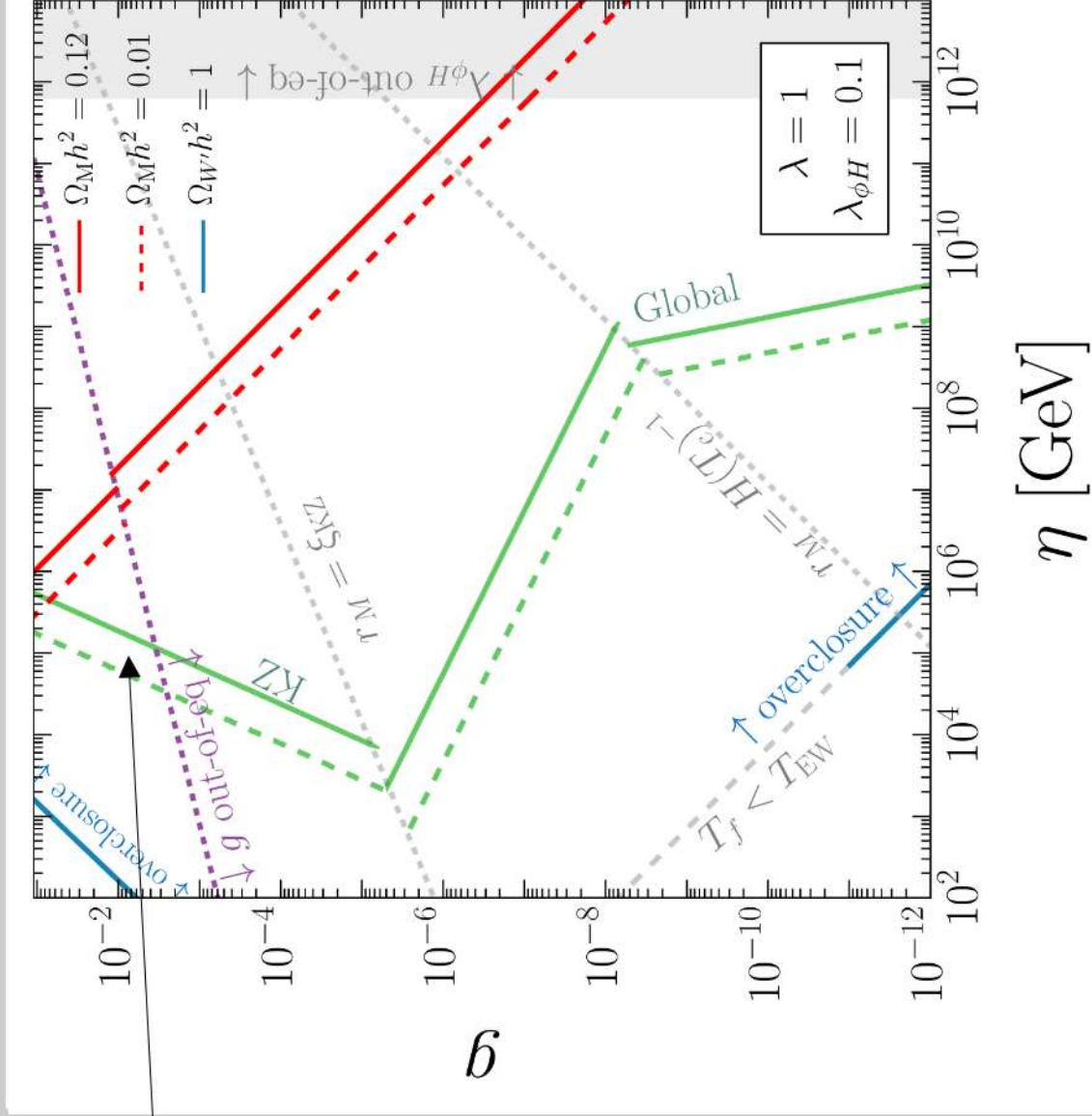
$W_{ele}^{\pm}$

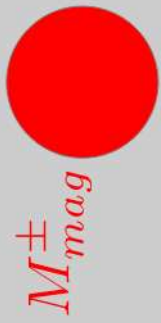
Second order

In principle **correlation length** diverges at T_c
but **time to relax** is **finite** due to expansion

$$\xi_{KZ} \simeq \frac{1}{H(T_c)} \left[\frac{H(T_c)^2}{2\lambda\eta^2} \right]^{0.29}$$

Kibble 1976
Zurek 1985





$M_{mag}^{\pm}$

$W_{ele}^{\pm}$

Second order

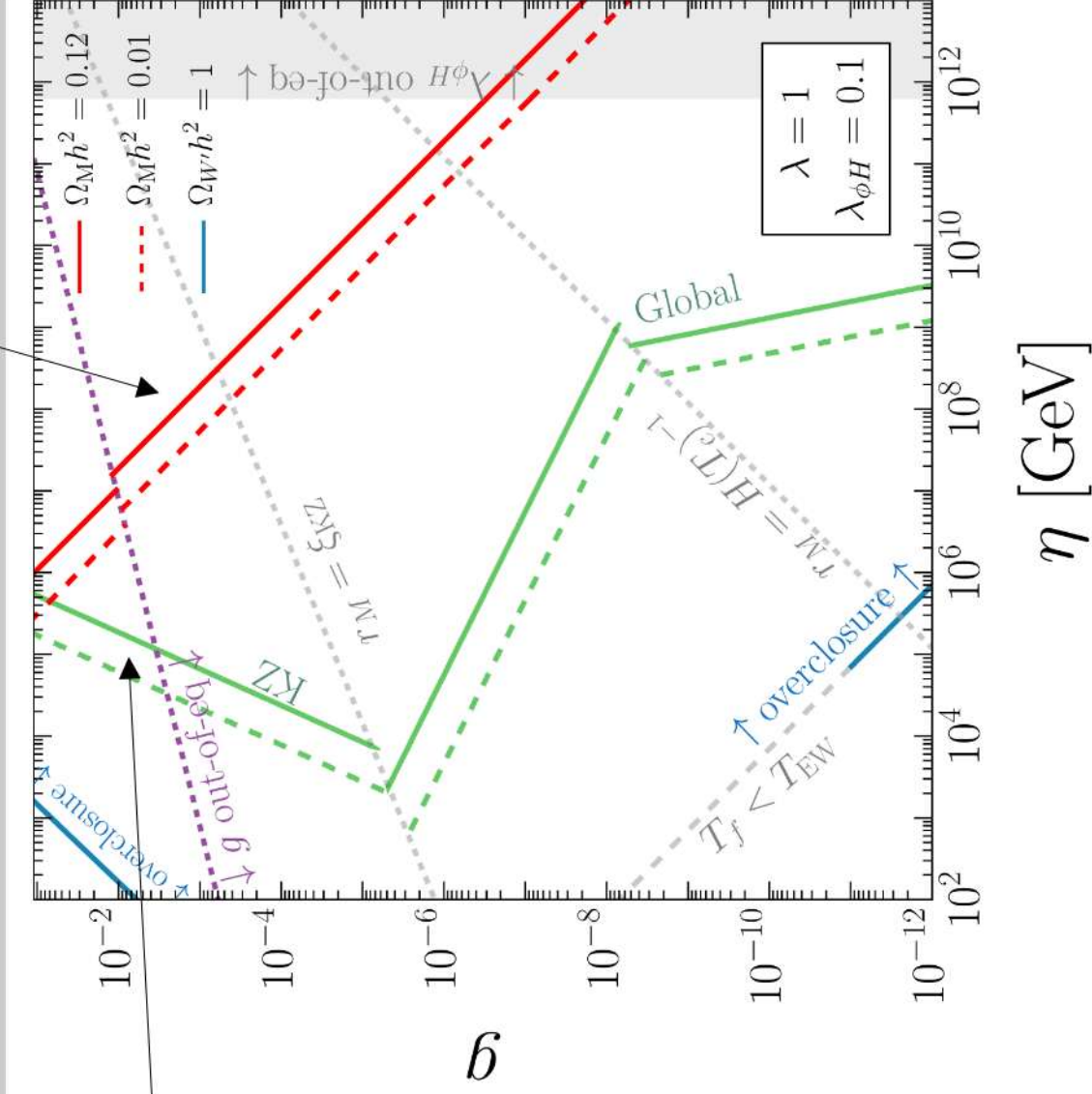
W thermal bath
dissipates energy of
monopoles **which**
thus can annihilate

In principle **correlation length** diverges at T_c
but **time to relax is finite** due to expansion

Preskill 1979

$$\xi_{KZ} \simeq \frac{1}{H(T_c)} \left[\frac{H(T_c)^2}{2\lambda\eta^2} \right]^{0.29}$$

Kibble 1976
Zurek 1985





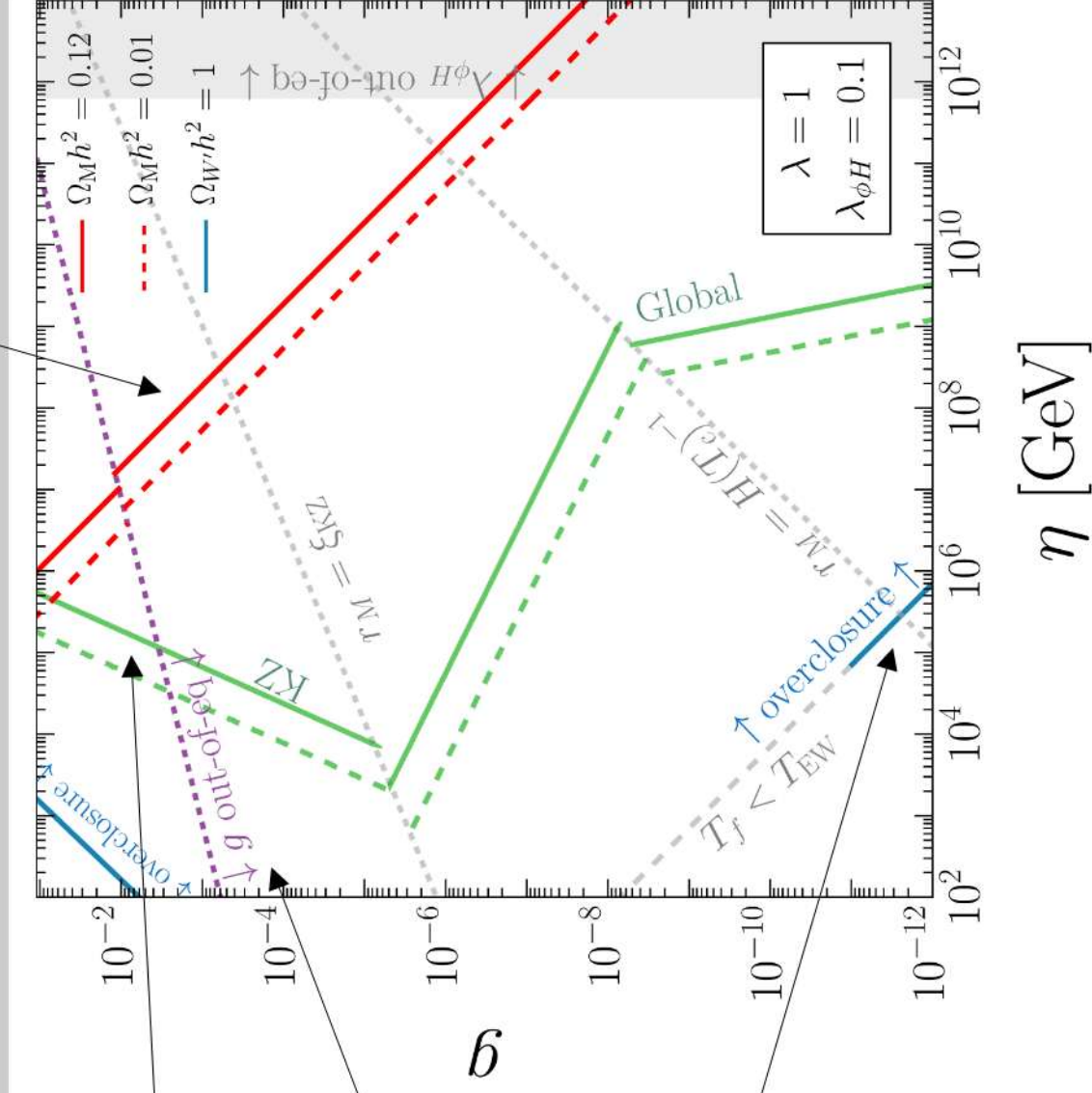
Second order

Preskill 1979

$$\xi_{KZ} \simeq \frac{1}{H(T_c)} \left[\frac{H(T_c)^2}{2\lambda\eta^2} \right]^{0.29} -$$

For small g transverse W 's are sub-thermal

Therefore, freeze-out determines W abundance



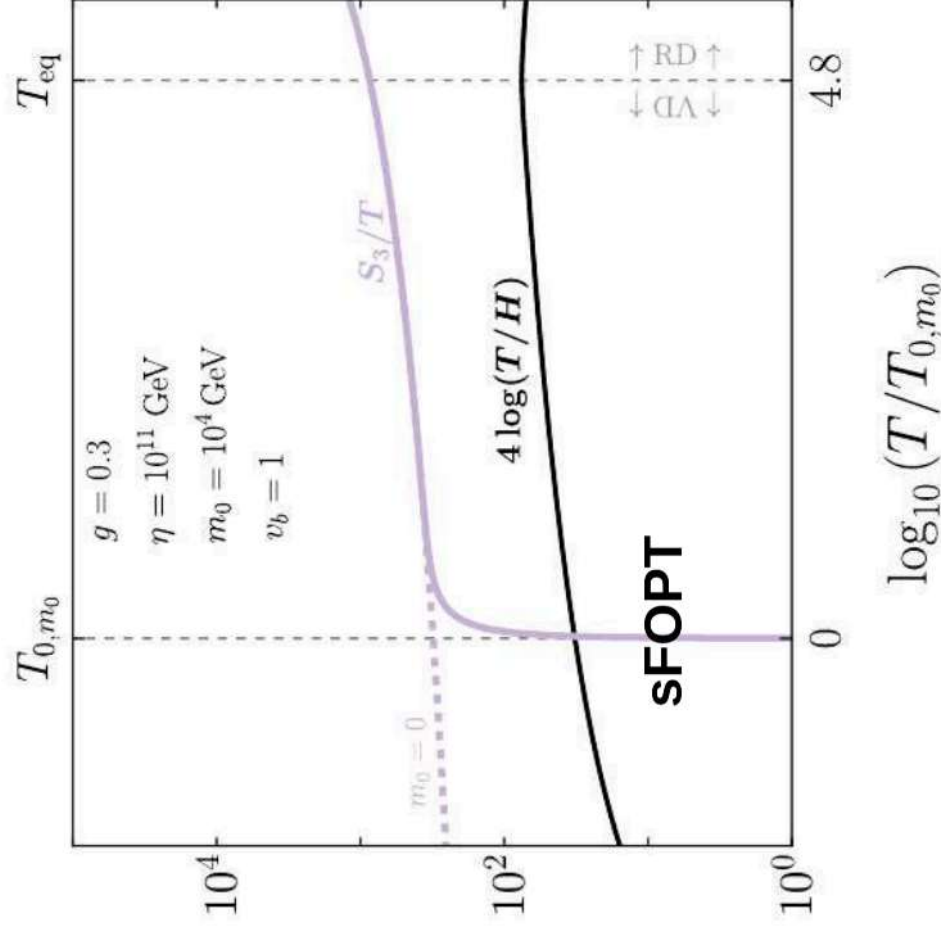
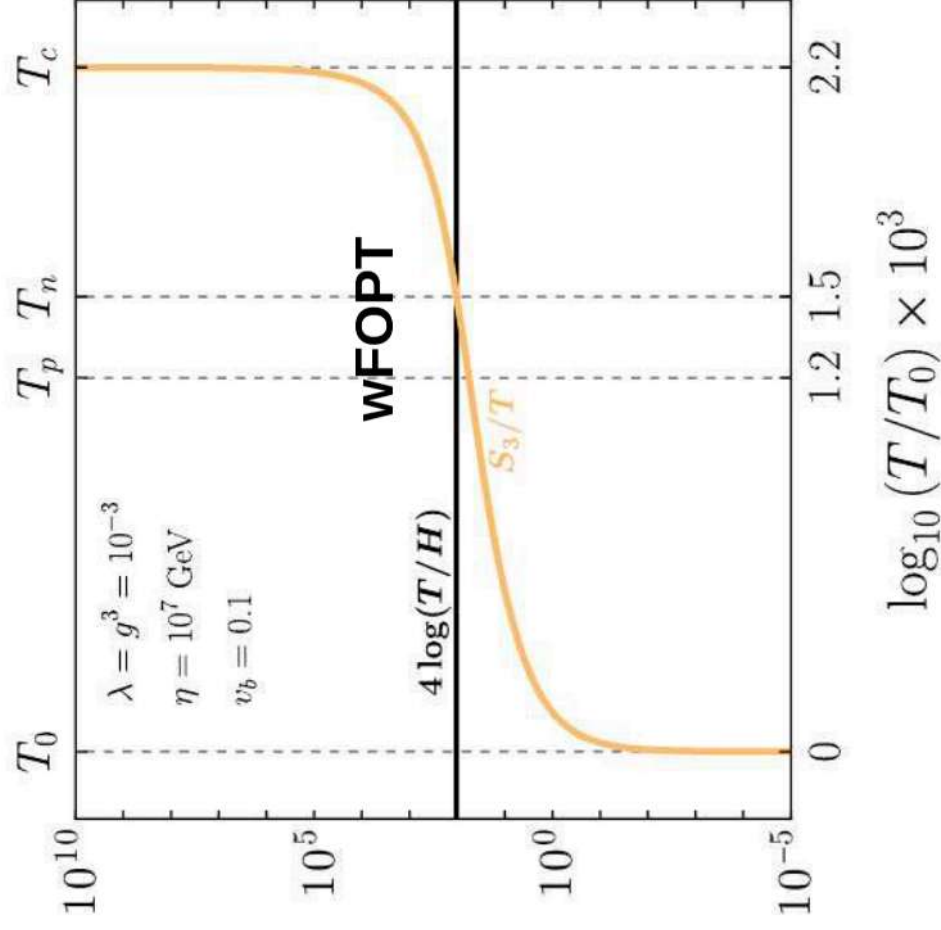
Nucleation rate vs Hubble expansion

Bounce action S_3 controls nucleation rate

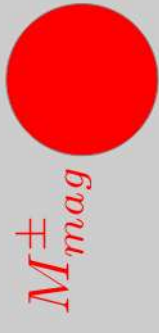
$$\Gamma(T) \simeq T^4 e^{-S_3/T}$$

Nucleation temperature defined by

$$\Gamma(T_n) = H(T_n)^4$$



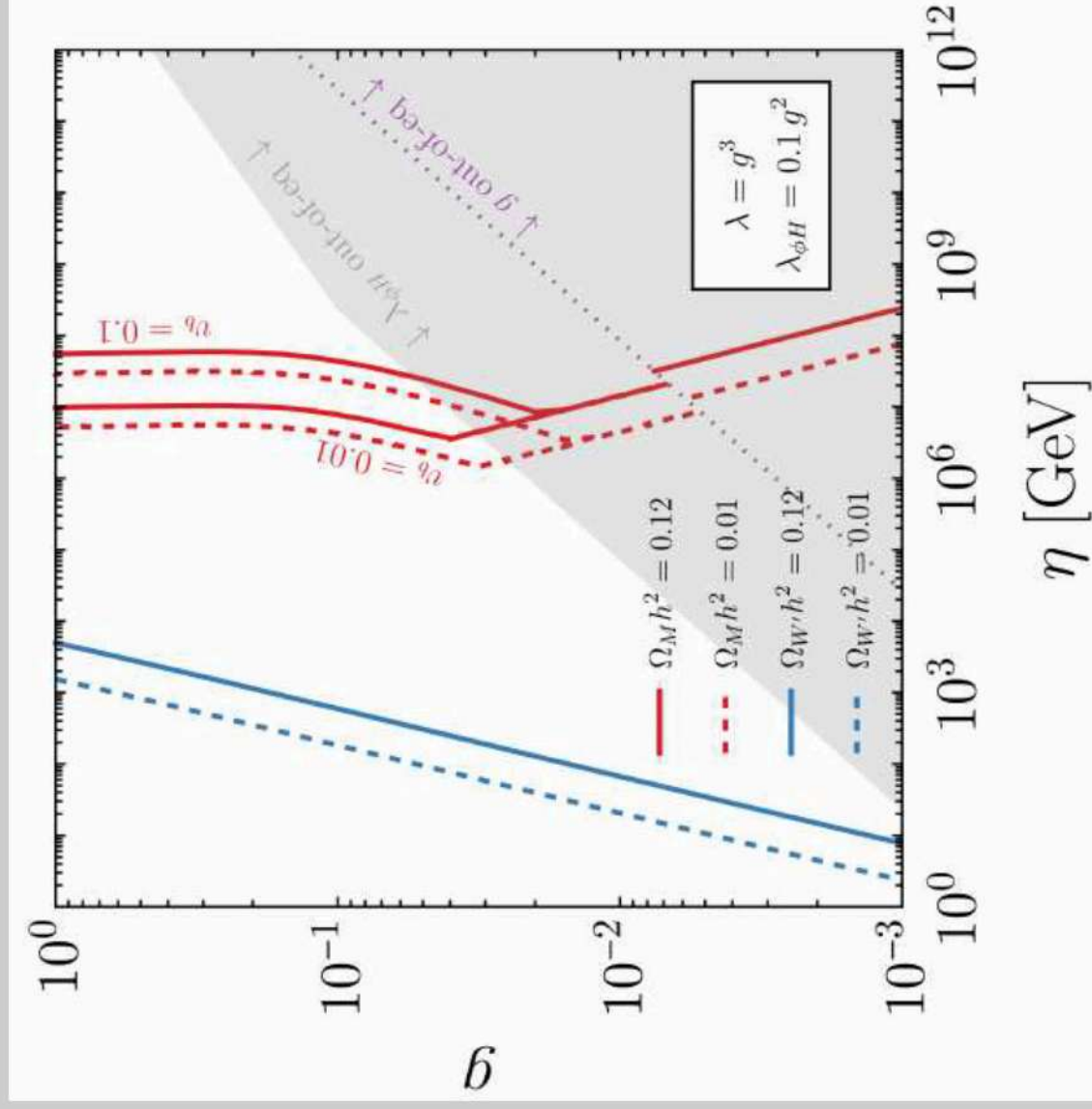
Weakly first order



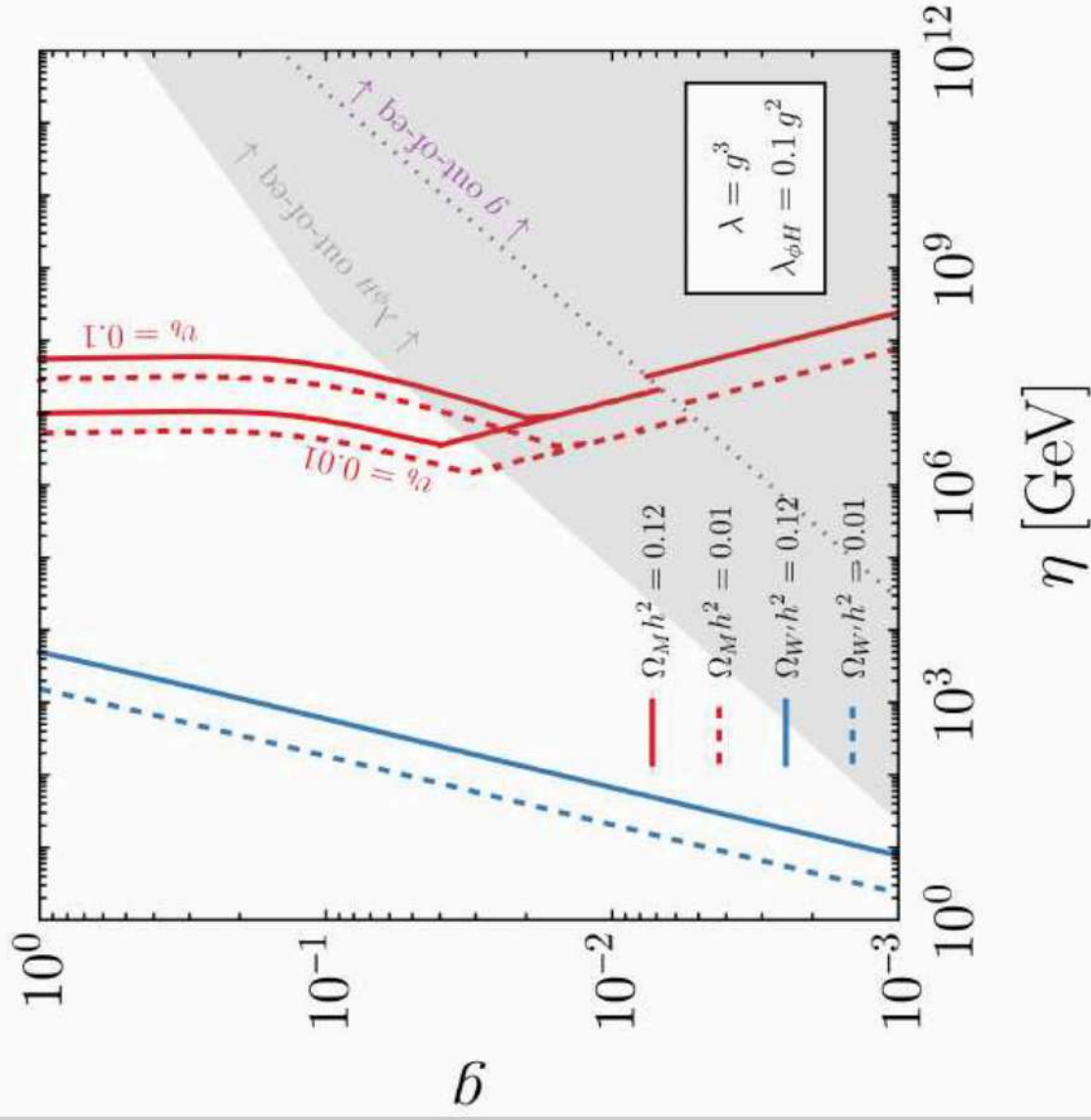
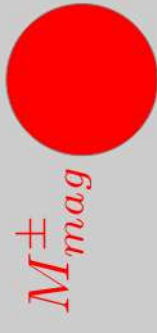
$M_{mag}^{\pm}$



$W_{ele}^{\pm}$



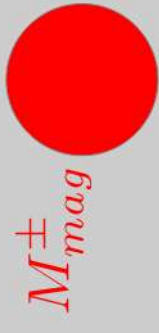
Weakly first order



Potential barrier present at T_c

Thermal fluctuations allow **nucleation**
of bubbles of true vacuum

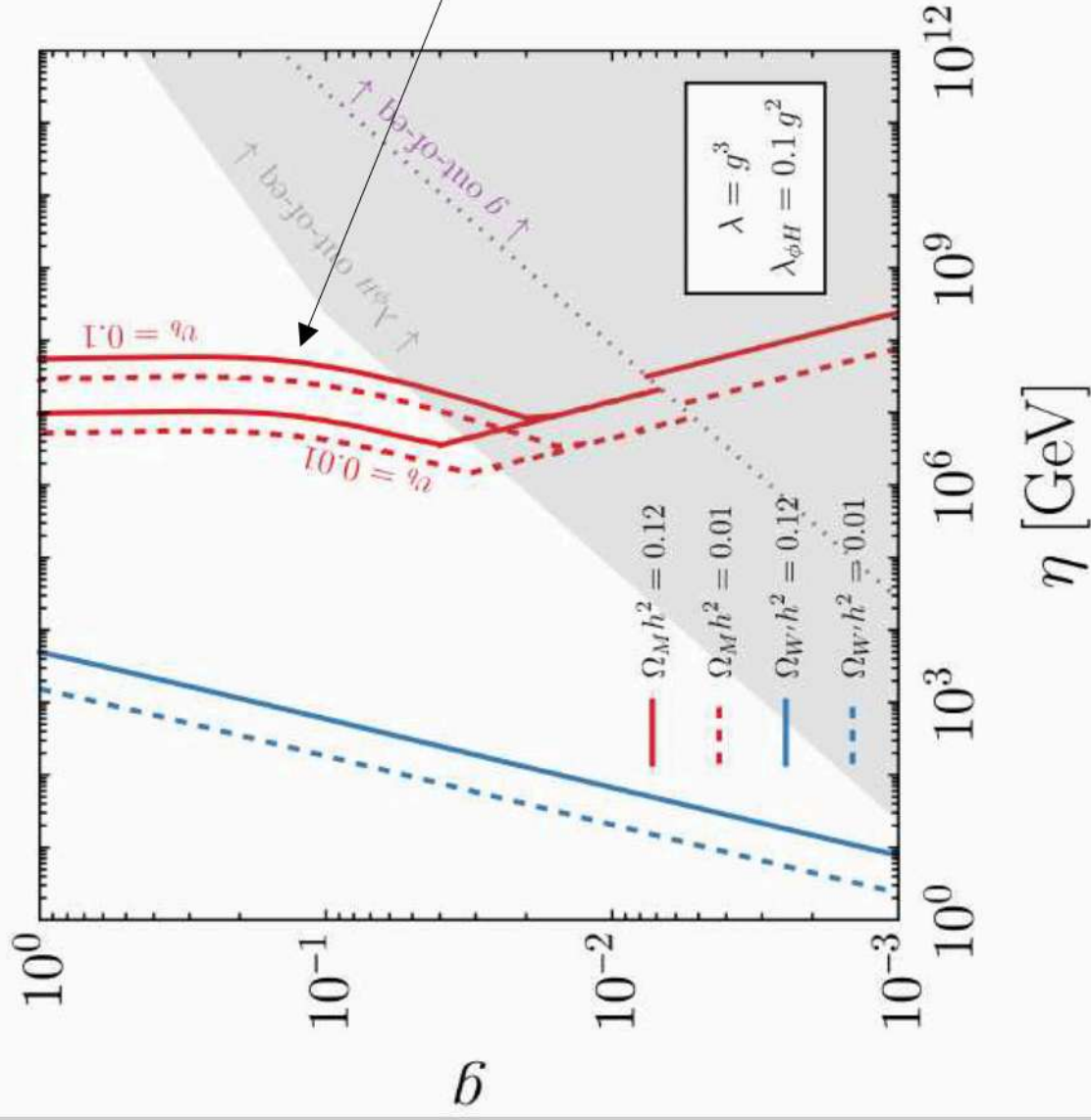
Weakly first order



$M_{mag}^{\pm}$



$W_{ele}^{\pm}$



Potential barrier present at T_c

Thermal fluctuations allow **nucleation** of bubbles of true vacuum

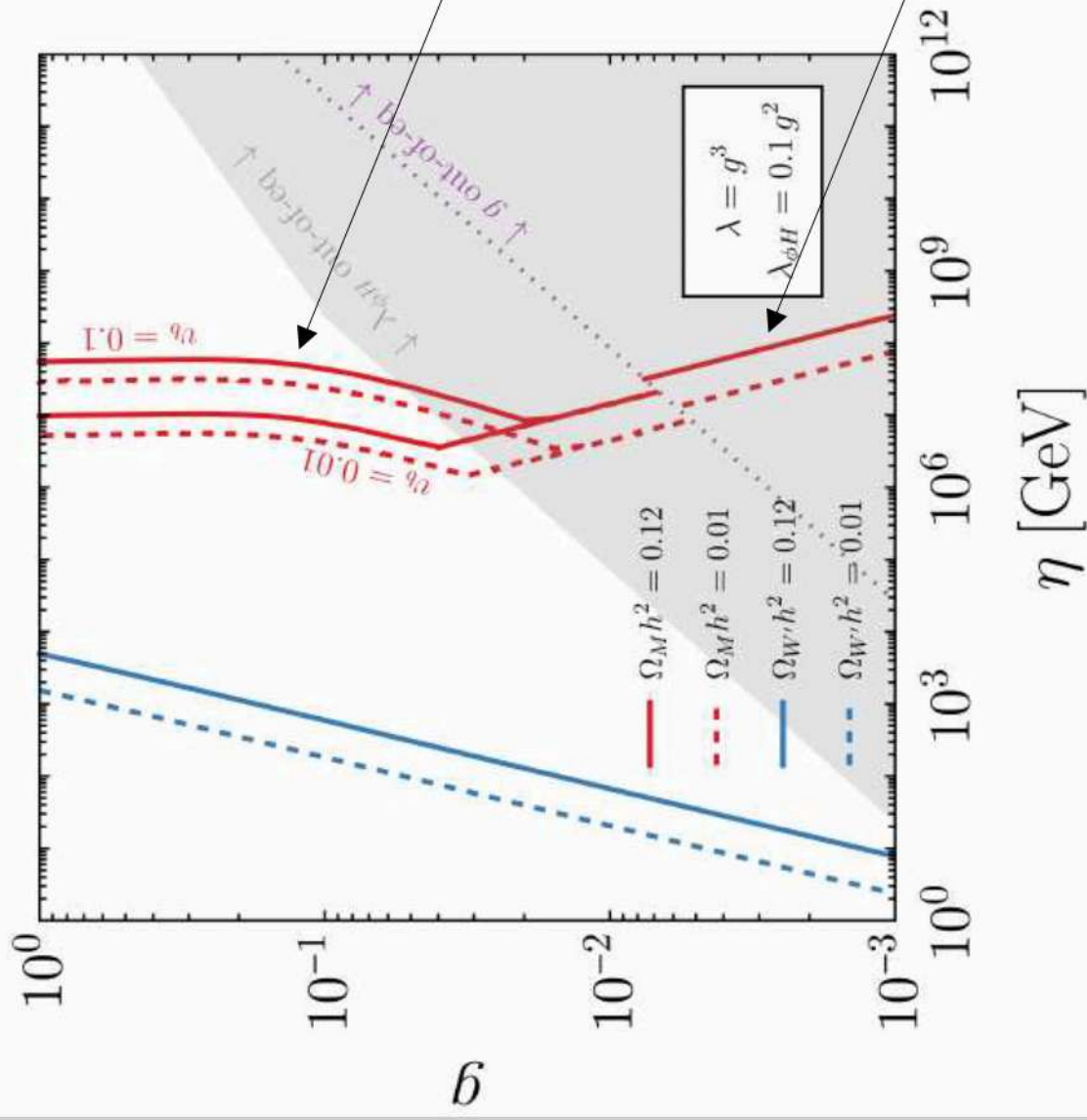
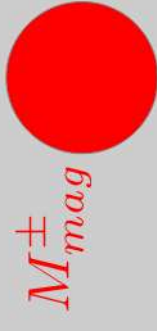
Bubble radius at percolation determines correlation length

$$\xi \simeq R_p \simeq 4.4 \frac{v_b}{\beta}$$

FOPT completion rate:

$$\beta \equiv \left. \frac{d \log \Gamma(t)}{dt} \right|_{t_p}$$

Weakly first order



Potential barrier present at T_c

Thermal fluctuations allow **nucleation** of bubbles of true vacuum

Bubble radius at percolation determines correlation length

$$\xi \simeq R_p \simeq 4.4 \frac{v_b}{\beta}$$

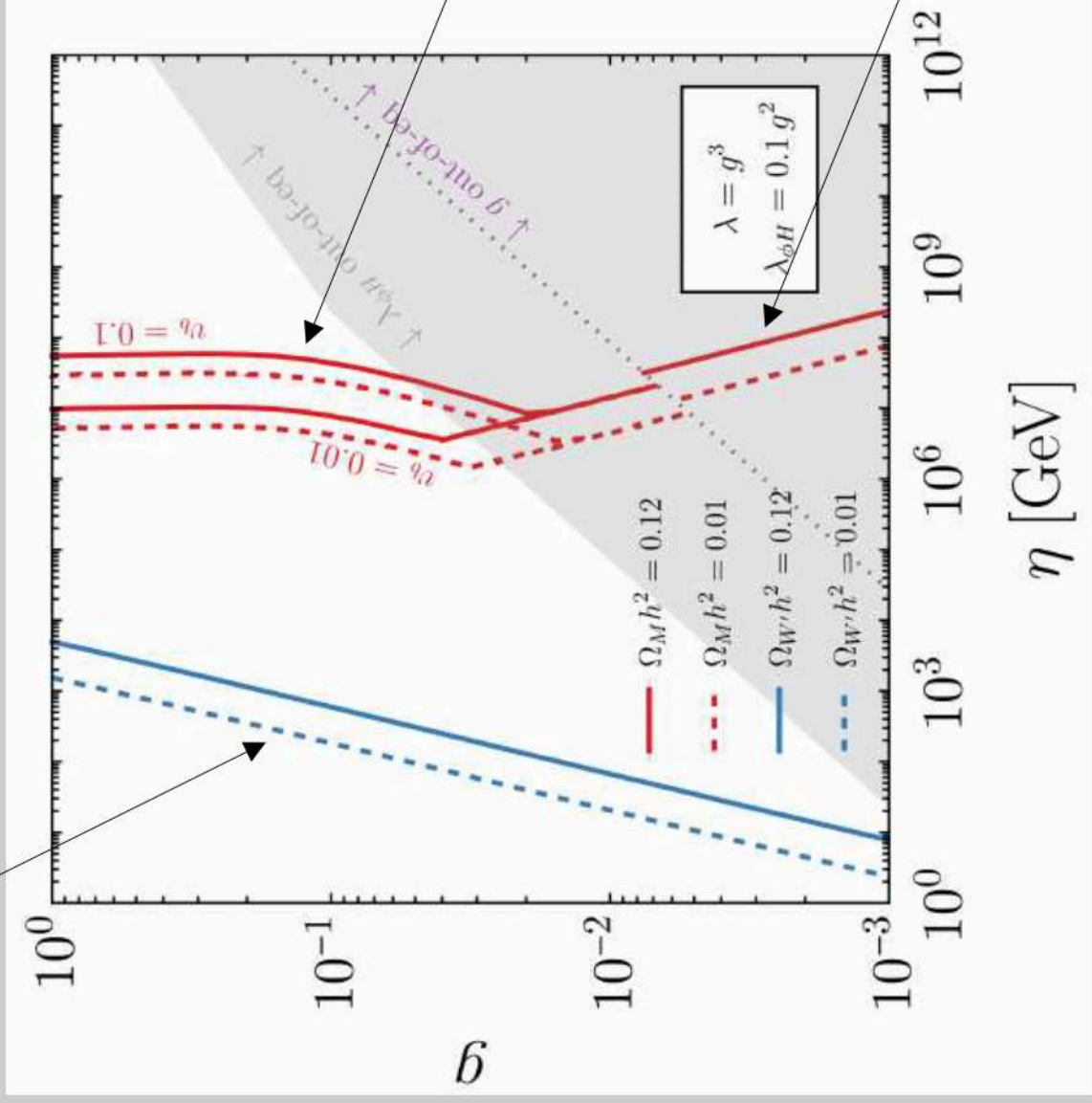
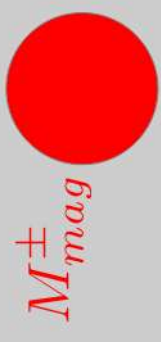
FOPT completion rate:

$$\beta \equiv \left. \frac{d \log \Gamma(t)}{dt} \right|_{t_p}$$

Later monopole annihilations further reduce abundance

Weakly first order

W freeze-out
dominate
DM abundance



Potential barrier present at T_c

Thermal fluctuations allow **nucleation**
of bubbles of true vacuum

Bubble radius at percolation
determines correlation length

$$\xi \simeq R_p \simeq 4.4 \frac{v_b}{\beta}$$

FOPT completion rate:

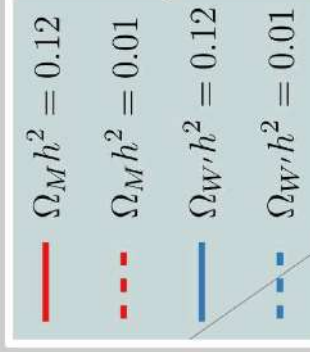
$$\beta \equiv \left. \frac{d \log \Gamma(t)}{dt} \right|_{t_p}$$

Later monopole annihilations
further reduce abundance

$M_{mag}^{\pm}$

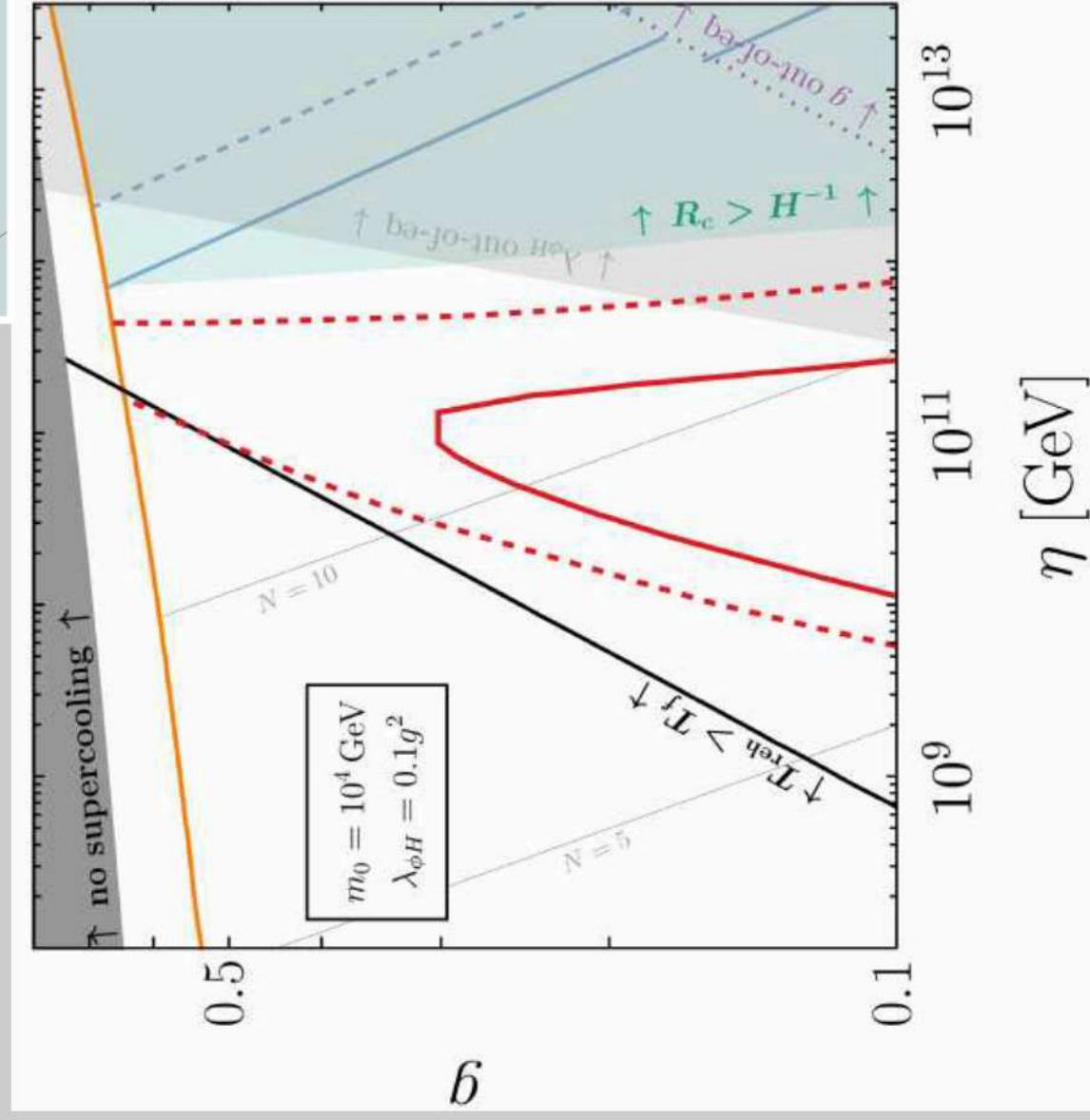
$W_{ele}^{\pm}$

Supercooled first order



Universe stuck in false vacuum
till it becomes vacuum-dominated

Supercooling: several e-folds of
inflation before bubble nucleation



$M_{mag}^{\pm}$

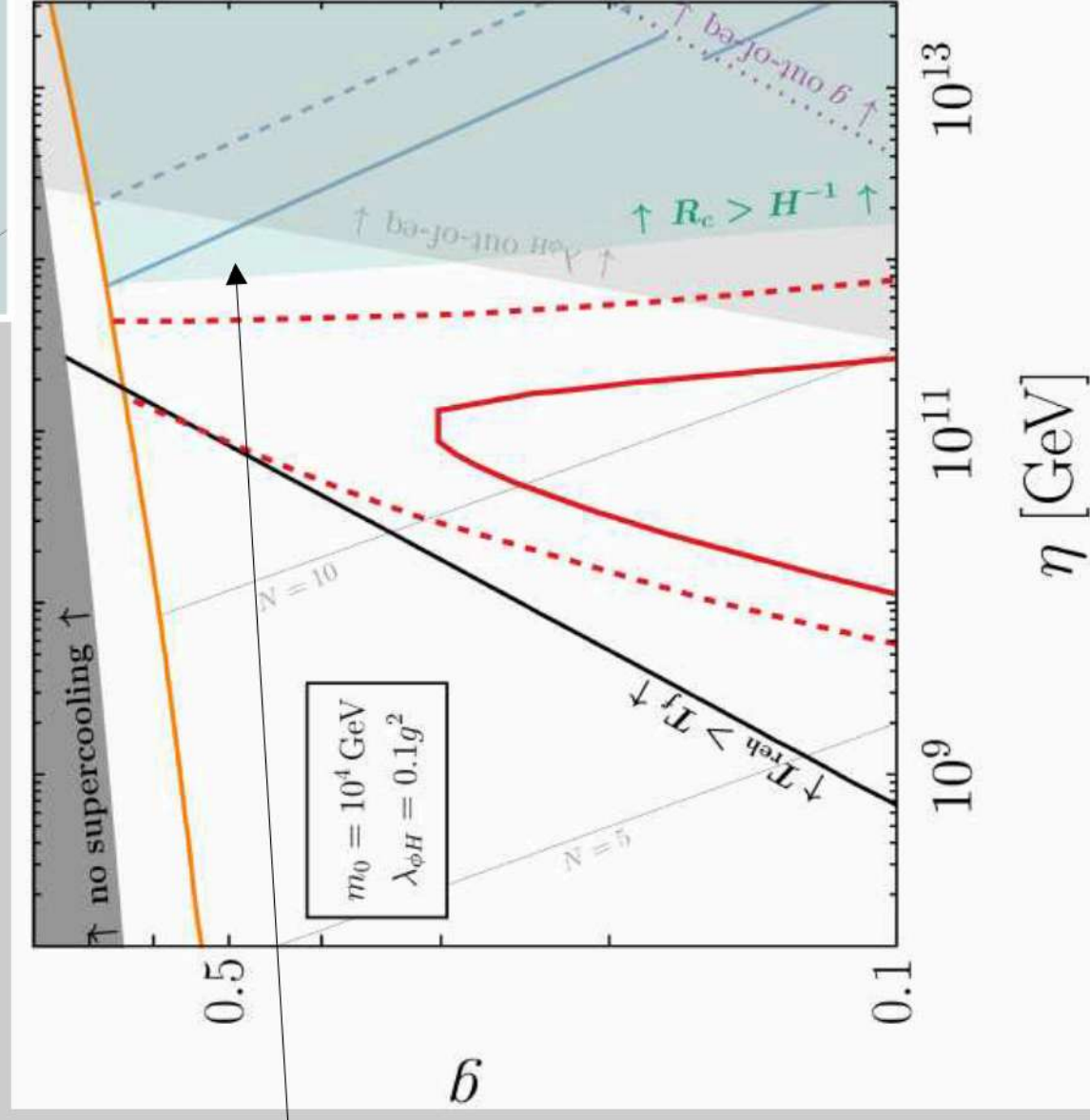
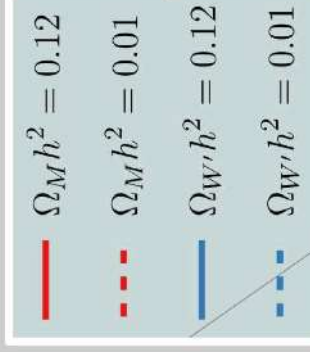
$W_{ele}^{\pm}$

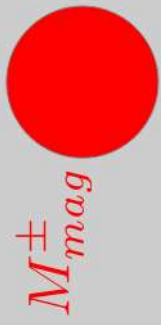
Supercooled first order

Universe stuck in false vacuum
till it becomes vacuum-dominated

Supercooling: several e-folds of
inflation before bubble nucleation

W's diluted exponentially





$M_{mag}^{\pm}$



$W_{ele}^{\pm}$

Supercooled first order

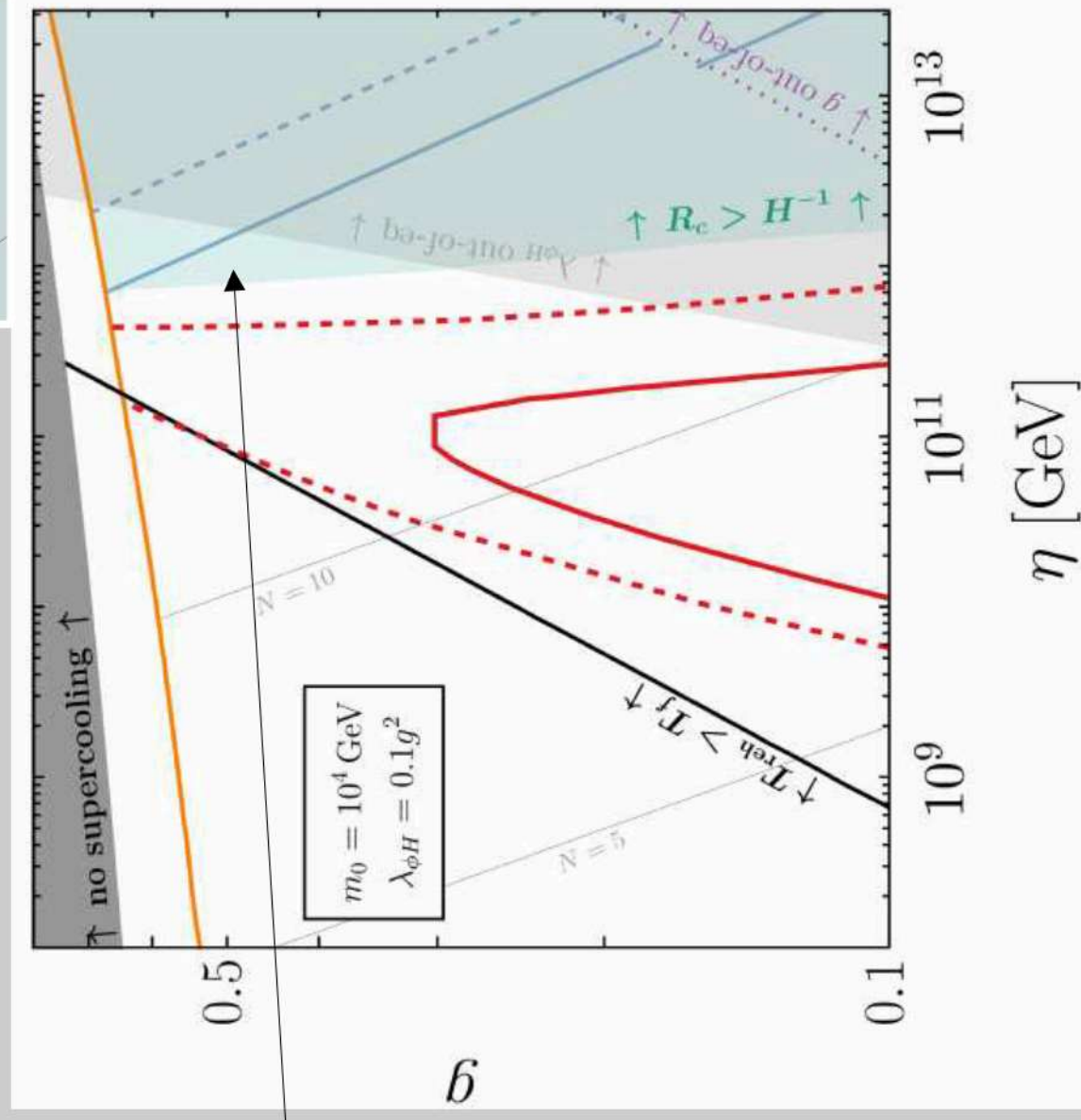
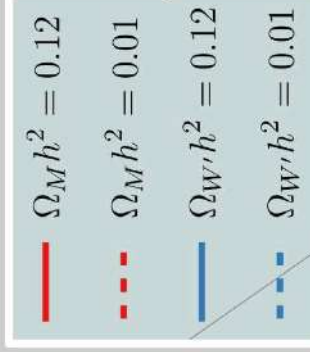
Universe stuck in false vacuum
till it becomes vacuum-dominated

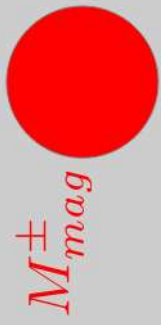
Supercooling: several e-folds of
inflation before bubble nucleation

W's diluted exponentially

Longer the supercooling,
larger the initial **critical bubble radius**

$$\xi \simeq R_p = R_{critical} + R_{expansion}$$





$M_{mag}^{\pm}$



$W_{ele}^{\pm}$

Supercooled first order

Universe stuck in false vacuum till it becomes vacuum-dominated

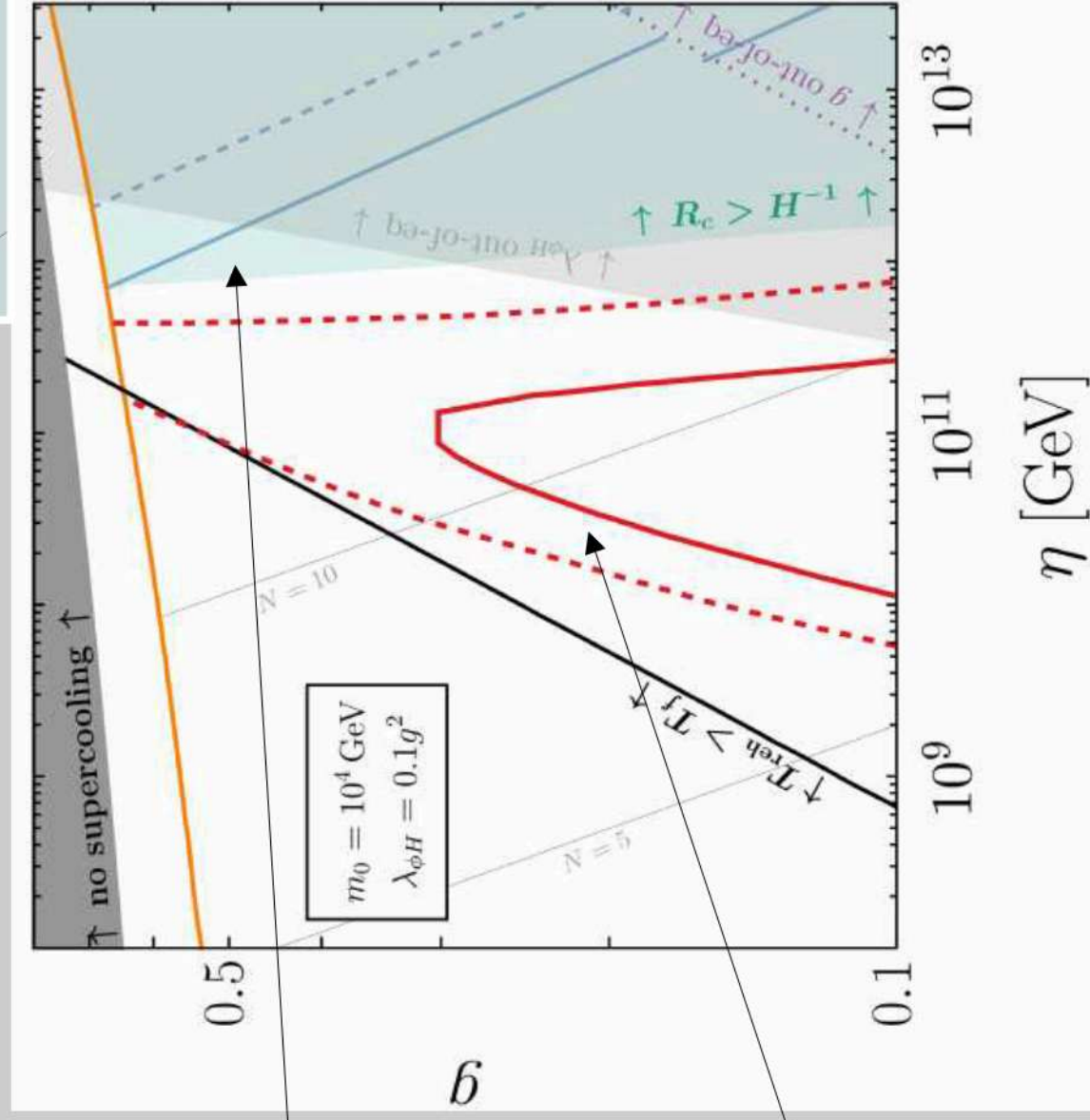
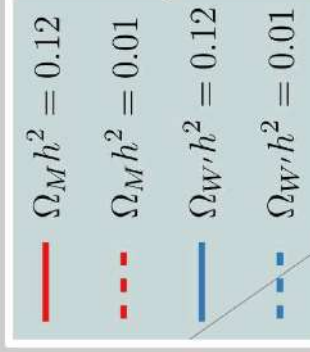
Supercooling: several e-folds of inflation before bubble nucleation

W's diluted exponentially

Longer the supercooling,
larger the initial **critical bubble radius**

$$\xi \simeq R_p = R_{critical} + R_{expansion}$$

Monopole abundance peaks at some minimal radius, and drops before reaching W ab



Dark matter goes electric !



No room for minimal monopole DM

F. Brummer, G. Ferrante, T. Fischer, M. Frigerio

PRD 113 (2026) L091701, arXiv:2509.21924

In all cases, **a small fraction of dark matter is made by monopoles**

Electric relics abundance >> Magnetic relics abundance

No room for minimal monopole DM

F. Brummer, G. Ferrante, T. Fischer, M. Frigerio
PRD 113 (2026) L091701, arXiv:2509.21924

In all cases, **a small fraction of dark matter is made by monopoles**

Electric relics abundance $\gg$ Magnetic relics abundance

A phenomenological ‘theorem’ for the **minimal dark sector**

For any symmetry breaking scale η ,
for any perturbative values of the couplings g & λ ,
one finds $\Omega_W \gg \Omega_M$

No room for minimal monopole DM

F. Brummer, G. Ferrante, T. Fischer, M. Frigerio
PRD 113 (2026) L091701, arXiv:2509.21924

In all cases, **a small fraction of dark matter is made by monopoles**

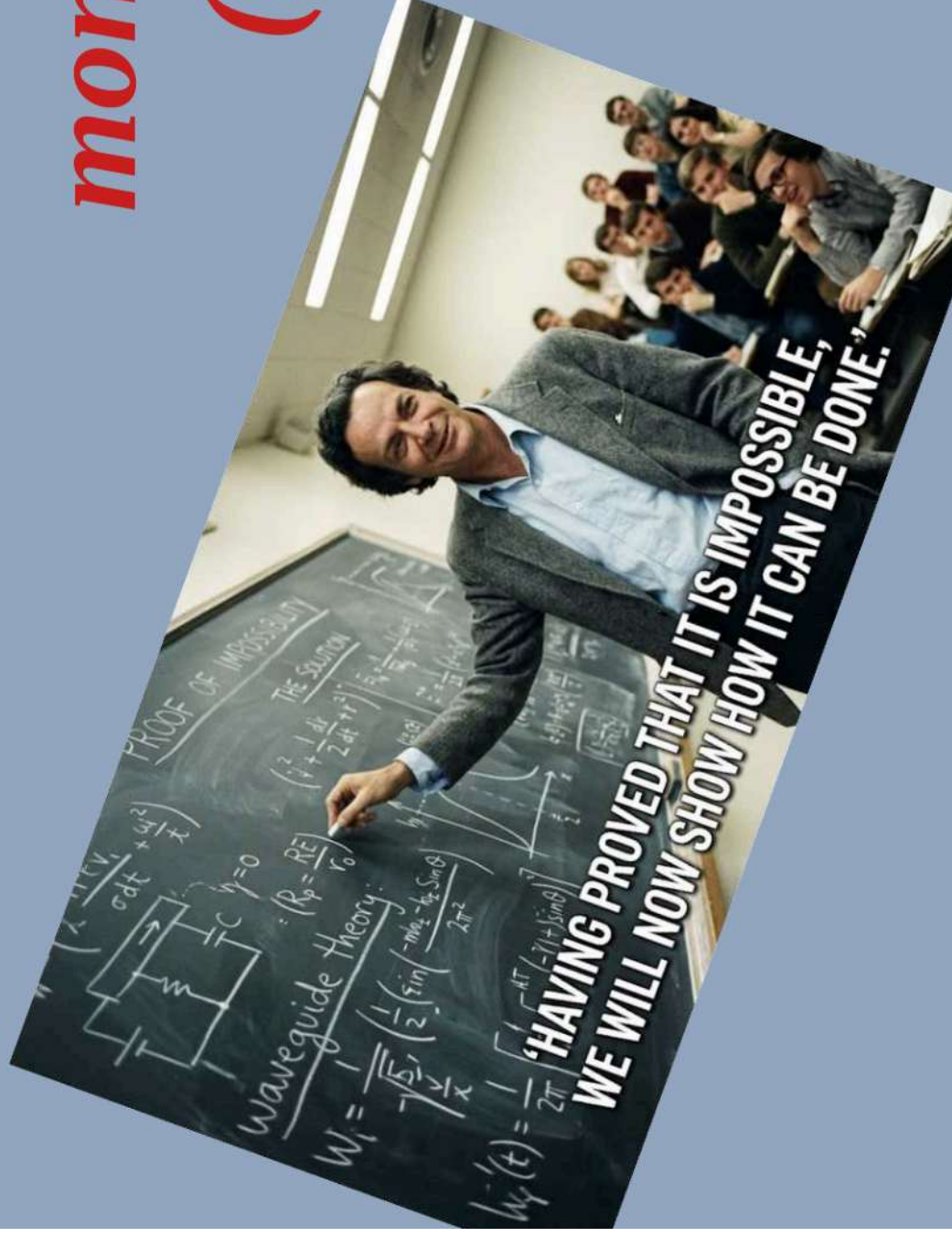
Electric relics abundance $\gg$ ***Magnetic relics abundance***

A phenomenological ‘theorem’ for the **minimal dark sector**

For any symmetry breaking scale η ,
for any perturbative values of the couplings g & λ ,
one finds $\Omega_W \gg \Omega_M$

[General remark: dark-matter candidates are very many,
well-motivated & predictive ones are a few,
and it is very hard to fully exclude any]

*Less minimal
models,
to realise
monopole DM
(maybe)*



Ways out for monopole DM

- *Through portals:*

Electric relics **annihilate efficiently into Standard Model** particles if

$$\text{large Higgs portal } \lambda_{\phi H} > \lambda, g^2$$

Ways out for monopole DM

- *Through portals:*

Electric relics **annihilate efficiently into Standard Model** particles if

$$\text{large Higgs portal } \lambda_{\phi H} > \lambda, g^2$$

But then scalar thermal potential is strongly deformed:

- modified nature of **dark phase transition** affects monopole abundance
- necessary interplay with **electroweak phase transition**: signatures?

To be studied

Ways out for monopole DM

- *Through portals:*

Electric relics **annihilate efficiently into Standard Model** particles if

$$\text{large Higgs portal } \lambda_{\phi H} > \lambda, g^2$$

But then scalar thermal potential is strongly deformed:

- modified nature of **dark phase transition** affects monopole abundance
- necessary interplay with **electroweak phase transition**: signatures?

To be studied

Portals to other sectors: e.g. coupling ϕ to an inflaton, to produce monopoles non-thermally at preheating

Ways out for monopole DM

- *Through different topologies:*

Different symmetry breaking leads to different topological defects

$$SO(3) \xrightarrow{\langle \phi_5 \rangle} O(2) \qquad \frac{SO(3)}{O(2)} \simeq RP^2 \qquad \pi_2(RP^2) = \mathbb{Z} \quad \pi_1(RP^2) = \mathbb{Z}_2$$

Ways out for monopole DM

- *Through different topologies:*

Different symmetry breaking leads to different topological defects

$$SO(3) \xrightarrow{\langle \phi_5 \rangle} O(2) \qquad \frac{SO(3)}{O(2)} \simeq RP^2 \qquad \pi_2(RP^2) = \mathbb{Z} \quad \pi_1(RP^2) = \mathbb{Z}_2$$

Such “ Alice ” electromagnetism is non-abelian !

- **both monopoles & cosmic strings**,
with non-trivial cosmological evolution
- **electric relics** also have different history

To be studied

Ways out for monopole DM

- *Through different topologies:*

Different symmetry breaking leads to different topological defects

$$SO(3) \xrightarrow{\langle \phi_5 \rangle} O(2) \qquad \frac{SO(3)}{O(2)} \simeq RP^2 \qquad \pi_2(RP^2) = \mathbb{Z} \quad \pi_1(RP^2) = \mathbb{Z}_2$$

Such “ Alice ” electromagnetism is non-abelian !

- **both monopoles & cosmic strings**,
with non-trivial cosmological evolution
- **electric relics** also have different history

To be studied

one Alice defect observed
at Bourse du Commerce
Paris, March 2025



Ways out for monopole DM

- *À la Grand Unification:*

Heavy dark, electric relics ($m_w = g \eta$) decay into
(much) lighter dark, electric relics
(as GUT scale particles decay into SM particles)

Ways out for monopole DM

- *À la Grand Unification:*

Heavy dark, electric relics ($m_W = g \eta$) decay into
(much) lighter dark, electric relics

(as *GUT* scale particles decay into *SM* particles)

However, no much space to hide light dark particles:

- if they behave like matter, they still contribute to dark matter
- if they behave like radiation, they contribute to N_{eff}

[recall that monopoles already imply a dark U(1) photon]

Suppressing electric relics

Add (anomaly-free) **dark fermions** to 't Hooft-Polyakov model :

$$\chi^i, \psi^i \sim \mathbf{2}_{SU(2)} \quad \mathcal{L} \supset -m_f \chi^i \epsilon_{ij} \psi^j - y \chi^i \epsilon_{ij} \phi^a (\sigma^a)^j_k \psi^k$$

After SSB, two Dirac fermions with **dark electric charge** $q = -\frac{1}{2}$:

$$\begin{aligned} m_{e'} &= m_f - y\eta \\ m_{\mu'} &= m_f + y\eta \end{aligned}$$

Suppressing electric relics

Add (anomaly-free) **dark fermions** to 't Hooft-Polyakov model :

$$\chi^i, \psi^i \sim \mathbf{2}_{SU(2)} \qquad \mathcal{L} \supset -m_f \chi^i \epsilon_{ij} \psi^j - y \chi^i \epsilon_{ij} \phi^a (\sigma^a)^j_k \psi^k$$

After SSB, two Dirac fermions with **dark electric charge $q = -\frac{1}{2}$** :

$$\begin{aligned} m_{e'} &= m_f - y\eta \\ m_{\mu'} &= m_f + y\eta \end{aligned}$$

$$W' \rightarrow e' \mu'$$

$$\mu' \rightarrow e'(e'\bar{e}') \quad \text{or} \quad \mu' \rightarrow e'\gamma'$$

Suppressing electric relics

Add (anomaly-free) **dark fermions** to 't Hooft-Polyakov model :

$$\chi^i, \psi^i \sim \mathbf{2}_{SU(2)} \quad \mathcal{L} \supset -m_f \chi^i \epsilon_{ij} \psi^j - y \chi^i \epsilon_{ij} \phi^a (\sigma^a)_k^j \psi^k$$

After SSB, two Dirac fermions with **dark electric charge** $q = -\frac{1}{2}$:

$$m_{e'} = m_f - y\eta$$

$$m_{\mu'} = m_f + y\eta$$

$$W' \rightarrow e' \mu' \quad \text{or} \quad \mu' \rightarrow e' \gamma'$$

Thermal population of e' freezes-out annihilating into dark radiation :

$$\langle \sigma v \rangle_{\bar{e}' e' \rightarrow \gamma' \gamma'} \approx \frac{g^4}{256 \pi m_{e'}^2} \quad \Omega_{e'} h^2 \sim 0.1 \left(\frac{0.4}{g} \right)^4 \left(\frac{m_{e'}}{100 \text{ GeV}} \right)^2$$

Electric relics are **sub-dominant DM component**

IF e' is sufficiently light: **well below the electroweak scale**

Irreducible dark radiation

$$\Delta N_{\text{eff}} = \frac{4}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{T_D^0}{T_{\text{SM}}^0} \right)^4 \times \left\{ \begin{array}{cc} 2 & (\gamma') \\ 7/2 & (e') \end{array} \right.$$

If very light, dark fermions would directly contribute to radiation: already excluded.

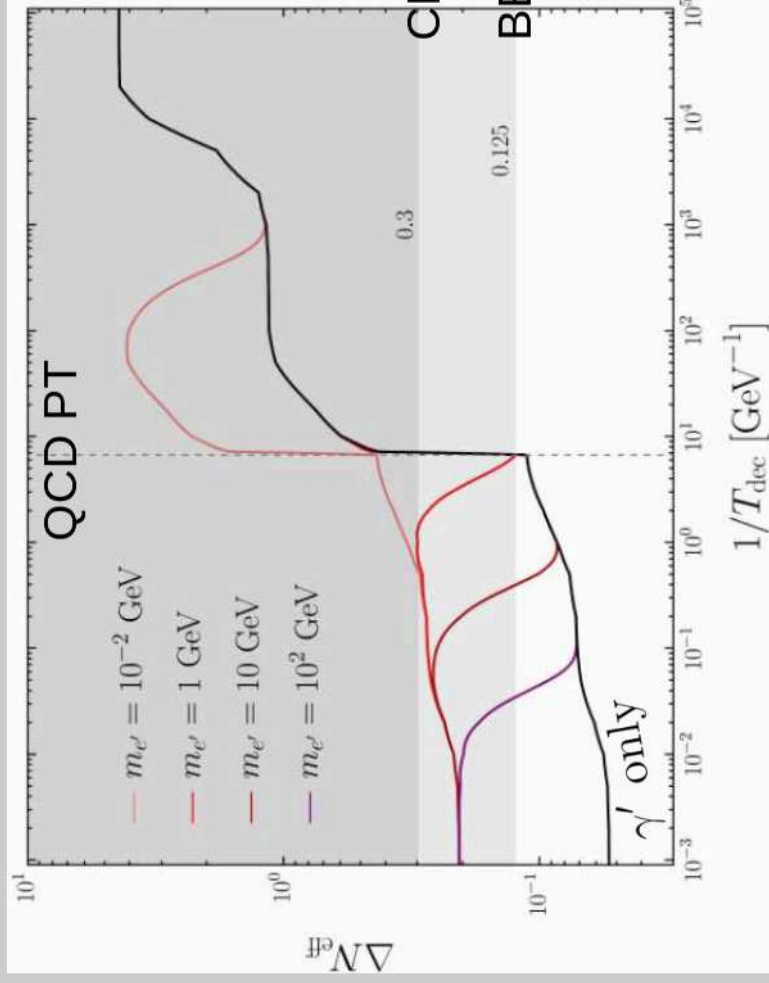
If heavier, they may **increase T_D^0 by injecting entropy into dark sector** after decoupling.

Irreducible dark radiation

$$\Delta N_{\text{eff}} = \frac{4}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{T_D^0}{T_{\text{SM}}^0} \right)^4 \times \left\{ \begin{array}{cc} 2 & (\gamma') \\ 7/2 & (e') \end{array} \right.$$

If very light, dark fermions would directly contribute to radiation: already excluded.

If heavier, they may **increase T_D^0** by **injecting entropy into dark sector** after decoupling.

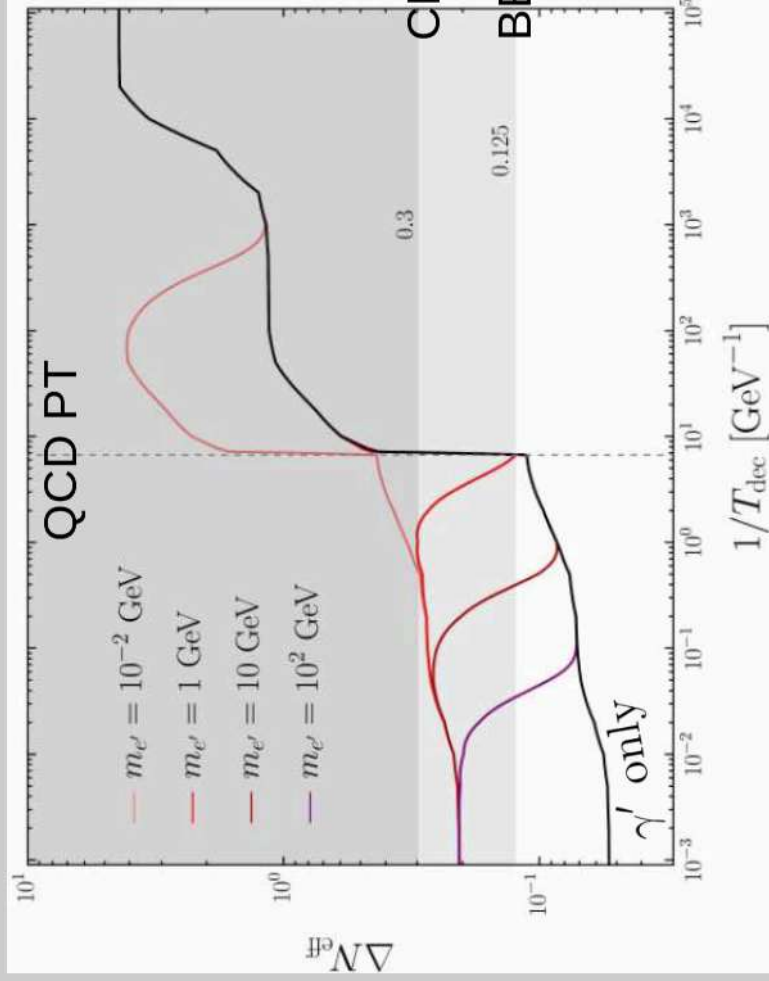


Irreducible dark radiation

$$\Delta N_{\text{eff}} = \frac{4}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{T_D^0}{T_{\text{SM}}^0} \right)^4 \times \left\{ \begin{array}{cc} 2 & (\gamma') \\ 7/2 & (e') \end{array} \right.$$

If very light, dark fermions would directly contribute to radiation: already excluded.

If heavier, they may **increase T_D^0 by injecting entropy into dark sector** after decoupling.



SM and dark sector are coupled
via **Higgs portal** :

$$h \leftrightarrow e' \bar{e}'$$

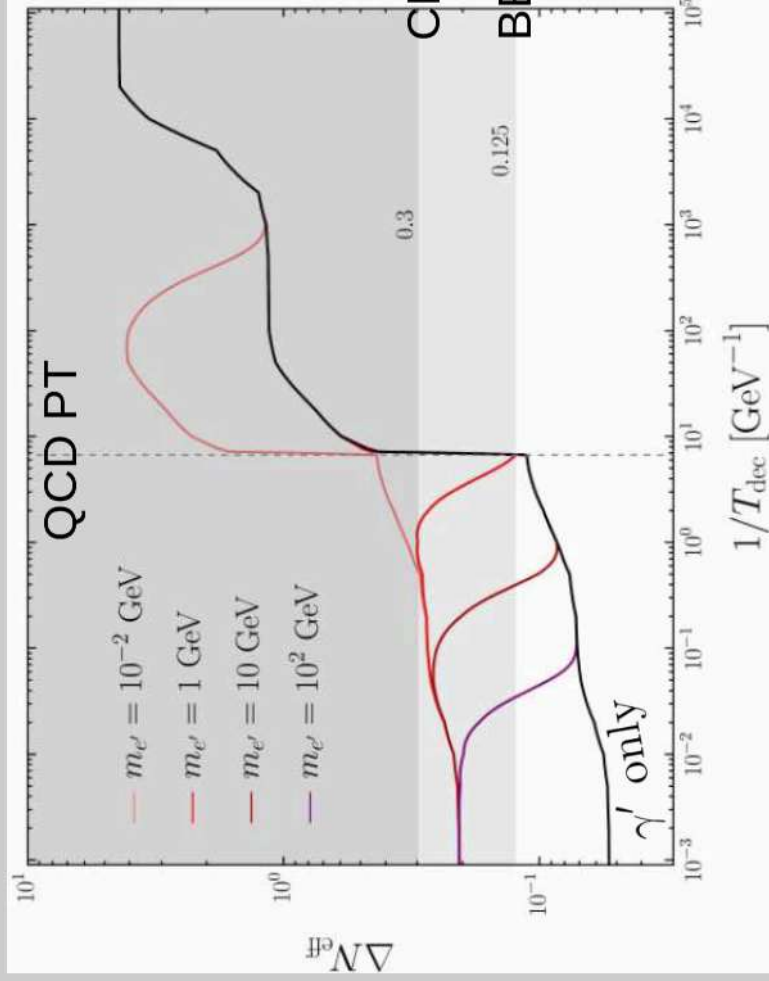
Rate suppressed by small mixing
between Higgs and dark scalar
 $\Rightarrow$ **early decoupling**

Irreducible dark radiation

$$\Delta N_{\text{eff}} = \frac{4}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{T_D^0}{T_{\text{SM}}^0} \right)^4 \times \begin{cases} 2 & (\gamma') \\ 7/2 & (e') \end{cases}$$

If very light, dark fermions would directly contribute to radiation: already excluded.

If heavier, they may **increase T_D^0** by **injecting entropy into dark sector** after decoupling.



SM and dark sector are coupled
via **Higgs portal** :

$$h \leftrightarrow e' \bar{e}'$$

Rate suppressed by small mixing
between Higgs and dark scalar
 $\Rightarrow$ **early decoupling**

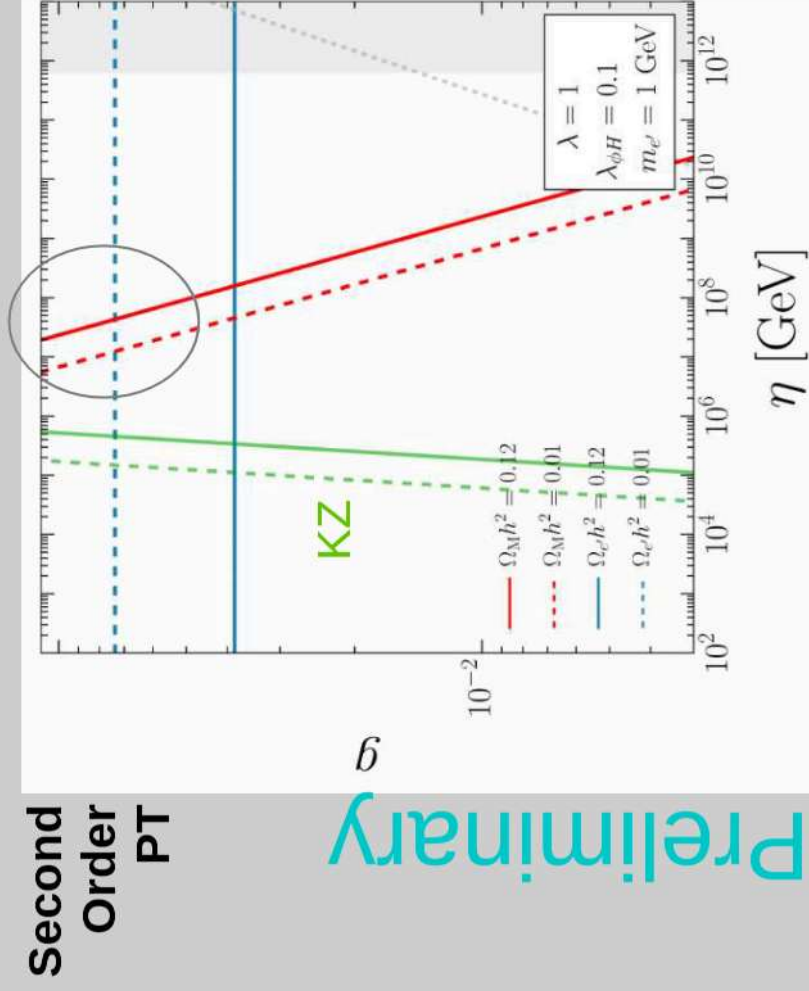
Dark photon + Electric relics
necessarily imply
 N_{eff} close to present bounds

Monopole abundance revisited (I)

- Initially [light electric relics](#) contribute to monopole annihilations, eventually their final abundance becomes negligible
- Monopole DM requires [large hierarchy of scales](#), $\eta \gg v$, thus the two sectors decouple early $\Rightarrow$ irreducible N_{eff}

Monopole abundance revisited (I)

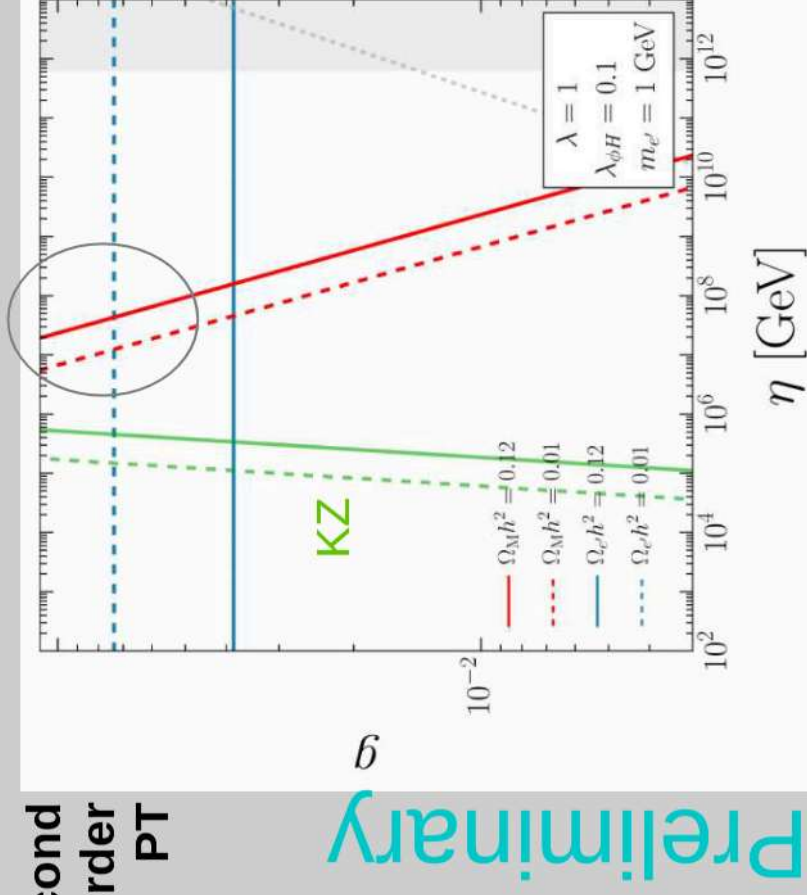
- Initially **light electric relics** contribute to monopole annihilations, eventually their final abundance becomes negligible
- Monopole DM requires **large hierarchy of scales**, $\eta \gg v$, thus the two sectors decouple early $\Rightarrow$ irreducible N_{eff}



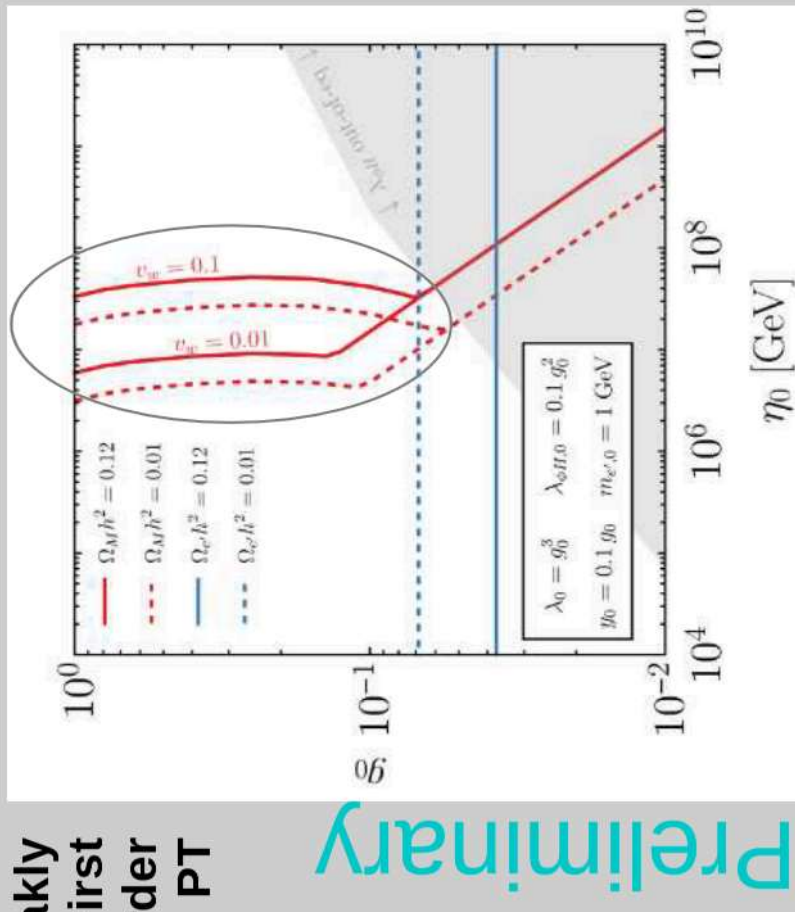
Monopole abundance revisited (I)

- Initially **light electric relics** contribute to monopole annihilations, eventually their final abundance becomes negligible
- Monopole DM requires **large hierarchy of scales**, $\eta \gg v$, thus the two sectors decouple early $\Rightarrow$ irreducible N_{eff}

**Second
Order
PT**



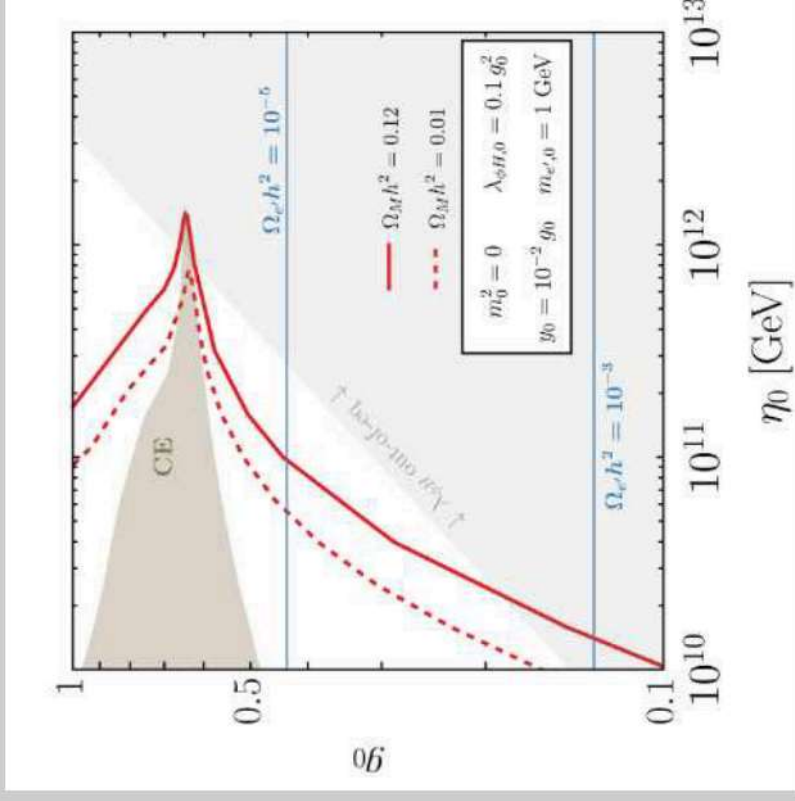
**Weakly
First
Order
PT**



Monopole abundance revisited (II)

Strong (cw)
First Order
PT

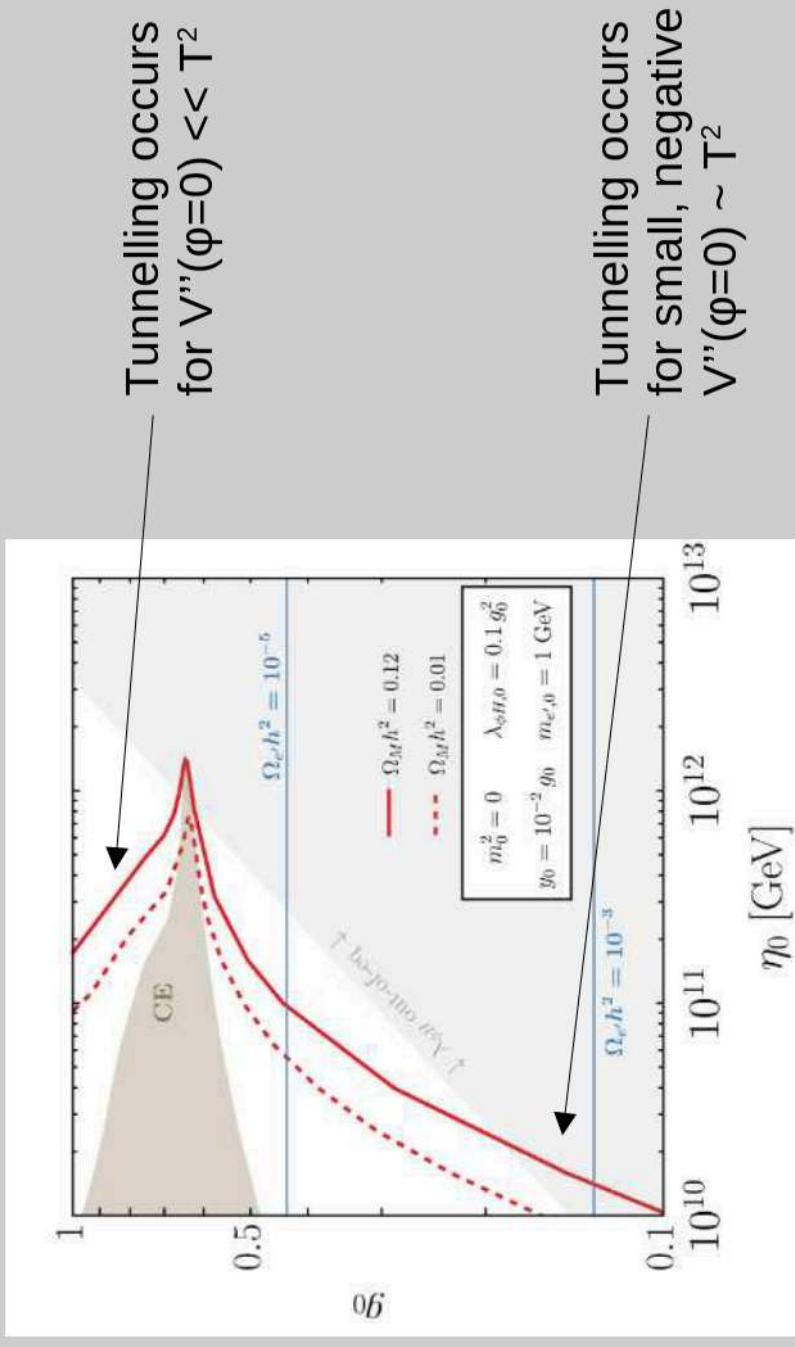
Preliminary



Monopole abundance revisited (II)

Strong (cw)
First Order
PT

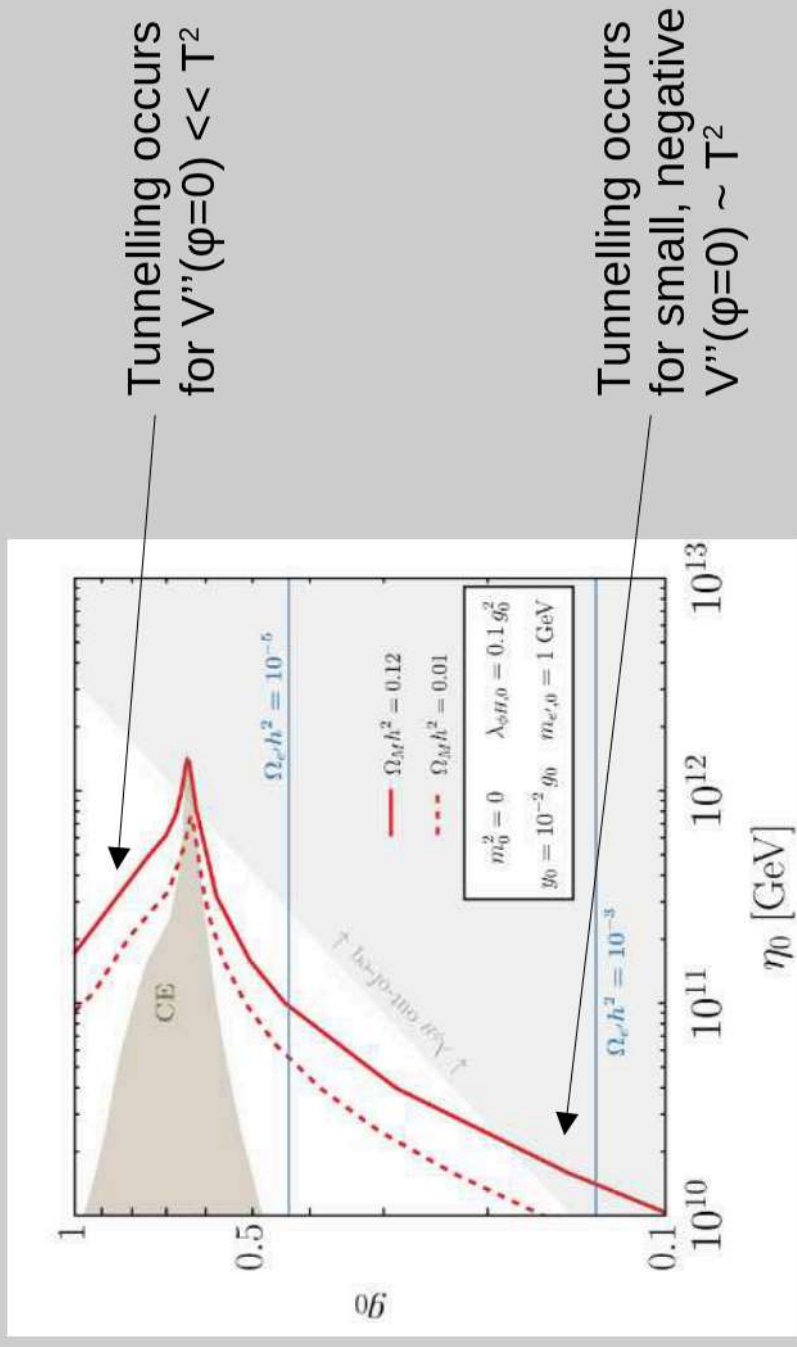
Preliminary



Monopole abundance revisited (II)

Strong (CW)
First Order
PT

Preliminary



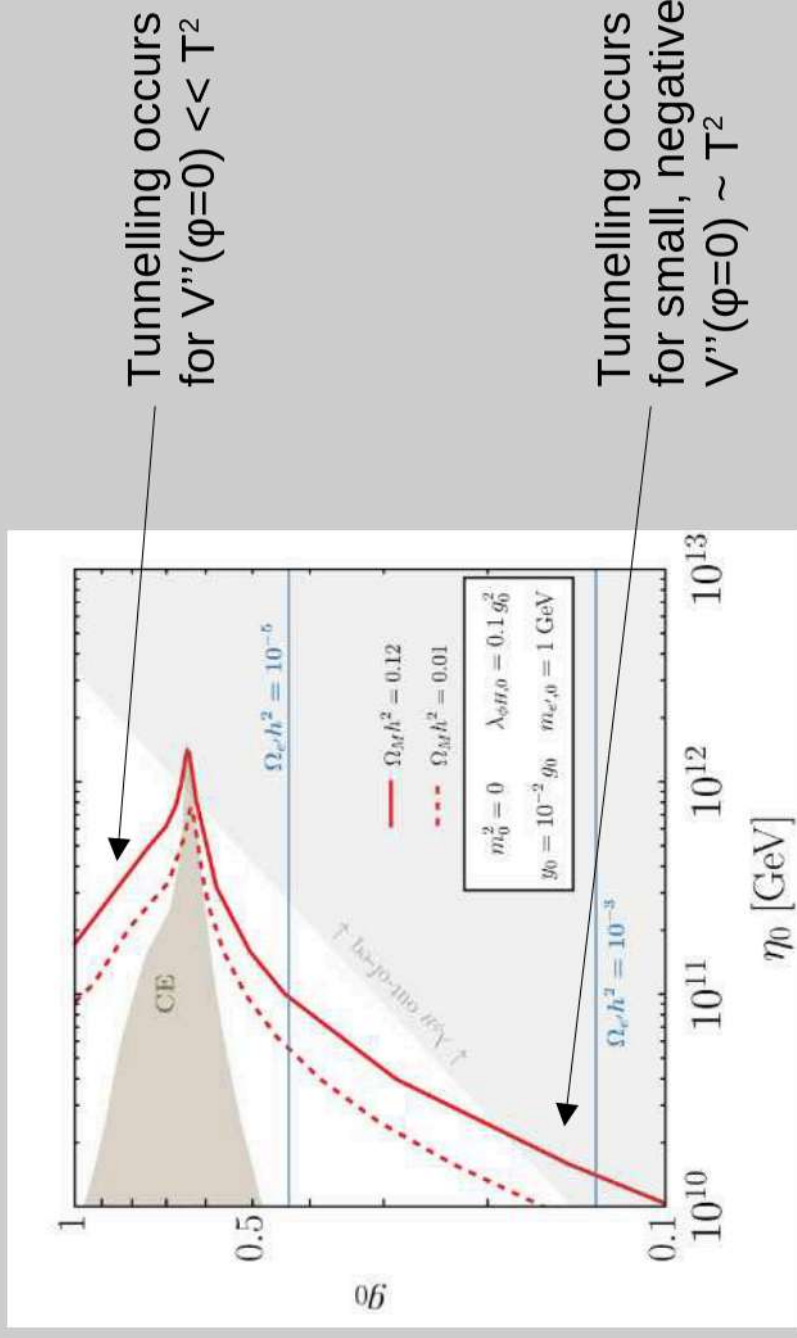
- In supercooled PT, there is large scale separation: $T_n \ll T_c$

⇒ need for **RGE improved thermal potential**: running couplings at $\mu \sim T$

Monopole abundance revisited (II)

Strong (CW)
First Order
PT

Preliminary



- In supercooled PT, there is large scale separation: $T_n \ll T_c$
 $\Rightarrow$ need for **RGE improved thermal potential**: running couplings at $\mu \sim T$
- The smaller is bubble radius, **the larger is gravitational-wave frequency**
 $\Rightarrow$ monopole DM beyond reach of Einstein telescope & Cosmic Explorer

Summary

- **In visible sector**, magnetic monopoles very rare
- **In dark sector**, monopoles generically subdominant
- Dark monopoles always **negligibly few in minimal model**
- In specific models with **light dark particles**, dark matter can be dominated by **heavy thermally-produced monopoles**
- Indirect signatures include **extra radiation** (unavoidably) and **gravitational waves** (if lucky)